



High Precision Half Life Measurement of ^{26}Na with GRIFFIN



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GRIFFIN

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[egfuakye-resources08](https://github.com/egfuakye-resources08)



[egfuakyeresources08](https://www.instagram.com/egfuakyeresources08)

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Motivation

- Our goal is to provide a half-life measurement of ^{26}Na as a first experimental test of GRIFFIN for high-precision work (eg. superallowed decay studies).
- The GRIFFIN result can be compared to a previously published high-precision measurement (Grinyer, 2005).
- $\sim 99\%$ of all β^- decays yield the 1809 keV γ -ray (Grinyer, 2008).

Decay Scheme of ^{26}Na

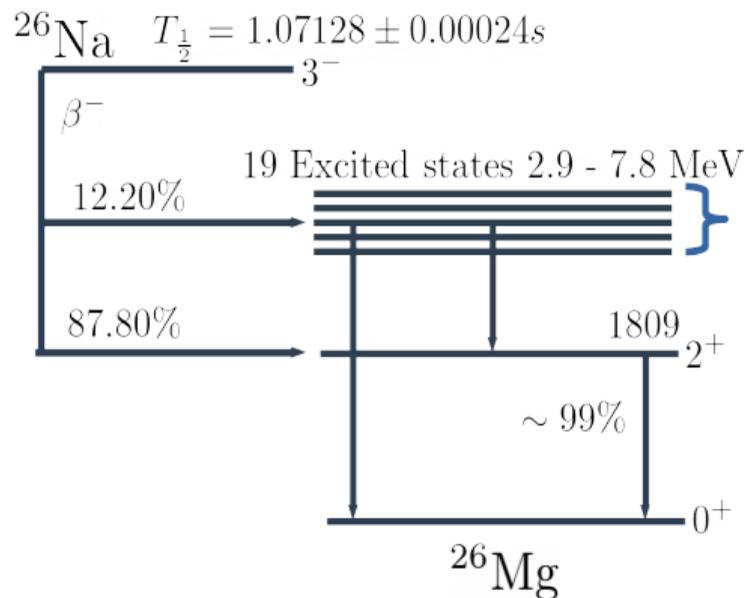


Figure 1: A simplified ^{26}Na β^- decay scheme to the stable daughter ^{26}Mg .



γ Counting — The GRIFFIN Spectrometer



Both hemispheres of the GRIFFIN array showing the beamline and central vacuum chamber encased in a white 20 mm plastic delrin absorber.

- The **S1140 Experiment** was performed in November, 2017.
- **Spherical array of 16 Clover detectors each consists of 4 HPGe Crystals**
- **~9.1% photopeak efficiency at 1.3 MeV**



Data were Collected in Cycles

Counts vs Time in cycles

The radioactive beam is then implanted into the tape.

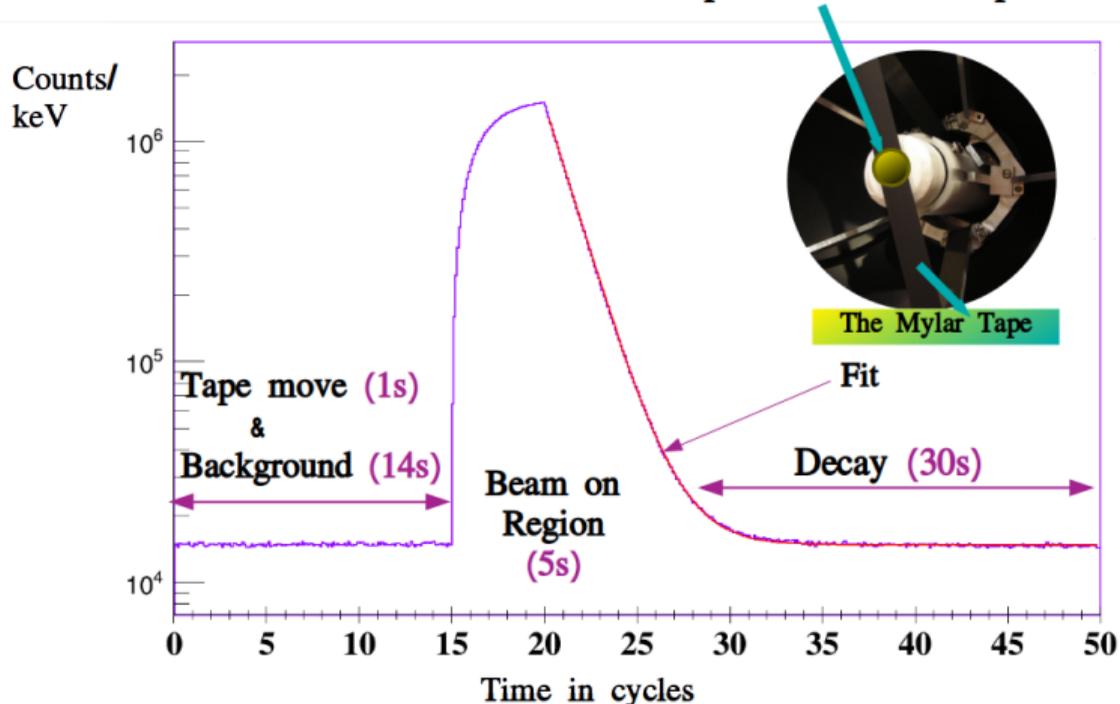


Figure 2: 1-D plot showing the cycle number versus the time in cycles without incomplete cycle.



^{26}Na Energy Spectrum

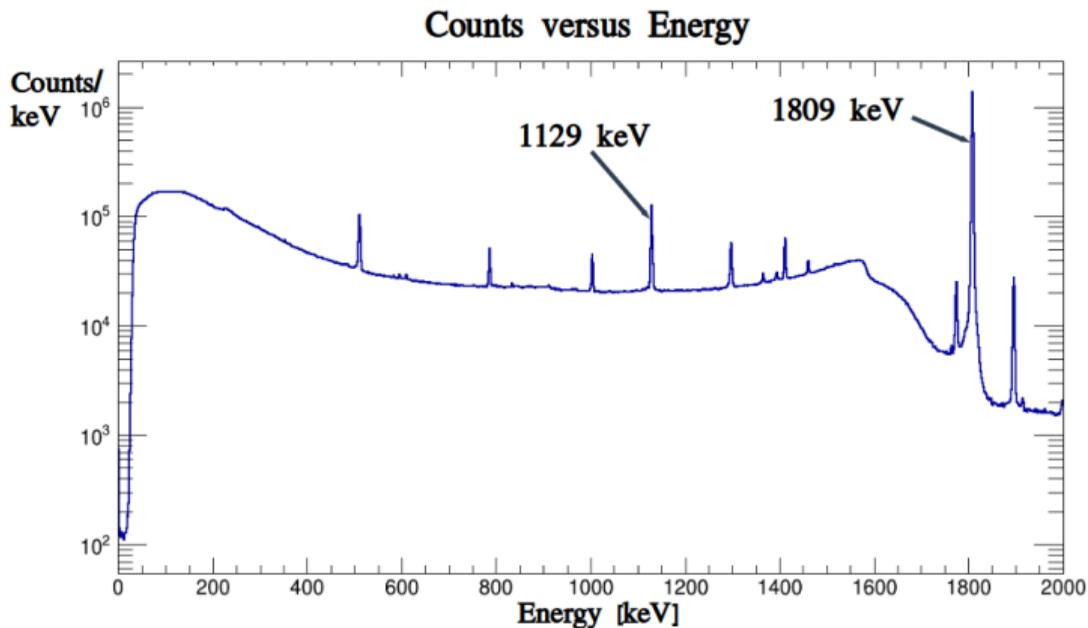


Figure 3: γ -ray singles spectrum for ^{26}Na with all the trigger events for a single run (40 mins).



Finding the peak to Gate 1809 [keV]

Typical zoomed in region (1760 - 1860 keV): Counts versus Energy

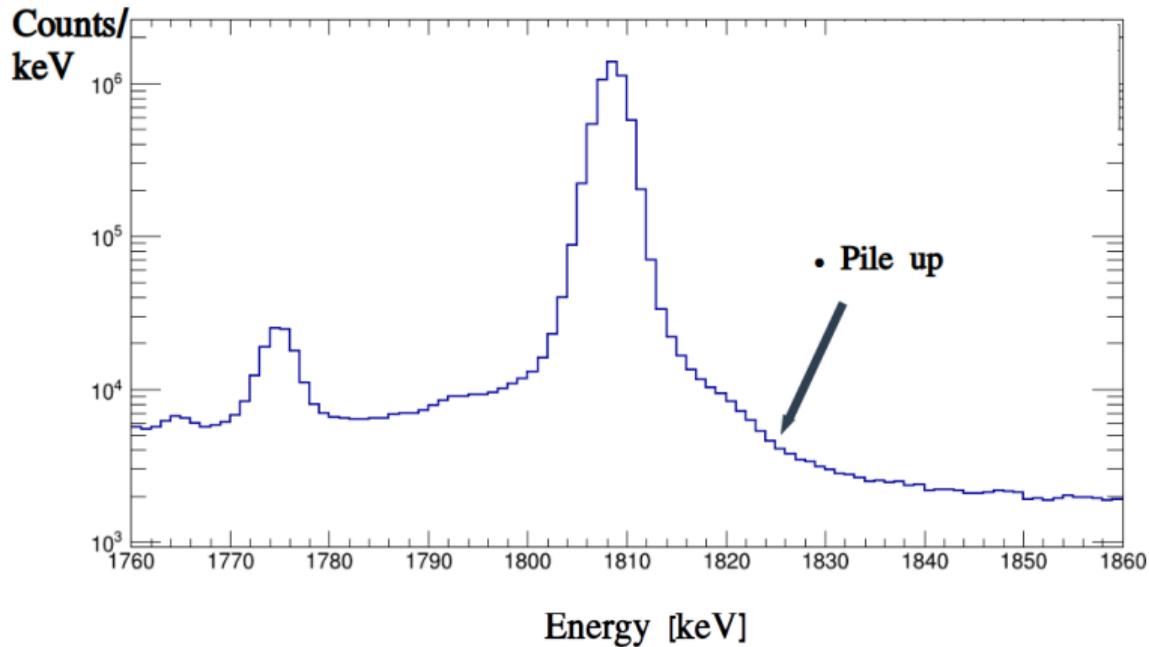


Figure 4: Typical zoomed in region (1760 - 1860 keV) from the γ -ray singles spectrum of ^{26}Na . The region due to pile up is clearly shown.



Selection Criteria Utilized

1

Decay data for the Na-26 experiment were collected in cycles(1, 14, 5, 30 s)★

- The first selection criterion: **REJECT** those cycles that had very few, or even zero, total counts recorded during the decay measurement.

2

Apply an energy gate on the 1809-keV transition in 26-Mg

3

Remove Pile Up Events using a gate on the K-Values



The precise values of the tape move, background, beam-on time and decay measurement were varied on a **run-by-run** basis.



Dead-time and Detector Pulse Pile-up Corrections

Dead time is the total period of time during which hit detections cannot be processed even if they are present.

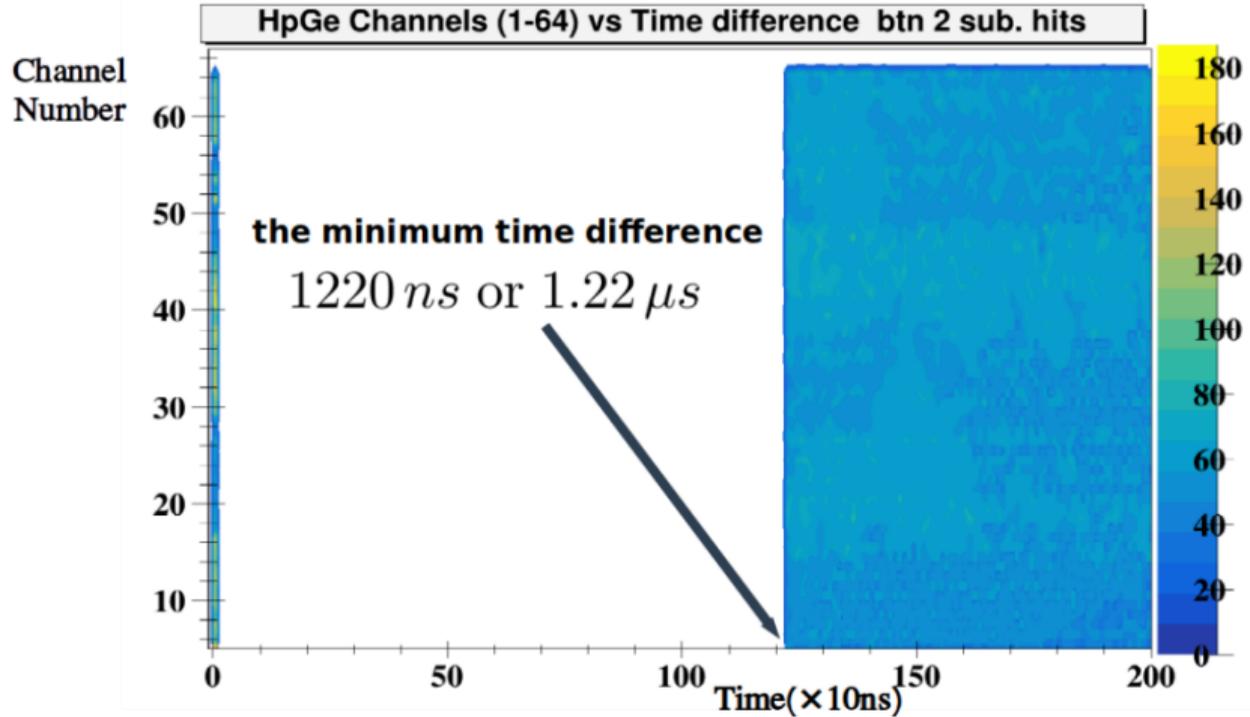
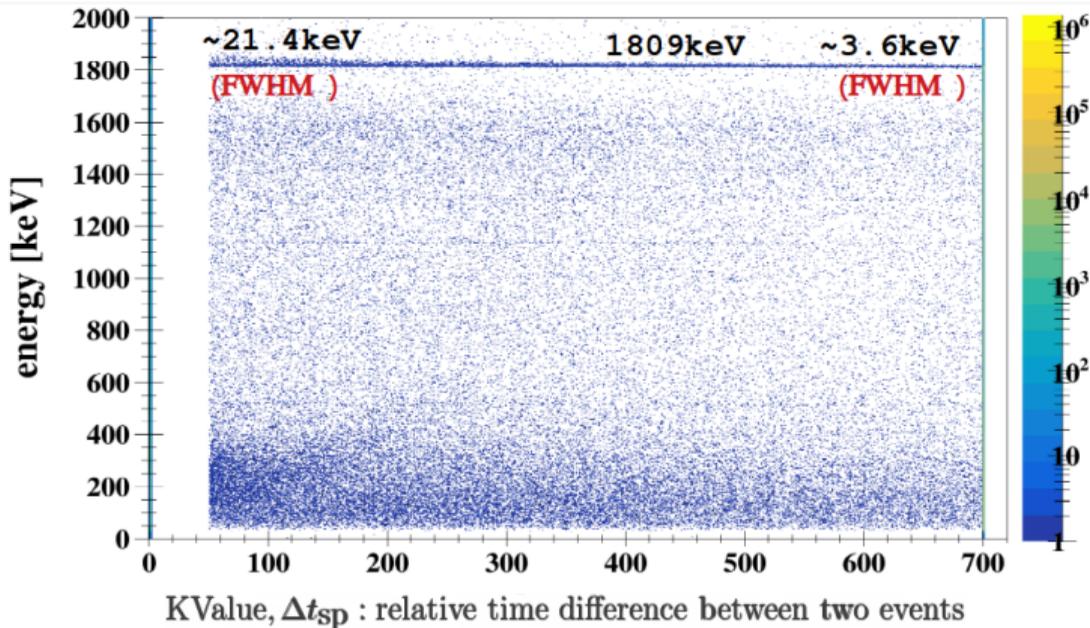


Figure 5: The dead time of the GRIFFIN DAQ shown by plotting the time interval of two consecutive γ -rays for each crystal.



Dead-time and Detector Pulse Pile-up Corrections

Signal pile-up occurs when more than one energy deposition from different physics events is present in a detector element during the processing time of the initial interaction.



One can clearly see the dependence of the energy resolution on the k-value. The energy resolution worsens with decreasing integration length as expected and vice versa.



Looking at the Pile Up and Single Events Spectra

Single Events (blue) KValue == 700 & Pile up Events Kvalue < 700

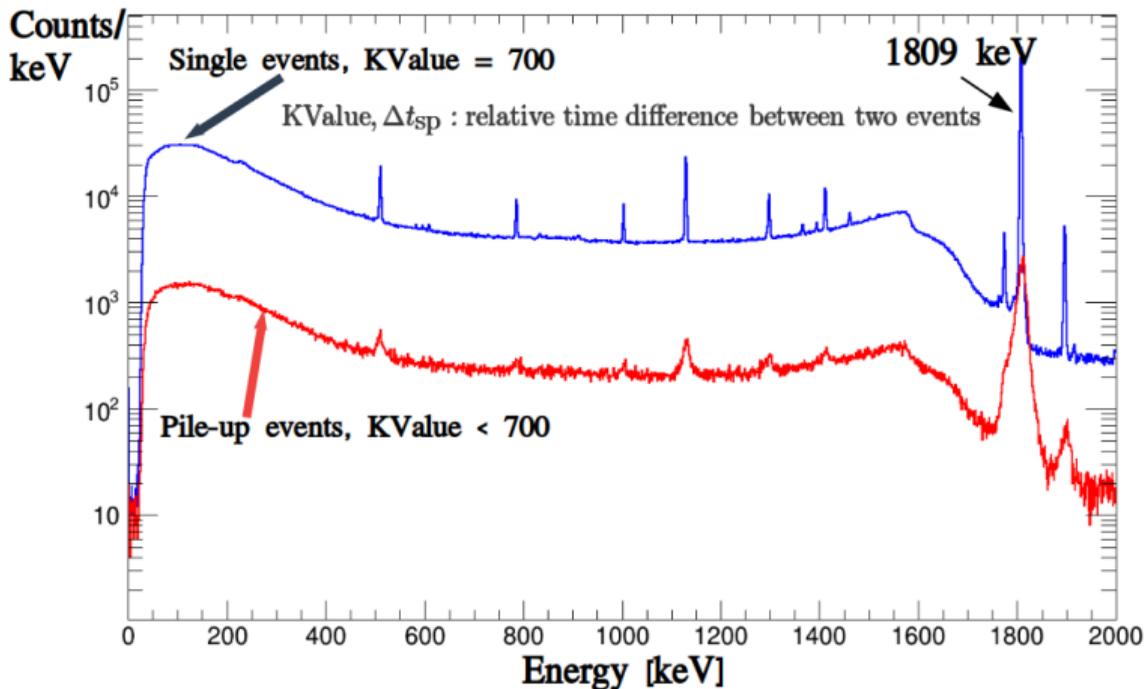


Figure 6: ^{26}Na Energy spectra to distinguish between single and pile-up events.



Dead-time and Detector Pulse Pile-up Corrections

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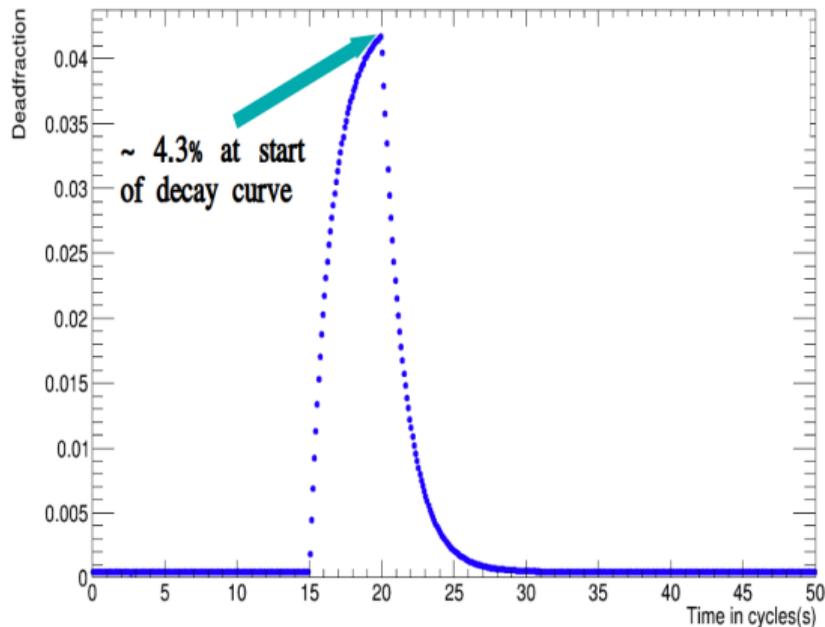
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Dead fraction versus time in cycles



Pile-up probability versus time in cycles

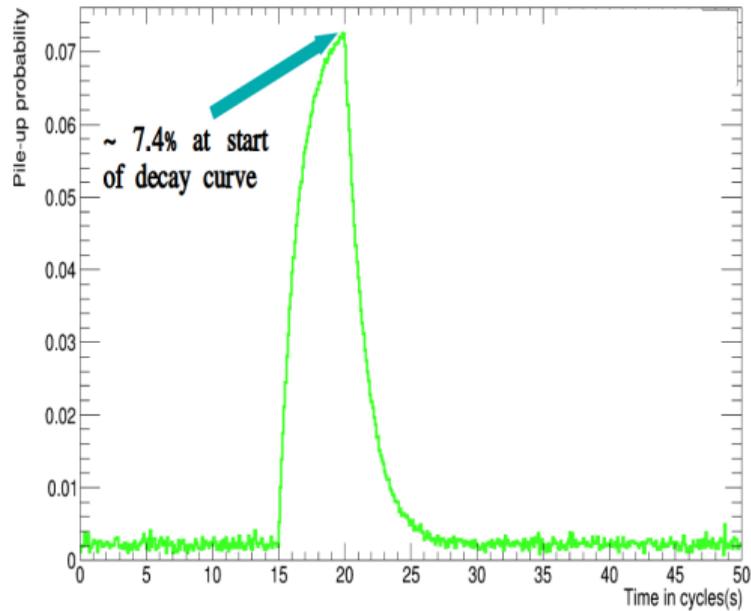


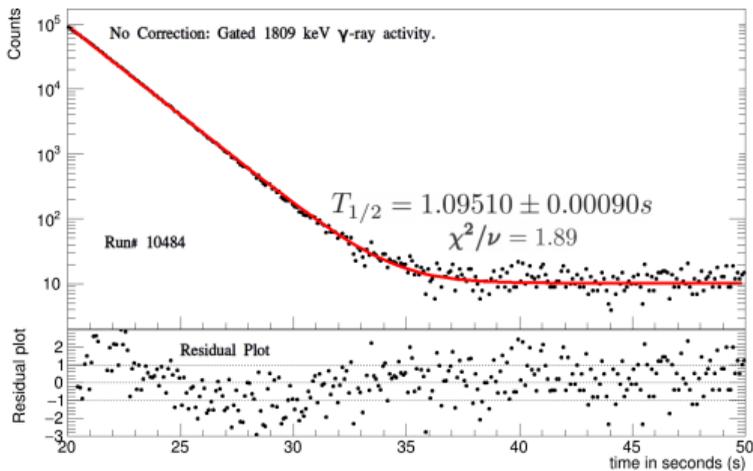
Figure 7: Left: the bin-by-bin dead fraction vs. time in cycles(s) for all events and right: the bin-by-bin pile-up probability vs. time in cycles(s) for all events.



Half-Life Analysis: ^{26}Na Gated 1809keV Activity

^{26}Na Gated 1809keV Activity with total decay time of 30s.

Uncorrected Data



1st order pile-up + dt correction

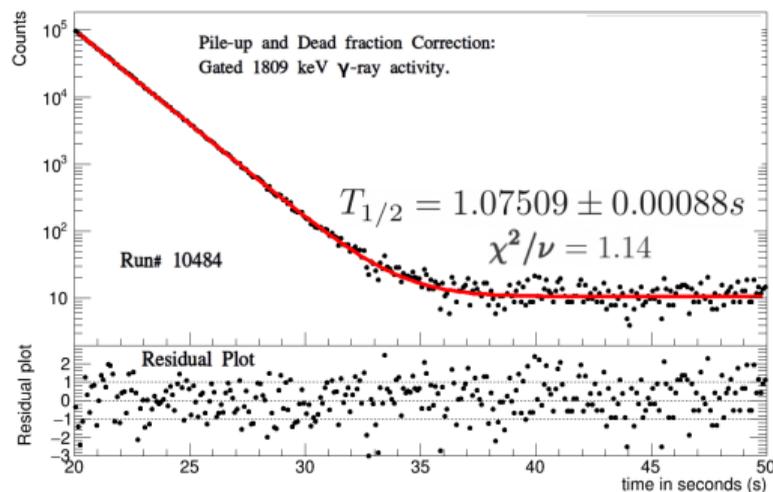


Figure 8: Non-corrected decay curve (left) and 1st order pile-up and dead-time (dt) correction decay curve(right) obtained from a single run following a gate on the 1809-keV transition in ^{26}Mg .



Half-Life Analysis: ^{26}Na Gated 1809keV Activity

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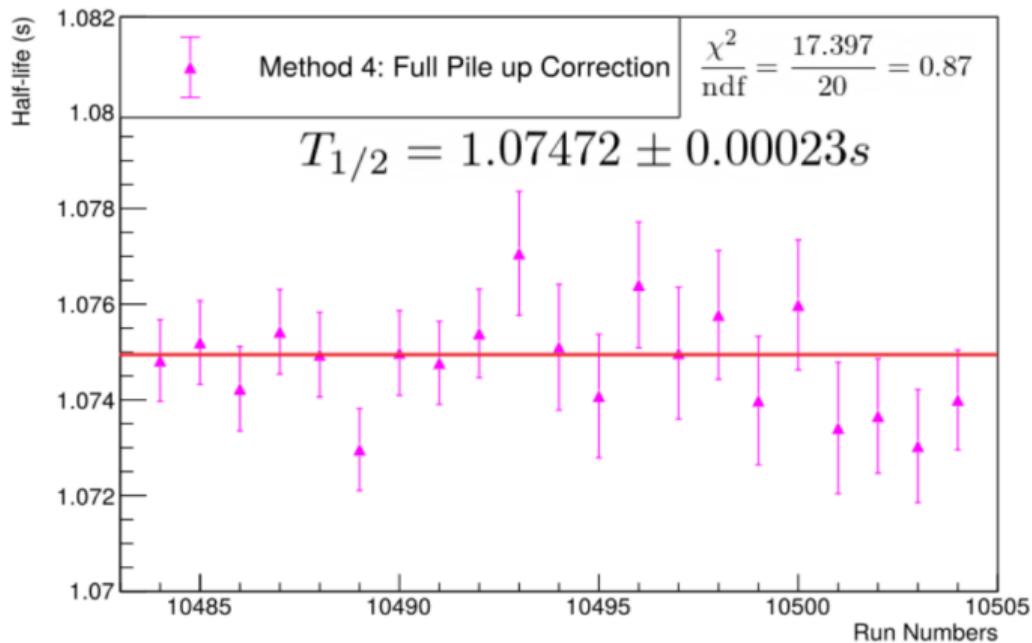
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Deduced half-life of ^{26}Na versus all the run numbers.



PileUp: Value < 700 & Not PileUp: KValue ==700

Figure 9: ^{26}Na : Deduced Half life versus run number (right). A weighted average of $T_{1/2} = 1.07472 \pm 0.00023\text{ s}$ is deduced from these data where the uncertainty is statistical.



Half-Life Analysis: ^{26}Na Gated 1809keV Activity

Leading-Channel Removal Plots

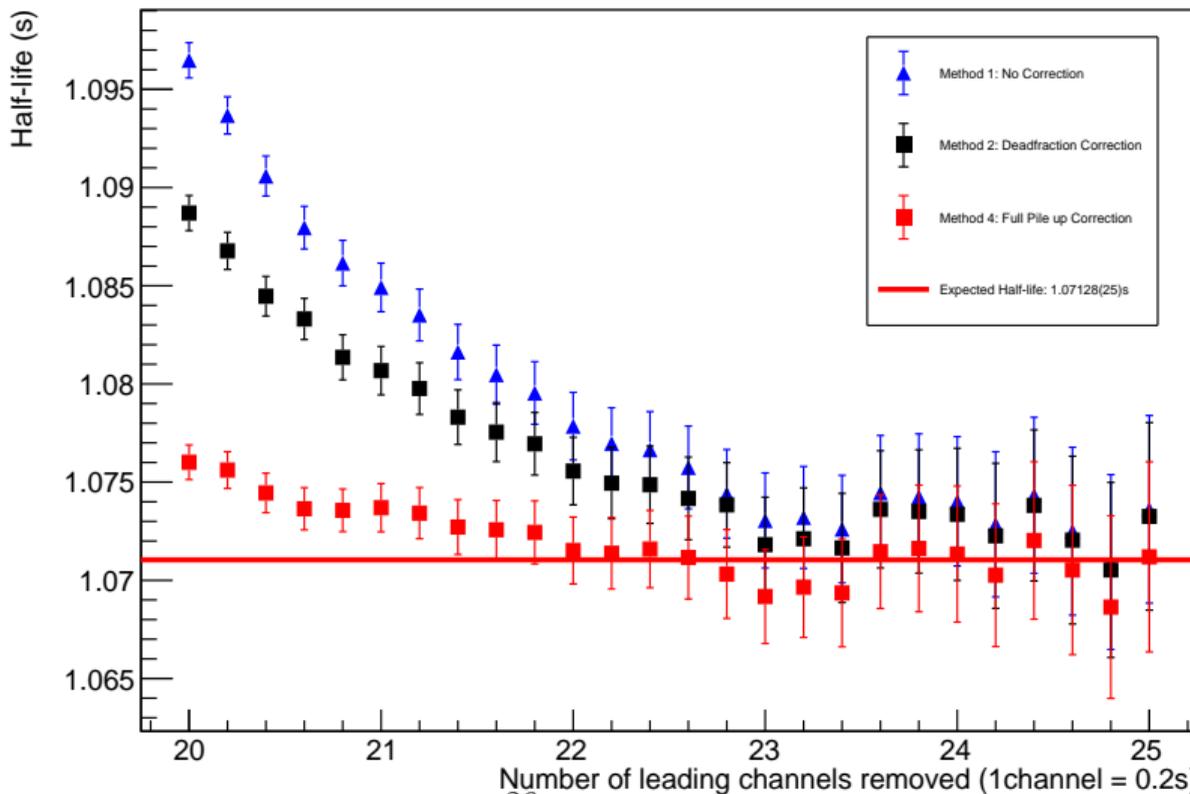


Figure 10: Deduced half-life of ^{26}Na vs. number of leading channels removed.



Rate-Dependent Refinements

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➤ **Pile-up Time Resolution**

- Corrects for pile-up events not resolved (in time) by the pile-up circuitry.

➤ **Trigger-Energy Threshold**

- Corrects for pile-up caused by sub threshold energy events.

➤ **Pile-up Detection Energy Threshold**

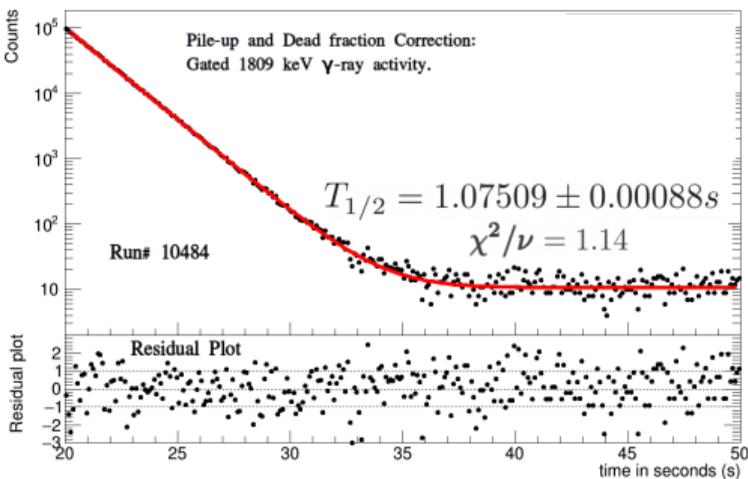
- Corrects for low energy pile-up events missed by the pile-up circuitry.



Half-Life Analysis: ^{26}Na Gated 1809keV Activity

Comparing 1st order pile-up correction to Higher order pile-up correction

1st order pile-up correction



Higher order pile-up correction

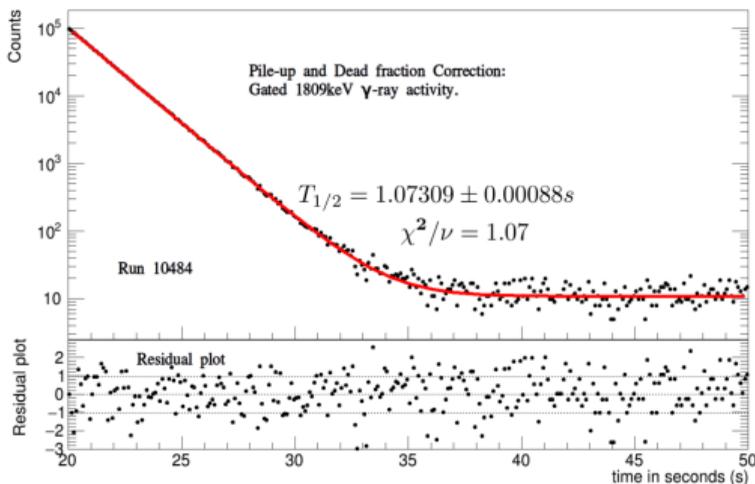
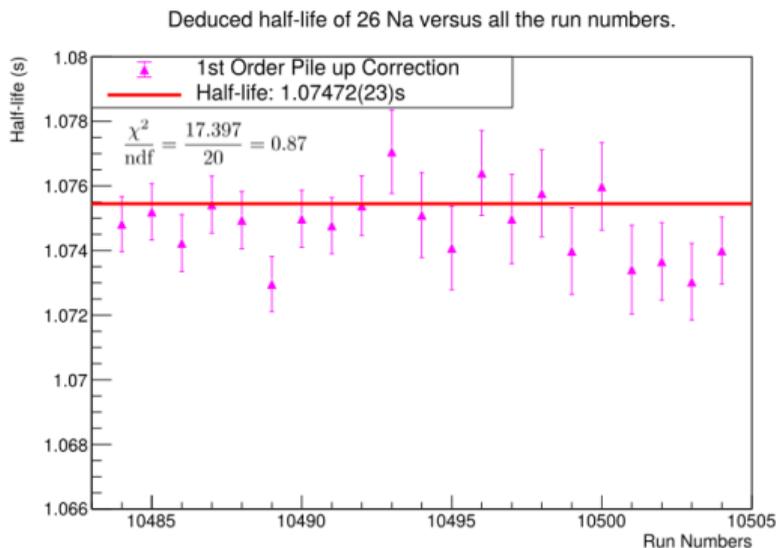


Figure 11: 1st order pile-up correction (left) and Higher order pile-up correction decay curve(right) obtained from a single run following a gate on the 1809-keV transition in ^{26}Mg .



^{26}Na Deduced Half life vs Run numbers

1st order pile-up correction



Higher order pile-up correction

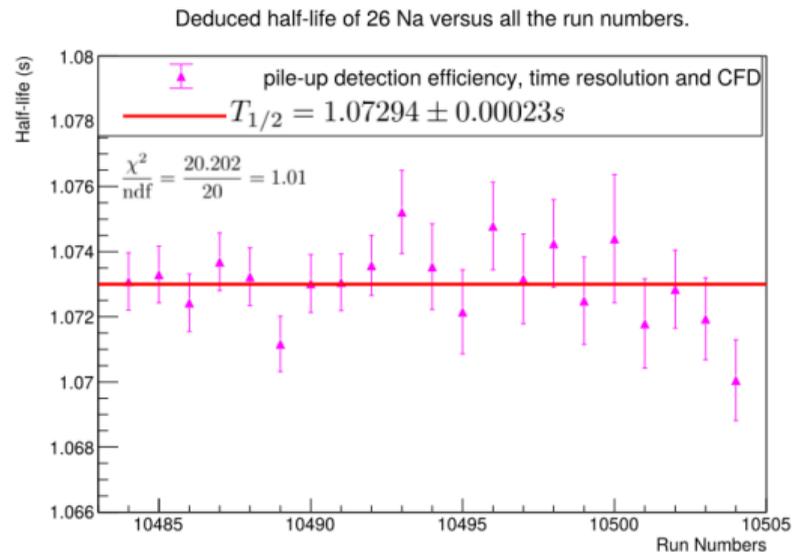


Figure 12: ^{26}Na : 1st order pile-up correction (left) and Higher order pile-up correction (right) of the deduced Half life versus run number.



Half-Life Analysis: ^{26}Na Gated 1809keV Activity

Leading-Channel Removal Plots

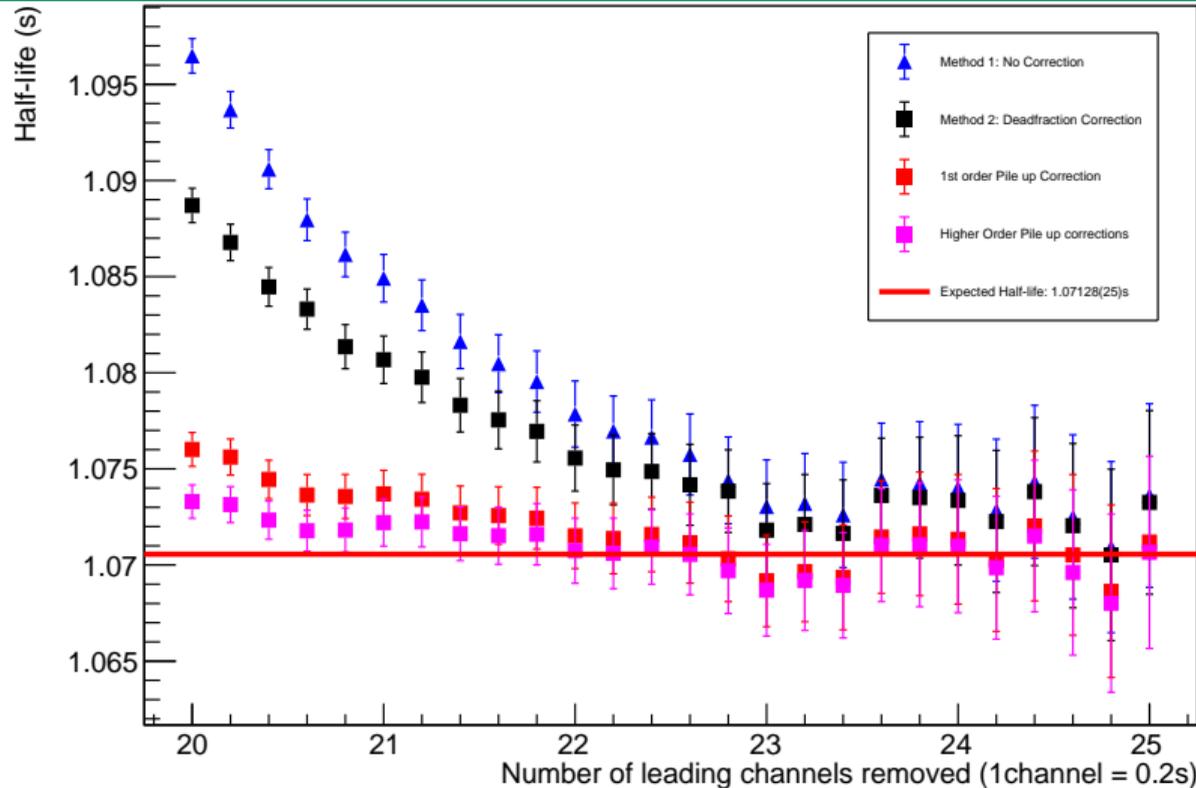


Figure 13: Deduced half-life of ^{26}Na vs. number of leading channels removed.



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- 1 The Half life for the 1809keV activity from ^{26}Na has been determined and was found to be $T_{\frac{1}{2}}(\text{avg}) = 1.07294 \pm 0.00023\text{s}$.
- 2 The results from the **higher order pile-up corrections** looks promising.
- 3 Grinyer et al. (2005) measured the high-precision half-life of ^{26}Na via β -counting. The half-life of ^{26}Na was determined to be $T_{\frac{1}{2}} = 1.07128 \pm 0.00025 \text{ s}$.
- 4 There is still work to do ($\sim 6\sigma$) on refining the pile-up correction and systematic uncertainties. Also need to explore summing effects in GRIFFIN.
- 5 Analysis of ^{14}O superallowed beta decay



COLLABORATORS

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- 1 Grinyer, G. (2008). High-precision half-life measurements for superallowed Fermi β decays (Doctoral dissertation).
- 2 Grinyer, G. F., Svensson, C. E., Andreoiu, C., Andreyev, A. N., Austin, R. A. E., Ball, G. C., ... & Zganjar, E. F. (2005). High precision measurements of Na 26 β - decay. *Physical Review C*, 71(4), 044309.
- 3 Zidar, T. (2019). Beta decay of neutron-rich 33Mg (Doctoral dissertation).
- 4 Svensson, C. E., & Garnsworthy, A. B. (2014). The GRIFFIN spectrometer. *Hyperfine Interactions*, 225(1), 127-132.)
- 5 Grinyer, G. F., Svensson, C. E., Andreoiu, C., Andreyev, A. N., Austin, R. A. E., Ball, G. C., ... & Zganjar, E. F. (2007). Pile-up corrections for high-precision superallowed β decay half-life measurements via γ -ray photopeak counting. *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, 579(3), 1005-1033.



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GRIFFIN

A.B. Garnsworthy et al.,

Regina GRIFFIN Group

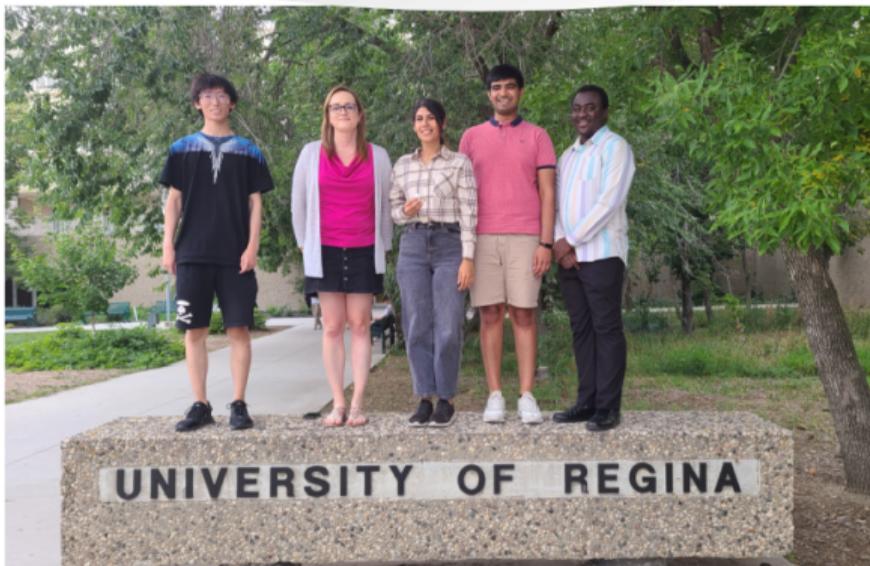


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Detector Pulse pile-up

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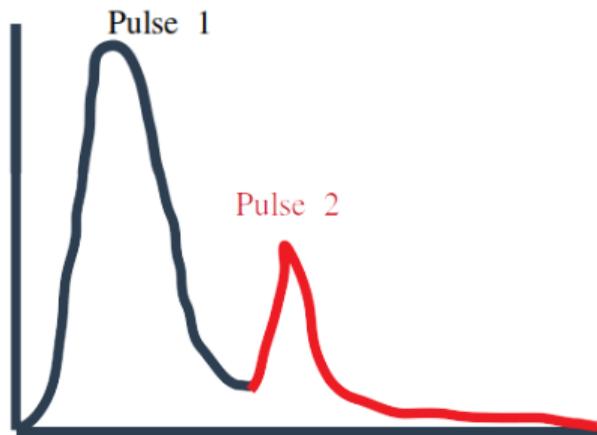
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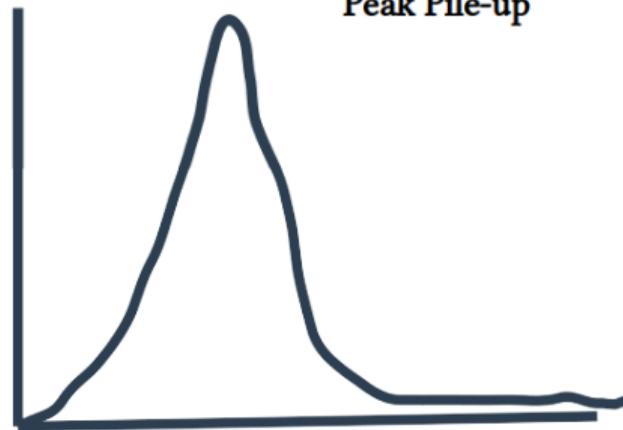
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Tail Pile-up



First order pulse pile-up where **pulse 2 is riding on the tail of pulse 1.**

Peak Pile-up



If the pulses **are very close in time**, the system will simply record the two pulses as a single event with a **combined pulse amplitude.**

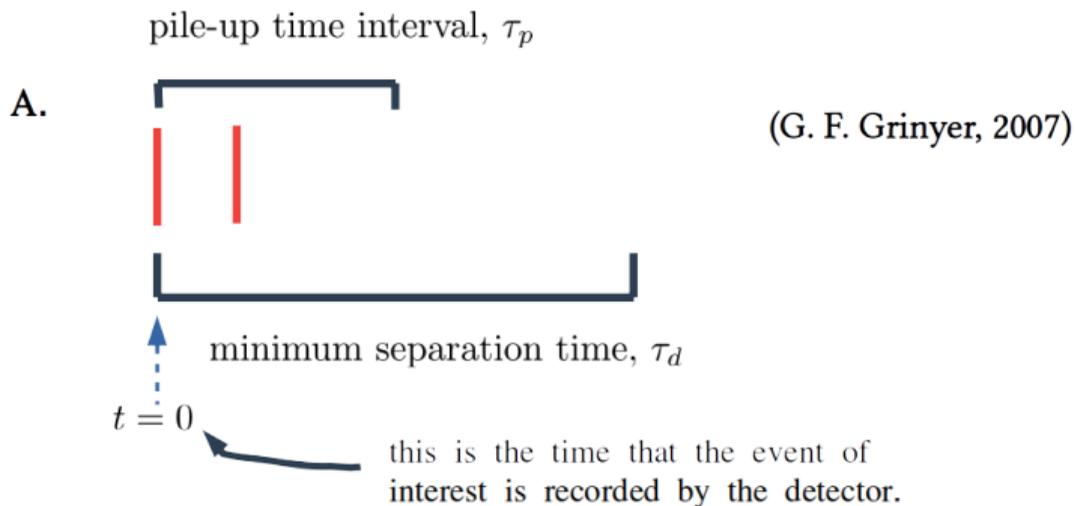
- The number of pile-up events depend strongly on the count rate of the system.



Common types of Pile-up

Post-piled-up

- Post pile-up is defined as the probability that the pile-up is caused by events arriving after the events of interest has been recorded.

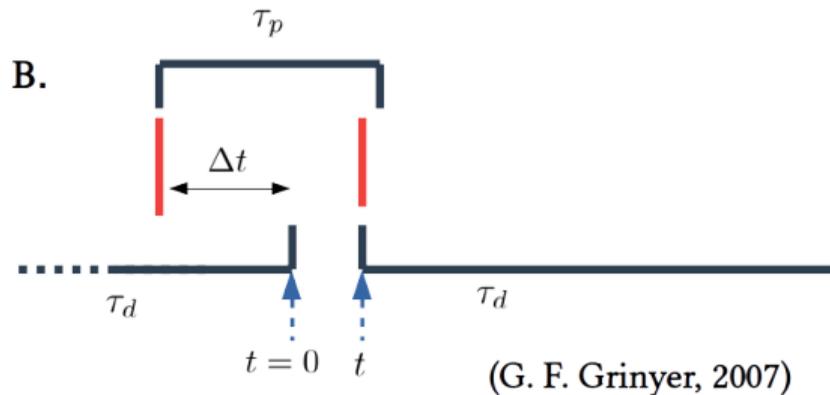




Common Types of Pile-up

II. Pre-piled-up

- The possibility that the event of interest is piled-up by an event that came before, in a process defined as “pre-pile-up”





Rejecting those Cycles with few or zero Counts

Cycle Number vs Time in cycles

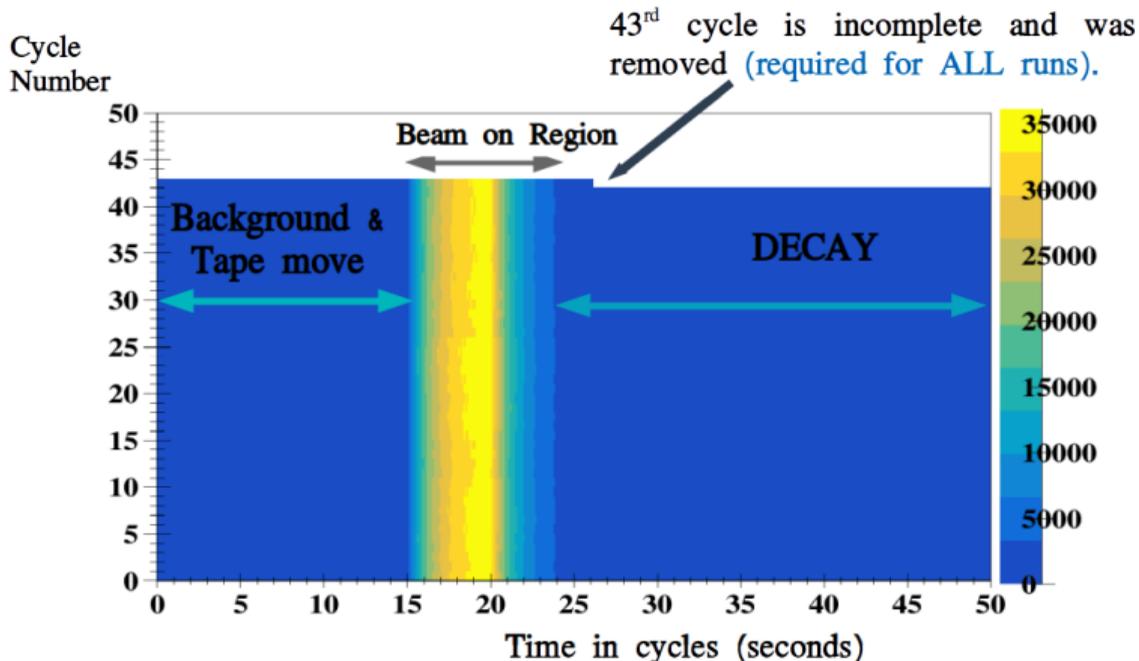


Figure 14: 2-D plot showing the cycle number versus the time in cycles, incomplete cycles were removed for all runs.



Analytical Expressions by (G. F. Grinyer, 2007)

$$P = 1 - e^{-(2-a_4)x} [e^{a_4x} + (1 - a_4)x] \quad 1$$

$$P = 1 - e^{-2x}(1 + \alpha x) \quad 2$$

$$P = \epsilon_p [1 - e^{-2x}(1 + x)] \quad 3$$

The probability of pile up with a **non zero time resolution, CFD** and **detection efficiency** in 1, 2 and 3 respectively.

$$P_{\text{fit-total}} = a_6 \left(1 - e^{-(2-a_4)x} [e^{a_4x} + a_5(1 - a_4)x] \right) \quad 4$$

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Bin-by-bin pile-up correction

1. Deadfraction Correction $D_i =$ Dead fraction

$$N'_i = \frac{N_i}{1 - D_i}$$

Deadtime is the total period of time during which hit detection cannot be processed even if they are present.

2. Higher Order Pile-up Corrections

**RATE DEPENDENT
CORRECTIONS**

$$N''_i = \frac{N_i}{(1 - D_i) \times (1 - P_{\text{fit-total}})}$$





Higher Order Pile-up Corrections

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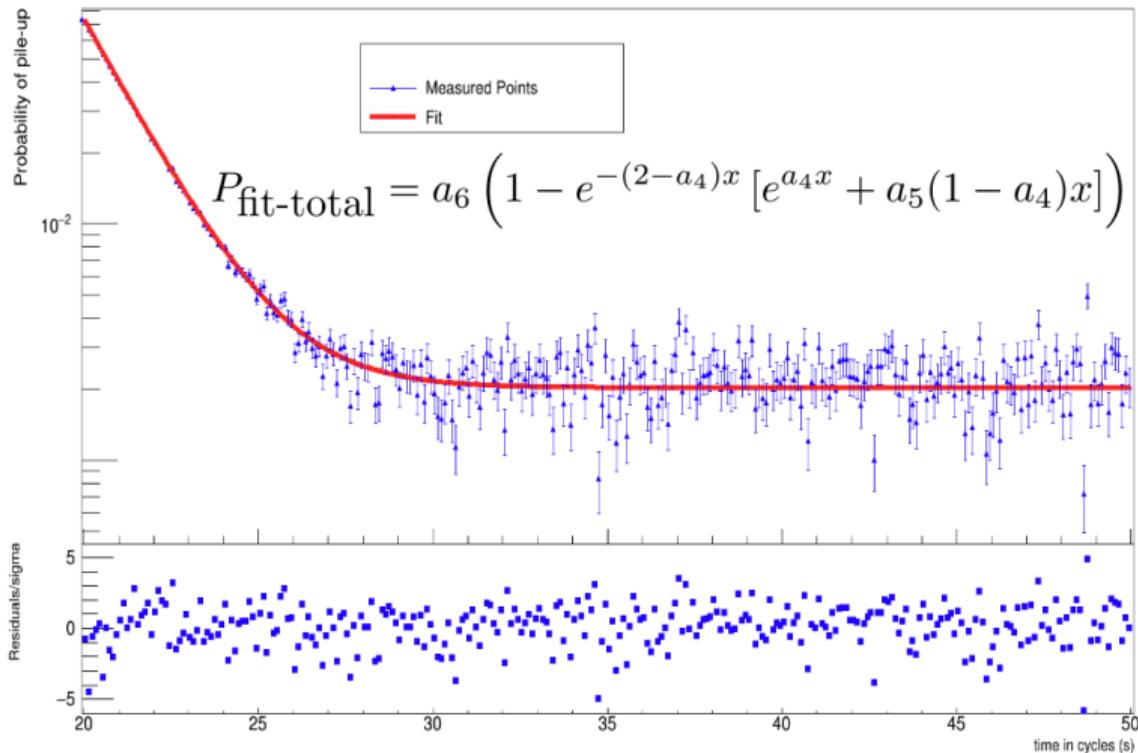


Figure 15: The fit of the probability of pile up with a non zero time resolution, trigger energy threshold and detection efficiency.



Detector Pulse pile-up

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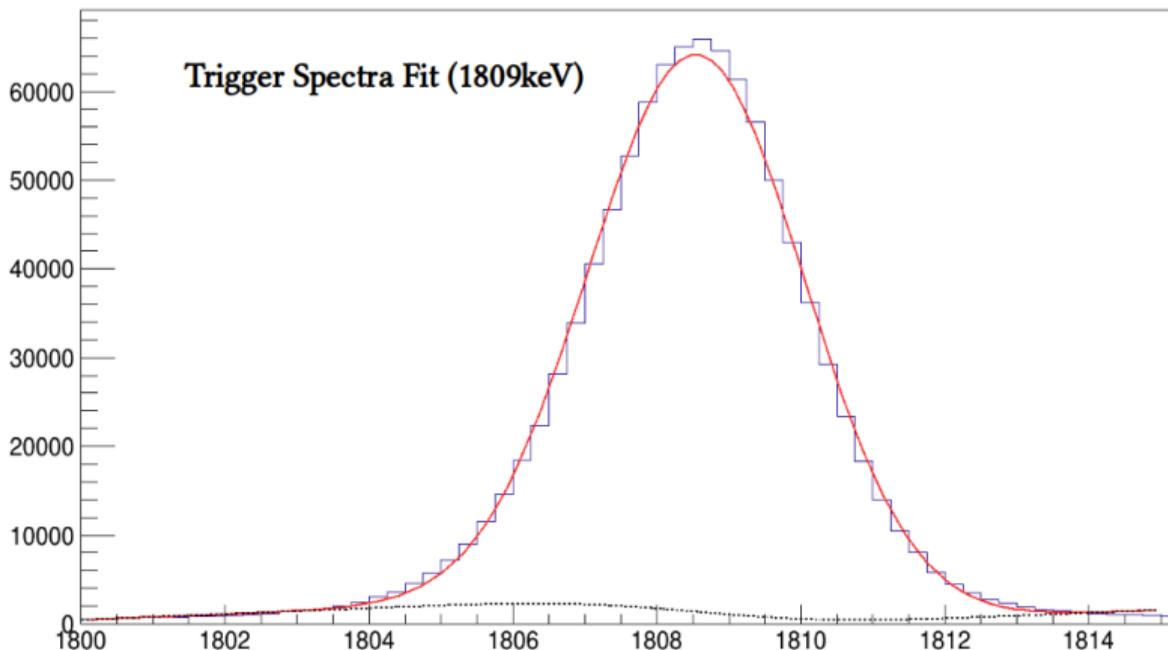
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Name: Chan1807_1799_to_1814
Centroid: 1808.560286 +/- 0.002099
Area: 942457.486746 +/- 1071.417292
FWHM: 3.521101 +/- 0.003560



Detector Pulse pile-up

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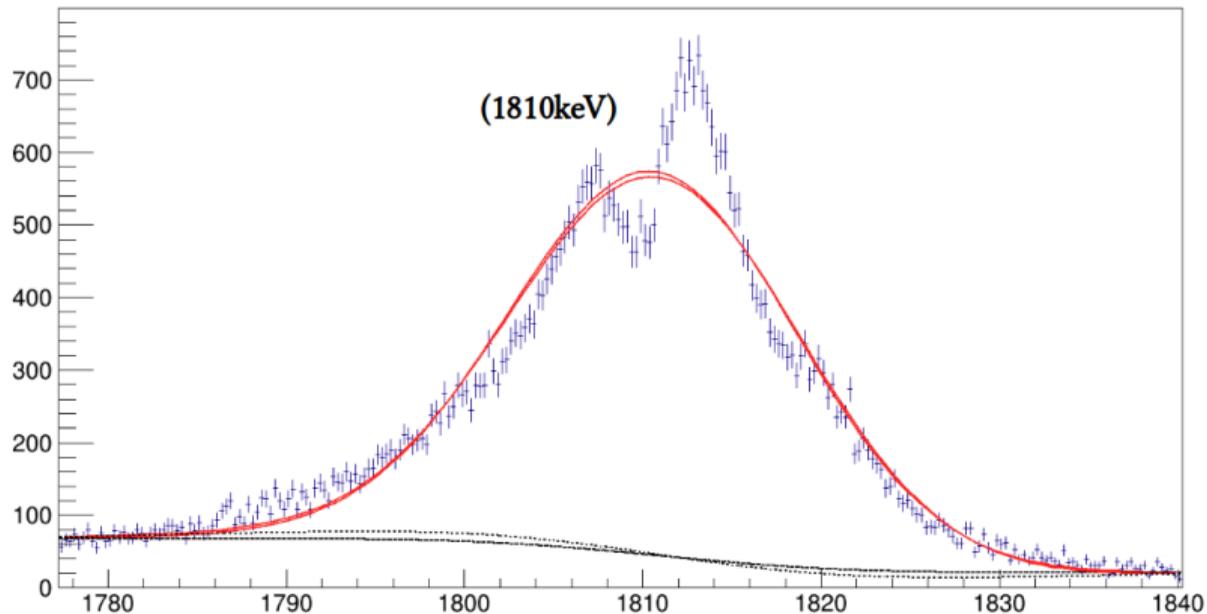
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gE: pile-up, Kvalue < 700

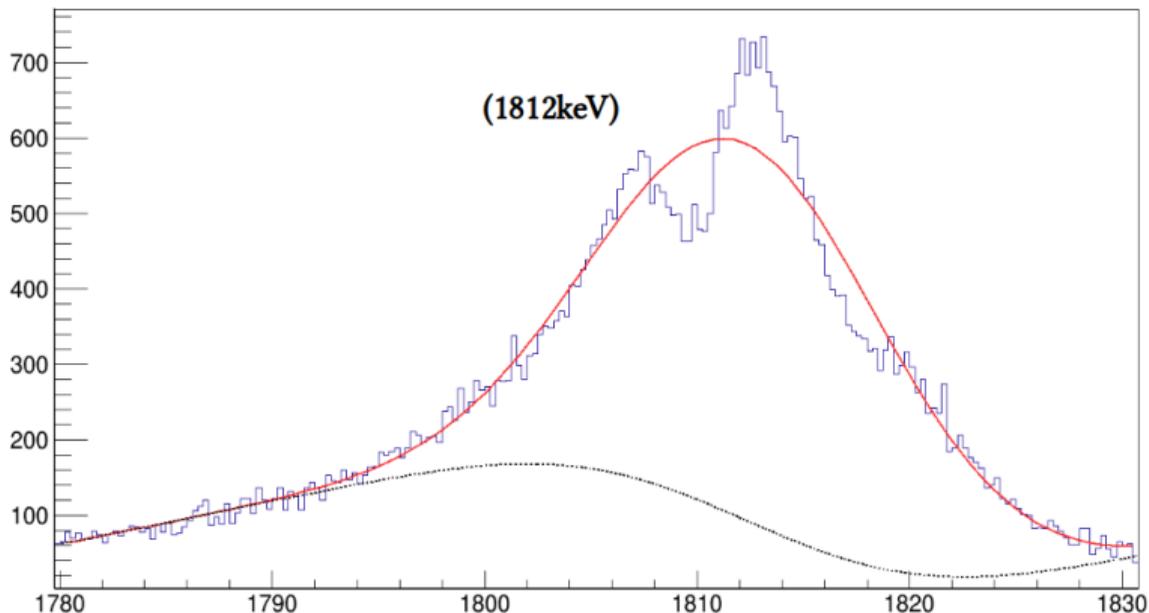


Name: Chan1809_1769_to_1849
Centroid: 1810.898453 +/- 0.074145
Area: 42637.835757 +/- 267.536881
FWHM: 19.244808 +/- 0.121344



Detector Pulse pile-up

gE: pile-up, Kvalue < 700



Name: Chan1805_1780_to_1830
Centroid: 1812.317813 +/- 0.098190
Area: 33952.185520 +/- 461.208716
FWHM: 15.985993 +/- 0.166816

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Step-by-Step Correction

1. Deadfraction Correction

$D_i =$ Dead fraction

$$N_i' = \frac{N_i}{1 - D_i}$$

Deadtime is the total period of time during which hit detection cannot be processed even if they are present.

2. 1st Order Pile-up Correction

$$N_i'' = \frac{N_i'}{1 - P_i}$$

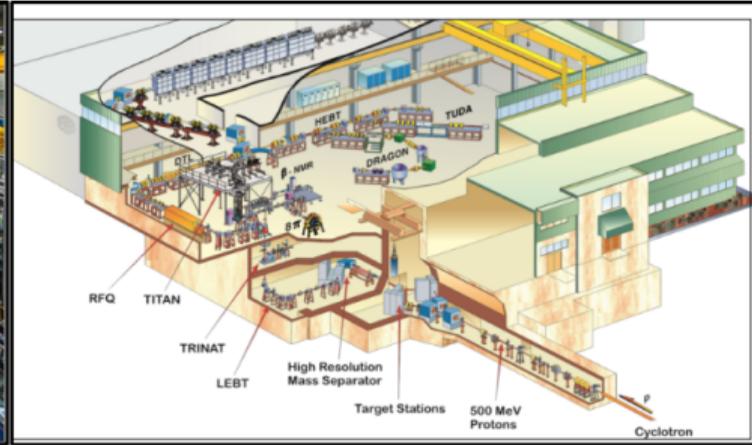
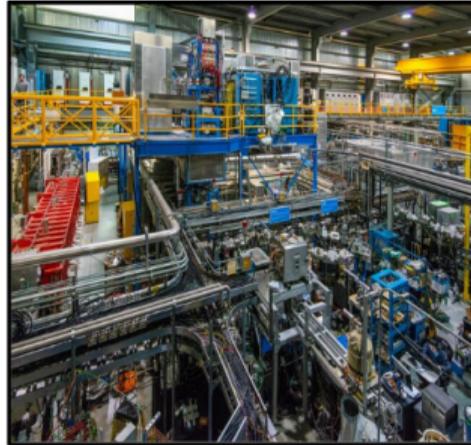
$$P_i = \frac{\text{Pile-up Events}}{\text{All Events}}$$

$$N_i'' = \frac{N_i}{(1 - D_i) \times (1 - P_i)}$$

★ RATE DEPENDENT CORRECTIONS



TRIUMF-ISAC



- Up to $100 \mu\text{A}$, 500 MeV protons from TRIUMF's main cyclotron are accelerated onto targets which produce high-intensity secondary radioactive ion beams by the ISOL technique.

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γ Counting — The 8π Spectrometer

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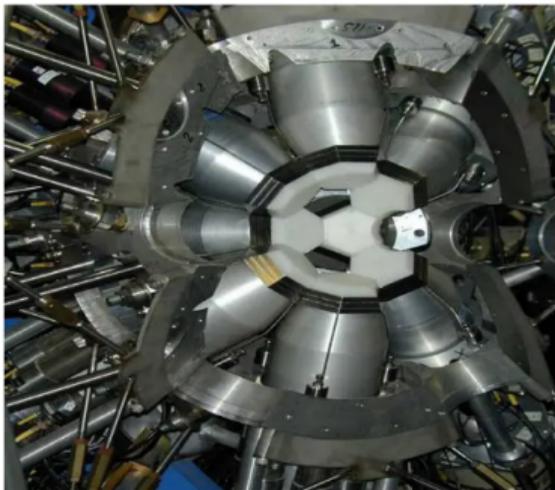
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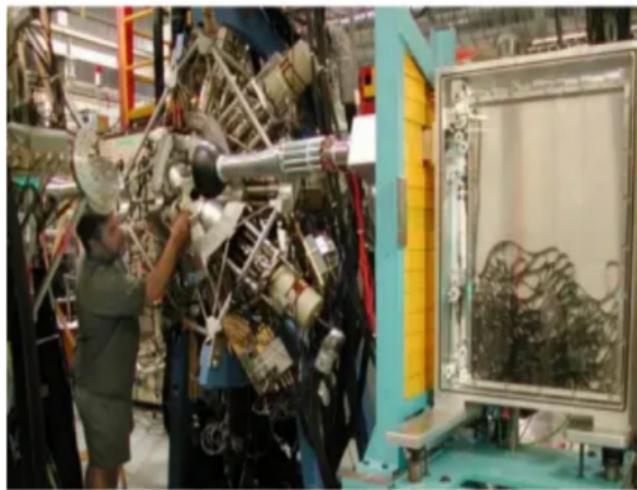
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One hemisphere of the 8pi Gamma-Ray Spectrometer at ISAC-I.



The collection box and lead shielding wall (yellow) for the moving tape collector system of the 8pi Spectrometer.

- **Spherical array of 20 BGO Compton suppressed HPGe detectors**
 - **~1% photopeak efficiency at 1.3 MeV**

After a decade of operation at ISAC-I, **the 8pi Spectrometer was decommissioned** in January 2014 to make way for the **new high-efficiency GRIFFIN spectrometer.**



Half-Life Analysis: ^{26}Na Gated 1809keV Activity

^{26}Na Deduced Half life vs Run numbers

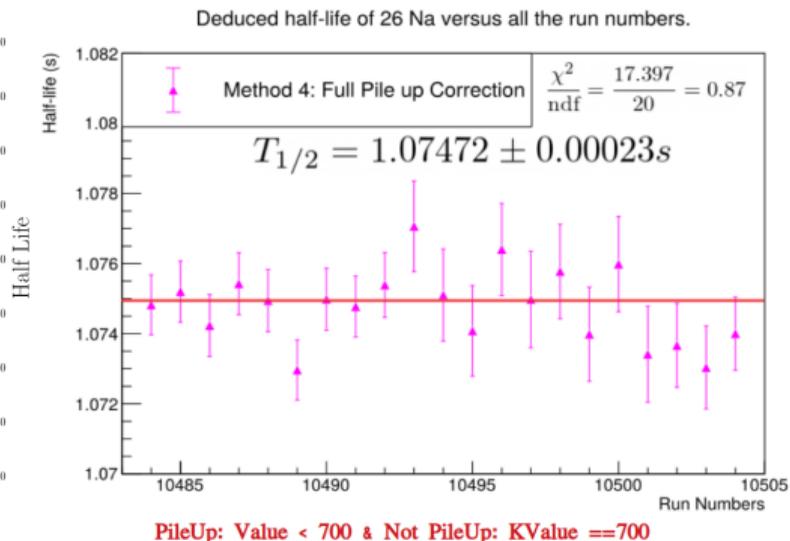
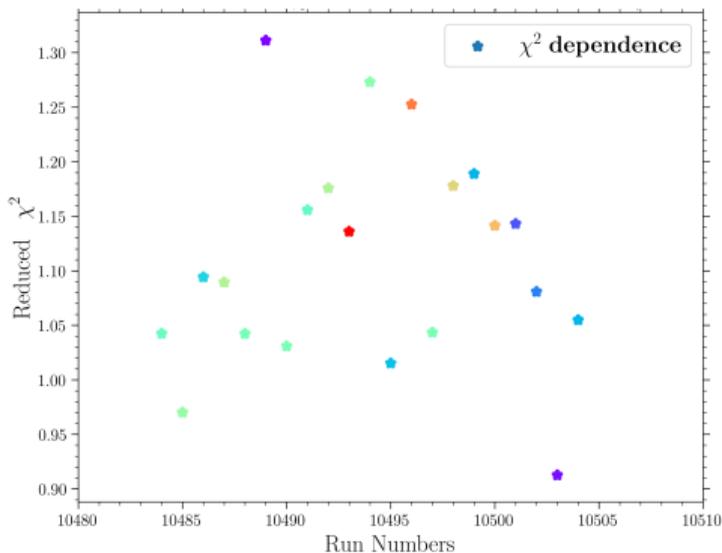


Figure 16: ^{26}Na : Reduced χ^2 vs run numbers(left) and deduced Half life versus run number (right). A weighted average of $T_{\frac{1}{2}} = 1.07472 \pm 0.00023 \text{ s}$ is deduced from these data where the uncertainty is statistical.



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Deduced half-life of ^{26}Na versus the electronic settings.

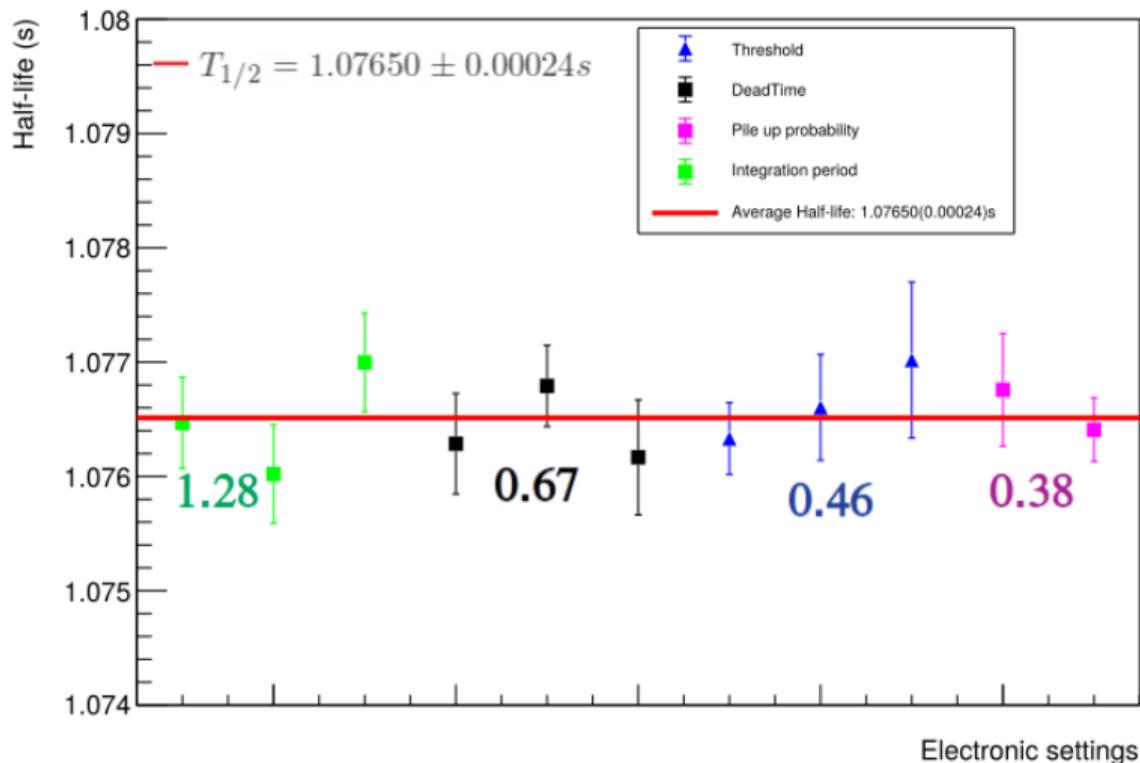


Figure 17: Run 10485: Deduced half-life of ^{26}Na vs. electronic settings



Exploring pile-up options

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Discussion

Half-Life
Analysis: ^{26}Na
Gated 1809keV
Activity

Summary
and Future
Work

Future Plans

Run # 10484: Counts vs. KValue

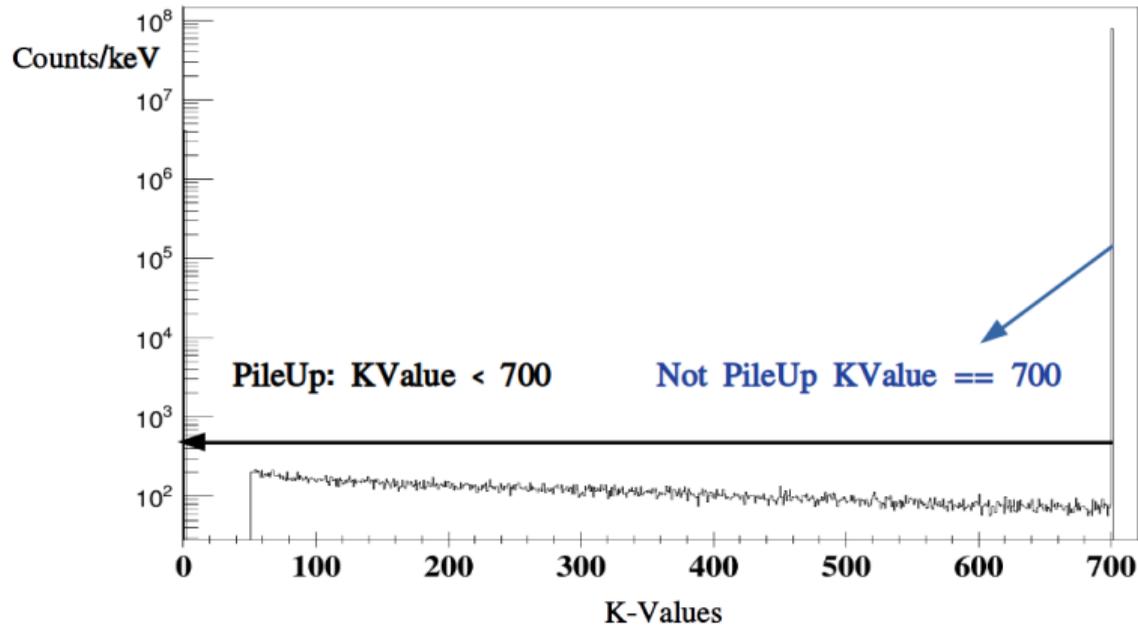


Figure 18: Pile option used: 1-D plot showing the counts versus the integration length.

