

Machine Learning Techniques for Water Cherenkov Event Reconstruction

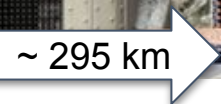
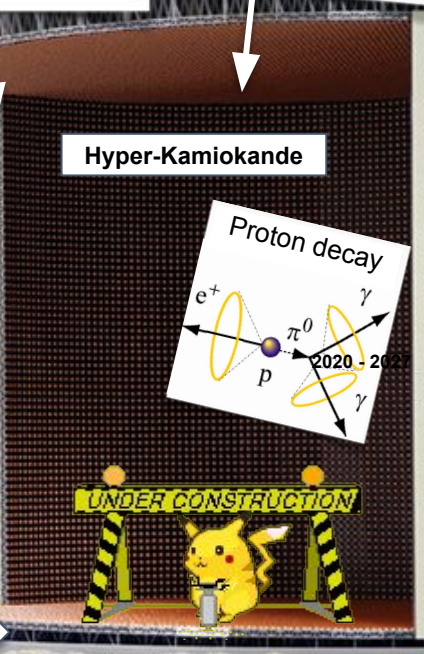
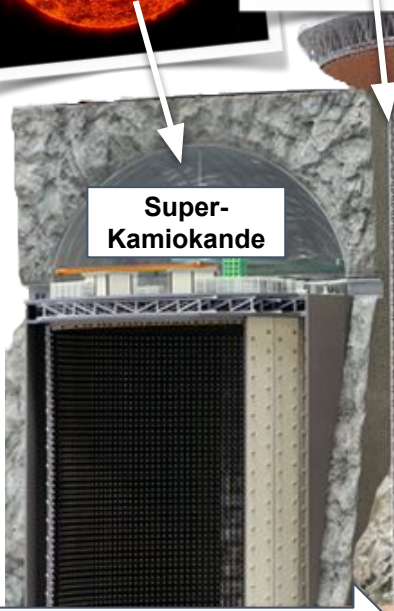
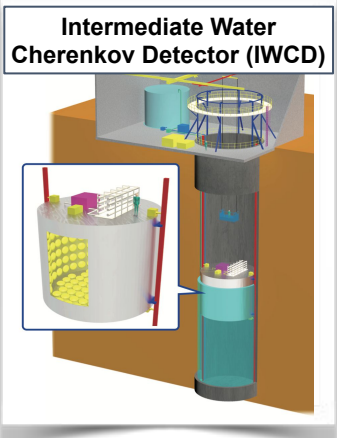
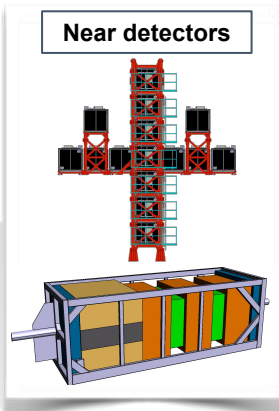
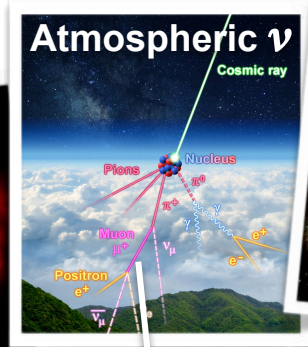
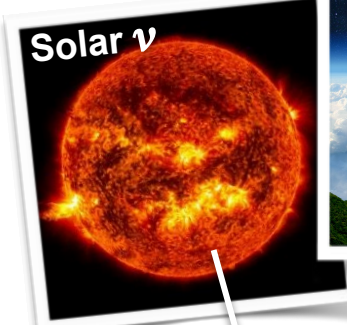
Nick Prouse & TRIUMF Hyper-Kamiokande group
TRIUMF Science Week, 19th July 2022

Water Cherenkov Neutrino Experiments

Current generation **Super-K** and **T2K** and next generation **Hyper-K** are world-leading neutrino experiments.

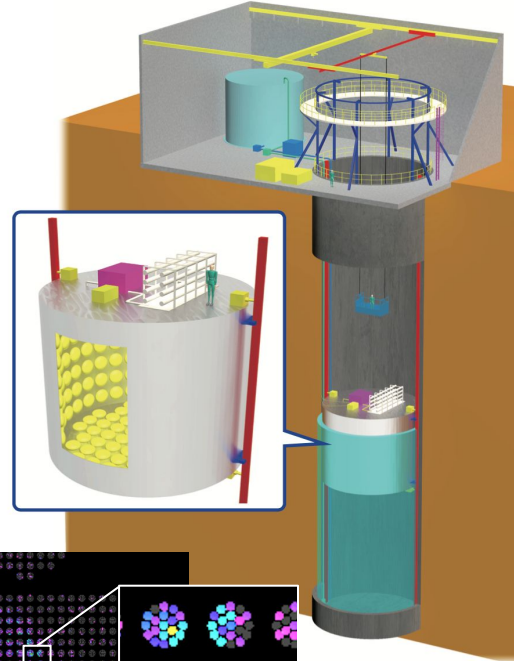
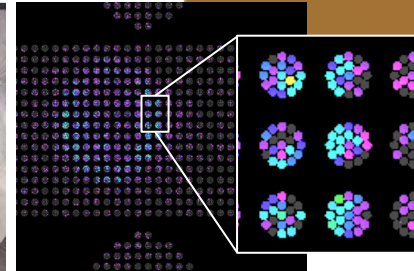
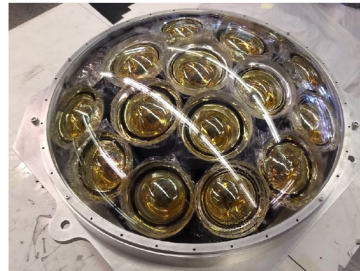
Broad & ambitious physics programmes covering many neutrino sources as well as proton decay measurements.

Water Cherenkov detector technology provides huge target mass with excellent particle ID and reconstruction capabilities.



The Intermediate Water Cherenkov Detector

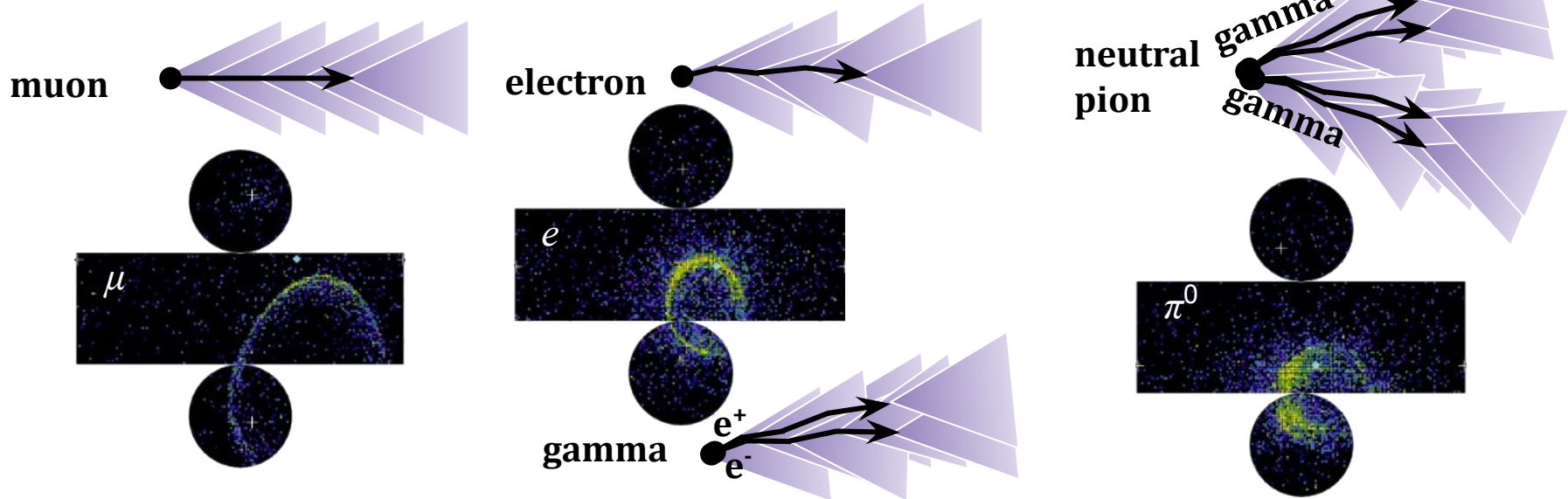
- Measures of flux and cross-section of mostly un-oscillated beam to reduce systematics at far detector
- Located ~ 1 km from ν beam source
- Moves vertically in ~ 50 m tall pit
 - spans range of angles off axis from ν beam for different ν energy spectra
- 6 m tall x 8 m diameter surrounded with ~ 500 multi-PMT modules (mPMTs)
 - 8 cm PMTs: Better position resolution
< 1 ns timing resolution
 - Additional directionality information
 - mPMTs will also be used for WCTE
 - Also in consideration for portion of far detector photo-coverage



Reconstruction in WC detectors

Classification: Particle type identification (PID)

- Different particles produce different types of rings



Regression: reconstructing particle's properties:

- Location and time of PMT hits allows triangulating position and direction
- Amount of charge observed at PMTs gives estimate of energy

Machine learning reconstruction for WC

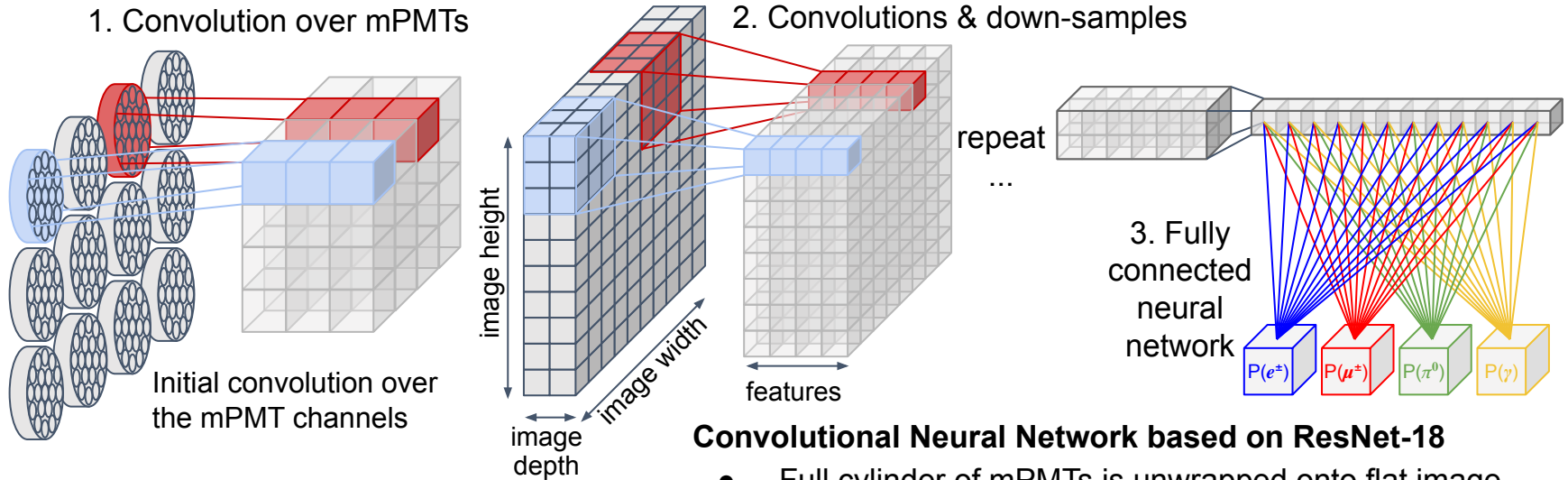
Limit of traditional maximum-likelihood reconstruction methods (fiTQun) is being reached

- Larger detector with more photosensors and smaller detector requiring greater precision
- Computation time is becoming a limiting factor

ML and deep neural networks have potential to push reconstruction further

- Very successful in areas of computer vision and image processing
- Potential to use all information without detector model approximations
- Very fast to run once neural networks have been trained
 - fiTQun on CPU: 1 event takes more than 1 minute
 - ML reconstruction on GPU: 100,000 events per minute

Deep network architectures



Convolutional Neural Network based on ResNet-18

- Full cylinder of mPMTs is unwrapped onto flat image
- One pixel per multi-PMT

Point Cloud Neural Network based on PointNet

- Applies to point-cloud of PMT hits in 3D space
- Uses 1x1 convolutions and learns transformations applied to points

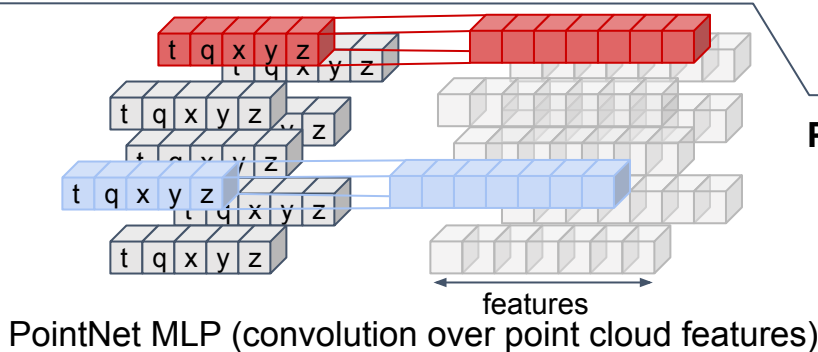
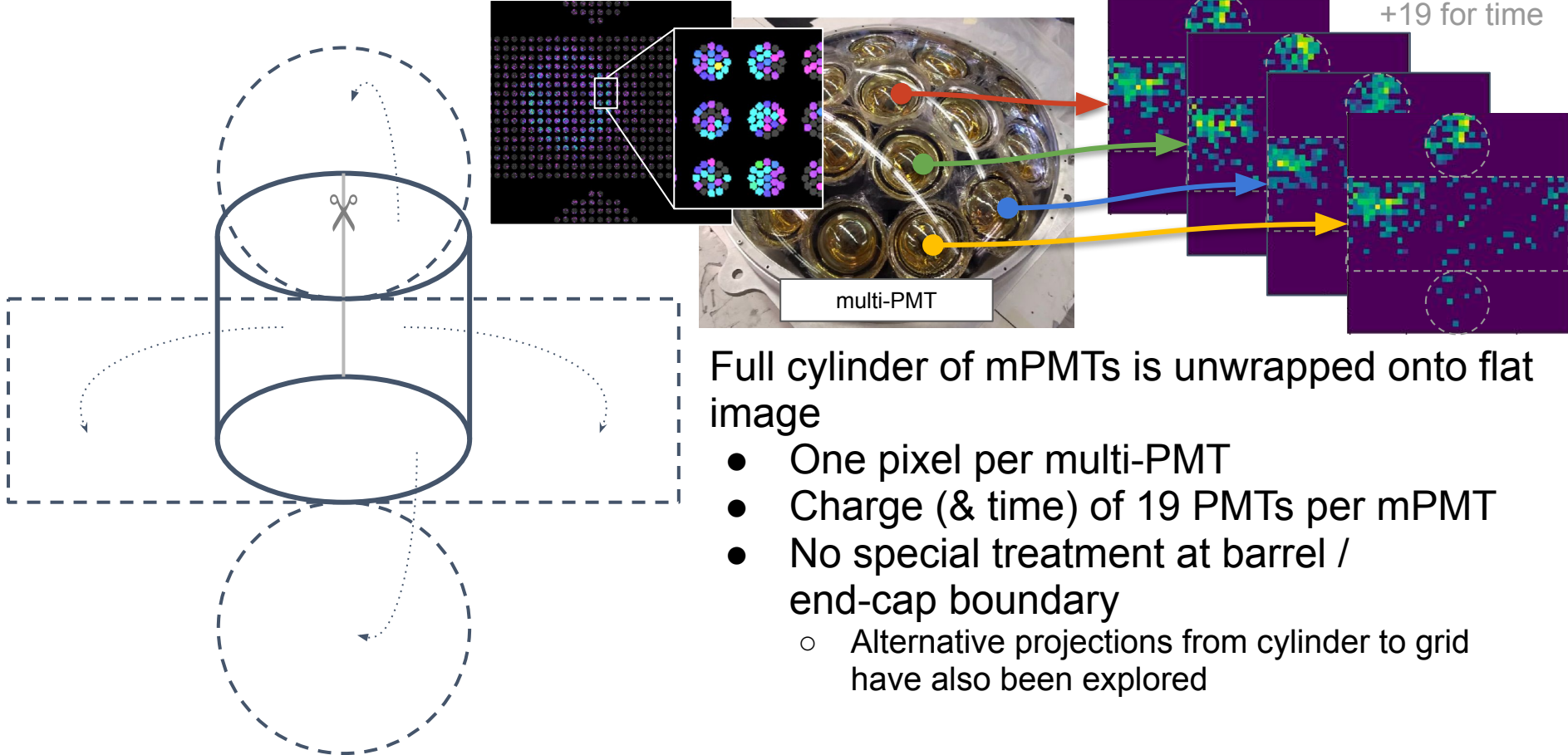


Image-like data for CNN

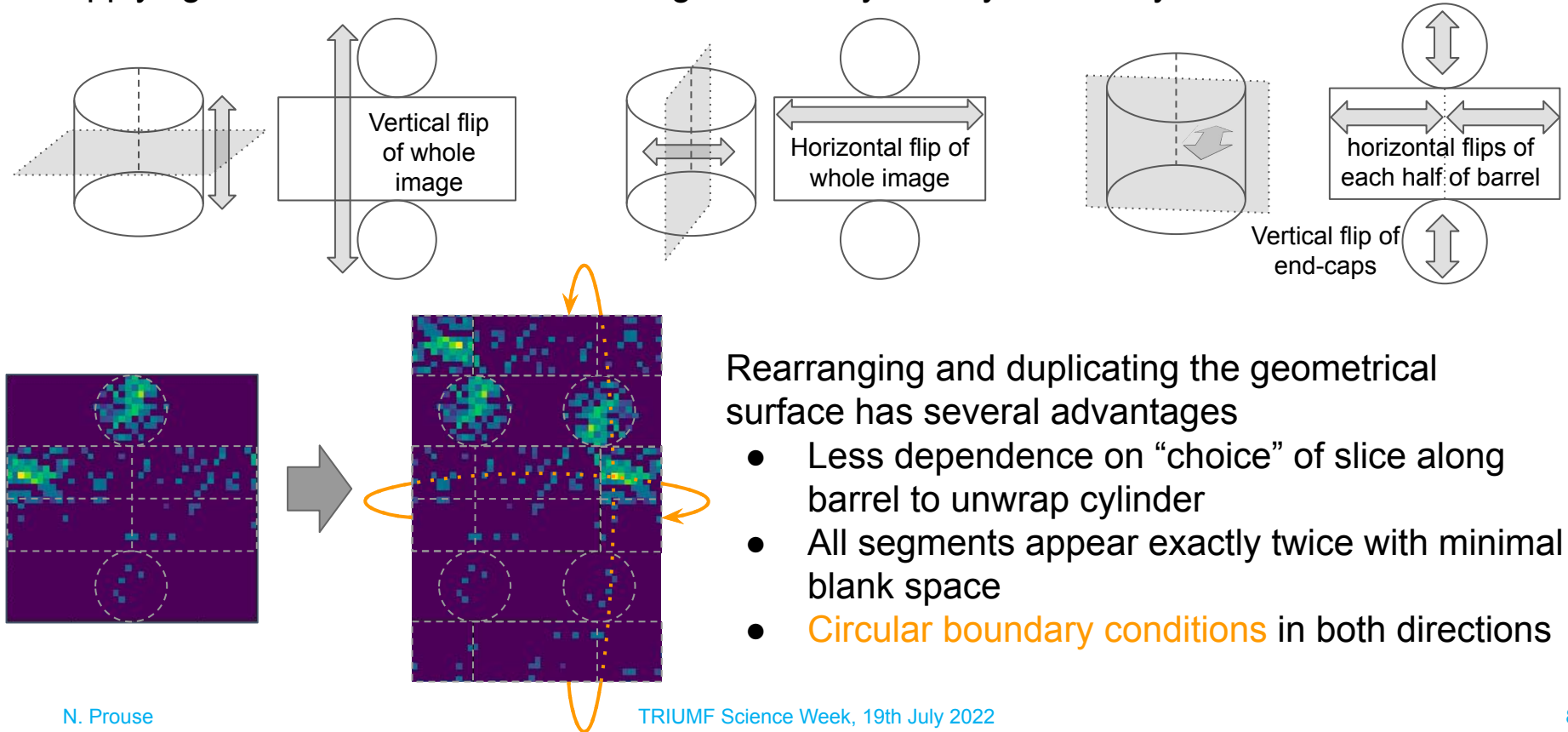


Full cylinder of mPMTs is unwrapped onto flat image

- One pixel per multi-PMT
- Charge (& time) of 19 PMTs per mPMT
- No special treatment at barrel / end-cap boundary
 - Alternative projections from cylinder to grid have also been explored

Data Transformations and Augmentation

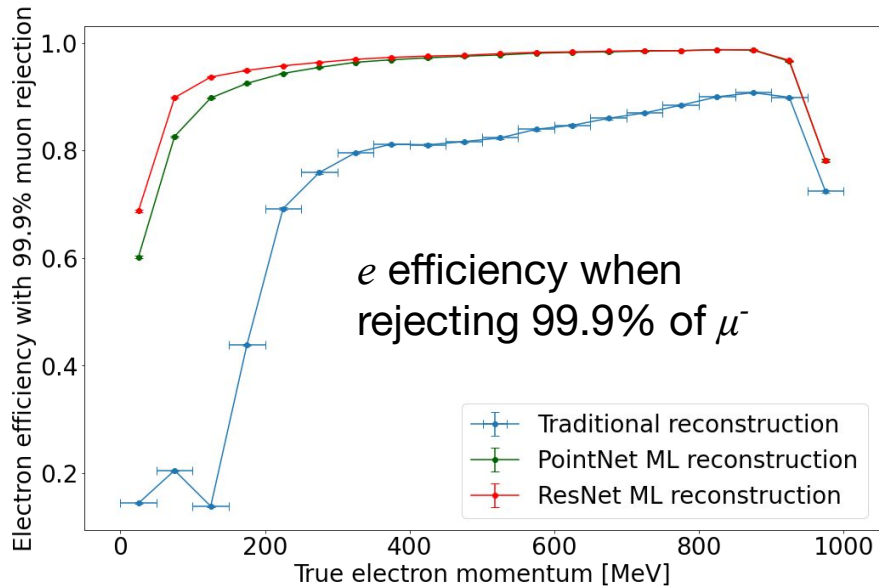
Applying random transformations using detector symmetry effectively increases dataset



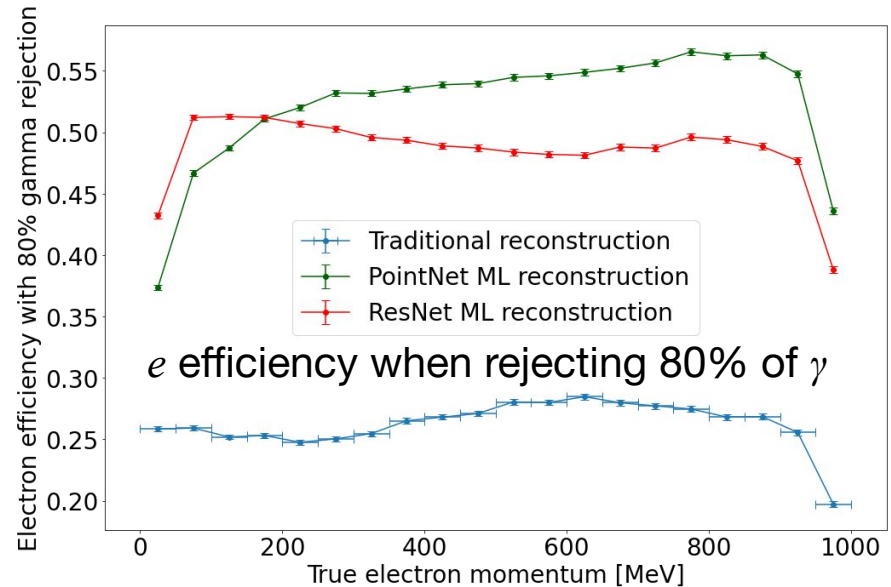
Rearranging and duplicating the geometrical surface has several advantages

- Less dependence on “choice” of slice along barrel to unwrap cylinder
- All segments appear exactly twice with minimal blank space
- **Circular boundary conditions** in both directions

Classification results



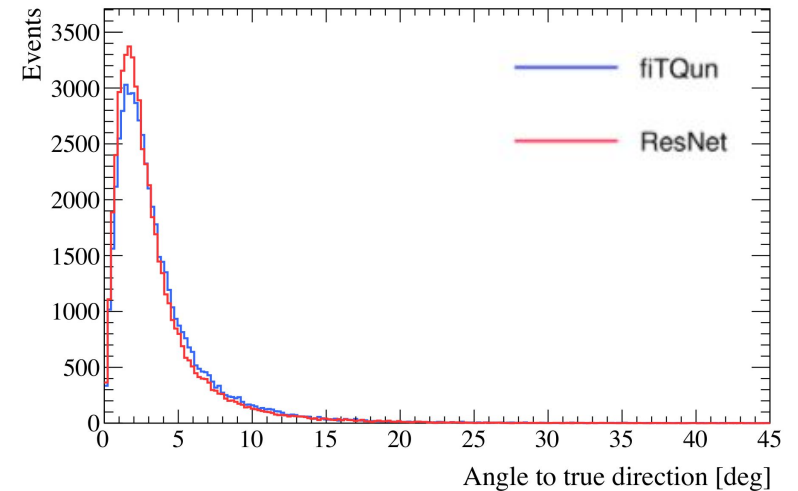
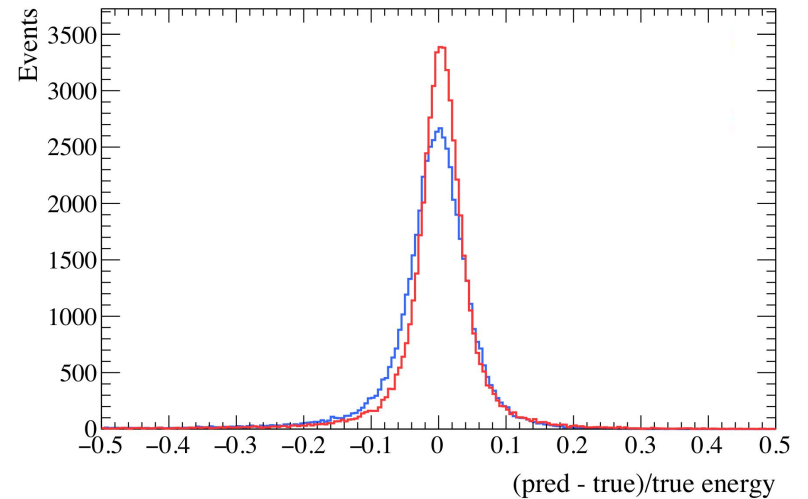
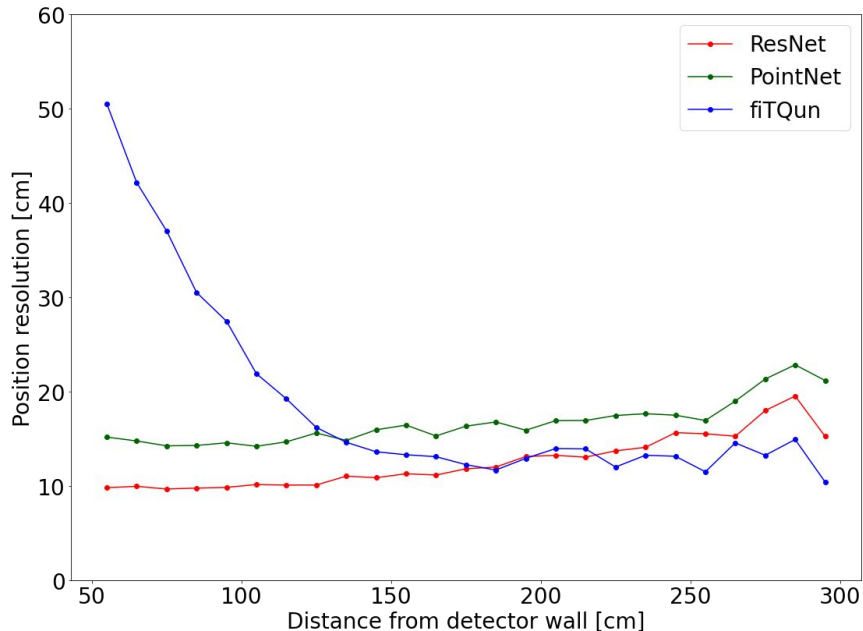
- ν_μ beam produces mostly μ , need rejection factor of 1000 for ν_e measurement
- Improved performance across energy range
- ResNet performs slightly better than PointNet for e vs μ classification



- γ and e almost indistinguishable in water Cherenkov detectors
- Discrimination has not been possible before
- PointNet performs better than ResNet for e vs γ classification

Position, direction, energy reconstruction

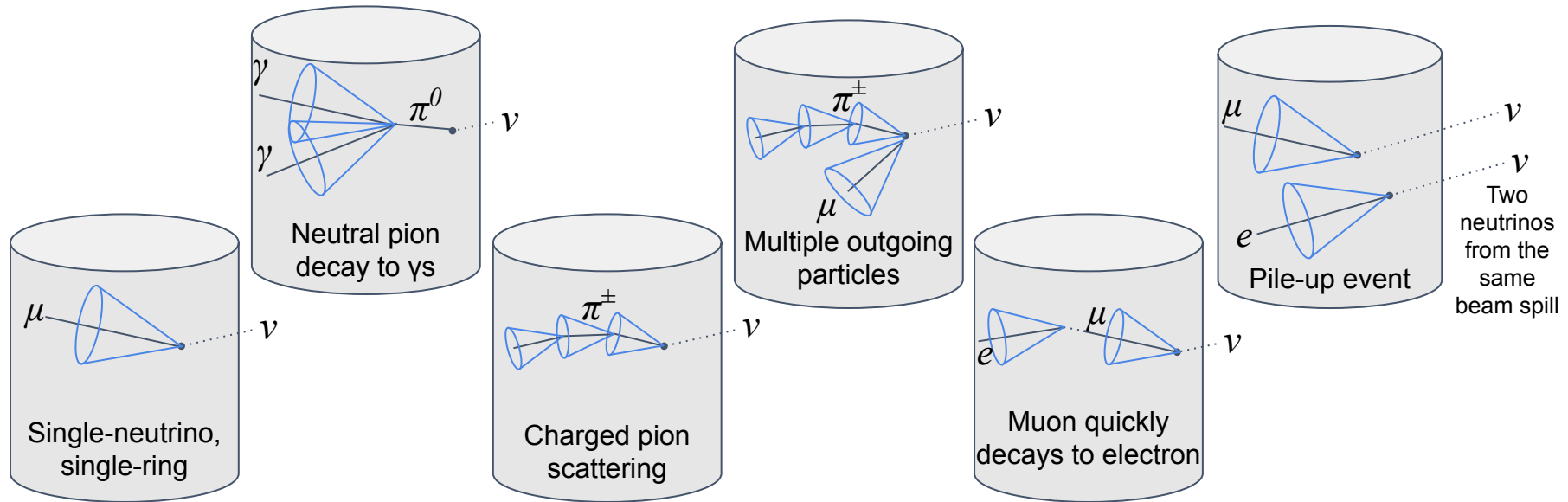
Output reconstructed quantities instead of classification variables



Multi-ring and multi-vertex events

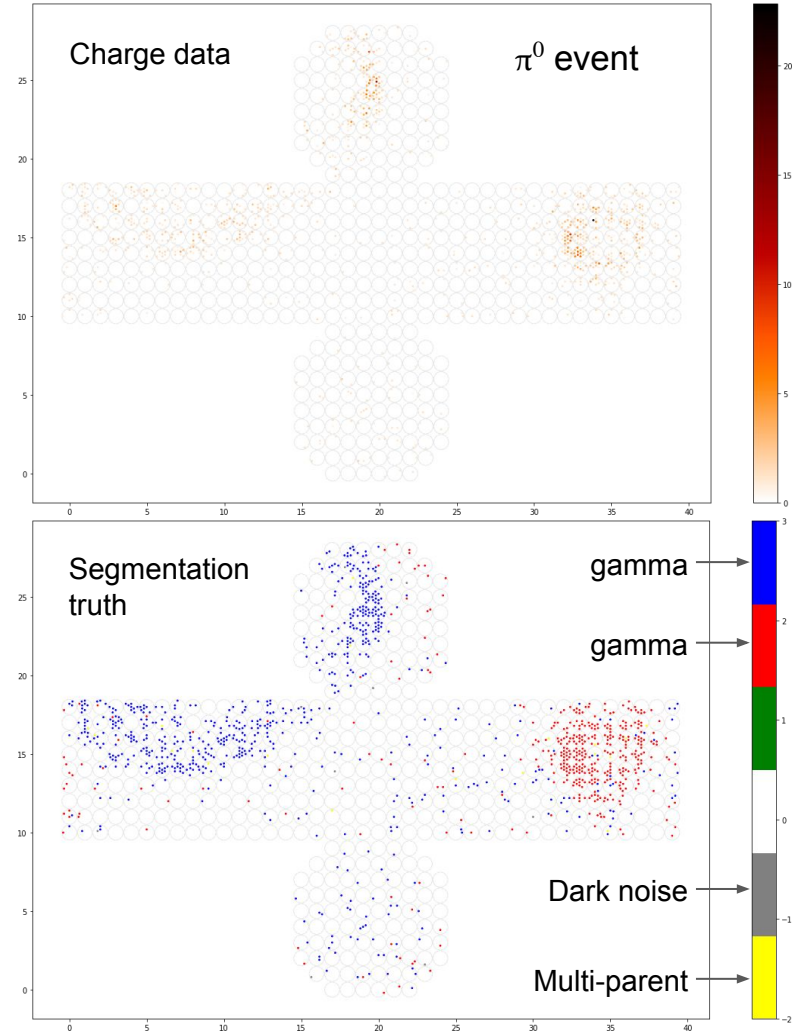
Need to develop ability to identify and reconstruct multi-ring and multi-vertex events

- Single-neutrino interactions can produce various multi-ring event topologies
- Pile-up of neutrino interactions is possible for IWCD due to proximity to beam source



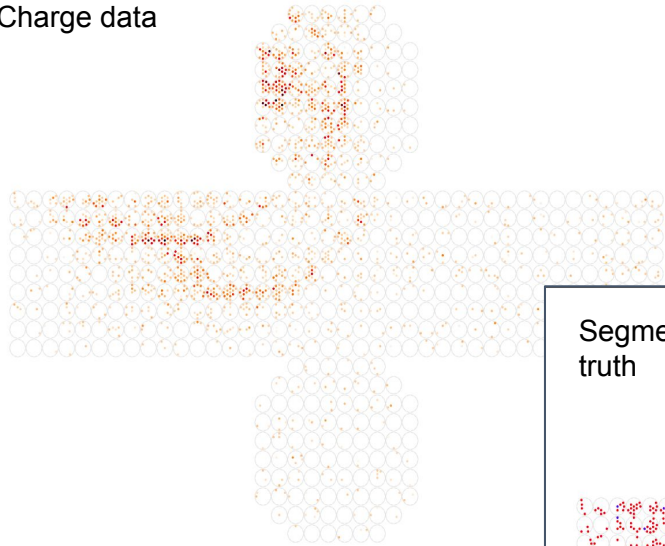
Segmentation networks

- Classification networks can be extended to perform segmentation
 - Deconvolutions and upsampling reverse convolutions and downsampling
 - Provides output value for each pixel
 - Currently using U-Net and FRRN
- Starting development with π^0 events
 - π^0 decay to produce two γ rings
 - Higher energy π^0 have overlapping rings

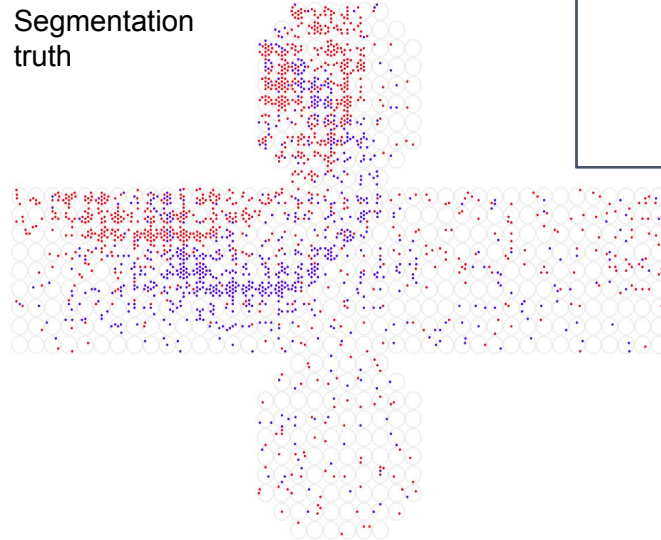


Segmentation results

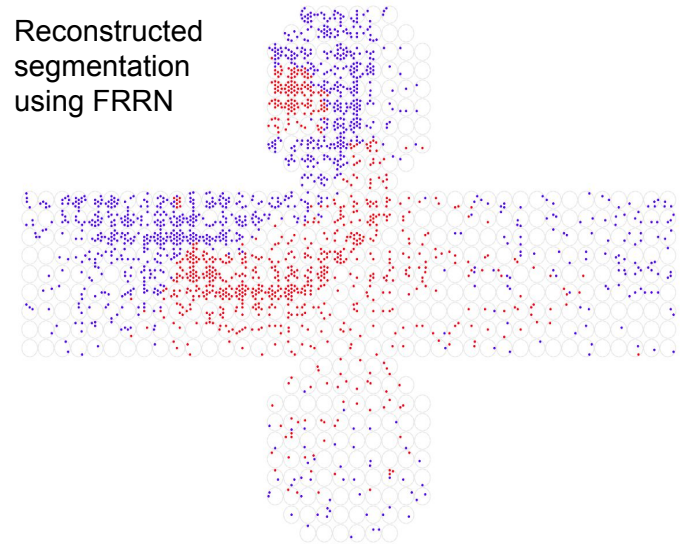
Charge data



Segmentation truth



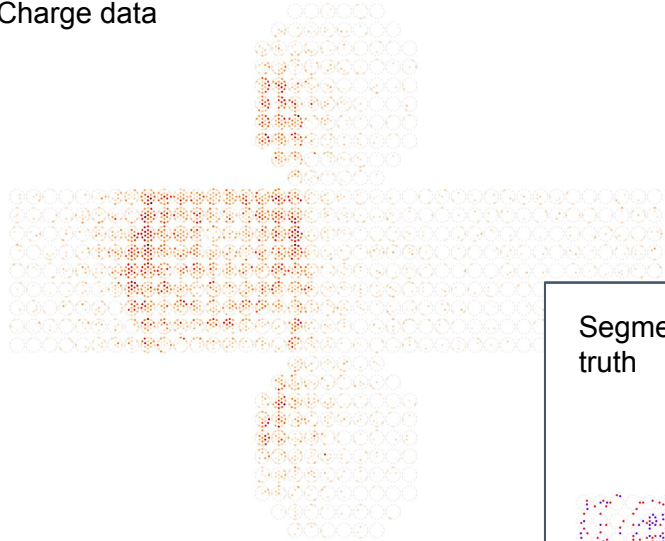
Reconstructed segmentation using FRRN



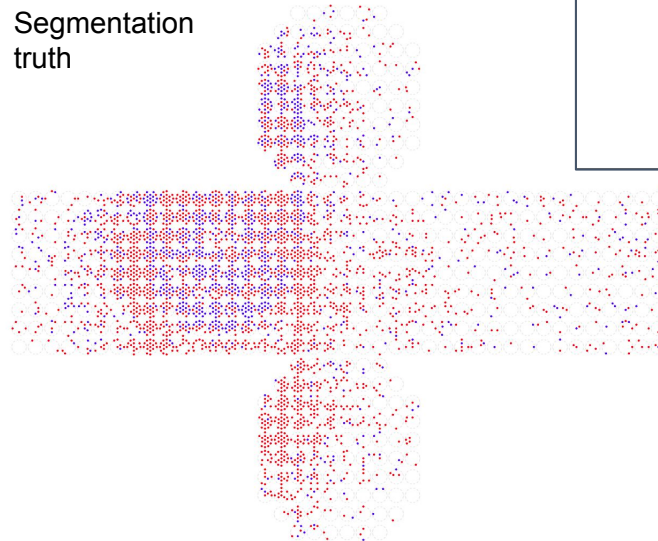
Works well with separated or partially overlapping rings

Segmentation results

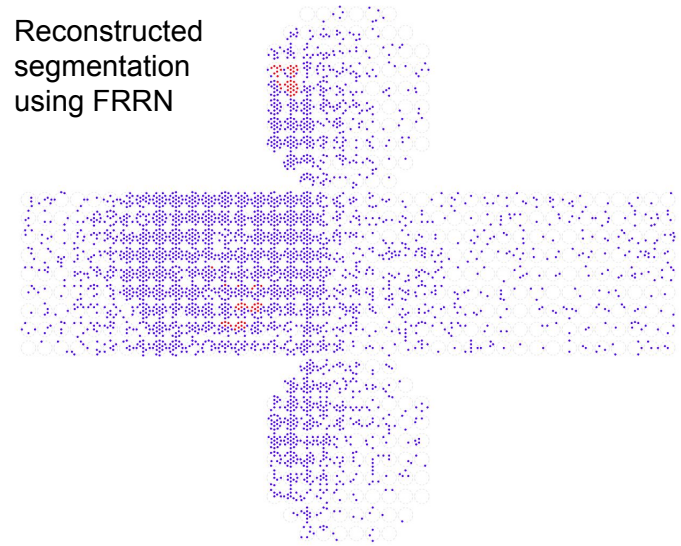
Charge data



Segmentation truth



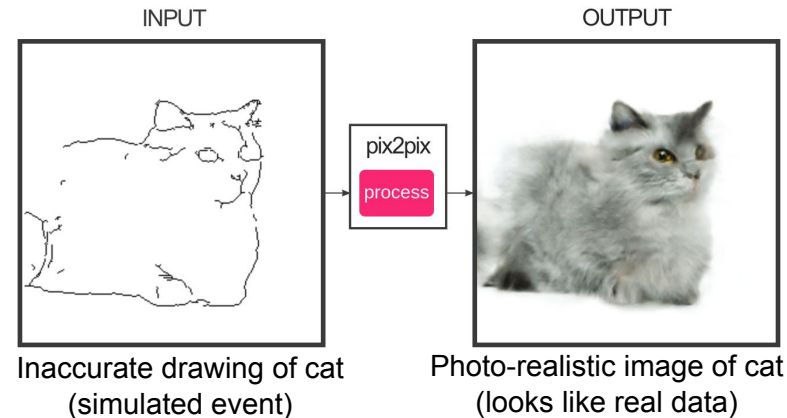
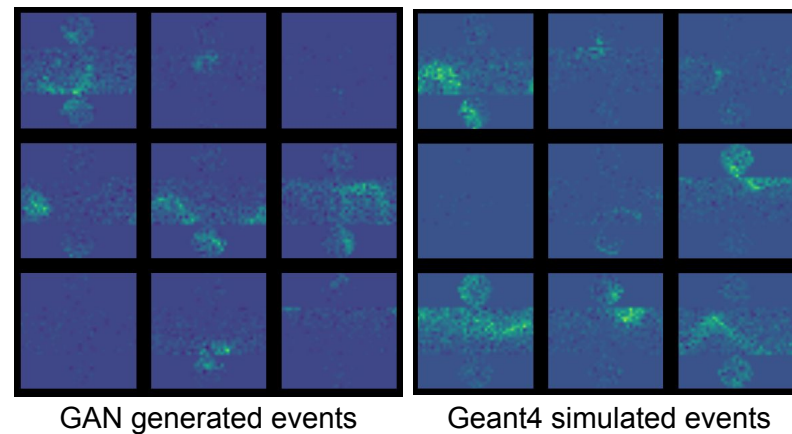
Reconstructed segmentation using FRRN



Poor reconstruction with some more overlapping rings

Generative networks

- Generative Adversarial Networks (GANs) create synthetic data
 - Generative network produces images
 - Train classifier to distinguish this from GAN output
 - Update GAN to produce data that classifier cannot distinguish
- Often used for faster or more accurate simulations or modifying data for different purposes
- Potential use for noise reduction
 - Add dark noise to simulated events
 - Train generative network to produce original events from noisy events
- Potential uses for detector calibration
 - Simulations assume some detector model not perfectly calibrated
 - Train network using both simulated and real data
 - Learn to modify simulated events to more closely match real data



Summary

Hyper-Kamiokande, the next-generation water Cherenkov neutrino detector has begun construction to start operation in 2027

- Both the far detector and IWCD will require new techniques to improve reconstruction, suppress backgrounds and reduce systematics

Machine learning can bypass the model approximations of old methods

- ResNet CNN and PointNet architectures already outperforming traditional methods
 - Improved reconstruction of particle position, direction and energy
 - Classification of particle types improves on existing selections and enables new analyses
- Additional benefit of huge increase in speed of reconstruction

Exploring other areas where machine learning can provide benefits

- Segmentation of multi-ring and multi-vertex events looks promising
- Generative networks to handle deficiencies in data



Appendix

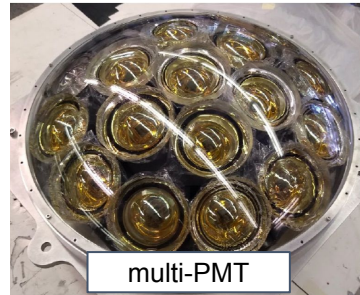
Hyper-K Detector

8 x increase in fiducial mass over Super-K

- 71 m tall x 68 m diameter = 258 kt total mass
188 kt fiducial mass

New photo-detector technology for increased sensitivity

- 20,000 B&L 50 cm PMTs = 20% photo-coverage
 - 1.5 ns timing resolution (half that of SK PMTs)
 - Double quantum efficiency of SK PMTs
- Additional photo-coverage from multi-PMT modules
 - 8 cm PMTs grouped in modules of 19 PMTs
 - Improved position, timing, direction resolution
 - Also used for in-situ calibration of 50cm PMTs



The Hyper-K Experiment

February 2020: Budget approved by Japanese government

May 2020: Univ. of Tokyo President and KEK Director General signed MOU:

Univ. of Tokyo to construct & operate Hyper-K detector

KEK to upgrade & operate J-PARC neutrino beam



Hyper-K's WC detectors

Hyper-K far detector

3rd generation of WC detectors at Kamioka

8 x increase in fiducial mass over Super-K

72 m tall x 68 m diameter = 258 kt total mass

188 kt fiducial mass

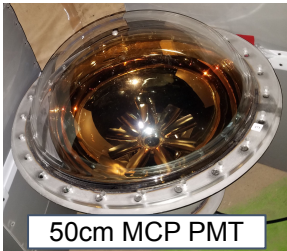
Baseline design: 40,000 B&L 50 cm PMTs

= 40% photo-coverage

New photo-detector technology to
provide increased sensitivity



50cm B&L PMT



50cm MCP PMT



Hyper-K's WC detectors

Intermediate detector (IWCD)

Located ~ 1 km from beam source

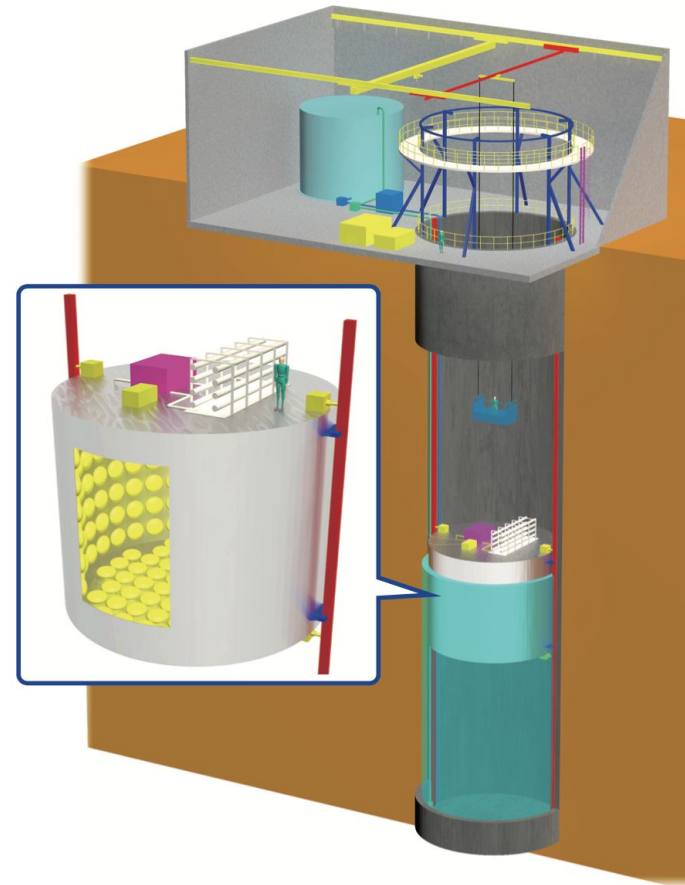
6 m tall x 8 m diameter inner detector

~ 500 multi-PMT modules

Measure combination of flux and cross-section to reduce systematics at far detector

High event rate, same detector technology and target nuclei as far detector

Moves vertically in ~50 m tall pit measuring different off-axis angles gives different ν energy spectra



Hyper-K's WC detectors

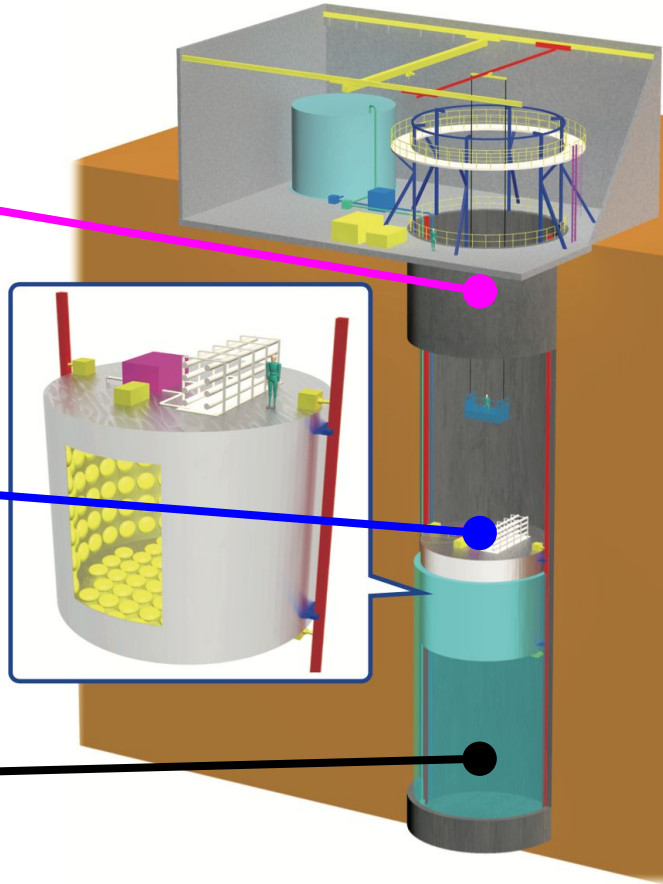
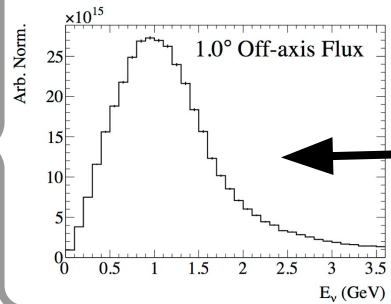
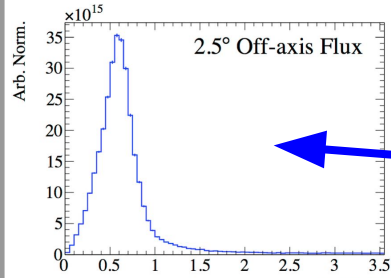
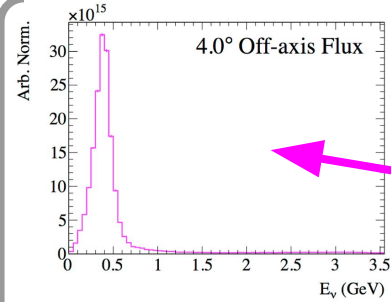
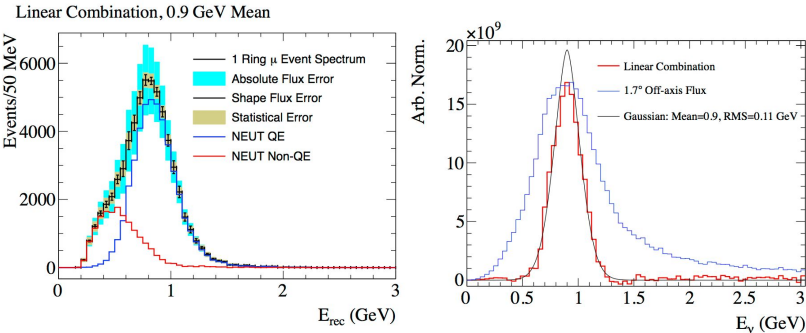
Off-axis spanning detector

ν energy spectrum depends on angle off-axis to the neutrino beam

Far detector @ 2.5° for peak at ~ 600 MeV

Moving IWCD varies angle, allowing measurements at different energies

Linear combinations allows mimicking mono-chromatic beam or far-detector spectrum



Hyper-K's WC detectors

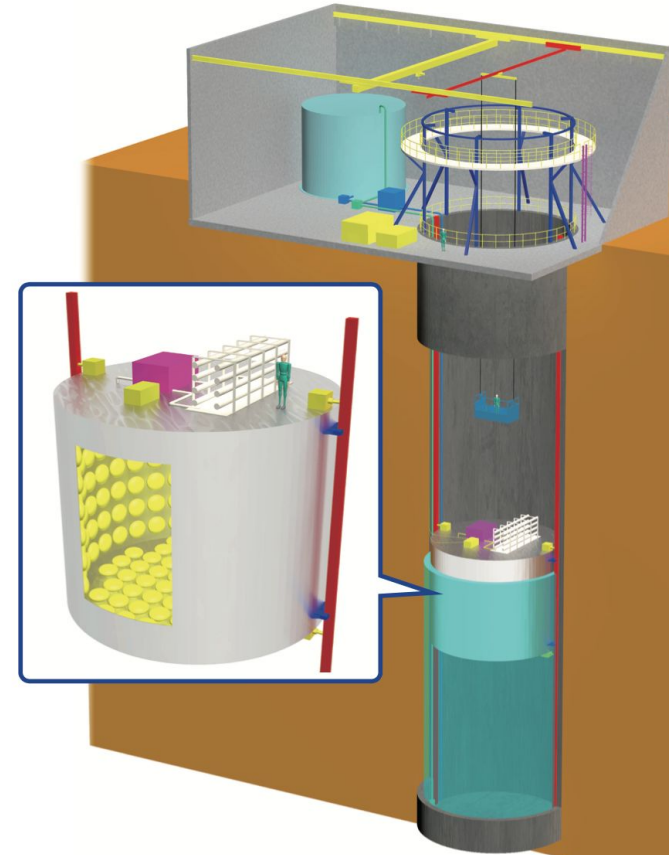
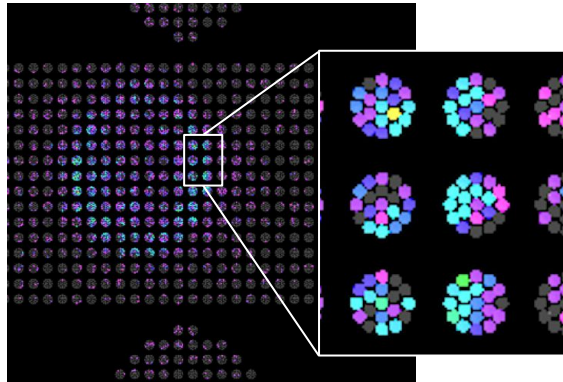
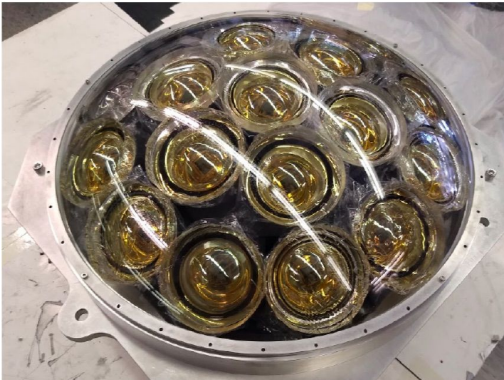
Multi-PMT modules

8 cm PMTs: Better position resolution
< 1 ns timing resolution

Additional directionality information

Need reconstruction to exploit additional information

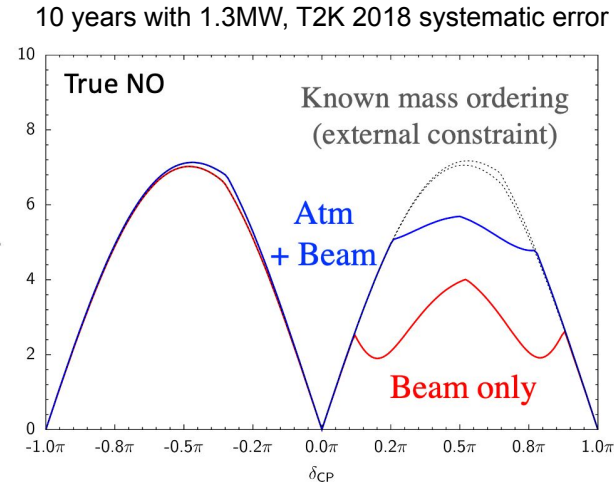
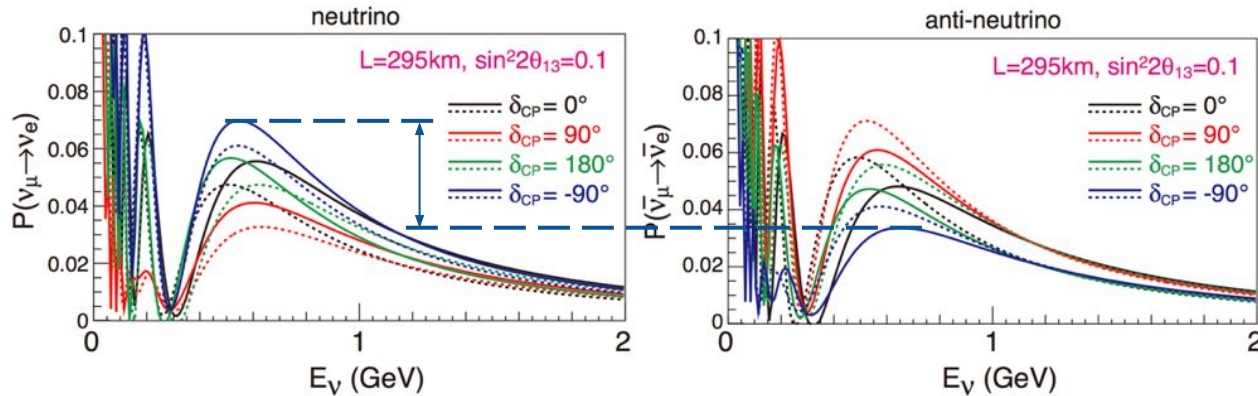
Necessary for smaller detector size



Also under investigation: Combining 50 cm PMTs + multi-PMT modules in far detector

Hyper-K's physics goals

Long-baseline neutrino oscillations: CP violation

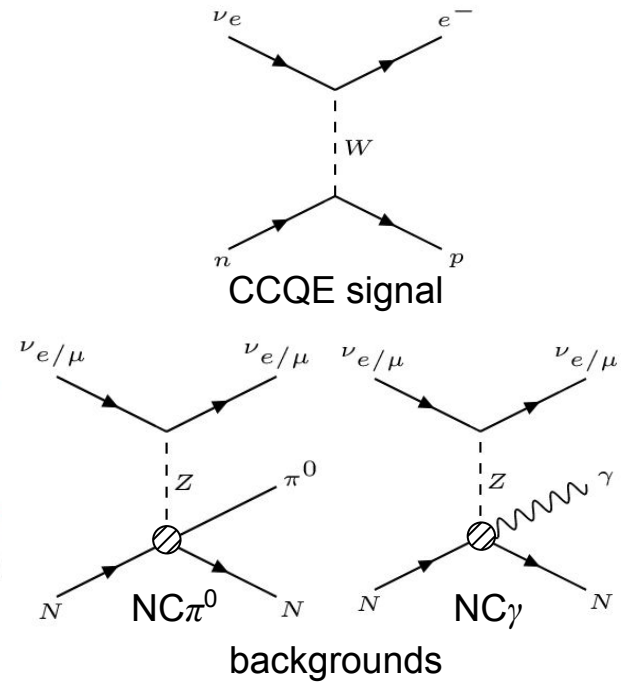
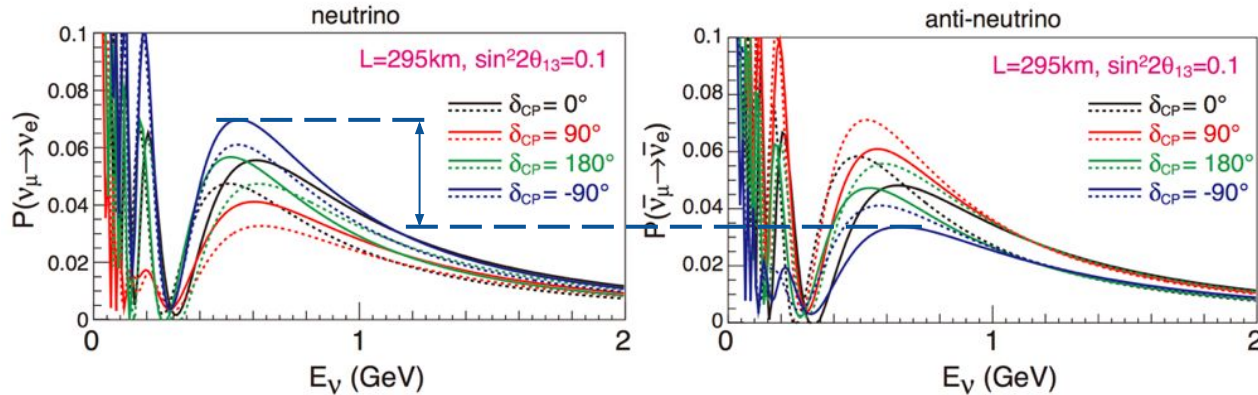


Combine beam and atmospheric neutrino observations for maximum sensitivity

- δ_{CP} precision comes mostly through difference in $P(\nu_{\mu} \rightarrow \nu_e)$ vs $P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e)$
- Effect of δ_{CP} can be degenerate with normal vs inverted mass ordering
- Atmospheric ν 's gain sensitivity to mass ordering by exploiting matter effect of Earth on oscillations

Hyper-K's physics goals

Long-baseline neutrino oscillations: CP violation



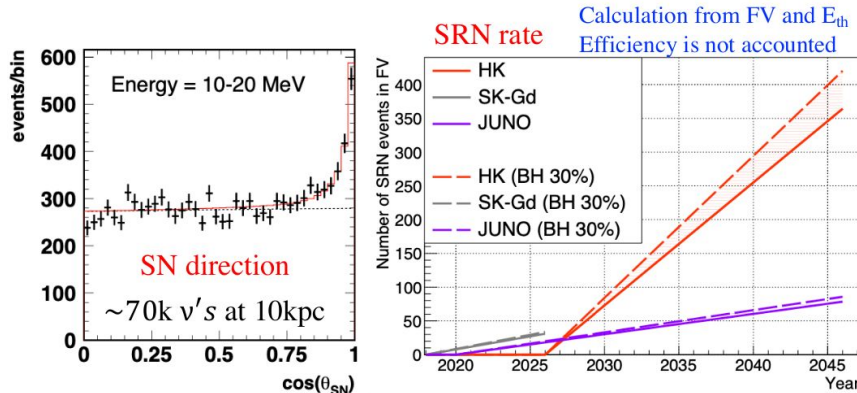
Oscillation maximum is at around 0.6 GeV

- Dominant signal ν_e interaction is charged current quasielastic (CCQE)
- Potential background sources:
 - Neutral current interactions (ν_e or ν_μ) producing neutral pions or gammas
 - Muons from ν_μ misidentified as electrons from ν_e

Hyper-K's physics goals

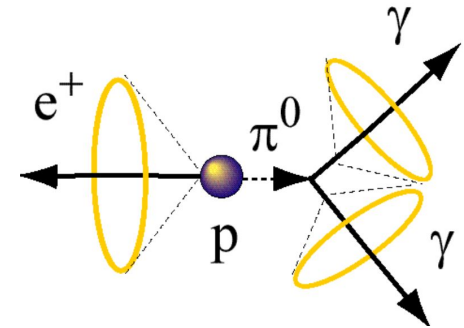
Neutrino astrophysics

- Solar ν 's: day/night asymmetry; hep ν 's; ${}^8\text{B}$ ν spectrum upturn
- Supernova ν 's: 1000's ν events for nearby supernova pointing, time & spectrum analysis; search for supernova relic ν 's



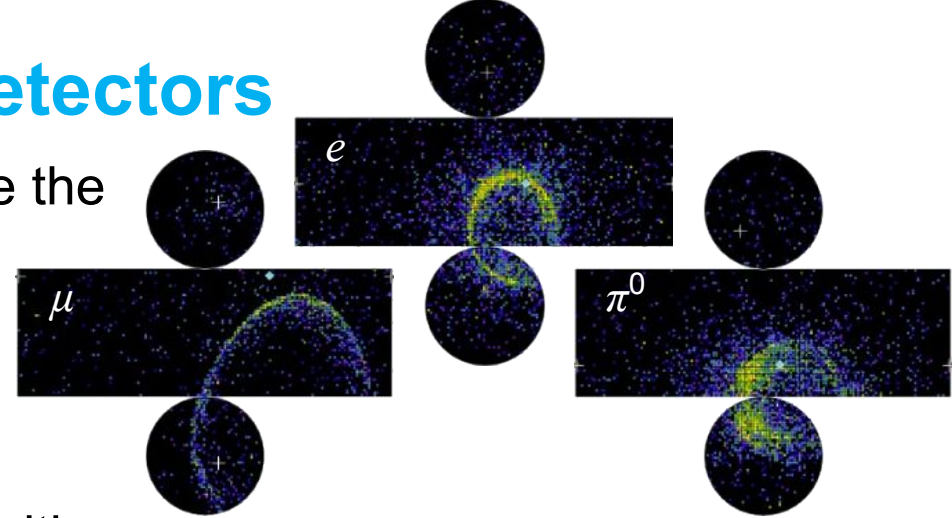
Proton decay

- Search to order of magnitude greater lifetime than current limit
- 10^{35} years for $p \rightarrow e^+ + \pi^0$
- 3×10^{34} years for $p \rightarrow \bar{\nu} + K^+$

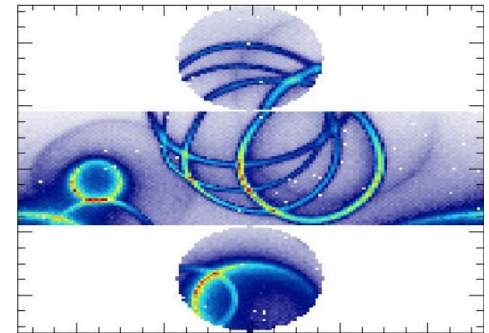


Reconstruction for WC detectors

Take raw detector data and determine the physics that occurred



- Particle type identification
 - Separate signal events from background
- Particle momentum, direction, position
 - Kinematics essential to determine incoming neutrino energy for neutrino oscillation probability
- Separating & reconstructing multi-ring events
 - Events with multiple particles / rings contribute to both signal & background
 - Multiple neutrinos can interact around the same time in IWCD

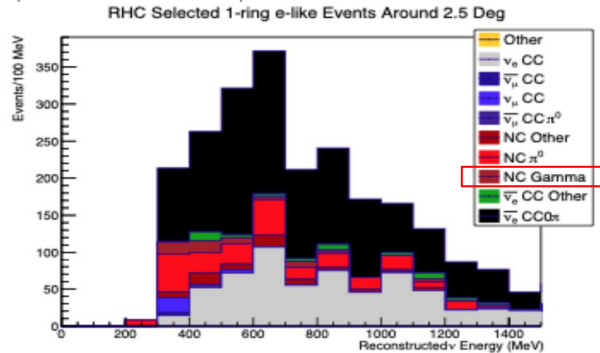
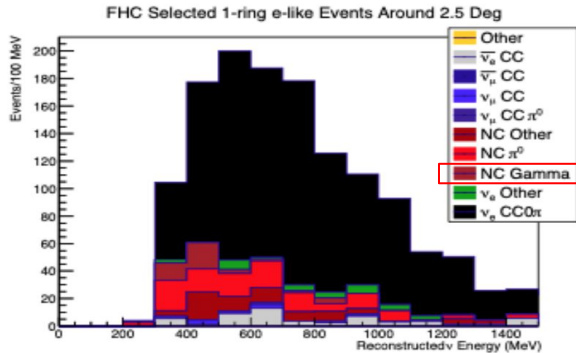


Physics Motivations

New opportunities beyond simple reconstruction improvement

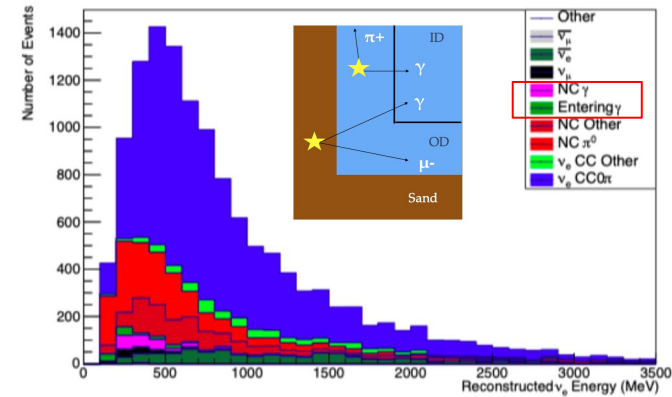
- NC γ discrimination and measurement

Systematic Type	Requirement	Motivation
$\sigma(\nu_e)/\sigma(\nu_\mu)$ to $\sigma(\bar{\nu}_e)/\sigma(\bar{\nu}_\mu)$ ratio	2.9-3.7%	CP violation search and precision δ_{CP} measurement.
$\sigma(\nu_e)/\sigma(\nu_\mu)$, $\sigma(\bar{\nu}_e)/\sigma(\bar{\nu}_\mu)$	3-5%	θ_{23} octant and precision θ_{23} measurement.
Intrinsic $\nu_e, \bar{\nu}_e$ and NC background normalizations	3-5%	CP violation search and precision δ_{CP} measurement.



2.7-4.0 degree off-axis range

Selected 1-ring e-like events



- Potential neutron tagging application

- Bottom-up calibration: Enable multitude of detector parameter variations

Traditional reconstruction method

fiTQun: Likelihood-based reconstruction for higher energies

- Originally developed for Super-K detector
 - Based on algorithm of MiniBooNE: <https://arxiv.org/abs/0902.2222>
- Uses full information of unhit PMTs + time & charge of hit PMTs:

$$L(\mathbf{x}) = \prod_j^{unhit} P_j(unhit|\mathbf{x}) \prod_i^{hit} P_i(hit|\mathbf{x}) f_q(q_i|\mathbf{x}) f_t(t_i|\mathbf{x})$$

Likelihood to maximise Candidate event hypothesis Probability of no hit at PMT Probability of hit at PMT Hit charge probability density Hit time probability density

- Probabilities calculated based on direct + scattered + reflected light
- Likelihood ratios used to distinguish particle types and single-ring / multi-ring event topology hypotheses

Machine learning reconstruction

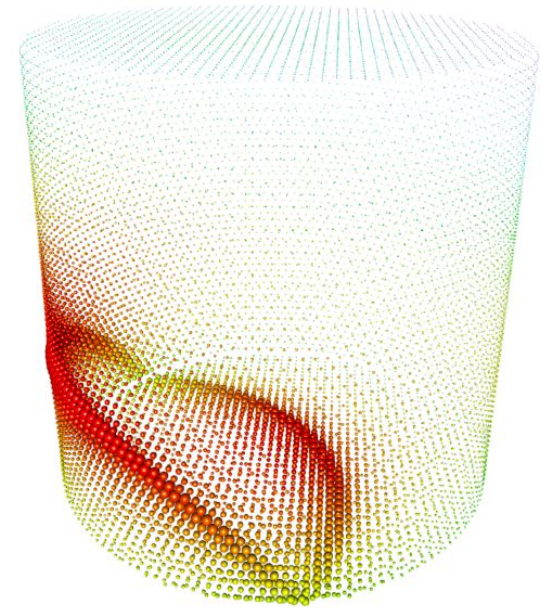
WatChMaL: cross-collaboration group formed to explore ML for WC

Common challenges for ML with WC detectors

- Cylindrical geometry
- High-resolution, sparse data

Many physics goals

- Maximise precision of new detectors
- Reconstruct complex event topologies
- Discriminate electron and gamma rings
- Improving detector calibration & systematics



WatChMaL.org

Machine learning reconstruction

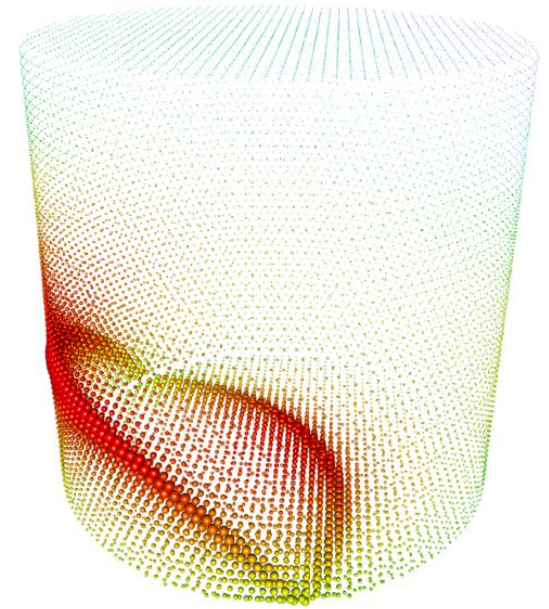
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WatChMaL.org

The IWCD detector

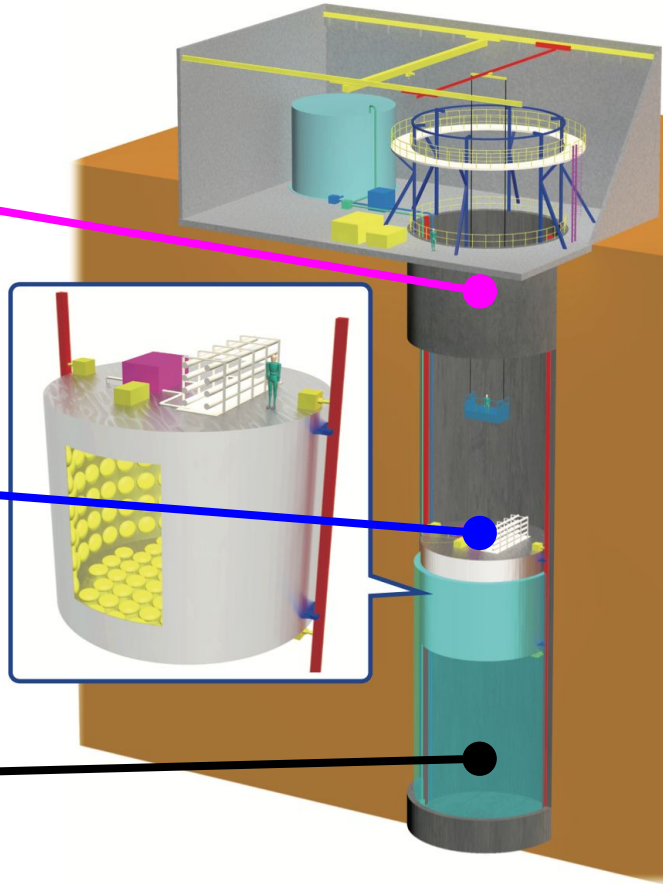
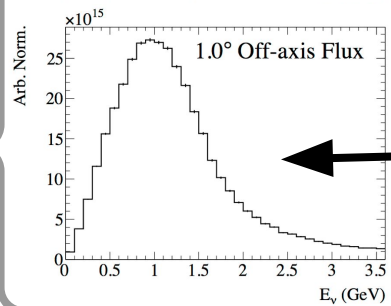
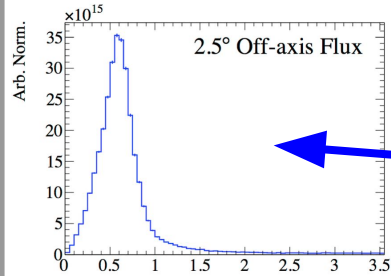
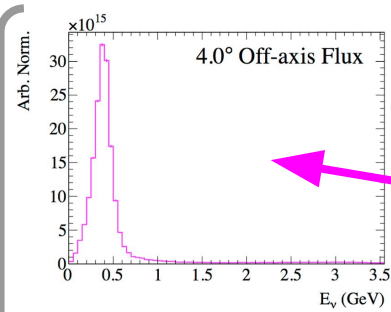
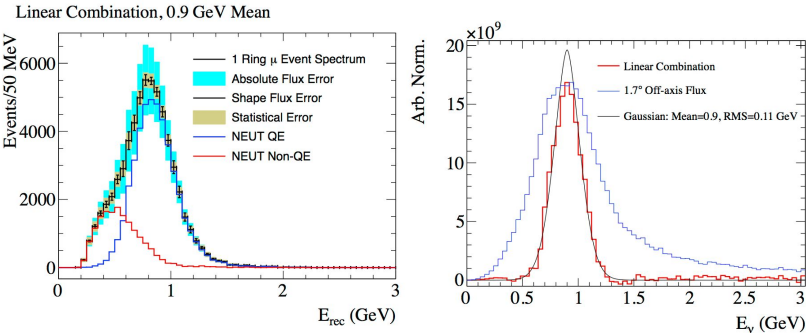
Off-axis spanning detector

ν energy spectrum depends on angle off-axis to the neutrino beam

Far detector @ 2.5° for peak at ~ 600 MeV

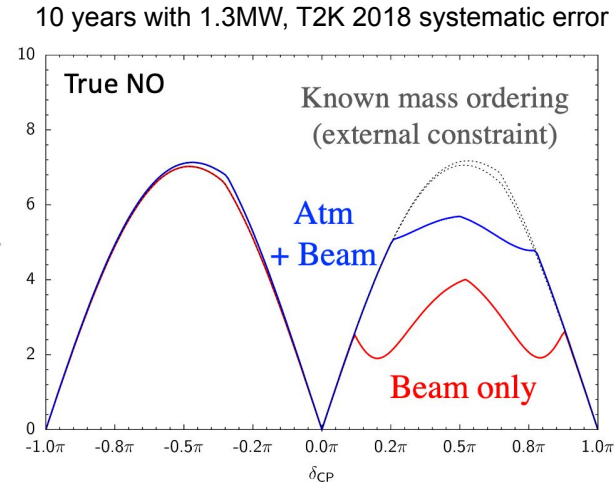
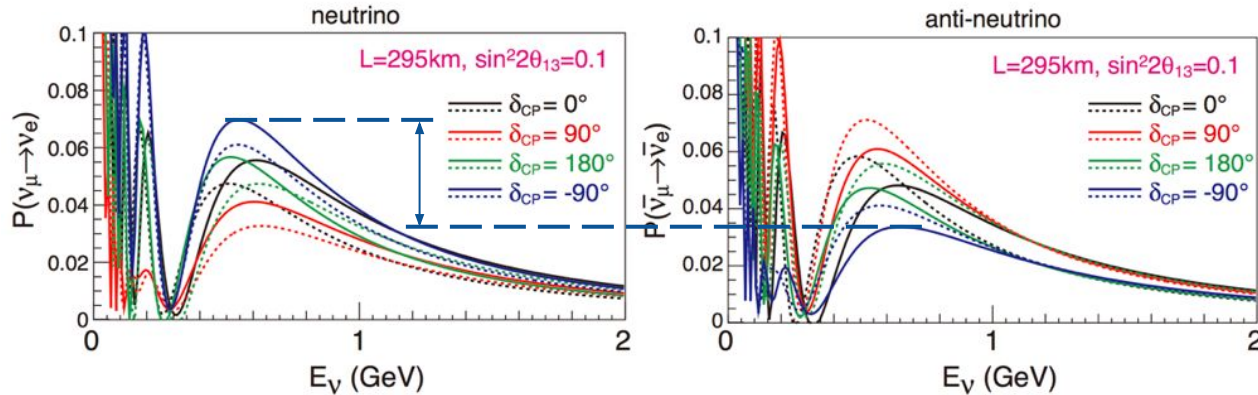
Moving IWCD varies angle, allowing measurements at different energies

Linear combinations allows mimicking mono-chromatic beam or far-detector spectrum



Hyper-K's physics goals

Long-baseline neutrino oscillations: CP violation

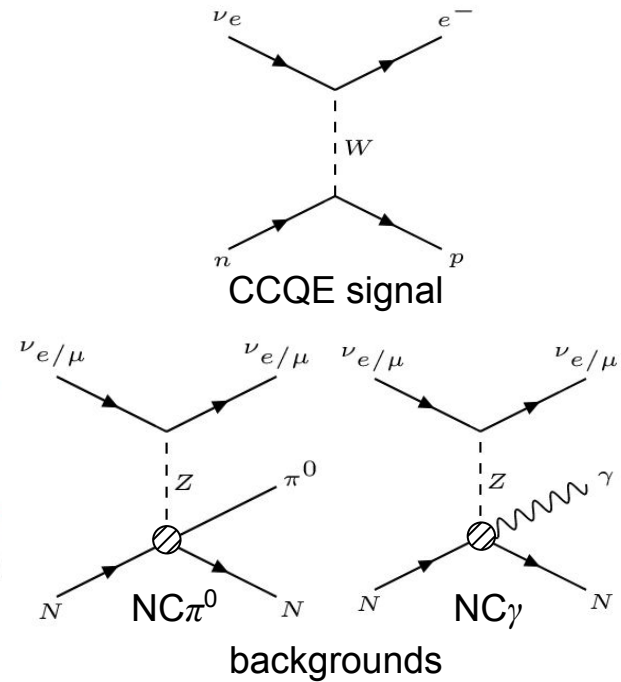
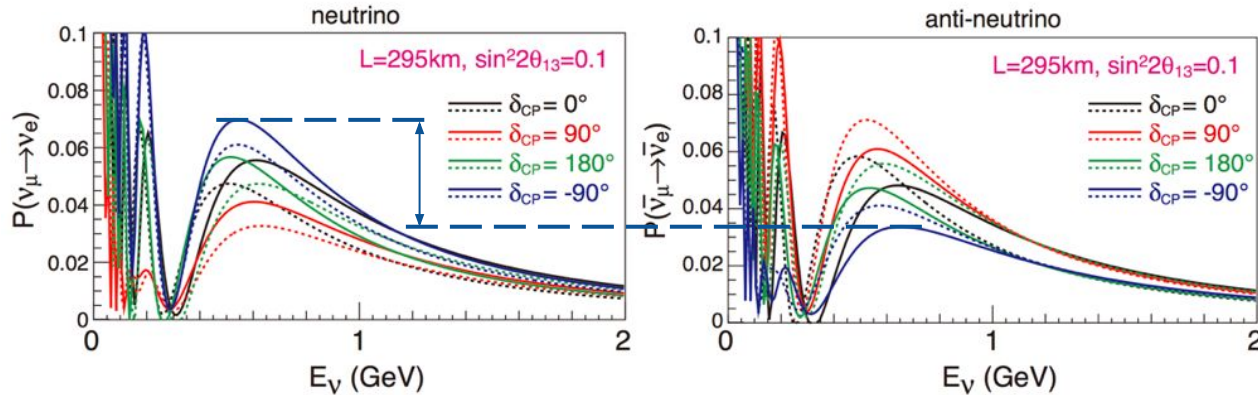


Combine beam and atmospheric neutrino observations for maximum sensitivity

- δ_{CP} precision comes mostly through difference in $P(\nu_{\mu} \rightarrow \nu_e)$ vs $P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e)$
- Effect of δ_{CP} can be degenerate with normal vs inverted mass ordering
- Atmospheric ν 's gain sensitivity to mass ordering by exploiting matter effect of Earth on oscillations

Hyper-K's physics goals

Long-baseline neutrino oscillations: CP violation



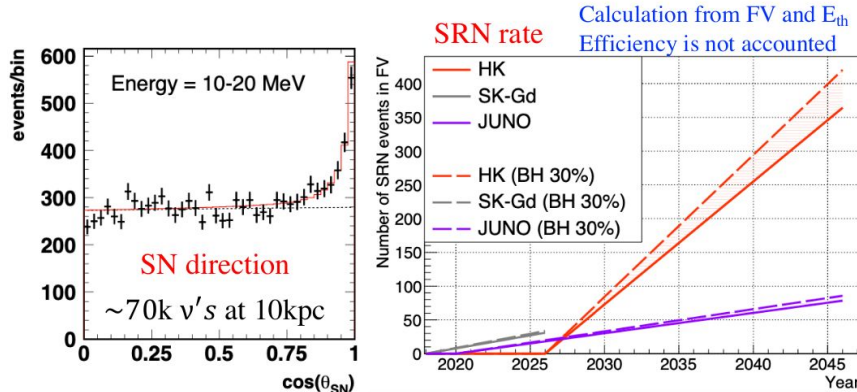
Oscillation maximum is at around 0.6 GeV

- Dominant signal ν_e interaction is charged current quasielastic (CCQE)
- Potential background sources:
 - Neutral current interactions (ν_e or ν_μ) producing neutral pions or gammas
 - Muons from ν_μ misidentified as electrons from ν_e

Hyper-K's physics goals

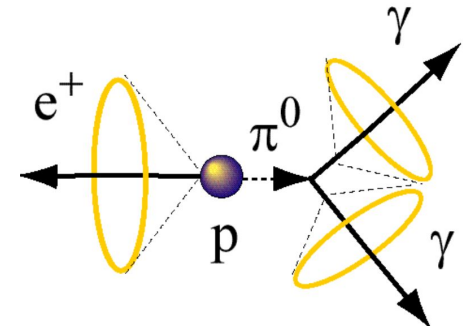
Neutrino astrophysics

- Solar ν 's: day/night asymmetry; hep ν 's; ${}^8\text{B}$ ν spectrum upturn
- Supernova ν 's: 1000's ν events for nearby supernova pointing, time & spectrum analysis; search for supernova relic ν 's



Proton decay

- Search to order of magnitude greater lifetime than current limit
- 10^{35} years for $p \rightarrow e^+ + \pi^0$
- 3×10^{34} years for $p \rightarrow \bar{\nu} + K^+$

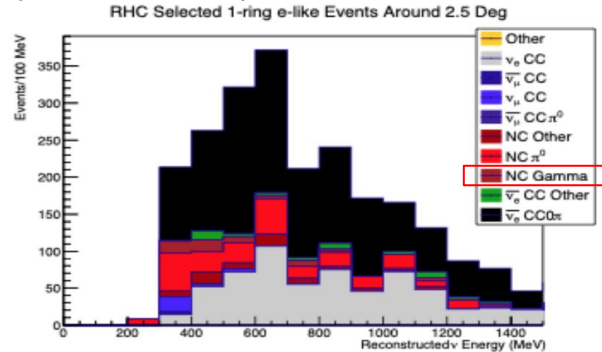
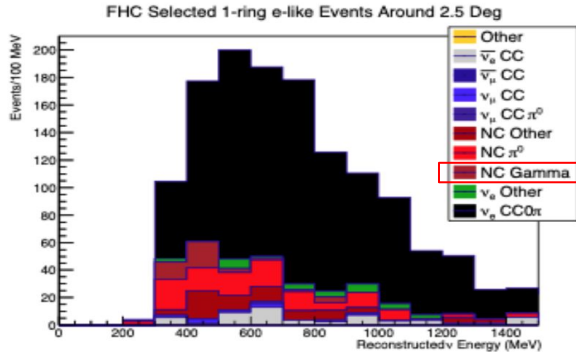


Particle type classification

New opportunities beyond simple reconstruction improvement

- NC γ discrimination and measurement

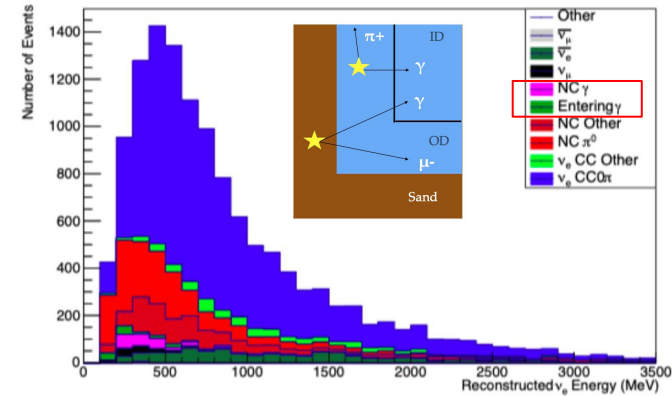
Systematic Type	Requirement	Motivation
$\sigma(\nu_e)/\sigma(\nu_\mu)$ to $\sigma(\bar{\nu}_e)/\sigma(\bar{\nu}_\mu)$ ratio	2.9-3.7%	CP violation search and precision δ_{CP} measurement.
$\sigma(\nu_e)/\sigma(\nu_\mu), \sigma(\bar{\nu}_e)/\sigma(\bar{\nu}_\mu)$	3-5%	θ_{23} octant and precision θ_{23} measurement.
Intrinsic $\nu_e, \bar{\nu}_e$ and NC background normalizations	3-5%	CP violation search and precision δ_{CP} measurement.



- Bottom-up calibration: Enable multitude of detector parameter variations

2.7-4.0 degree off-axis range

Selected 1-ring e-like events



- Potential neutron tagging application

Traditional reconstruction method

fiTQun: Likelihood-based reconstruction for higher energies

- Originally developed for Super-K detector
 - Based on algorithm of MiniBooNE: <https://arxiv.org/abs/0902.2222>
- Uses full information of unhit PMTs + time & charge of hit PMTs:

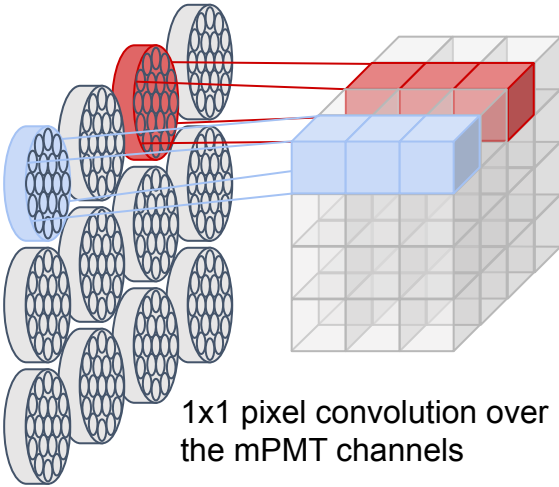
$$L(\mathbf{x}) = \prod_j^{unhit} P_j(unhit|\mathbf{x}) \prod_i^{hit} P_i(hit|\mathbf{x}) f_q(q_i|\mathbf{x}) f_t(t_i|\mathbf{x})$$

Likelihood to maximise Candidate event hypothesis Probability of no hit at PMT Probability of hit at PMT Hit charge probability density Hit time probability density

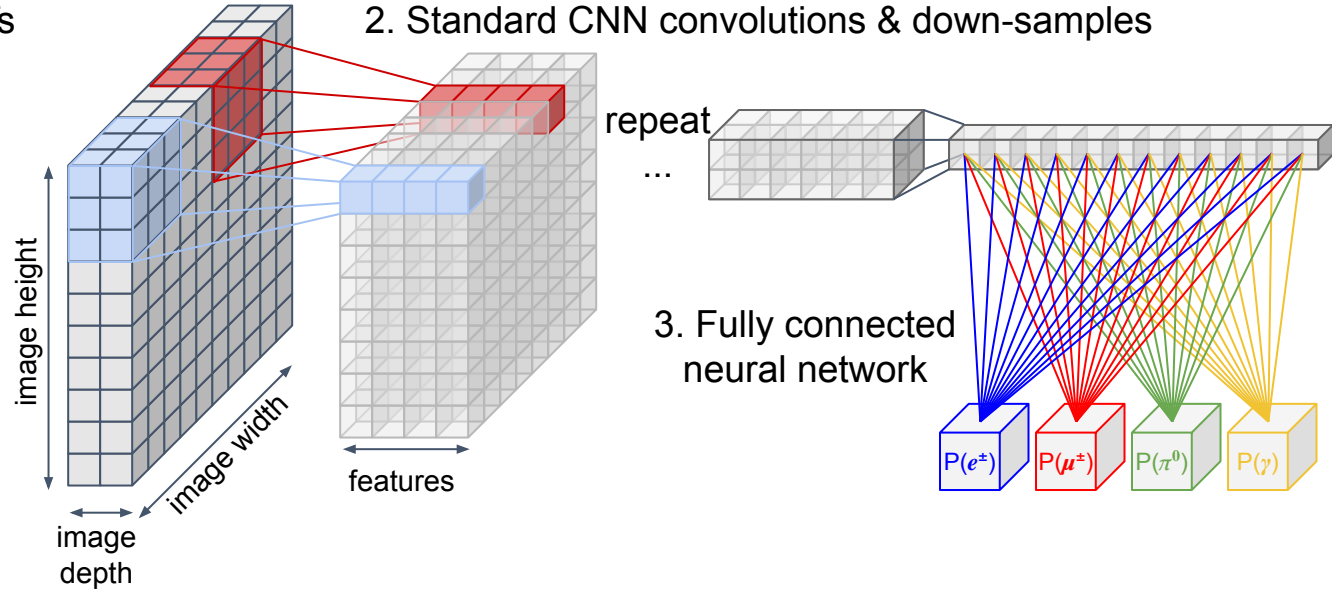
- Probabilities calculated based on direct + scattered + reflected light
- Likelihood ratios used to distinguish particle types and single-ring / multi-ring event topology hypotheses

CNN Architecture

1. Convolution over mPMTs



2. Standard CNN convolutions & down-samples



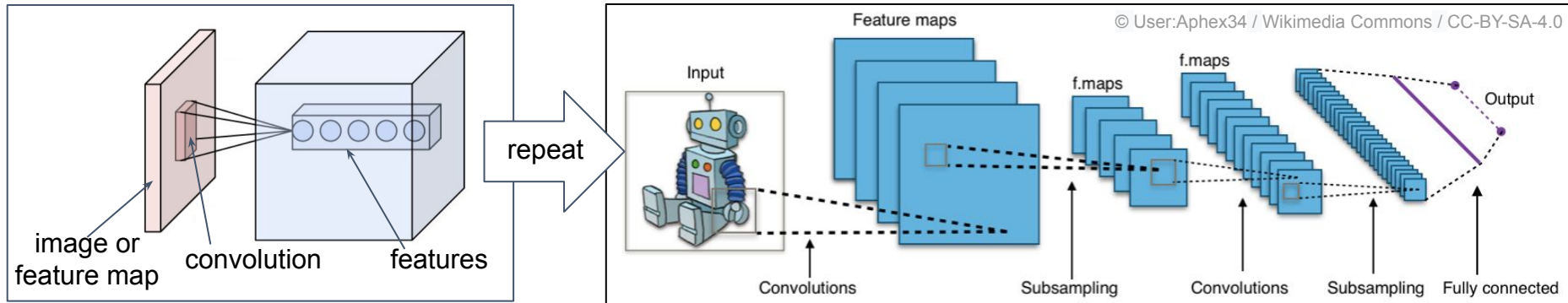
3. Fully connected neural network



Network based on ResNet-18 CNN architecture [arXiv:1512.03385]

- Replaced initial 7x7 pixel convolution with 1x1 convolutions over all channels
 - Equivalent to convolution over the 19 PMTs within each mPMT

Convolutional neural networks hugely successful in image processing

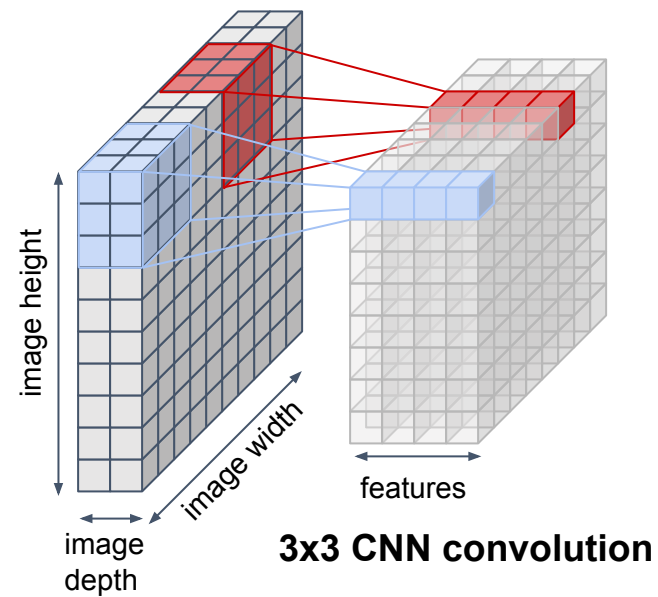


- Start with image with pixel values ('features'): T and Q at each PMT
- Scan many small (e.g. 3x3) convolution kernels across image
 - Increases number of features
- Downsample image (e.g. 2x2 max-pooling)
 - Decreases number of pixels
- End with 1-D array of features, feed into traditional fully-connected neural network
- Learn convolution and final network weights through 'back-propagation' of loss

PointNet architecture

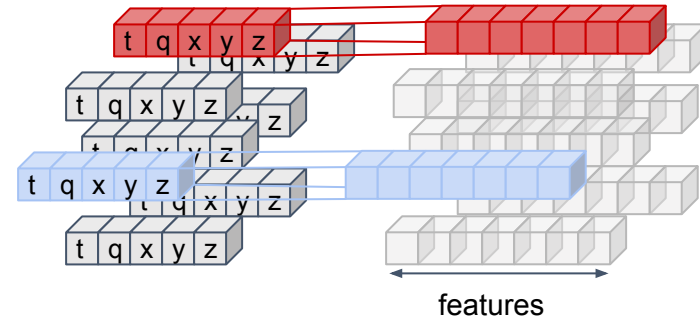
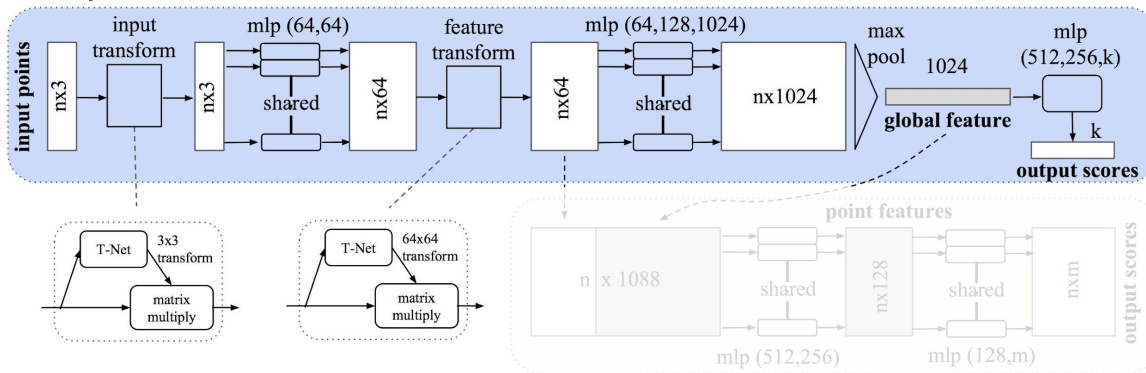
PointNet designed to work on 'point clouds' rather than images of pixels

- Each hit PMT is a 'point' with time, charge & position, not fixed to grid
- Convolution-like operations act on each point's charge, time and position
- Learn global transformations applied to all points
- Single pooling layer from all points to 1D array
- Can apply to any detector geometry



3x3 CNN convolution

Classification Network

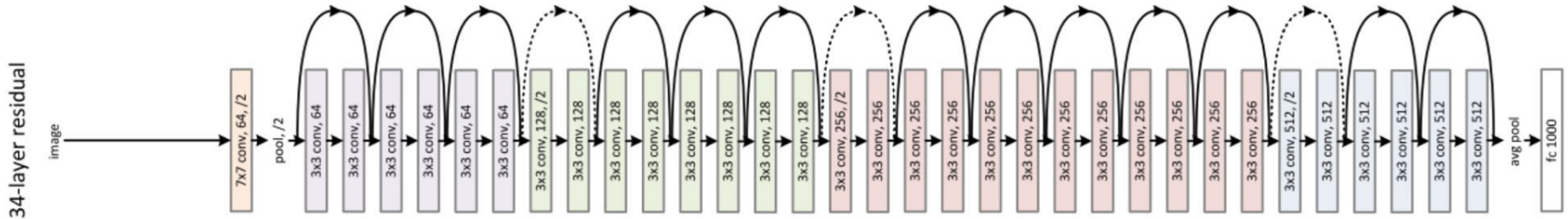
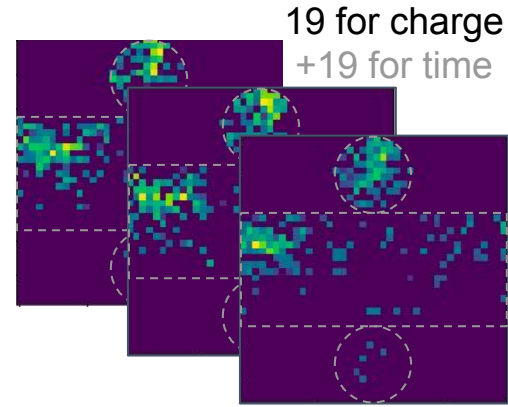


PointNet MLP (1x1 convolution on point cloud)

CNN architecture

Full cylinder of mPMTs is unwrapped onto 40x40 image

- 38 channels: charge & time of 19 PMTs per mPMT
- No special treatment for geometrical effects at boundary between barrel and end-caps
- Data augmented by reflecting / rotating around tank axis

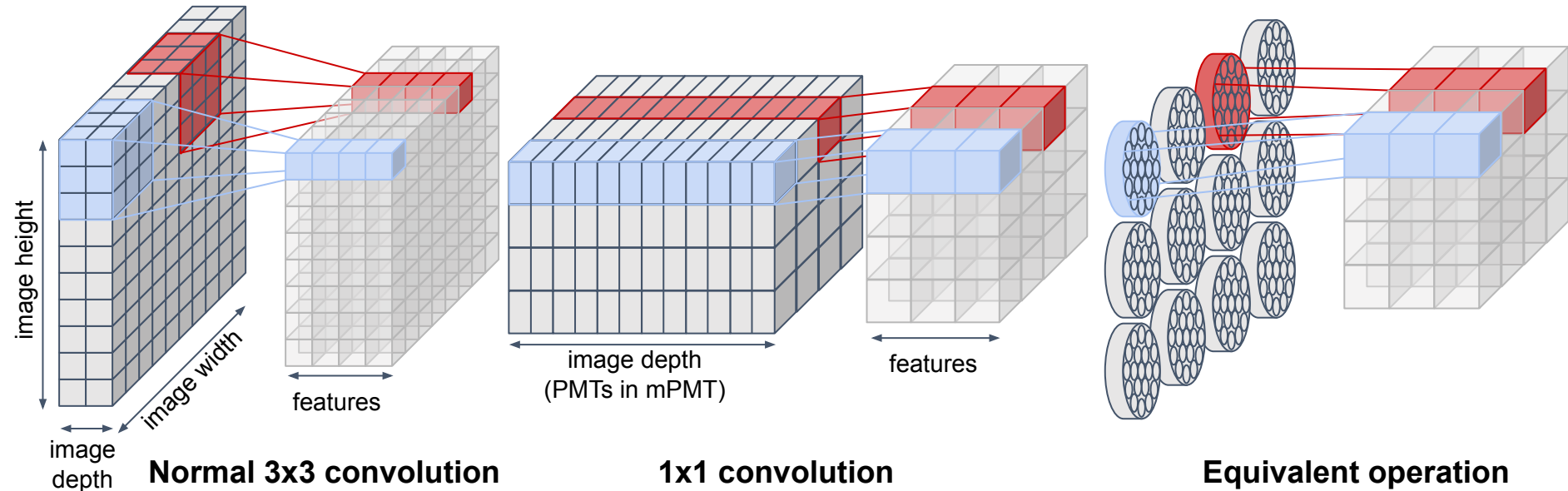


Mostly using ResNet-18 architecture [arXiv:1512.03385]

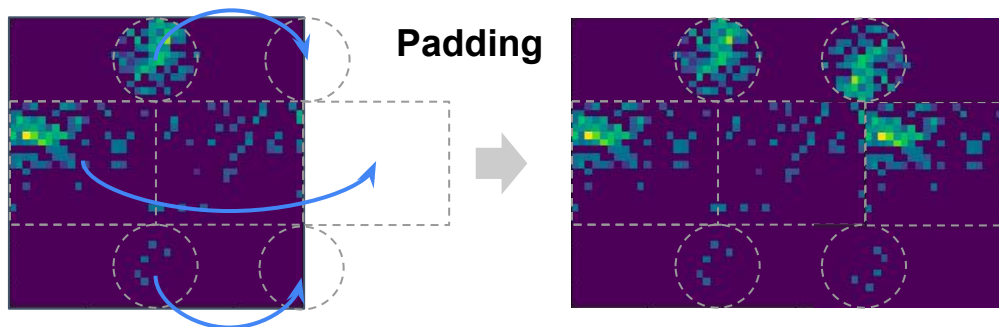
- Initial 1x1 convolution added to act on the 19 PMTs of each mPMT
- Also explored deeper networks with small improvement

CNN architecture

Treating each PMT inside mPMT as a channel, starting with 1x1 convolution
→ equivalent to doing a 'convolution' over each mPMT

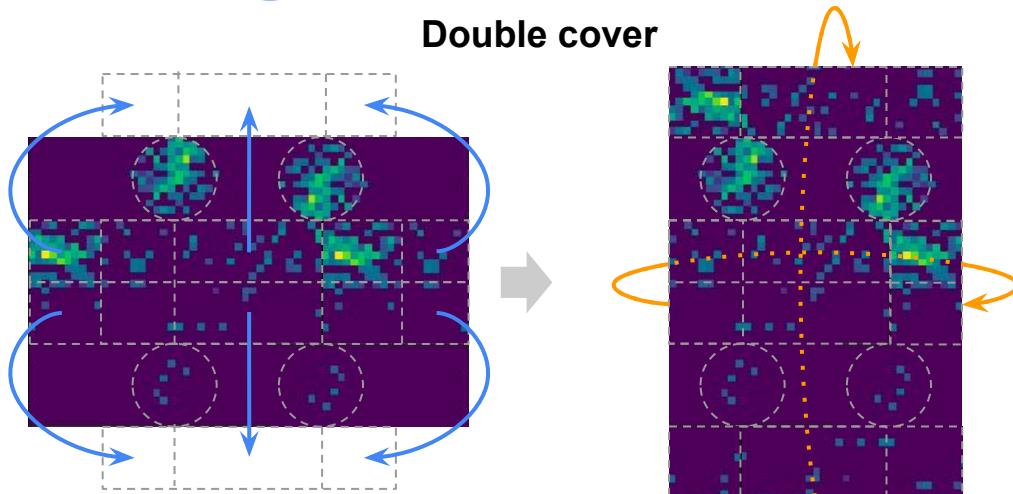


'Double cover' images



'Padding' the image improves accuracy for some events

- Original image 'slices' along barrel at arbitrary position
- Some events have rings that span this slice
- Repeat part of the image after rotating tank to help CNN learn events where ring is sliced



Rearranging and duplicating in a more complex pattern has additional advantages

- All segments appear exactly twice
- **Circular boundary conditions** in both directions
- Minimal blank space

Topological map to square

$$X_{\pm} = W(\rho, z) \frac{\pi \pm \phi}{2\pi}$$

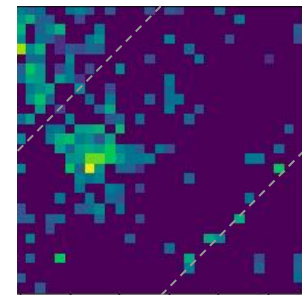
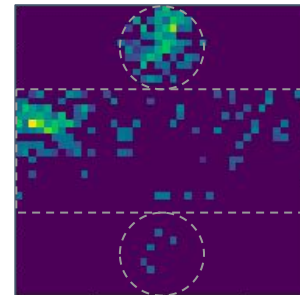
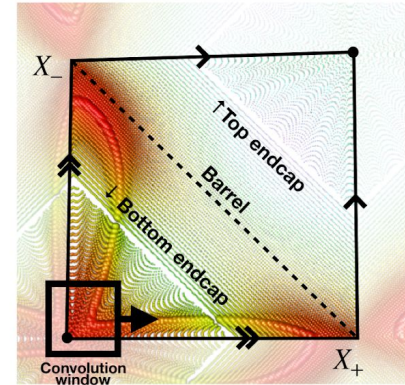
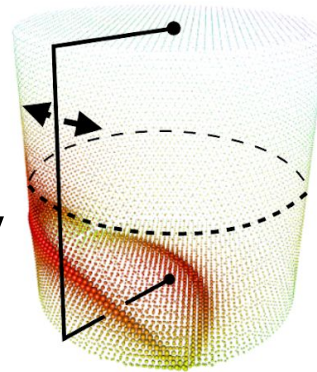
$$W(\rho, z) = \sqrt{\frac{\rho^2 + 2Rz + RH}{R^2 + RH}}$$

Solve differential eq. for constant Jacobian

$$dX_+ dX_- = \left| \frac{\partial(X_+, X_-)}{\partial(\rho, \phi)} \right| d\rho d\phi$$

Alternative map onto square with boundary conditions preserving topology of cylinder

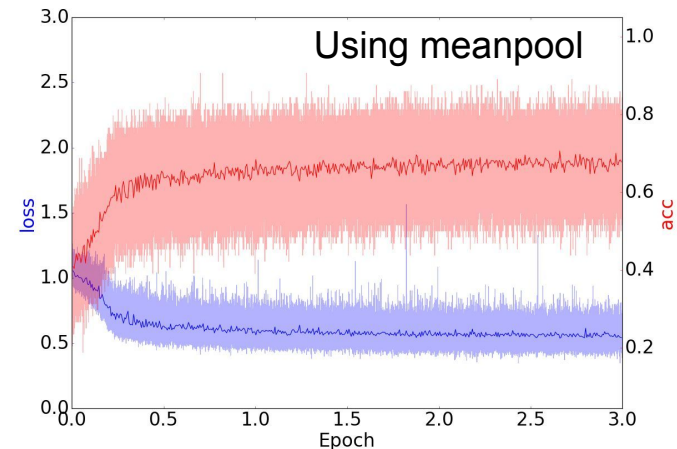
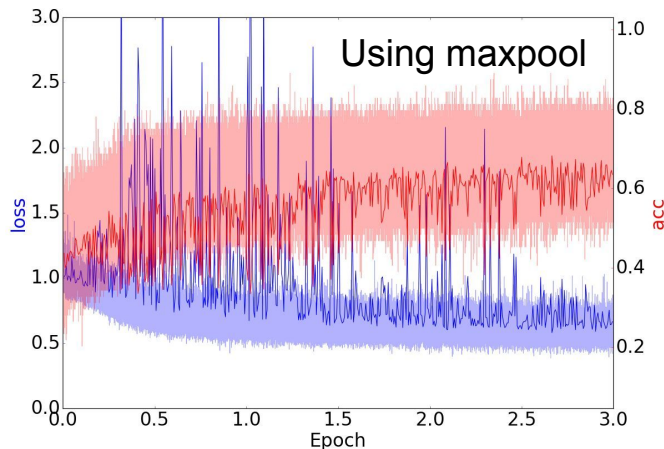
- Cut open along barrel to centre of end caps (solid line)
- Deform onto square, keeping density of PMTs constant
- Place mPMTs onto nearest pixel
- Use boundary conditions identifying edges of square (indicated by arrows)
 - Pad image with copy of pixels from the corresponding edge



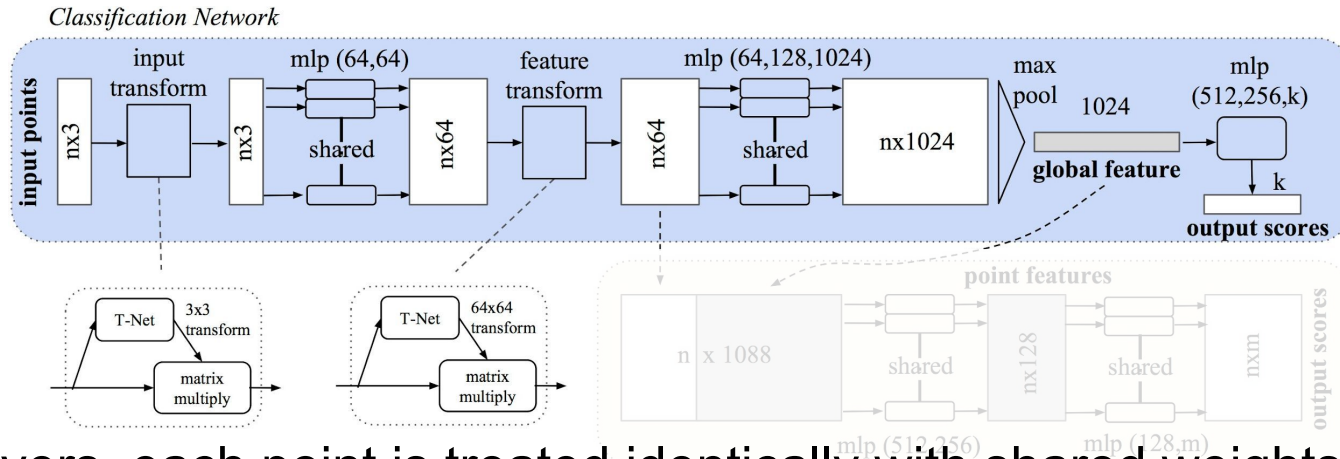
PointNet architecture

Some changes to standard PointNet give improvements

- Severe overfitting until max. features reduced from 1024 to 256
 - Possibly due to limited batch size with larger network
 - Data augmentation could also help
- We find that mean pool works better than standard max pool here
 - PointNet usually picks key points to learn features, but aggregating information from all points seems better for our tasks



PointNet architecture



In MLP layers, each point is treated identically with shared weights

- Similar to each pixel treated the identically in a CNN
- But without downsampling, information does not transfer between points

Instead ‘T-Nets’, resembling PointNet, learn transformations of the points

- Linear transformation is learnt to e.g. rotate all input vectors
- Feature transform allows global information to affect individual points

Single downsampling layer at the end of the network collapses all points

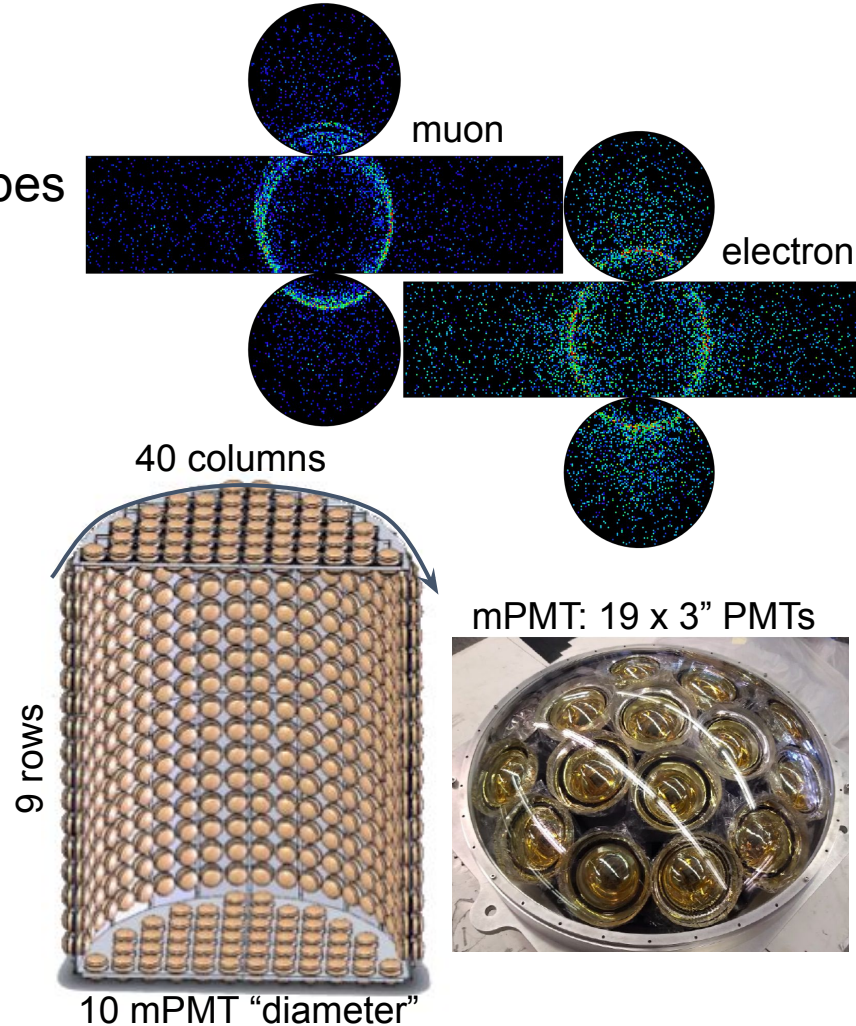
Particle type classification

Initial studies to classify $\mu / \pi^0 / e / \gamma$ particle types

- μ vs e is classified extremely well by traditional methods (>99% accuracy)
- e vs π^0 works reasonably well, but could be improved
- e vs γ has not been used successfully with traditional methods

Simulated 3M of each type in IWCD detector

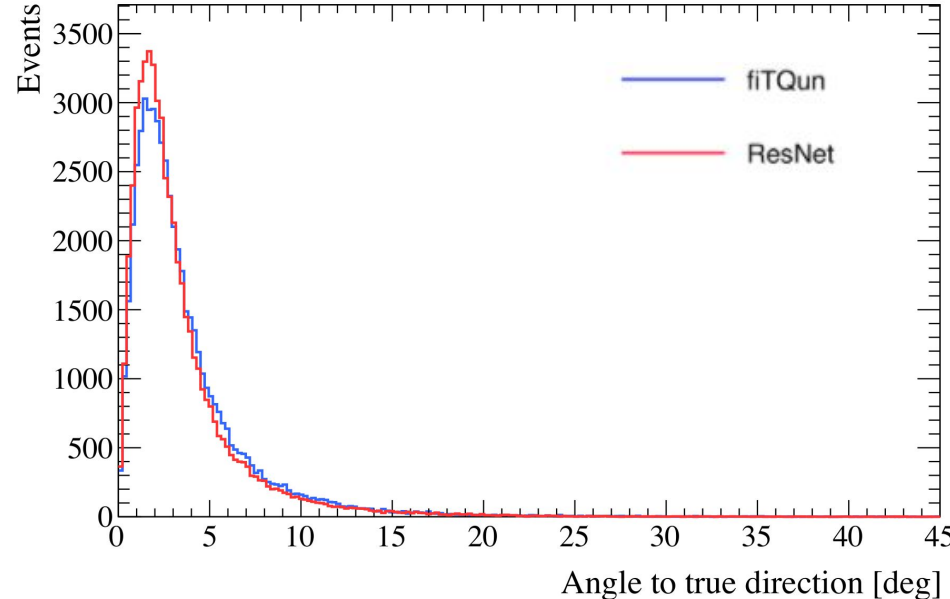
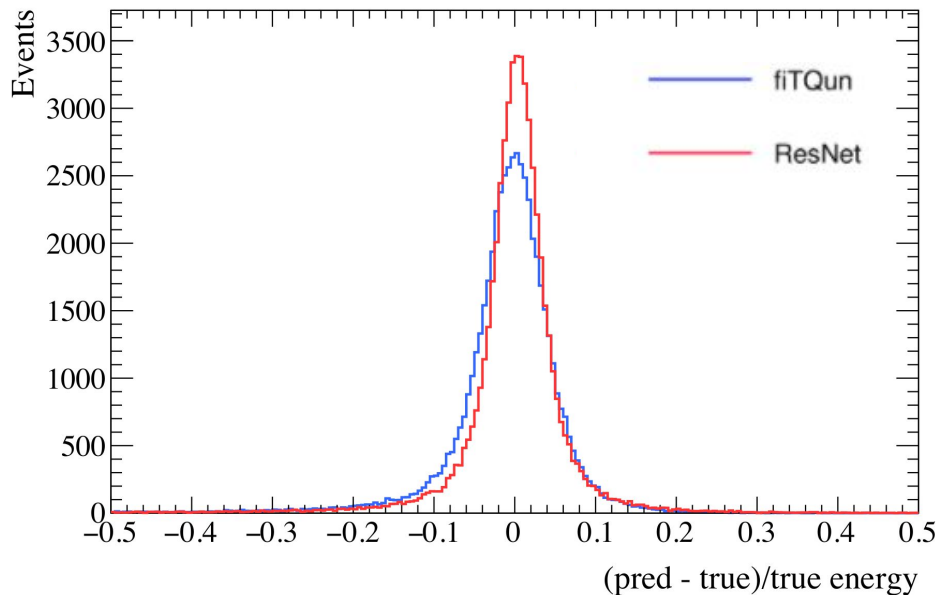
- 0 - 1 GeV energy above threshold
- Uniform positions, isotropic directions
- Split full dataset into 50% : 10% : 40% for training : validation : testing



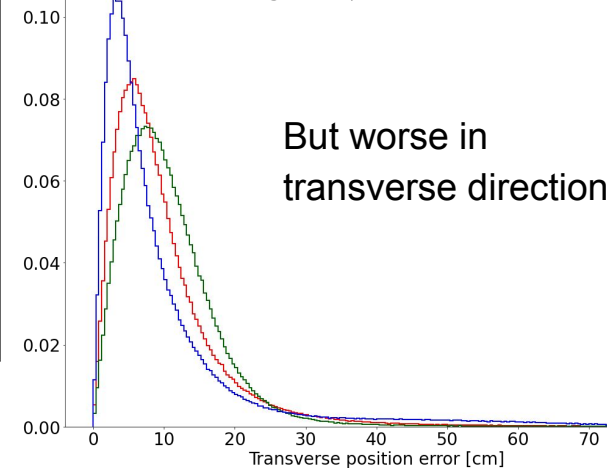
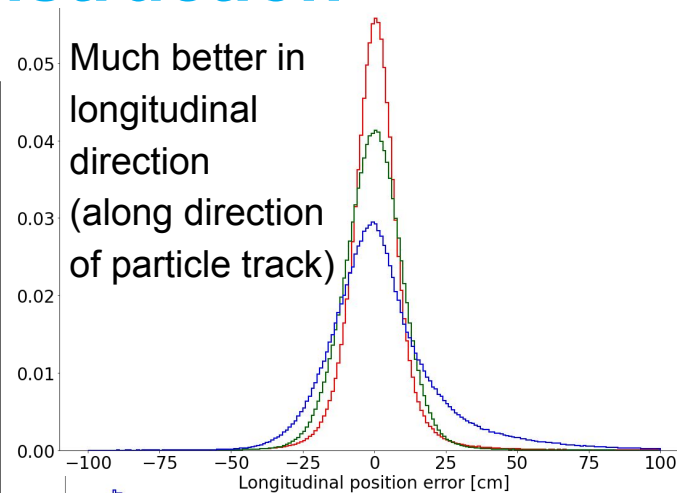
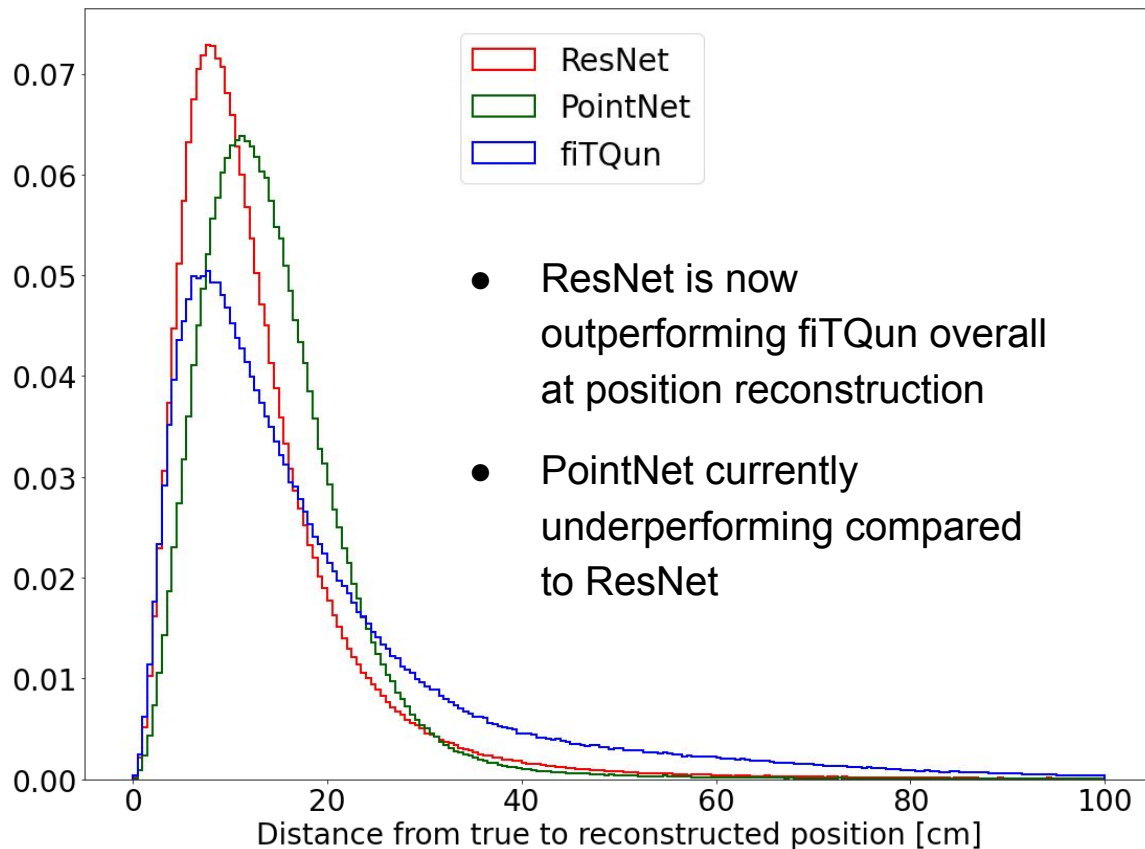
Position, direction, energy reconstruction

Similar ResNet and PointNet architectures as used for classification

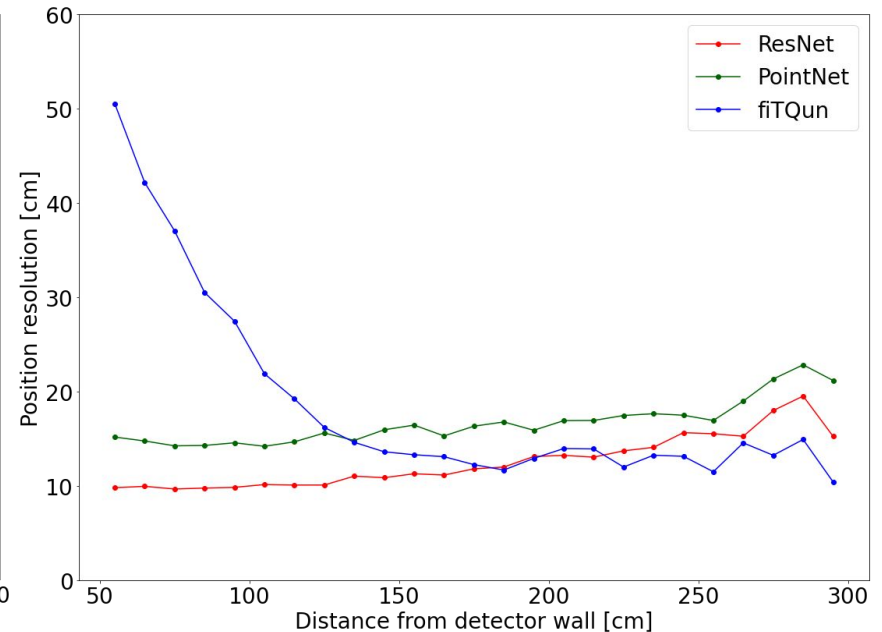
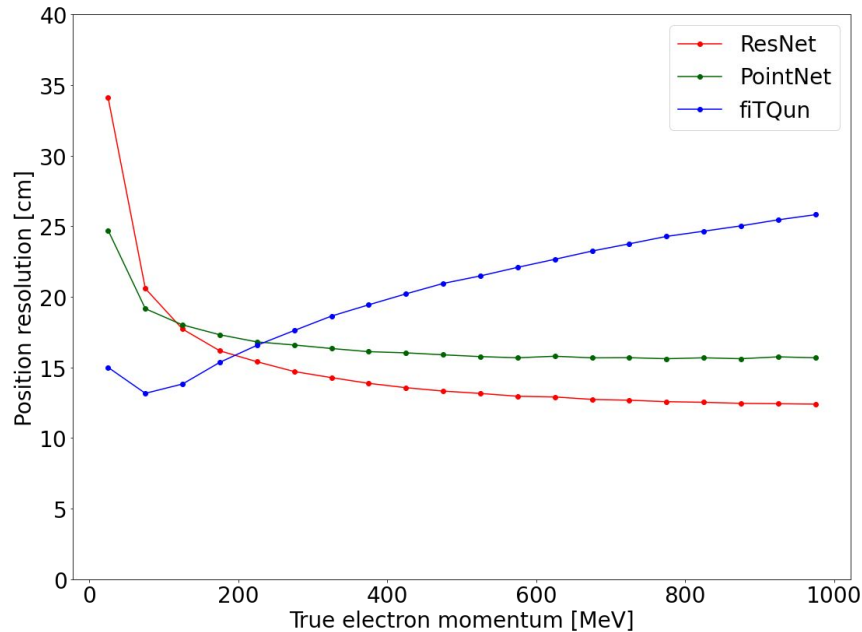
- Output reconstructed quantities instead of classification variables
- Use Huber loss to minimise true-reconstructed residuals
- ResNet is outperforming fiTQun at energy and direction reconstruction



Position, direction, energy reconstruction

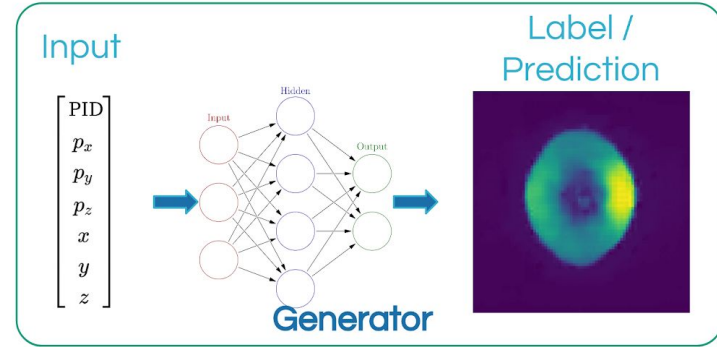
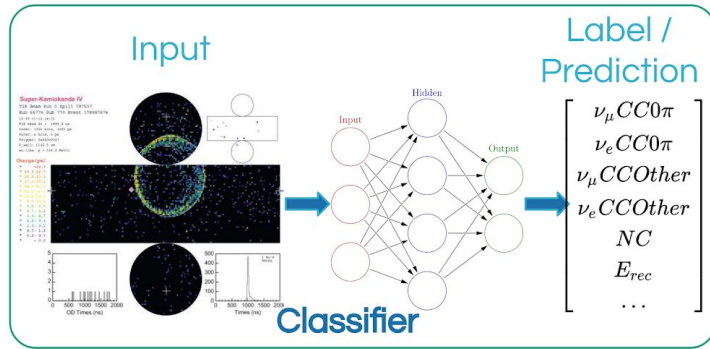


Position, direction, energy reconstruction



- Improvement in reconstruction with ML mainly in events close to detector wall
 - Approximations in likelihood calculation break down when close to PMTs
 - Could allow expansion of detector fiducial volume to allow increased statistics
- ML reconstruction could be improved at lower energy
 - potentially struggles to learn reconstruction of sparse events

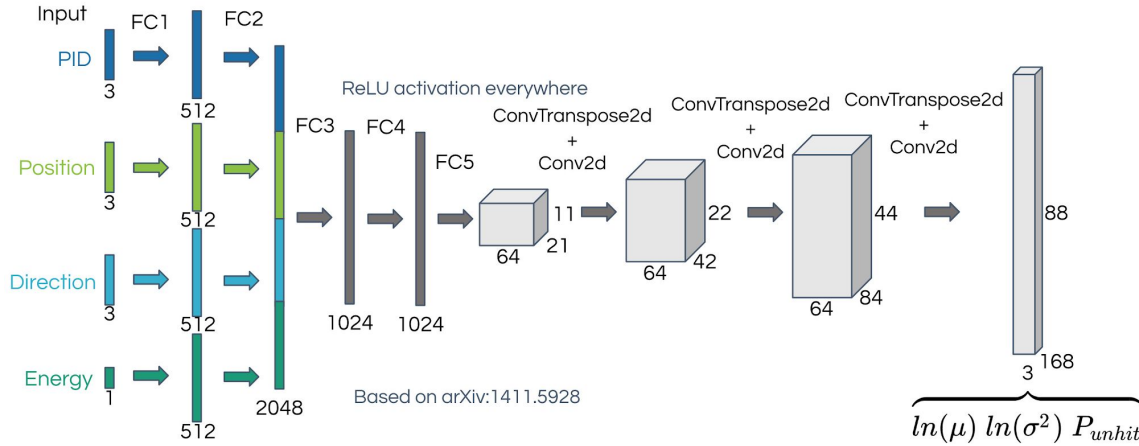
Cherenkov ring generator



Investigating hybrid method using generative network

- Generative network can predict PMT hit charge and time
- Use to replace likelihoods in traditional reconstruction
- Combine learning ability of CNN with physics domain knowledge of traditional reconstruction
- Simple replacement for existing reconstruction in full analysis chain

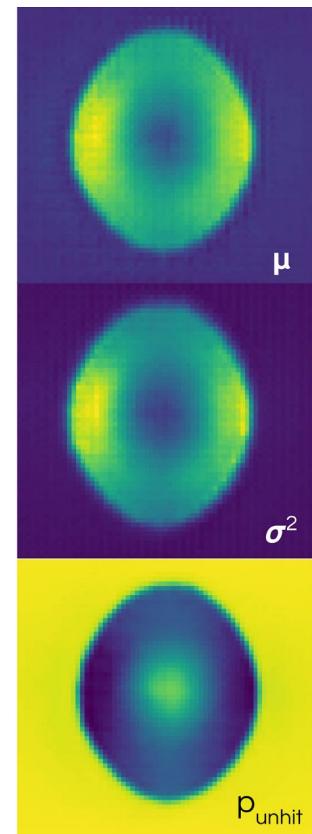
Cherenkov ring generator



$$\text{Loss} = -\ln(\mathcal{L}) = -\sum_{unhit} \ln(P_{unhit}) - \sum_{hit} \ln(1 - P_{unhit}) - \sum_{hit} \frac{1}{2} \left[\ln(2\pi\sigma^2) + \frac{(q_{obs} - \mu)^2}{\sigma^2} \right]$$

Network outputs likelihoods for hits observed at PMT

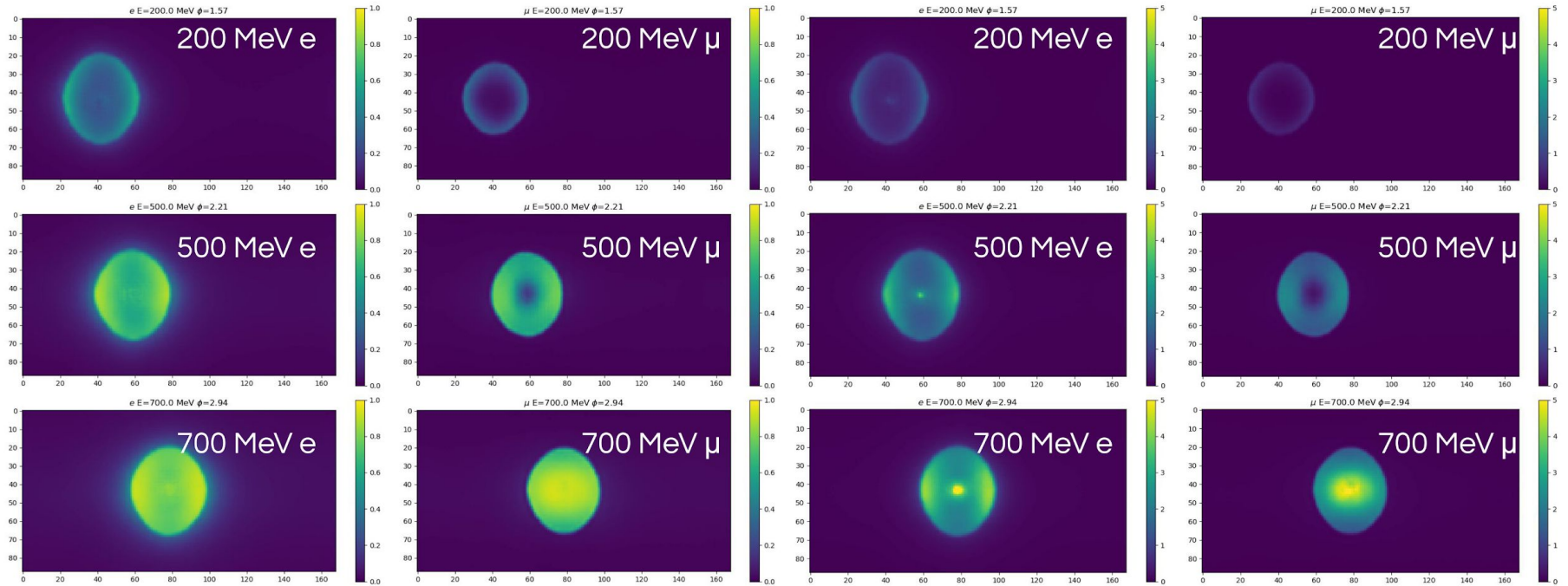
- Probability of PMT being hit
- Gaussian pdf (μ , σ) for charge



Cherenkov ring generator

Hit probability
X
Mean charge

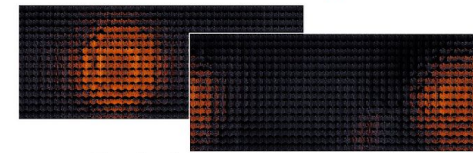
Hit probability



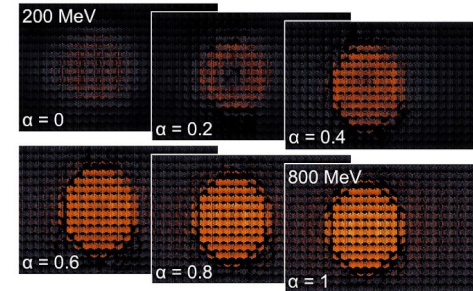
Generative networks

Also considering using generative networks for improved detector systematics

- Train generative network to reproduce real data: removed dependence on MC
- Train GAN to take simulated event and make it look like real data
 - Reduce detector systematics by ‘fixing’ mismodelled detector simulation
- Initial work on VAE showed some promise, but struggled with noise and sharp details
- Now we are investigating GANs

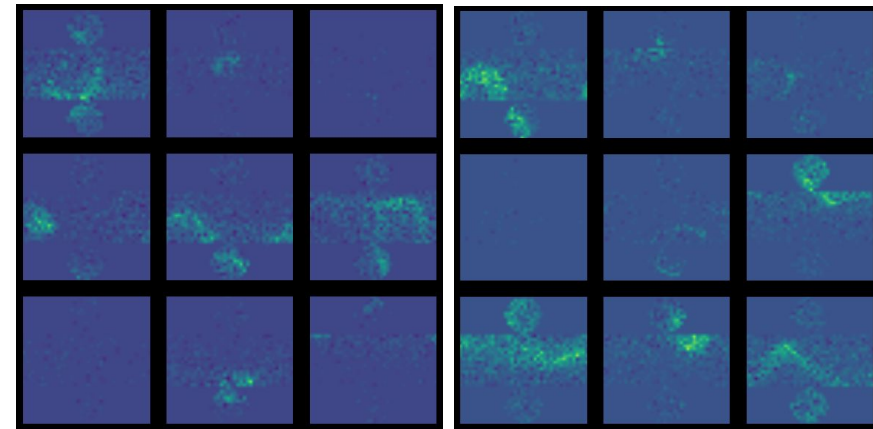


Randomly generated new events



Interpolate between 200 MeV and 800 MeV events

arXiv:
1911.02369



GAN generated events

Geant4 simulated events