

# Recent highlights from the GRIFFIN spectrometer

Gamma-Ray Infrastructure For Fundamental  
Investigations of Nuclei

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*Victoria Vedia TRIUMF Science week*



# TRIUMF: Canada's National Laboratory for Accelerator-based science



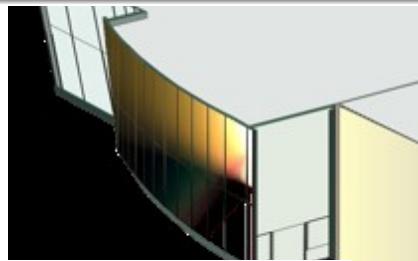
- 18 m in diameter
  - 520 MeV proton beam
  - 4 beamlines
- > 50 years of accelerator-based science and innovation

# ISAC: Isotope Separator and ACcelerator

## ISAC-I and ISAC-II Facility

### ISAC II:

- 10 AMeV for A<150
- 16AMeV for A<30



### ISAC I:

60 keV & 1.7 AMeV

ISOL facility with ***high primary beam intensity*** (100  $\mu$ A, 500MeV, p)  
Delivering RIBs since 1999.

17/07/2022

Victoria Vedia TRIUMF Science week

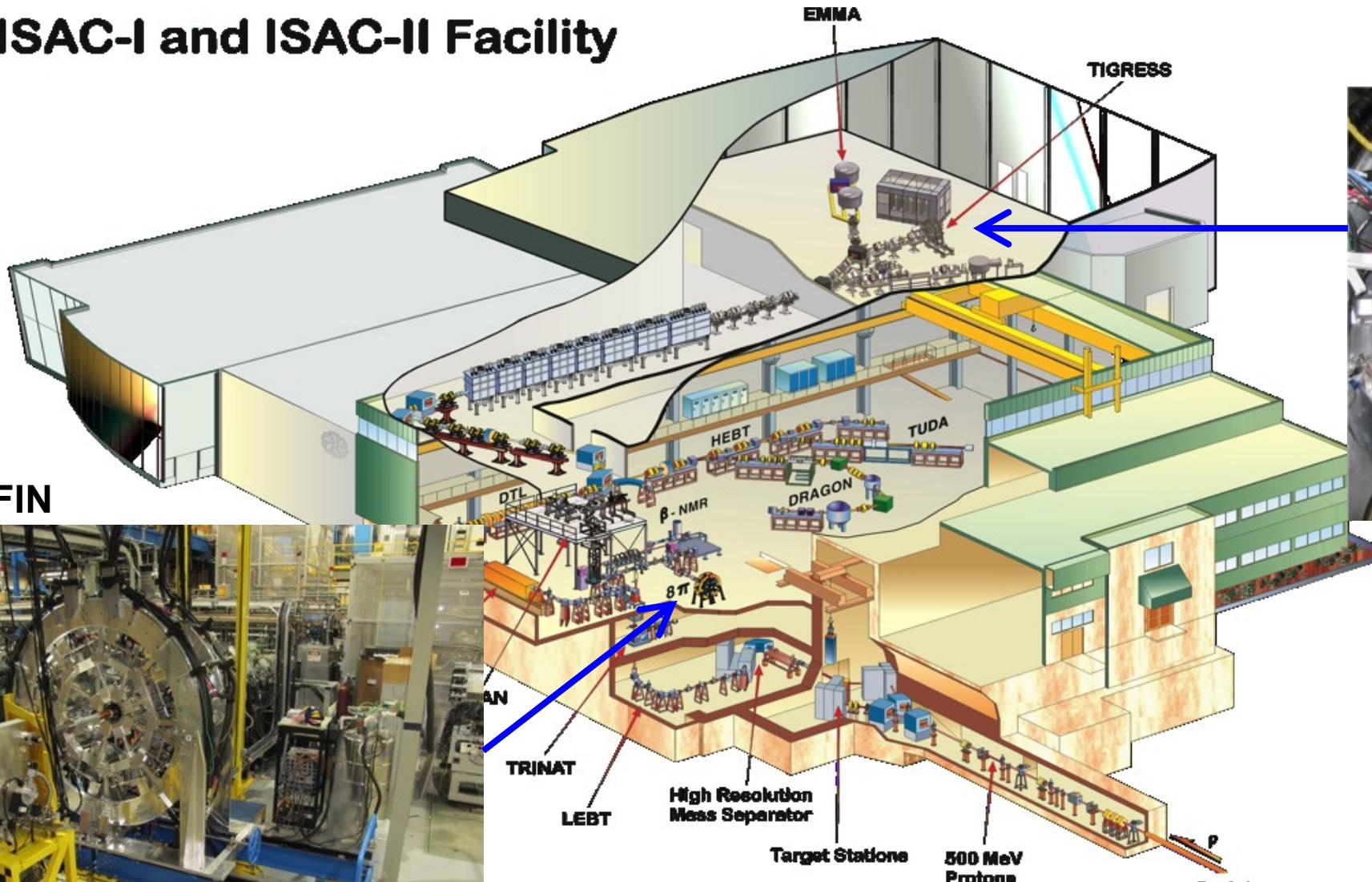
500MeV p<sup>+</sup> at 100 $\mu$ A  
on ISOL target

Targets: SiC, TiC,  
NiO, Nb, ZrC, Ta,  
TaC, ThO, UO, UCx  
Ion sources:  
Surface, TRILIS,  
FEBIAD, IG-LIS

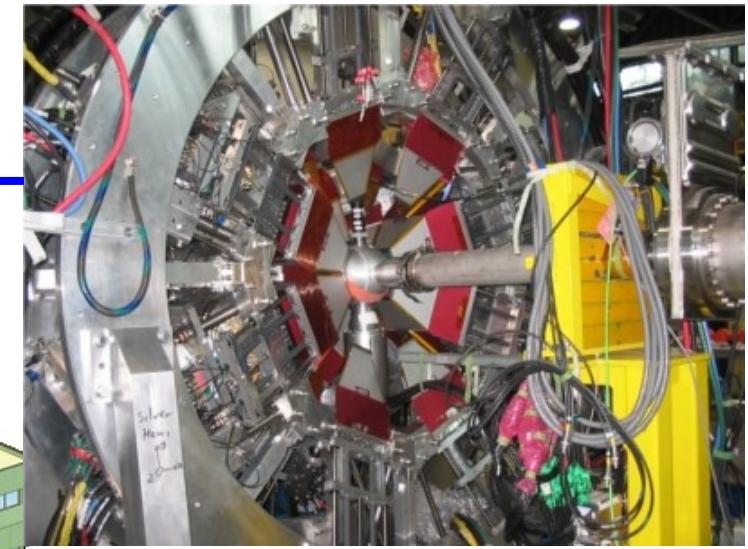


# Gamma-Ray Spectroscopy at ISAC

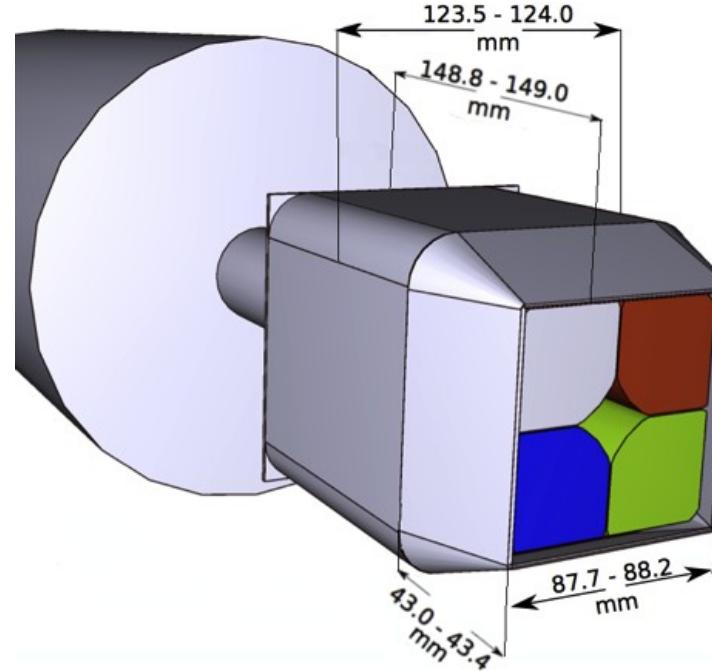
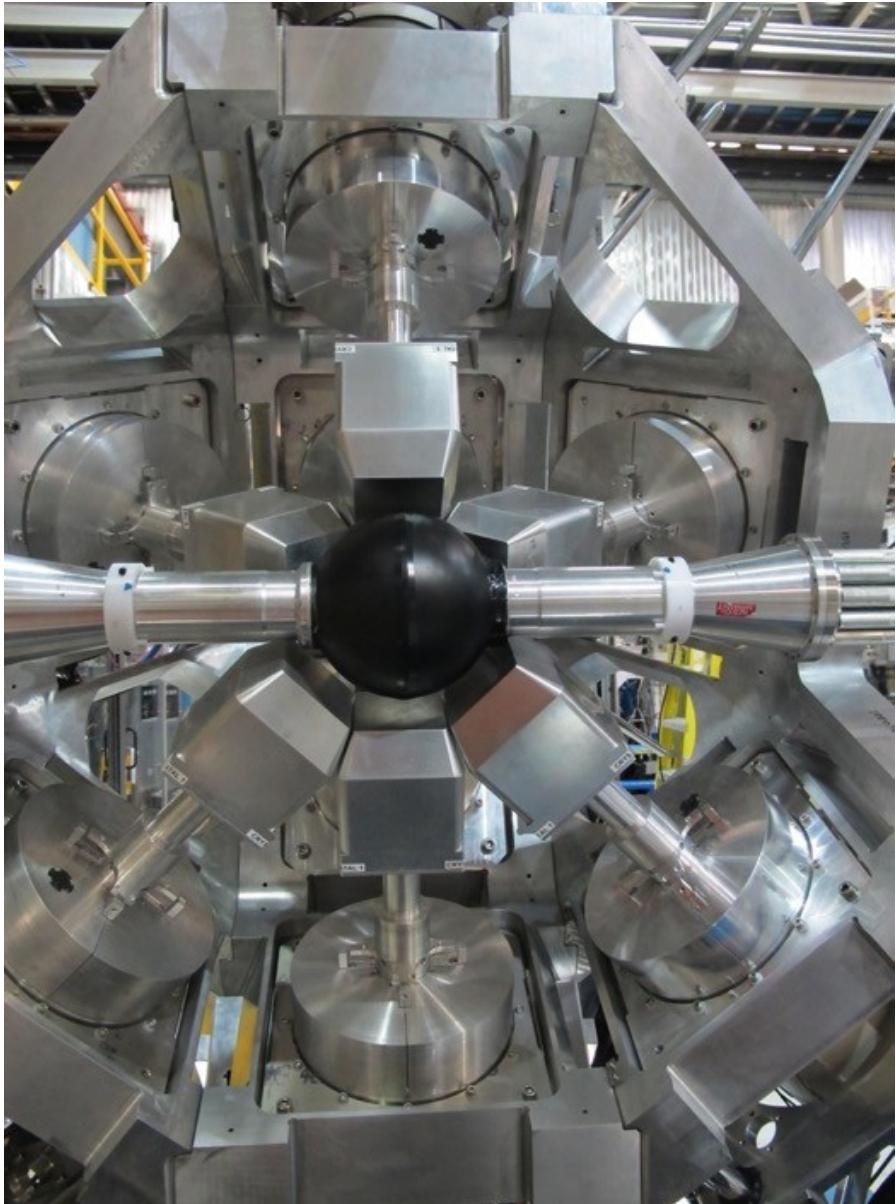
## ISAC-I and ISAC-II Facility



## TIGRESS



# GRiffin spectrometer



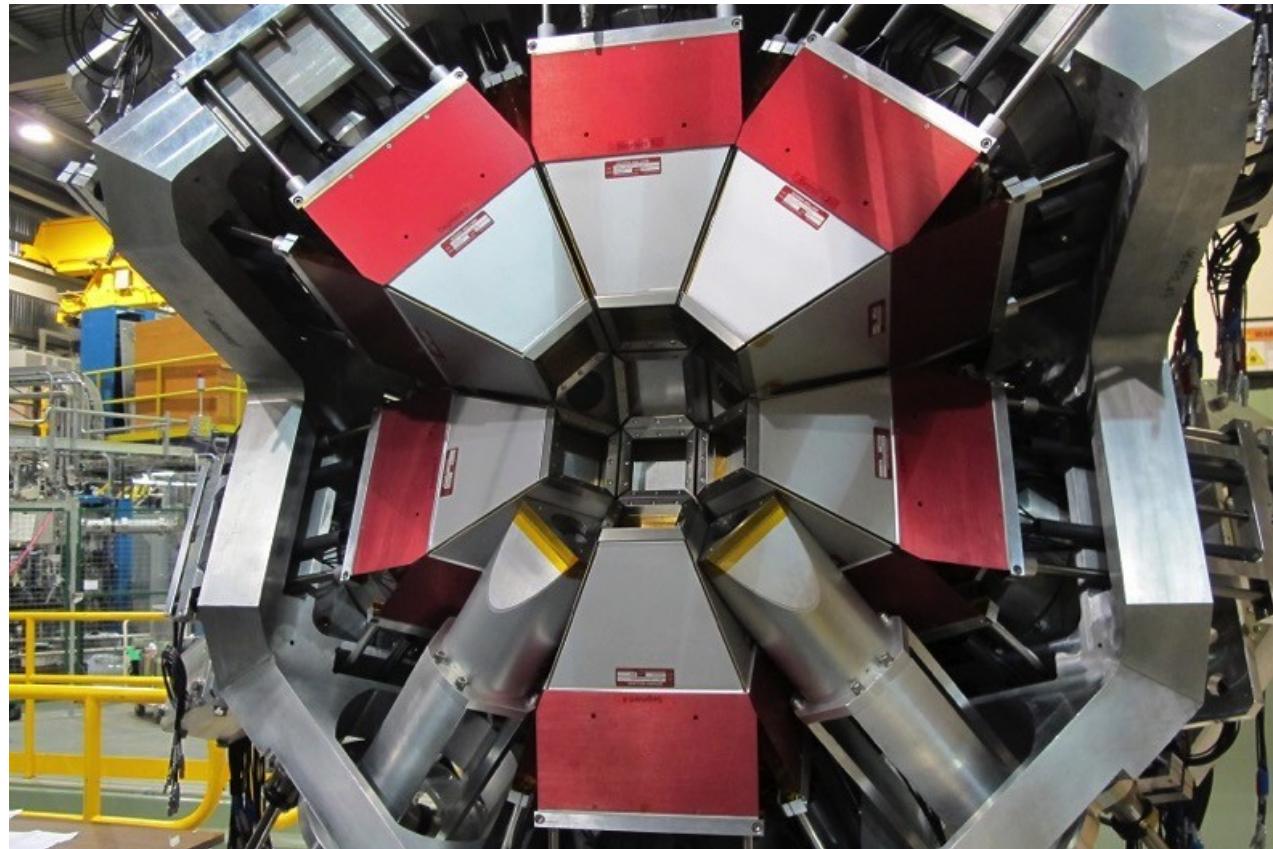
- 16 Clover HpGe detectors
- 4 HPGe crystals in each cryostat (addback)

Average Performance of all 64 crystals (16 clovers):  
Energy resolution@ 121keV = 1.12(6) keV  
Energy resolution@ 1.3MeV = 1.89(6) keV  
Photo-peak Rel. Eff. @ 1.3MeV = 41(1) %

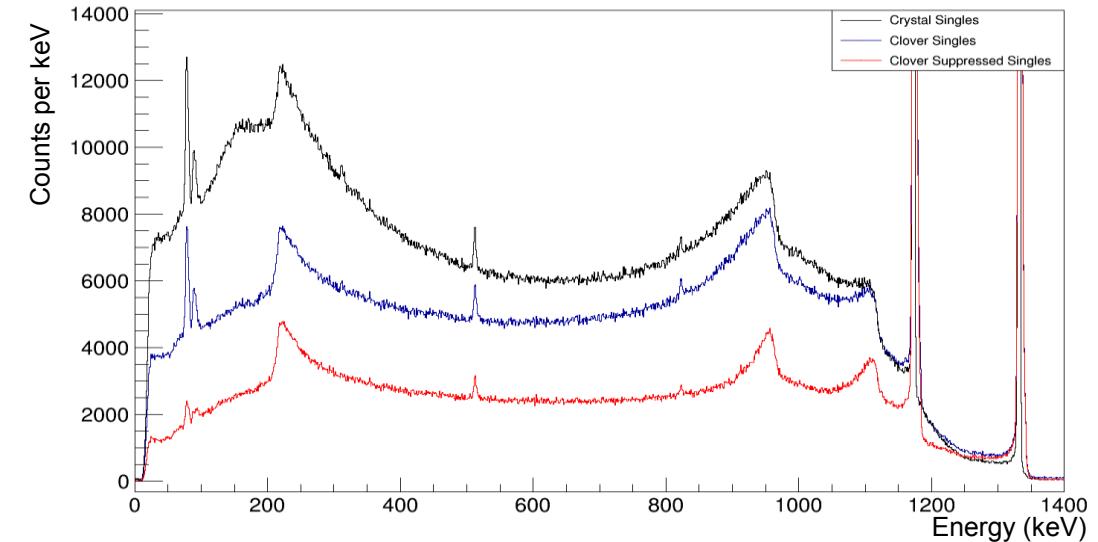
U. Rizwan *et al.*, NIM A 820, 126 (2016)

# GRiffin Compton and Background Suppression Shields

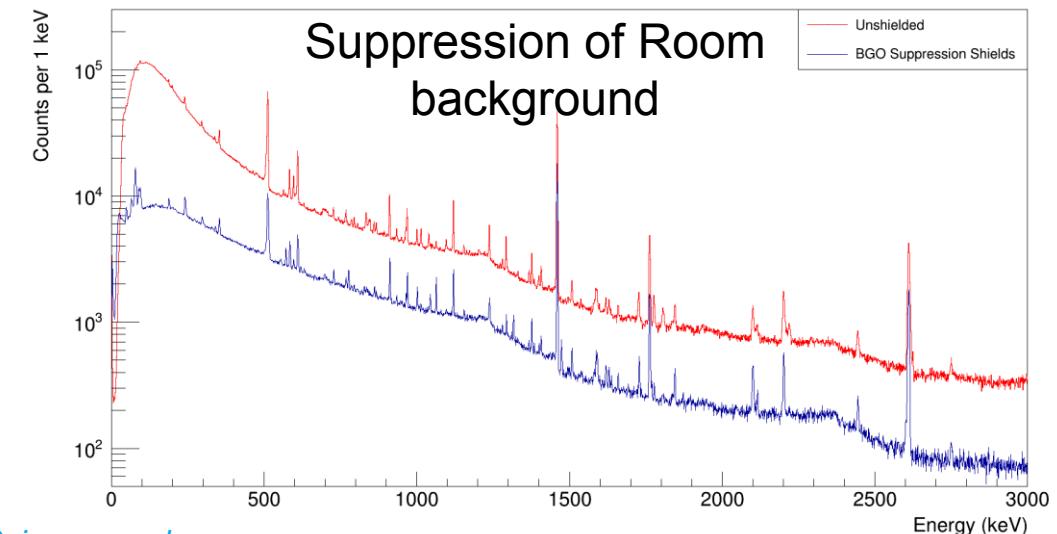
- All performance acceptance testing completed at Simon Fraser University
- Array has operated with full-suppression since June 2018.



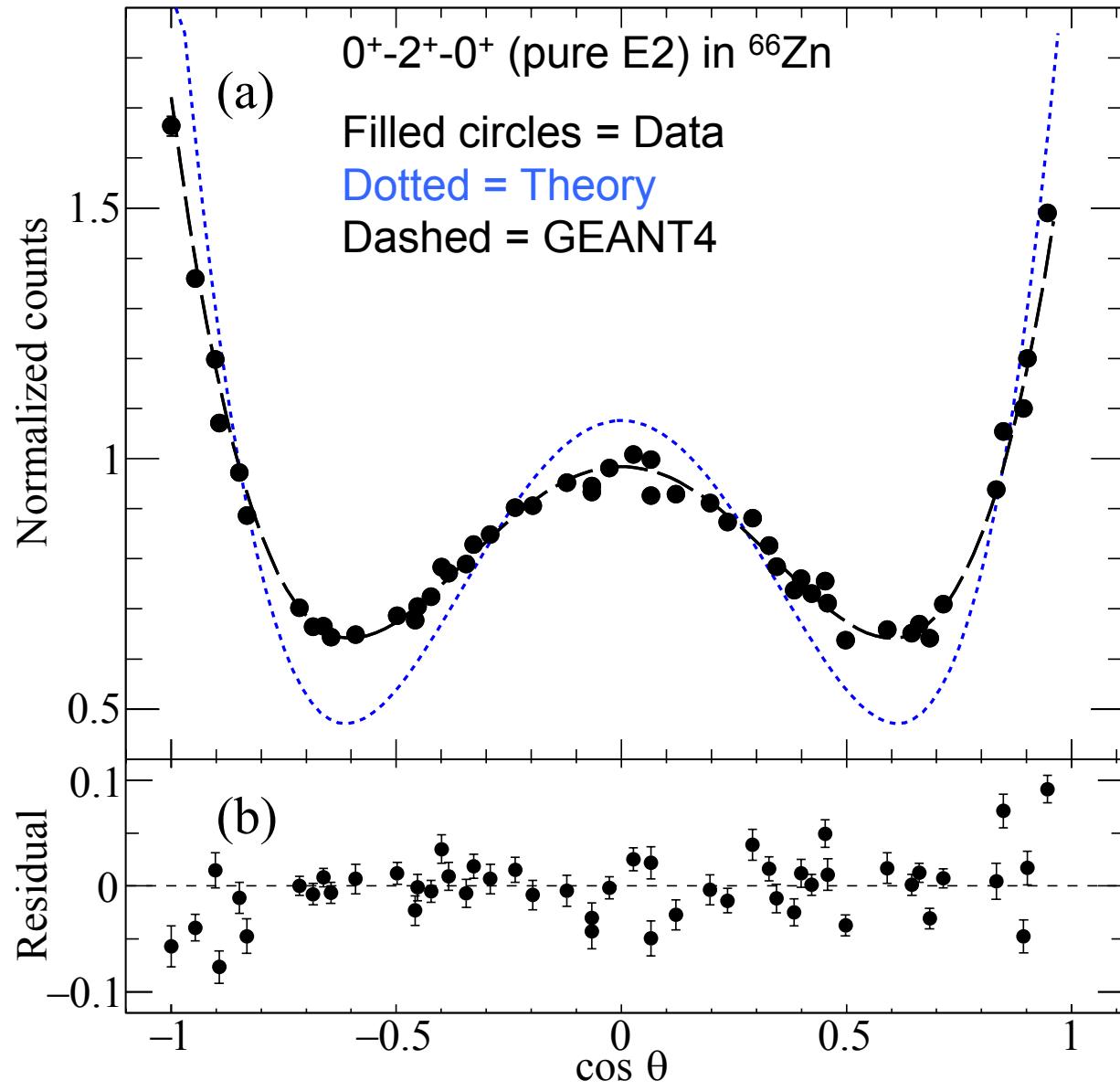
Online hardware suppression now available  
in GRIF-C filter



3 Hour Room Background



# Gamma-Gamma Angular Correlation Analysis



J.K. Smith, A.C. MacLean *et al.*  
NIM A 922, 47 (2019).  
<https://arxiv.org/abs/1807.07570>

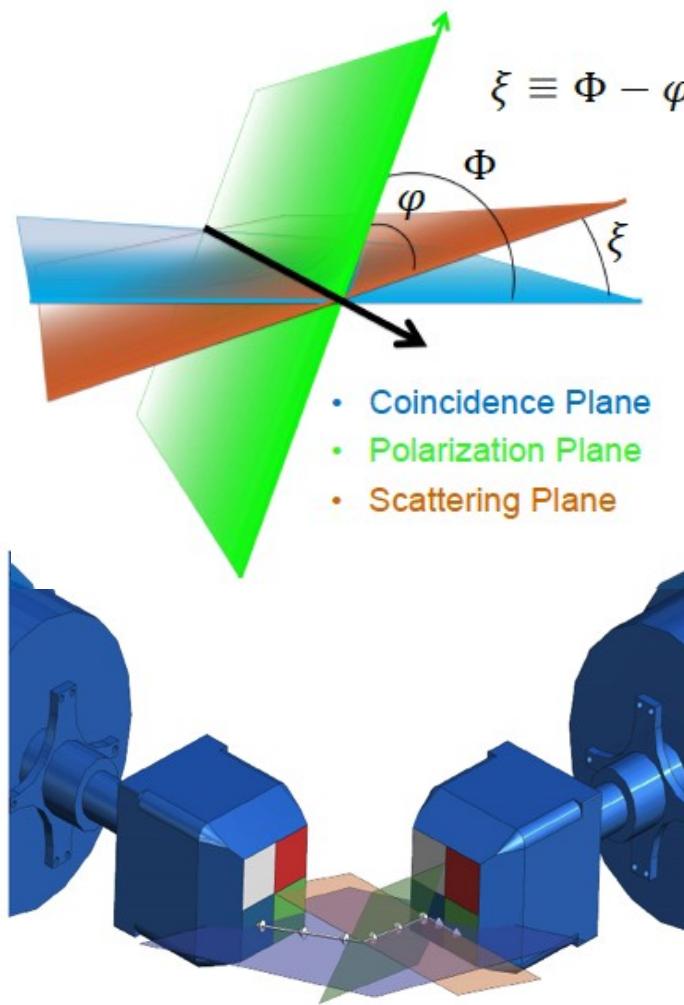
Development of  $\gamma-\gamma$  angular correlation analysis techniques with GRIFFIN.

- Finite size and shape of crystals means theoretical distribution is attenuated.
- Obtain ‘template’ from high-statistics GEANT4 simulation
- Fit template to experimental data.

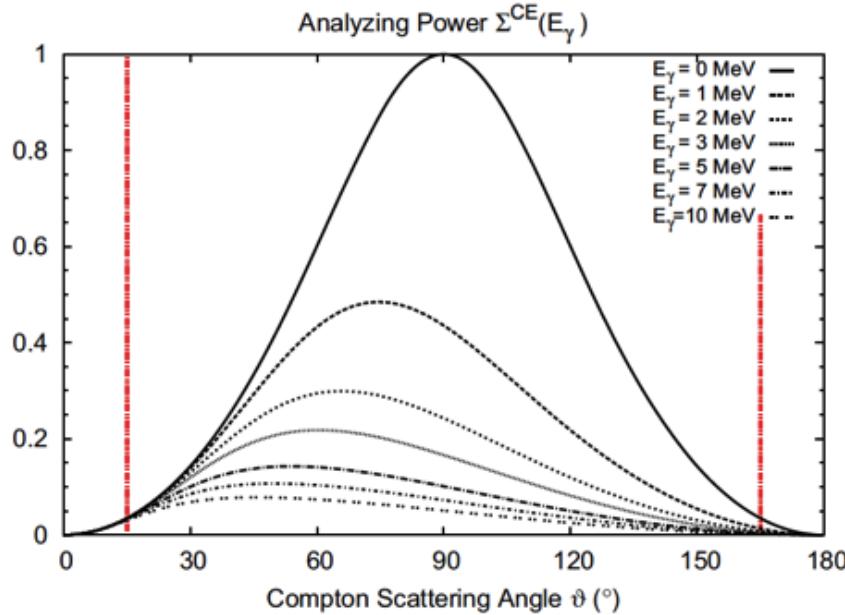
Ideally:

- Fit experimental data
- Plug coefficients into simple equations
- Obtain corrected ‘true’ coefficients

# Compton Polarimetry using GRIFFIN



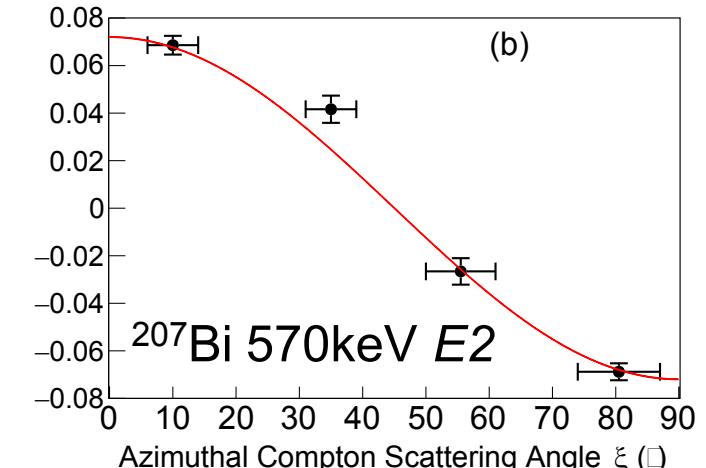
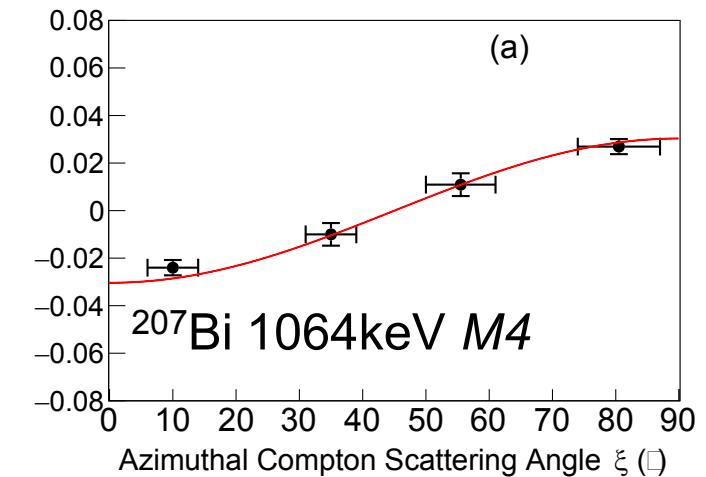
Define Polarization plane from  $\gamma-\gamma$  coincidence detection.  
Then examine azimuthal scattering angle to determine electric or magnetic nature of the radiation.



Dan Southall, TRIUMF research student, 2016

A.B. Garnsworthy et al., NIMA 918, 9 (2019)

B. Alikhani et al., NIMA 675, 144 (2012).



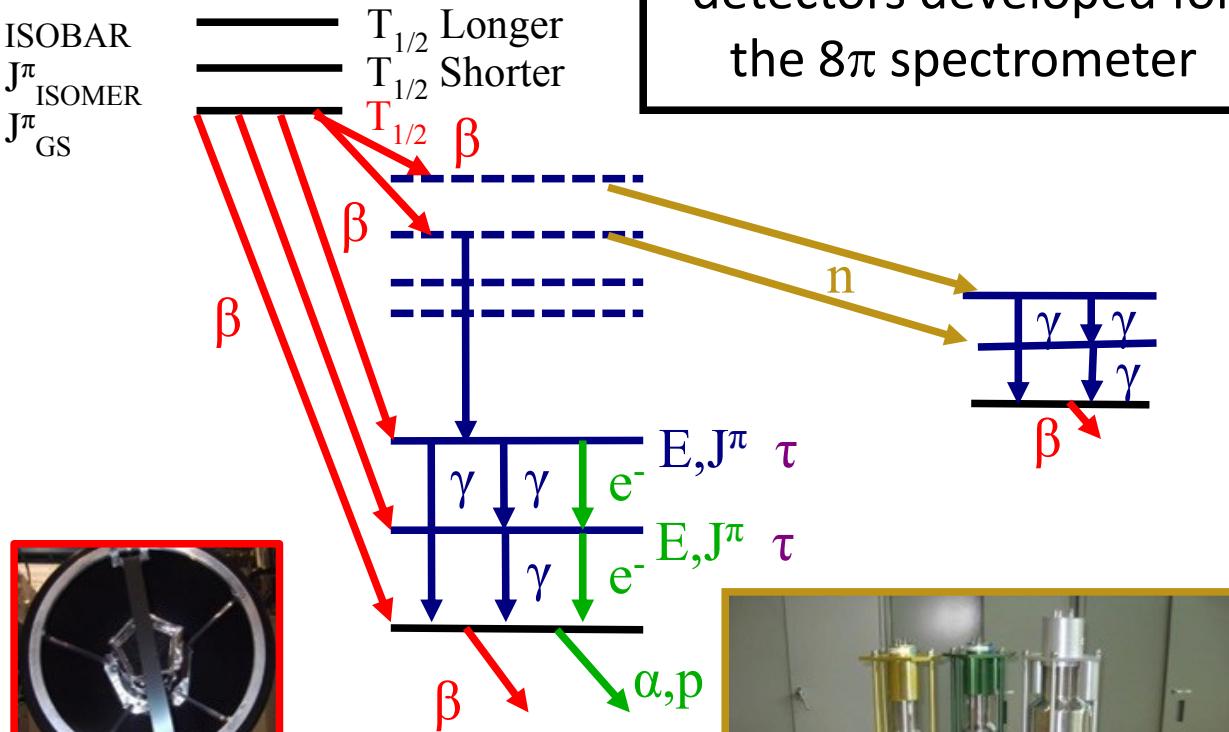
# GRiffin Ancillary Detectors



Fast, in-vacuum tape system  
Enhances decay of interest

ISOBAR  
 $J^\pi$   
ISOMER  
 $J^\pi$   
GS

—  $T_{1/2}$  Longer  
—  $T_{1/2}$  Shorter  
—  $T_{1/2}$

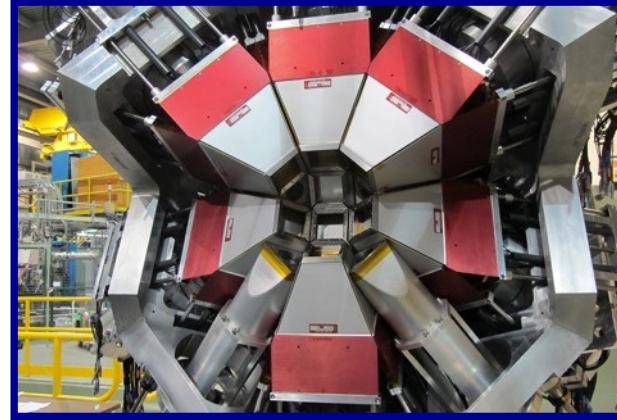


SCEPTAR: 10+10 plastic scintillators

Detects beta decays and determines branching ratios

17/07/2022

GRiffin reuses the full suite of ancillary detectors developed for the  $8\pi$  spectrometer



HPGe: 16 Compton-suppressed Clovers  
Detect gamma rays and determines branching ratios, multipolarities and mixing ratios

LaBr<sub>3</sub>: 8 Compton-suppressed LaBr<sub>3</sub>  
Fast-timing of photons to measure level lifetimes



Zero-Degree Fast scintillator  
Fast-timing signal for betas

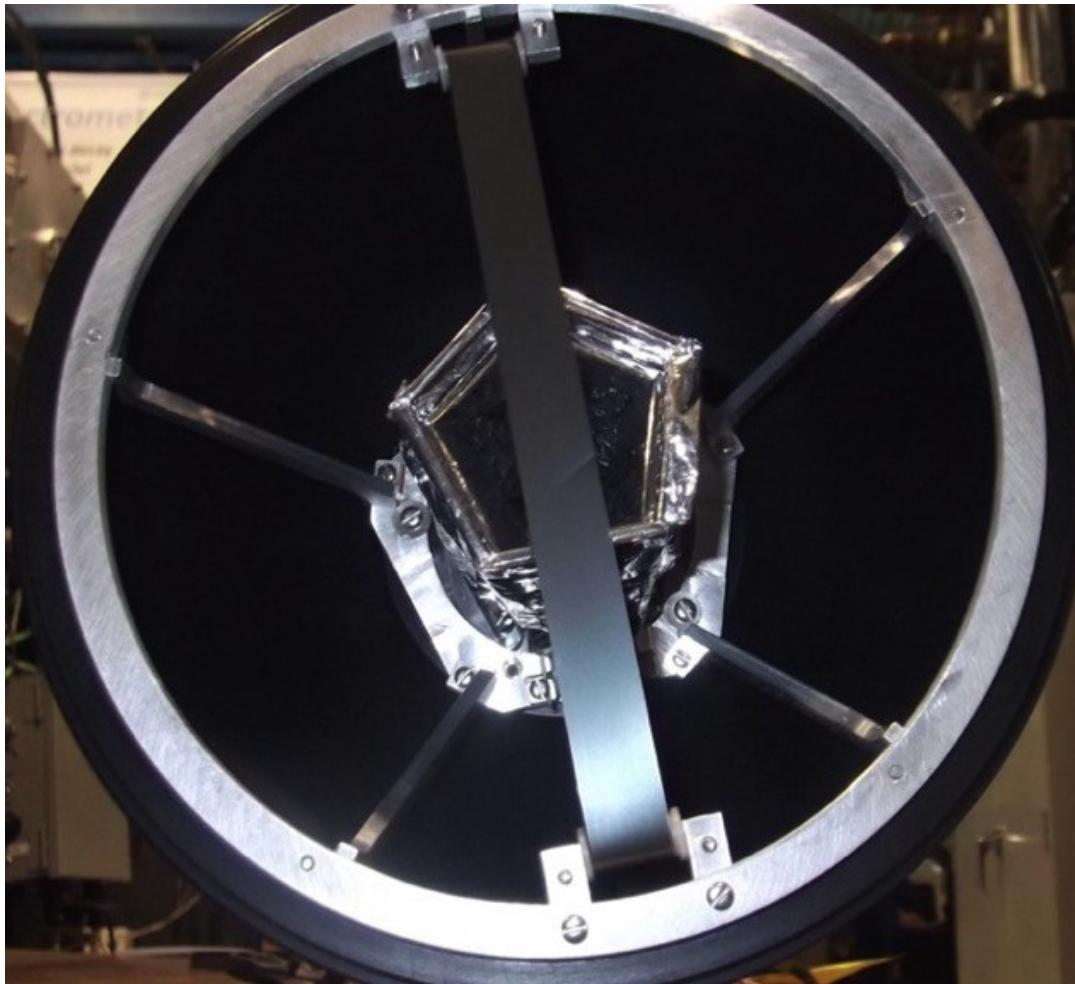


PACES: 5 Cooled Si(Li)s  
Detects Internal Conversion Electrons and alphas/protons

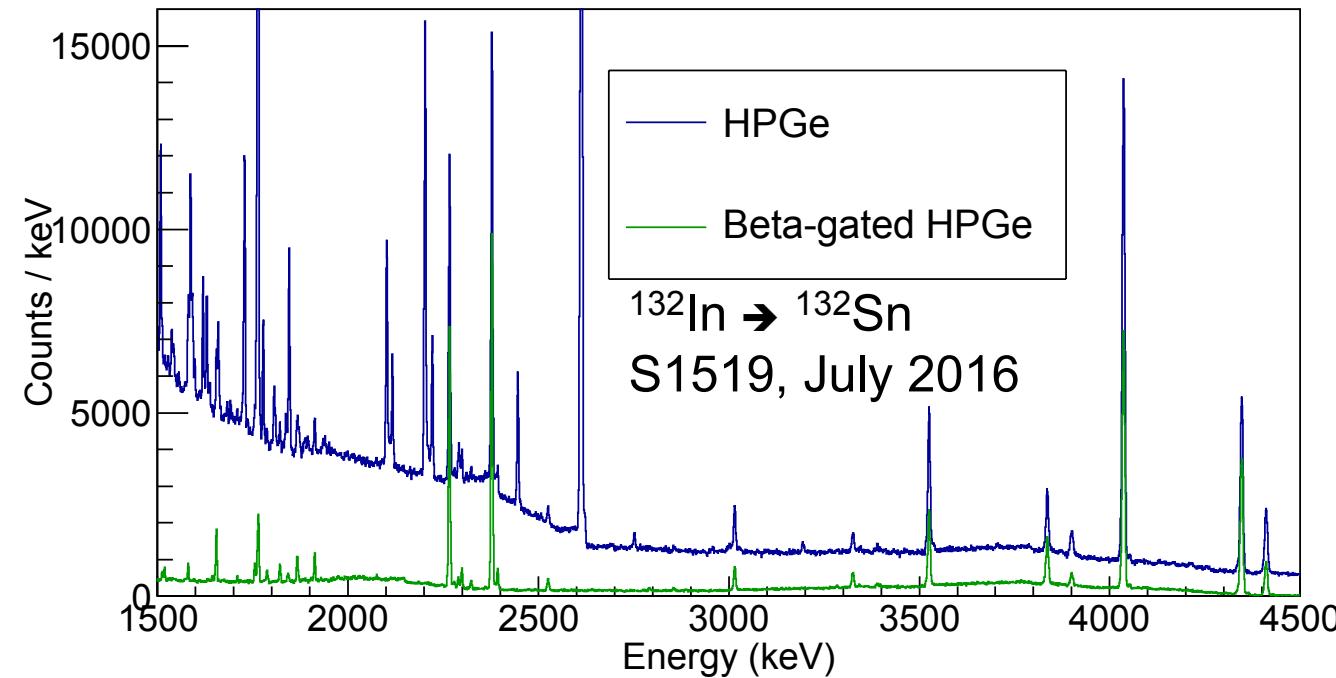


DESCANT Neutron array  
Detects neutrons to measure beta-delayed neutron branching ratios

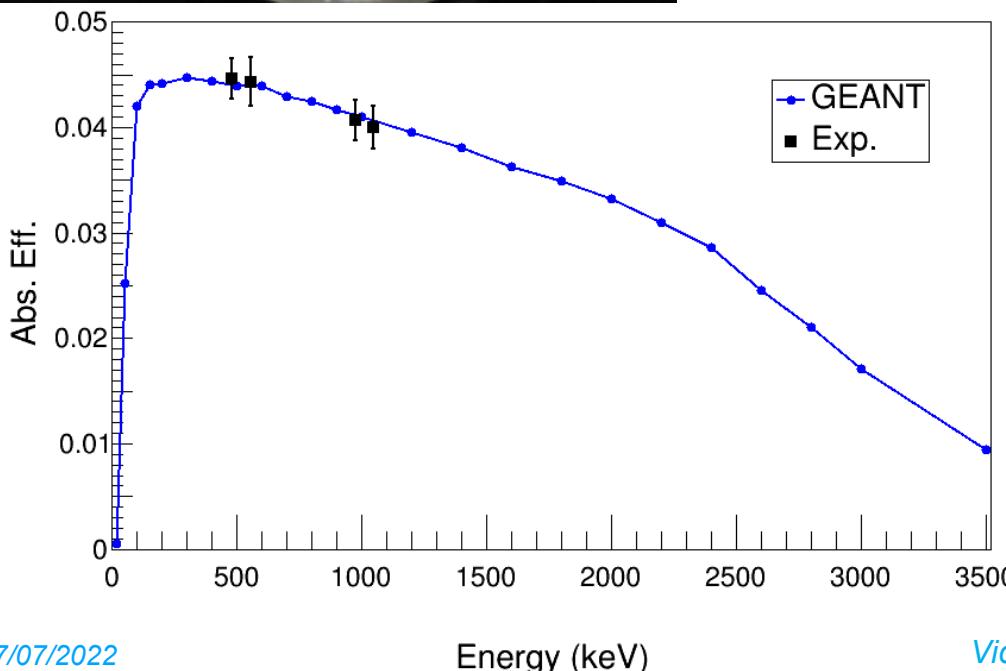
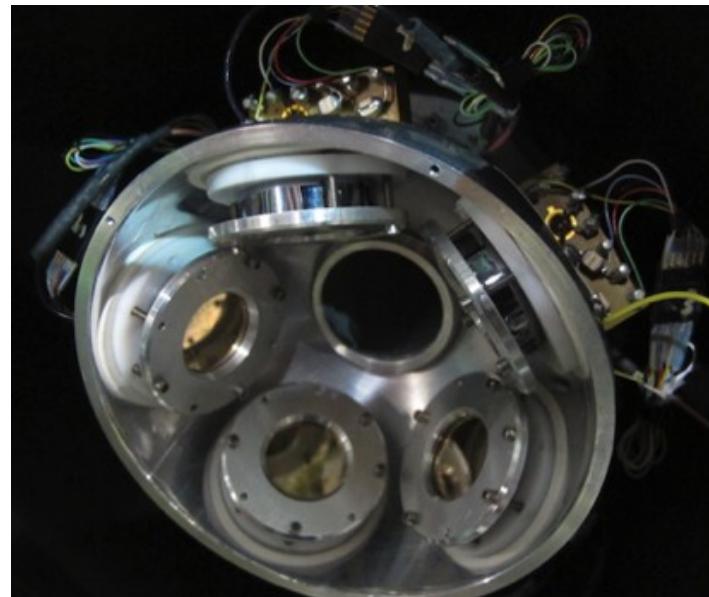
# SCEPTAR - SCintillating Electron-Positron Tagging ARray



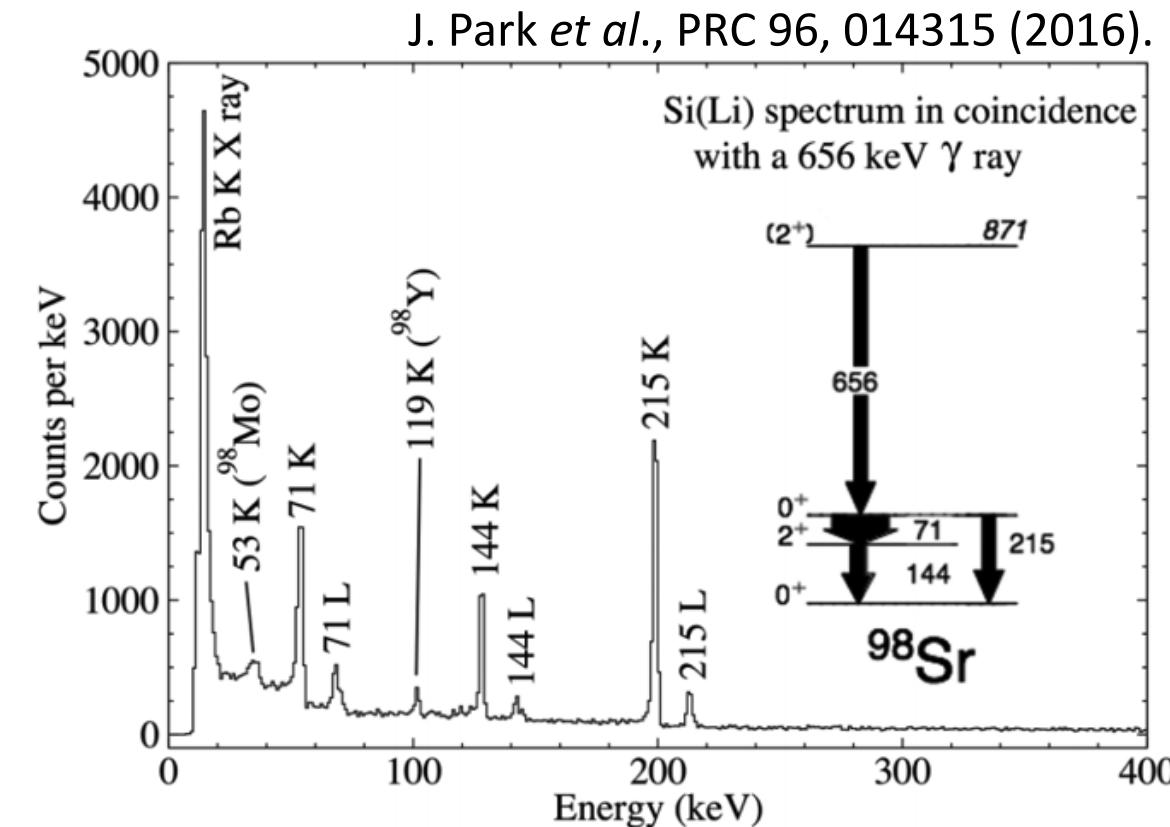
- Two hemispheres of 10 plastic scintillators
- Detects beta particles with ~80% solid angle coverage
- Improves peak-to-background of HPGe spectra
- Reduces random background by ~5 orders of magnitude



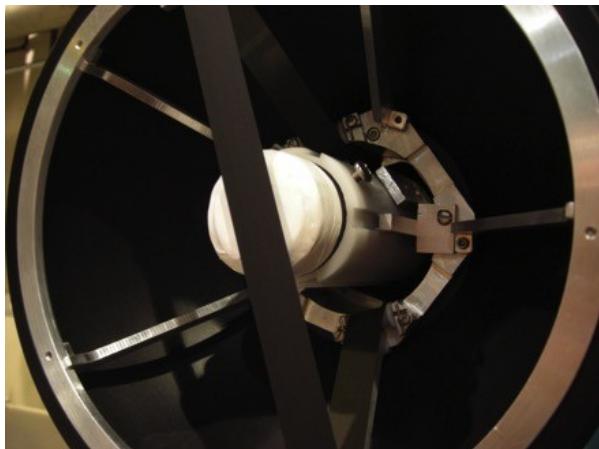
# PACES - Pentagonal Array for Conversion Electron Spectroscopy



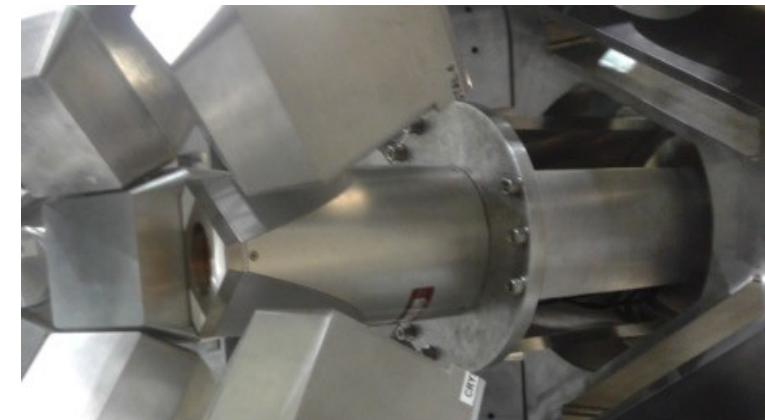
- Five 5mm thick, 200mm<sup>2</sup> Si(Li), LN<sub>2</sub>-cooled Si diode and FET
- Solid angle coverage: 1.4% each, 7% total
- 2 keV resolution for electrons



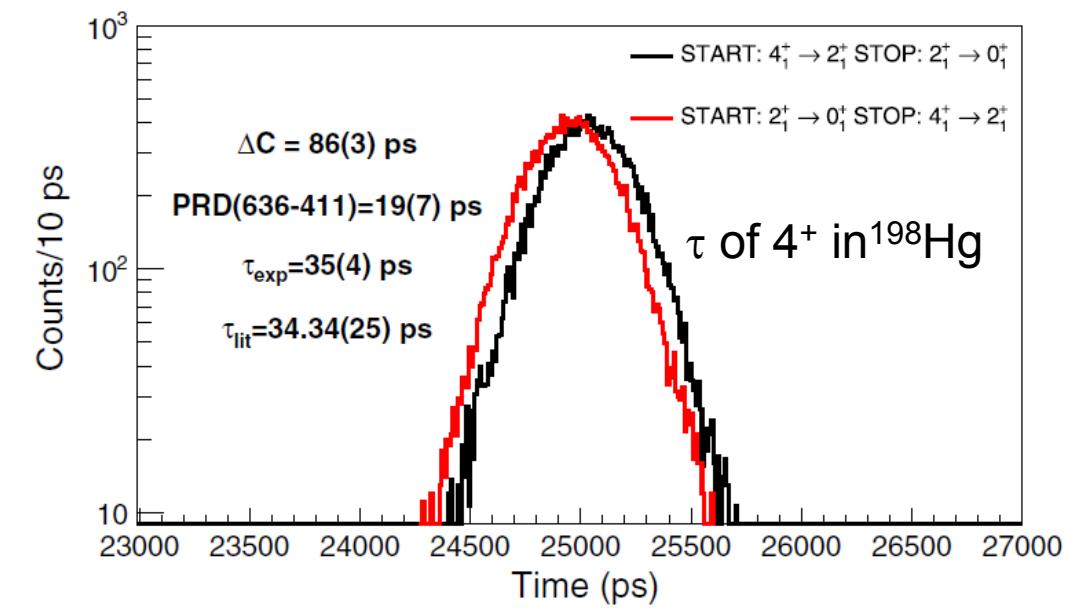
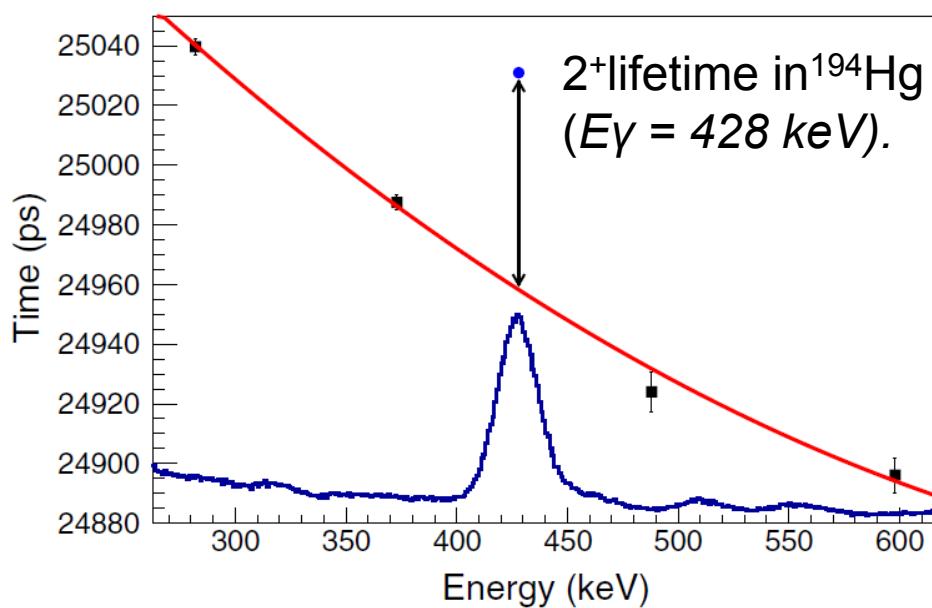
# $\text{LaBr}_3$ Fast-Scintillator Array for Excited-State Lifetime Measurements



- Eight  $\text{LaBr}_3(\text{Ce})$  2"x2" cylindrical crystal
- Source-detector distance=12.5 cm. (unshielded) and 13.5 cm (with BGO shield)
- Fast beta scintillator (BC422Q).
- Hybrid analogue + digital electronics, excellent time resolution

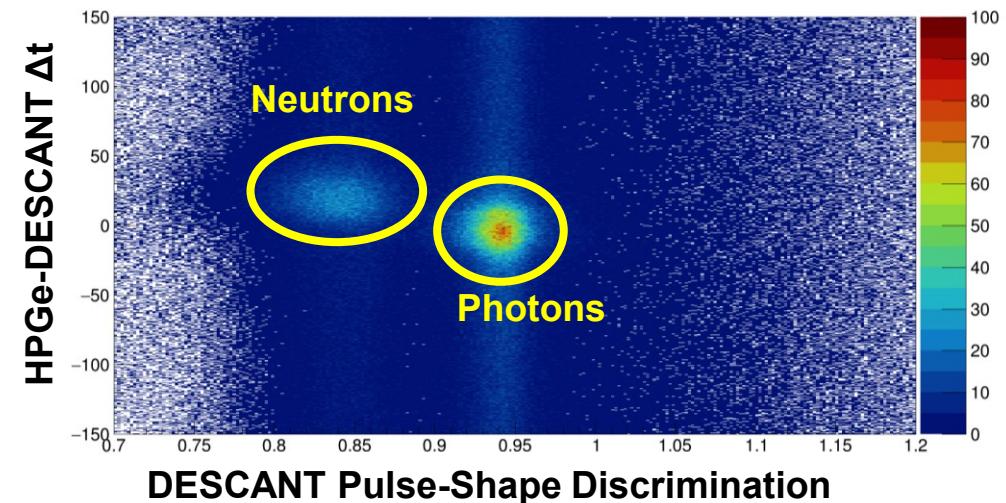
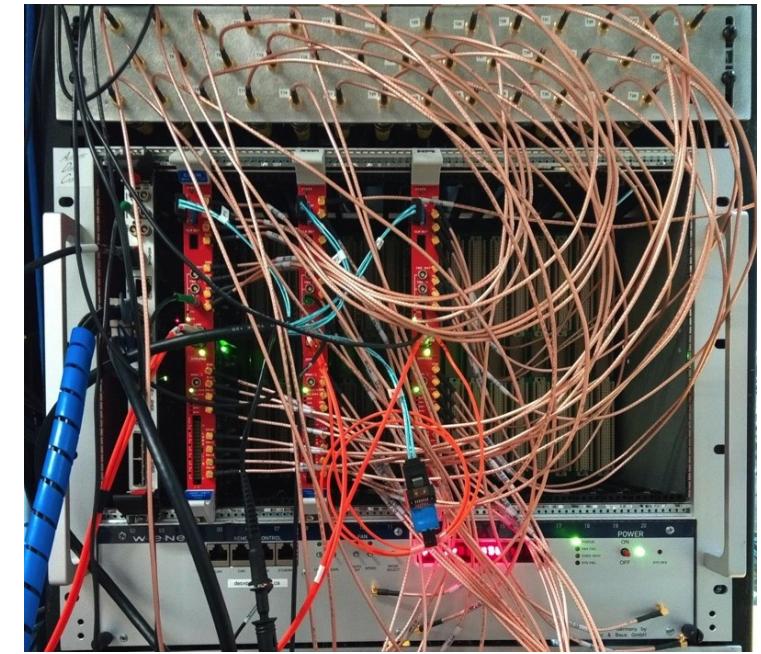
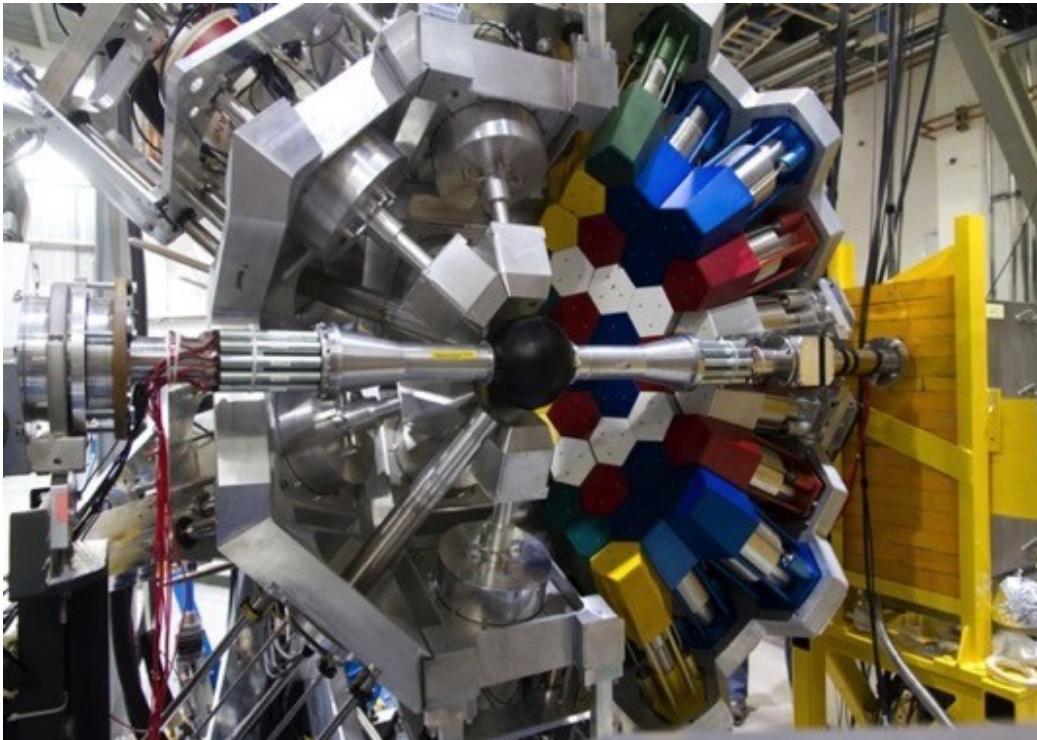


BGO shield for each  $\text{LaBr}_3(\text{Ce})$



# GRiffin+DESCANT

- 70 element array of deuterated scintillator for neutron detection covering  $\sim 1\pi$  solid angle, (50cm flight path).
- Enables beta-gamma-ICE-neutron spectroscopy
- Five CAEN VX1730, 500MHz, 14-bit digitizers.
- Neutron-gamma discrimination from pulse shape and TOF
- GRIFFIN and DESCANT read out separately and events combined offline using timestamps. Used in S1602 beamtime in Aug 2019.



# GRiffin DAQ System

A.B. Garnsworthy *et al.*, NIM A 853, 85 (2017).

Custom Digital Electronics Modules designed and built by TRIUMF and Université de Montréal

## Programmable Logic Pulse Generator

32 Channels  
NIM or TTL



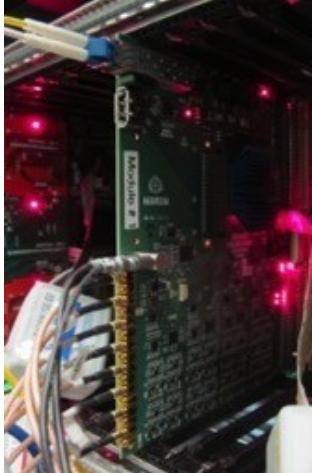
## Clock Distribution Module

10MHz precision  
Clock  
Low-jitter fan-out  
to all modules



## GRIF-16 Module

16 chans  
100MHz,  
14bit



## Primary and secondary Collector Modules

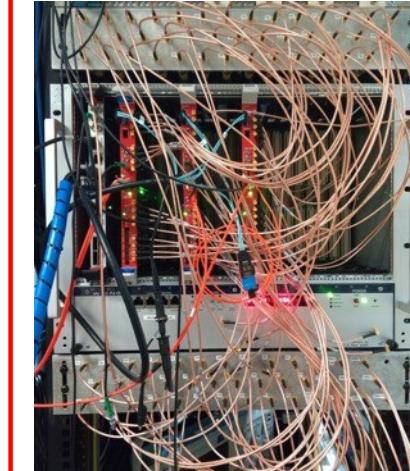
- 625MB/s link to each digitizer
- 1.25Gb/s link to data storage.



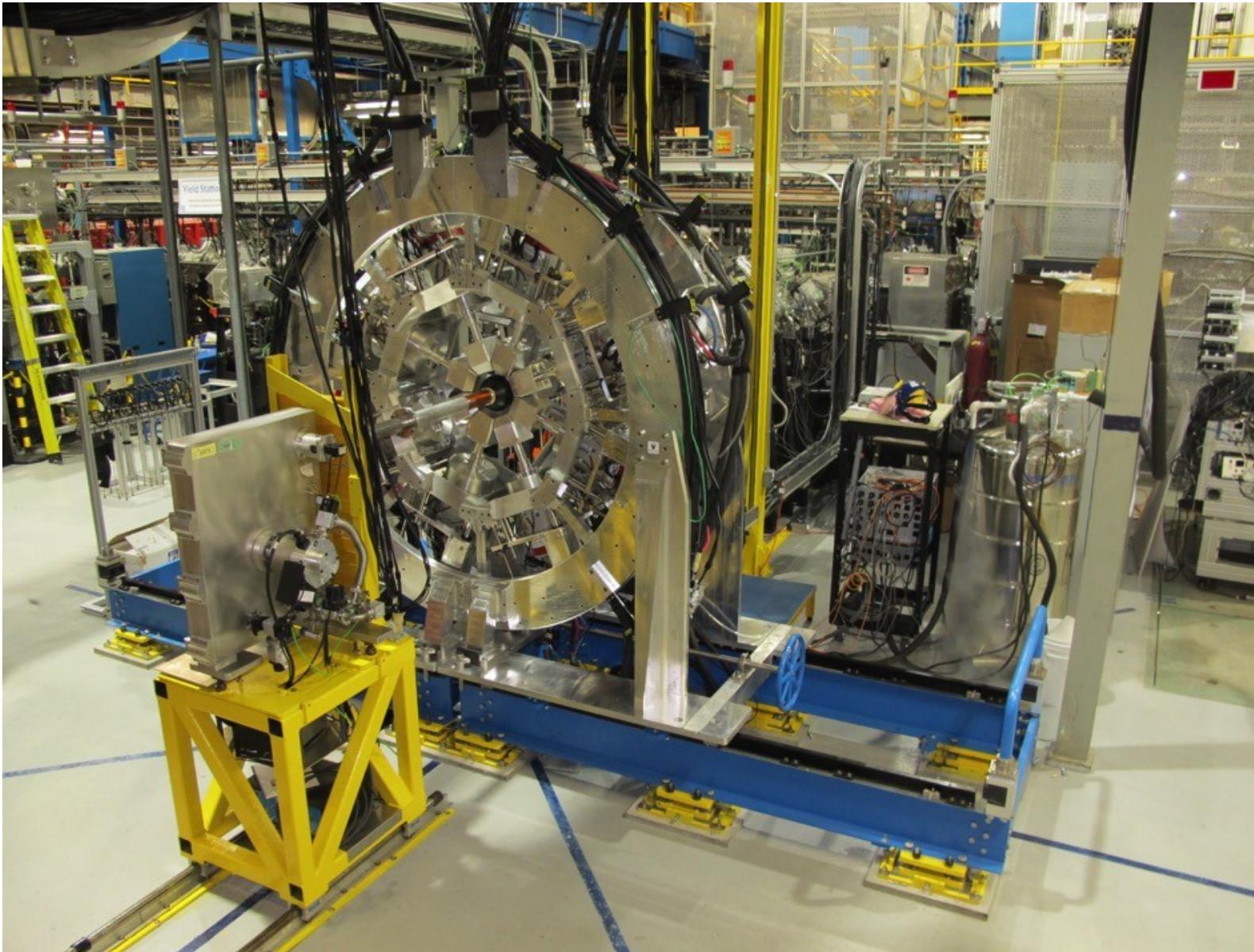
**High data through-put:**  
*50kHz per crystal, >300MB/s total*  
**For ultra-high-statistics studies**

**High accountability:**  
*Deadtime, pile-up, event tracing*  
**For precision measurements**

CAEN 500MHz,  
14 bit digitizers  
used for  
DESCANT.



# The GRIFFIN Spectrometer for precision decay studies at ISAC



Technical publications:

“Characteristics of GRIFFIN high-purity germanium clover detectors”,  
U. Rizwan, *et al.*, NIM A 820, 126 (2016).  
arXiv:1711.05287

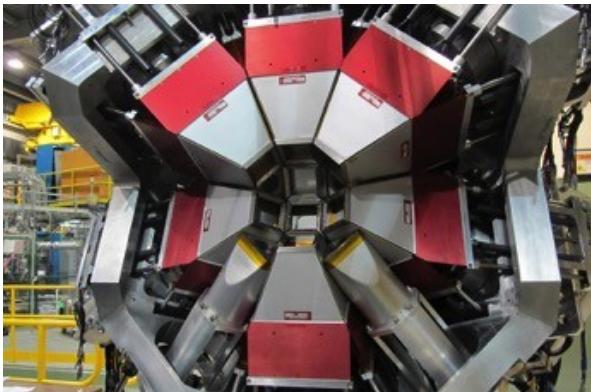
“The GRIFFIN data acquisition system”,  
A.B. Garnsworthy *et al.*, NIM A 853, 85 (2017).  
arXiv:1711.06236

“The GRIFFIN Facility for Decay-Spectroscopy Studies at TRIUMF-ISAC”,  
A.B. Garnsworthy *et al.*, NIM A 918, 9 (2019).  
arXiv:1809.07183

“ $\gamma\gamma$  angular correlation analysis techniques with the GRIFFIN spectrometer”,  
J.K. Smith *et al.*, NIM A 922, 47 (2019).  
arXiv:1807.07570

[griffin.triunf.ca](http://griffin.triunf.ca)

# The GRIFFIN Spectrometer for precision decay studies at ISAC

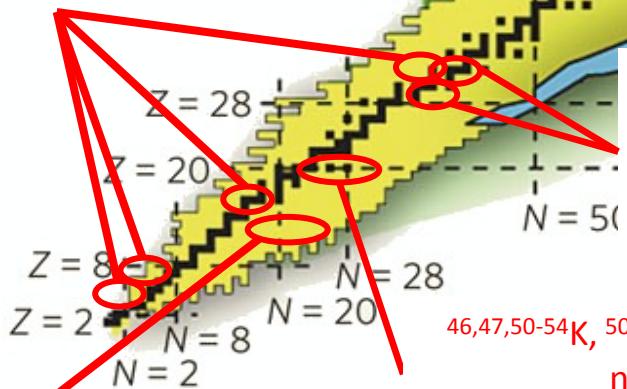


GRIFFIN is a powerful decay spectrometer for nuclear structure, astrophysics and fundamental interaction studies.

$^{160-166}\text{Eu}$ ,  $^{156,158,160,162,166}\text{Tm}$ :  
Development of collectivity in rare-earth region

$^{118}\text{In}$ : Intruder states at closed shells  
K. Ortner *et al.*, PRC 102, 024323 (2020).

$^{10}\text{C}$ ,  $^{14}\text{O}$ ,  $^{22}\text{Mg}$ ,  $^{62}\text{Ga}$ : Superallowed Fermi beta decays  
A.D. MacLean *et al.*, PRC 102, 054325 (2020).  
M.R. Dunlop *et al.*, PRC 96, 045502 (2017).



$^{31,32}\text{Na}$ ,  $^{33-35}\text{Mg}$ ,  $^{34}\text{Al}$ :  
Island of inversion

$^{46,47,50-54}\text{K}$ ,  $^{50}\text{Ca}$ : Single-particle and pair states near doubly-magic  $^{48}\text{Ca}$   
J.K. Smith *et al.*, PRC 102, 054314 (2020).  
J. Pore *et al.*, PRC 100, 054327 (2019).  
A.B. Garnsworthy *et al.*, PRC 96, 044329 (2017).

$^{188-200}\text{TI}$ : Development of collectivity in Hg isotopes  
B. Olaizola *et al.*, PRC 100, 024301 (2019).

$^{228,230}\text{Fr}$ : Probing Octupole deformation and collectivity in Radium isotopes.

$^{142-152}\text{La}$ : Octupole collectivity and shape coexistence in Ce isotopes

$^{145,146}\text{Cs}$ :  $\beta$ -delay neutron measurements with DESCANT, fast-timing with  $\text{LaBr}_3$

$^{128-132}\text{Cd}$ ,  $^{129-133}\text{In}$ :  
Nuclear structure and r-process nucleosynthesis at the N=82 shell closure  
F.H. Garcia *et al.*, Phys. Rev. C 103, 024310 (2021).  
Y. Saito *et al.*, PRC 102, 024337 (2020).  
K. Whitmore *et al.*, PRC 102, 024327 (2020).  
R. Dunlop *et al.*, PRC 99, 045805 (2019).  
R. Dunlop *et al.*, PRC 93, 062801(R) (2016).

## Technical and Overview Publications

- J.K. Smith *et al.*, NIM A 922, 47 (2019).
- A.B. Garnsworthy *et al.*, NIM A 918, 9 (2019).
- A.B. Garnsworthy *et al.*, NIM A 853, 85 (2017).
- U. Rizwan *et al.*, NIM A 820, 126 (2016).
- A.B. Garnsworthy, Acta Phys. Pol. B, 47, 713 (2016).
- C.E. Svensson and A.B. Garnsworthy, Hyp. Int. 225, 127 (2014).

# Superallowed Fermi $\beta$ Decay

$$ft = \frac{K}{|M_{fi}|^2 g^2}$$

phase space (Q-value) →  $ft$  =

half-life, branching ratio →  $|M_{fi}|^2 g^2$

K → constants  
Weak coupling strength matrix element

For the special case of  $0^+ \rightarrow 0^+$  (pure Fermi)  $\beta$  decays between isobaric analogue states (superallowed) the matrix element is that of an isospin ladder operator:

$$|M_{fi}|^2 = (T - T_z)(T + T_z + 1) = 2 \quad (\text{for } T=1)$$

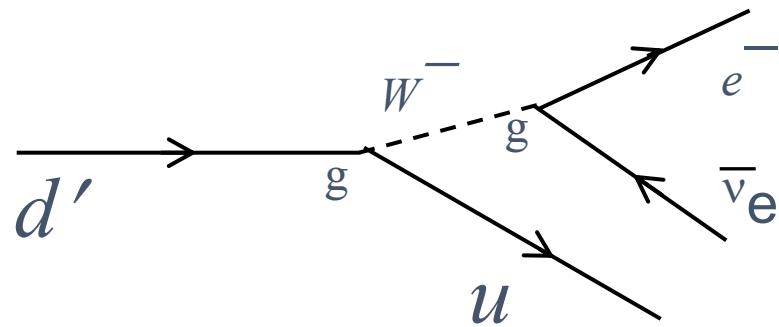
Strategy: Measure superallowed ft-values, deduce  $G_V$  and  $V_{ud}$ :

Vector coupling constant

$$ft = \frac{K}{2 G_V^2} \quad |V_{ud}| = G_V / G_F \leftarrow \text{Fermi coupling constant}$$

# The Standard Model of particle physics

The CKM matrix plays a central role in the Standard Model



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$|d'\rangle = V_{ud}|d\rangle + V_{us}|s\rangle + V_{ub}|b\rangle$$

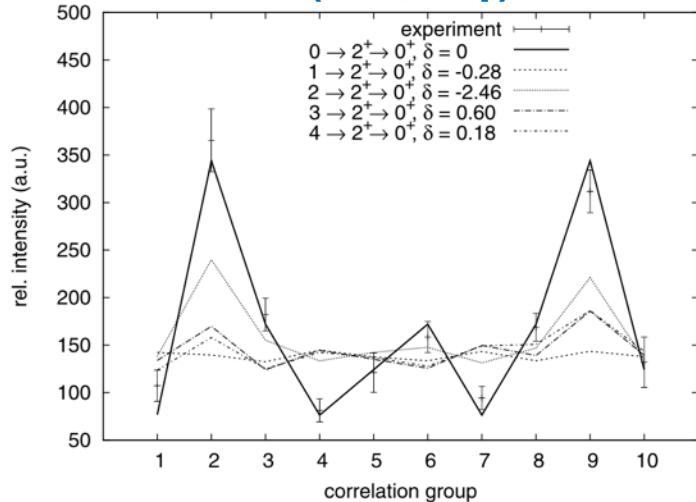
In the Standard Model the CKM matrix describes a unitary transformation:

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$

The first row of the CKM matrix provides the most demanding experimental test of the unitarity condition.

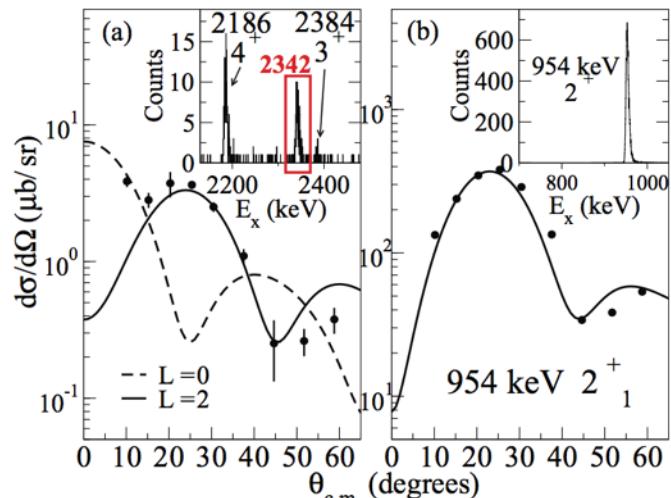
# A study of the $^{64}\text{Zn}(p,t)^{62}\text{Zn}$ reaction disagrees with previous transfer reaction measurements on the spin of the 2.342 keV level in $^{62}\text{Zn}$

$^{61}\text{Ni}(\text{He},2\text{ny})$



M. Albers et al., Nuc. Phys. 847, 180 (2010).

K. G. Leach et al., Phys. Rev. C 88, 031306(R) (2013).

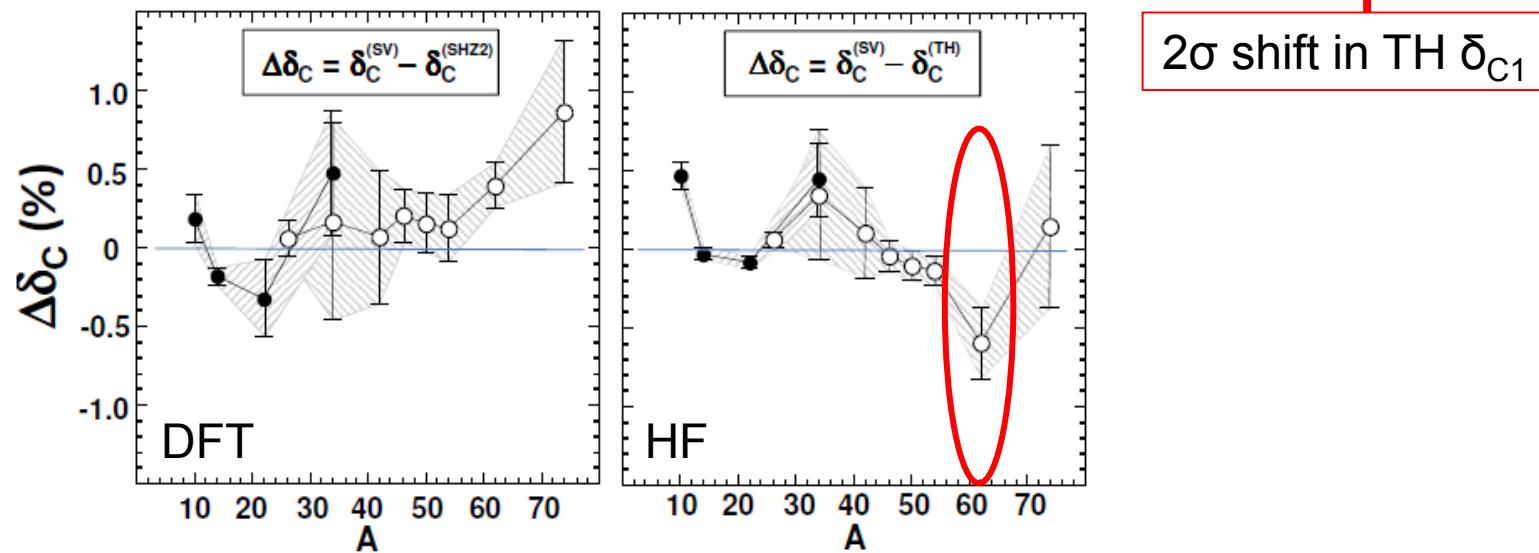


K. G. LEACH et al.

PHYSICAL REVIEW C 88, 031306(R) (2013)

TABLE II. A comparison of the unscaled and scaled isospin-mixing correction terms for  $^{62}\text{Zn}$ , using both the previous  $0_2^+$  excitation energy from Ref. [27] and the value presented here. The result of the new energy scaling lowers the  $\delta_{C1}$  central value by nearly a factor of two. The adopted values in each case are shown in bold and result from the average of the MSDI3 and GXPF1 calculations. The uncertainties used for the adopted values are described further in the text.

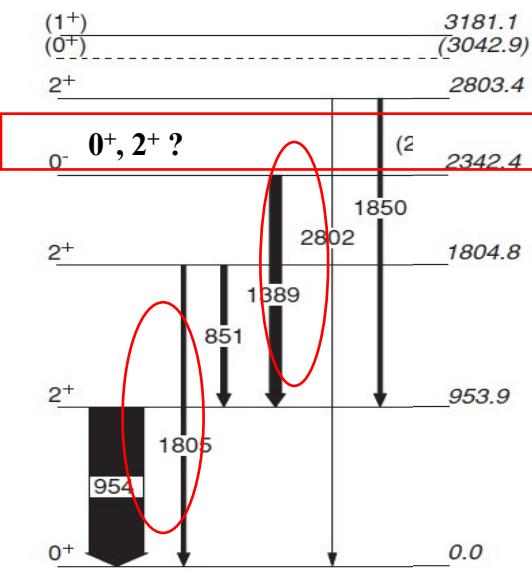
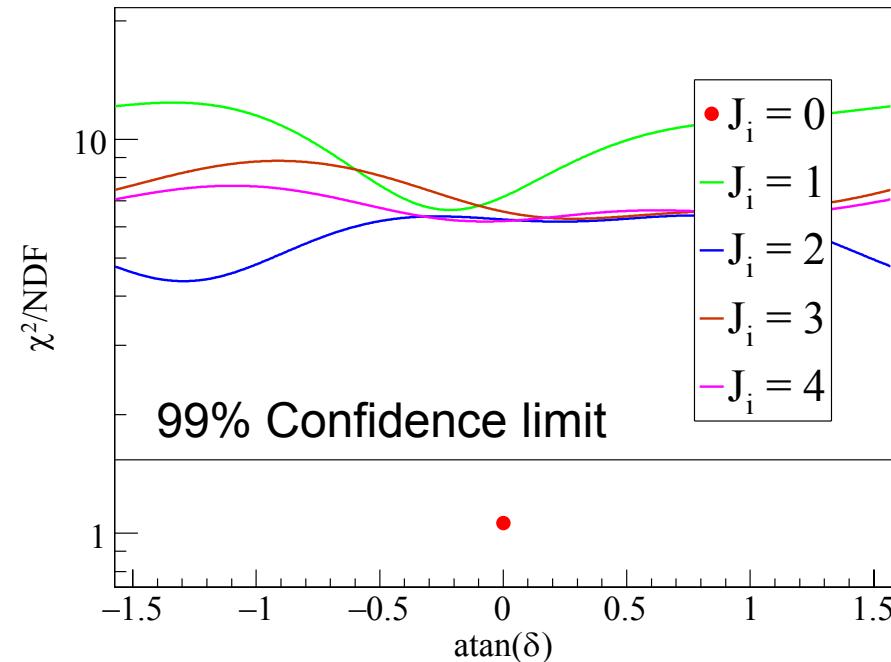
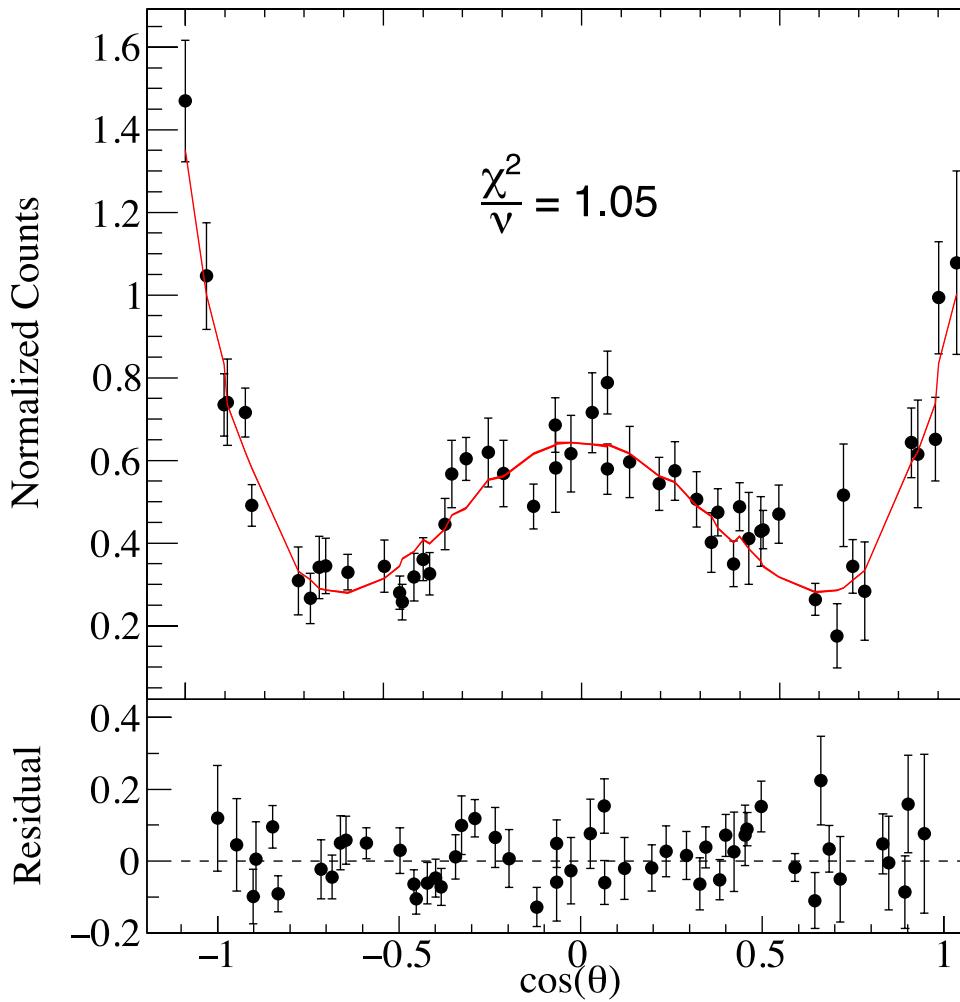
Interaction	Shell model	Unscaled		Ref. [27]	Previous scaling		This work	New scaling	
		$E_x(0_2^+)$ (MeV)	$\delta_{C1}^1$ (%)		$E_x(0_2^+)$ (MeV)	$\delta_{C1}^1$ (%)		$E_x(0_2^+)$ (MeV)	$\delta_{C1}^1$ (%)
MSDI3		2.263	0.089	0.350	2.342	0.084	0.329	3.045	0.049
GXPF1		2.320	0.160	0.221		0.159	0.219		0.093
Adopted value		<b>0.120(40)</b>		<b>0.275(55)</b>		<b>0.070(35)</b>		<b>0.160(70)</b>	



W. Satula et al., Phys. Rev. C 86, 054316 (2012)

# GRiffin result is definitive

A. MacLean, University of Guelph



- Definitive measurement with GRiffin assigns  $0^+$  to the 2342keV state in  $^{62}\text{Zn}$ .
- Important nuclear data for refining the isospin-symmetry-breaking corrections

A.D. MacLean *et al.*, PRC 102, 054325 (2020).

# GRiffin studies around doubly-magic $^{132}\text{Sn}$

Two beamtime periods with GRIFFIN

2 publications, 4 in preparation

- 2 PhD thesis, 1 Masters thesis
- 1 PhD thesis in progress

"Beta-decay and beta-delayed neutron decay of the  $N=82$  nucleus  $^{131}\text{In}$ ",

R. Dunlop et al., PRC 99, 045805 (2019).

$^{129}\text{In}$  July 2016, ~600pps, 2.7hrs

$^{131}\text{In}$  July 2016, ~600pps, 2hrs

$^{132}\text{In}$  July 2016, ~70pps, 63hrs

$^{133}\text{In}$  July 2016, ~1pps, 18hrs

Led by Corina Andreoiu

F. Garcia, PhD thesis in progress (SFU)

K. Whitmore et al., PRC 102, 024327 (2020).

F.H. Garcia et al., Phys.Rev.C103,024310 (2021)

$^{128}\text{Cd}$  Aug 2015, ~1000pps, 6.5hrs

$^{129}\text{Cd}$  Aug 2015, ~150pps, 13hrs

$^{130}\text{Cd}$  Aug 2015, ~25pps, 38hrs

$^{131}\text{Cd}$  Aug 2015, ~1pps, 32hrs

Led by Iris Dillmann and Reiner Kruecken

N.Bernier, PhD thesis (2018) UBC

Y. Saito, MSc thesis (2018) UBC

R. Dunlop, PhD thesis (2019) Uni. Of Guelph

Y. Saito et al., PRC 102, 024337 (2020)

1 manuscripts in preparation

Te130 7.9E20 y 0+	Te131 25.0 m 3/2+ *	Te132 3.204 d 0+	Te133 12.5 m (3/2+)*	Te134 41.8 m 0+	Te135 19.0 s (7/2-)	Te136 17.5 s 0+	Te137 2.49 s (7/2-)
$\beta^-$ 33.80	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-n$	$\beta^-n$
Sb129 4.40 h 7/2+ *	Sb130 39.5 m (8-)*	Sb131 23.03 m (7/2+)*	Sb132 2.79 m (4+)*	Sb133 2.5 m (7/2+)*	Sb134 0.78 s (0-)*	Sb135 1.71 s (7/2+)*	Sb136 0.82 s $\beta^-n, \beta^-2n, ...$
$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-n$	$\beta^-n, \beta^-2n, ...$
Sn128 59.07 m 0+ *	Sn129 2.23 m (3/2+)*	Sn130 3.72 m 0+ *	Sn131 56.0 s (3/2+)*	Sn132 39.7 s 0+ *	Sn133 1.45 s (7/2-)	Sn134 1.12 s 0+ *	Sn135
$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-n$	$\beta^-n$	
In127 1.09 s (9/2+)*	In128 0.84 s (3+)*	In129 0.61 s (9/2+)*	In130 0.32 s (1-)*	In131 0.282 s (9/2+)*	In132 0.201 s (7-)*	In133 180 ms (9/2+)*	In134 138 ms $\beta^-n$
$\beta^-n$	$\beta^-n$	$\beta^-n$	$\beta^-n$	$\beta^-n$	$\beta^-n$	$\beta^-n$	$\beta^-n$
Cd126 0.506 s 0+ *	Cd127 0.37 s (3/2+)*	Cd128 0.34 s 0+ *	Cd129 0.27 s (3/2+)*	Cd130 0.20 s 0+ *			
$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-n$			
Ag125 166 ms	Ag126 107 ms	Ag127 109 ms					
$\beta^-$	$\beta^-$	$\beta^-$					

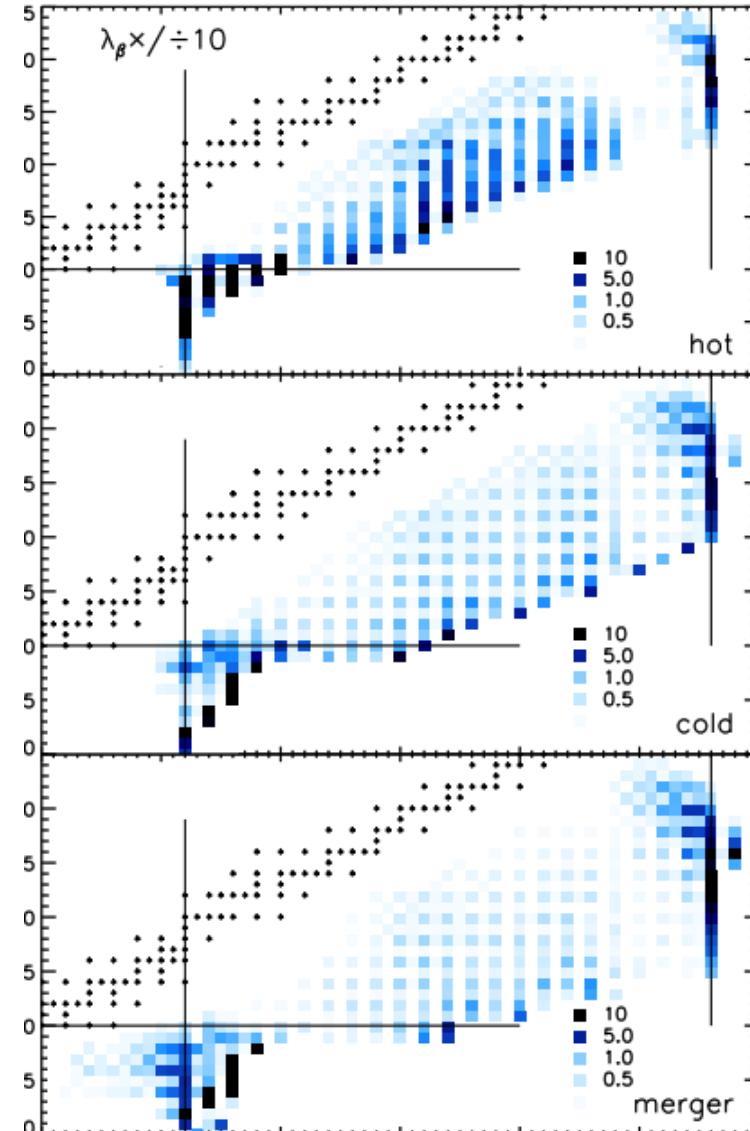
78

80

84

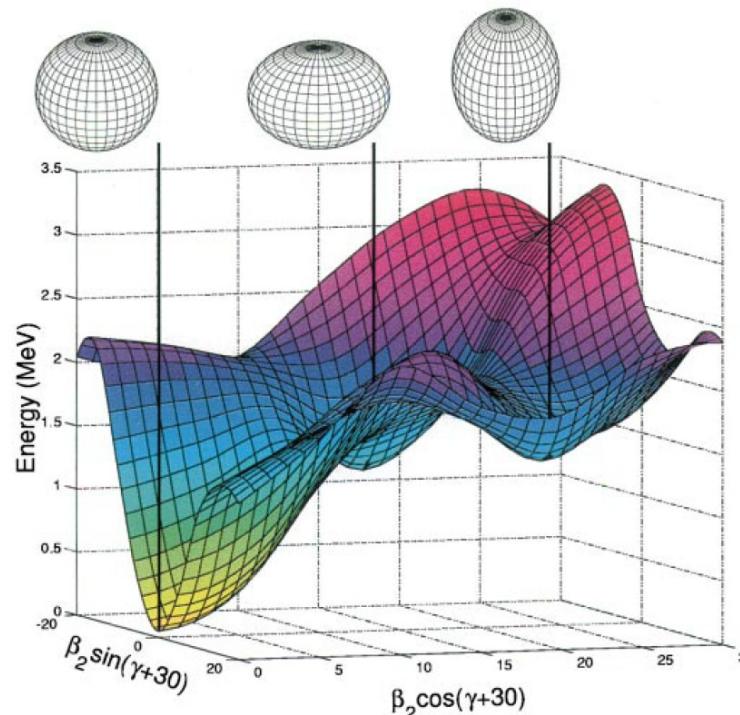
"Half-Lives of Neutron-Rich  $^{128-130}\text{Cd}$ ",  
R. Dunlop et al., PRC 93, 062801(R) (2016).

Key nuclear data for r-process

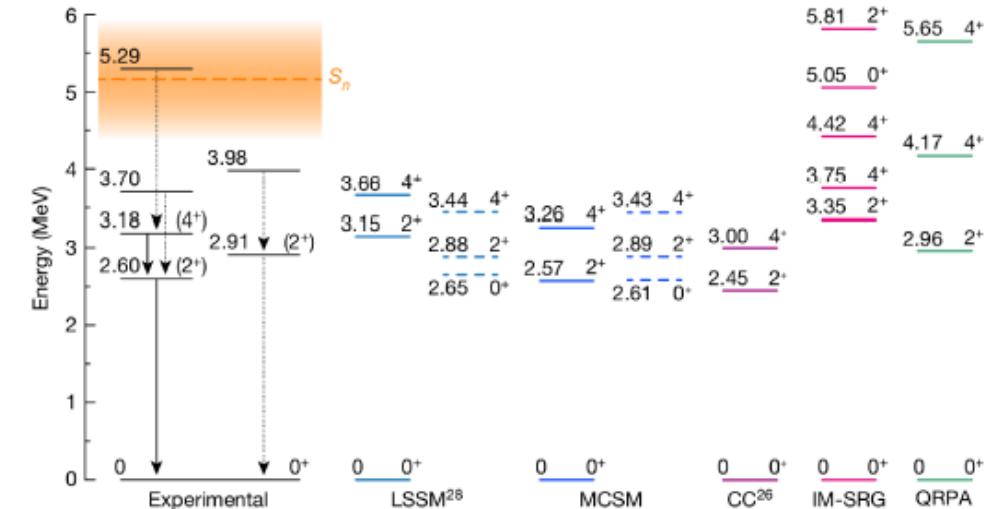


M. Mumpower et al., Prog. Part. Nucl. Phys. 86, 86 (2016)

# Shape Coexistence in $^{80}\text{Ge}$



A recent experiment probed the structure of doubly magic  $^{78}\text{Ni}$ .



- $^{186}\text{Pb}$  with three low-lying  $0^+$  states
  - Z=82 closed shell, N=104 mid-shell
  - Ground, oblate, prolate
  - 2p-2h and 4p-4h proton excitations out of Z=82 spherical closed shell into  $h_{9/2}$ , e.g.
  - Excitations interact with open neutron shell

Andreyev et al., Nature 405 (2000) 430

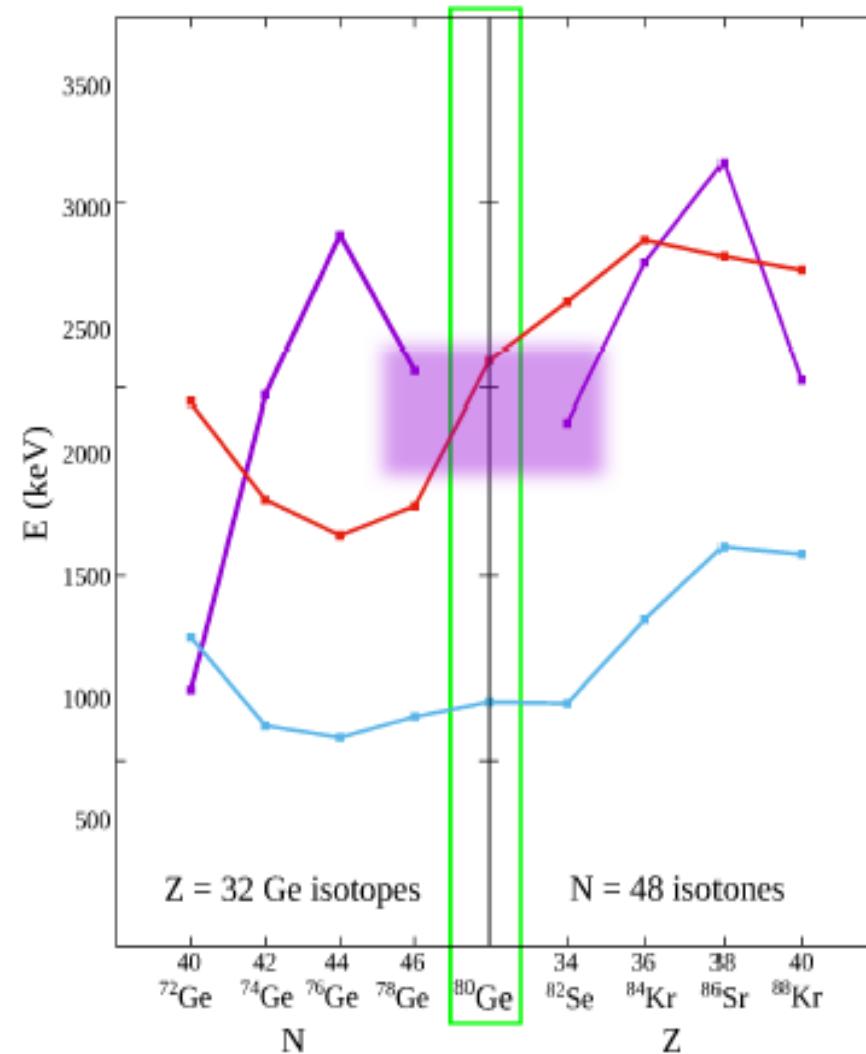
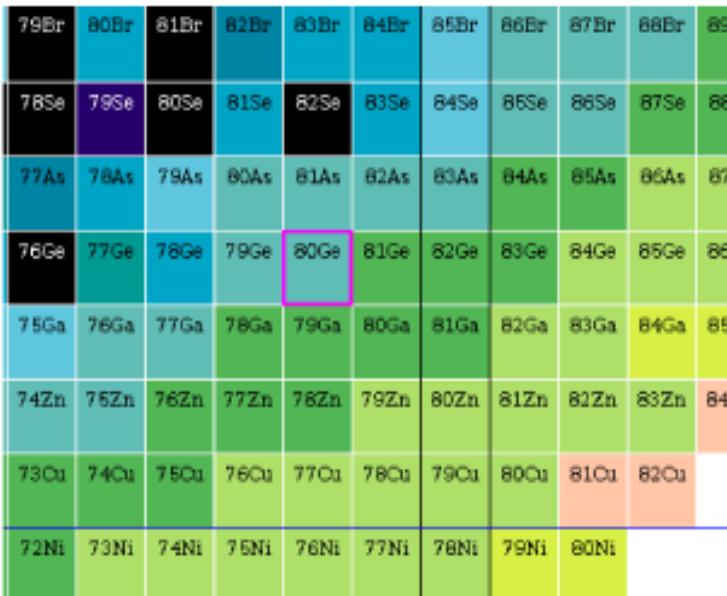
Duguet et al., PLB 559 (2003) 201

An excited  $2^+$  state was observed at only 0.31 MeV above the  $2^+_1$ , suggesting shape coexistence in this nucleus.

Taniuchi, R et al., Nature 569 (2019) 53

# Shape Coexistence in $^{80}\text{Ge}$

Nowacki *et al.*\* proposed  $^{78}\text{Ni}$  to be a portal to the fifth island of inversion.



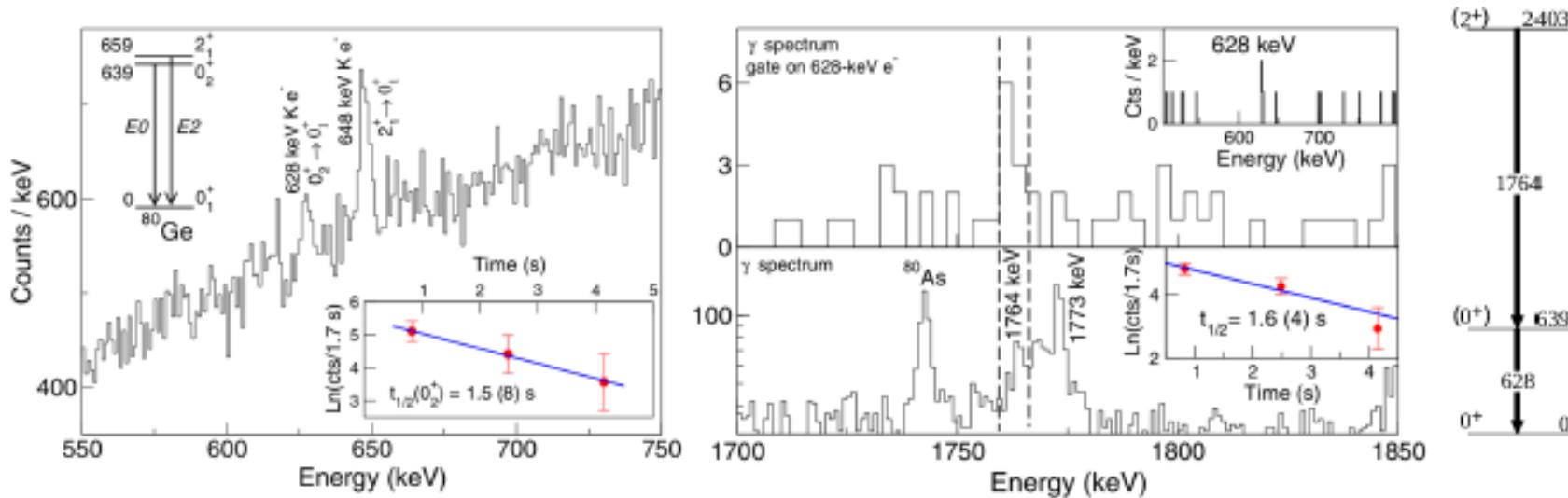
NNDC, Brookhaven National Laboratory

\*Nowacki, F., Poves, A., Caurier, E. and Bounthong, B., *PRL* 117, 272501 (2016)

# Shape Coexistence in $^{80}\text{Ge}$

An experiment at ALTO reported a new state  $0^+$  state in  $^{80}\text{Ge}$  at 639 keV, from observation of a conversion electron peak at 628 keV.

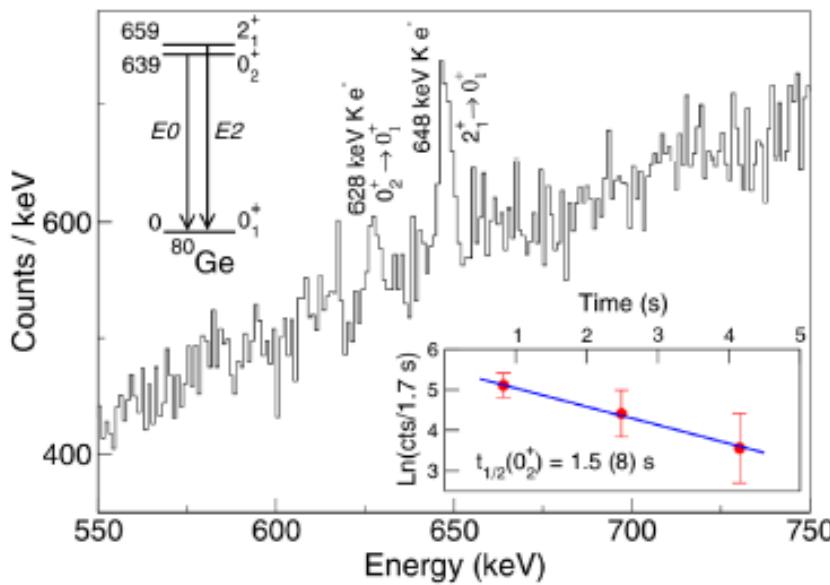
A coincidence was also observed between the 628-keV conversion electron and a 1764-keV  $\gamma$ -ray from a new state at 2403 keV.



The binding energy of the K-shell electron in  $^{80}\text{Ge}$  is 11 keV

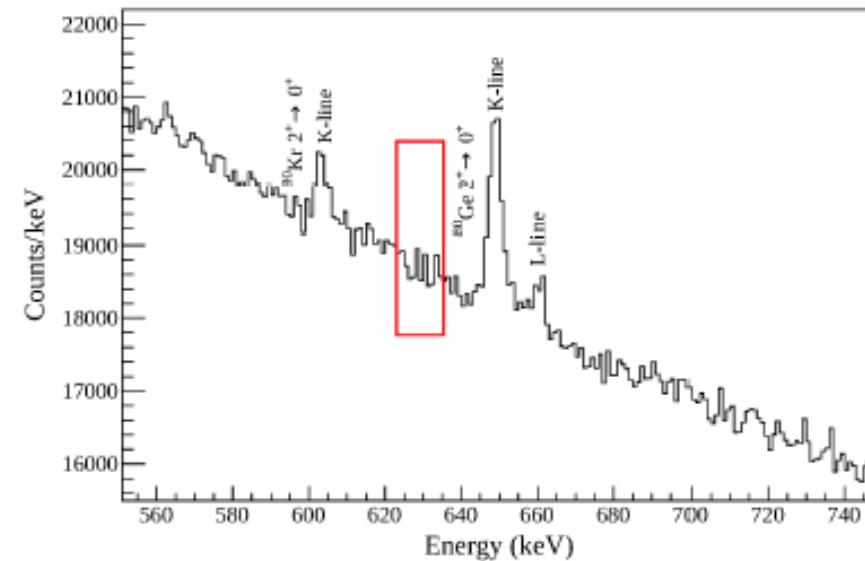
# Shape Coexistence in $^{80}\text{Ge}$

The GRIFFIN experiment used PACES, but did not detect the 628-keV conversion electron peak.



ALTO I<sup>628</sup>: ~0.08%

Gottardo, A. et al., PRL 116, 182501 (2016)  
Garcia, F. H. et al., PRL 125, 172501 (2020)

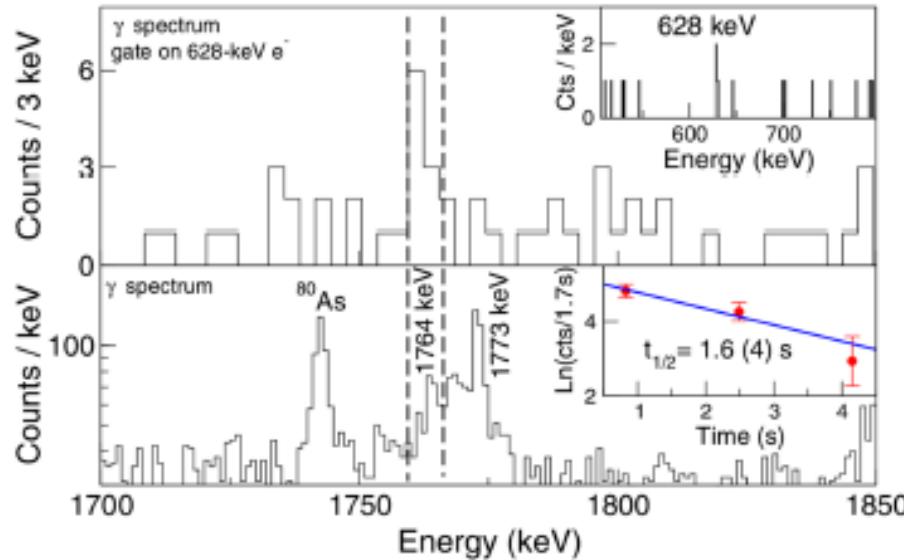


GRIFFIN 2 $\sigma$  limit: <0.02%

F.H. Garcia et al., PRL 125, 172501 (2020).

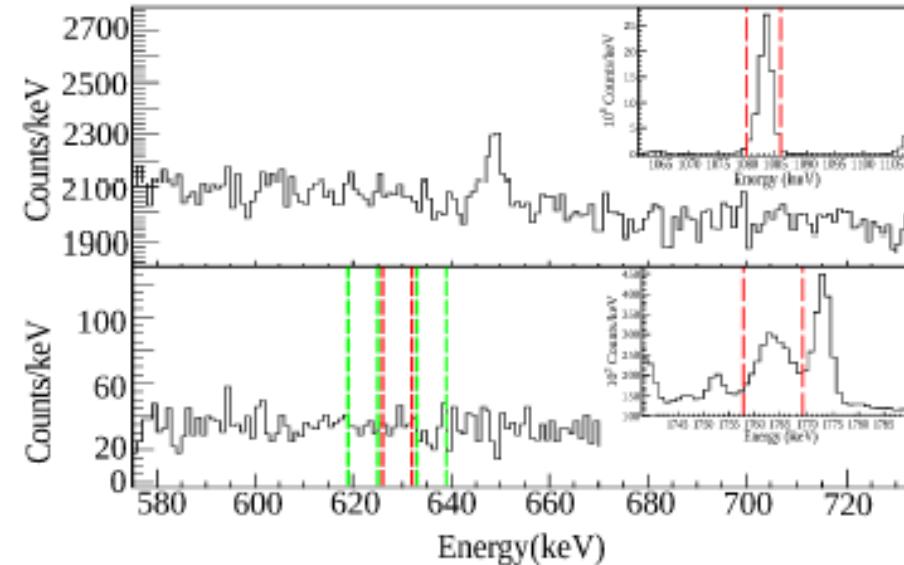
# Shape Coexistence in $^{80}\text{Ge}$

Detection limits were calculated to verify non-observation.



ALTO  $I_{1764}/I_{1772} : 0.3$

Gottardo, A. et al., PRL 116, 182501 (2016)  
Garcia, F. H. et al., PRL 125, 172501 (2020)



GRIFFIN  $I_{1764}/I_{1772} 2\sigma \text{ limit: } 0.003$

F.H. Garcia et al., PRL 125, 172501 (2020).

# Future developments and Physics opportunities

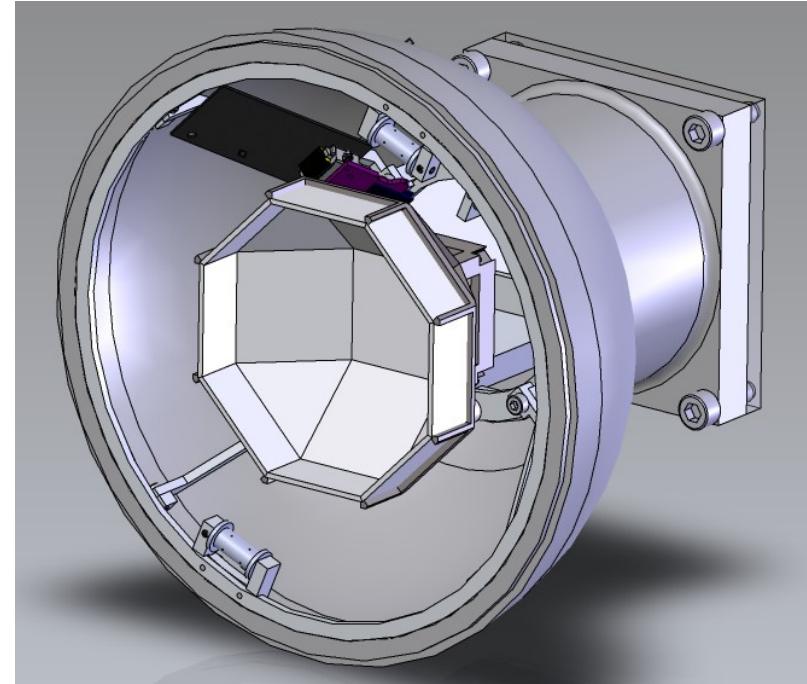
## Ancillary detector for Rare Isotope Event Selection (ARIES)

### A major upgrade of the SCEPTAR beta-tagging array for GRIFFIN

#### New ARIES beta-tagging array enables:

- Counting of high source activities ~20MBq with ~90% solid-angle coverage.
- Beta-gamma angular correlations with >50 unique angles.
- Beta-gamma fast coinc. timing (few ps) with LaBr<sub>3</sub>(Ce) detectors (x2 eff. increase over ZDS).
- Easy and economical replacement of detectors contaminated with long-lived activity.

Geometry optimized for GRIFFIN with 1 beta paddle for each HPGe crystal,  
+ 8 triangles + 4 downstream = (36 US)+(40 DS) = 76 total channels



- 1.5mm thick BC422Q ultra-fast plastic scintillator.
- Light read-out using SiPM sensors printed on flexible circuit board ~50µm thickness and held in place with a 3D-printed support structure will provide energy and fast-timing signal.
- Processing the GRIFFIN DAQ.



#### Physics opportunities

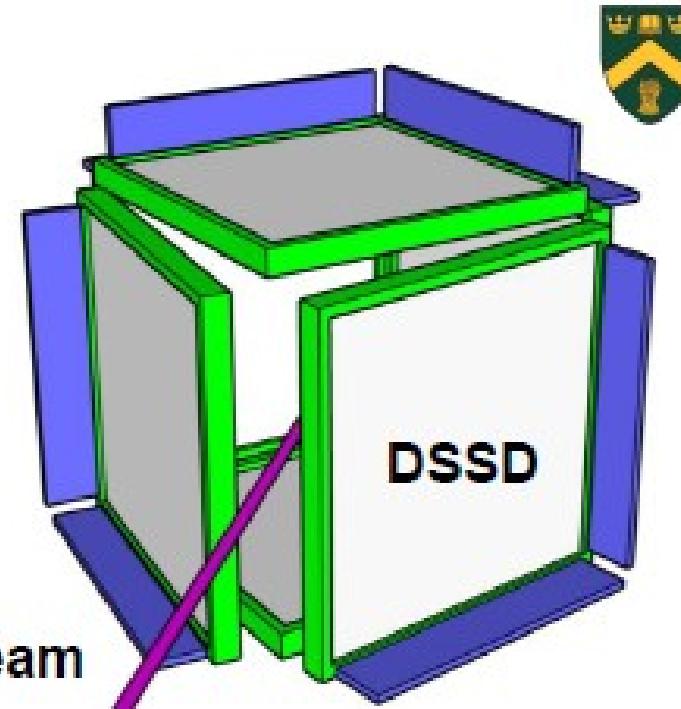
- Lifetime measurements
- β–γ angular correlations
- POLARIS: Spin polarized beams to GRIFFIN



# Future developments and Physics opportunities

## RCMP: Regina Cube for Multiple Particles

- Auxiliary detector for GRIFFIN
  - Charged particle detector
  - $\alpha$  decay and  $\beta$  delayed particles
  - Multiple particles ( $\beta^2 p$ ,  $\beta\alpha p$ , ...)
- 6 DSSD detectors (micron BB7)
  - Active area:  $64 \times 64 \text{ mm}^2$
  - $6 \times (32+32)$  strips = 384 channels
  - Thickness: 1mm (~12 MeV protons)
  - Resolution  $\leq 50 \text{ keV}$  (FWHM)
- Preliminary design study
  - Compatibility with GRIFFIN
  - Optimized physical geometry
  - Estimated overall efficiency
  - Quantified transparency to  $\gamma$  rays
  - Michael Hladun (Regina)\*



University of Regina

**DAEMON:**  
**Detector Array for Energy Measurements Of Neutrons**

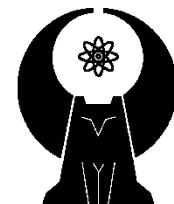
# Thank you!!!

Also many thanks for the plots slides or material to A.B. Garnsworthy, F.H. Garcia, A.D. MacLean, C.Andreoiu and G. Hackman

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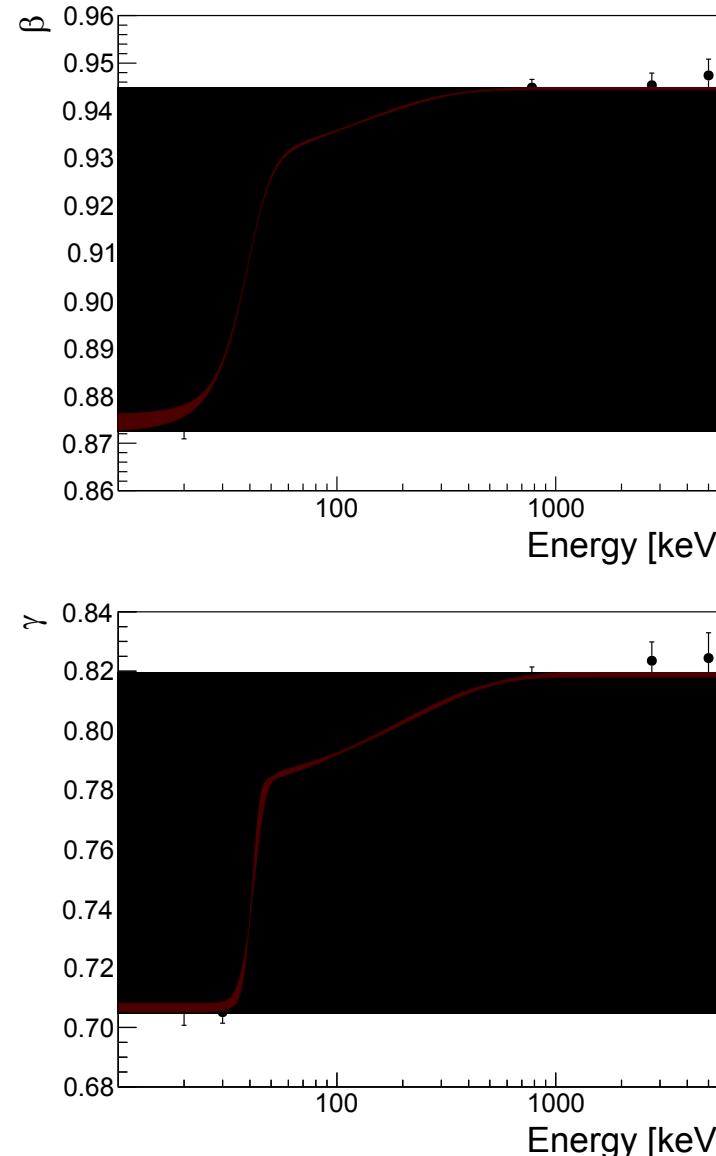
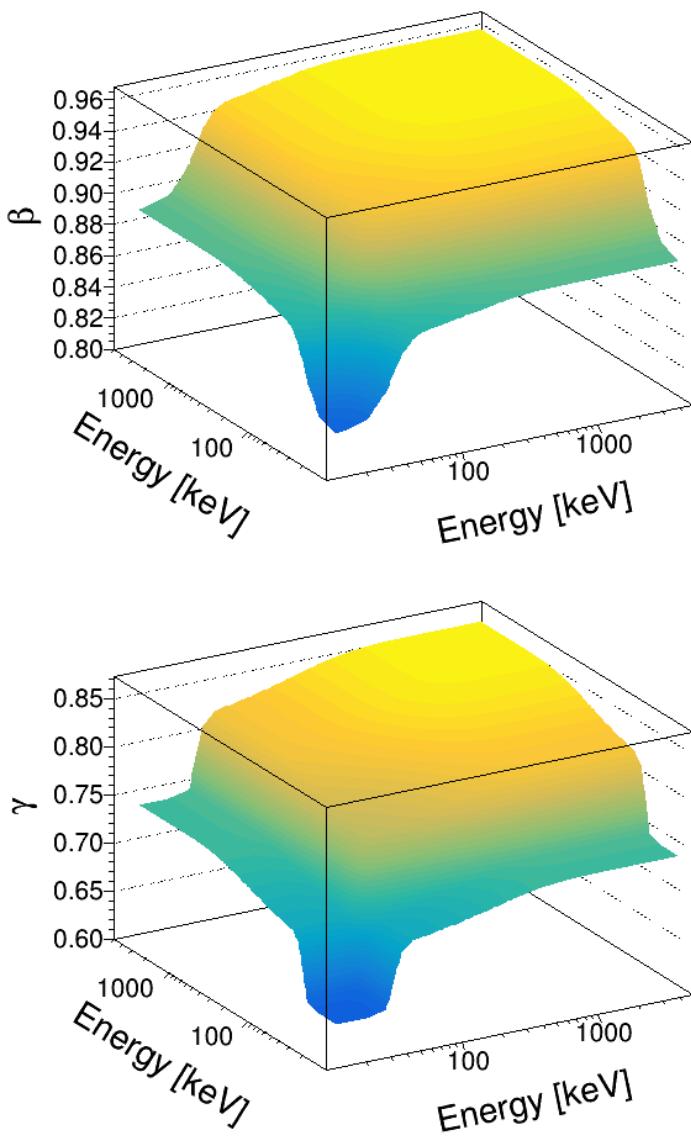
vvedia@triumf.ca

*Victoria Vedia TRIUMF Science week*



GRIFFIN

# Gamma-Gamma Angular Correlation Analysis



J.K. Smith, A.C. MacLean *et al.*  
NIM A 922, 47 (2019).  
<https://arxiv.org/abs/1807.07570>

Development of  $\gamma-\gamma$  angular correlation analysis techniques with GRIFFIN.

- Map the attenuation coefficients over the full  $\gamma-\gamma$  energy surface.

$$W(\theta) = A_{00}[1 + a_2 P_2(\cos \theta) + a_4 P_4(\cos \theta)]$$

where

$$a_i = A_{ii}/A_{00}.$$

$a_2 = \beta c_2$ , and  $a_4 = \gamma c_4$ ,  
where  $c$  is fitted coefficient, and  $a$  is true coefficient

$\beta$  and  $\gamma$  coefficients are available for the 110mm distance here:

<https://griffincollaboration.github.io/AngularCorrelationCoefficients/>