

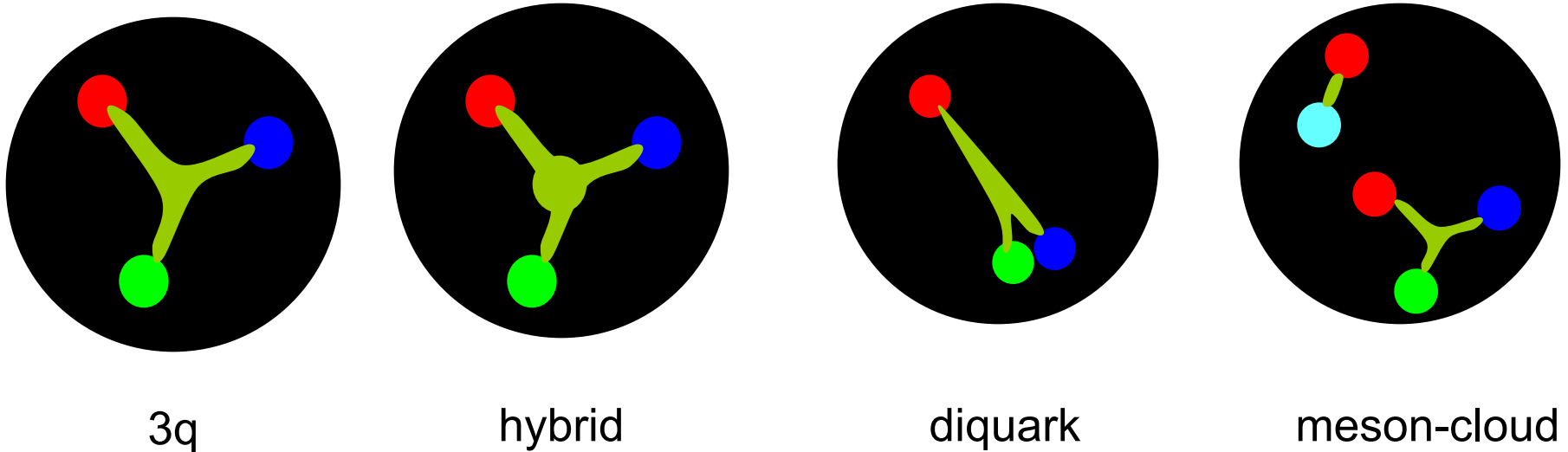
# **Colored and Colorless Correlations in Hadrons**

**Takashi Nakano**

Research Center for Nuclear Physics, Osaka University

**IUPAP Nuclear Science Symposium @ SURA, June 14-15, 2022**

# What are effective degrees of freedom ?



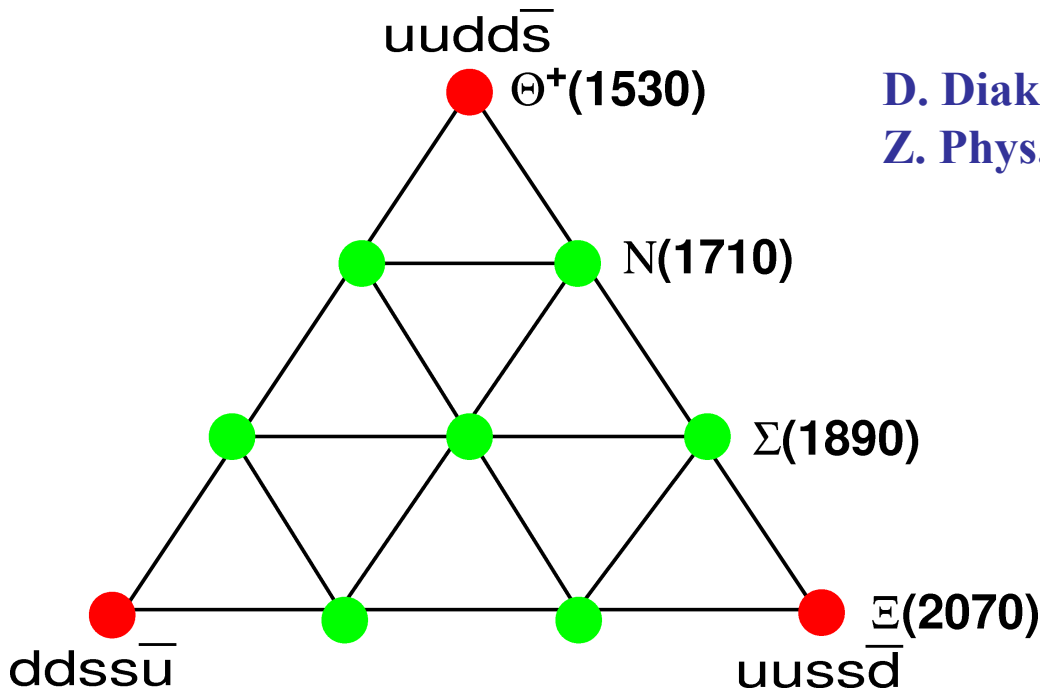
$$|B = 1 \rangle = a_0 |3q \rangle + a_1 |(qq)(qq)\bar{q} \rangle + a_2 |MB \rangle + \dots$$

- **How can we learn about the structure of the hadrons from their production and decay?**

# Pentaquark

The antiquark has a different flavor than the other 4 quarks.

D. Diakonov, V. Petrov, and M. Polyakov,  
*Z. Phys. A* 359 (1997) 305.



- **Exotic:  $S=+1$**
- **Low mass: 1530 MeV**
- **Narrow width:  $\sim 15$  MeV**
- **$J^P=1/2^+$**

$$M = [1890 - 180 \cdot Y] \text{ MeV}$$

# Baryon masses in constituent quark model

$$m_u \sim m_d = 300 \sim 350 \text{ MeV}, m_s = m_{u(d)} + 130 \sim 180 \text{ MeV}$$

- Mainly 3 quark baryons:

$$M \sim 3M_q + (\text{strangeness}) + (\text{symmetry})$$

- $\pi$ , K, and  $\eta$  are light:

Nambu-Goldstone bosons of spontaneously broken chiral symmetry.

- 5-quark baryons, naively:

$$M \sim 5M_q + (\text{strangeness}) + (\text{symmetry})$$

1700~1900 MeV for  $\Theta^+$



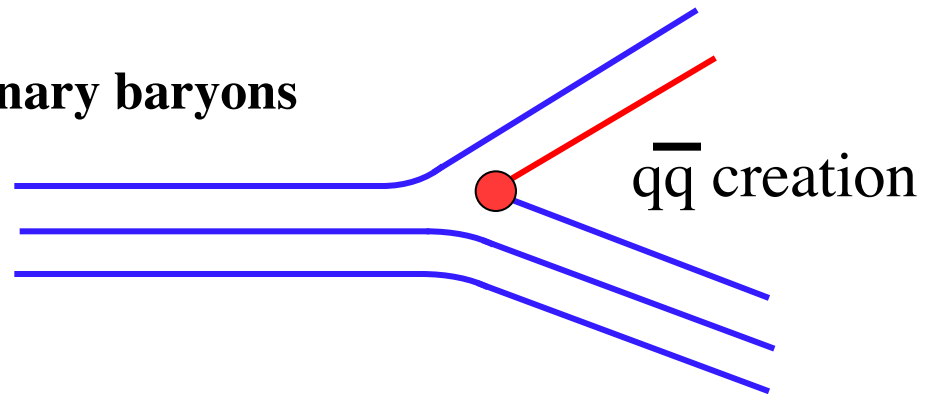
# Fall-apart decay problem

- DPP predicted the  $\Theta^+$  with  $M=1530\text{MeV}$ ,  $\Gamma<15\text{MeV}$ , and  $J^P=1/2^+$ .
- Naïve QM (and many Lattice calc.) gives  $M=1700\sim 1900\text{MeV}$  with  $J^P=1/2^-$ .
- But the **negative parity** state must have very wide width ( $\sim 1\text{ GeV}$ ) due to “fall apart” decay.

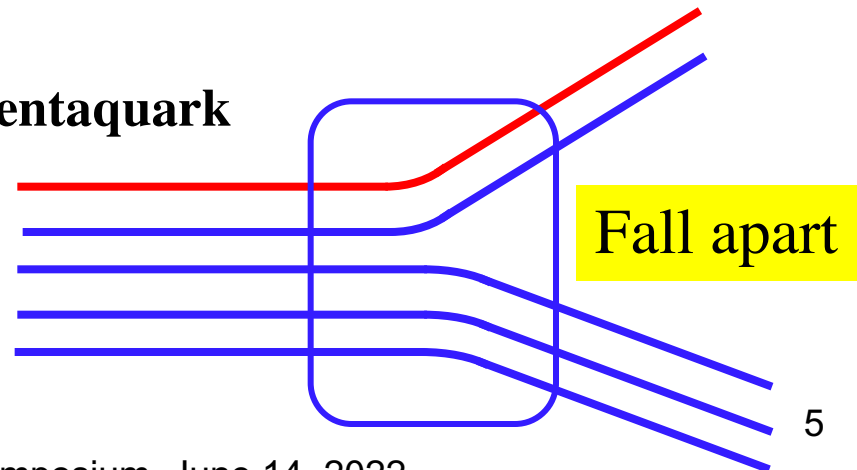
## Positive Parity?

- Positive parity requires P-state excitation.
- Expect state to get heavier.
- Need counter mechanism.

Ordinary baryons



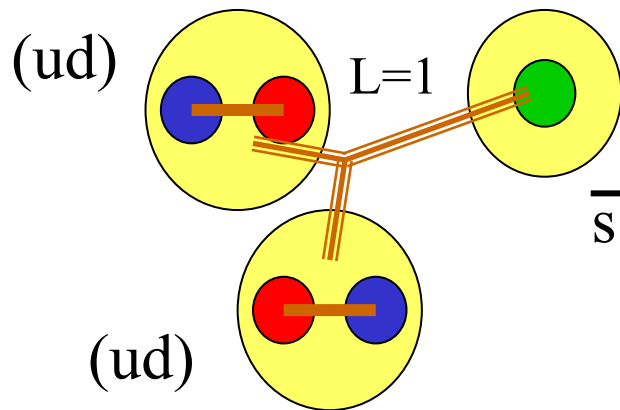
For pentaquark



# A di-quark model for pentaquarks

$$[ud][ud]\bar{s} \quad \text{JW hep-ph/0307341}$$

$$\text{JM hep-ph/0308286}$$



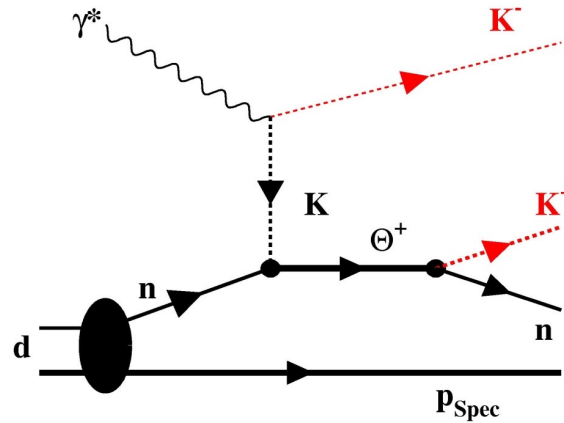
L=1, one unit of orbital angular momentum needed to get  $J^P=1/2^+$

Uncorrelated quarks:  $J^P = 1/2^-$

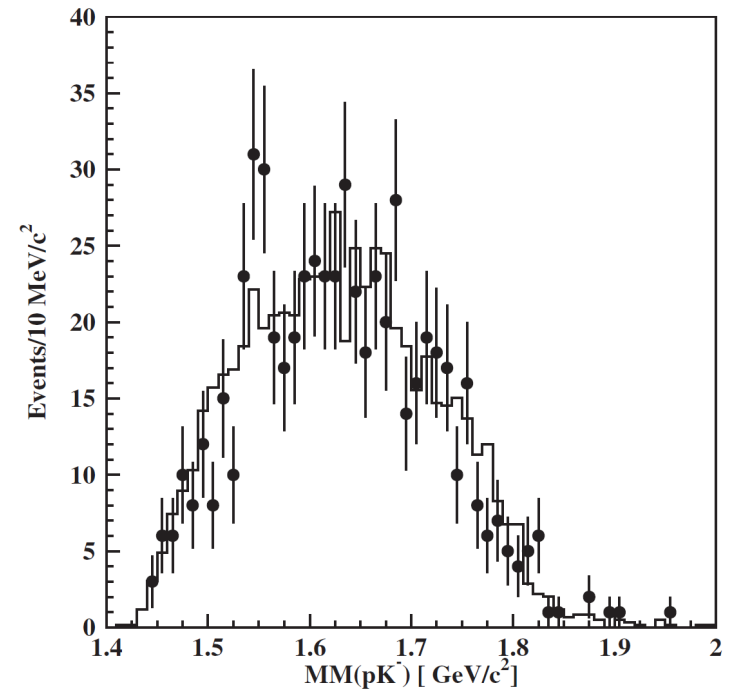
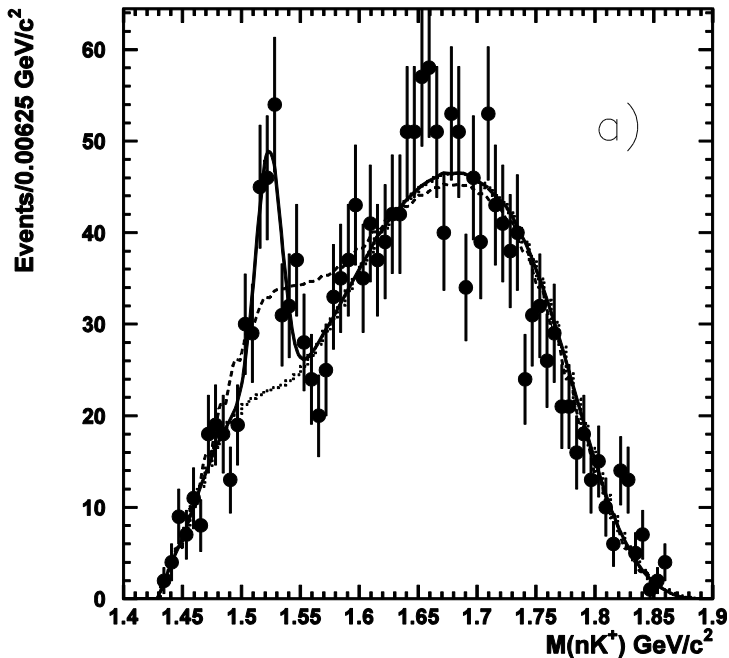
**Decay Width:**  $\langle [ud][ud]\bar{s} \mid [uud][u\bar{s}] \rangle = \frac{1}{2\sqrt{6}} \Gamma \approx \frac{200 \text{ MeV}}{(2\sqrt{6})^2} \approx 8 \text{ MeV}$

# Pentaquark $\Theta^+$ search in photo-production

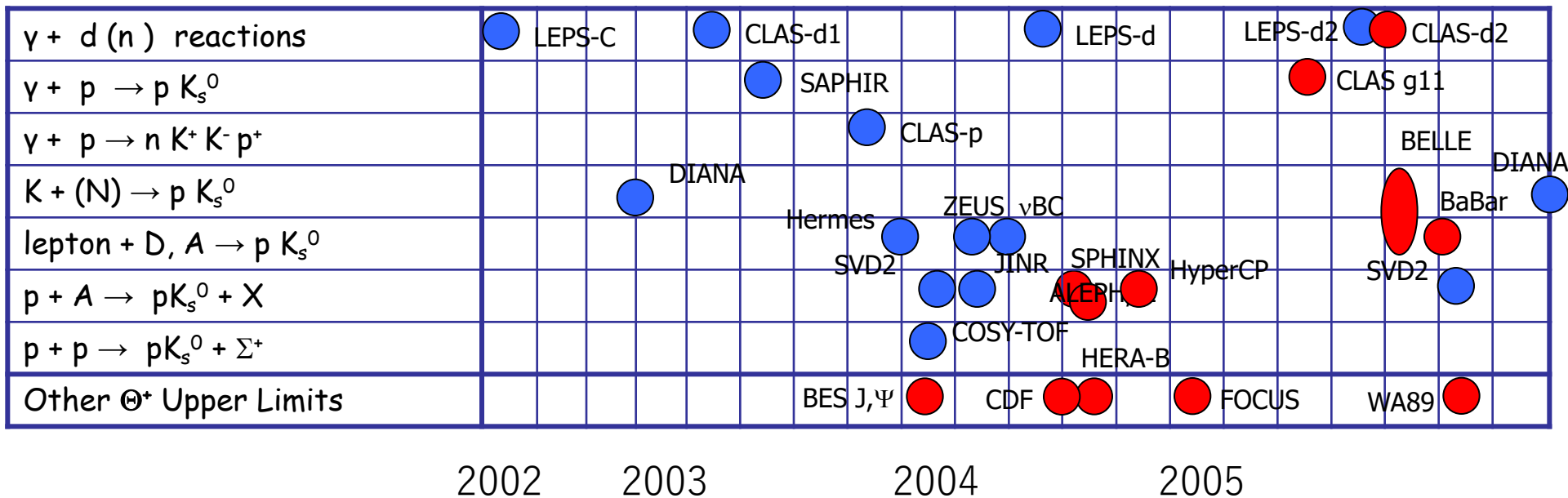
LEPS  
positive



CLAS  
negative



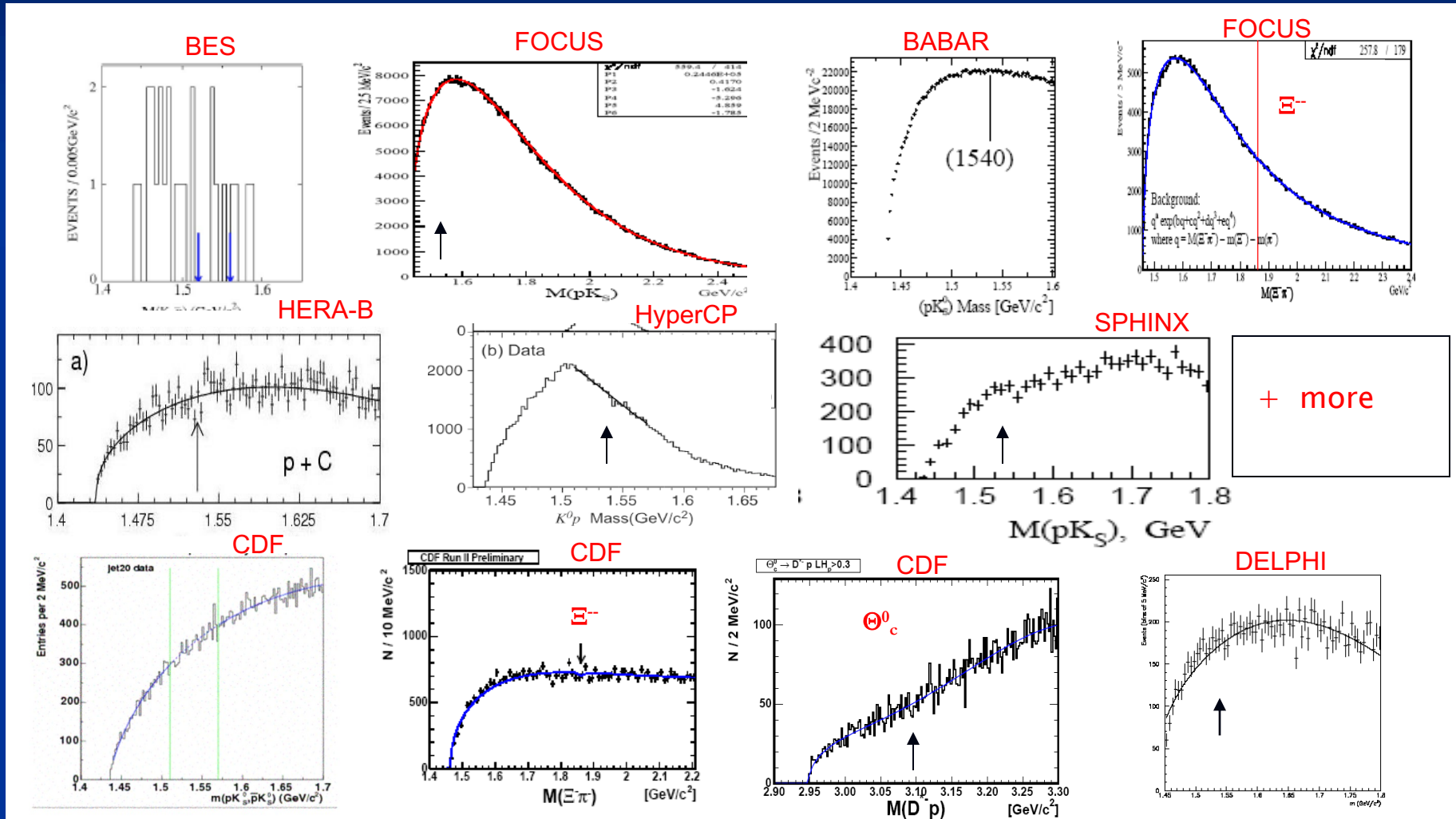
# Time dependent experimental status of $\Theta^+$



Blue circle : Positive result

Red circle : Negative result

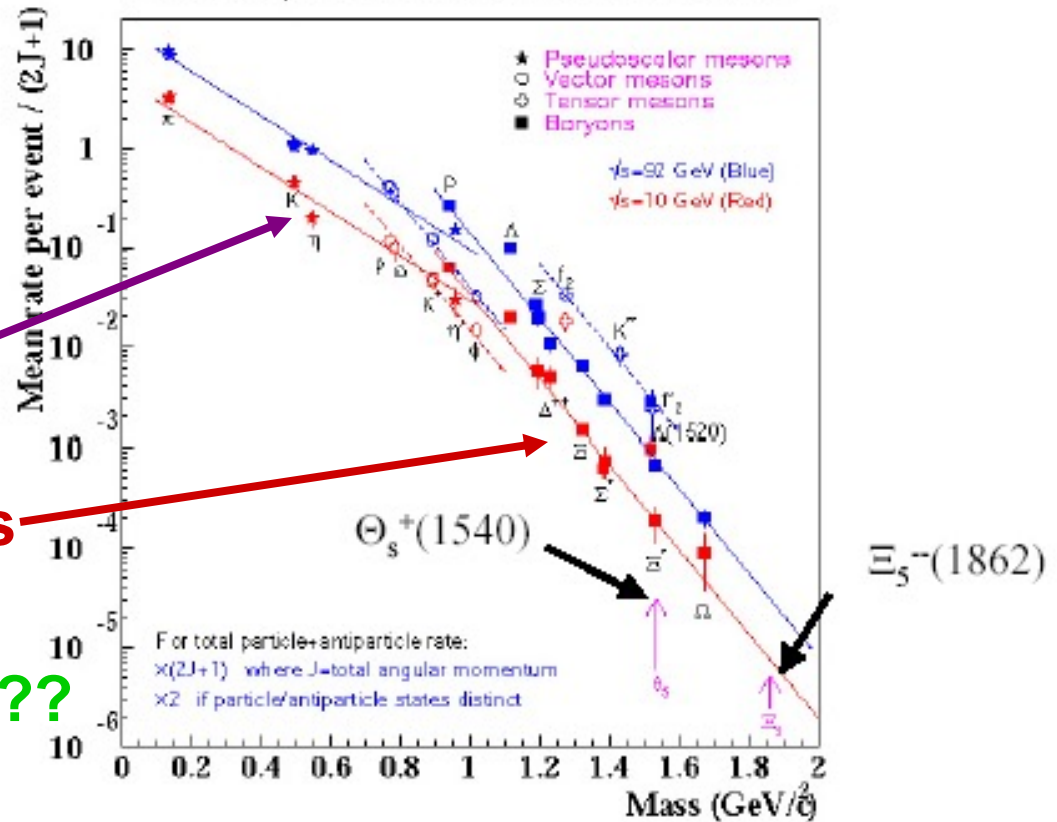
# Null results for Pentaquarks in High energy experiments





# Hadron Rate in $e^+e^- \rightarrow \text{Hadron}$

Hadron production in  $e^+e^- \rightarrow \text{Hadrons}$



Slope for mesons

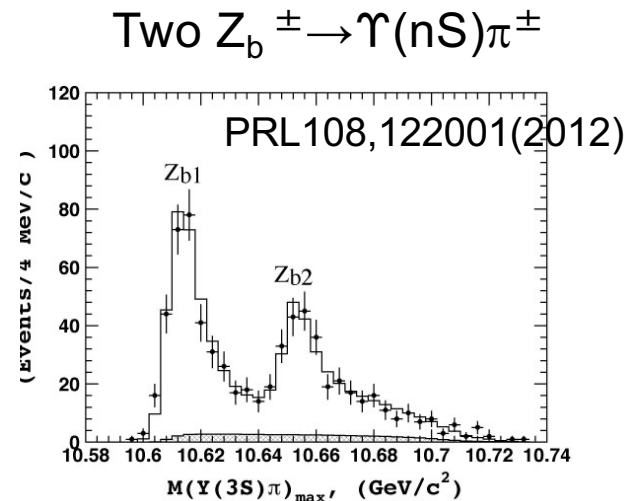
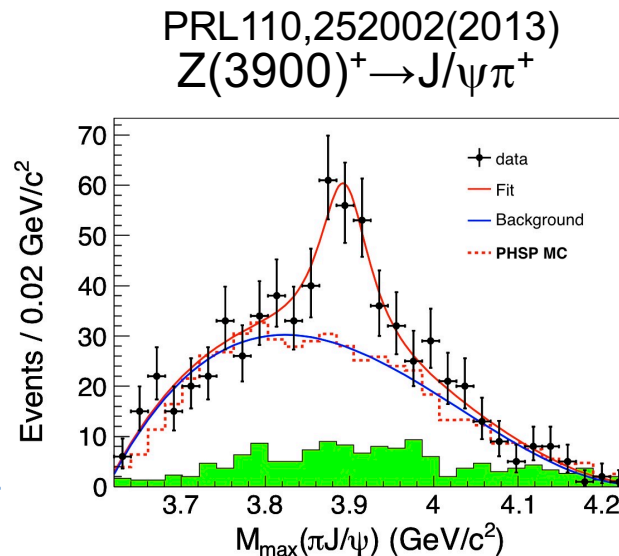
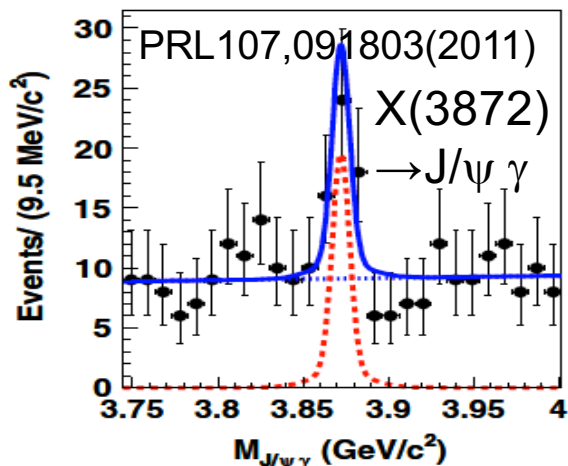
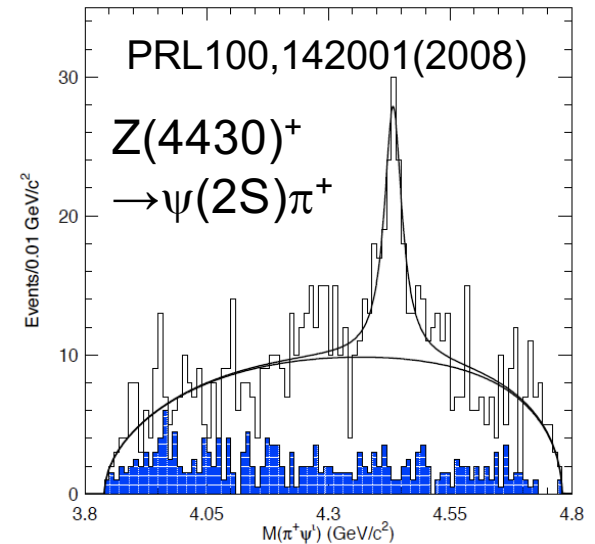
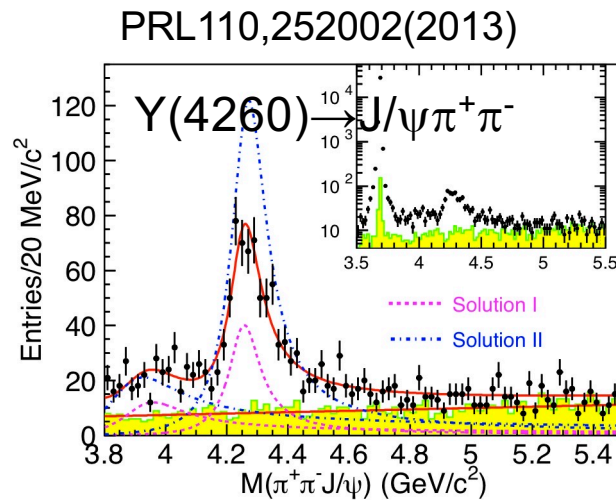
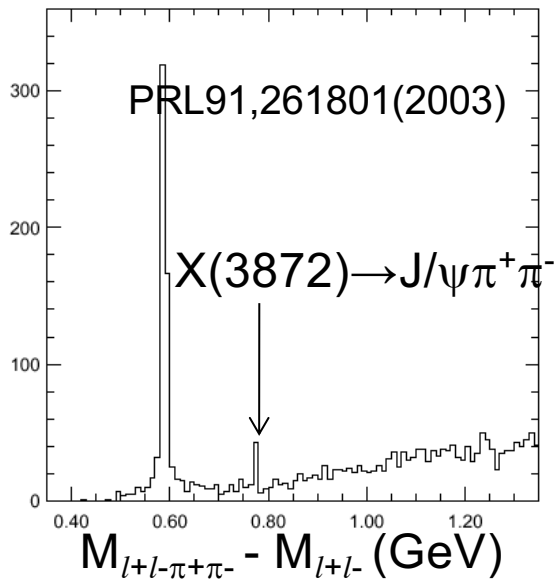
Slope for baryons

Slope for pentaquarks??

Assuming the Pentaquark production is the same as baryon production we expect the total production of  $\Theta_s^+$ ,  $\Xi_5^-$  per event continuum to be  $\Theta_s^+ = 7 \times 10^{-4}$ ,  $\Xi_5^- = 3. \times 10^{-5}$

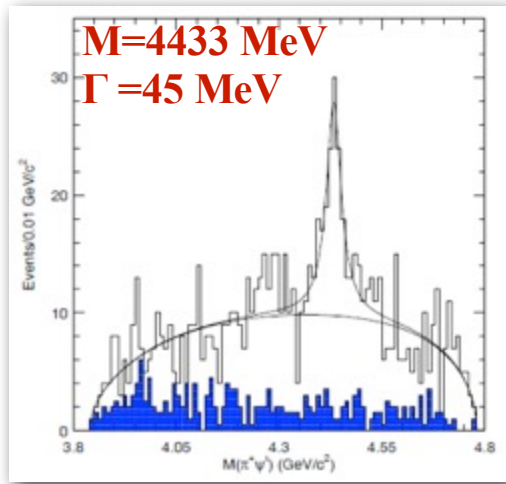
7/22/2004

# “XYZ” sensations at Belle

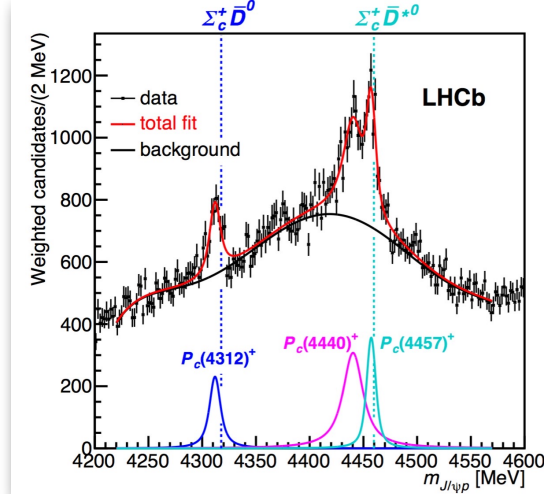


# Explicitly Exotic Hadrons

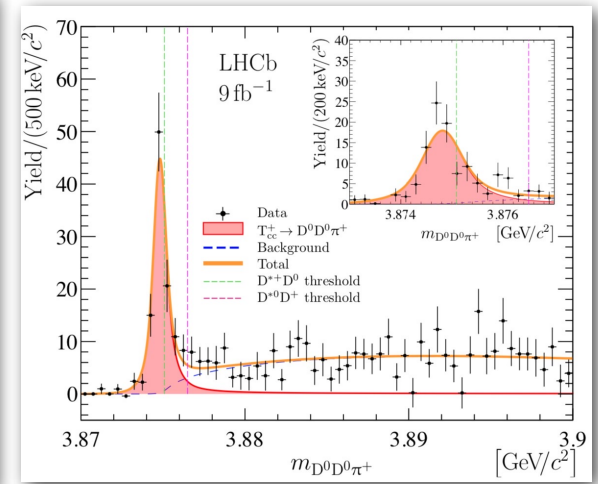
**$Z_c^+(4430)$**  Belle  
*PRL 100 (2008) 142001*



**$P_c(4312)$  ( $4440$ ) ( $4457$ )** LHCb  
*PRL 115 (2015), PRL 122 (2019)*



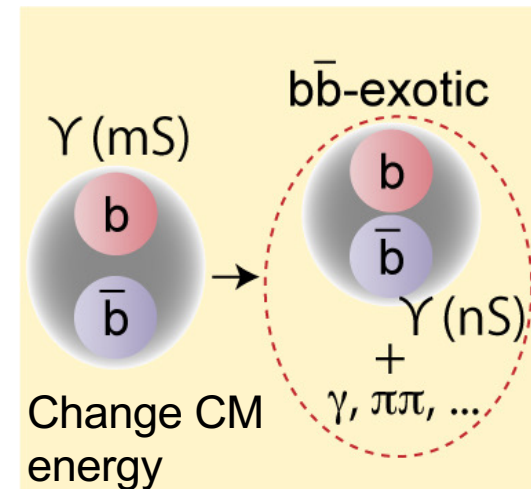
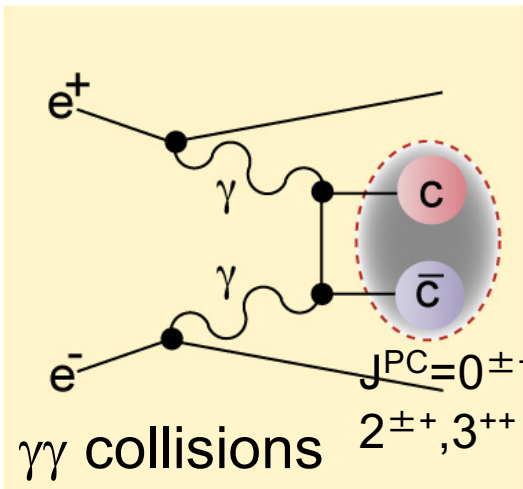
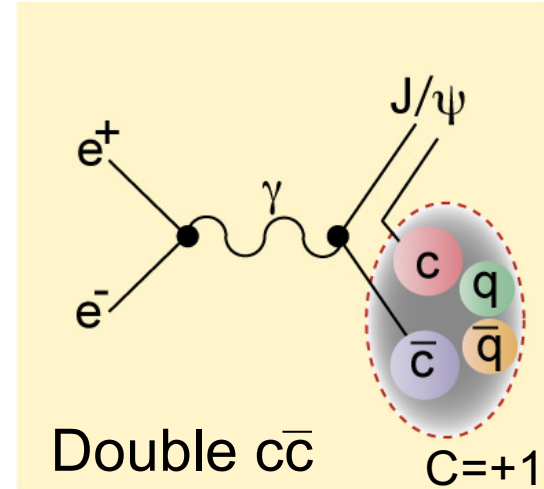
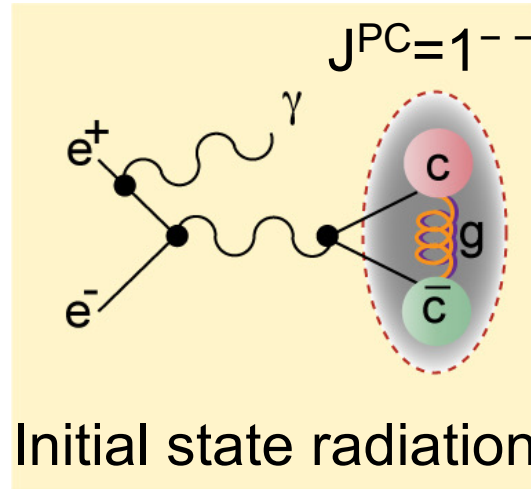
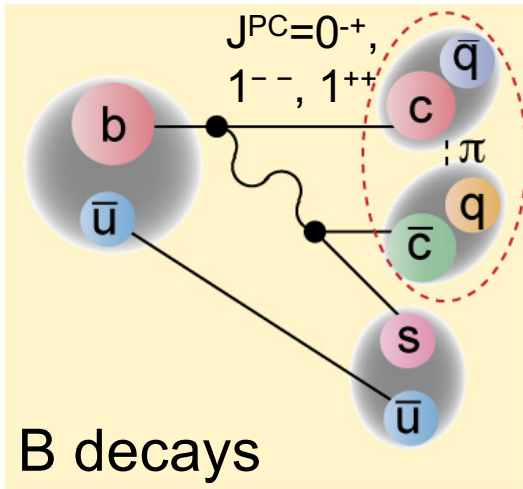
**$T_{cc}$**  LHCb  
*arXiv:2109.01038, 2109.01056*



These hadrons require *new components* beyond the minimum constituent quarks, ex. colorless meson  $\bar{q}q$  or colored diquark  $qq$ .



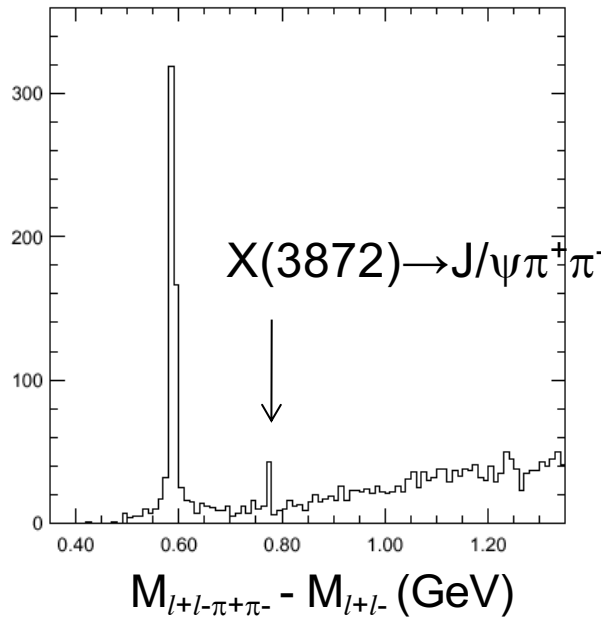
# Variety of recorded reactions



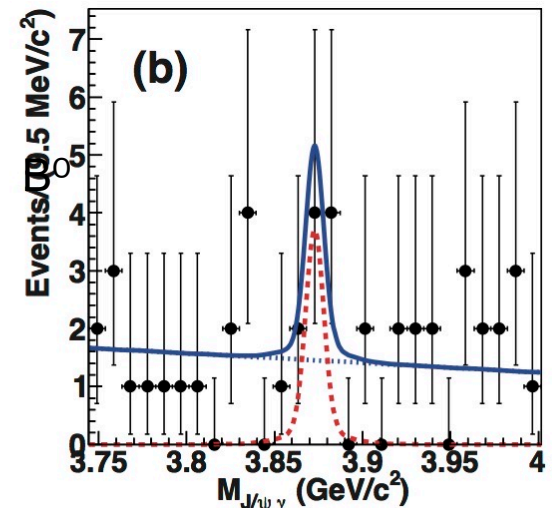
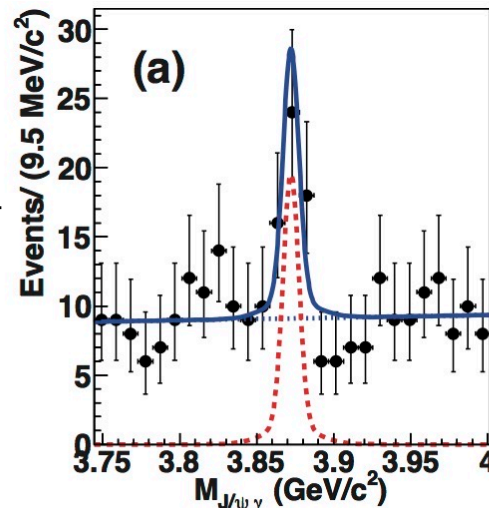
Allowed/favored production process depends on quantum numbers of a hadron.

# Spin-Parity of X(3872)

Belle PRL91,261801(2003)



$X(3872) \rightarrow J/\psi \gamma; C=+1$



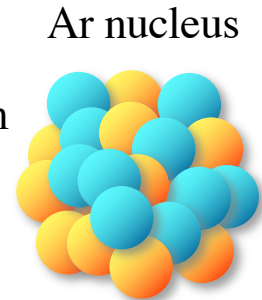
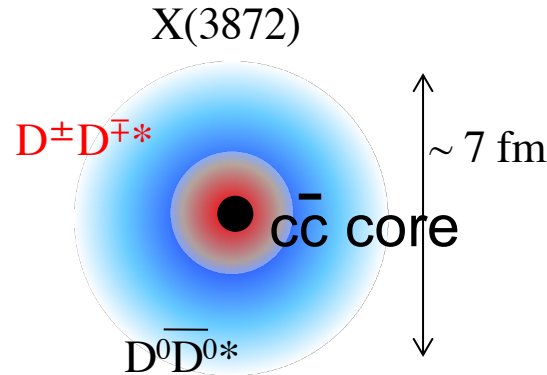
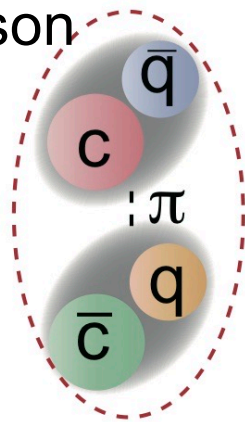
Belle PRL07,091803(2011)

$J^{PC}=1^{++}$  (Belle, BaBar, CDF, LHCb) from  $J/\psi \pi^+\pi^-$  angular distribution.  
(PRL110, 222001(2013) and cited papers)

$\text{Br}(X(3872) \rightarrow D^0 \bar{D}^{*0})$  is about  $\text{Br}(X(3872) \rightarrow J/\psi \pi^+\pi^-) \times 10$ .

# Admixture : Plausible interpretation for X(3872)

Meson-meson molecule



E. J. Eichiten et al. Phys. Rev. D 73, 014014 (2006);  
 A. M. Badalin et al. Phys. Rev.D 85, 031103 (2012);  
 S. Takeuchi, K. Shimizu and M.Takizawa PTEP2014, 123D01(2014).

$\bar{D}D^*$  component is coupled with the same  $J^{PC}$   $c\bar{c}$ ,  $\chi_{c1}(2P)$  (unseen).

→ can explain  $\text{Br}(X \rightarrow D^0 \bar{D}^{*0}) / \text{Br}(X \rightarrow J/\psi \pi^+ \pi^-)$  is about 10.

→ pure molecule; too fragile to have prompt produced in Tevatron/LHC.

→ another  $\chi_{c1}(2P)$  dominant state would become broad.

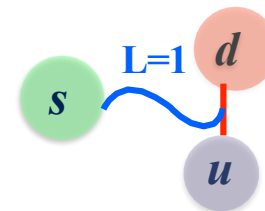
# A Puzzle in Baryon Spectroscopy

$\Lambda(1405)$  ( $1/2^-$ ) is the lowest negative parity baryon, even below  $N^*$ .

## 2 competing pictures:

### 1. *P-wave excitation*

uds with  $S=1/2$ ,  $L=1$  orbital excitation  $\Rightarrow J^\pi=1/2^-$  and  $3/2^-$



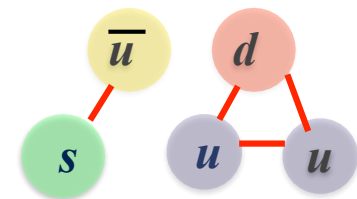
spin-orbit partner  $\Lambda(1520)$   $3/2^-$  is too high?

### 2. *Additional $qq^{\text{bar}}$ pair*

qqq( $qq^{\text{bar}}$ )  $L=0$  state (NO orbital excitation)

$S=1/2$ ,  $L=0 \Rightarrow J^\pi=1/2^-$

likely to be  $N(1/2^+) + \bar{K}(0^-)$  bound state

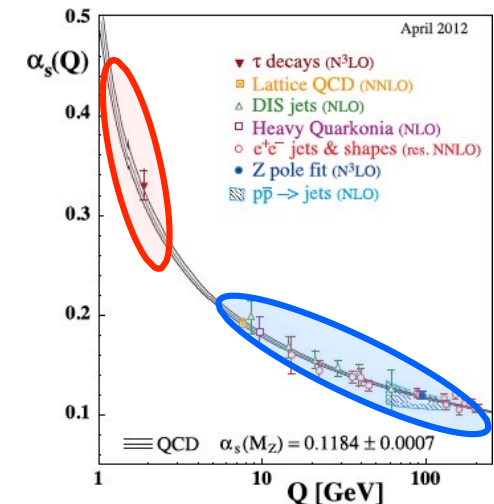
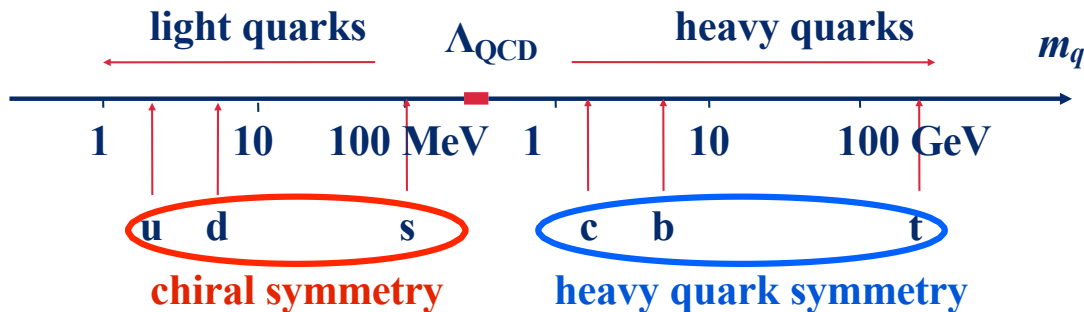


## Similar competition in

$X(3872)$  ( $1^+$ )  $\sim c\bar{c}^{\text{bar}}$  ( $^3P_1$ ) +  $DD^*\bar{\text{bar}}$  (S-wave)

# Heavy Quark Dynamics

Dynamics of heavy quarks (c, b) is perturbative and nonrelativistic. It decouples from light quarks.



Magnetic gluon coupling is suppressed.

$$\propto \frac{1}{m_Q}$$

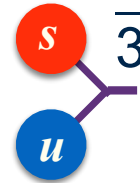
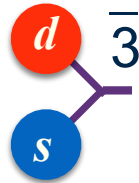
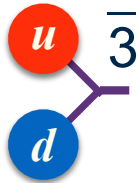
$\Rightarrow$  *Heavy quark symmetry* : Light quarks do not feel the mass and spin of the heavy quark (in the limit  $m_Q \rightarrow \infty$ ).

# Diquarks in Heavy Baryons

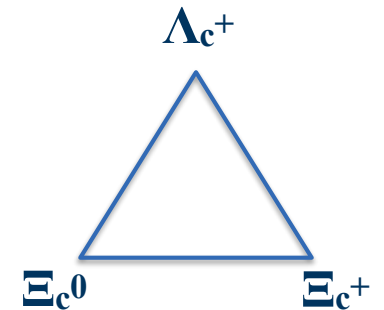
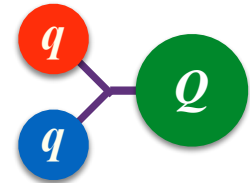
## ‡ Scalar diquark $S(0^+)$

$L=0, S=0$ , color  $3^{\text{bar}}$   $\rightarrow$  flavor  $SU(3)_f$   $3^{\text{bar}}$  (**antisym**):

$$[ud]=(ud-du), [ds]=(ds-sd), [su]=(su-us)$$



$\Rightarrow$  flavor  $3^{\text{bar}}$  HQ baryons:  $\Lambda_Q, \Xi_Q$

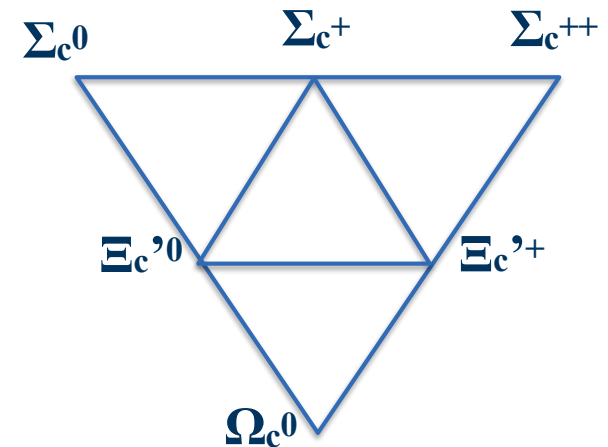


## ‡ Axial vector diquark $A(1^+)$

$L=0, S=1$ , color  $3^{\text{bar}}$   $\rightarrow$   $SU(3)_f$  6 (sym)

$uu, \{ud\}, dd, \{us\}, \{ds\}, ss$

$\Rightarrow$  flavor 6 HQ baryons:  $\Sigma_Q, \Xi_Q', \Omega_Q$

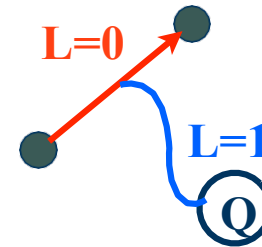


# Diquarks in Excited Heavy Baryons

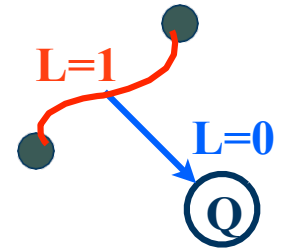
P-wave excited states of heavy baryons,  $\Lambda_Q$ ,  $\Sigma_Q$ , .. Two distinctive modes:  $\lambda$  and  $\rho$  modes

$E(\lambda\text{-mode}) < E(\rho\text{-mode})$   
generally in the quark model

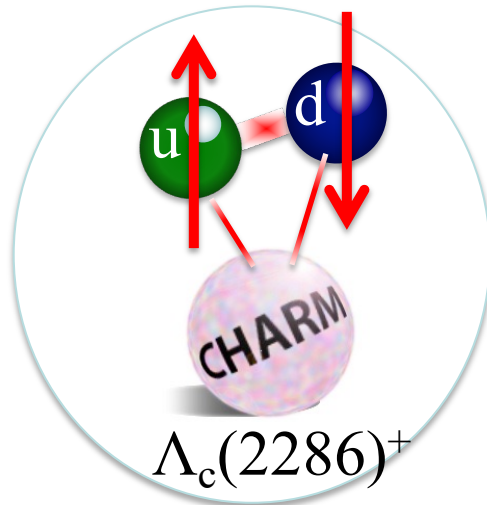
$\lambda$  mode



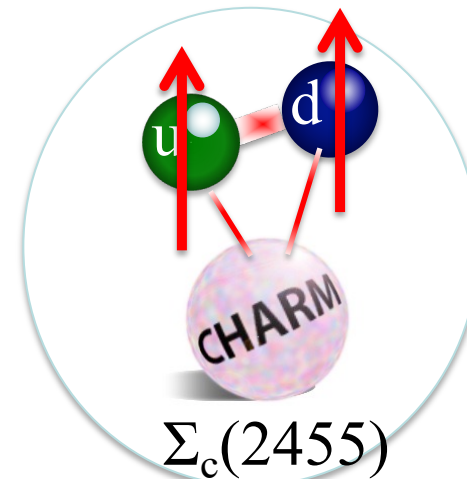
$\rho$  mode



Scalar diquark  
"good diquark"



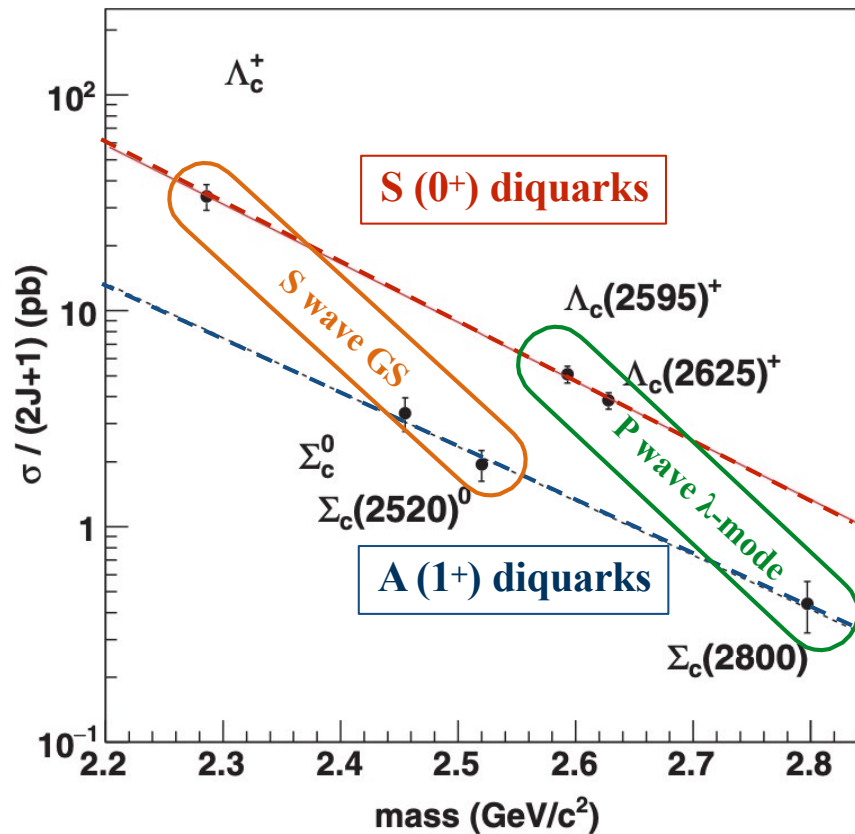
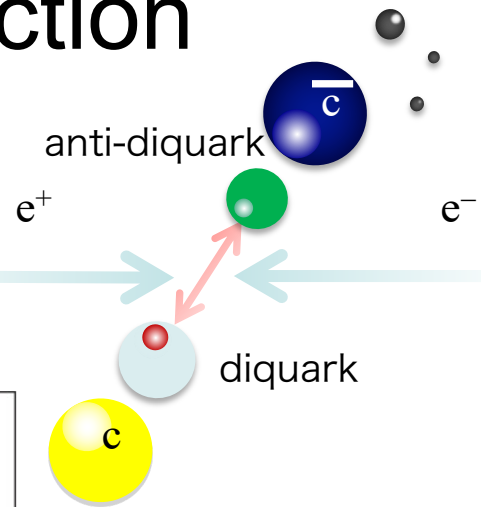
Axial vector diquark  
"bad diquark"



# Charm Baryon Production

Production cross sections of hyperons and charmed baryons from  $e^+e^-$  annihilation near  $\sqrt{s} = 10.52$  GeV

Belle Collaboration, Phys. Rev. D97, 072005 (2018)





# Diquark in Lattice QCD

**M(1<sup>+</sup>) - M(0<sup>+</sup>) for Lattice QCD**

*Alexandrou, de Forcrand, Lucini, PRL 97 (2006) 222002*

**Quench QCD, from gauge-invariant Qqq system**

**M(1<sup>+</sup>) - M(0<sup>+</sup>) ~ 200-220 MeV**

*Babich, et al., PR D76 (2007) 074021*

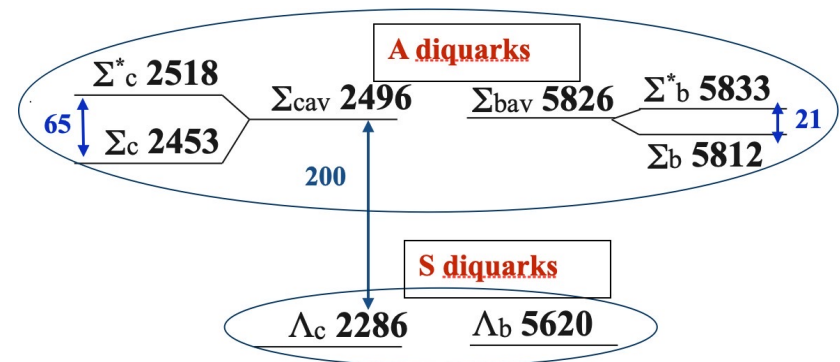
**Quench QCD, Landau gauge**

**M(1<sup>+</sup>) - M(0<sup>+</sup>) ~162 MeV**

*Y. Bi, et al., Chinese Physics C40 (2016)*

**Full QCD, Landau gauge**

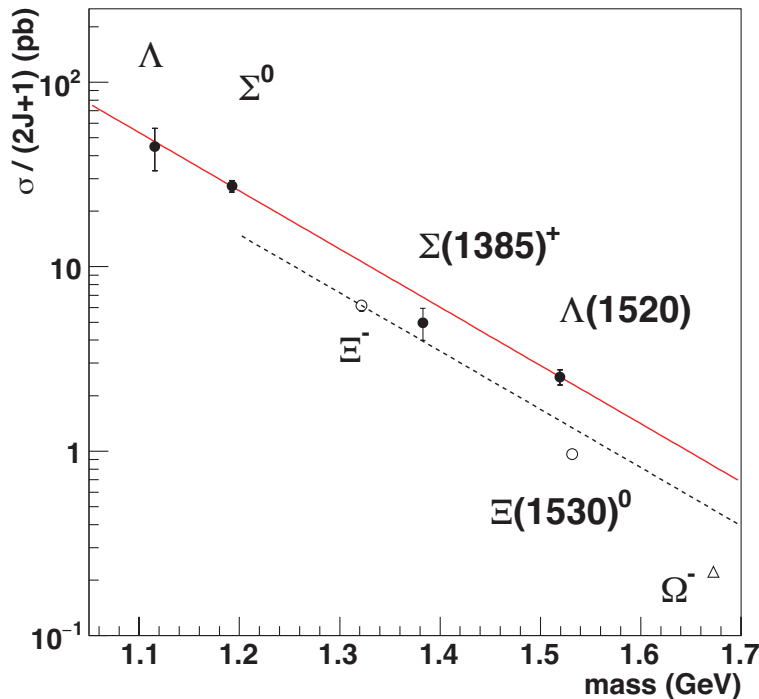
**M(1<sup>+</sup>) - M(0<sup>+</sup>) ~290 MeV**



# Hyperon Production

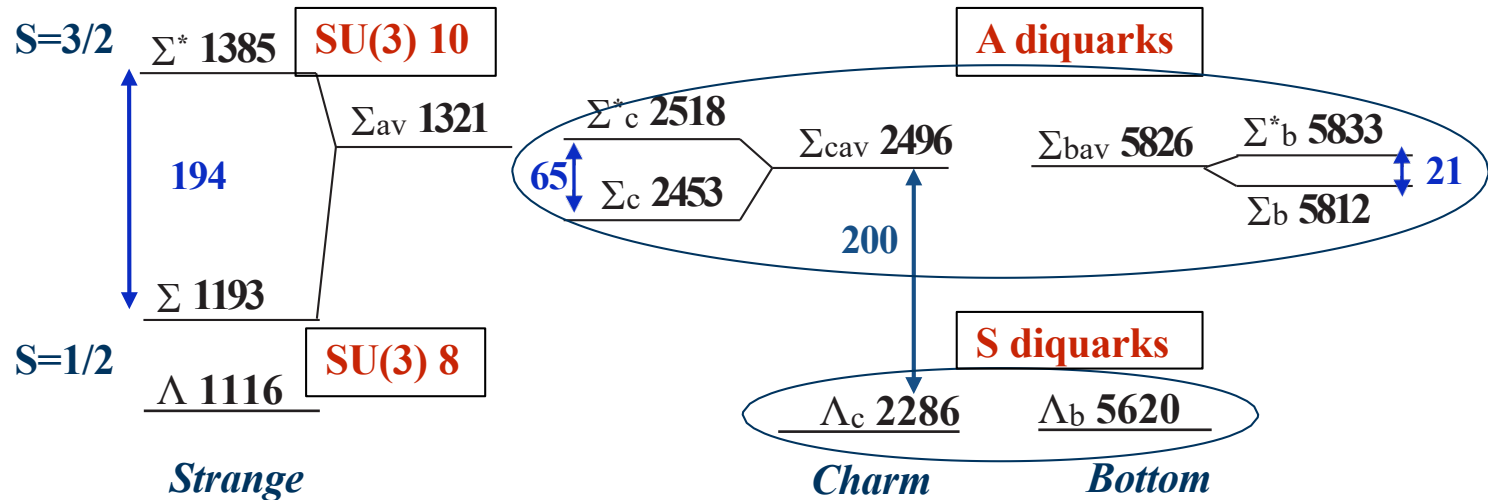
Production cross sections of hyperons and charmed baryons  
from  $e^+e^-$  annihilation near  $\sqrt{s} = 10.52$  GeV

Belle Collaboration, Phys. Rev. D97, 072005 (2018)



- $\Lambda$ 's and  $\Sigma$ 's are on a line with possible suppression of  $\Sigma(1385)^+$
- Spin-spin interaction may compete with diquark correlation
- Measurement of  $\Lambda(1405)$  will be interesting

# Diquarks in Strange and Charm



In the strange sector, the spin-spin force splits SU(3) 8 and 10.

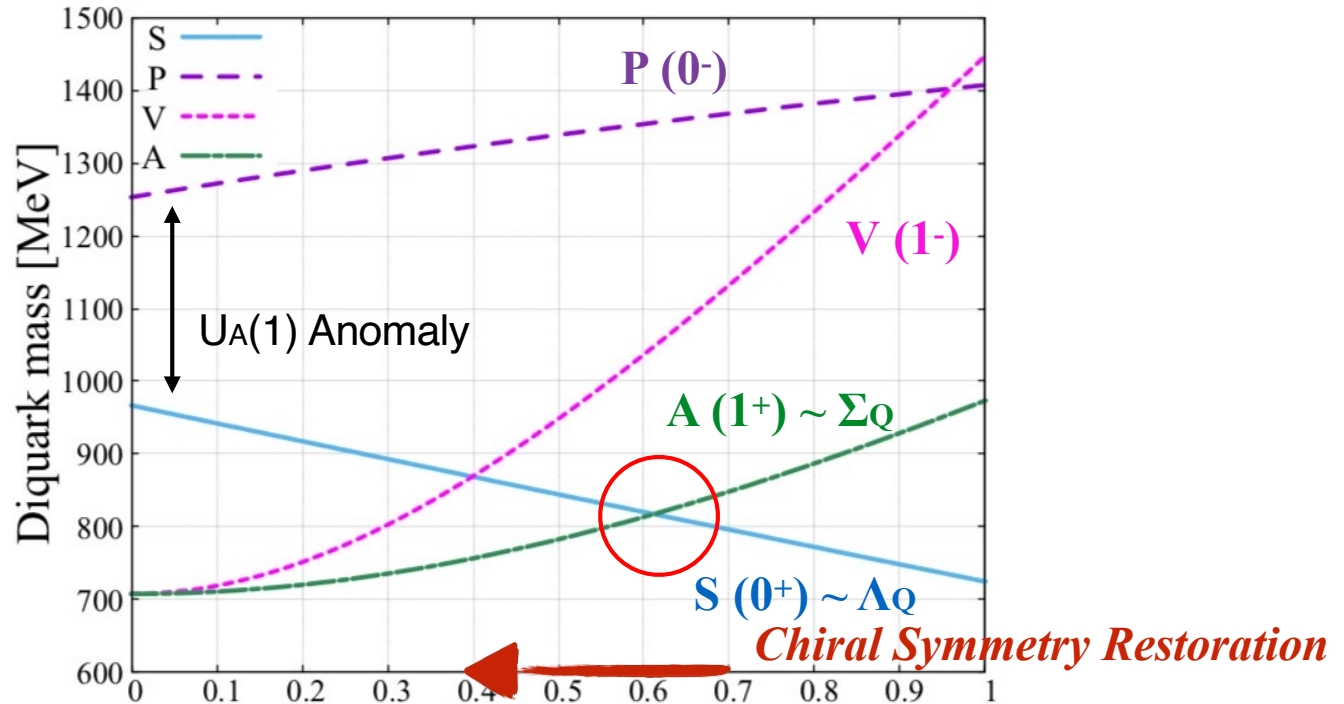
In the heavier sectors, the heavy-quark spin symmetry suppresses  $\Sigma_Q(1/2) - \Sigma_Q(3/2)$  splitting.

Diquark structure appear clearly in charm and bottom

# Diquark masses and chiral symmetry

## Mass changes of the $0^+$ and $1^+$ diquarks under chiral restoration

*Y. Kim, Y.R. Liu, M.Oka, K. Suzuki, Phys. Rev. D 104, 054012 (2021)*



Possible inversion of the scalar and axial-vector diquarks

→ may be significant for the behaviors of heavy baryons and diquark condensates in dense matter.

# Doubly Heavy Tetraquarks

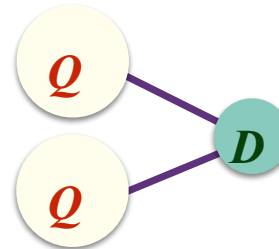
- The same model is applied to DHTQ

Y. Kim, M. Oka, K. Suzuki, *Phys. Rev. D* **105**, 074021 (2022)

- Potential between a heavy quark and a diquark

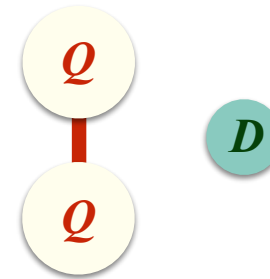
$$V_0(r) = -\frac{\alpha}{r} + \lambda r + C$$

$$V_{ss}(r) = (\mathbf{s}_i \cdot \mathbf{s}_j) \frac{\kappa}{M_i M_j} \frac{\Lambda^2}{r} \exp(-\Lambda r)$$



- Potential between heavy quarks  
(a la Semay-Silvestra Brac)

$$V(r) = -\frac{\alpha}{r} + \lambda r^p + C + (\mathbf{s}_i \cdot \mathbf{s}_j) \frac{8\kappa}{3m_i m_j \sqrt{\pi}} \frac{e^{-r^2/r_0^2}}{r_0^3}$$



- *Predictions*

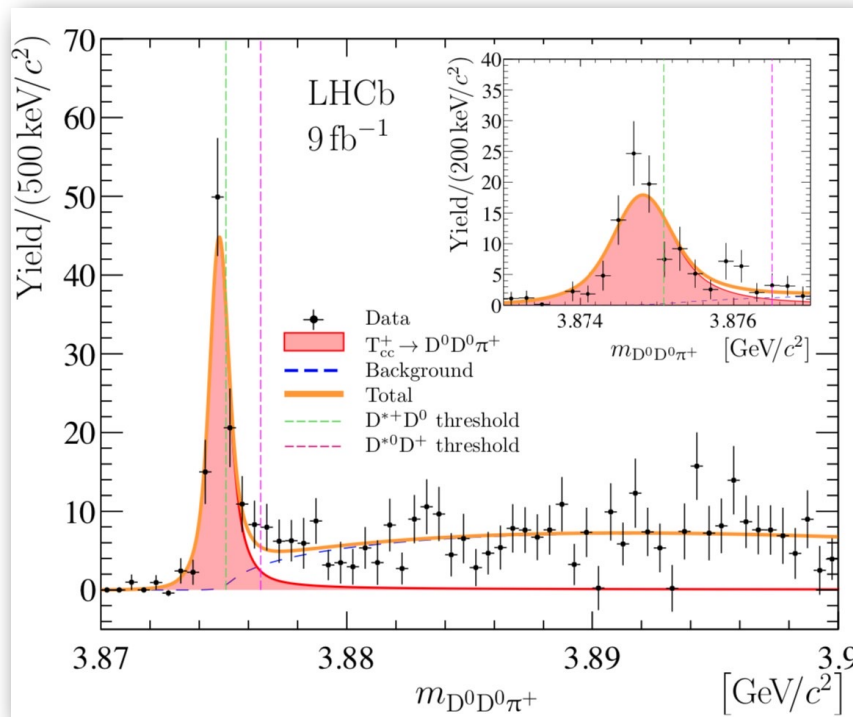
$M(T_{bb}) = 10489 \text{ MeV}$  below  $BB^*$  threshold

$M(T_{cc}) = 3961 \text{ MeV}$  above  $DD^*$  threshold

# Observation of $T_{cc}$

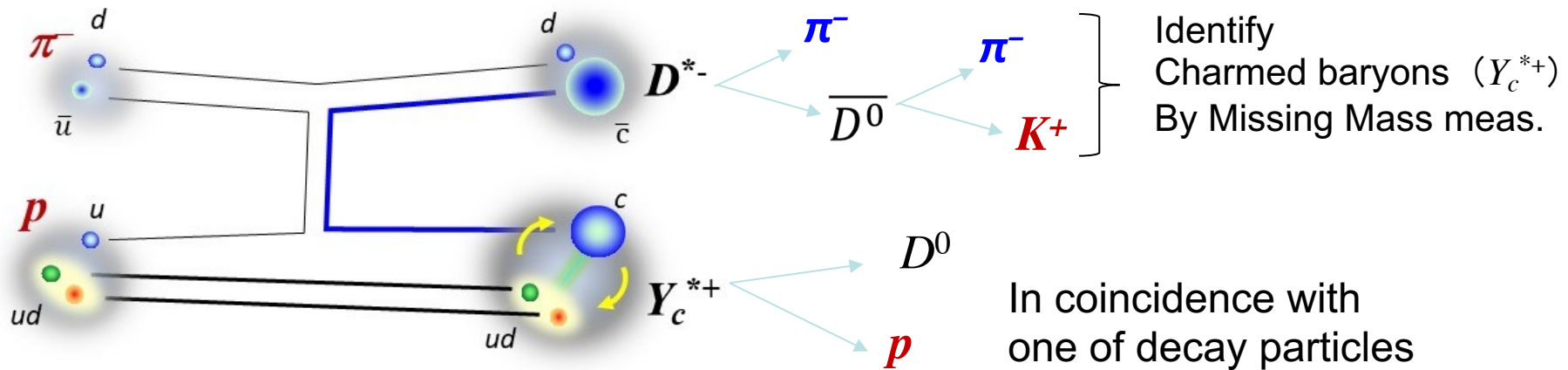
$T_{cc}$  LHCb

*arXiv:2109.01038, 2109.01056*



- Very close to  $D^{*+}D^0$  threshold
- Likely to be  $D^*D^0$  molecule
- May require 4q core for the production at LHCb

# Measurement of charmed baryons ( $Y_c^{*+}$ ) formations and decays



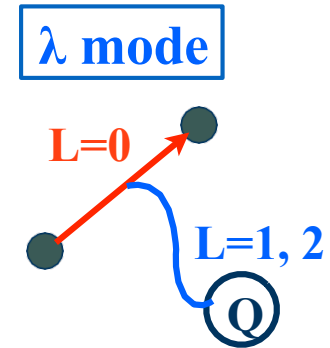
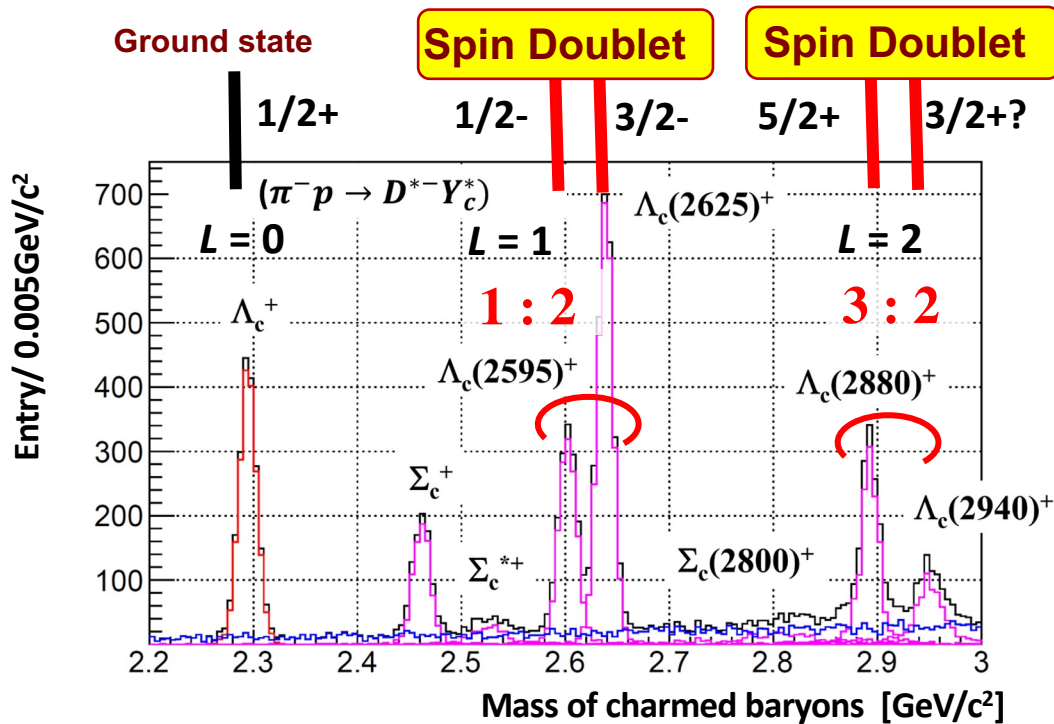
Missing Mass Meas.

@J-PARC E50 Experiment

- Inclusive/systematic measurement of  $Y_c^{*+}$
- Decay branching ratios (independent meas. of decay particles)

# Expected spectrum

$\lambda$  mode states



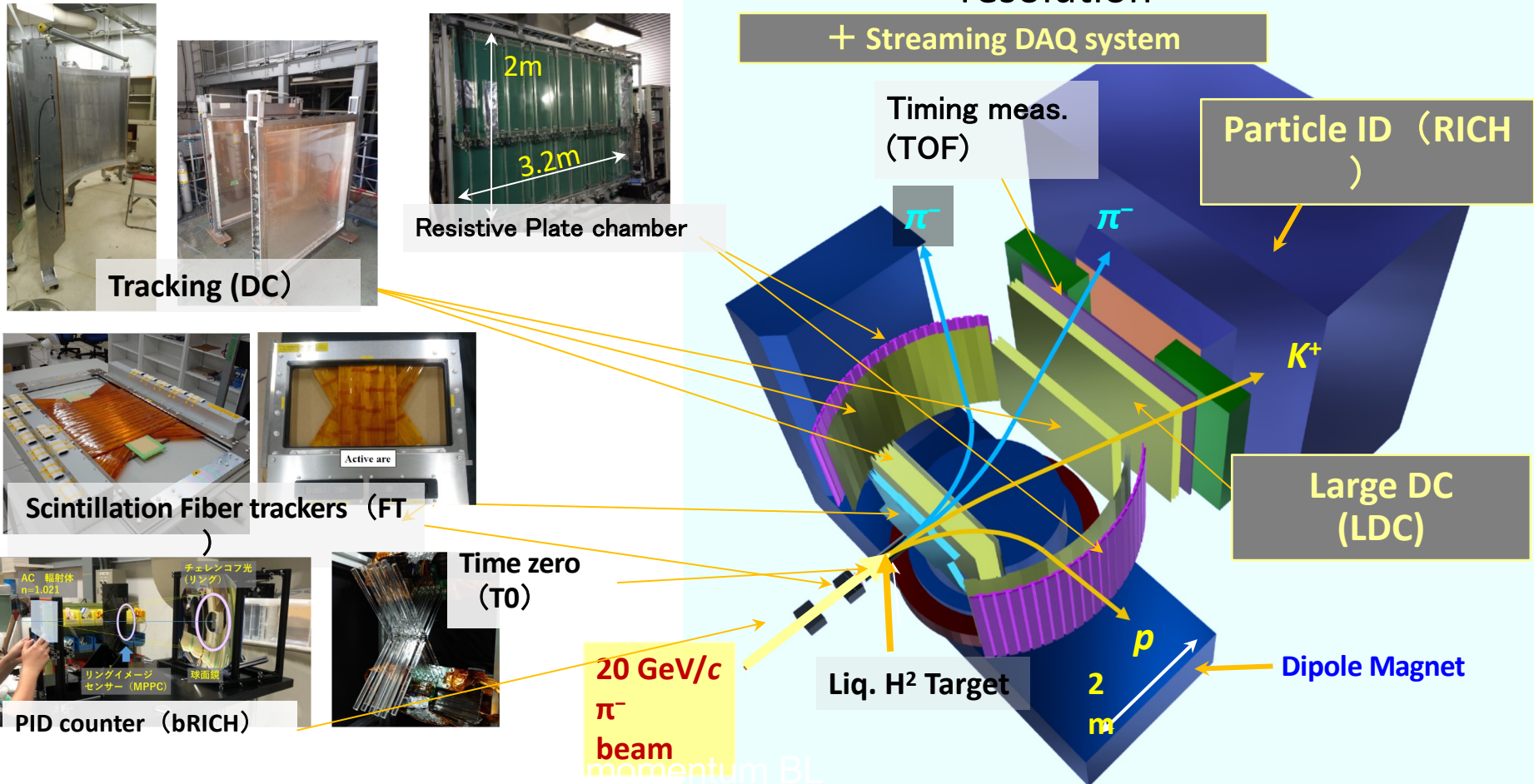
Production rate to be  $L:L+1$   
 → determine spin-parities

Requires high resolution and good PID at very high rate

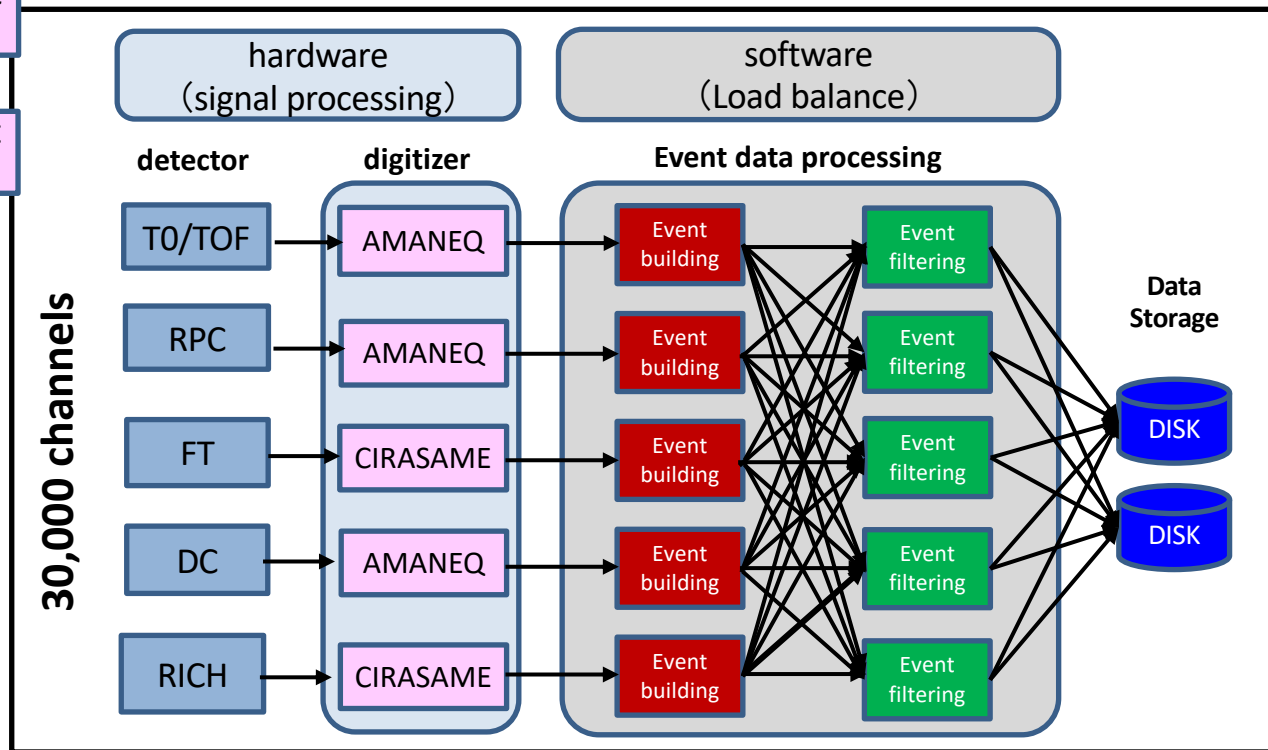
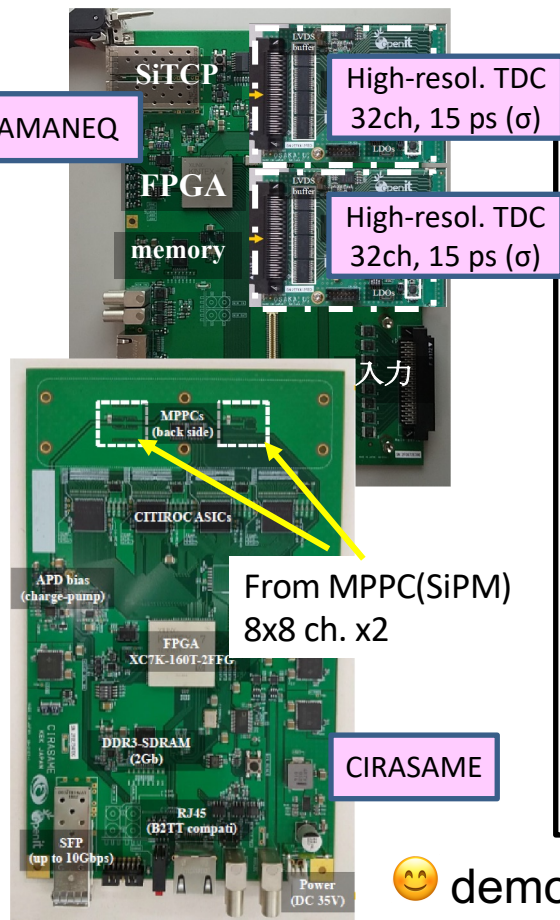


# E50 Spectrometer

Large Solid Angle、PID system、high-resolution

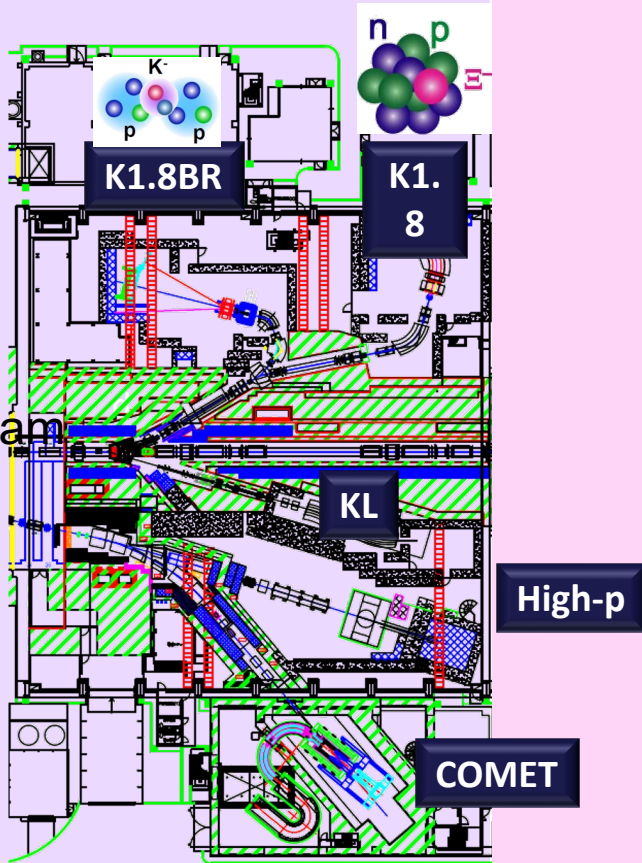


# Streaming DAQ system



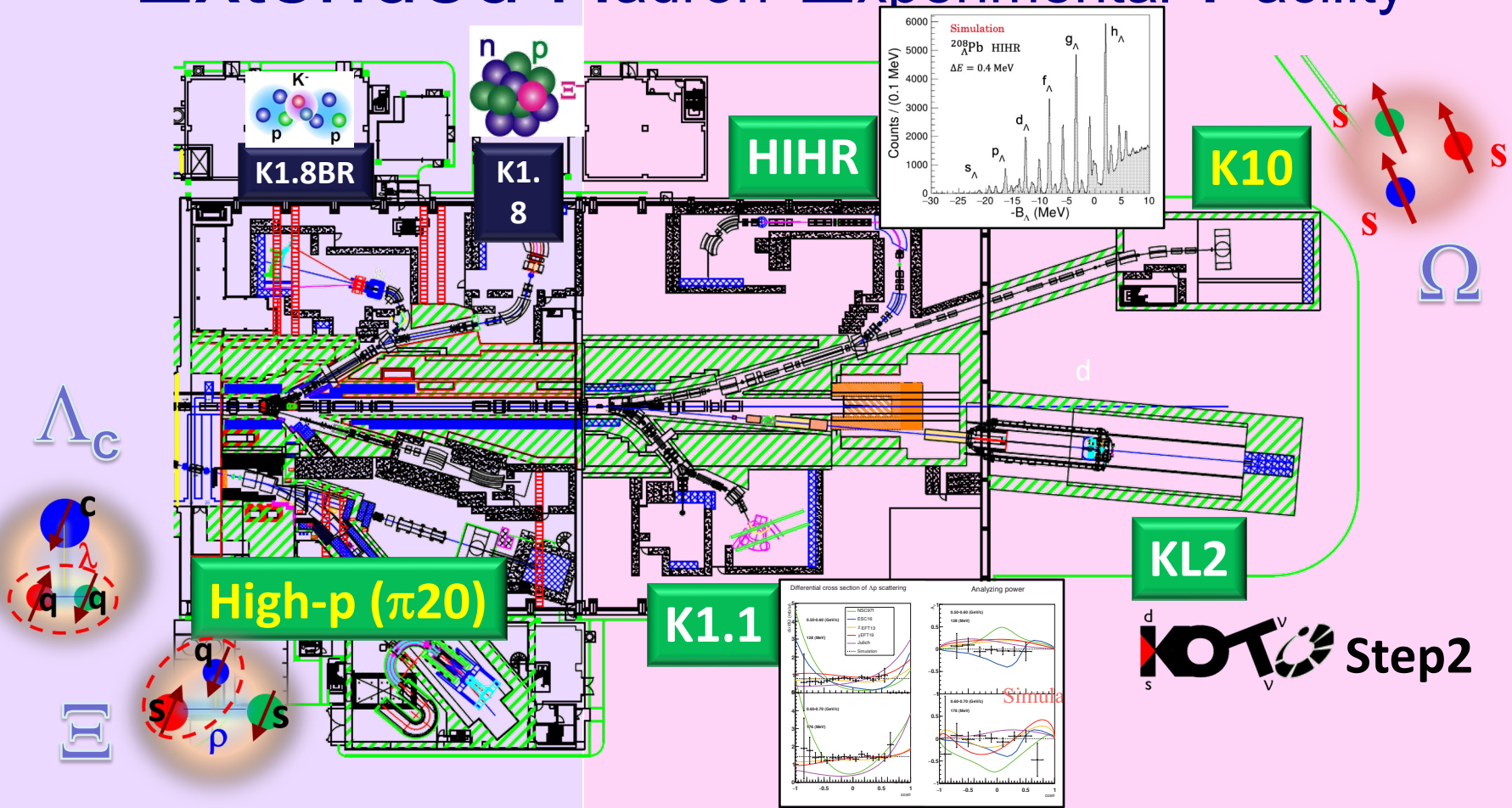
😊 demonstrated in test experiments: R. Honda, PTEP 2021, 123H01)

# Current Hadron Experimental Facility





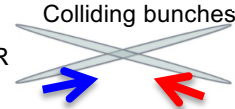
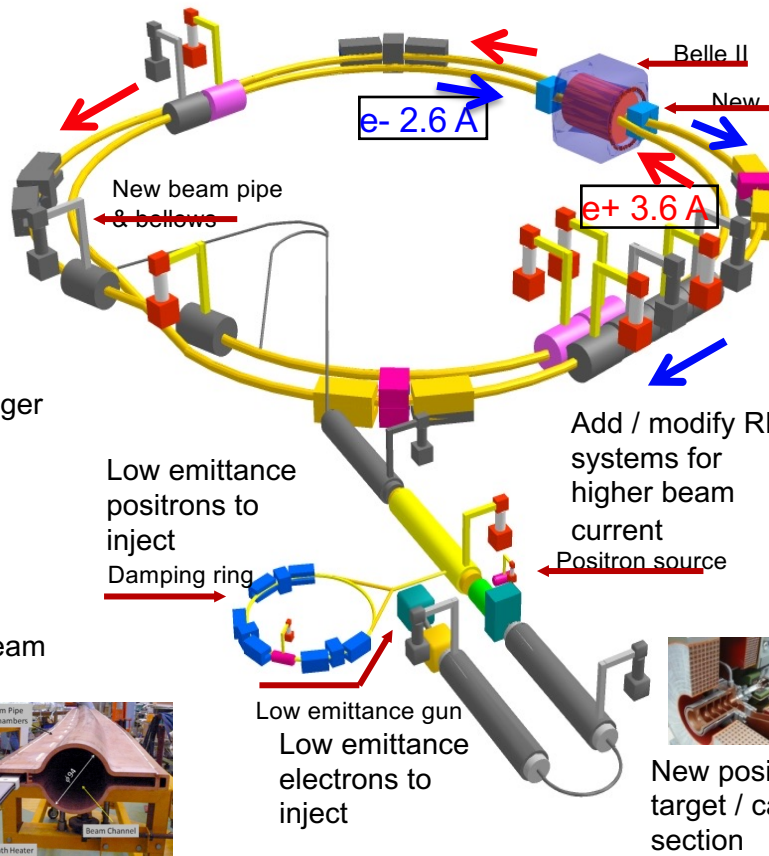
# Extended Hadron Experimental Facility



# SuperKEKB collider



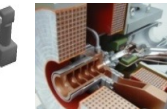
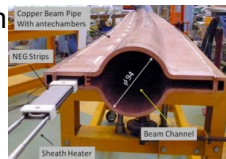
Replace short dipoles with longer ones (LER)



New superconducting /final focusing quads near the IP



TiN-coated beam pipe with antechamber



New positron target / capture section

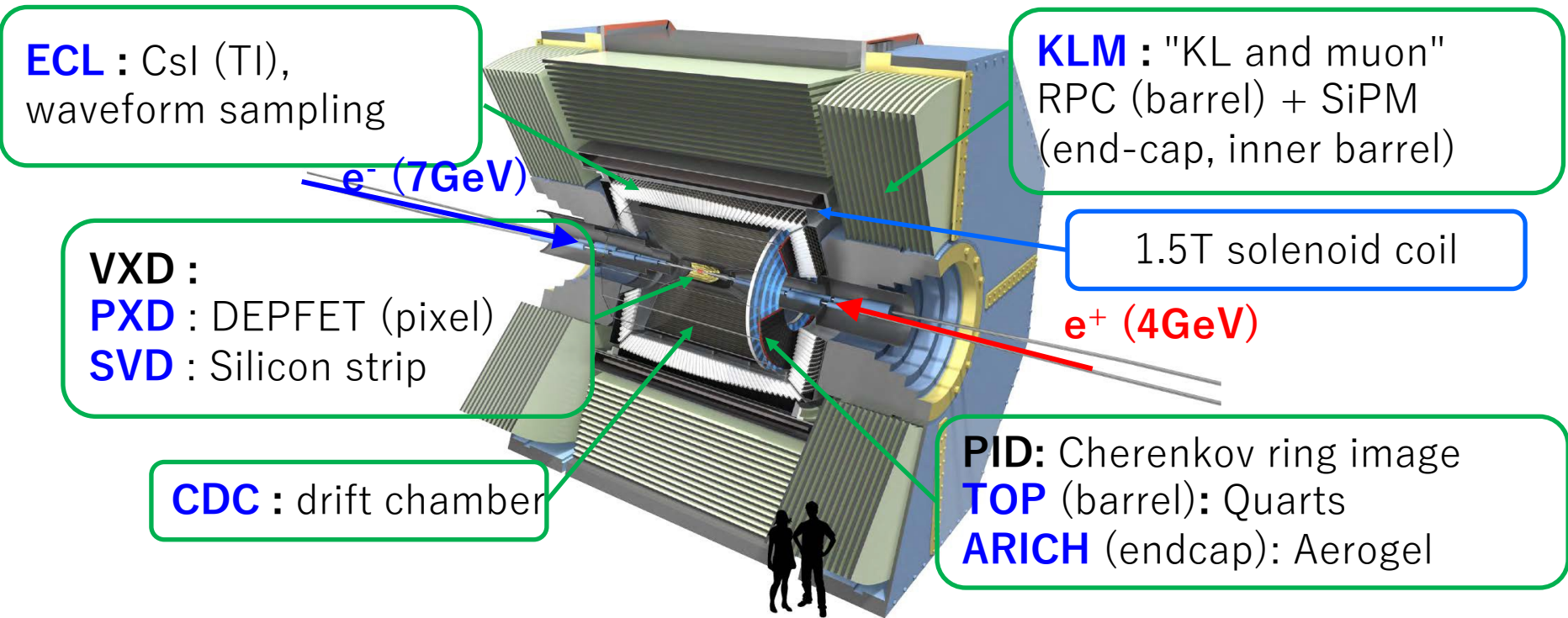
KEKB  $\times 40$

- Nano-beam
- Increase currents

➔ Peak luminosity :  $2.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1} \Rightarrow 8.0 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$   
 Beam energy : 3.5 / 8.0 GeV  $\Rightarrow 4.0 / 7.0 \text{ GeV}$

Boost factor  $\sim 2/3$

# Belle II detector



**ECL** : CsI (TI),  
waveform sampling

**KLM** : "KL and muon"  
RPC (barrel) + SiPM  
(end-cap, inner barrel)

**VXD** :  
**PXD** : DEPFET (pixel)  
**SVD** : Silicon strip

1.5T solenoid coil

**CDC** : drift chamber

**PID**: Cherenkov ring image  
**TOP** (barrel): Quarts  
**ARICH** (endcap): Aerogel

- Issues to overcome**
- Beam background
  - High rate capability
  - Boost  $\sim 2/3$



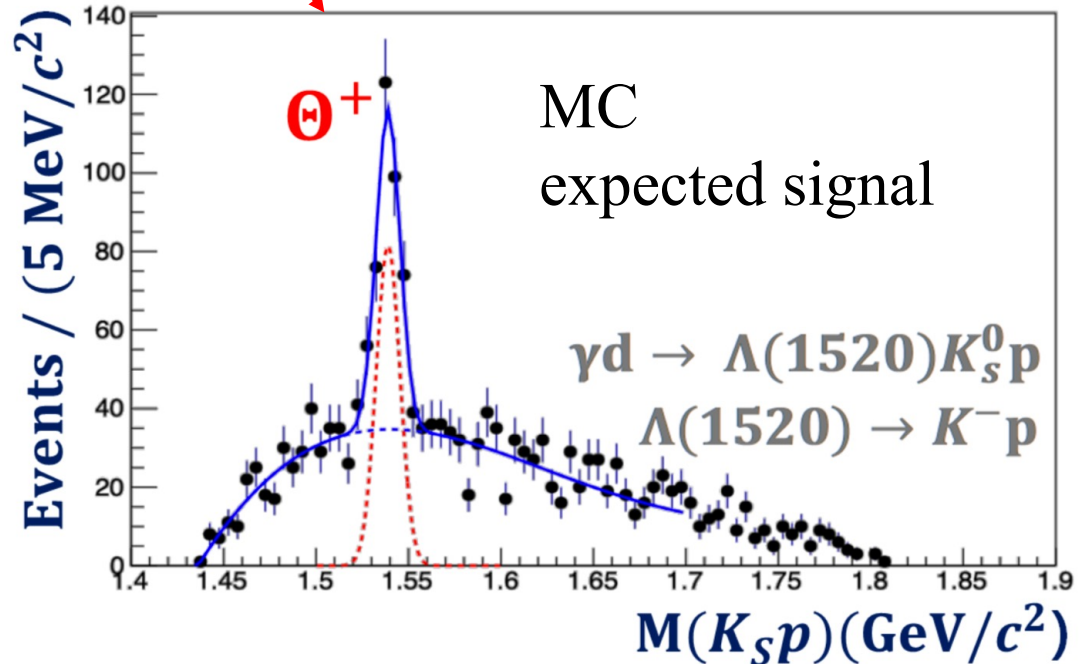
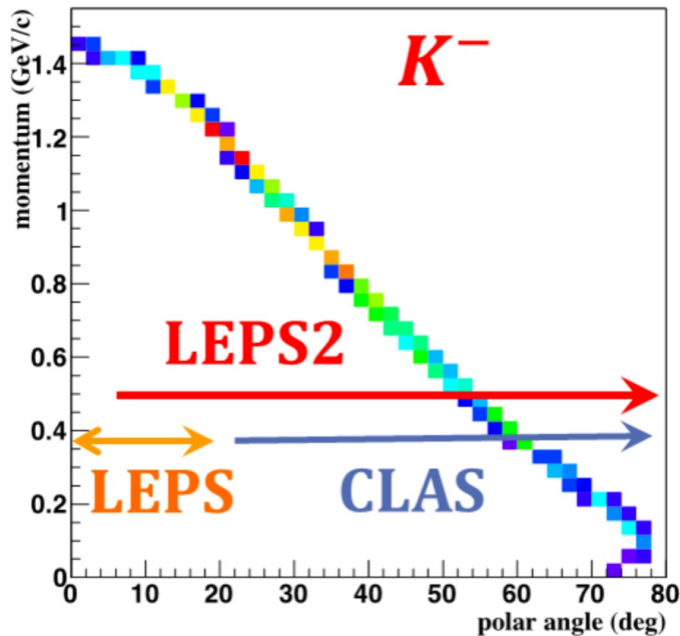
- Technical choice**
- Finer segmentation, waveform sampling.
  - Material change
  - Larger angular coverage (CDC, SVD)
  - Closer to the IP (PXD) 3  $\rightarrow$  2cm
  - Particle ID improve ( $K/\pi$ )(TOP, ARICH)

# Pentaquark $\Theta^+$ search @ LEPs2

$$\gamma d \rightarrow \Theta^+ K^- p \quad \text{Strangeness tagging}$$

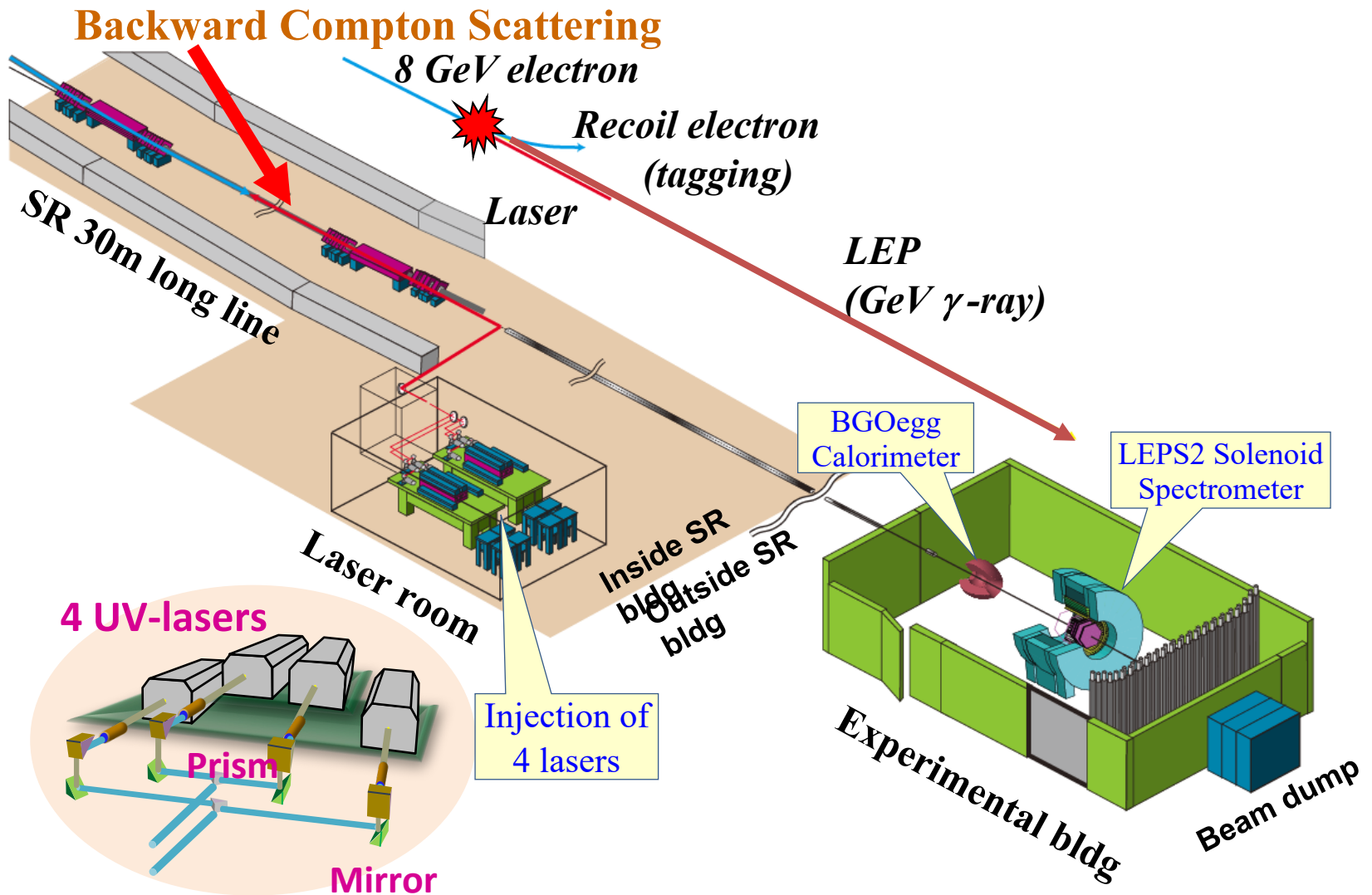
$$\Theta^+ \rightarrow K_S^0 p \rightarrow \pi^+ \pi^- p \quad \text{Invariant mass measurement}$$

Wide angle coverage





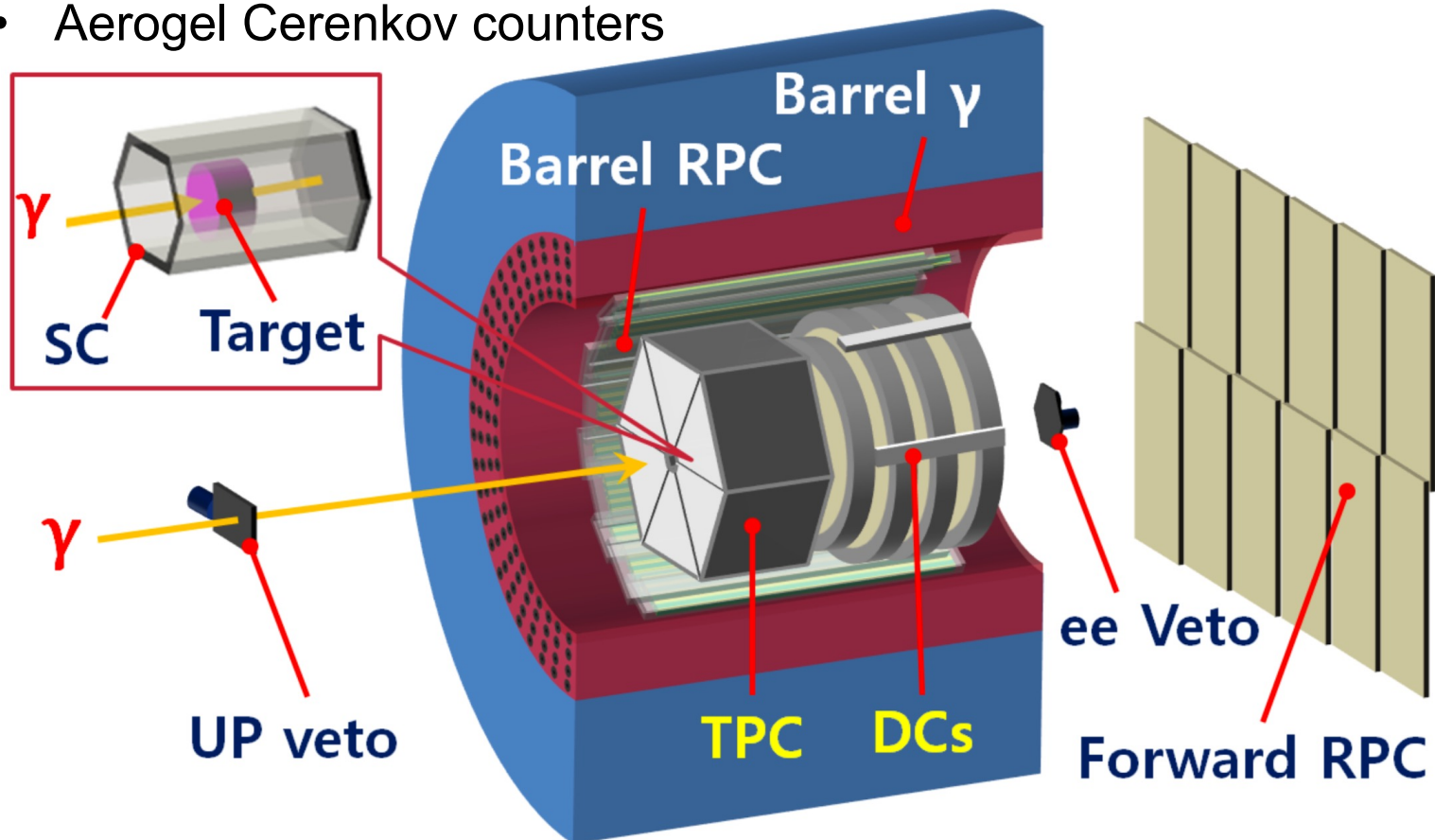
# LEPS2 Beamline



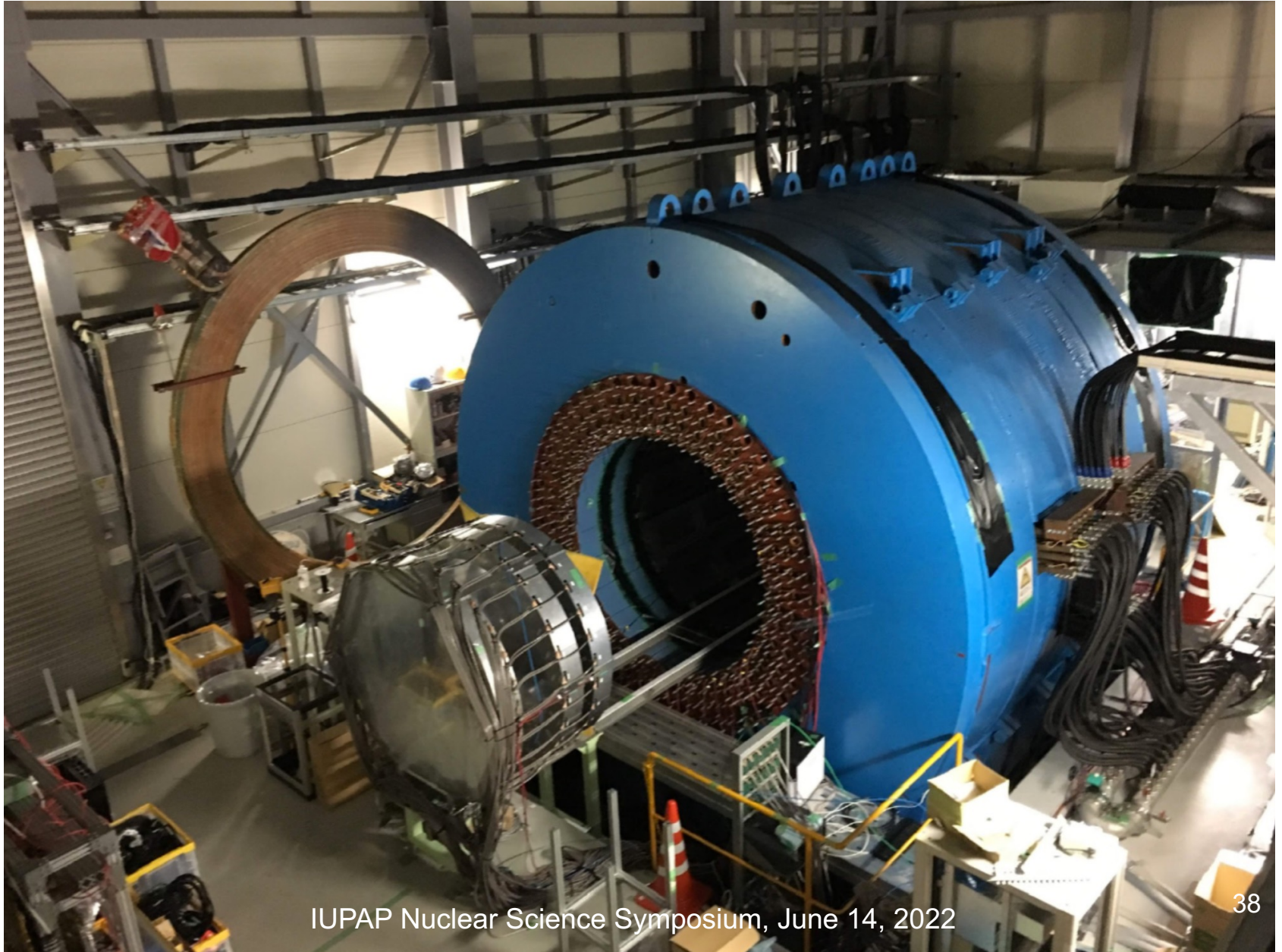


# Solenoid spectrometer

- Timing counter: SC, Forward and Barrel RPCs
- Tracker: TPC, DCs
- EM calorimeter: Barrel  $\gamma$
- Aerogel Cerenkov counters



# Solenoid spectrometer



# Summary

- Hadron spectroscopy including exotic hadrons is shedding lights on “effective” degrees of freedom for hadron structure and excitation, *ex. molecular states, diquarks, collective motions*.
- Production and decay of heavy hadrons is promising to reveal the dynamics and roles of diquarks.
- High-intensity and wide-acceptance facilities such as J-PARC (with Hadron Hall Extension in near future), Belle II@Super KEKB, and LEPS2@SPring-8 will provide us with opportunities to explore the colored and colorless correlations further.

# Acknowledgement

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