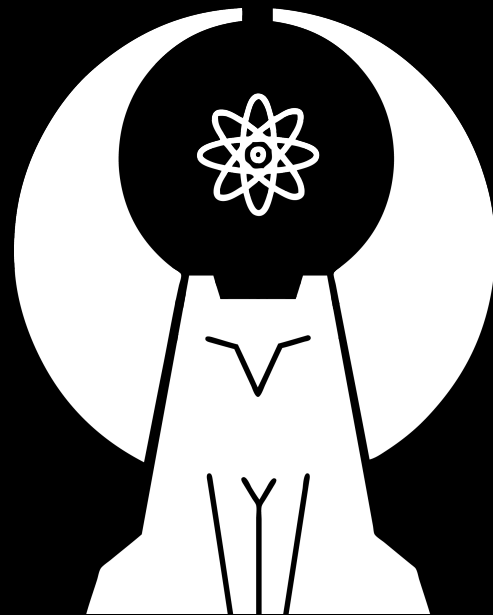


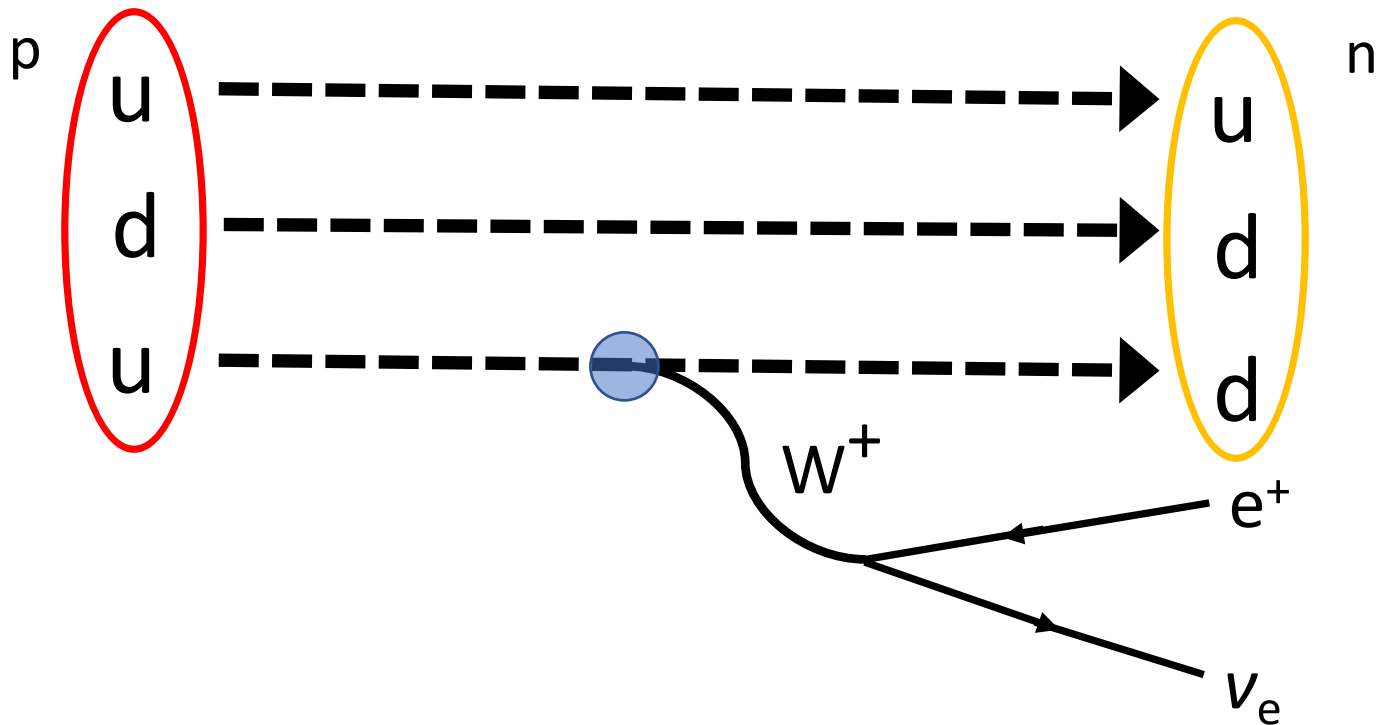
# High-Precision Measurement of the Superallowed Fermi Beta Decay of $^{62}\text{Ga}$

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Andrew MacLean  
University of Guelph  
February 16, 2020

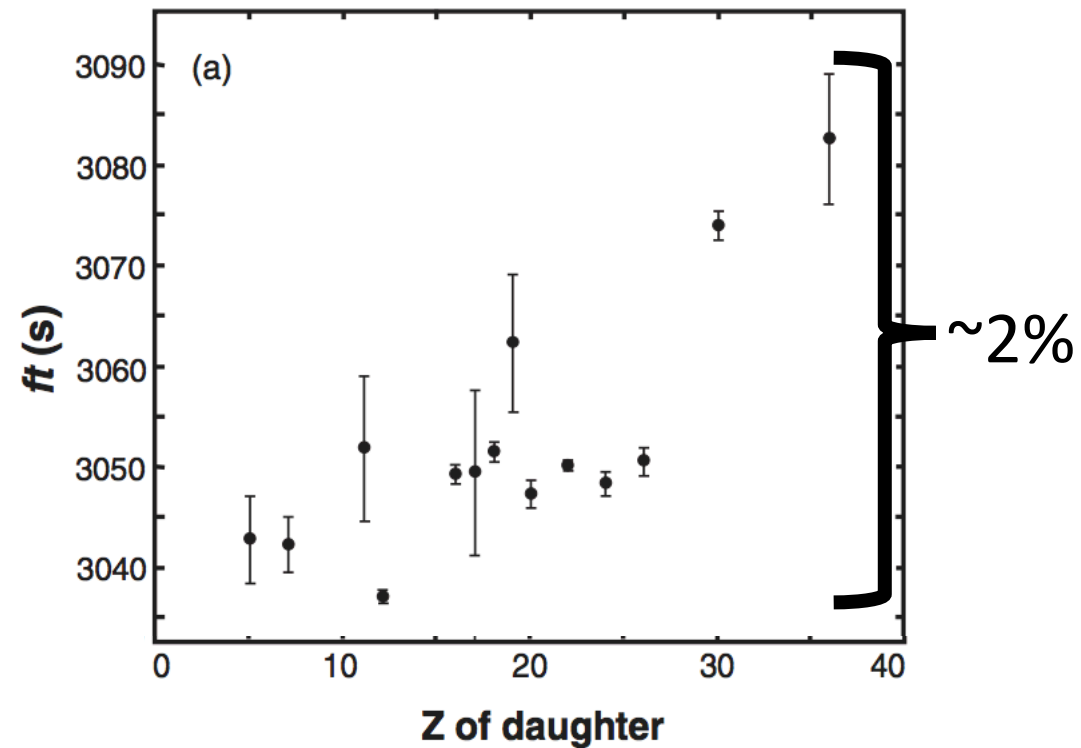
# Beta Decay and $ft$ Values



$$g |M_{fi}|^2 = G_V^2 |M_{fi}(F)|^2 + G_A^2 |M_{fi}(GT)|^2$$

$$ft = \frac{K}{g^2 |M_{fi}|^2}$$

In the special case of pure Fermi transitions between isobaric analogue states.



$$ft = \frac{K}{2G_V^2} = \text{constant}$$

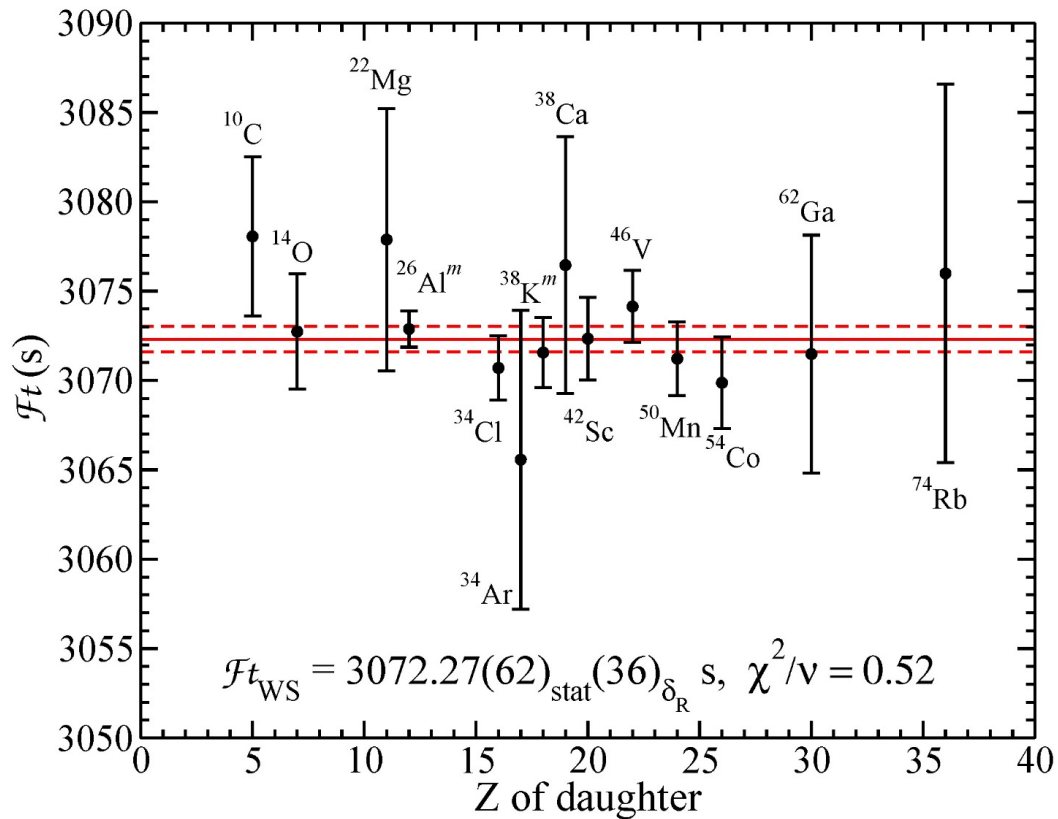
# Superallowed Fermi Beta Decay

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$

- $\delta'_R$  &  $\delta_{NS}$  transition-dependent radiative correction.
  - Dependent on hadronic structure, positron interacting with Coulomb field.
- $\Delta_R^V$  transition-independent radiative correction.
  - Universal and independent of nucleus involved, higher energy physics.
- $\delta_C$  isospin symmetry breaking correction.
  - Configuration mixing between  $0^+$  states and imperfect overlap of proton and neutron radial wavefunctions.

# Superallowed Fermi Beta Decay

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$



CKM Matrix

$$|V_{ud}| = \frac{G_V}{G_F} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

As of 2015, good agreement with unity.

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9994(5)$$

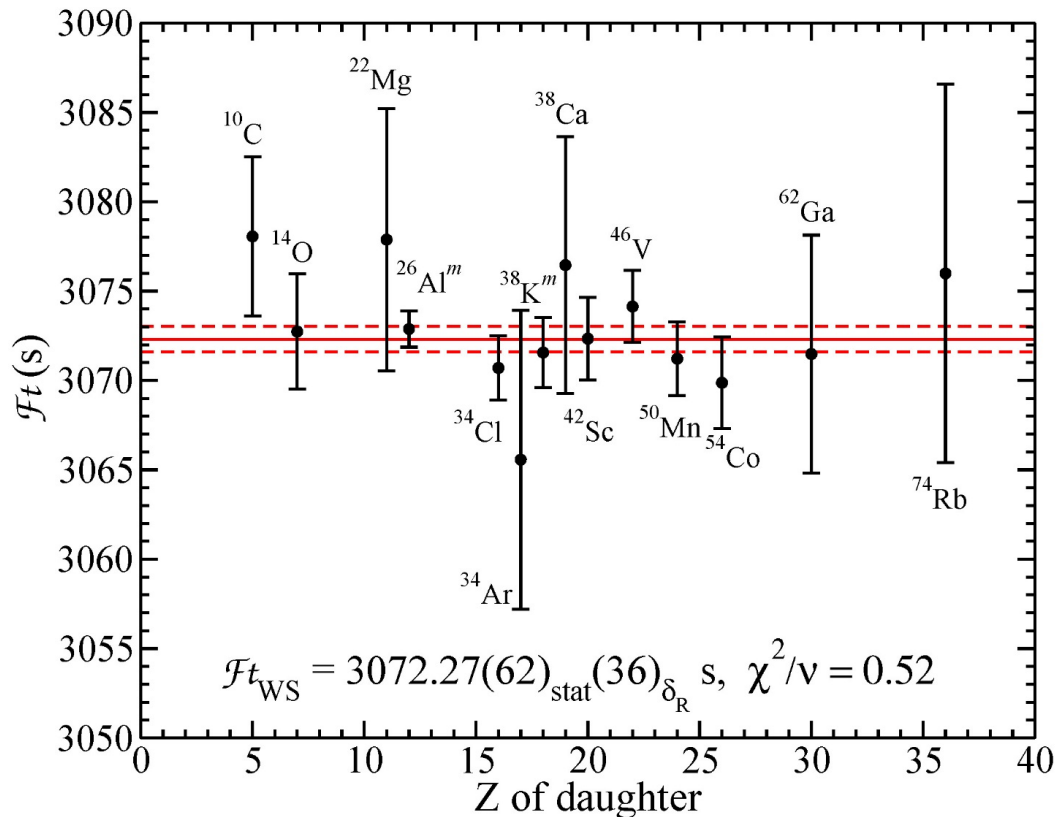


# Superallowed Fermi Beta Decay

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) =$$

$$\frac{K}{2G_V^2(1 + \Delta_R^V)}$$

NEW as of 2019



CKM Matrix

$$|V_{ud}| = \frac{G_V}{G_F} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

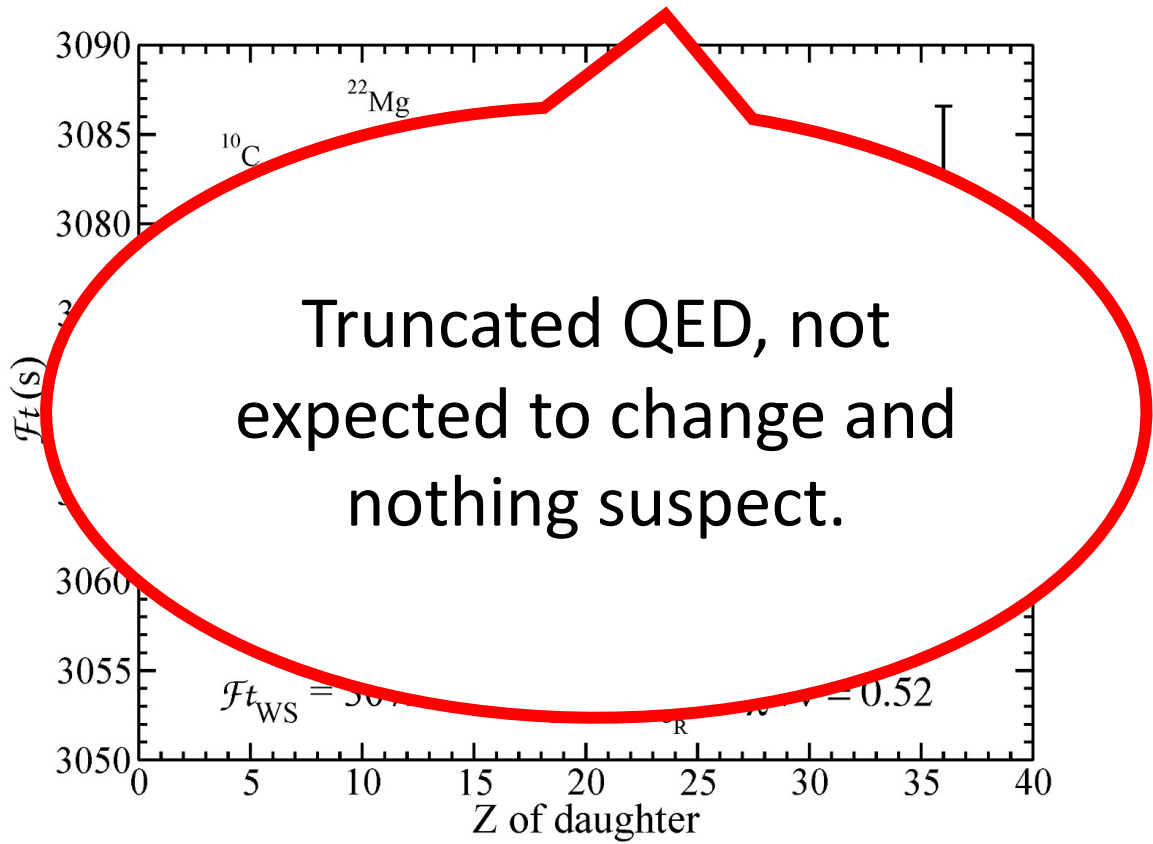
As of 2019, poor agreement with unity.

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9984(4)$$



# Superallowed Fermi Beta Decay

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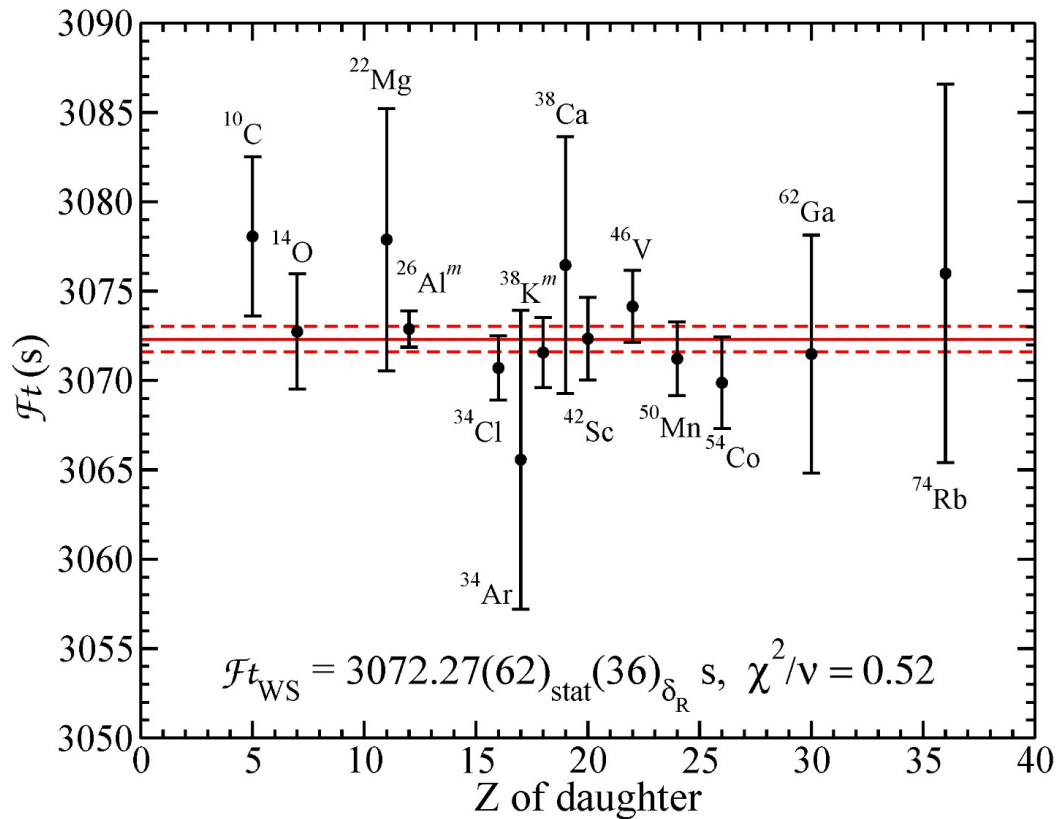
As of 2019, poor agreement with unity.

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9984(4)$$



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$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$



Involves detailed nuclear structure and can be difficult to calculate.

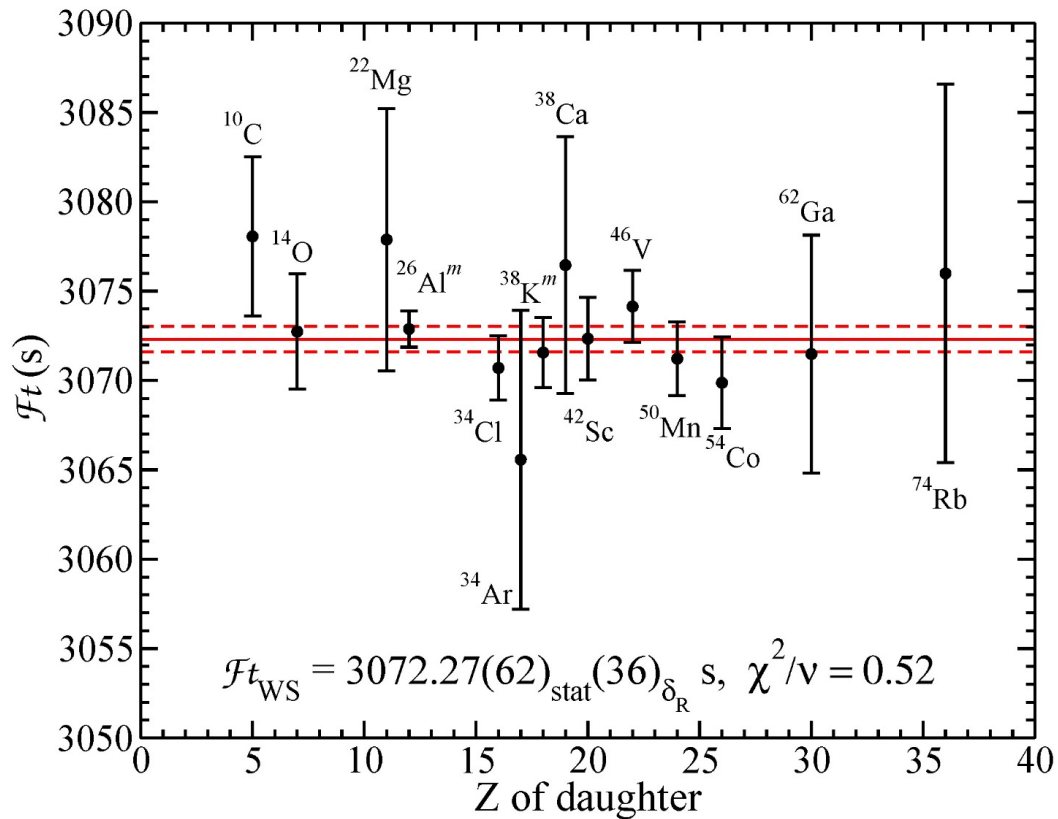
matrix  
 $\left. \begin{matrix} ub \\ cb \\ V_{tb} \end{matrix} \right\}$

As of 2019, poor agreement with unity.

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9984(4)$$

# Superallowed Fermi Beta Decay

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$



Involves detailed nuclear structure and can be difficult to calculate.

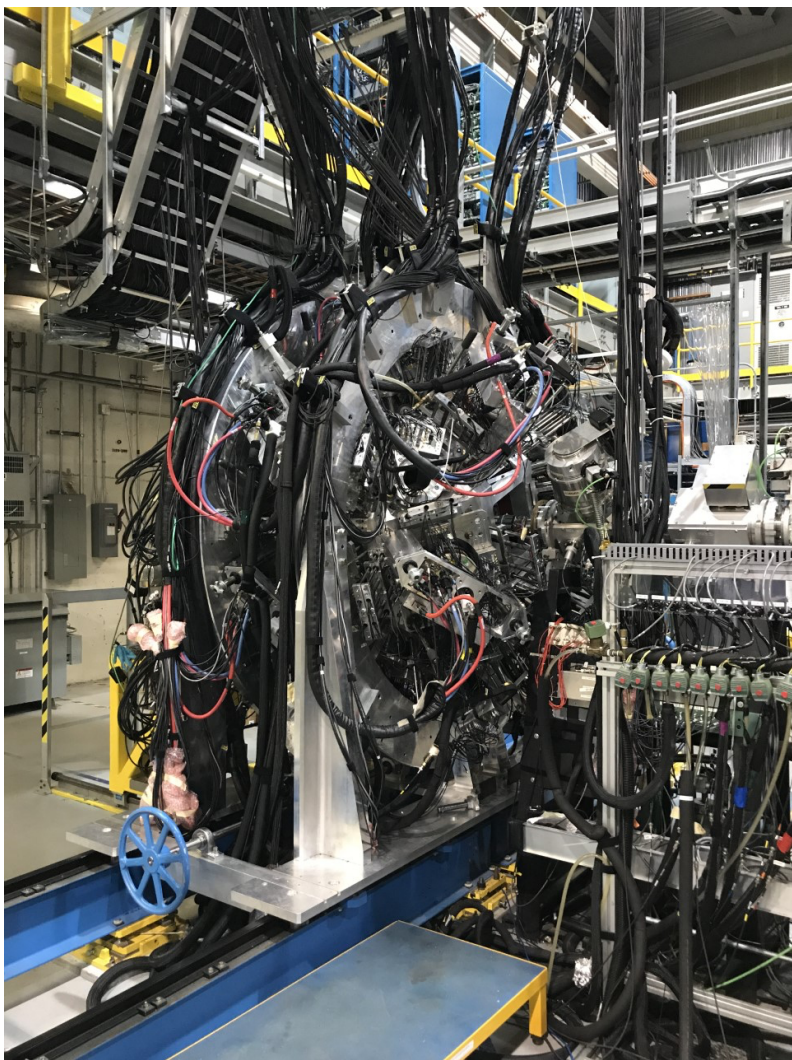
matrix  
 $\left. \begin{matrix} ub \\ cb \\ V_{tb} \end{matrix} \right\}$

As of 2019, poor agreement with unity.

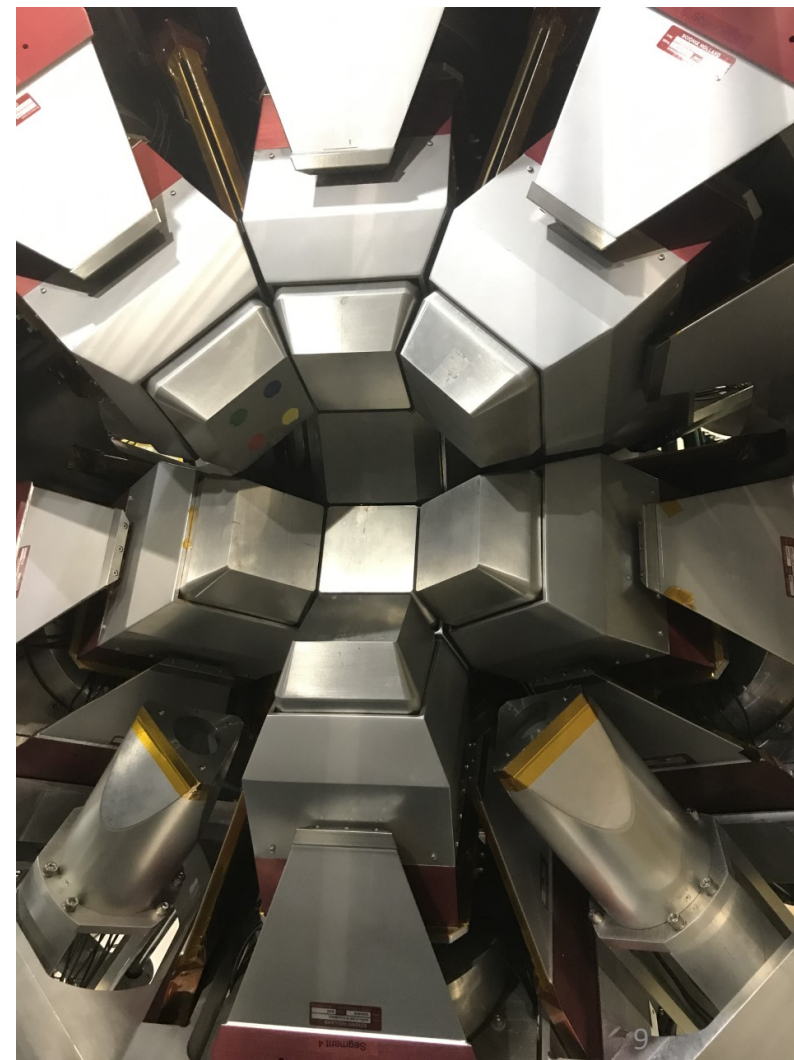
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9984(4)$$



# GRIFFIN



- High efficiency gamma-ray spectrometer.
- 16 large volume HPGe clover type detectors.
- Large assortment of ancillary detectors.
- For this work SCEPTAR was used to detect beta particles.

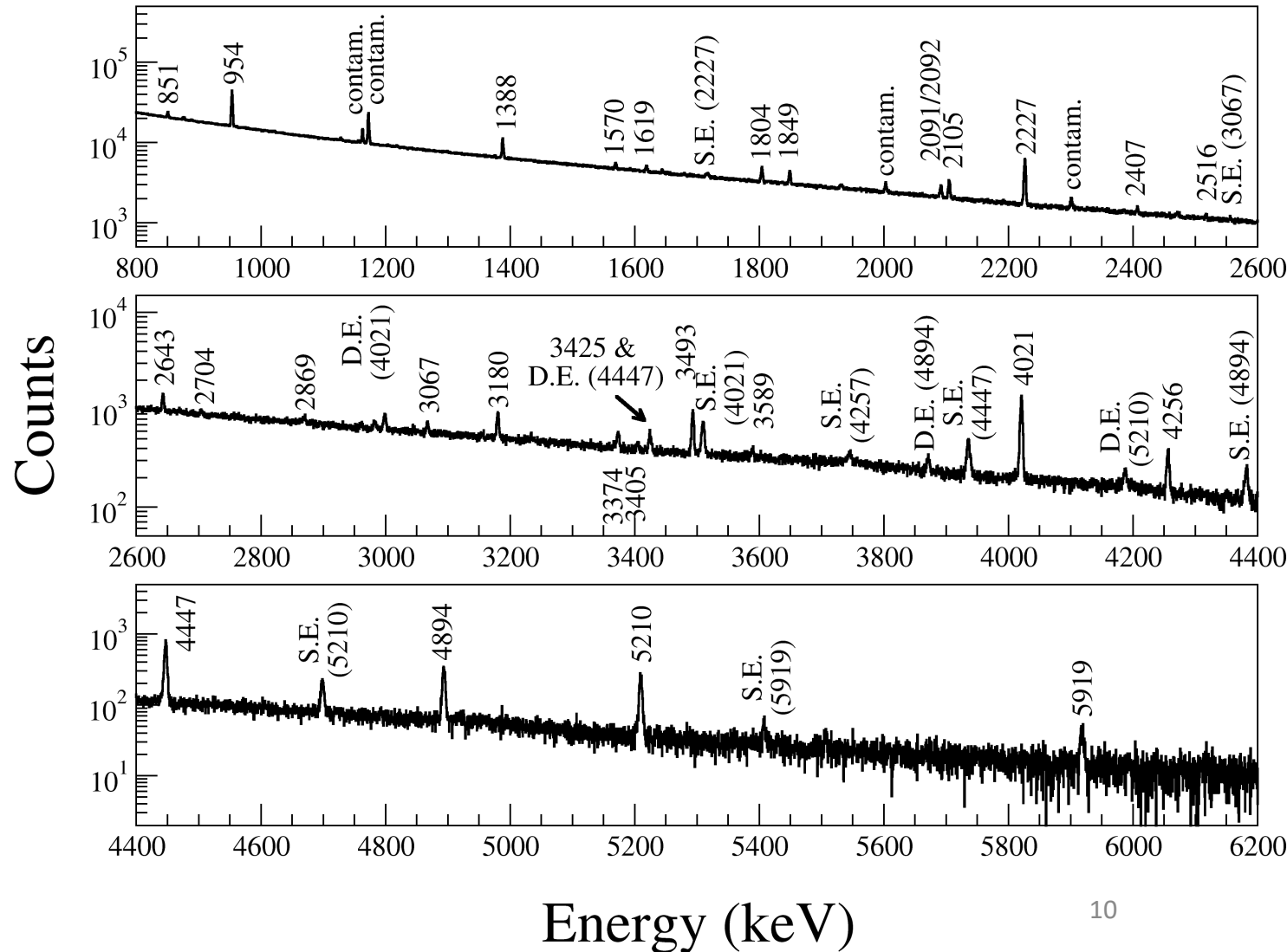


# $^{62}\text{Ga}$ Experiment

Singles spectra from the GRIFFIN spectrometer after 6 days of collecting data at  $\sim 8000$  ions/s.

Able to vastly expand knowledge on the structure of the daughter,  $^{62}\text{Zn}$ .

With available statistics, performed  $\gamma$ - $\gamma$  angular correlations.

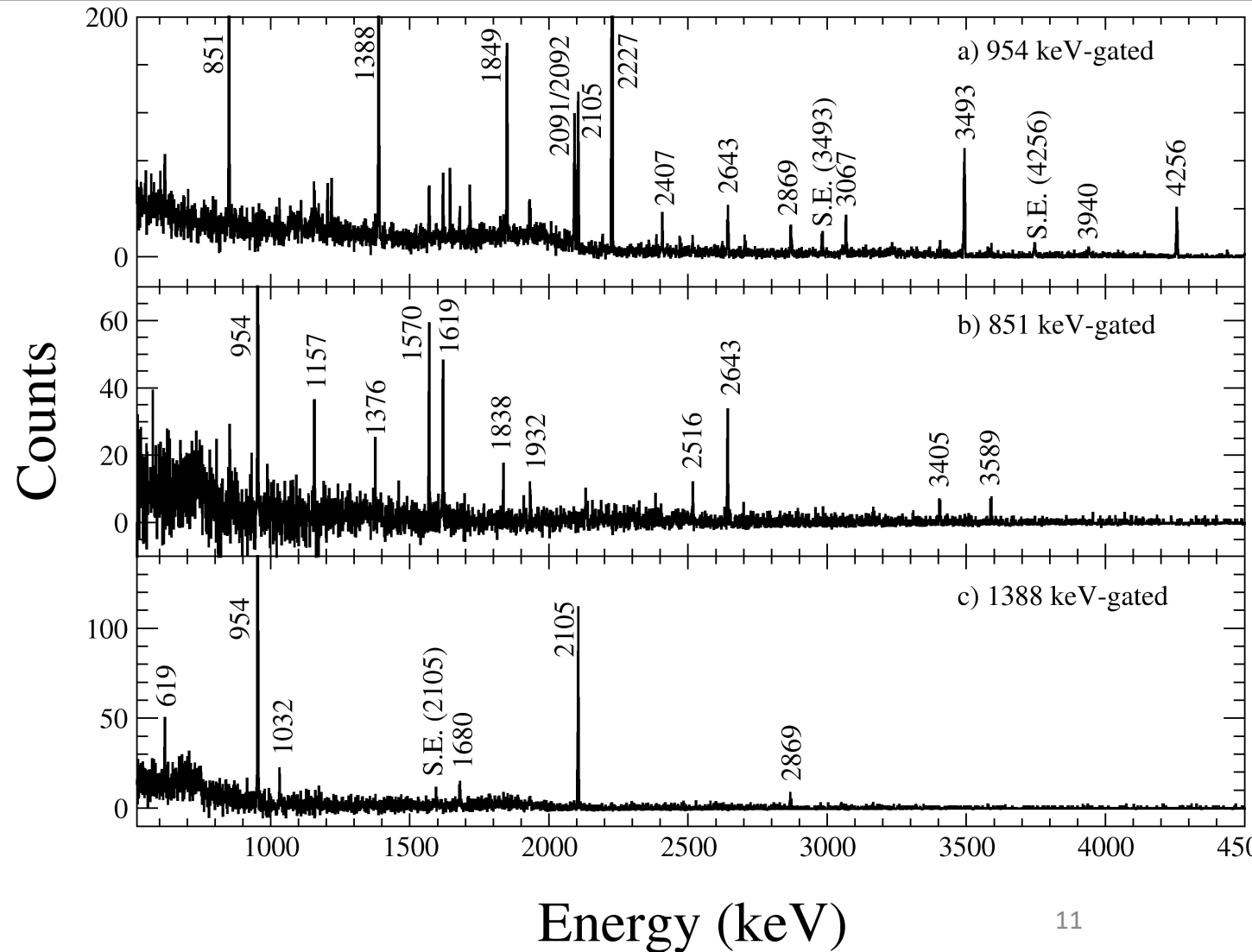


# $^{62}\text{Ga}$ Experiment

Excellent statistics to perform coincidence analysis.

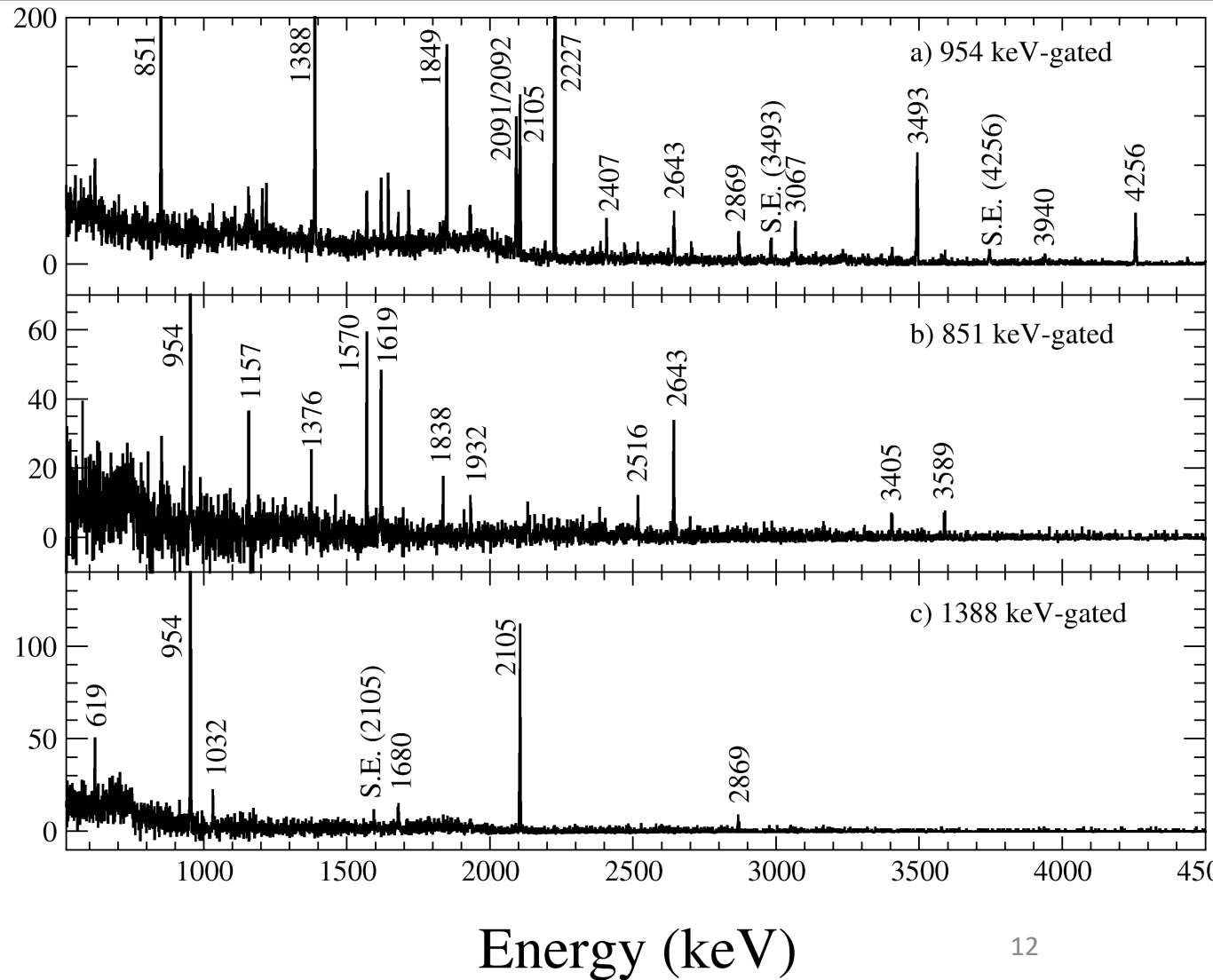
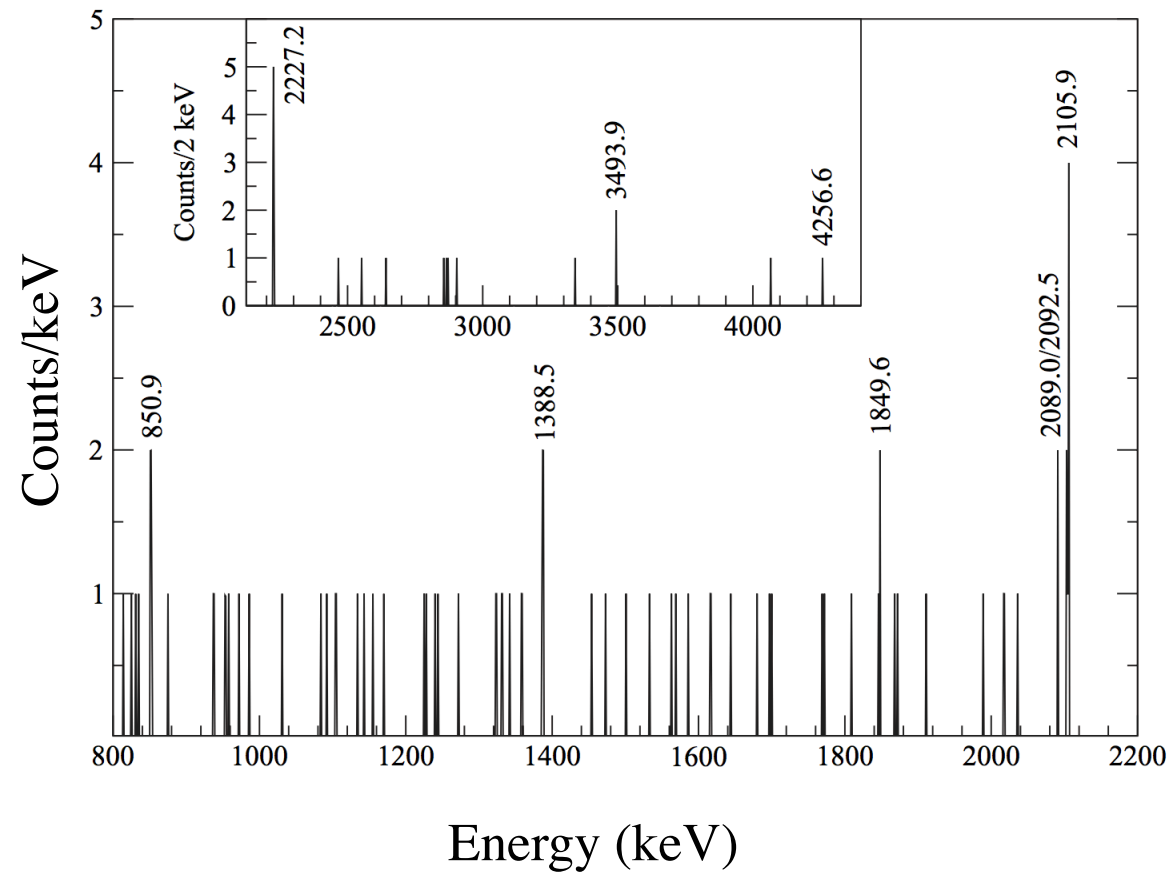
High confidence in placement of transitions in level scheme.

Allowed several doublets to be properly identified and given proper intensities.



# $^{62}\text{Ga}$ Experiment

Previous measurement



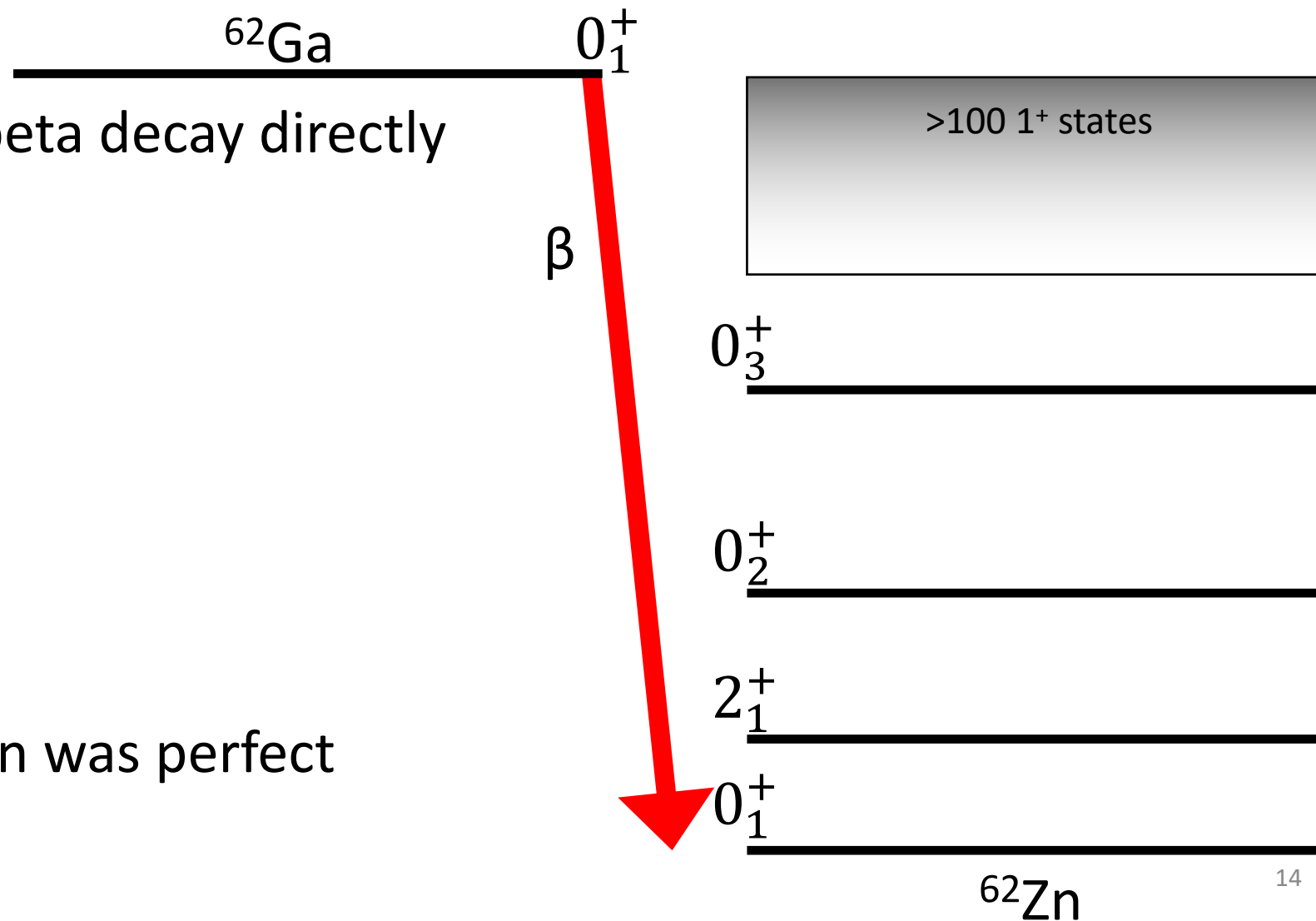




# Superaligned Branching Ratio

How frequently do you beta decay directly to the ground state?

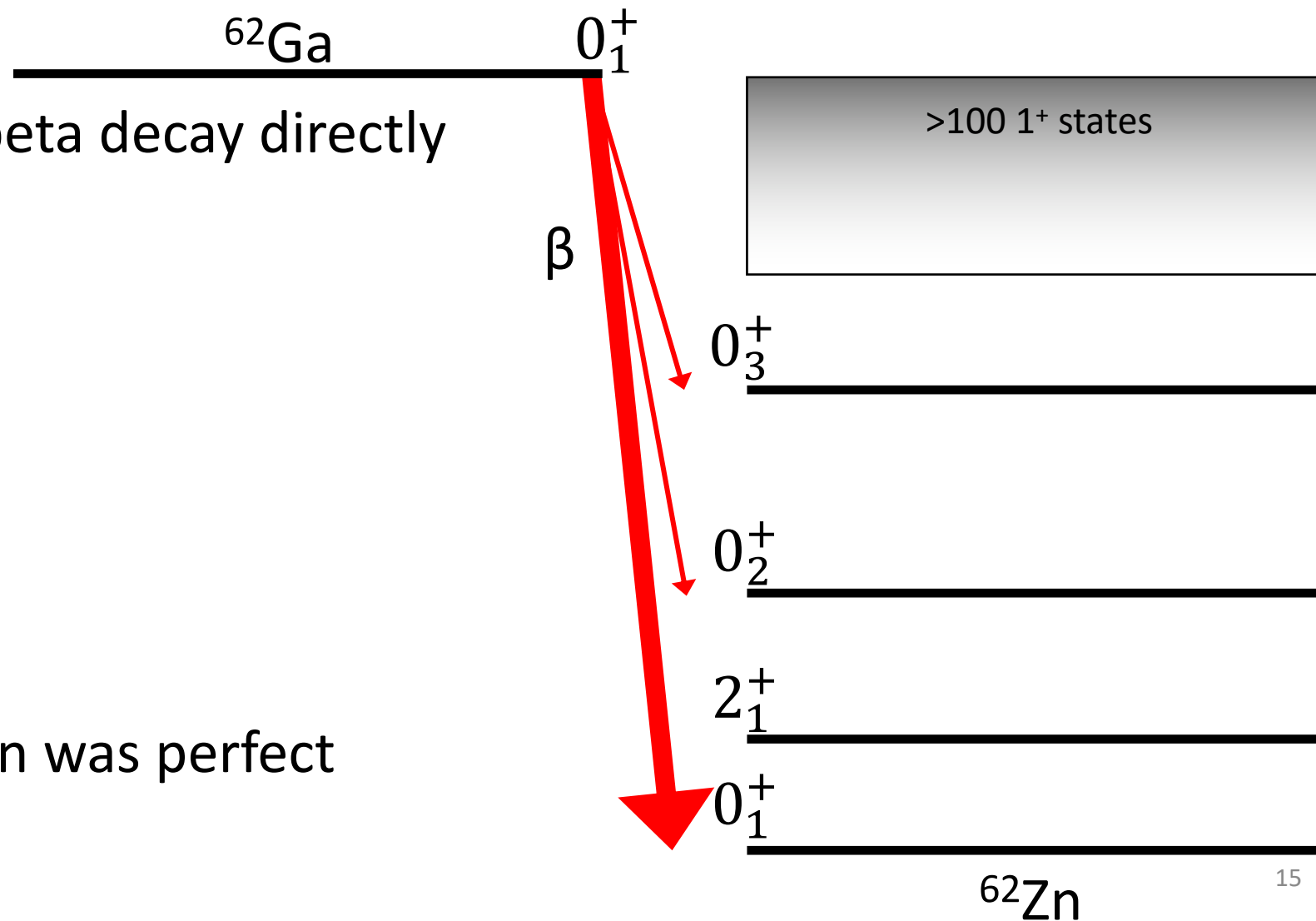
Would be 100% if isospin was perfect symmetry.



# Superaligned Branching Ratio

How frequently do you beta decay directly to the ground state?

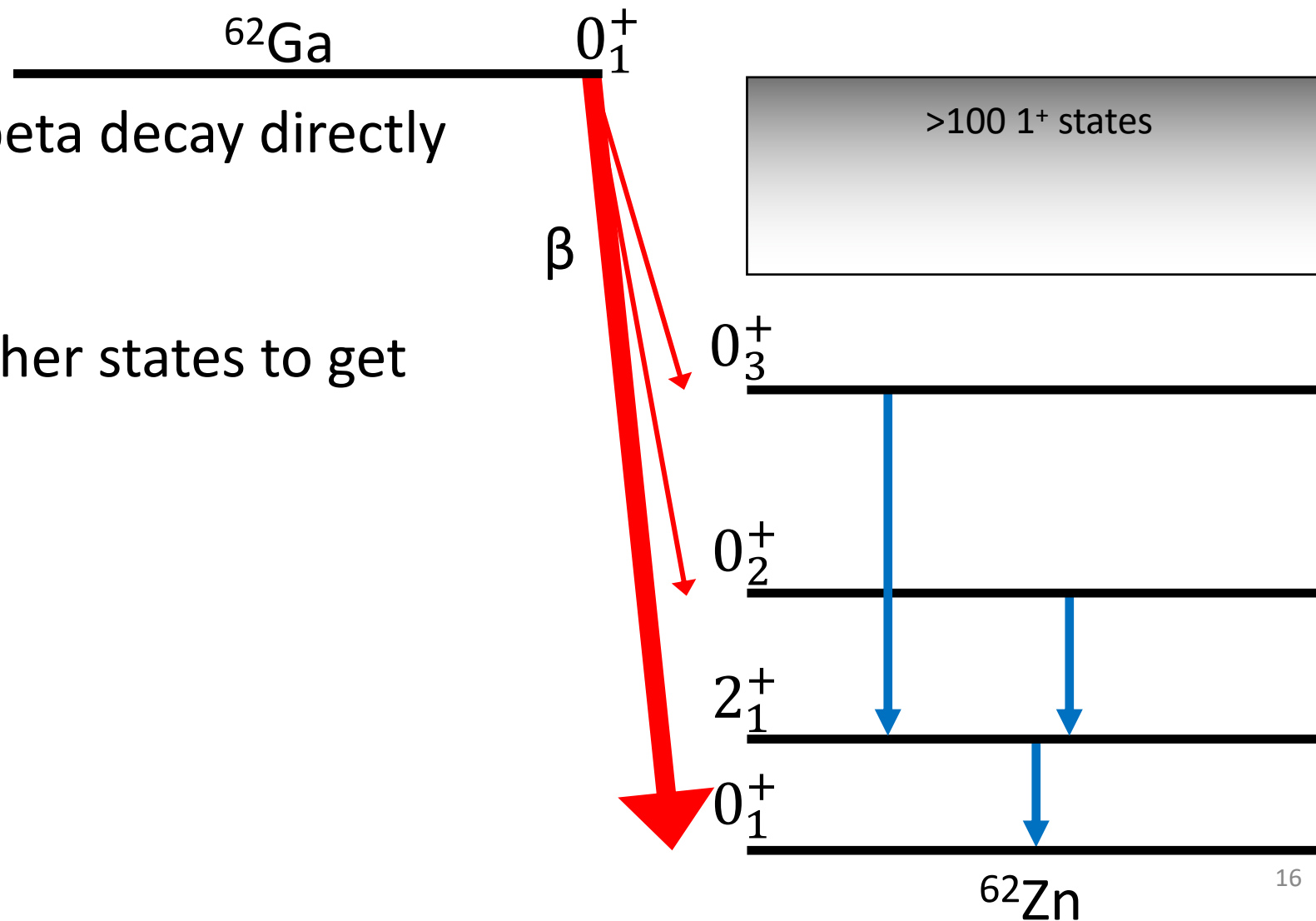
Would be 100% if isospin was perfect symmetry **but it's not.**



# Superaligned Branching Ratio

How frequently do you beta decay directly to the ground state?

Use gamma-rays from other states to get the beta feeding.

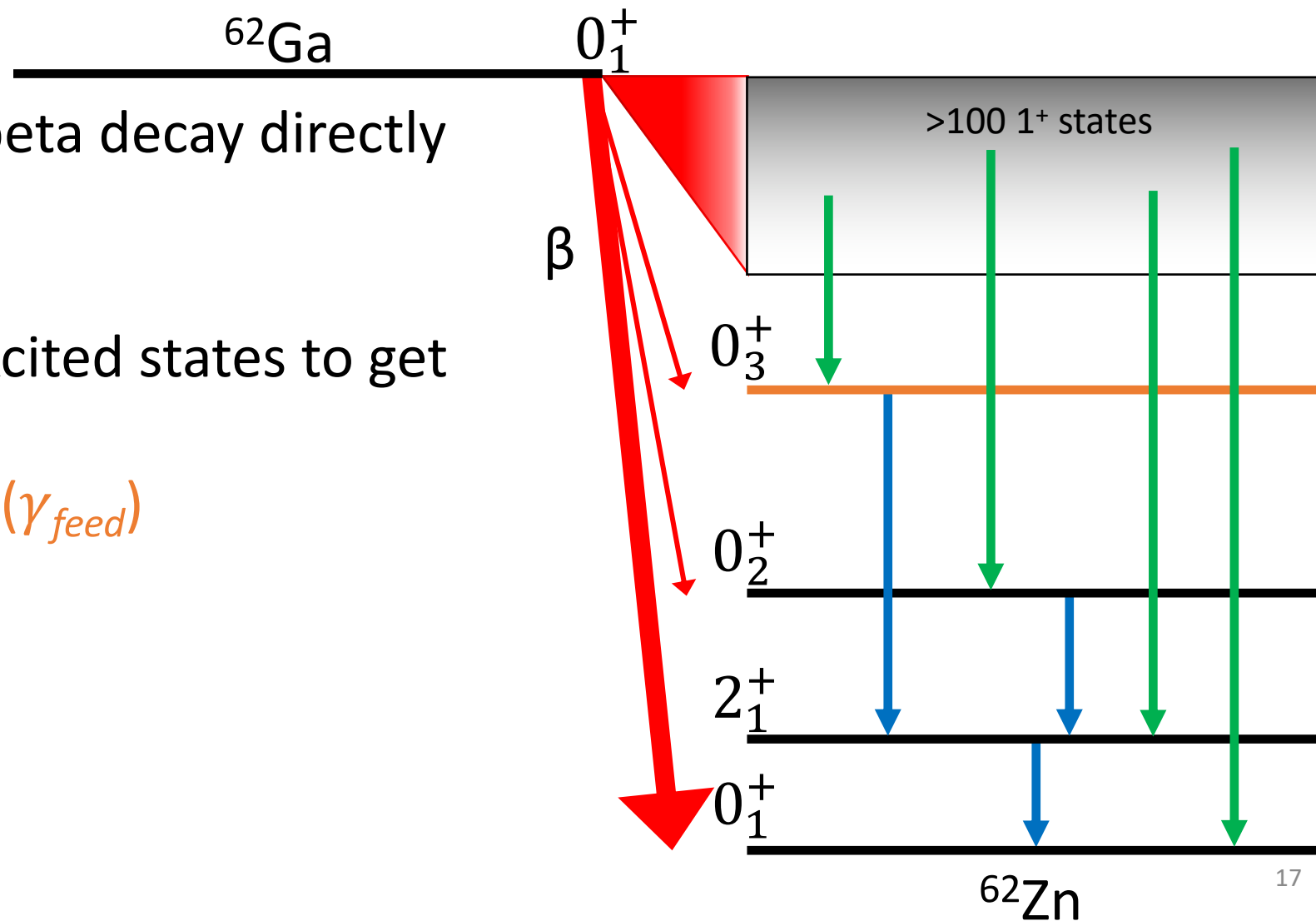


# Superaligned Branching Ratio

How frequently do you beta decay directly to the ground state?

Use gamma-rays from excited states to get the beta feeding.

- $I(\beta_{feed}) = I(\gamma_{drain}) - I(\gamma_{feed})$



# Superaligned Branching Ratio

How frequently do you beta decay directly to the ground state?

Use gamma-rays from excited states to get the beta feeding.

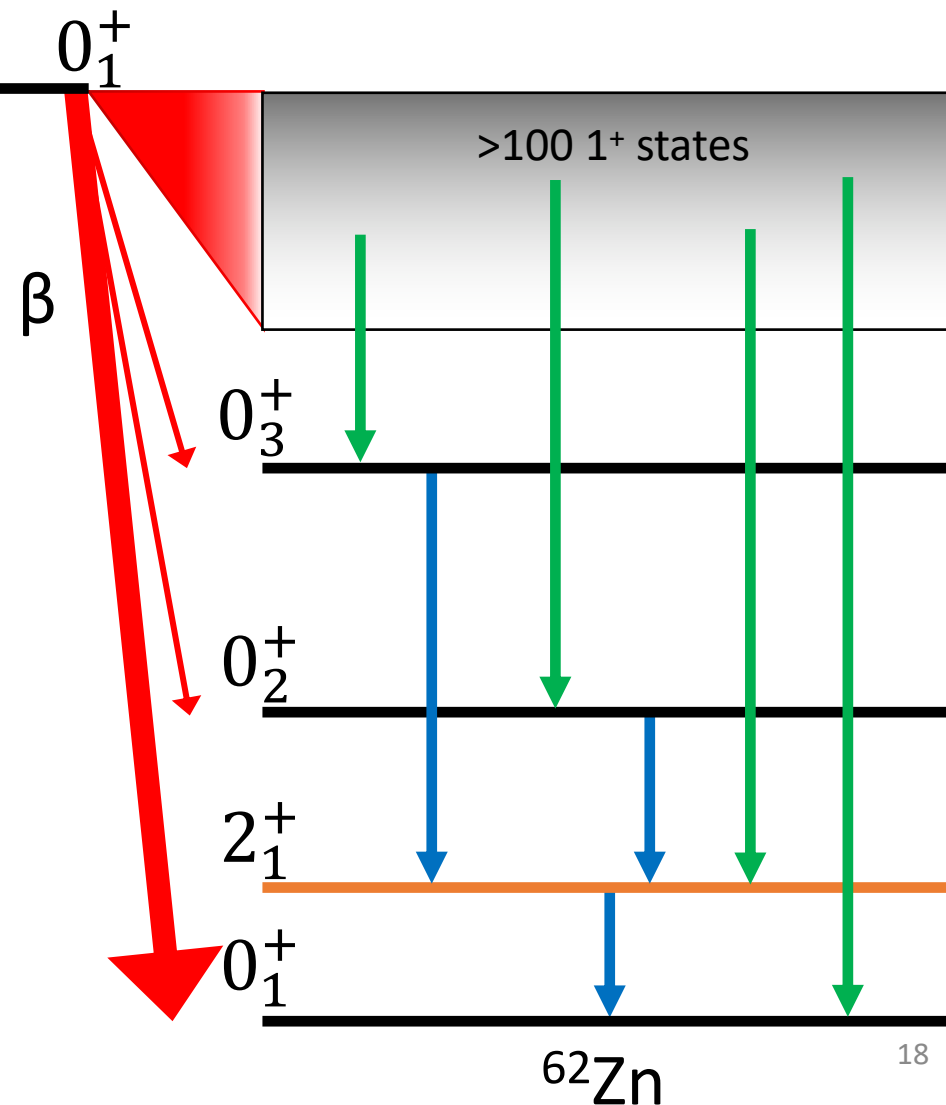
- $I(\beta_{feed}) = I(\gamma_{drain}) - I(\gamma_{feed})$

2+ levels should see no direct beta feeding.

- $I(\gamma_{feed}) = I(\gamma_{drain})$

The 954 keV level  $\gamma_{drain} - \gamma_{feed} = -7(10)$  ppm

Previous work was 122(27) ppm



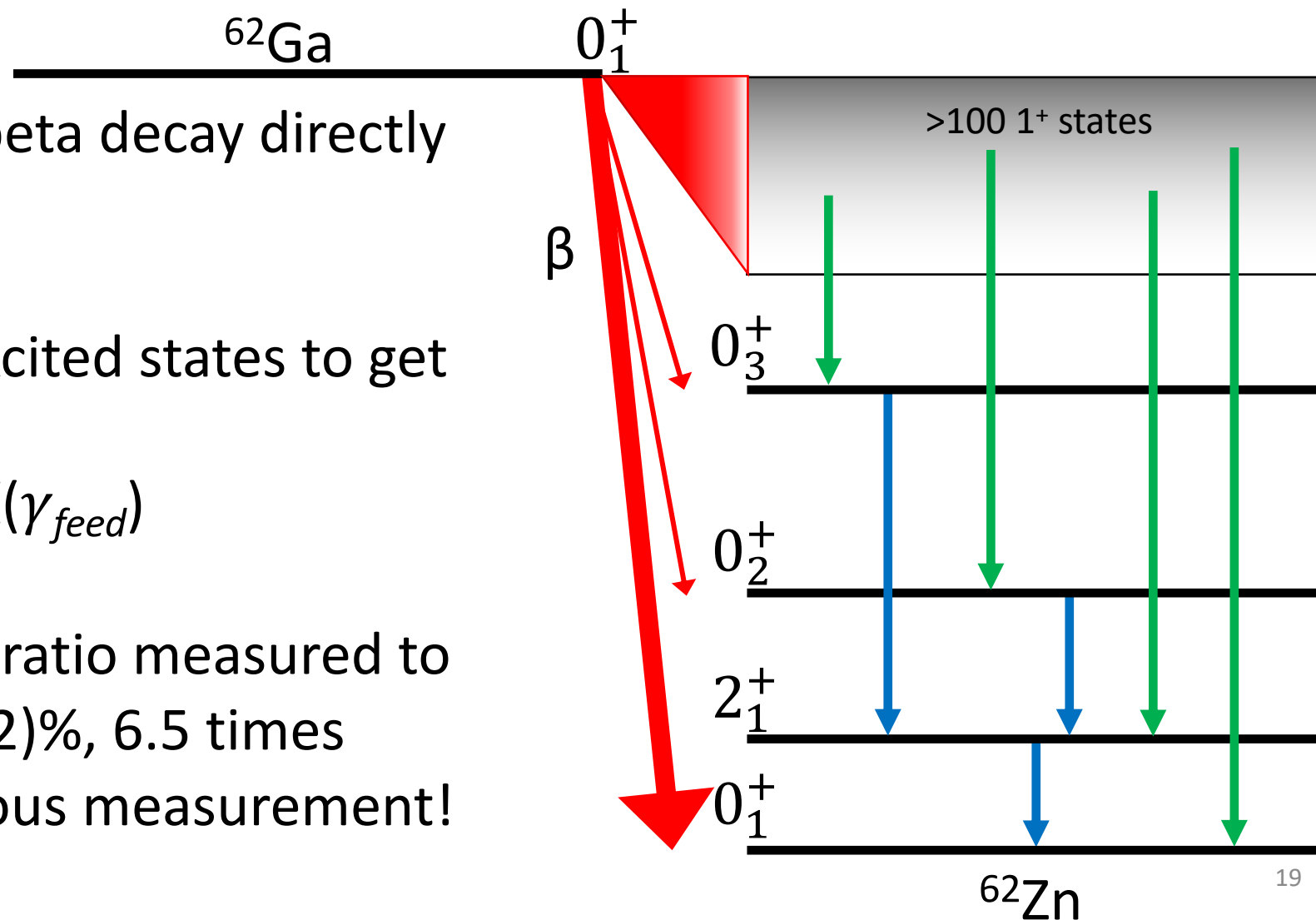
# Superaligned Branching Ratio

How frequently do you beta decay directly to the ground state?

Use gamma-rays from excited states to get the beta feeding.

- $I(\beta_{feed}) = I(\gamma_{drain}) - I(\gamma_{feed})$

Superaligned branching ratio measured to a precision of 99.8647(12)%, 6.5 times more precise than previous measurement!



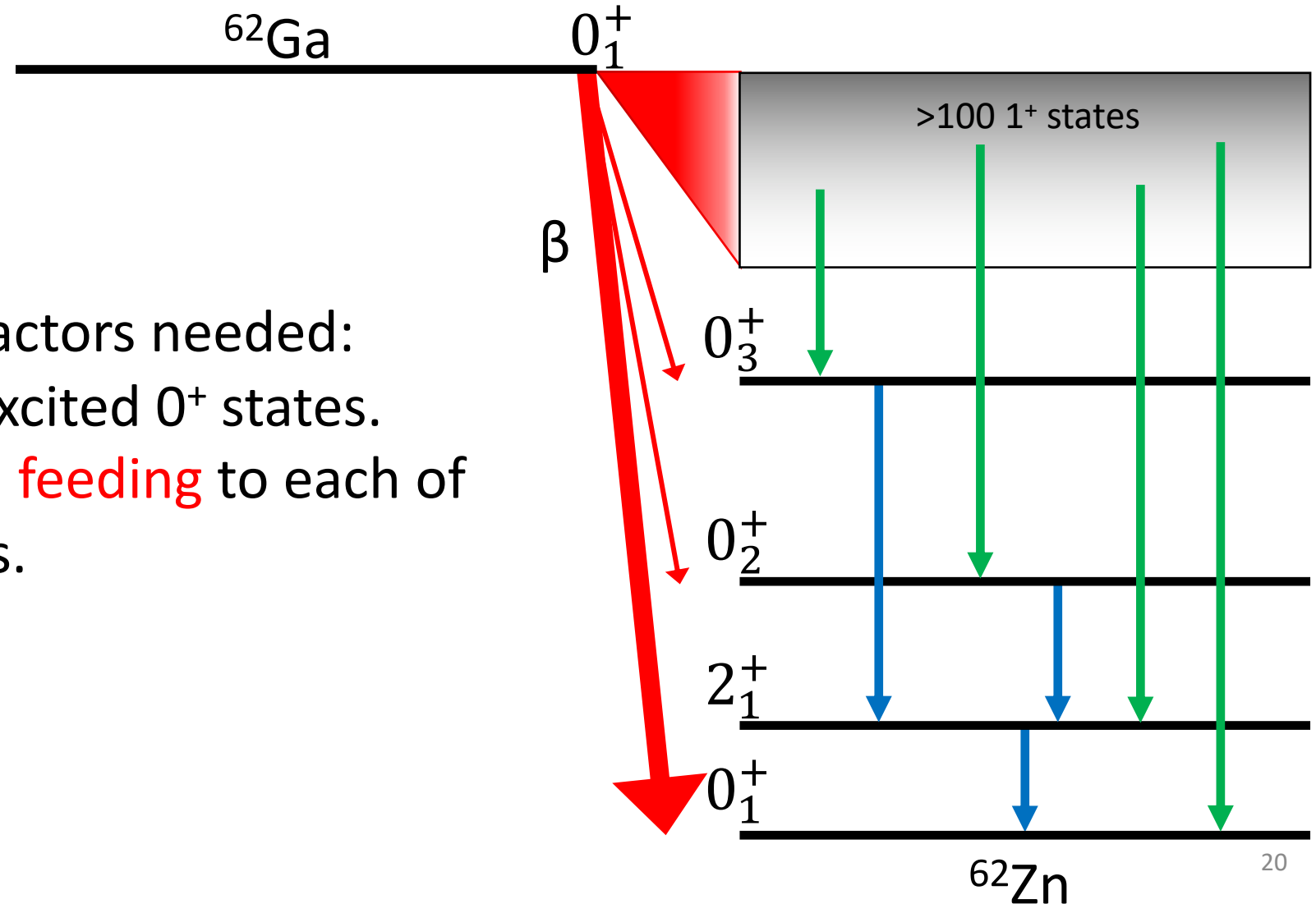
# How do we test $\delta_C$ ?

$$\delta_C = \delta_{C1} + \delta_{C2}$$

To determine  $\delta_{C1}$  two factors needed:

1. The energy of the excited  $0^+$  states.
2. The amount of **beta feeding** to each of the excited  $0^+$  states.

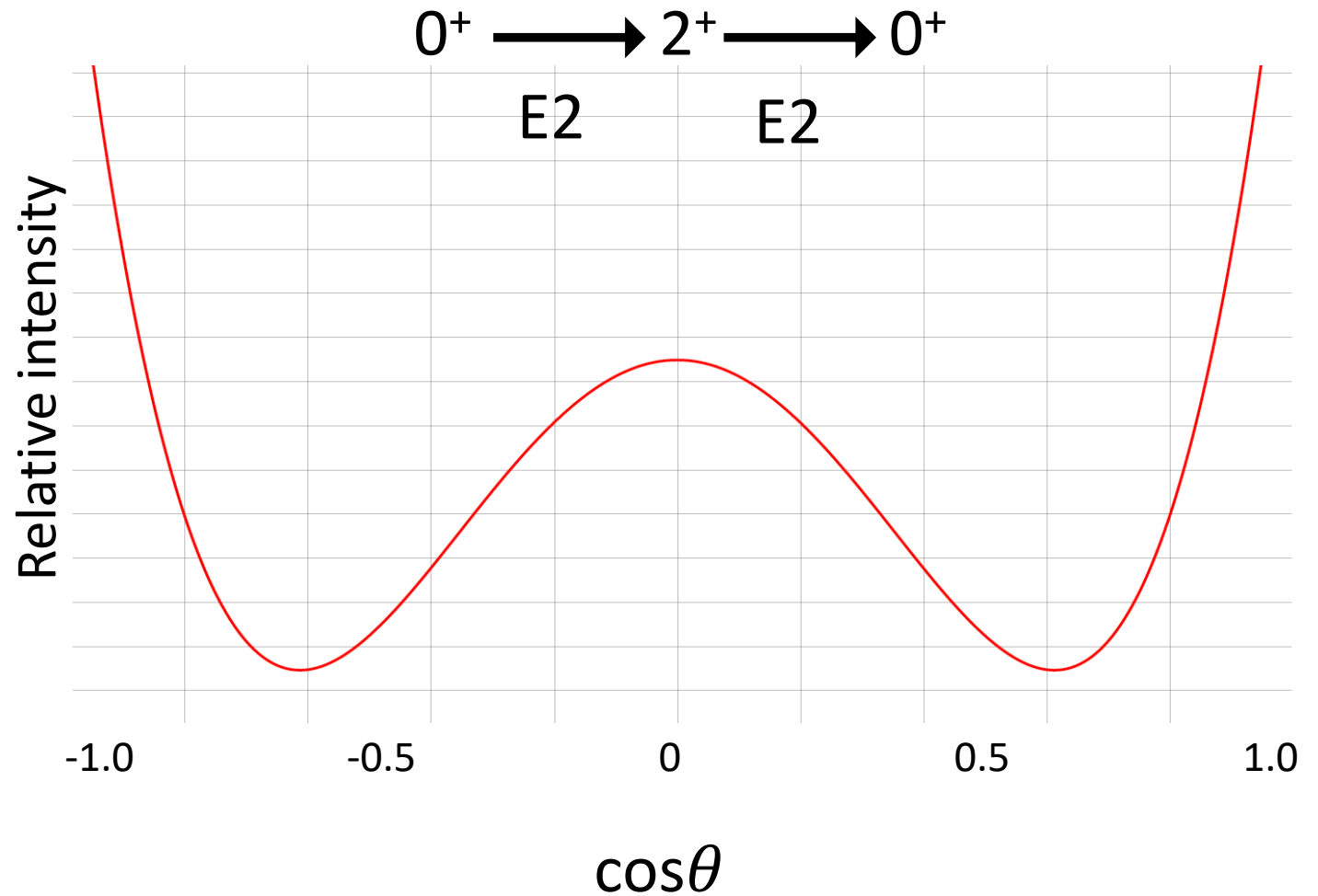
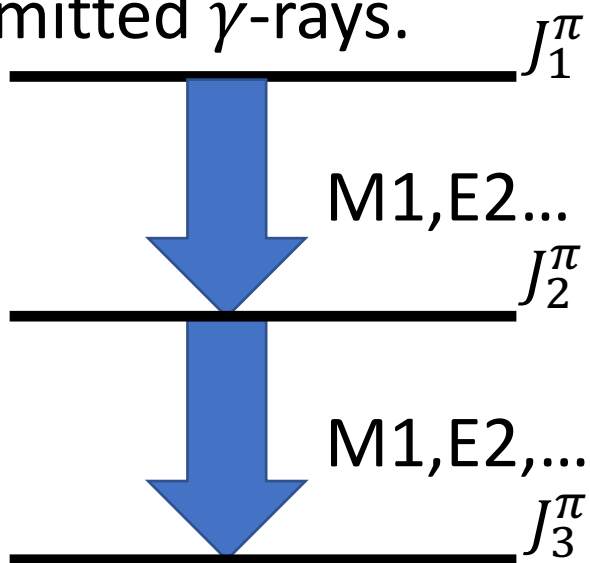
➤  $I(\gamma_{drain}) - I(\gamma_{feed})$ .





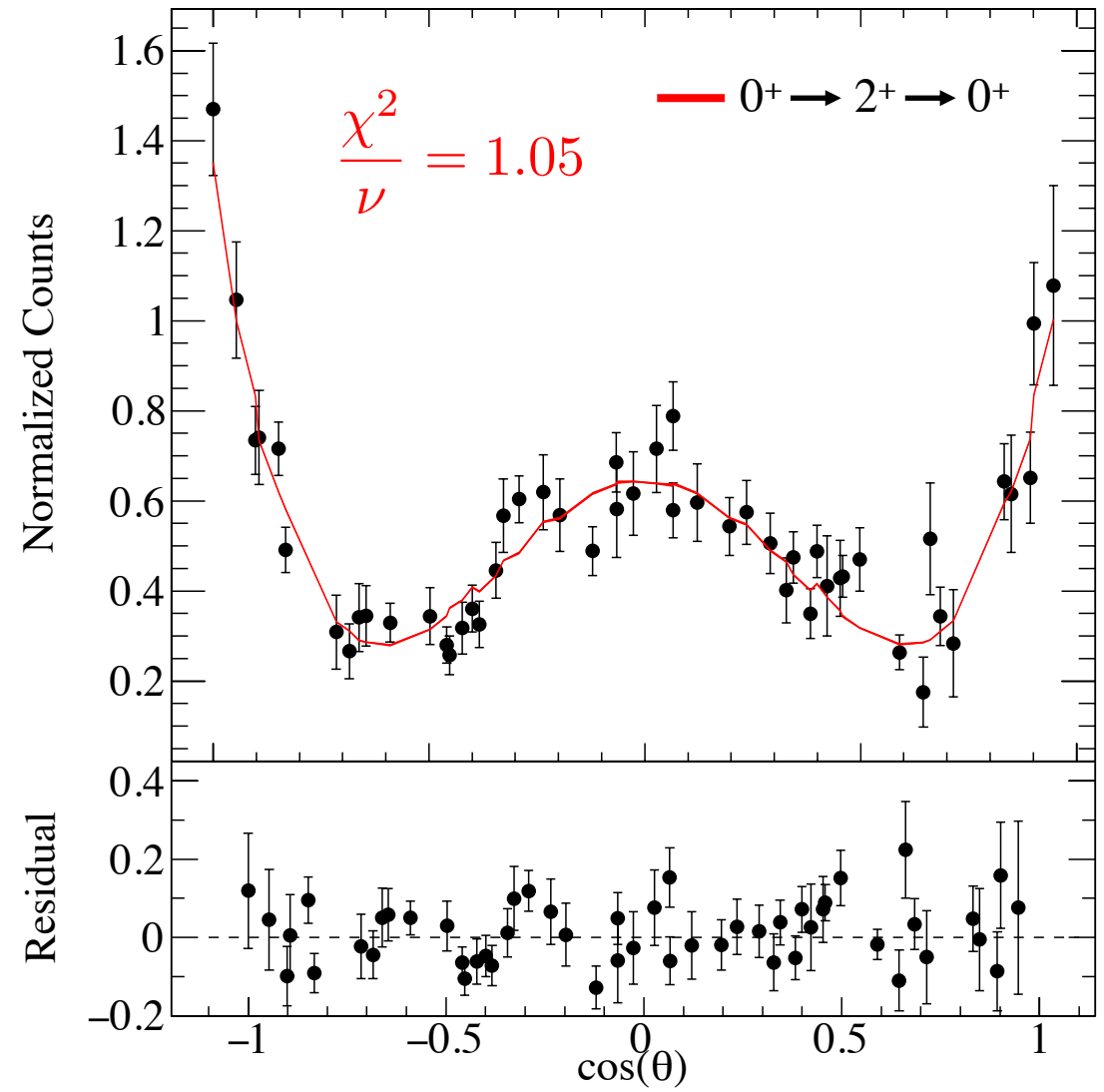
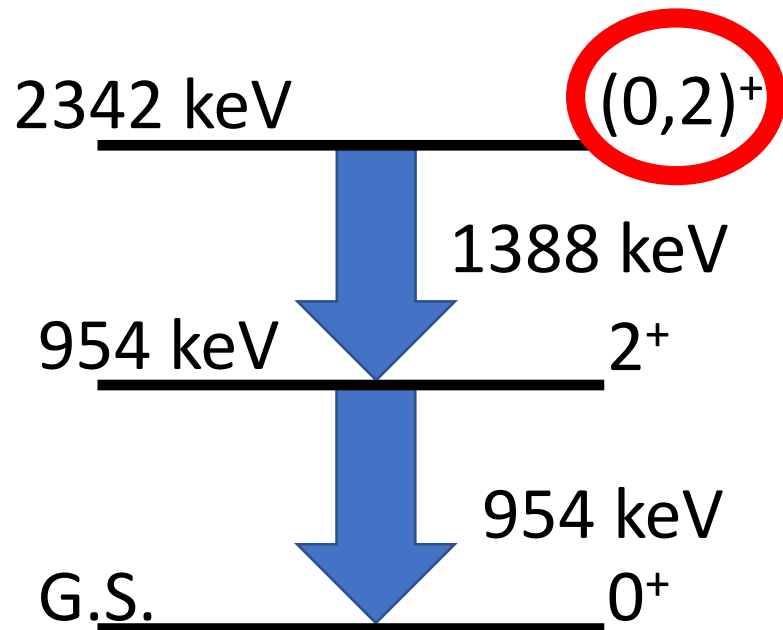
# Gamma-Gamma Angular Correlations

Coincident gamma-rays, in general, have a spatial correlation, dependent on the spins of the nuclear states and multipole character of the emitted  $\gamma$ -rays.



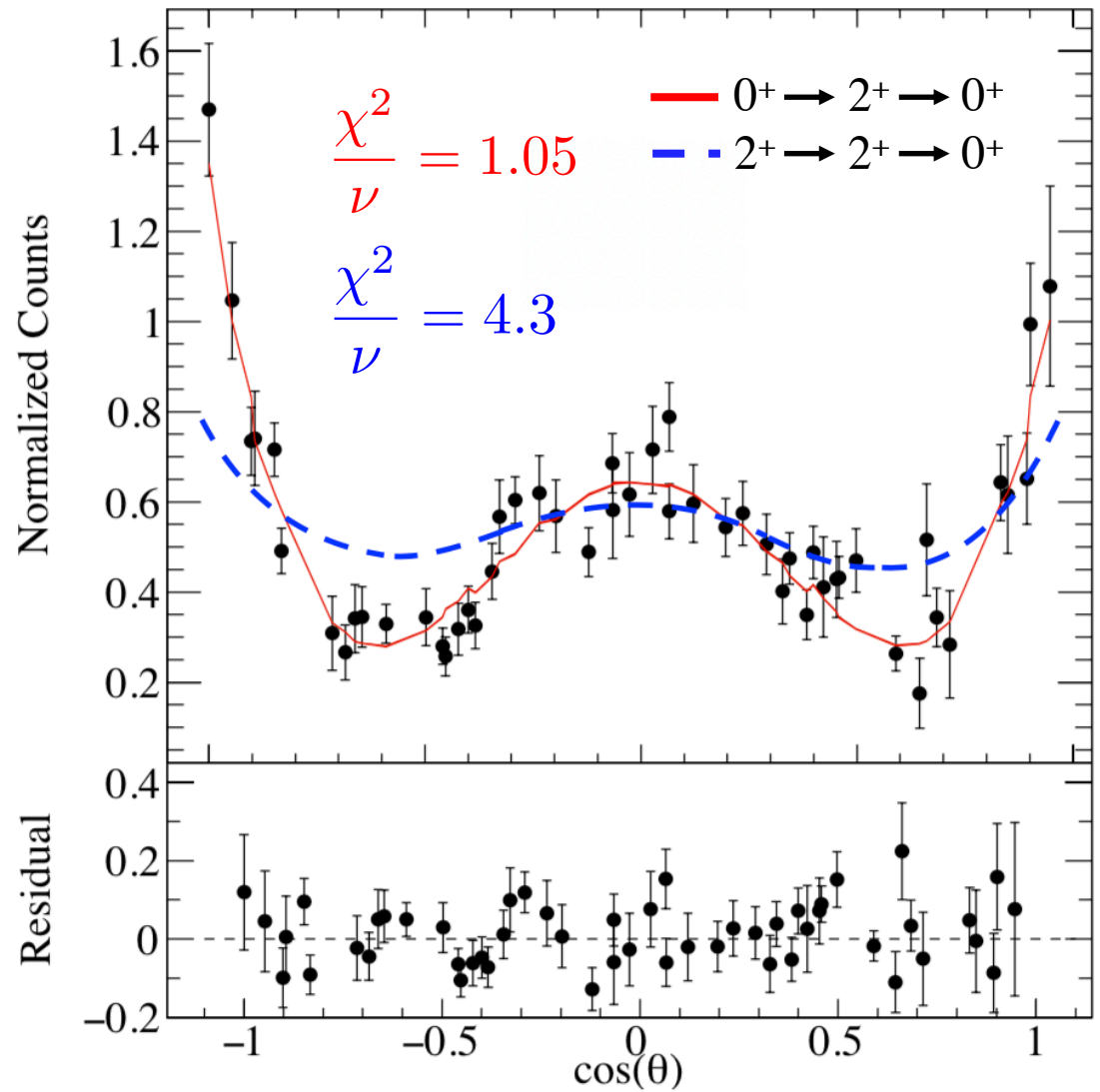
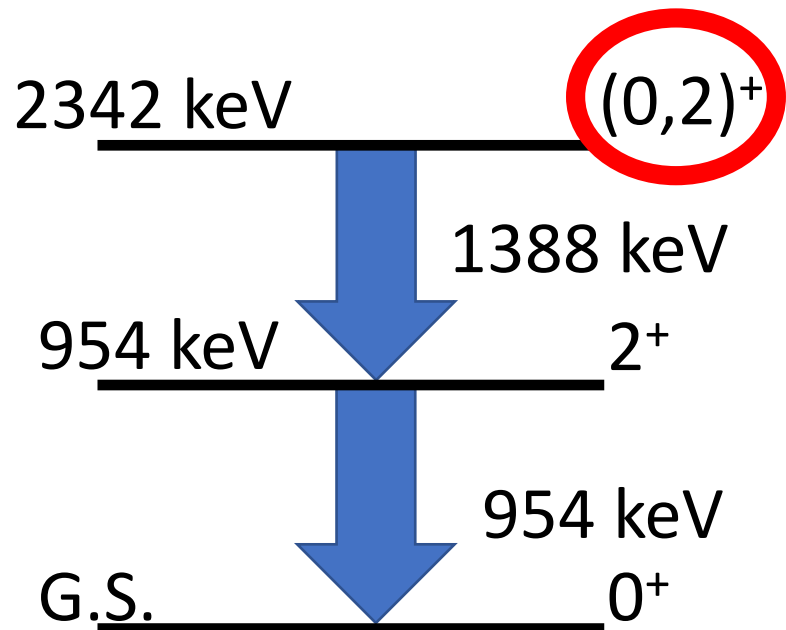
# Gamma-Gamma Angular Correlations

Angular correlation measurement of the 1388-954 keV cascade in daughter nucleus,  $^{62}\text{Zn}$ , compared to Geant4 simulation.



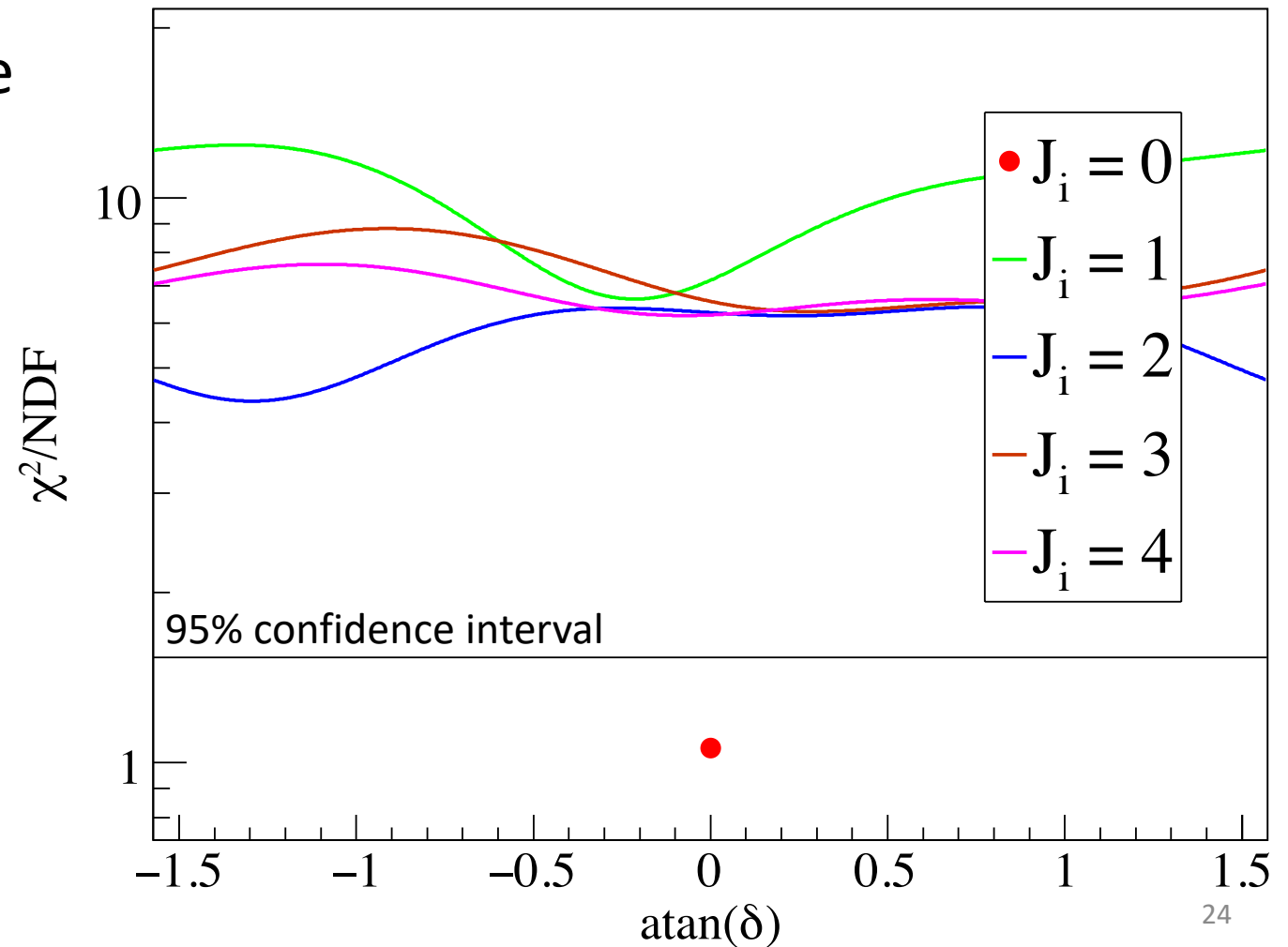
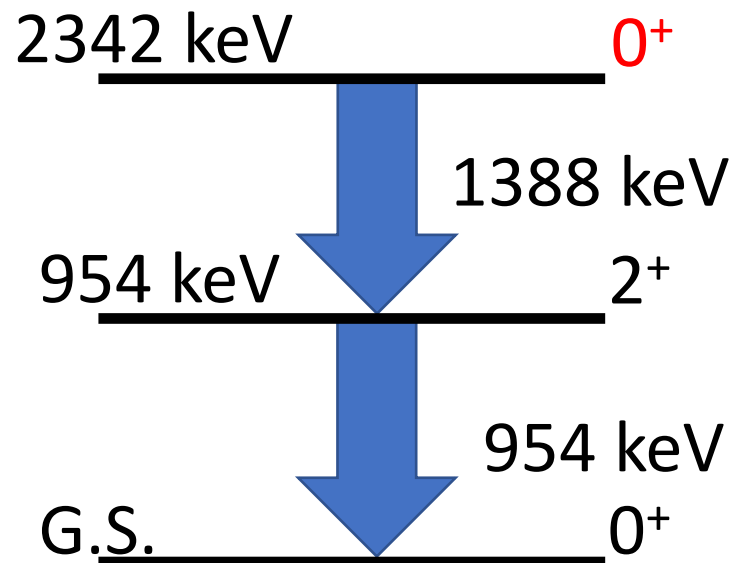
# Gamma-Gamma Angular Correlations

Angular correlation measurement of the 1388-954 keV cascade in daughter nucleus,  $^{62}\text{Zn}$ , compared to Geant4 simulation.



# Gamma-Gamma Angular Correlations

Allowing spin of 2342 keV state to vary can clearly identify the spin as an excited  $0^+$  state.



# Isospin Symmetry Break Correction

$E_{\text{level}}$ (keV)	$n$	$\delta_{C1_{exp}}^n$ (%)	$\delta_{C1_{theo}}^n$ (%)	Ratio (theo/exp)
2342	1	0.032(3)	0.083(20)	2.59(25)
3045	2	0.038(4)	0.203(20)	5.34(77)

- Over estimation from theory.
- Factor of 2.6 for the first excited  $0^+$  state and over a factor of 5 for the second excited  $0^+$  state.
- Third, fourth and fifth excited  $0^+$  states, only limits were set on the isospin symmetry breaking correction from this experiment.

Thank you!

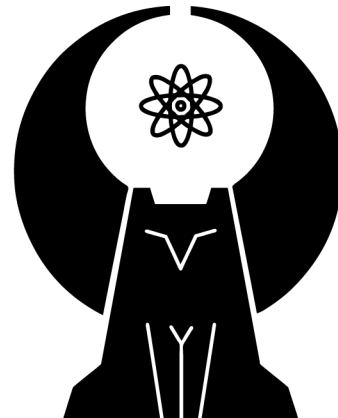


**TRIUMF**

Special thanks to the GRIFFIN collaboration, funding agencies and you for your time!



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Fondation canadienne pour l'innovation



**NSERC**  
**CRSNG**

# Thank you!

**UNIVERSITY**  
*of* **GUELPH**

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A. I. Kilic  
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I. Dillmann  
A. B. Garnsworthy  
G. Hackman  
H. P. Patel  
B. Olaizola  
Y. Saito  
J. Smallcombe



**SIMON FRASER**  
**UNIVERSITY**

C. Andreiou  
K. Whitmore



J. K. Smith



# Back-up Slides





# Summary

- New calculations of  $\Delta_R^V$  has changed  $V_{ud}$ , creating a significant disparity from unitarity in the top row of the CKM matrix.
- Leads to three possible explanations,
  1. The top row of the CKM matrix may need to be revisited.
  2. There may physics beyond the standard model.
  3. The theoretical corrections used to determine the  $\mathcal{F}t$ -values may need a larger model space.
- Experimentally we can measure the configuration mixing between  $0^+$  states, allowing for limits to be set on  $\delta_{C1}$ .
- From observations in experiment, the mixing predicted by theory is significantly over estimated.

# Implications of Recent Calculations

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$

Recent calculations have reduced the uncertainty on  $\Delta_R^V$  and additionally changed its central value.

Producing disagreement with unity in the CKM matrix.

$$\Delta_{Rnew}^V = 2.467(22)\%$$

$$|V_{ud}|_{new} = 0.97370(21)_{\mathcal{F}t}(10)_{RC}$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9984(4) \sim 4\sigma \text{ disagreement from unity!!}$$

**Uncertainty dominated by  $\mathcal{F}t$ .**

# Implications of Recent Calculations

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$

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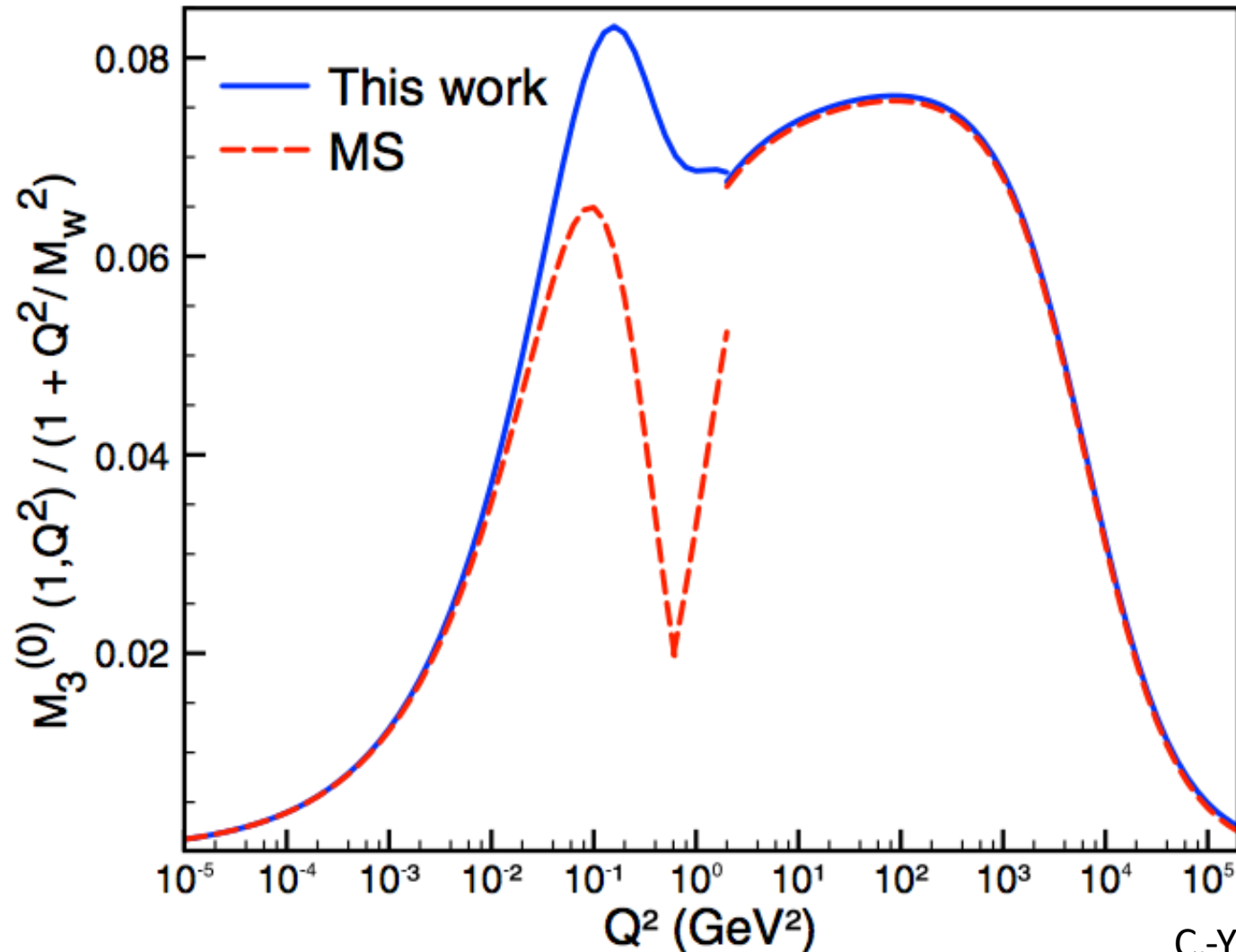
$$\Delta_{Rold}^V = 2.361(38)\%$$

$$|V_{ud}|_{old} = 0.97420(10)_{\mathcal{F}t}(18)_{RC}$$

**Good agreement from unity**

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9994(5)$$

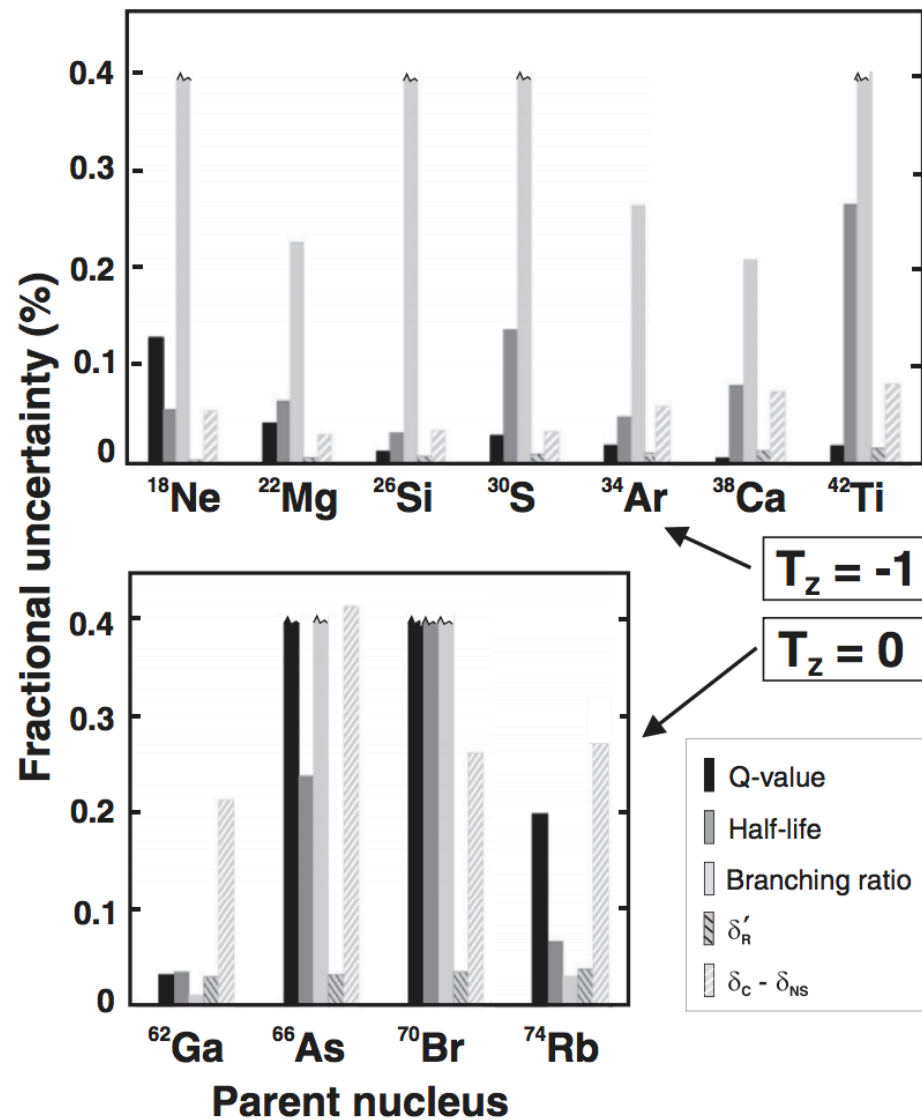
# New $\Delta_R^V$ Calculation



Integrate this to get new value, red is old function blue is new function.

1. Assume no physics other than Born at low  $Q$ .
2. Require function to vanish as  $Q^2$  approaches 0.
3. Integral must match pQCD not the function itself.

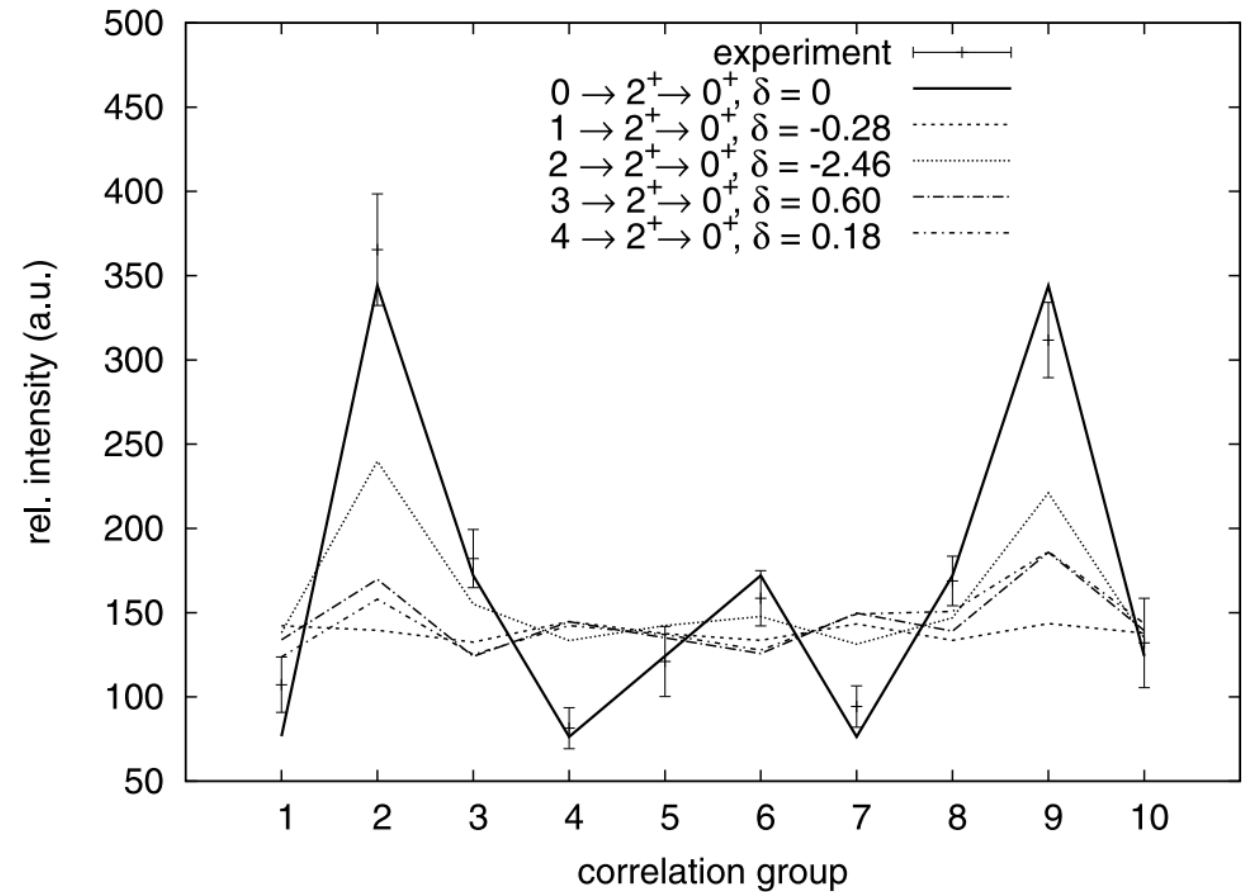
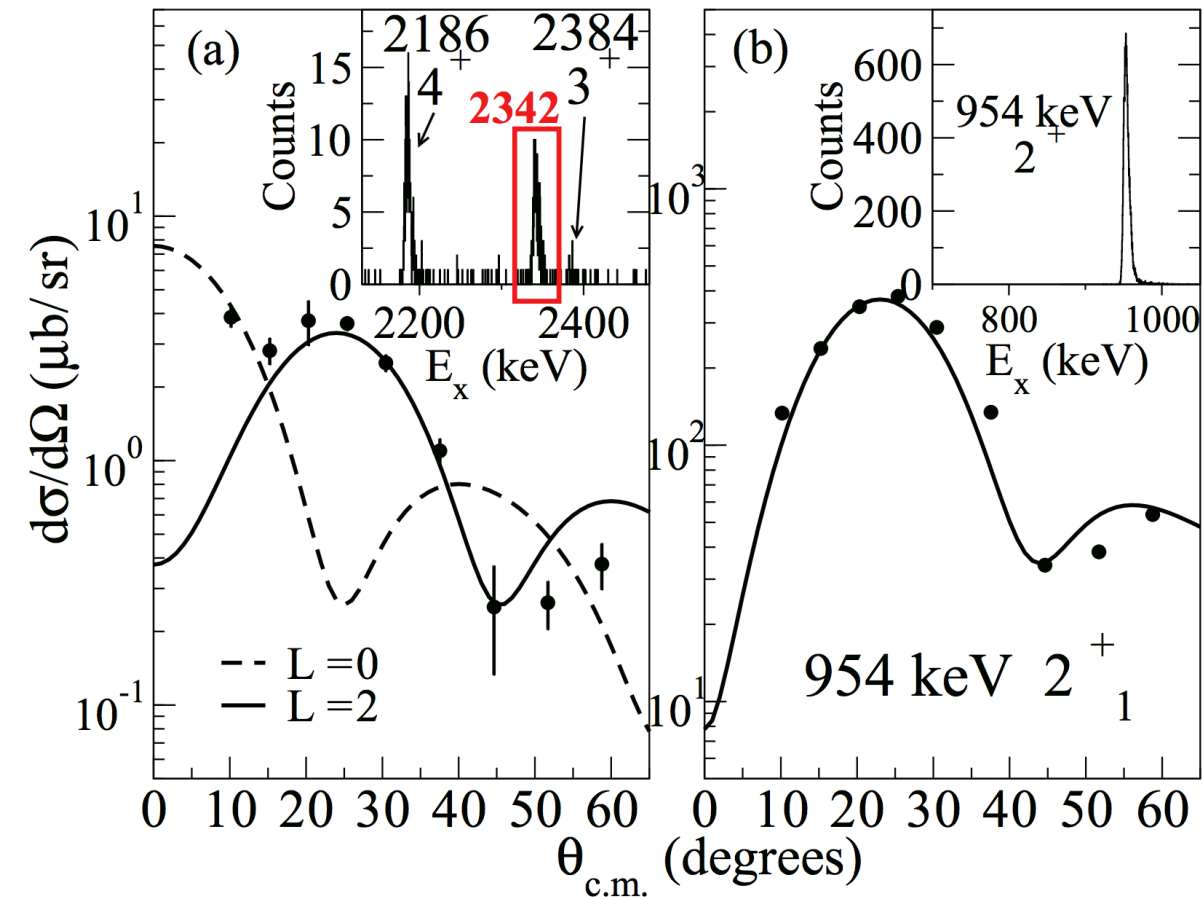
# Fractional Uncertainties



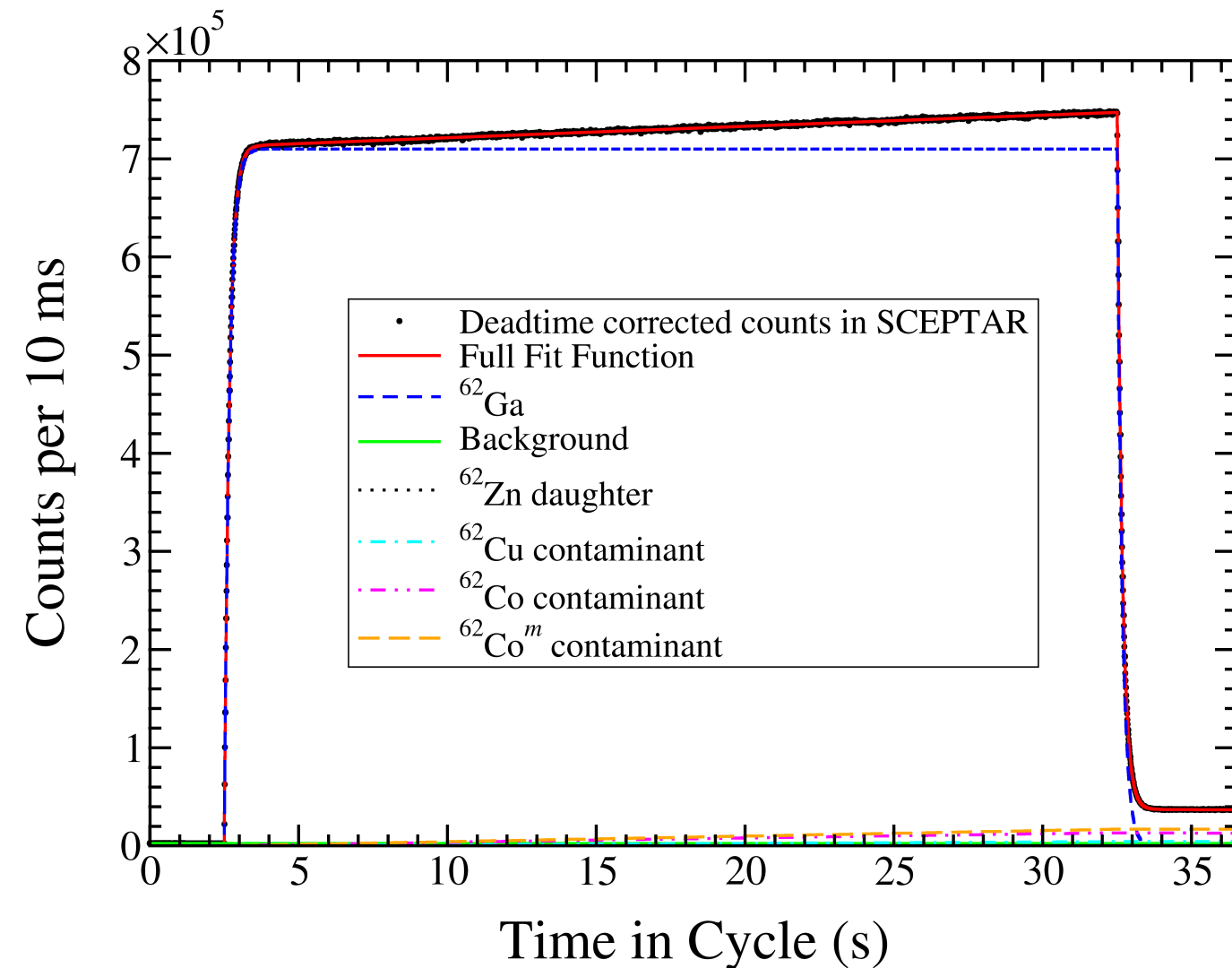
Fractional uncertainty in superallowed emitters, for the theoretical corrections in heavier nuclei  $\delta_c$  is the dominant source of uncertainty.

# Spin assignment of 2.34 MeV state

Two discrepant measurements assigning the spin of the 2.34 MeV state as  $2^+$  and  $0^+$ .

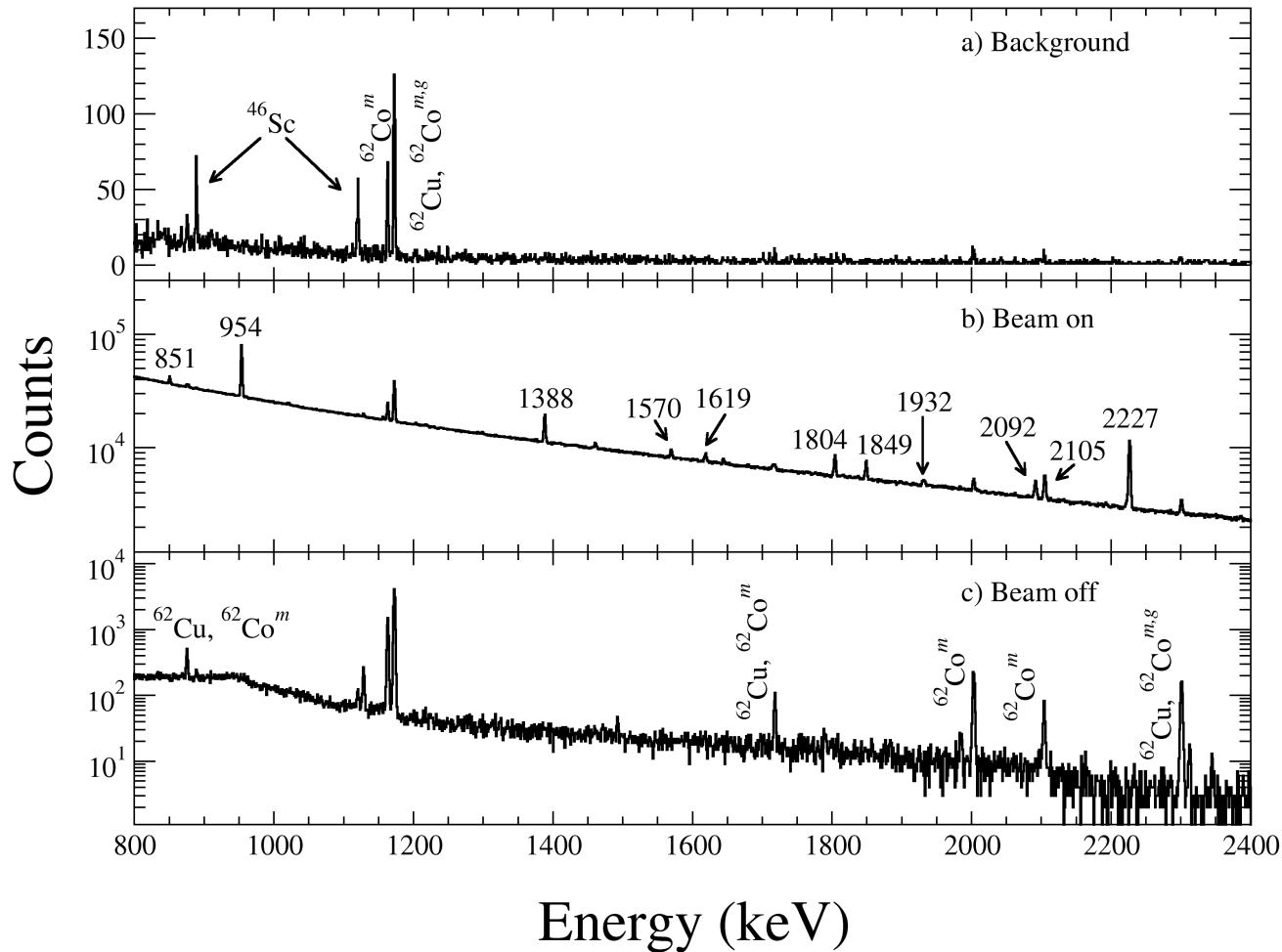


# Beta Cycle Fit



Fit to the beta cycles, integrating gives the total number of beta decays observed from  $^{62}\text{Ga}$ .

# Contaminants



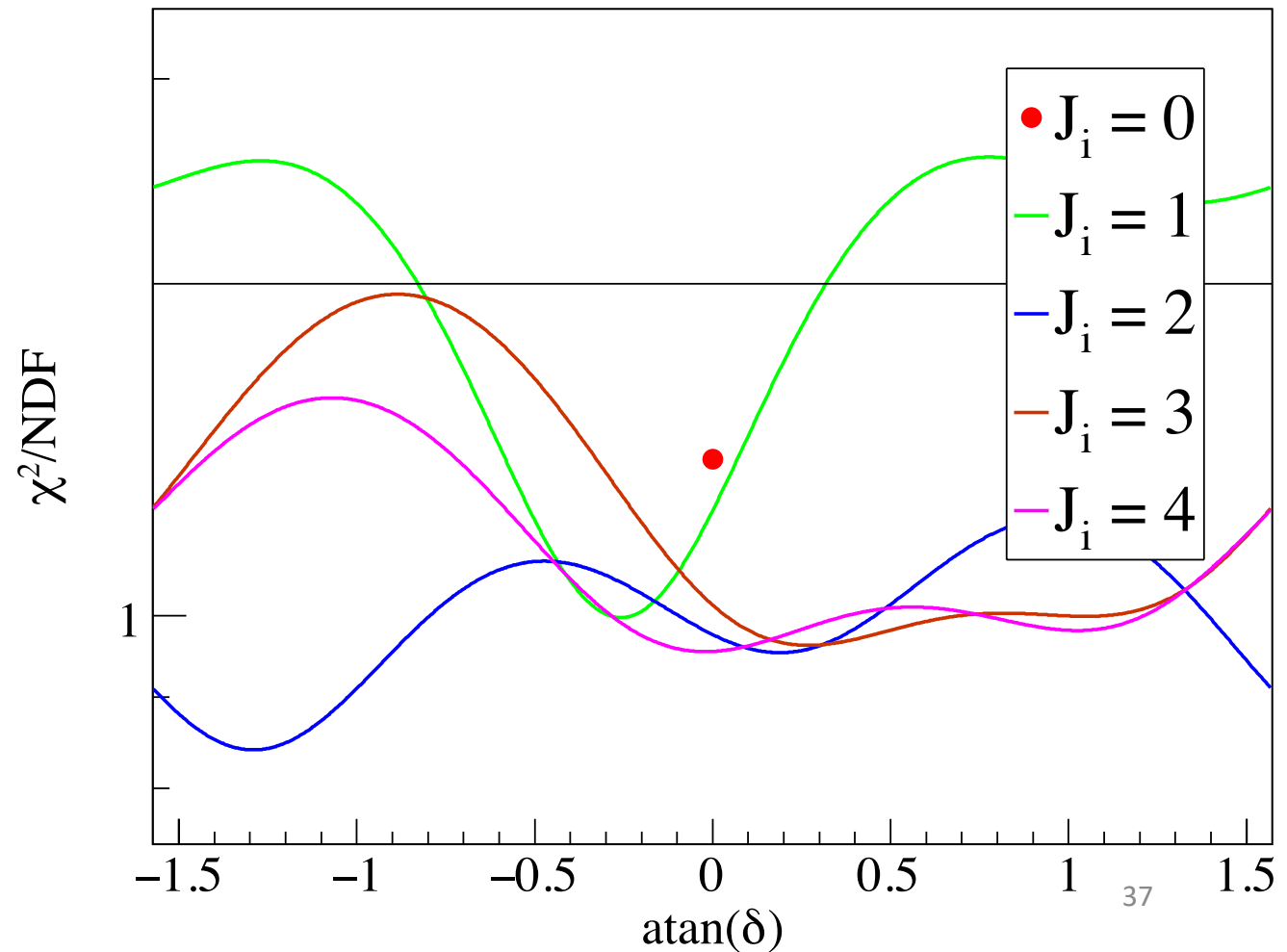
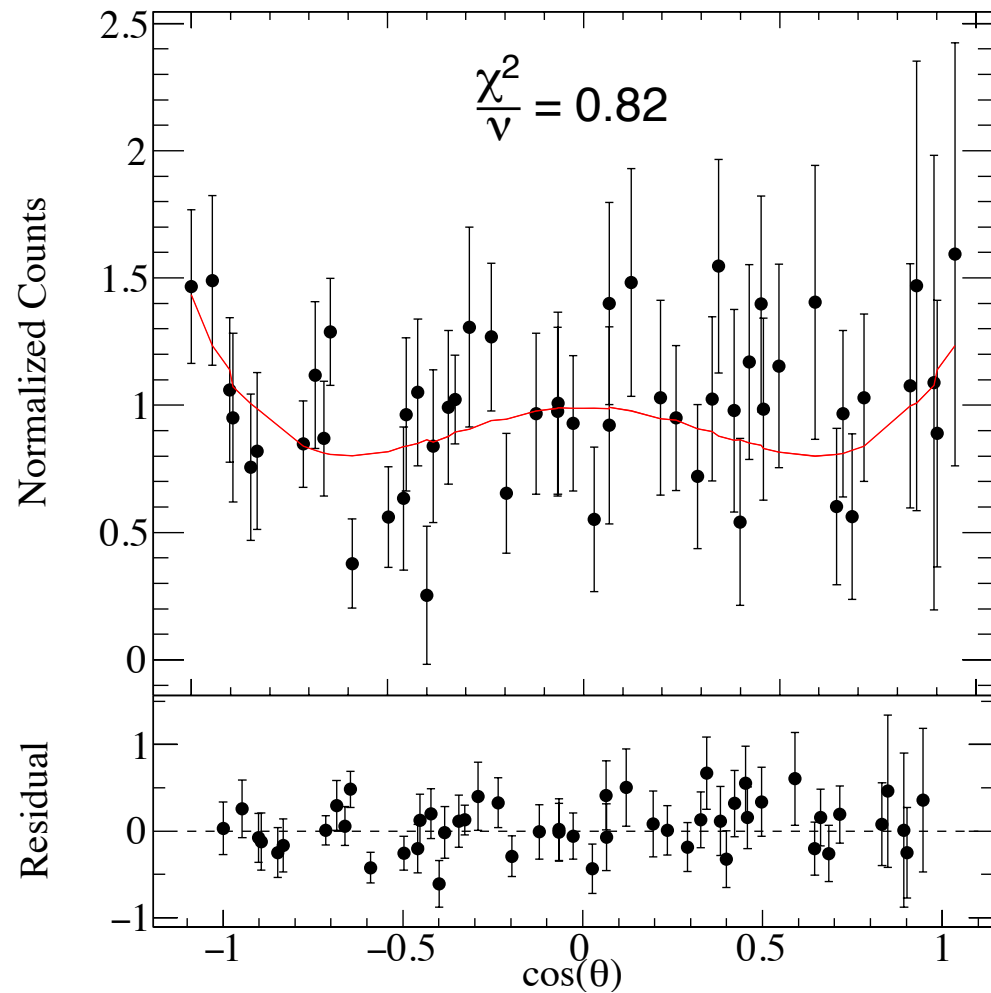
Gamma-ray spectrum gated at different points in the cycle to see contaminants.

<sup>62</sup>Co, <sup>62</sup>Cu and <sup>46</sup>Sc being the primary contaminants.



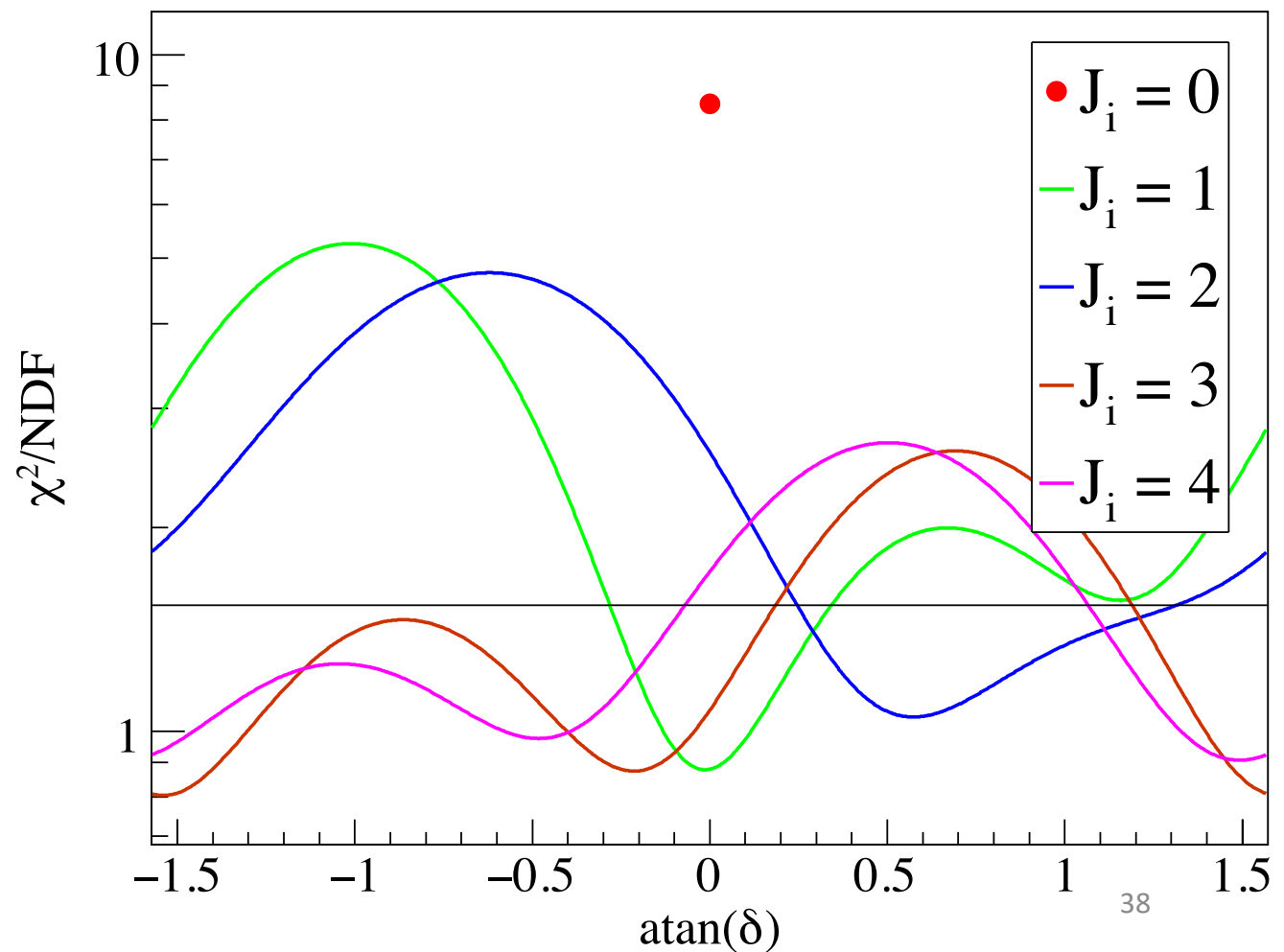
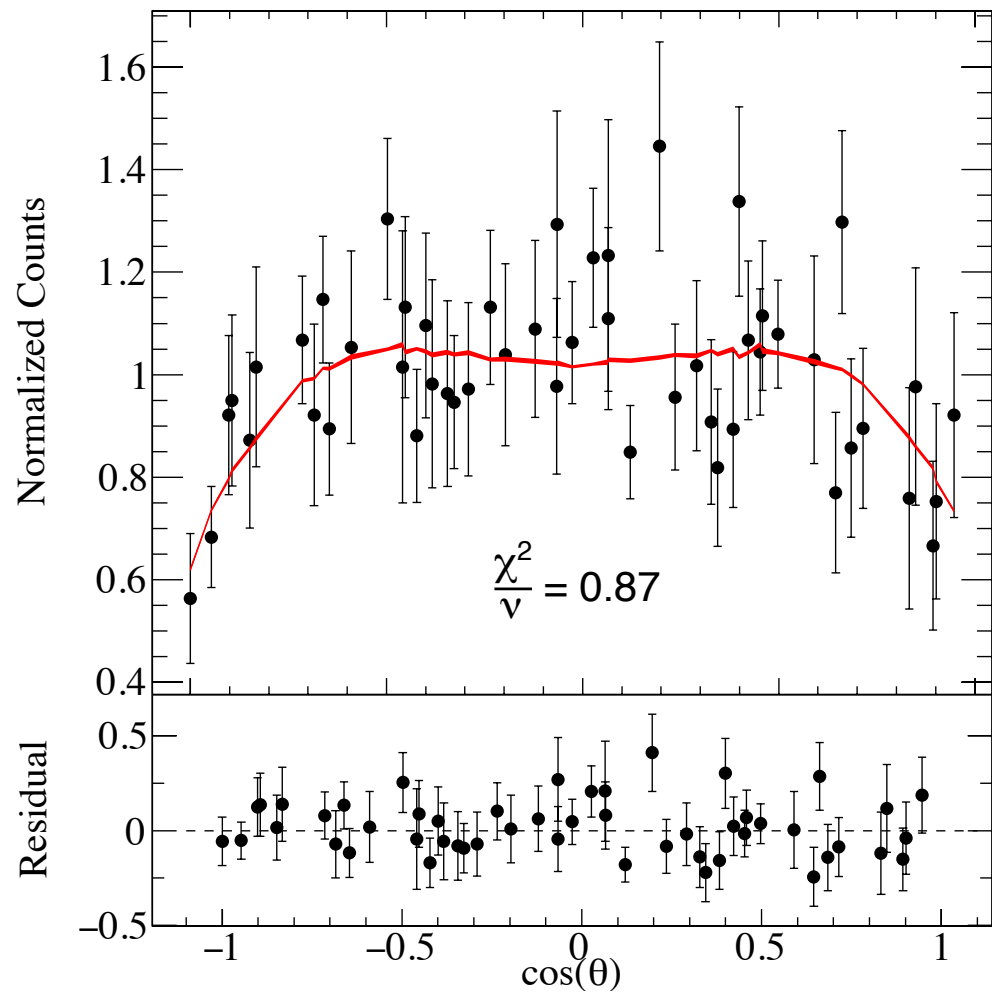
# Angular Correlations

851-954 keV cascade, known  $2^+ \rightarrow 2^+ \rightarrow 0^+$



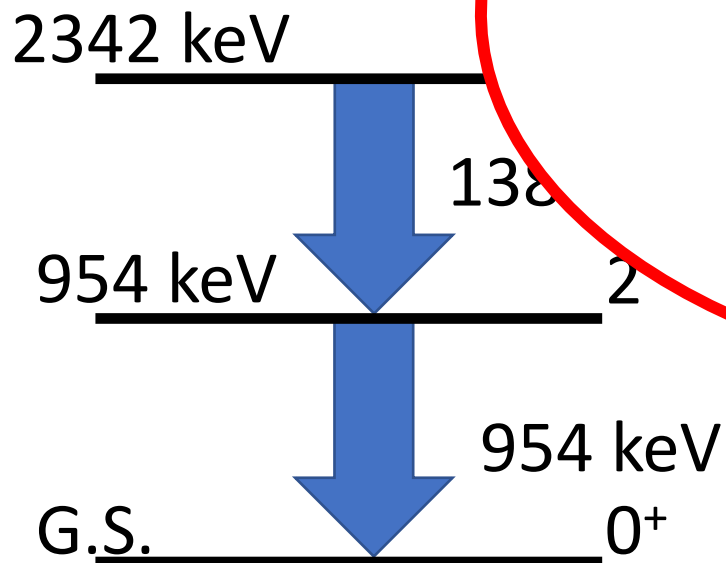
# Angular Correlations

2226-954 keV cascade, known  $1^+ \rightarrow 2^+ \rightarrow 0^+$

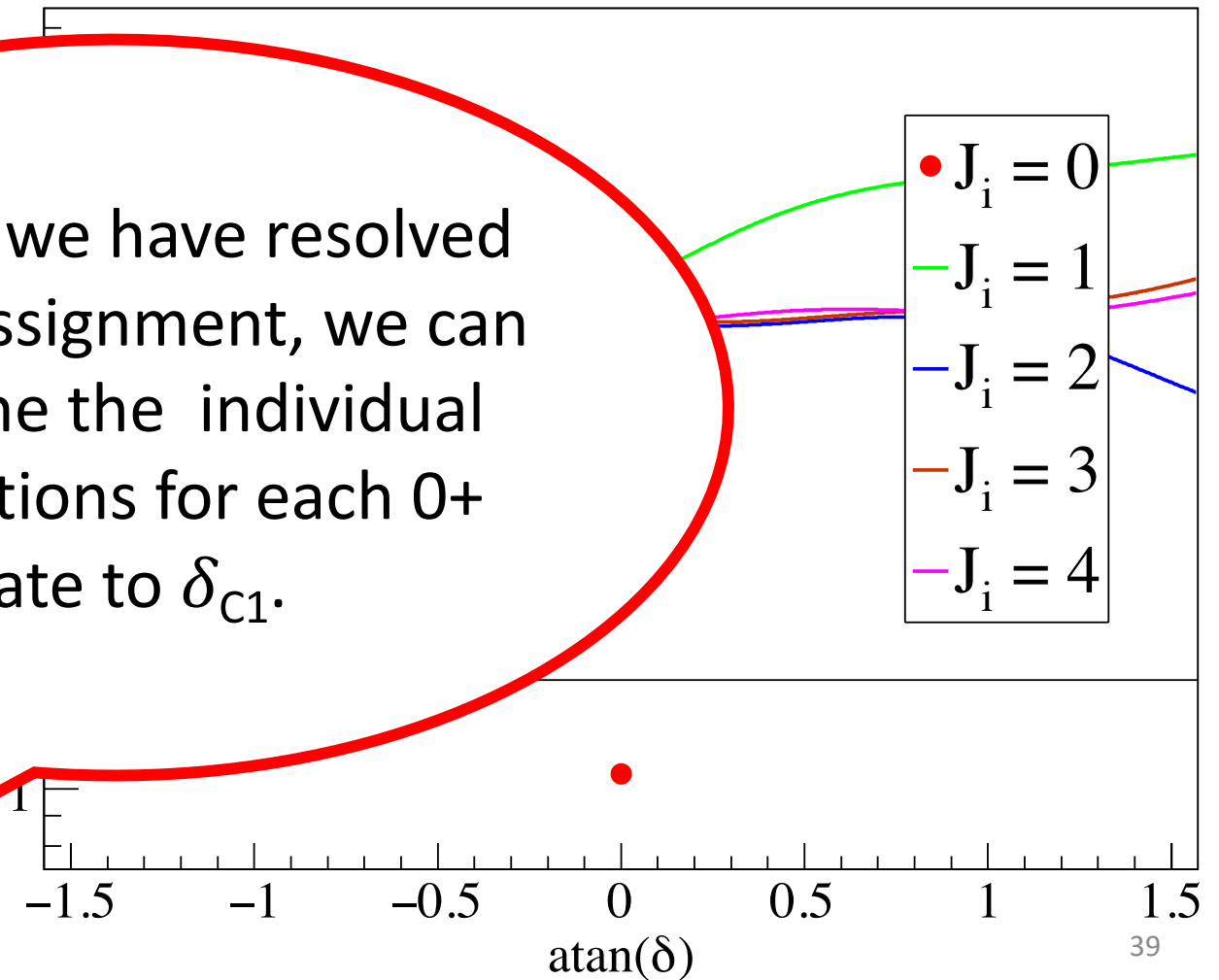


# Gamma-Gamma Angular Correlations

Allowing spin of 2342 keV state to vary can clearly identify spin as an excited  $0^+$



Now that we have resolved the spin assignment, we can determine the individual contributions for each  $0^+$  state to  $\delta_{C1}$ .

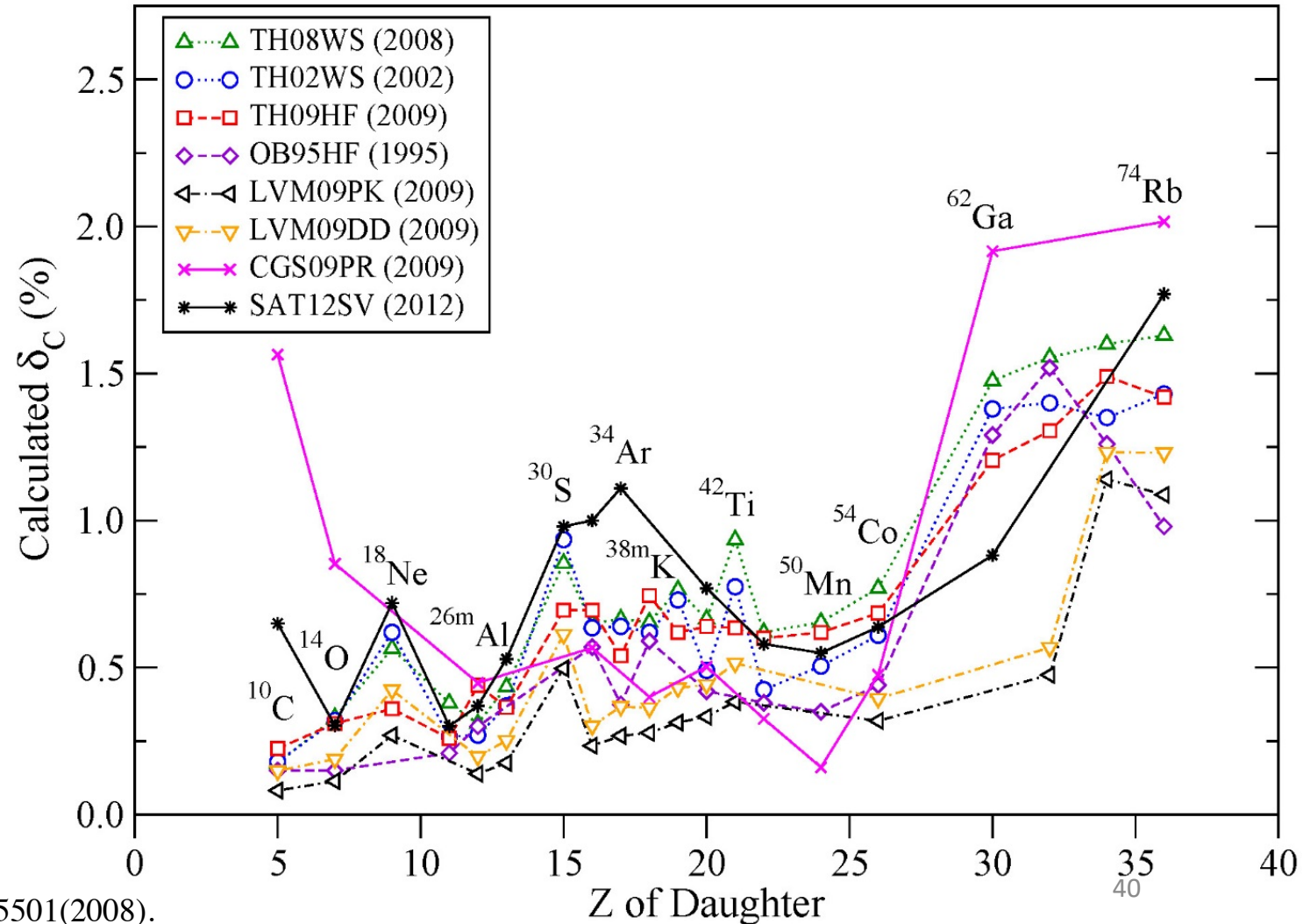


# Constraining Theory

$$\delta_C = \delta_{C1} + \delta_{C2}$$

$\delta_{C1}$  – Configuration mixing of  $0^+$  states.

$\delta_{C2}$  – Imperfect overlap of proton and neutron radial wavefunctions.



# Possible Solutions

Possible sources of disagreement:

1. One of  $|V_{ud}|$ ,  $|V_{us}|$ , or  $|V_{ub}|$  may need to be re-evaluated.
2. There could be physics which exists beyond the Standard Model.
3. The applied corrections currently used for the  $\mathcal{F}t$ -values may need to be further scrutinized and include a larger model space.

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$

# Possible Solutions

Possible sources of disagreement:

1. One of  $|V_{ud}|$ ,  $|V_{us}|$ , or  $|V_{ub}|$  may not be known well enough.
2. There could be physics which exist which are not included in the current theory.
3. **The applied corrections currently used should be further scrutinized and include**

Dominant source of uncertainty (especially heavy nuclei).

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$