

Kaon Electromagnetic Form Factor

Presented
by

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Scientific Motivation

- ❖ What are the form factors for strange mesons?
- ❖ How to validate different models of meson structure (form factor)?
- ❖ Does the pole of kaon meson dominate the longitudinal cross-section?
- ❖ How do the Longitudinal and Transverse cross-sections depend on the Q^2 (i.e. Test for QCD factorization)?

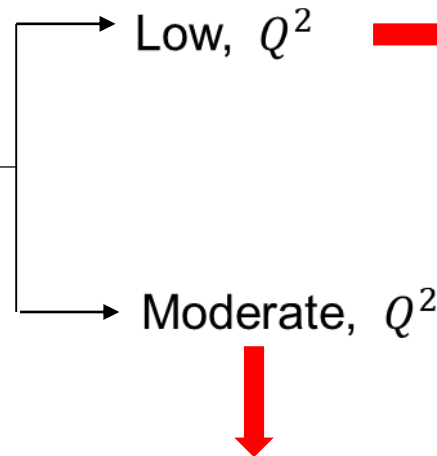
Meson Form Factor

Form factor: Elastic electron hadron scattering, $eK \rightarrow e'K'$

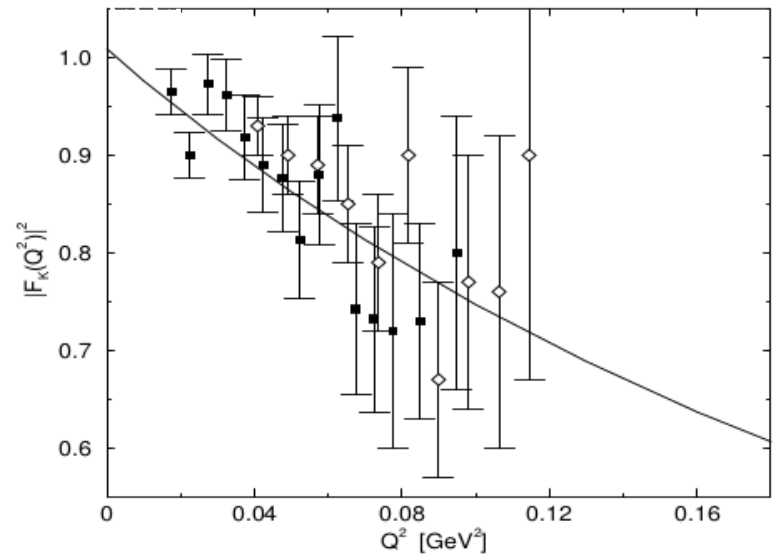
$$(p_1 + p_2) F_K(Q^2) = \langle K(p_2) | J_\mu(0) | K(p_1) \rangle$$

- ❖ Electromagnetic F_K , can be calculated exactly at very large momentum transfer Q^2 , with perturbative QCD

Form factor



JLab regime



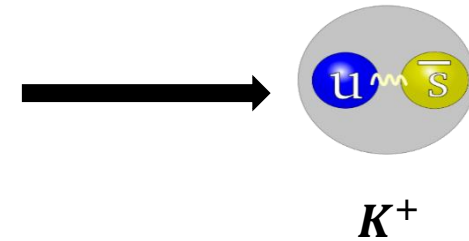
[Amendolia, et al., PL B178 (1986) 435]

$$\sqrt{\langle r_K^2 \rangle} = 0.53 \pm 0.05 \text{ fm}$$

Meson Form Factor

For moderate Q^2 , the form factor remains a theoretical challenge

Clearest case for studying the effect in internal structure of hadron when replacing a lighter quark (d) with heavier one (s)



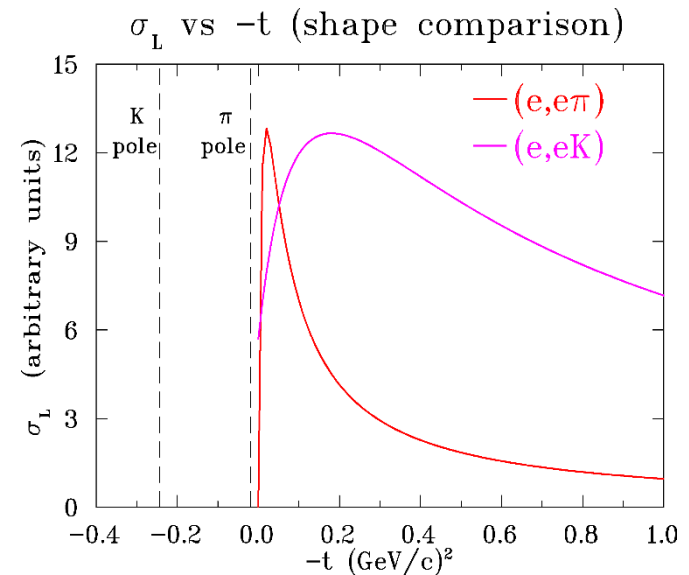
No “free” Kaon target

Kaon cloud of the proton be used in the same way as the pion to extract kaon form factor via $p(e, e' K^+) \Lambda$

The kaon pole is further away from the kinematically allowed region

In the Born term model F_K , appears as

$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_K^2)} g_{K\Lambda N}^2(t) F_K^2(Q^2, t)$$

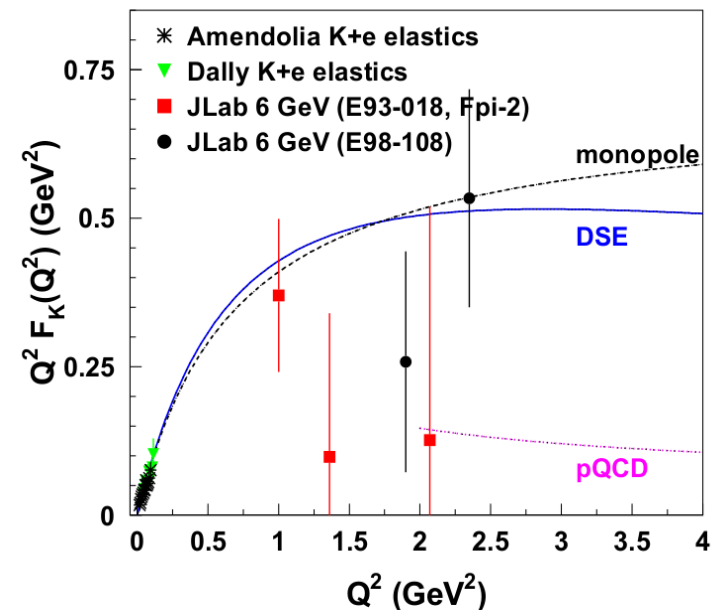


Experimental Determination of Form Factor

- ❖ Model is required to extract the Form factor from longitudinal cross-section
- ❖ First measurement of F_K well above the resonance region
- ❖ Measure form factor to $Q^2=3 \text{ GeV}^2$ with good overlap with elastic scattering data.
- ❖ Previous JLab studies lead us to expect that we can extract K^+ form factor from $-t < 0.8 \text{ GeV}^2$ σ_L data

VGL Regge model

$$F_K(Q^2) = \frac{1}{1 + \frac{Q^2}{\Lambda_K^2}}$$

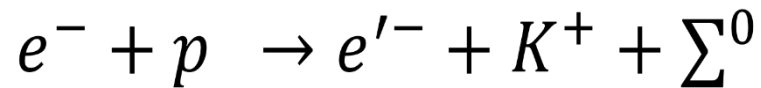


For VGL/Regge calculation, assume $\Lambda_K^2=0.67 \text{ GeV}^2$, and $\Lambda_{K^*}^2=1.5 \text{ GeV}^2$.

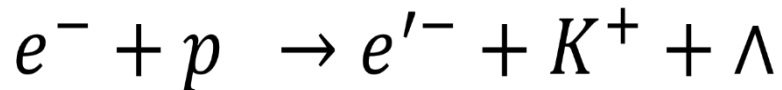
Reaction and Scattering Planes

E12-09-011, Kaon L-T

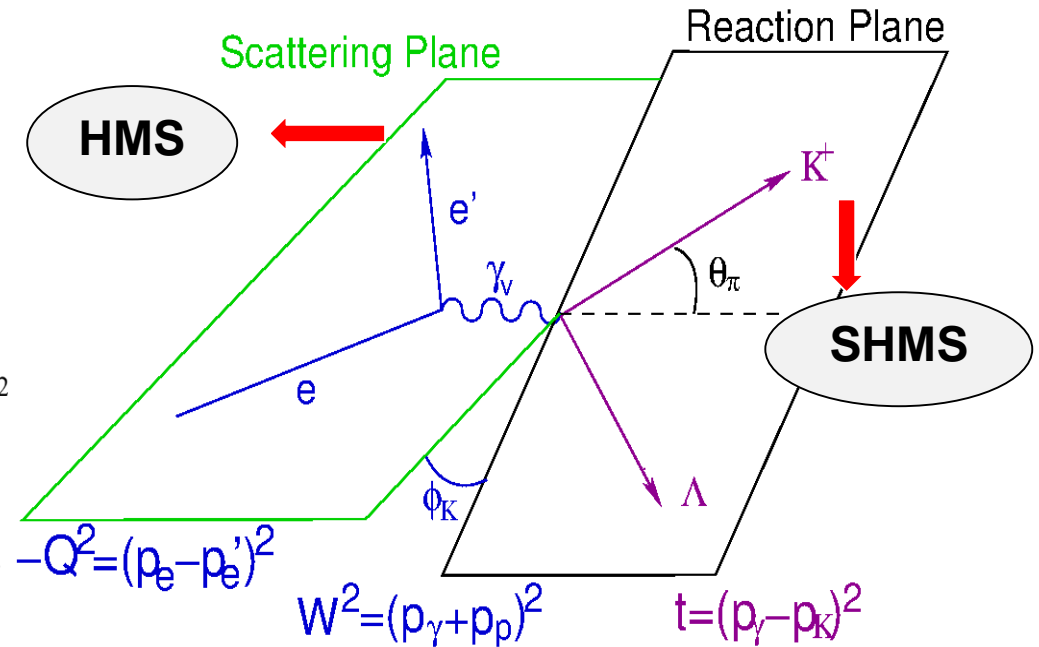
Completely exclusive reaction



$$M_{\Sigma^0} = 1192.64 \text{ MeV}^2/c^2$$



$$M_{\Lambda} = 1115.68 \text{ MeV}^2/c^2$$



Missing mass equation

$$M_{miss} = \left[(E_b + m_p - E_{e'} - E_{K^+})^2 - (\vec{P}_e - \vec{p}_{e'} - \vec{p}_{K^+})^2 \right]^{\frac{1}{2}}$$

Rosenbluth Separation Technique

Rosenbluth separation technique is required;

Measurement of cross-section at least two values of ε , while fixing the values of W , Q^2 and $-t$

$$2\pi \frac{d^2\sigma}{dtd\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

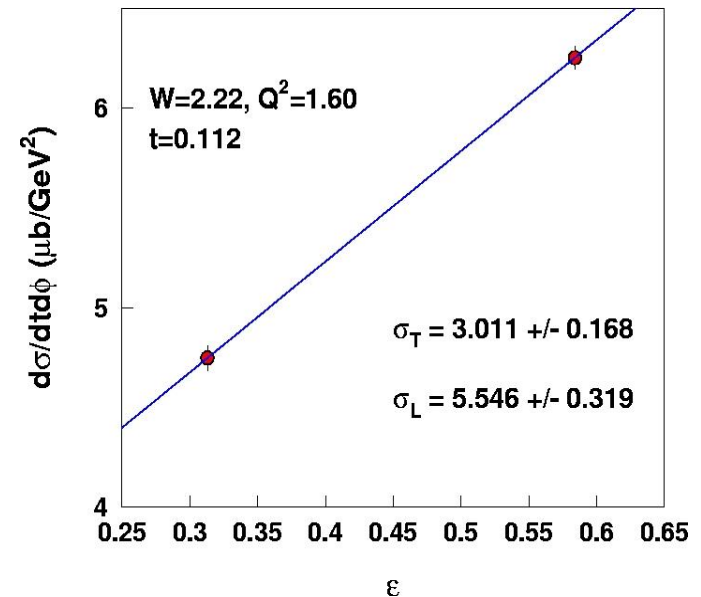
Virtual-photon polarization:

$$\varepsilon = \left(1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \tan^2 \frac{\theta_{e'}}{2} \right)^{-1}$$

L/T Separation example

❖ For parallel kinematics

$$2\pi \frac{d\sigma}{dtd\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt}$$



Kaon LT Data Collected

E12-09-011 experiment ran in Hall C at Jefferson Lab over the fall 2018 and spring 2019

E (GeV)	Q^2 (GeV ²)	W (GeV)	$x = Q^2 / 2m_p (E - E')$	$\epsilon_{\text{High}} / \epsilon_{\text{Low}}$
10.6/8.2	5.5	3.02	0.40	0.53/0.18
10.6/8.2	4.4	2.74	0.40	0.72/0.48
10.6/8.2	3.0	3.14	0.25	0.67/0.39
10.6/6.2	3.0	2.32	0.40	0.88/0.57
10.6/6.2	2.115	2.95	0.21	0.79/0.25
4.9/3.8	0.5	2.40	0.09	0.70/0.45

Rosenbluth Separation Technique

❖ For non parallel kinematics

The interference terms (LT & TT) will be separated out from the non parallel data
(i.e. detected K^+ not parallel to virtual photon momentum)

$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

Low epsilon:

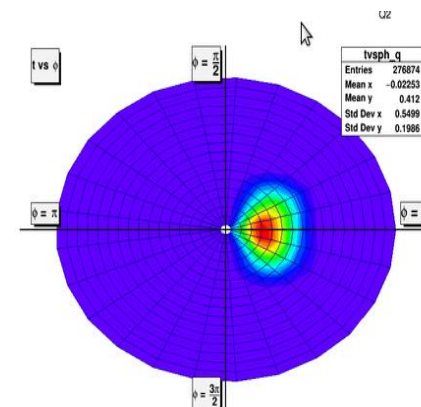
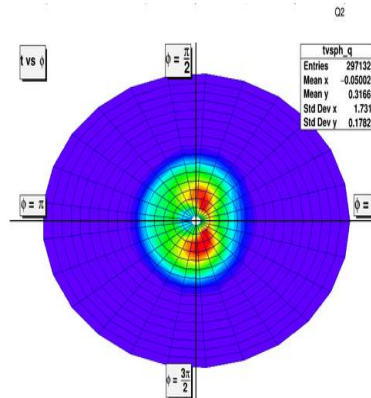
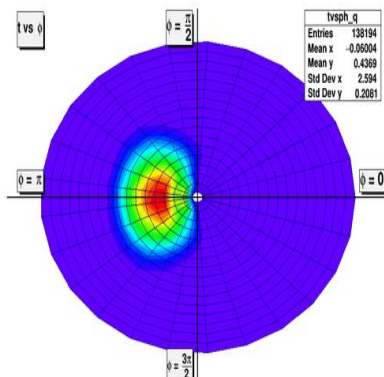
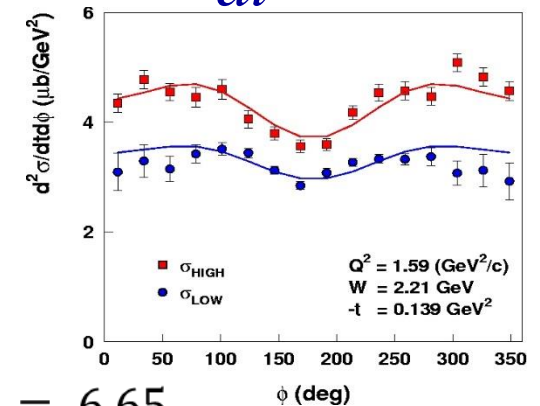
$$E_b = 10.6 \text{ GeV} \quad Q^2 = 3.0 \text{ GeV}^2 \quad W = 3.14 \text{ GeV}$$

$$x = 0.25$$

$$\theta_{SHMS} = 12.42 \text{ (Left)}$$

$$\theta_{SHMS} = 9.42 \text{ (Center)}$$

$$\theta_{SHMS} = 6.65 \text{ (Right)}$$



Subtraction of Random Coincidence

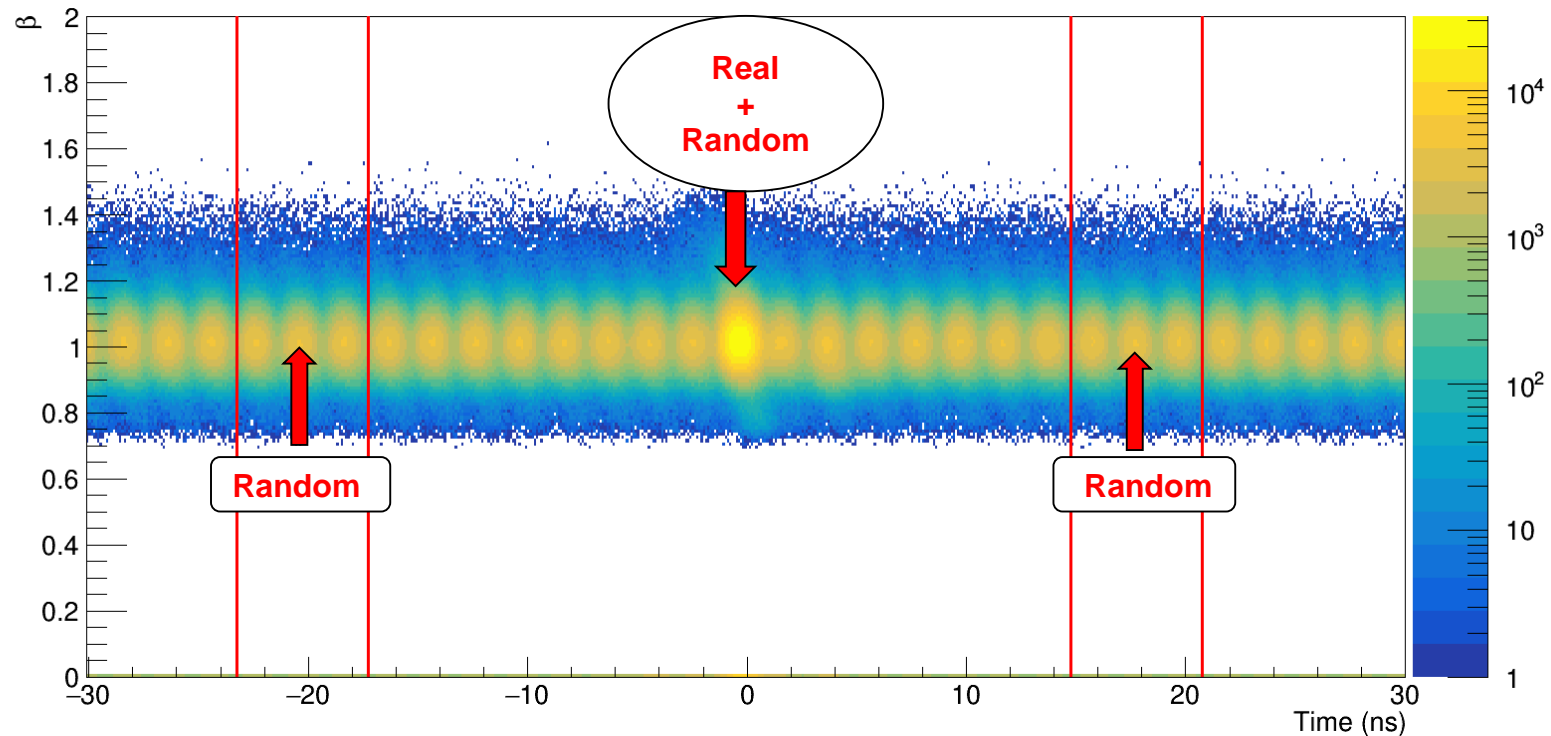
$$E_b = 4.9 \text{ GeV} \quad Q^2 = 0.5 \text{ GeV}^2$$

$$w = 2.40 \text{ GeV} \quad x = 0.09$$

$$\theta_{SHMS} = 6.0 \text{ (right)} \quad I = 16 \text{ } \mu\text{A}$$

$$t_{coin} = t_{HMS} - t_{SHMS}$$

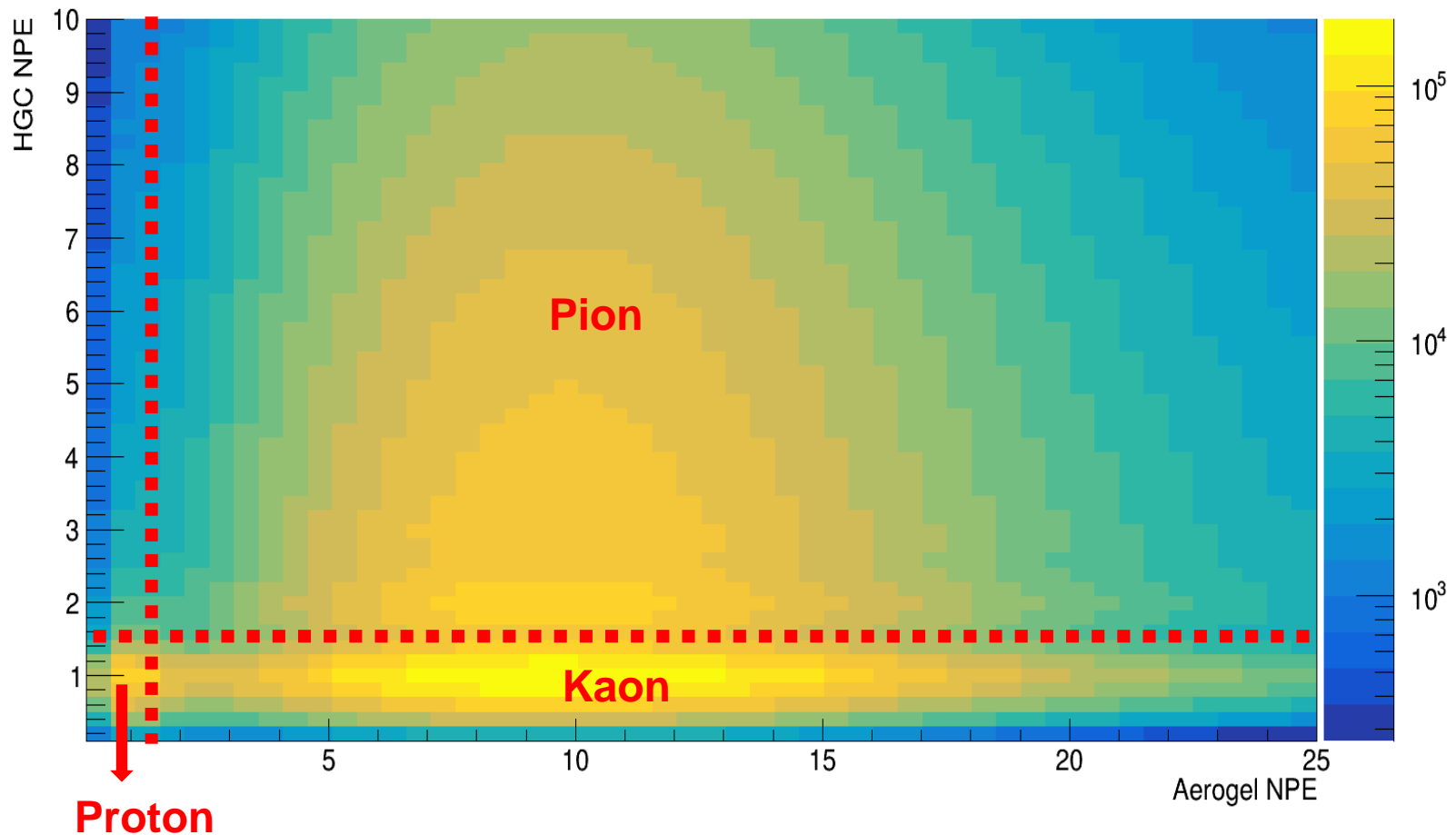
Kaon Coincident Time vs β for ROC1 (w/ particle ID)



Particle Identification (PID)

The selection of kaon is done using Heavy-Gas Cerenkov and Aerogel Cerenkov detectors

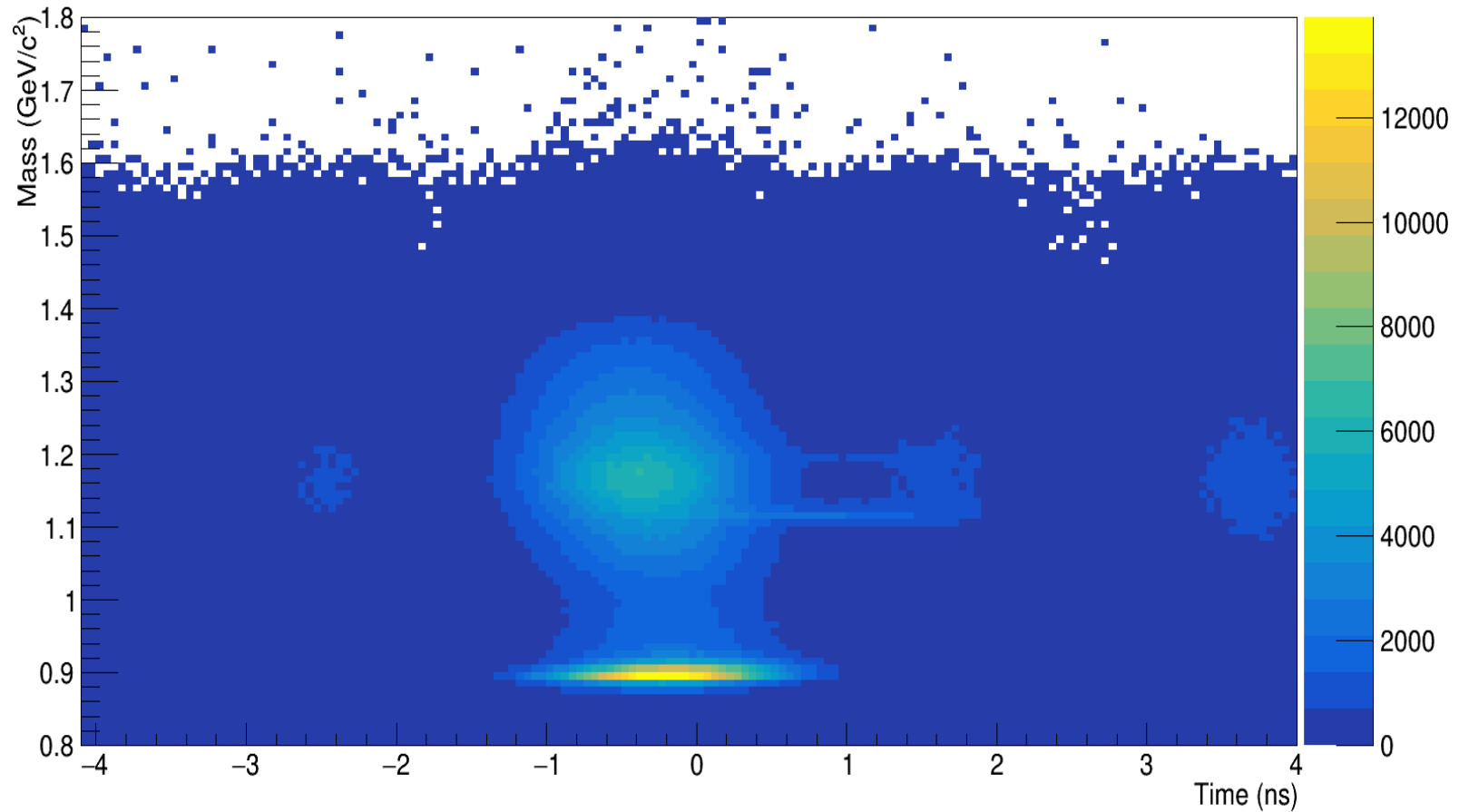
NPE in SHMS Aerogel and Heavy Gas



Missing Mass Reconstruction

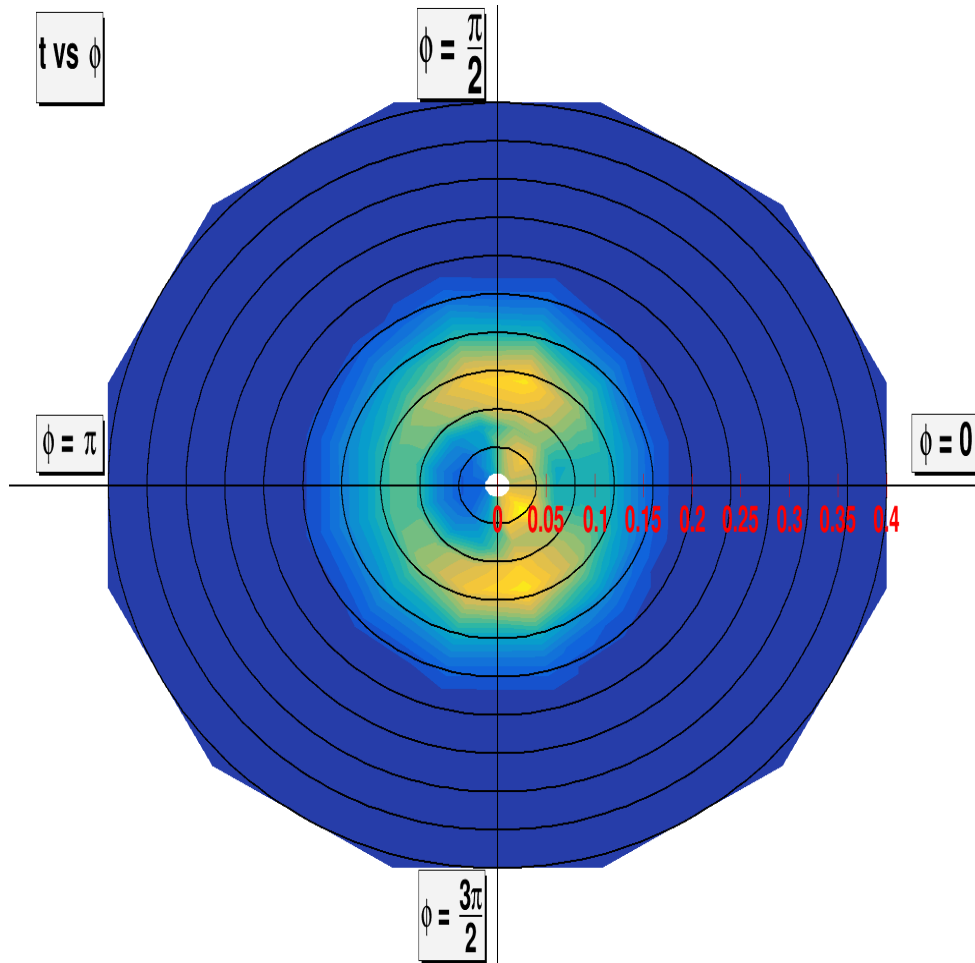
Missing mass
$$M_{miss} = [(E_b + m_p - E_{e'} - E_{K^+})^2 - (\vec{p}_e - \vec{p}_{e'} - \vec{p}_{K^+})^2]^{1/2}$$

Kaon Missing mass vs Coincidence Time

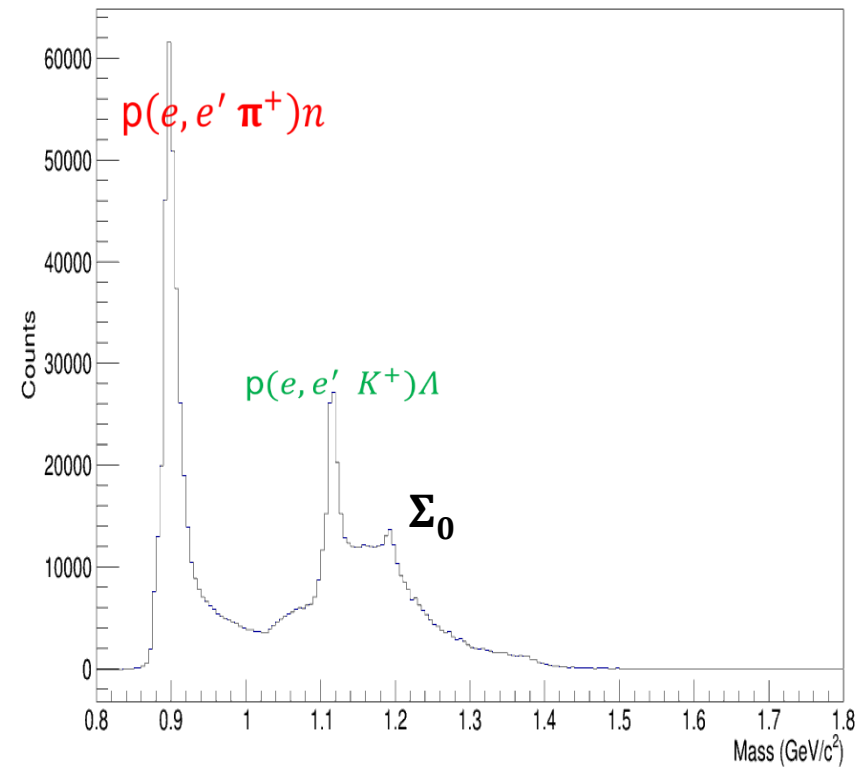


Missing Mass Reconstruction

$$M_{miss} = [(E_b + m_p - E_{e'} - E_{K^+})^2 - (\vec{P}_e - \vec{p}_{e'} - \vec{p}_{K^+})^2]^{1/2}$$



Kaon Missing mass with Cuts (Random Subtracted)



Future Perspective

- ❖ We are preparing for comprehensive particle identification (PID) analysis.
- ❖ Systematic studies on cryotarget boiling, deadtime, luminosity dependence, e-p elastic scattering to determine the reliability of data.
- ❖ Very precise measurement (separation) of the longitudinal cross-section.
- ❖ Checking that data will allow for the extraction of form factor of kaon.
- ❖ Study for the QCD factorization.

Thank you

**Thanks to CINP for
travel award**