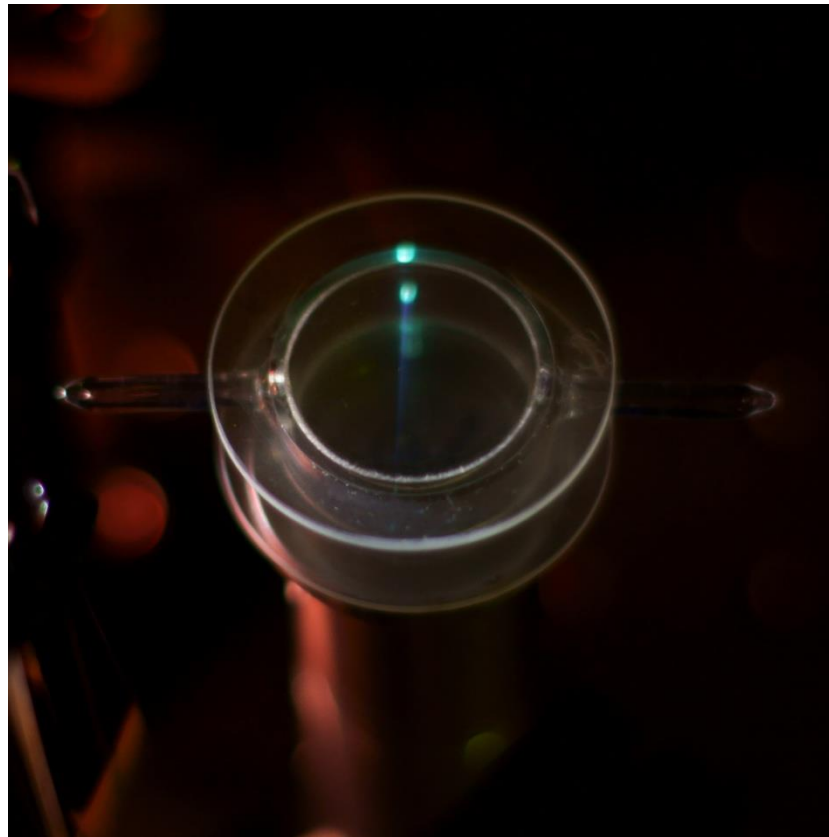


^{199}Hg EDM Measurement



Brent Graner
University of Washington
October 16, 2017

A time-reversal-sensitive atomic clock

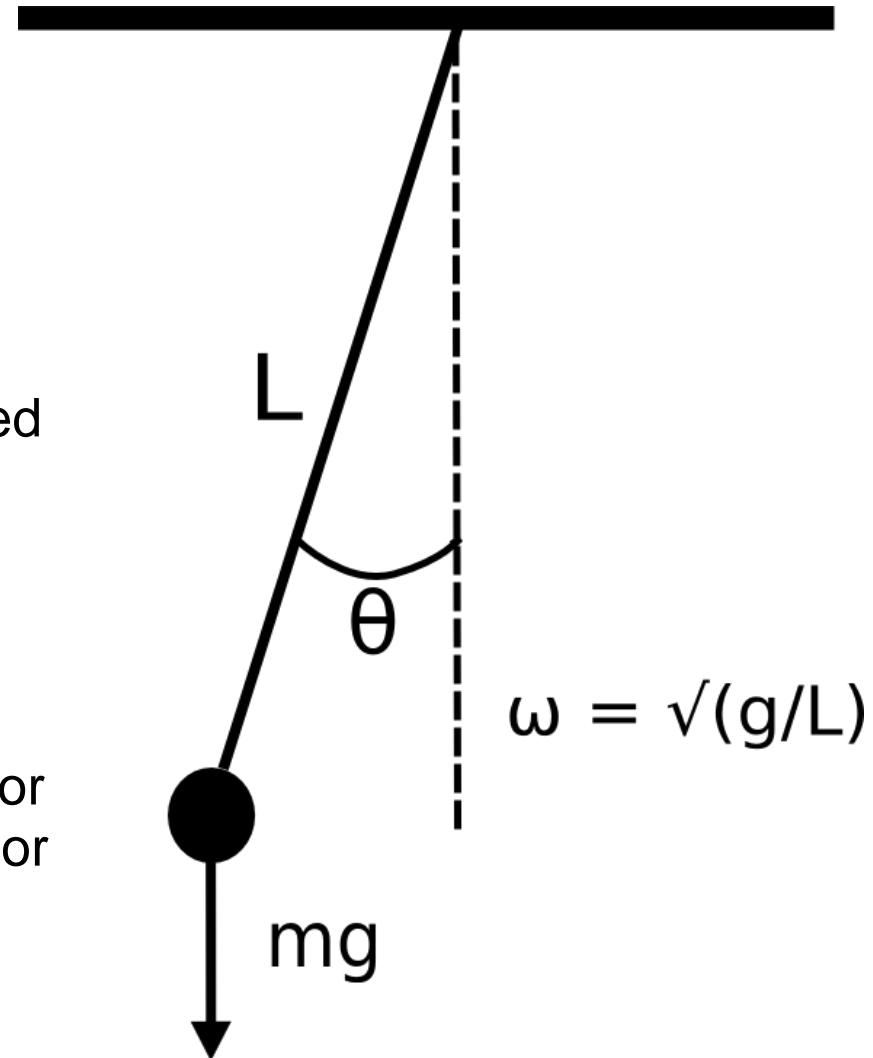
Traditional clocks consist of an oscillator and escapement (i.e. counter)

More precise clocks are made by:

1) Using oscillators with more well-defined frequency (atoms vs. pendulum)

2) Isolating the oscillator from external disturbances

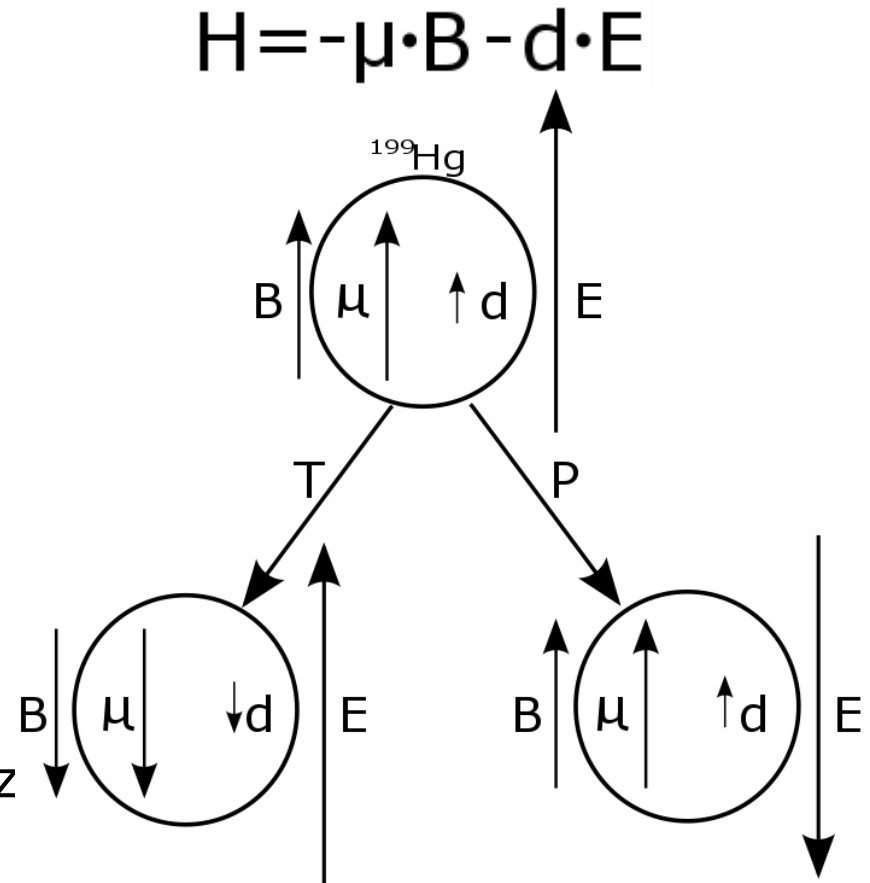
3) Using a reference oscillator checked for phase deviation from the primary oscillator (Ramsey Method)



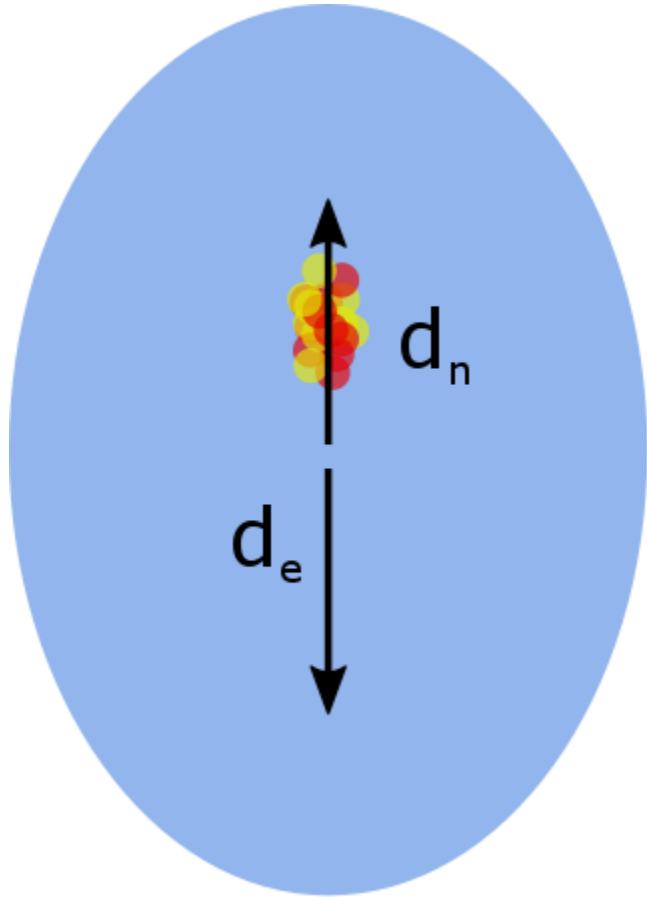
T and CP Symmetry Breaking

- EDM represents charge separation
- Units of $e \cdot \text{cm}$
- EDM must point along (nuclear) spin axis
- Transforms like angular momentum (P-even, T-odd)
- Breaks time-reversal (T) symmetry of the Hamiltonian
- CPT conservation follows from Lorentz invariance

T violation is equivalent to CP violation



Atomic vs. Neutron EDMs



.Schiff's Theorem: An EDM of a point-like nucleus would be perfectly screened by non-relativistic electrons interacting electrostatically

.The EDM of an atomic system is due to the operator product of the EDMs of constituent particles and a P-odd, T-odd n-n or e-n interaction:

$$\mathbf{d}_{\text{atom}} = 2 \sum_M \frac{\langle K | \hat{\mathbf{D}} | M \rangle \langle M | \hat{H}_{PT} | K \rangle}{E_K - E_M} = d_{\text{atom}}(\mathbf{F}/F)$$

.This P-even, T-odd “EDM” has a P,T-odd dipole interaction with electric field \mathbf{E}

The Schiff Moment

.Schiff's Theorem has 3 assumptions:

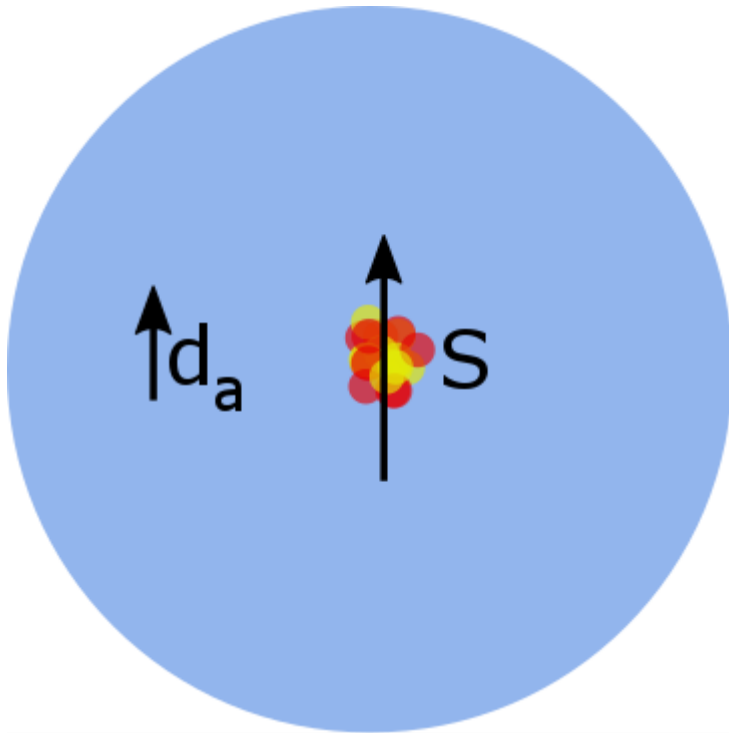
- 1) Point-like nucleus
- 2) Non-relativistic electrons
- 3) Electrostatic interactions

.The Schiff moment **S** is the dominant P, T-odd nuclear moment (e fm³):

$$\mathbf{S} = \frac{1}{10} \left[\int e\rho(\mathbf{r})\mathbf{r}r^2 d^3r - \frac{5}{3} \mathbf{d} \frac{1}{Z} \int \rho(\mathbf{r})r^2 d^3r \right]$$

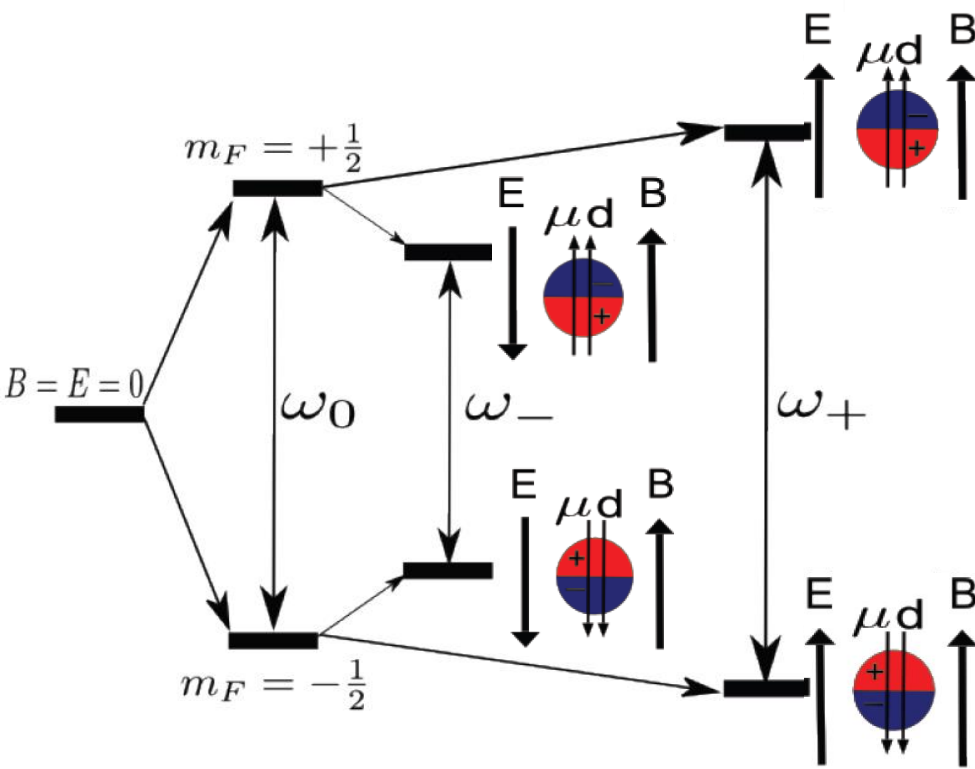
.**S** goes to 0 in the limit of a point nucleus

.Heavier nuclei give larger **S** values, larger atomic EDM/nuclear EDM ratios



Measurement principle: Larmor frequency observation

$$H = -\boldsymbol{\mu} \cdot \mathbf{B} - d \cdot \mathbf{E}$$



- Measurement is done on the ground state (1S_0) hyperfine manifold with $|F|=1/2$

- \mathbf{d}_{atom} must always be parallel to $\boldsymbol{\mu}$

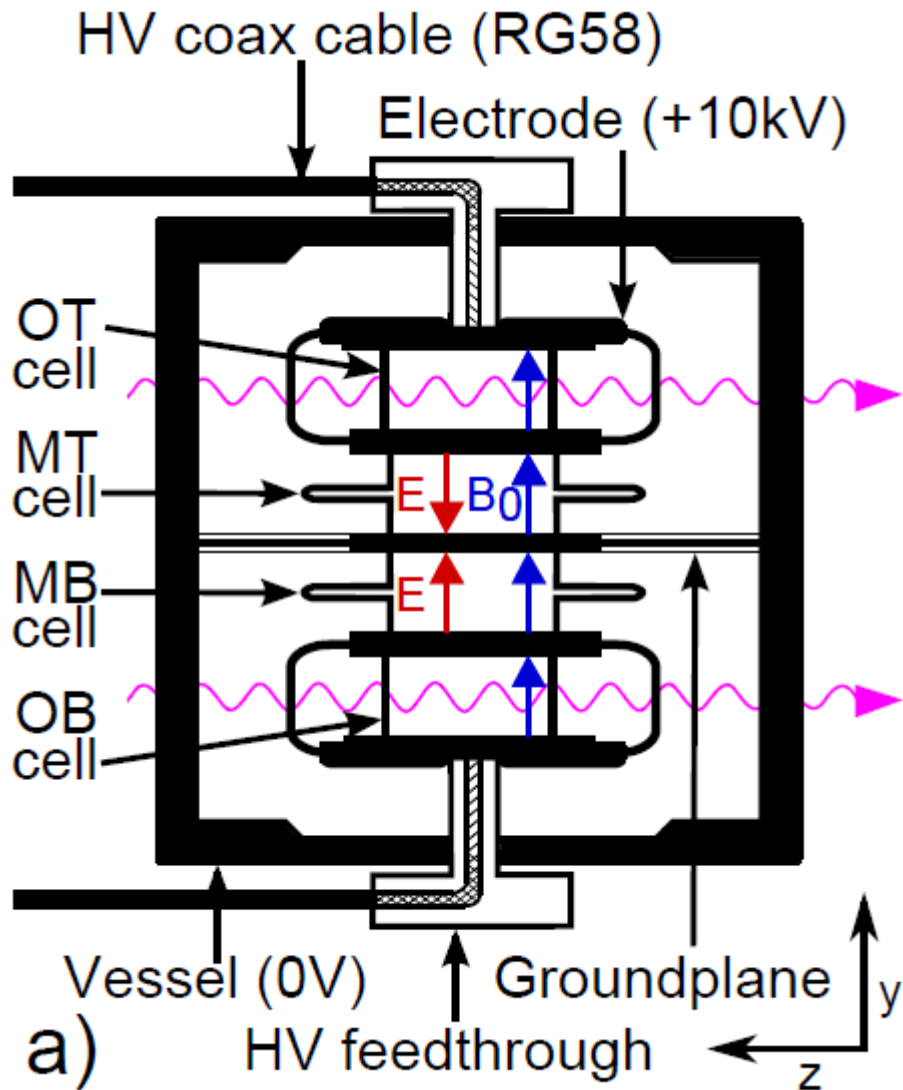
- The 2 energy levels will shift farther apart or closer together when \mathbf{E} is applied

- For $B = 15\text{mG}$, $E = 10\text{kV/cm}$, we get $\Delta\omega/\omega < 10^{-10}$

- This gives $\Delta E < 3.1 \cdot 10^{-25} \text{ eV!}$

Level diagram of ^{199}Hg ground state with parallel $\boldsymbol{\mu}$ and \mathbf{d}_{atom} in parallel, antiparallel \mathbf{E} and \mathbf{B} fields

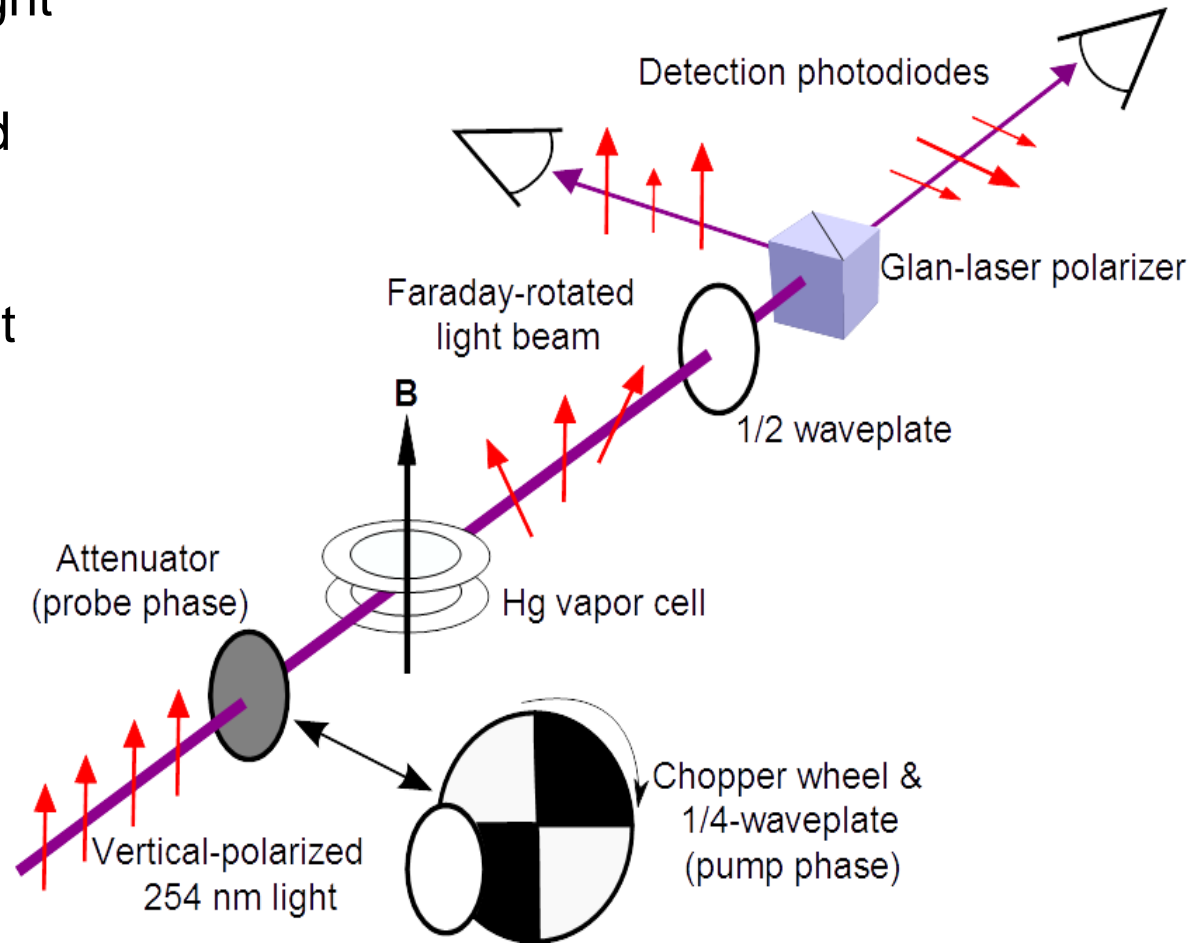
Measurement Technique



- Atoms are contained in a stack of 4 vapor cells in a common B field
- 2 conducting plastic electrodes at the same potential hold the 2 outer cells
- Opposite E field causes an EDM to shift the relative frequency of the 2 inner cells
- ^{199}Hg is pumped to align spins with laser beams
- Precession is observed by detecting Faraday rotation of weak, linear polarized light

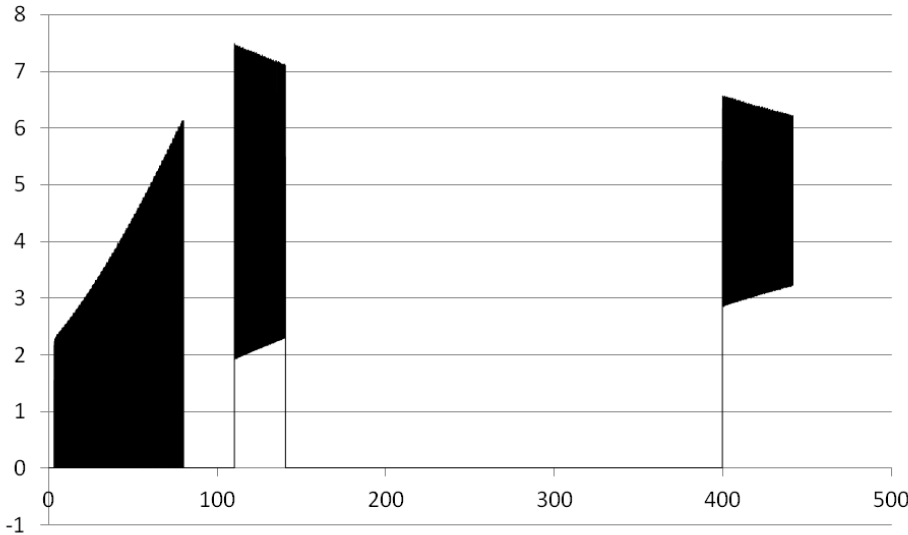
Faraday Rotation Detection

- Atomic polarization changes the index of refraction for σ_+ and σ_- light
- Incoming linearly polarized probe light is rotated
- Rotation angle oscillates at the Larmor frequency
- A polarizing beam splitter separates the beam into vertical, horizontal components
- Intensity of 2 orthogonal polarization states oscillate out of phase



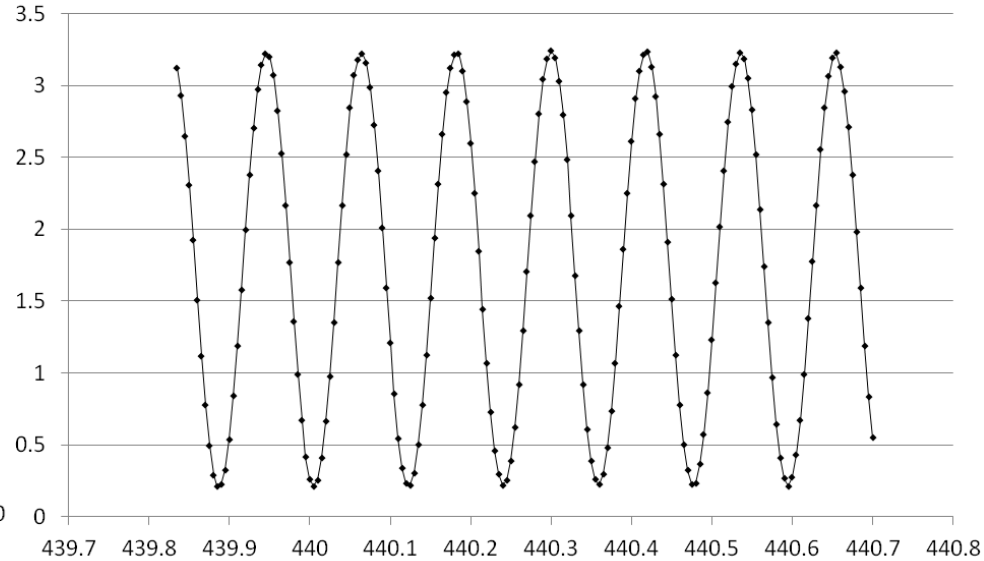
Phase Difference Analysis

^{199}Hg EDM raw data (run 16030, 5/29/2013)



Photodiode signal (V) vs. time (seconds)

^{199}Hg EDM run 16030 data excerpt (-3.0V offset)



Photodiode signal (V) vs. time (seconds)

• Instead of fitting a single long sample for ω , we can apply the Ramsey method: fit 2 samples for $\Delta\phi$ with light off in between for time Δt

• Freq. difference $(\omega_{\text{MT}} - \omega_{\text{MB}}) = \Delta\phi_{\text{MT-MB}}(t_f) - \Delta\phi_{\text{MT-MB}}(t_i)$

• d_{Hg} signal = $\Delta_{\text{HV}}[(\omega_{\text{MT}} - \omega_{\text{MB}}) - 1/3(\omega_{\text{OT}} - \omega_{\text{OB}})]$

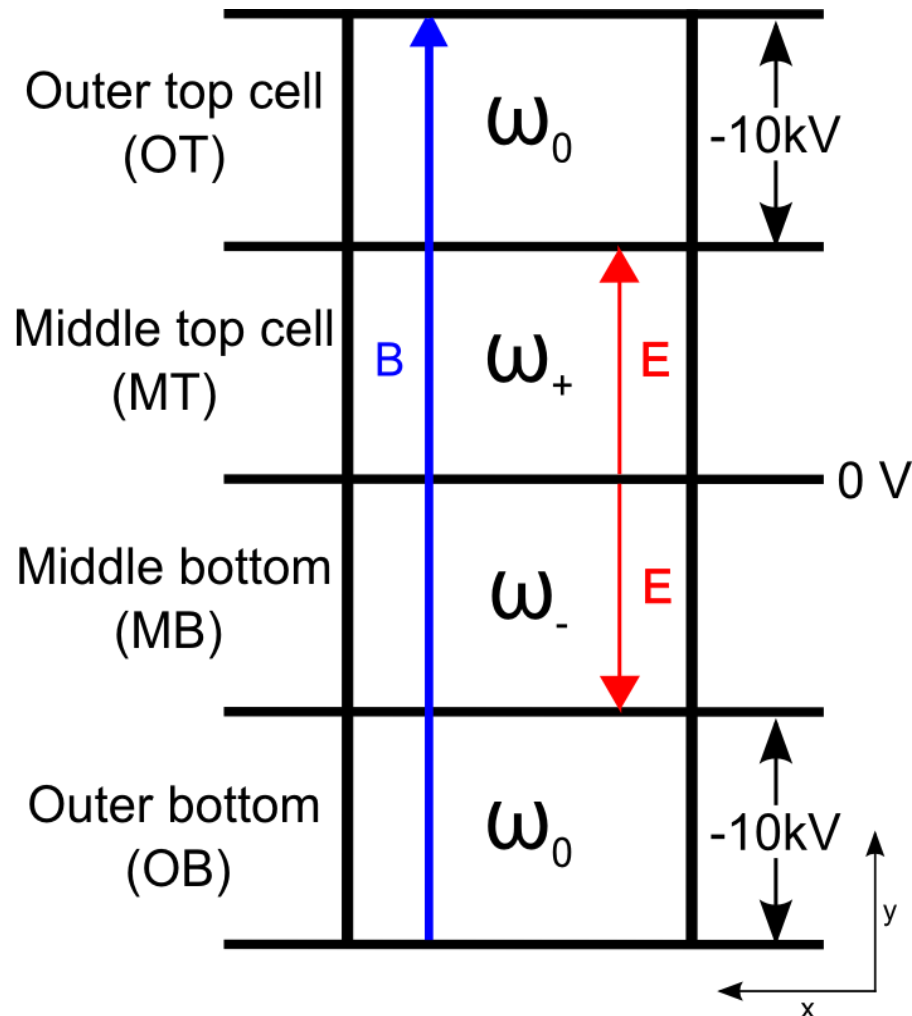
Digital Phase Analysis

- For each pair of cells, we measure $\Delta\omega$ from $\Delta\varphi_{\text{initial}}$ and $\Delta\varphi_{\text{final}}$
- For cell a or b, our signal is proportional to $S_{a,b}(t) = \sin(t\omega \pm t\Delta\omega + \varphi \pm \Delta\varphi)$
- It can be shown that if $\omega\Delta t = \pi/2$, then

$$S_1(t) * (1/2)[S_2(t + \Delta t) - S_2(t - \Delta t)] - S_2(t) * (1/2)[S_1(t + \Delta t) - S_1(t - \Delta t)] \\ = \sin(2t\Delta\omega + 2\Delta\varphi) \approx 2t\Delta\omega + 2\Delta\varphi$$

- The data can then be fit to a straight line
- We tune our precession frequency ω_0 to match the condition $\omega\Delta t = \pi/2$ for our analog-to-digital conversion rate (2 kHz, 10 points averaged, $\Delta t = 5$ ms)
- $\Delta\varphi_{\text{initial}}$ is measured at the end of the first probe period, $\Delta\varphi_{\text{final}}$ is measured at the beginning of the second probe period

B Gradient Noise Reduction



- With our 4-cell setup, outer 2 cells are used as magnetometers

- EDM signal is equivalent to a 3rd-order B_y field gradient correlated with \mathbf{E} :

$$\mathbf{d}_{\text{atom}} = \Delta_{\text{HV}} [(\omega_{\text{MT}} - \omega_{\text{MB}}) - 1/3(\omega_{\text{OT}} - \omega_{\text{OB}})]$$

- In principle, this should cut down \mathbf{B} field gradient noise

- In practice, outer cells are more useful for looking at potential systematics

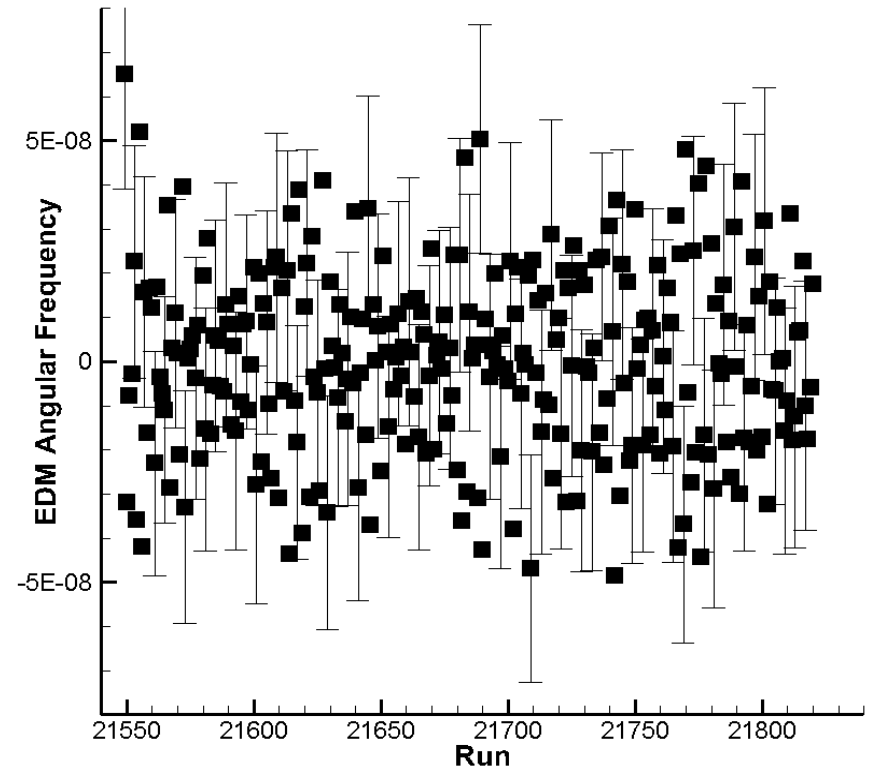
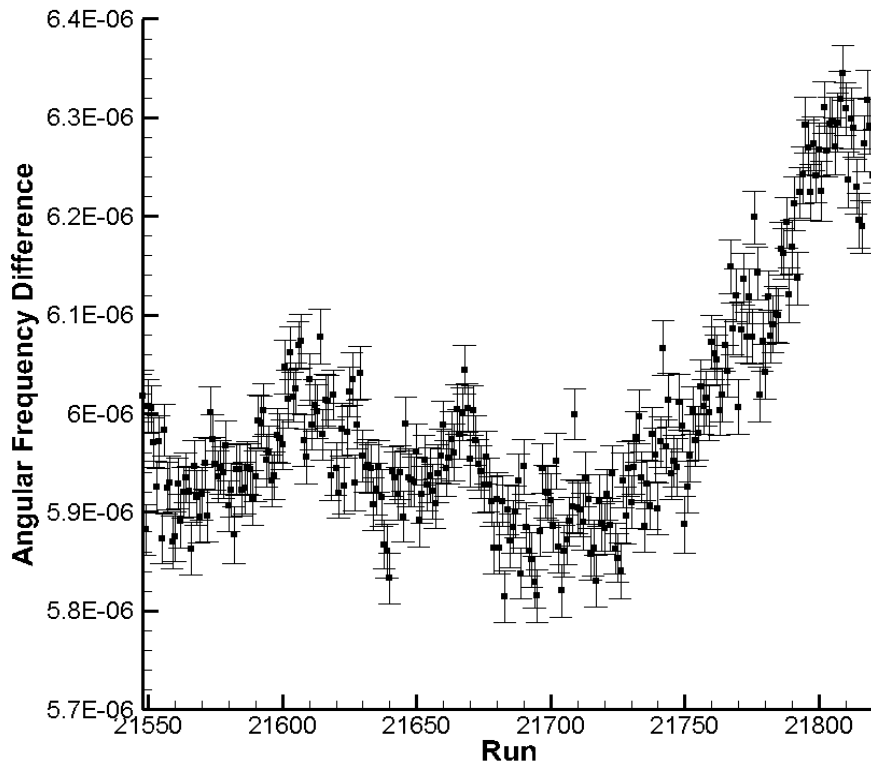
- Blind offset is applied to EDM-sensitive channels

HV Correlation Analysis

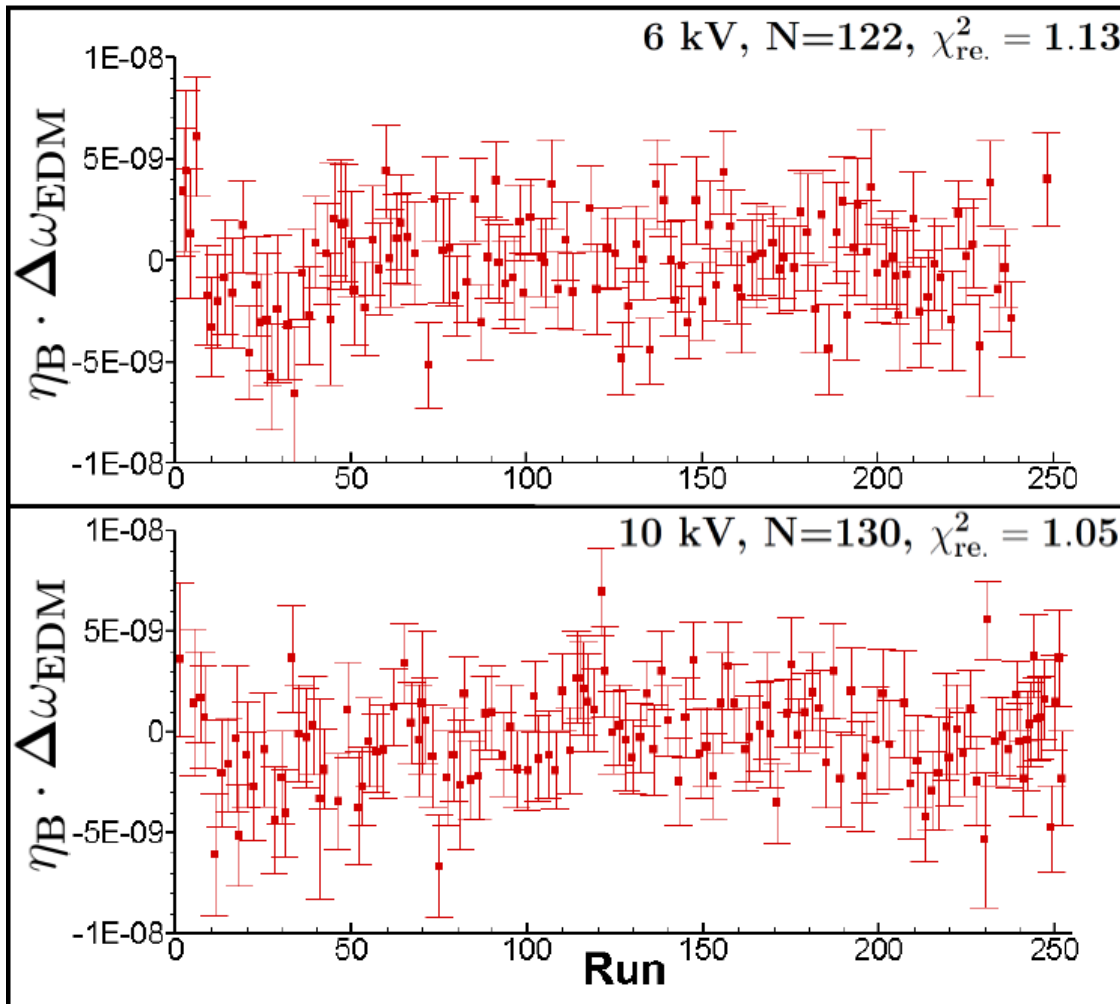
.Raw frequency difference measurements are dominated by low-frequency noise on B-field gradient

.Take the HV-correlated signal: $(-1)^i \{ (1/2)(\Delta\omega_{i-1} + \Delta\omega_{i+1}) - \Delta\omega_i \}$

.Resulting signal is insensitive to slow drifts in the 3rd-order B_y gradient

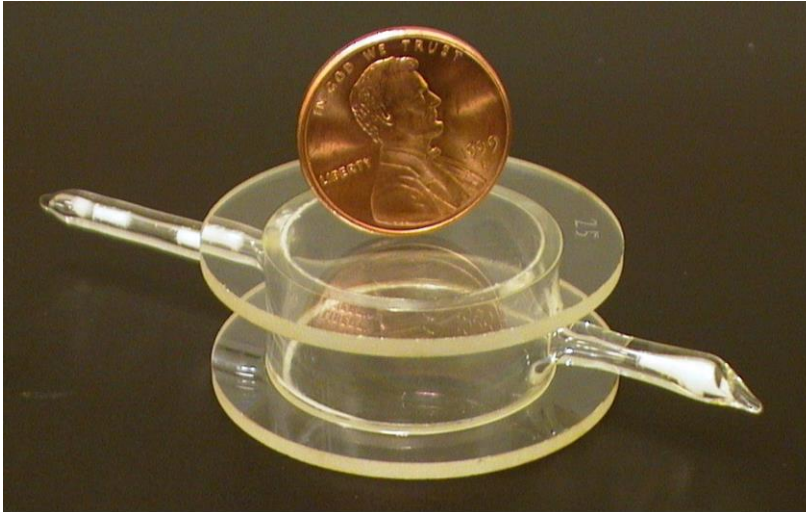


Statistical Performance



- 2009 EDM paper had statistical sensitivity of $6.43 \cdot 10^{-10} \text{ s}^{-1}$
- New data set has an avg. daily error bar $2.0 \cdot 10^{-9} \text{ s}^{-1}$
- 252 runs remain after cuts
- New EDM data set has a stat. error of $1.45 \cdot 10^{-10} \text{ s}^{-1}$

Performance Improvements

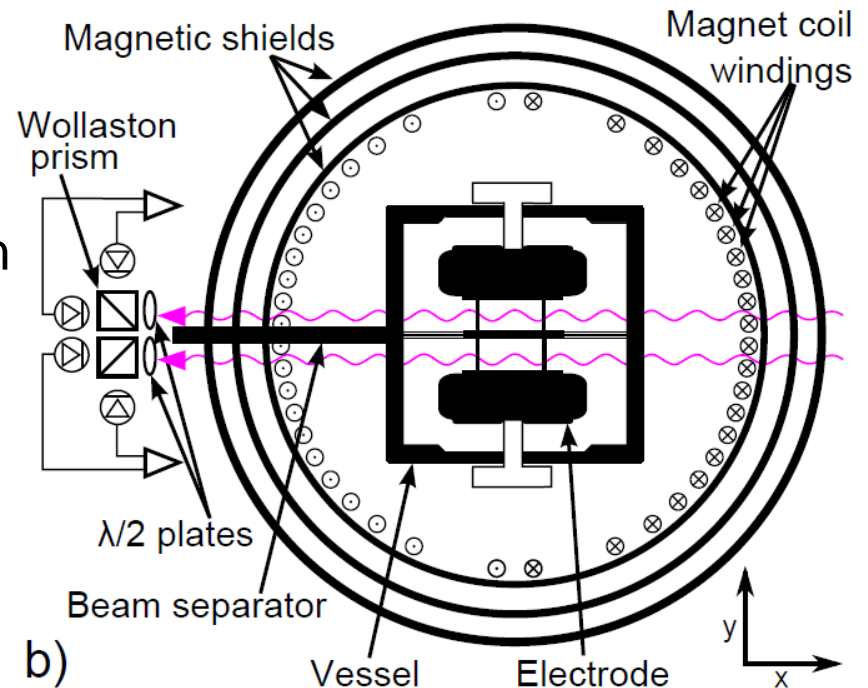


- New generation of vapor cells have coherence lifetimes of 500-1000s (up from 100-200s)

- New cells do not lose coherence time with UV exposure

- New data analysis technique eliminates frequency shifts, relaxation due to probe light

- New magnet coil allows for better trimming of **B**-field gradients, less eddy-current magnetic noise



Vapor Cell Development

- UV curing epoxy contains sulfur, can outgas and react with Hg
- New cells are bonded with Lesker KL-5 vacuum leak sealant
- Droplets of Hg can be found on waxed inner cell surfaces
- Liquid Hg in droplets or films exchanges unpolarized atoms with polarized vapor
- Resonant UV light promotes nucleation in saturated Hg vapor

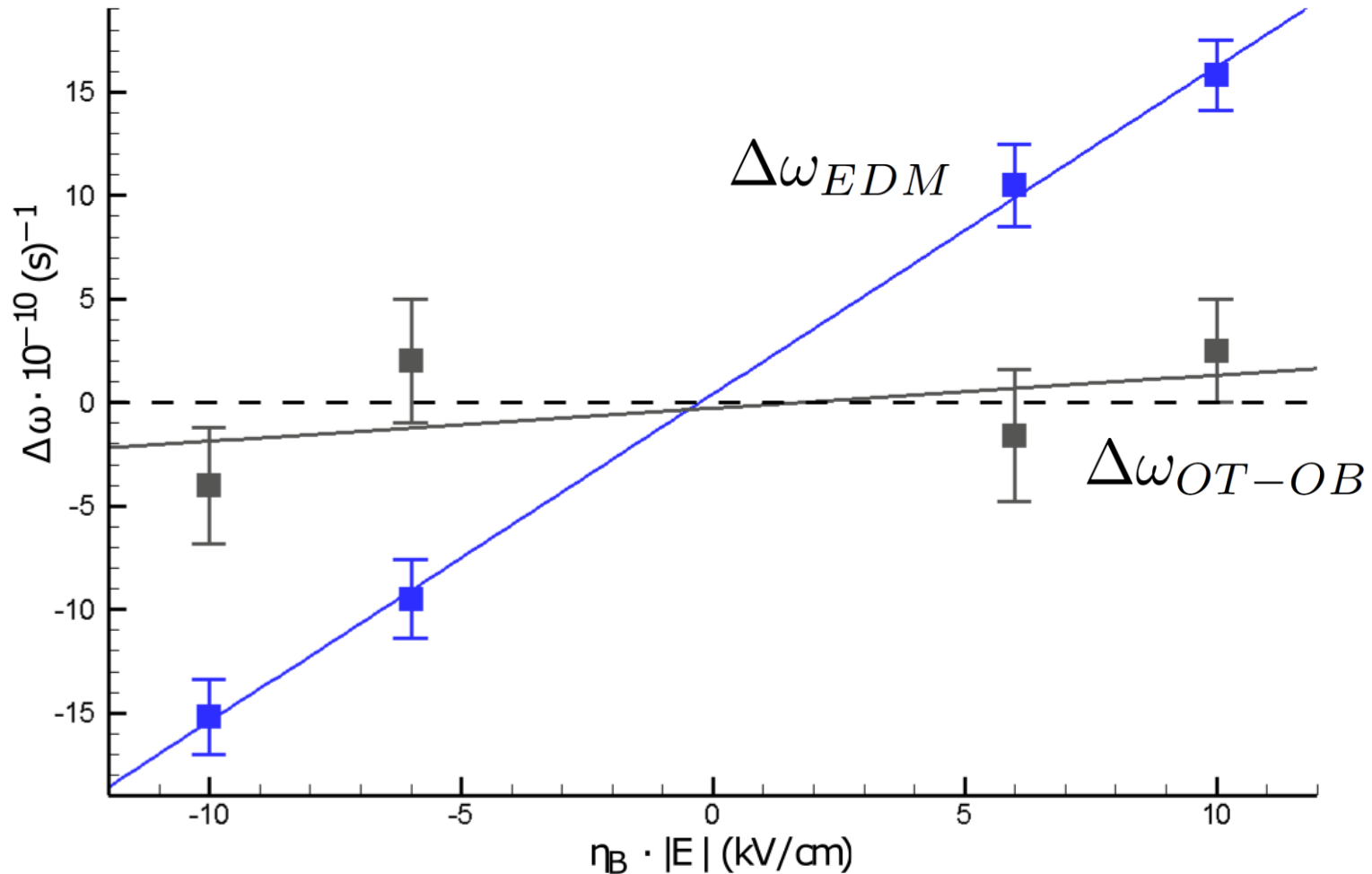


Systematic Performance

Source	Error (10^{-31} e cm)
Axial Cell Motion	12.6
Leakage Currents	5.02
Radial Cell Motion	3.36
E ² effects	3.04
Parameter Correlations	2.33
$\mathbf{v} \times \mathbf{E}$ \mathbf{B} fields	2.29
Charging Currents	1.83
Geometric Phase	0.06
<u>Quadrature sum</u>	14.8

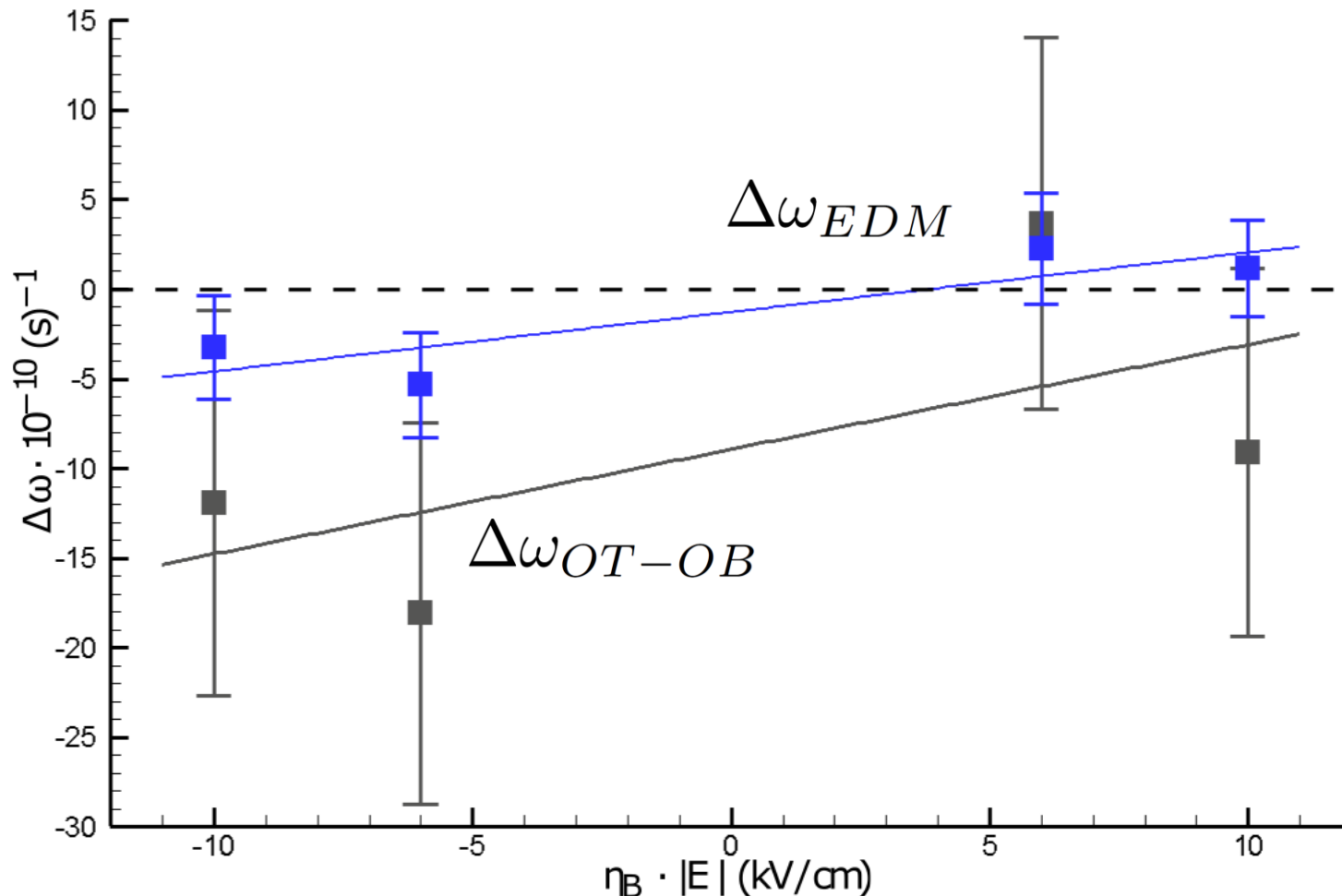
EDM Field Dependence

• A substantial nonzero EDM signal would be linear, with no outer cell HV correlation

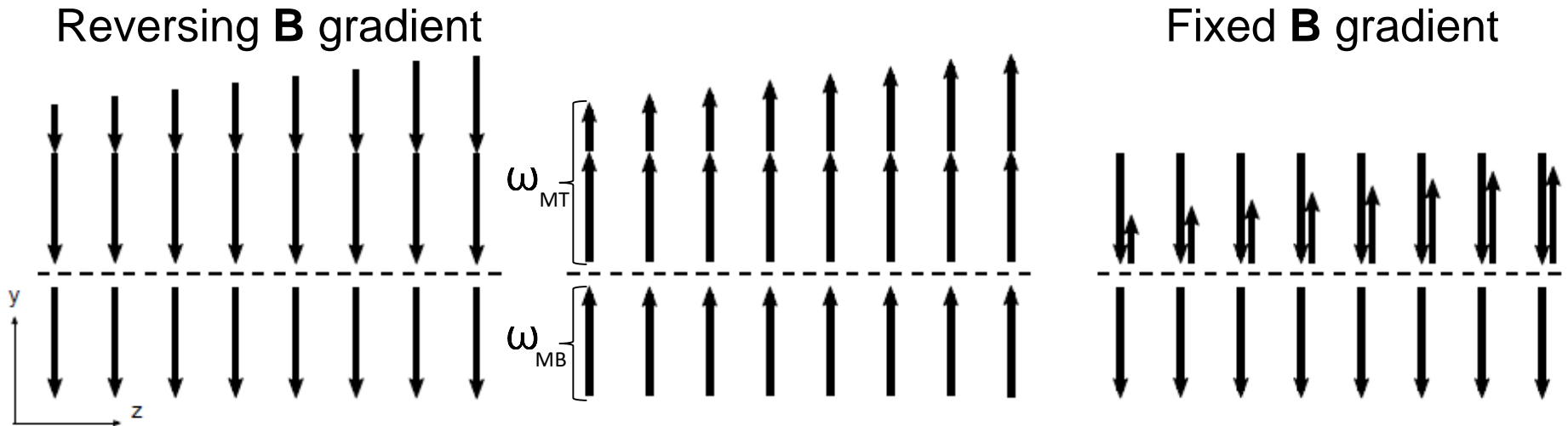


Systematics: Cell Motion

- Latest EDM data has a HV-correlated outer cell difference
- Errors and field dependence suggest this is driven by linear gradients



Systematics: Cell Motion



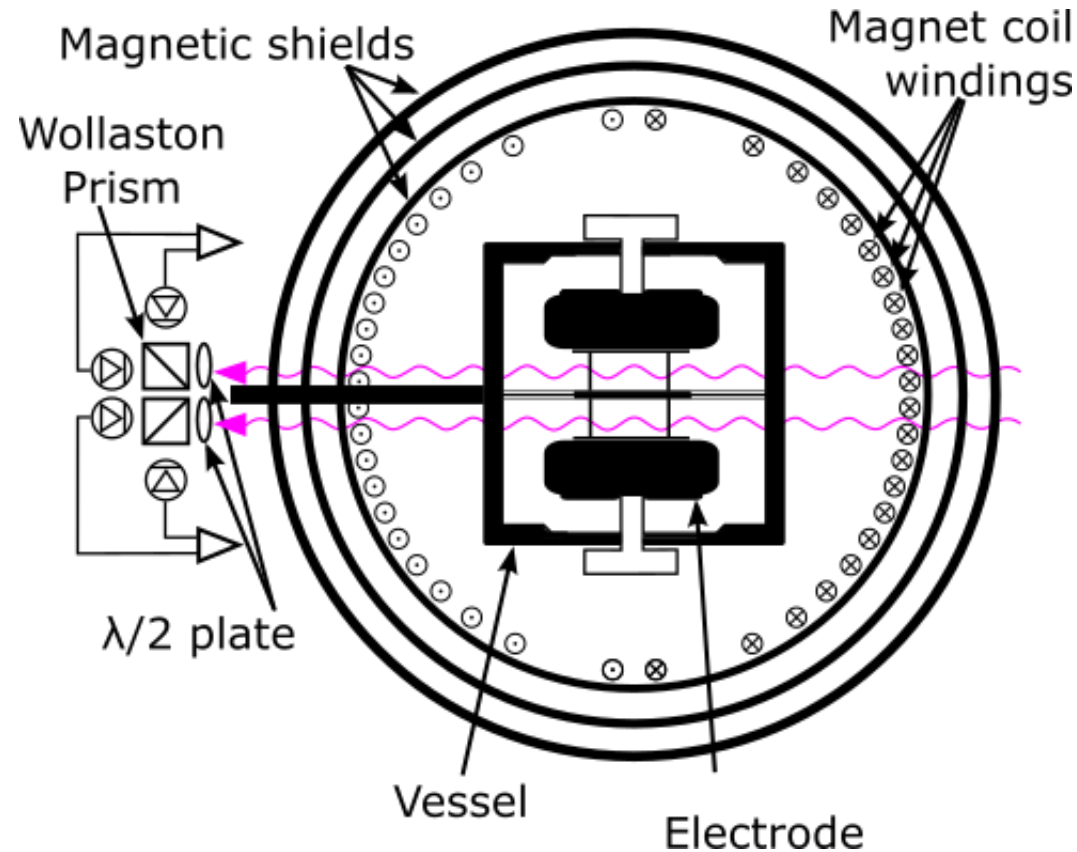
- HV-correlated cell motion through \mathbf{B} gradients generates frequency shifts
- Gradients that reverse with \mathbf{B}_0 will give a fixed freq. shift
- Fixed gradients give a reversible freq. shift-mimics EDM behavior
- Gradients perpendicular to the shield axis reverse to within 5%

Systematics: Cell Motion

.Gradients perpendicular to the shield axis reverse to within 5%

.5% of the part of the EDM frequency shift signal that does not reverse with \mathbf{B}_0 is the Radial Cell Motion systematic

.Measured \mathbf{B} gradients suggest this motion is approximately 2 nm



Source	Error (10^{-31} e cm)
Axial Cell Motion	12.6
Radial Cell Motion	3.36

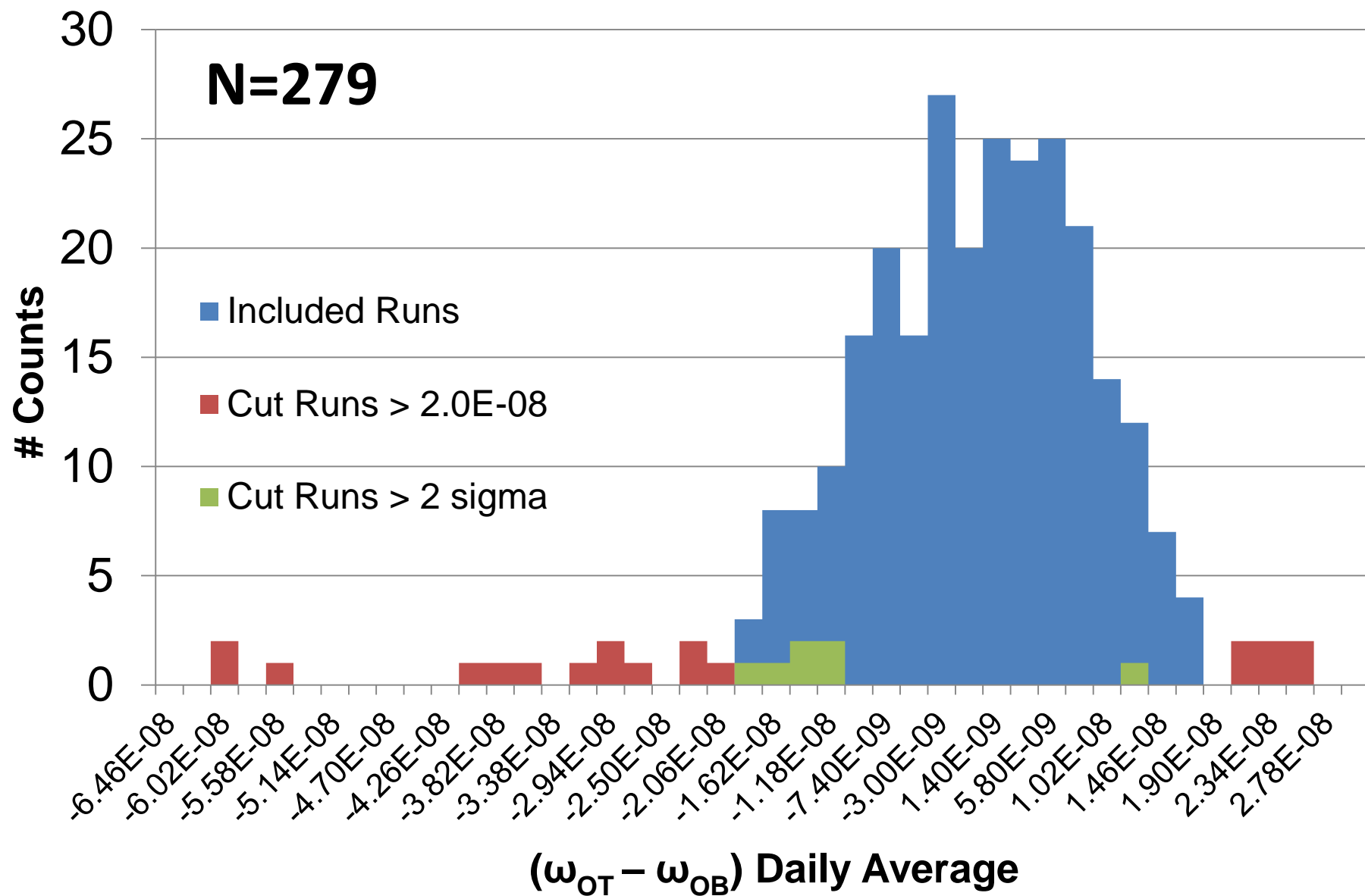
Axial Motion Constraints From Cut Data

- We have 285 completed days (runs) in the data set
- 32 days were excluded from the set b/c of HV-correlated ($\omega_{OT} - \omega_{OB}$)
- Cut criteria:
 1. $|\Delta\omega_{OT-OB}| > 2.0\sigma$ or $2.0 \times 10^{-8} \text{ s}^{-1}$
 2. $|\Delta\omega_{(OT-MT)+(OB-MB)}| > 3.0\sigma$ or $1.5 \times 10^{-8} \text{ s}^{-1}$
- We use the set of excluded data (32 cut runs + 63 systematic runs) to estimate the EDM dependence on outer cell $\Delta\omega$ due to axial motion:

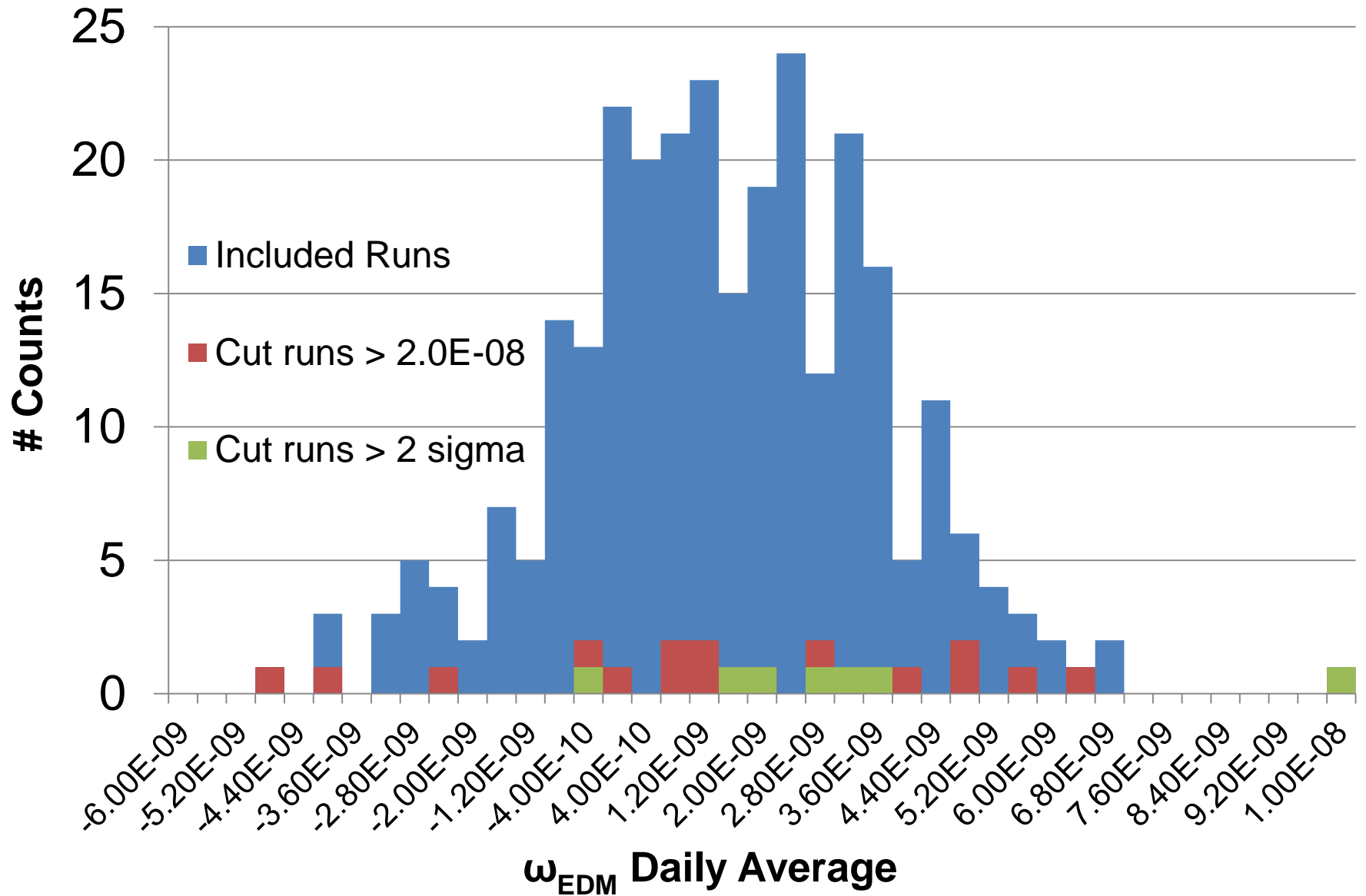
$$\frac{\eta_B \cdot (\Delta\omega_{EDM}^{ex.} - \Delta\omega_{EDM})}{\eta_B \cdot (\Delta\omega_{OT-OB}^{ex.} - \Delta\omega_{OT-OB})} = (1.6 \pm 5.7) \times 10^{-2}$$

- Excluded runs show that 7% of the outer cell freq. difference feeds through onto EDM channel

Outer Cell Daily Avg. Freq. Difference



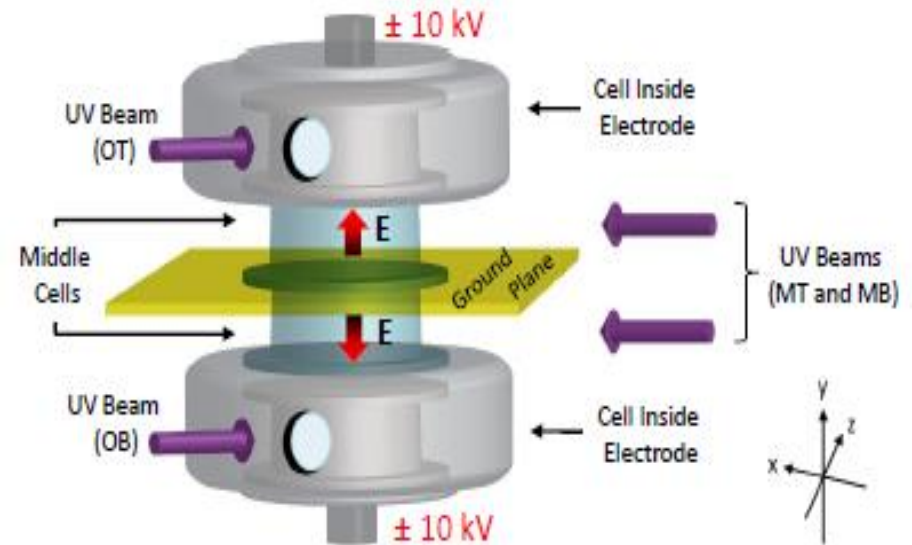
EDM Result Bias



Systematics: Leakage Currents

- '09 EDM data leakage current correlation = 0.42 pA
- Flowing dry N₂ continuously helps reduce leakage
- Field emission from sharp points on electrode surfaces can be reduced by polishing
- Ground plane coating of SnO₂ instead of Au eliminates photoelectric currents
- New measurement has 5 or 10x less leakage current than prev. measurement

Source	Error (10 ⁻³¹ e cm)
Leakage Currents	5.0
Quadrature sum	14.8



Systematics: Parameter Correlations

- Signals correlated with EDM and HV are treated as potential systematics
- Each parameter contribution is the product of correlations + 1σ
- Total systematic $\Delta\omega = 1.41 \cdot 10^{-11}$ (cf. statistical error $\Delta\omega = 1.45 \cdot 10^{-10}$)

Parameter	HV correlation	error	EDM Sig. correlation	error	Systematic
Avg. Lifetime	-2.72E-05	5.57E-04	-1.50E-09	7.97E-10	1.17E-12
Avg. Amplitude	2.45E-06	1.50E-06	-6.51E-07	6.02E-07	3.33E-12
Transmission	-3.40E-06	6.14E-06	2.83E-08	2.78E-08	2.96E-13
Laser Int.	-3.06E-07	7.91E-07	9.54E-08	9.93E-08	1.11E-13
Diode Current	6.72E-09	4.62E-08	8.82E-06	7.42E-06	4.70E-13
Green Piezo	5.18E-08	3.55E-06	6.36E-10	3.93E-09	2.30E-15
UV Piezo	2.29E-07	3.12E-07	-5.36E-10	2.62E-09	7.45E-16
Grad Coil 1	2.12E-10	1.64E-09	-5.74E-05	3.34E-04	1.30E-13
Grad Coil 2 (endcaps)	1.71E-09	2.81E-09	-3.89E-05	1.12E-04	2.87E-13
Grad Coil 3	8.60E-11	1.37E-09	1.04E-04	2.65E-04	1.53E-13
Main Coil	-1.30E-09	3.40E-09	1.89E-05	1.37E-04	2.14E-13
dBy/dx Coil	1.09E-10	2.85E-09	3.53E-05	2.69E-05	1.04E-13
Bx	-2.41E-05	2.46E-05	-1.36E-07	1.83E-08	6.66E-12
By	5.06E-08	1.60E-07	-2.37E-08	6.62E-09	5.01E-15
Bz	-1.35E-05	5.96E-06	-4.10E-07	4.49E-08	8.05E-12
Fluxgate (By)	2.69E-09	2.36E-08	6.47E-07	4.69E-07	1.71E-14
Normalized Vertical quad PD	1.17E-07	9.62E-08	-6.89E-07	1.27E-06	2.43E-13
Normalized Horizontal quad PD	6.70E-08	9.78E-08	-6.89E-07	1.27E-06	1.55E-13
Slab Temperature	-3.57E-25	1.50E-15	-1.38E-06	8.59E-07	2.08E-21
Table Temperature	3.24E-25	1.50E-15	-2.83E-07	5.52E-07	4.26E-22
Air Temperature	-1.95E-05	1.62E-05	-4.72E-08	4.20E-08	2.04E-12
Chopper Frequency	2.21E-06	4.19E-06	6.19E-07	3.56E-07	4.08E-12

Systematics: E^2 Effects

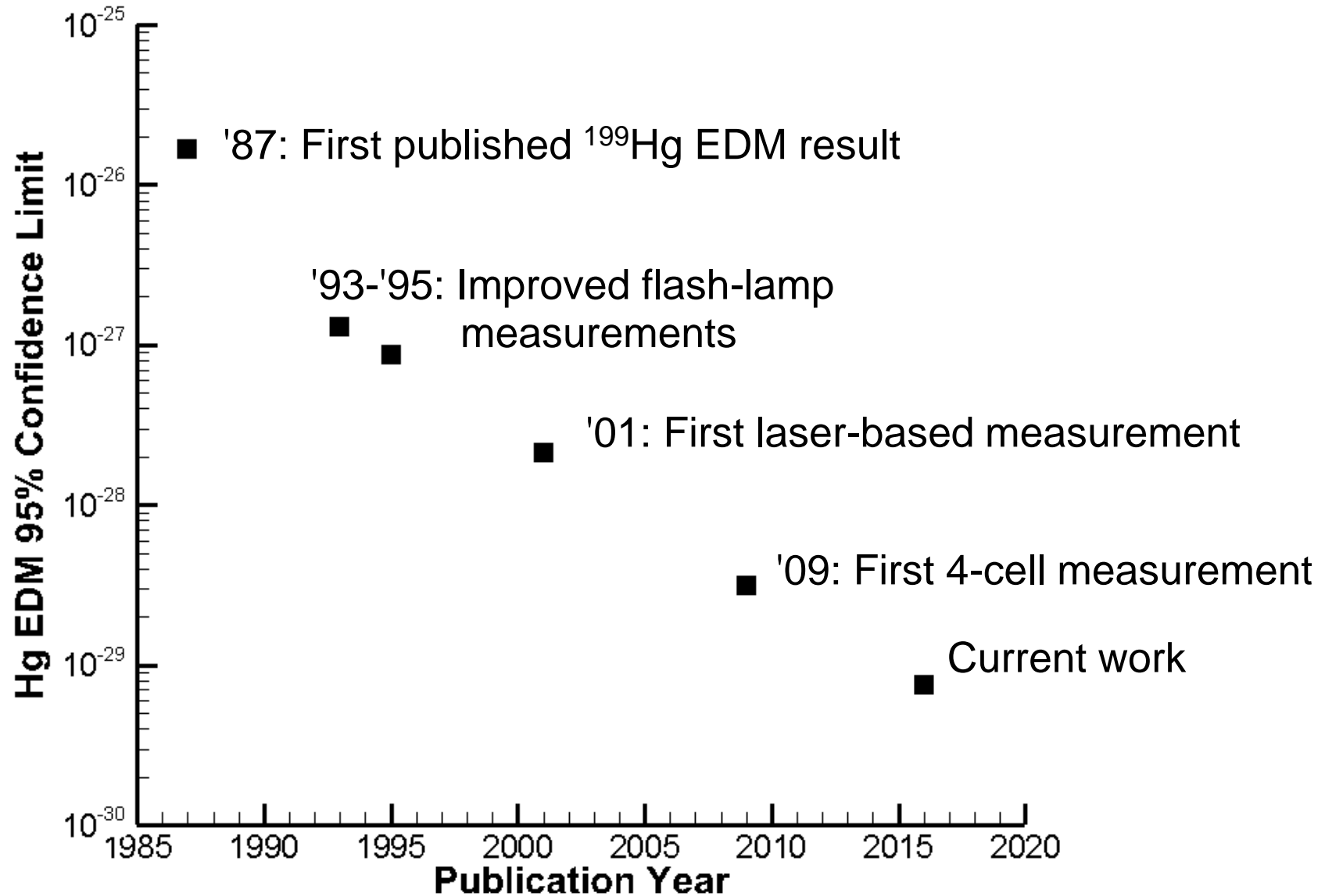
Source	Error (10^{-31} e cm)
Axial Cell Motion	12.6
Leakage Currents	5.02
Radial Cell Motion	3.36
E^2 effects	3.04
Parameter Correlations	2.33
$\mathbf{v} \times \mathbf{E}$ \mathbf{B} fields	2.29
Charging Currents	1.83
Geometric Phase	0.06
<u>Quadrature sum</u>	14.8

- Any effect that couples $\Delta\omega_{\text{EDM}}$ to $|\mathbf{E}|$ is a systematic if $|\mathbf{E}_+|$ is different from $|\mathbf{E}_-|$
- We measure $|\mathbf{E}_+| - |\mathbf{E}_-|$ using the quad. Stark shift
- Measure $\Delta\omega_{\text{EDM}}(|\mathbf{E}|)$ by taking ~ 10 scans each day at 0 kV between ± 10 kV or ± 6 kV

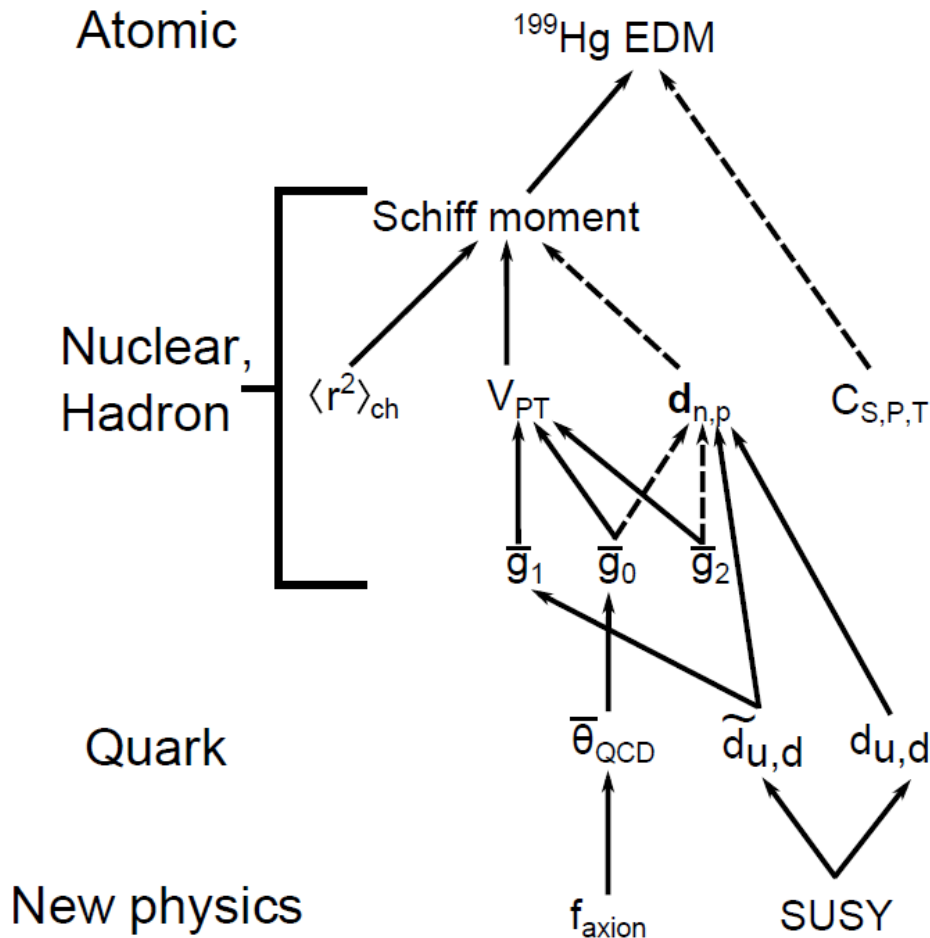
Null Result and New Limits

- We find ^{199}Hg EDM $d_{Hg} = (2.20 \pm 2.75_{stat} \pm 1.48_{syst}) \times 10^{-30} e \cdot \text{cm}$
- Combined error bar $\sigma = 3.123 \times 10^{-30} e \cdot \text{cm}$
- Set a 95% confidence limit by solving $\frac{1}{\sigma\sqrt{2\pi}} \int_{-L}^L e^{-(\mu-x)^2/2\sigma^2} dx \geq 0.95$
- New upper limit on $|d_{Hg}| < 7.4 \times 10^{-30} e \cdot \text{cm}$
- Improves our 2009 limit $|d_{Hg}| < 3.1 \times 10^{-29} e \cdot \text{cm}$ by a factor of 4
- If theoretical calculations are correct, $|d_{Ra}| < 7.5 \times 10^{-27} e \cdot \text{cm}$

Hg EDM Limits vs. Time



Hg EDM Limits on CP-odd Parameters



• Hg EDM results can be used to put limits on CP-odd parameters

• It is necessary to assume the EDM has only 1 contribution

• $d_{\text{Hg}} < 7.4 \cdot 10^{-30} \text{ e cm}$

• $\rightarrow \theta_{\text{QCD}} < 8.5 \cdot 10^{-11}$

• $d_n < 1.6 \cdot 10^{-26} \text{ e cm}$

The Team

Blayne Heckel

Norval Fortson

Eric Lindahl

Jennie Chen

Former Students and Postdocs:

Tom Loftus

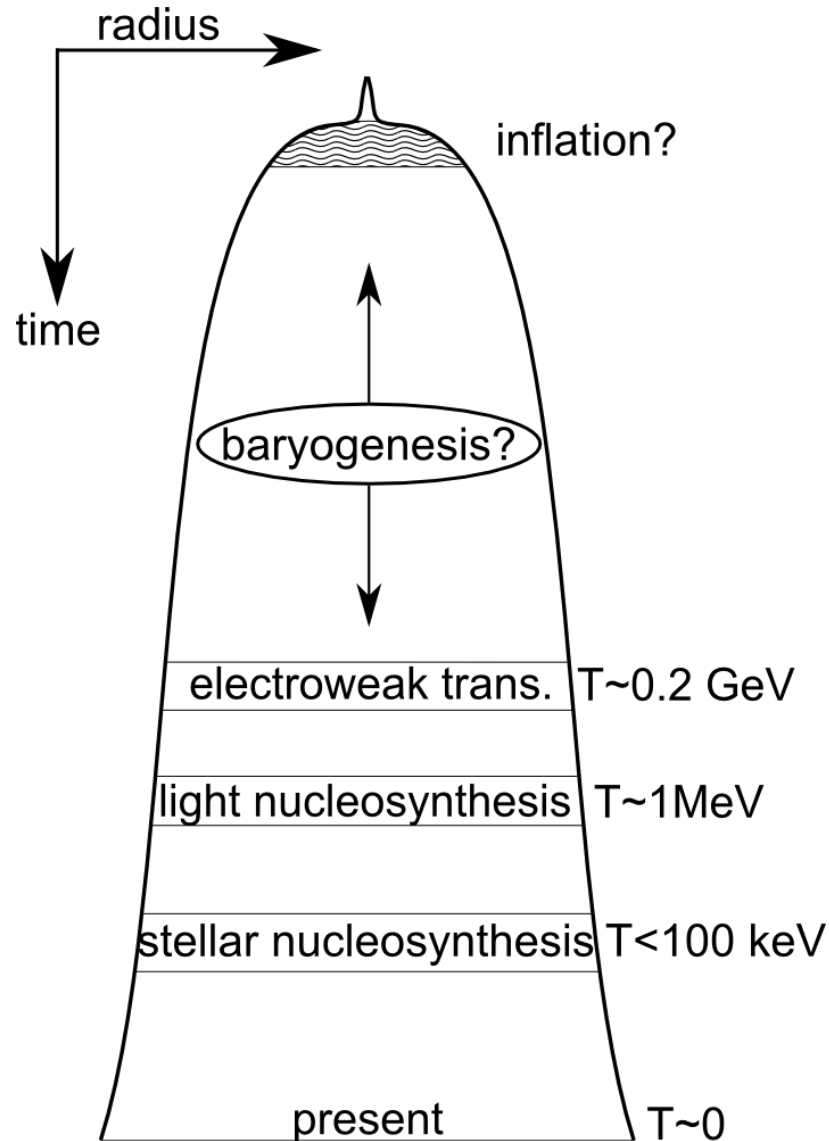
Nathan Kurz

Adam Kleczewski

Clark Griffith

Matt Swallows

CP violation and baryogenesis



- No theory explains the ‘excess’ of matter over antimatter:

$$\eta = \frac{n_B - n_{\bar{B}}}{\gamma} = (6.14 \pm 0.25) \cdot 10^{-10}$$

- Any baryogenesis model needs to satisfy the Sakharov conditions:
 - 1. Baryon number violation
 - 2. CP symmetry violation
 - 3. Departures from thermal equilibrium
- Higgs is too massive for a workable theory based in standard model physics

What does a B-violating process look like?

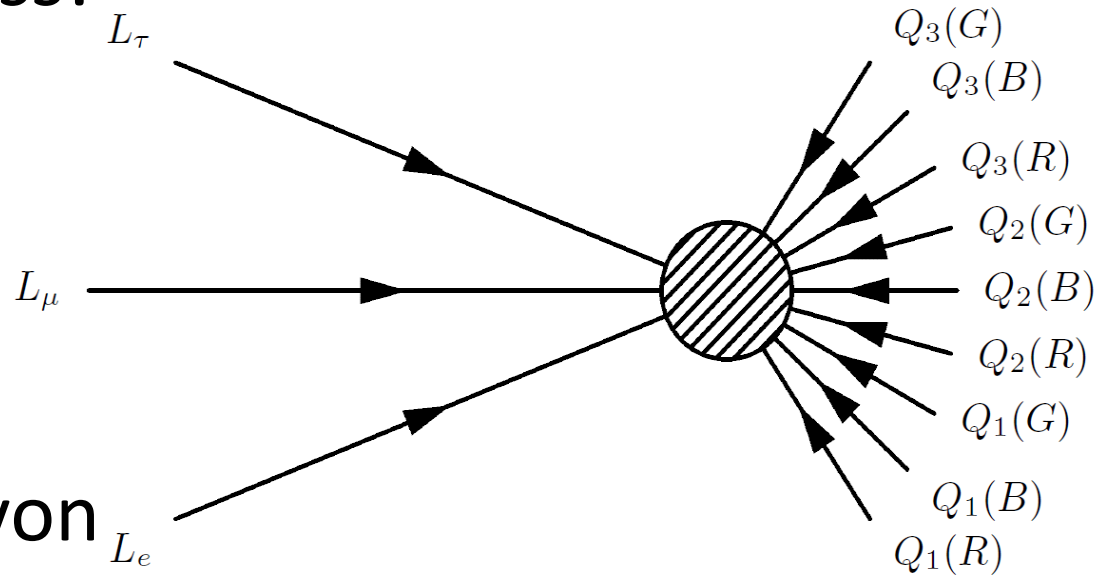
- Best-known example is the *sphaleron process*:

- $\Delta B = +/-3$

- Conserves B-L

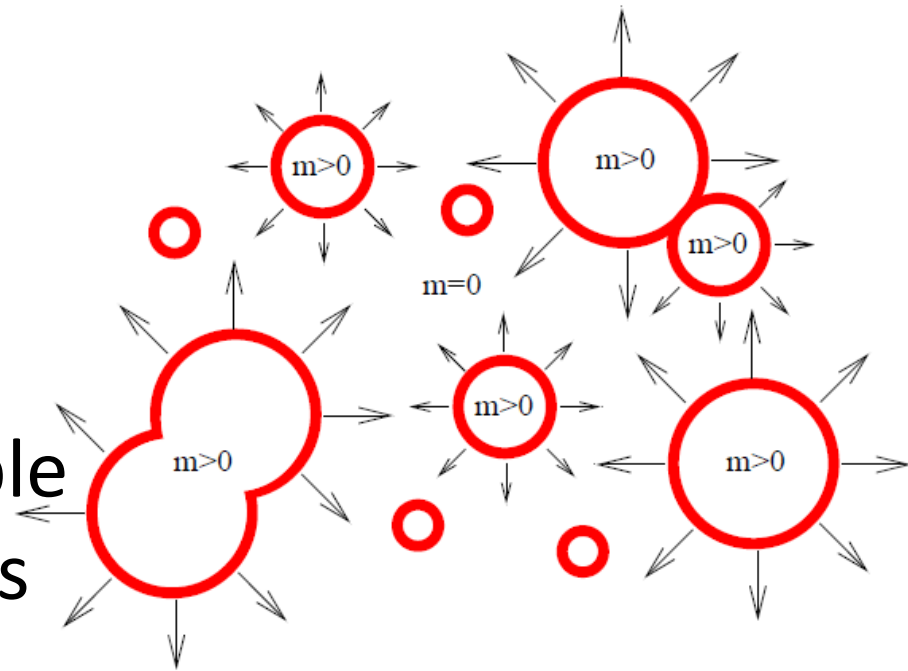
- Suppressed below ~ 100 GeV

- Could generate baryon excess from lepton excess (*leptogenesis*)

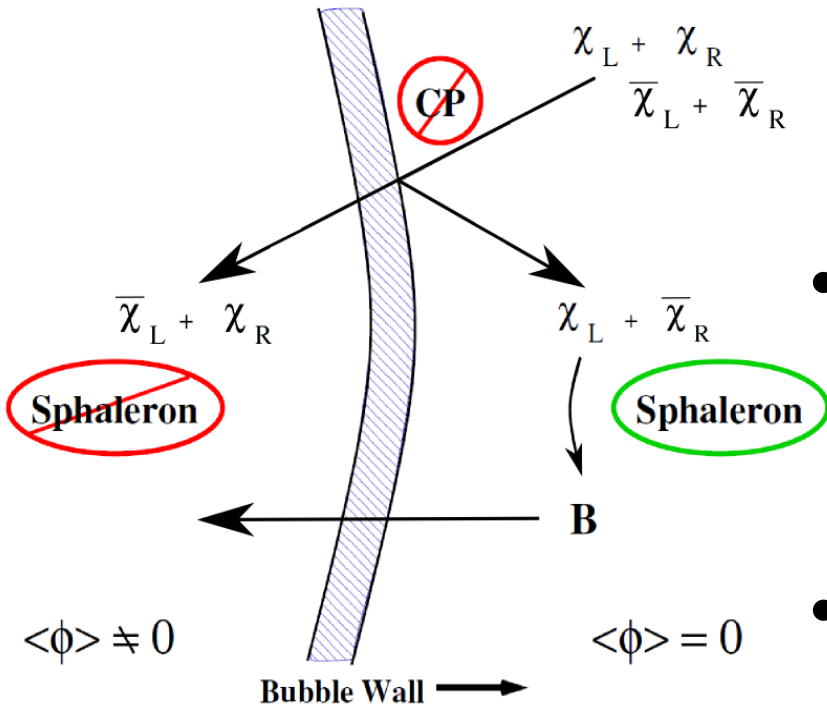


Out-of equilibrium decay: Electroweak baryogenesis (EWBG)

- Popular baryogenesis models focus on the EW symmetry breaking
- Higgs field acquires multiple vacuum expectation values
- Regions of broken EW symmetry can expand like bubbles
- Interactions at the walls violate CP, are out of eq.

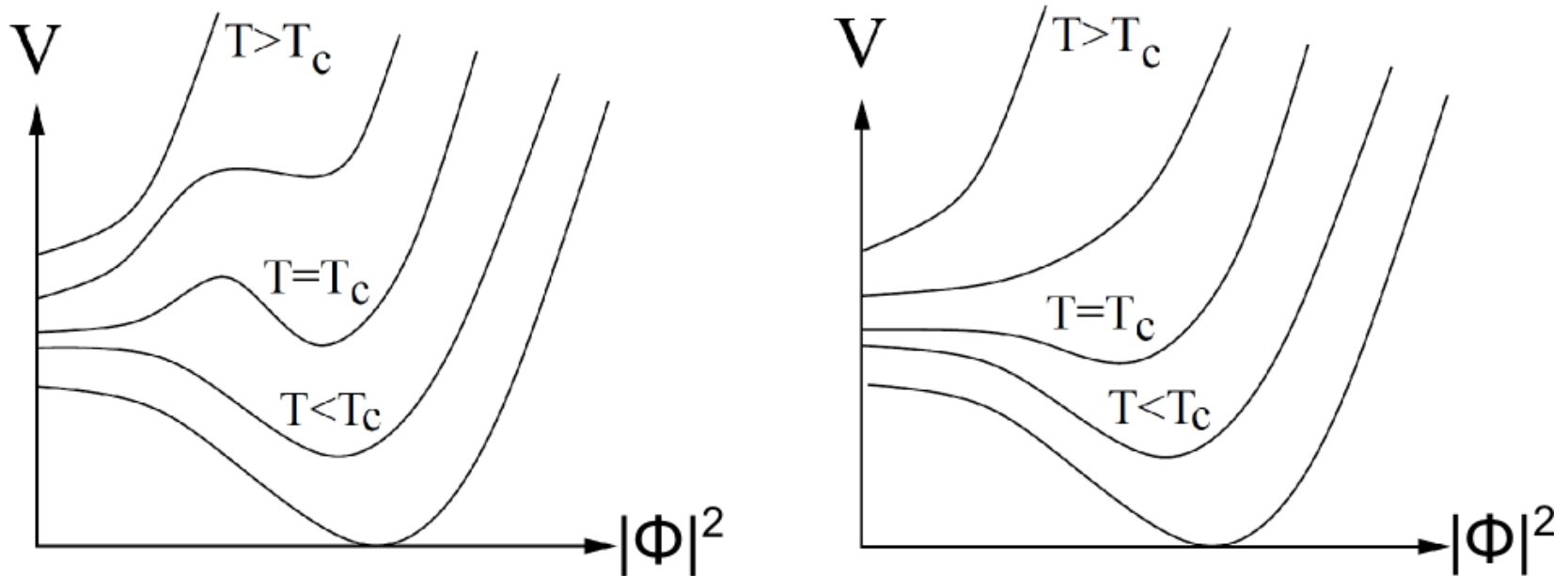


Where do the baryons actually come from?



- CP-violating interactions at the wall reflect LH particles, RH antiparticles
- Sphaleron process does not couple to RH (anti)particles, is frozen out by large $M_{W,Z}$
- Net flux of baryons outside diffuses in before eq. is established

First-order phase transitions in EWBG



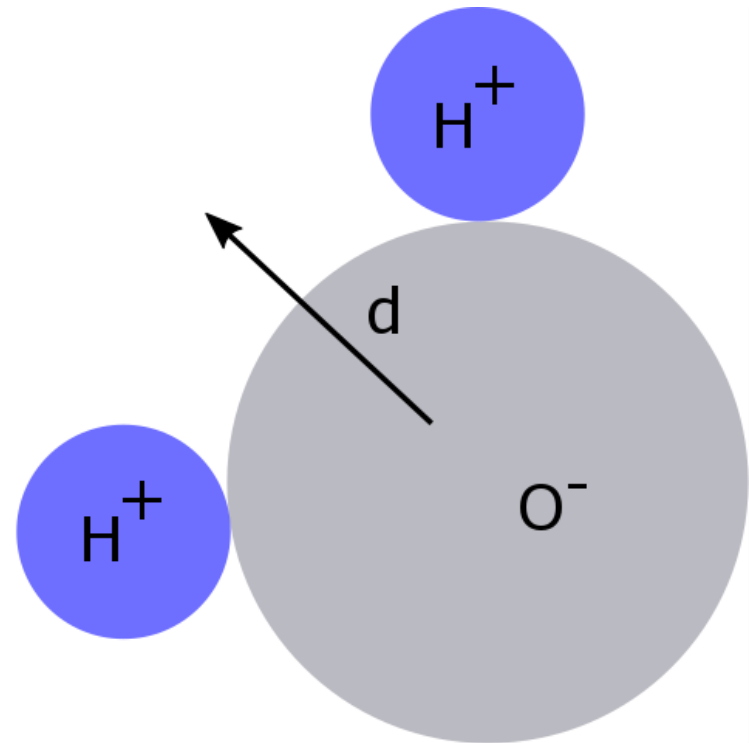
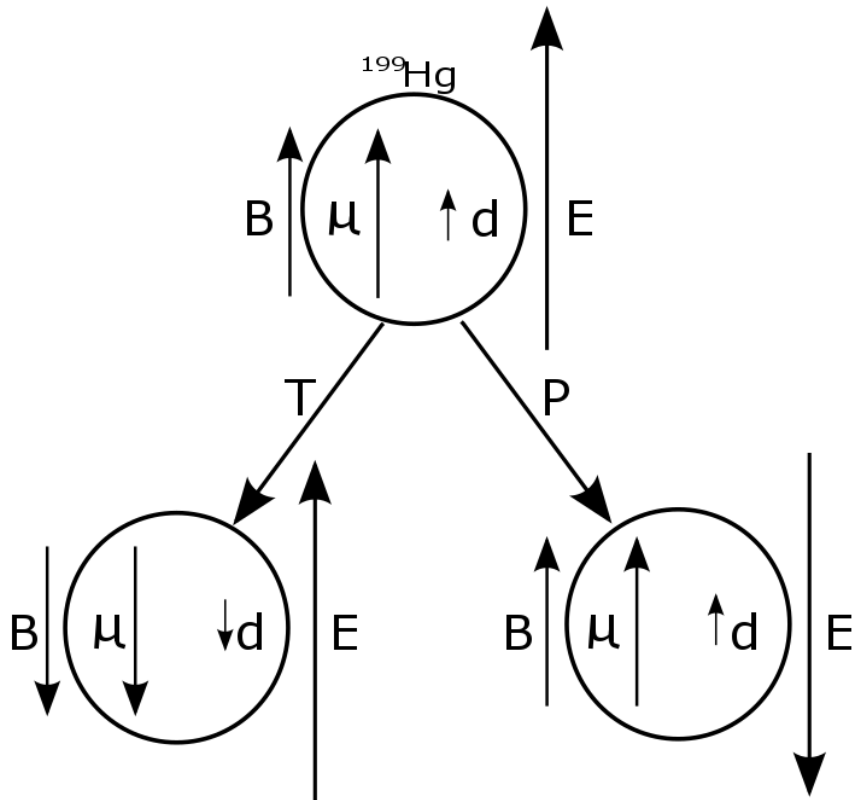
- For bubble nucleation, the electroweak symmetry breaking must be a first-order phase transition
- The effective Higgs potential at high temp. must have degenerate minima ($T = T_c$, left diagram)

Can this happen under the Standard Model?

- No.
- CP-violation in the CKM matrix is insufficient to create large enough particle number asymmetries outside the bubbles of non-zero Higgs VEV
- Electroweak symmetry-breaking transition in the SM cannot involve bubble nucleation with $M_{\text{Higgs}} > 75 \text{ GeV}$

Atomic vs. Molecular EDMs

- Parity violation requires a fixed EDM projection onto spin axis
- Molecules have additional degrees of freedom-EDMs have no definitive spin projection



Cell Motion Causes

	Sequence	MT cell	MT $\Delta\omega(10^{-10}\text{s}^{-1})$	MB cell	MB $\Delta\omega(10^{-10}\text{s}^{-1})$
.Magnetic shielding defects may cause gradients	1	IV	(-6.82 ± 7.7)	II	(-7.32 ± 7.7)
	2	II	(-31.70 ± 7.5)	IV	(17.20 ± 8.3)
	4	V	(-8.05 ± 9.0)	IV	(-5.20 ± 8.7)
.HV-correlated quadratic gradients appear larger on top	5	IV	(-5.17 ± 8.2)	V	(1.28 ± 7.1)
	6	II	(-7.35 ± 6.9)	V	(-2.29 ± 6.6)
	7	II	(2.16 ± 5.8)	V	(10.00 ± 5.5)
	8	V	(2.50 ± 6.5)	II	(-2.05 ± 6.1)
.Welded shield seam is nearest outer top cell	9	II	(13.10 ± 6.8)	V	(-15.6 ± 6.6)
	10	IV	(6.28 ± 7.9)	V	(-7.33 ± 7.4)
	11	V	(7.52 ± 8.8)	IV	(-6.49 ± 8.8)
.Effect of cell motion changes from sequence to sequence	12	IV	(-9.45 ± 9.4)	II	(-0.98 ± 9.2)
	13	II	(-4.04 ± 7.2)	IV	(-7.48 ± 7.2)
	14	V	(-27.30 ± 8.3)	II	(28.50 ± 8.3)
	Average:		(-4.24 ± 2.1)		(-0.02 ± 2.0)