

Searches for periodic resonance signals in the dielectron and diphoton channels in ATLAS

Ho Chun Lau (Kyle)

MSc in University of Alberta (Supervisor Prof. Doug Gingrich)

WNPPC

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Motivation

- The Standard Model is not complete
- Gravitation? Hierarchy problem? Higgs naturalness problem?
- String theory predicts the existence of the gravitational force carrier – [Graviton](#)
- [Periodic resonances](#)? Most studies focus on [non-periodic resonances](#)

Motivation

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- **Periodic resonances?** Most studies focus on non-periodic resonances

Benchmark Model:

- **Clockwork theory** is a model-building mechanism to generate fundamental particles
- **Clockwork theory** suggested graviton with **different mass modes** and **periodic resonances**

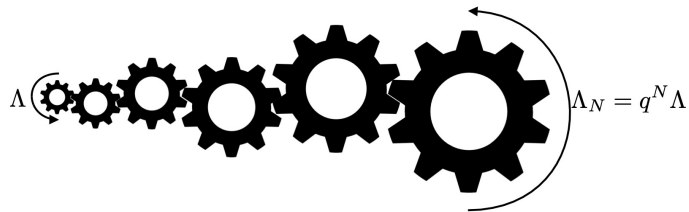
The full work is recorded at <https://cds.cern.ch/record/2754323> (internal only)

Clockwork theory

- Live in warped 5D metric

$$ds^2 = e^{\frac{4}{3}k\pi R} (\eta_{\mu\nu} dx^\mu dx^\nu + \pi^2 dR^2)$$

- Provide a mechanism to generate particles in all ranges of scales.



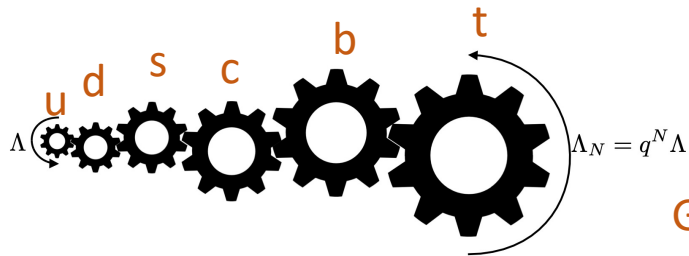
- With a small interaction scale Λ , we can leverage **discretely** to an exponentially large Λ

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Getting top quark from up quark!

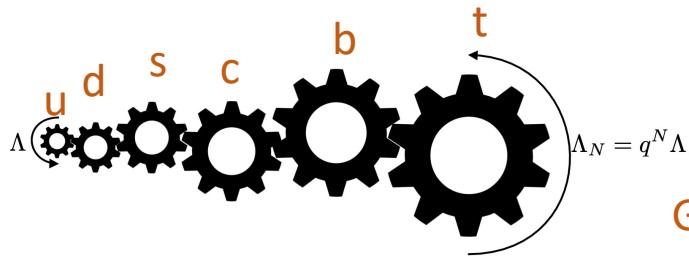
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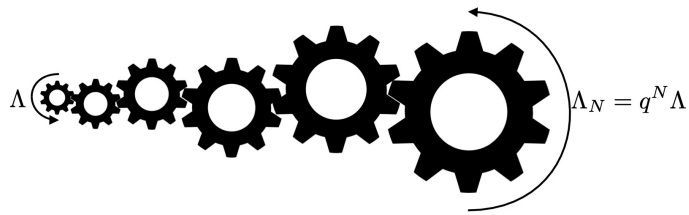
Getting top quark from up quark!

- With a small interaction scale Λ , we can leverage **discretely** to an exponentially large Λ
- A solution to the Hierarchy problem similar to Little String Theory
- A solution to the Higgs naturalness problem similar to Large Extra Dimension model(LED) and the Randall-Sundrum(RS) model

Undetermined parameters k , M_5 , R

$$ds^2 = e^{\frac{4}{3}k\pi R}(\eta_{\mu\nu}dx^\mu dx^\nu + \pi^2 dR^2)$$

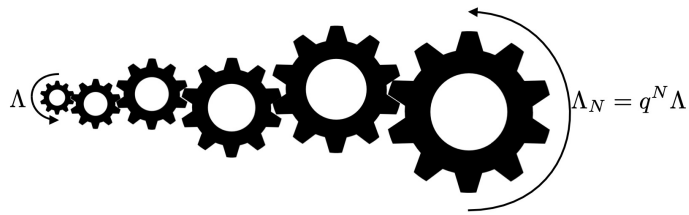
- k Higgs-curvature is a metric parameter, the “spring constant” for the clockwork model
- R is the cut-off range for the high dimension gravitational potential
- M_5 fundamental scale related to Λ , also known as 5D reduced Planck mass



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- Related by an equation, where M_p is the 4D(3+1) Planck mass.

$$M_P^2 = \frac{M_5^3}{k} (e^{2\pi k R} - 1)$$

$$k, M_5, R \quad M_P^2 = \frac{M_5^3}{k} (e^{2\pi k R} - 1)$$

- 4D Planck mass M_p can be obtained by rewriting Newtonian Gravitational potential

$$V(r) = \frac{Gm_1m_2}{r} = \frac{m_1m_2}{M_p^2 r}$$

- Extend the potential to 4+n dimensions

$$V(r) = \frac{m_1m_2}{M_n^{2+n}} \frac{1}{r^{1+n}} \quad (\text{in } 4+n\text{-Dimensions})$$

- Make consistent with Newtonian gravity, setting cut off range R so that we get 4D potential at $r \gg R$.

$$V(r) = \frac{m_1m_2}{M_n^{2+n}} \frac{1}{R^n} \frac{1}{r} \quad (\text{in } 4+n\text{-Dimension but } r \gg R)$$

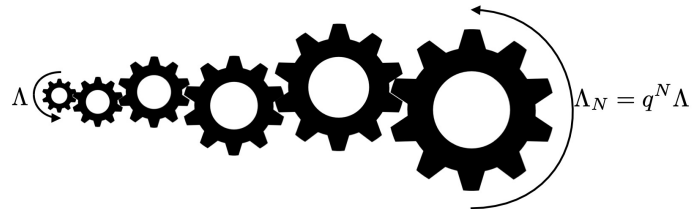
k, M_5, R

$$V(r) = \frac{m_1 m_2}{M_p^2} \frac{1}{r} = \frac{m_1 m_2}{M_n^{2+n}} \frac{1}{R^n} \frac{1}{r}$$

$$M_n^{2+n} = \frac{M_p^2}{R^n}$$

- $n=1$ for one extra space $M_5^3 = \frac{M_p^2}{R}$

- Adding in the curved metric effect, we obtain $M_P^2 = \frac{M_5^3}{k} (e^{2\pi k R} - 1)$



+

$$ds^2 = e^{\frac{4}{3}k\pi R} (\eta_{\mu\nu} dx^\mu dx^\nu + \pi^2 dR^2)$$

Searching Routine

Simulating Physics

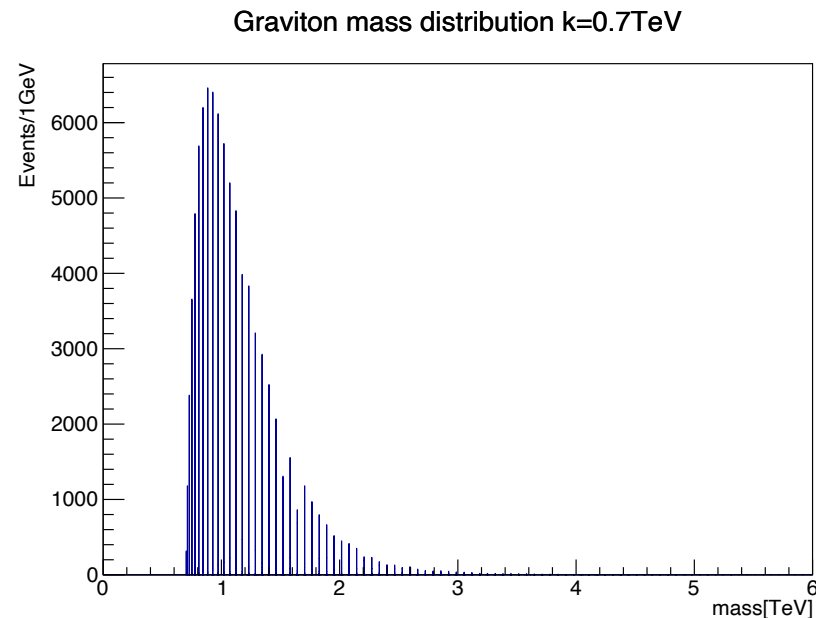
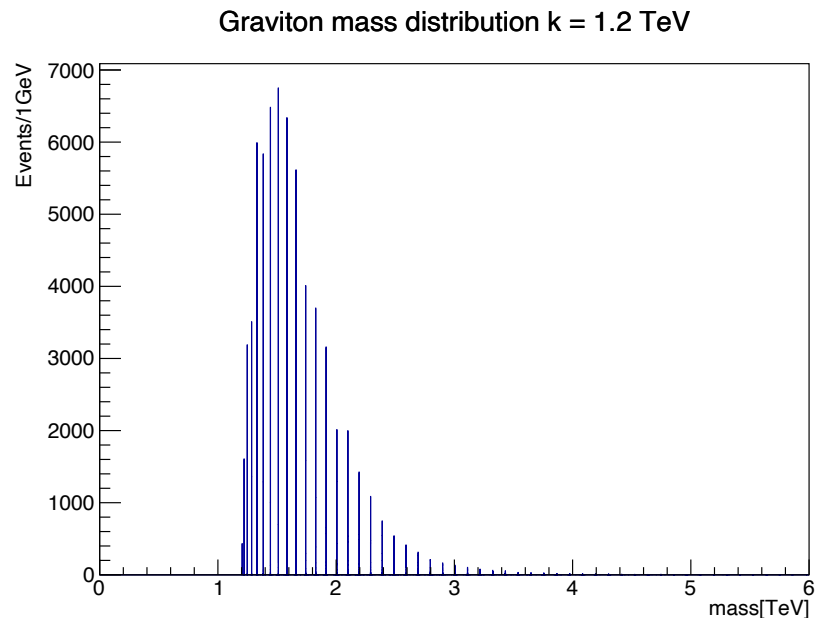
Simulating Detector
Responses

Analyzing responses

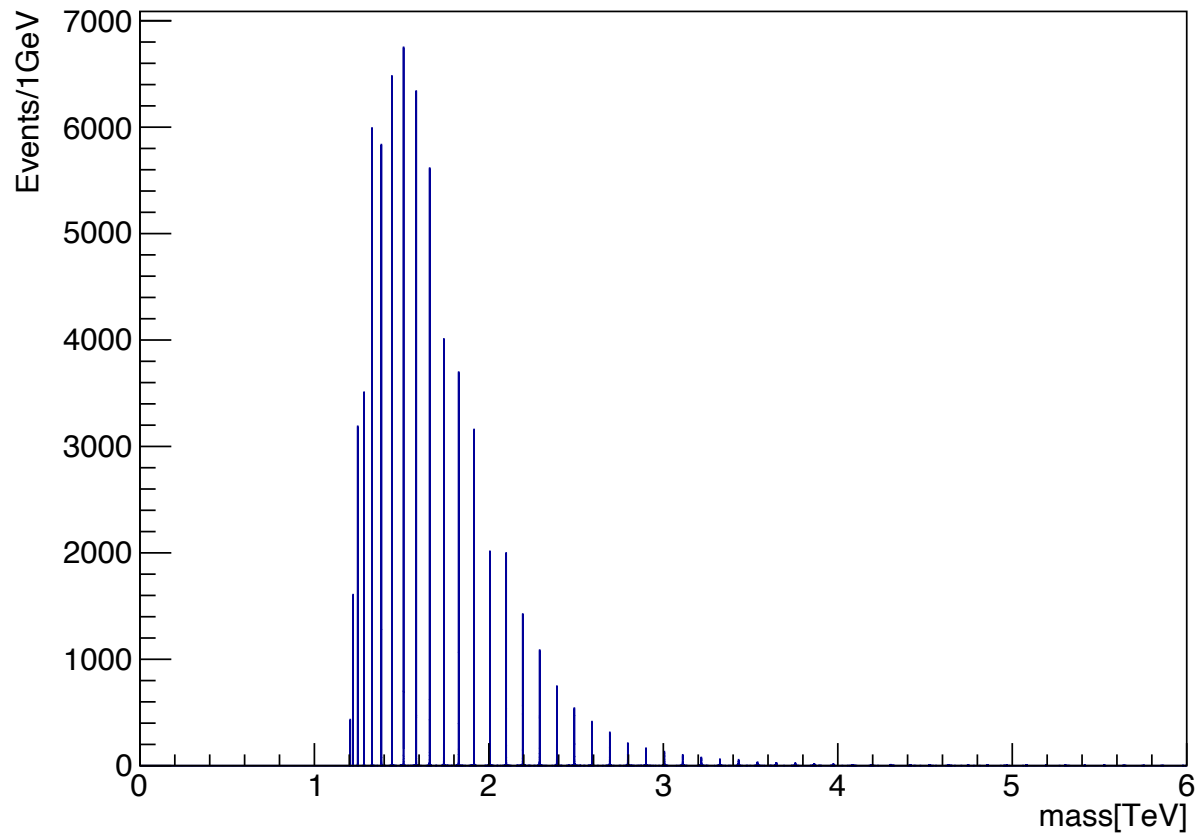
Clockwork graviton Physics

- Clockwork gravitons are predicted to have different mass modes, each having a different mass and interaction strength.
- $\text{Br}(G \rightarrow \gamma\gamma) = 4\%$ $\text{Br}(G \rightarrow ee) = 2\%$
- Search the phase space (k, M_5) by simulating clockwork graviton at different (k, M_5)

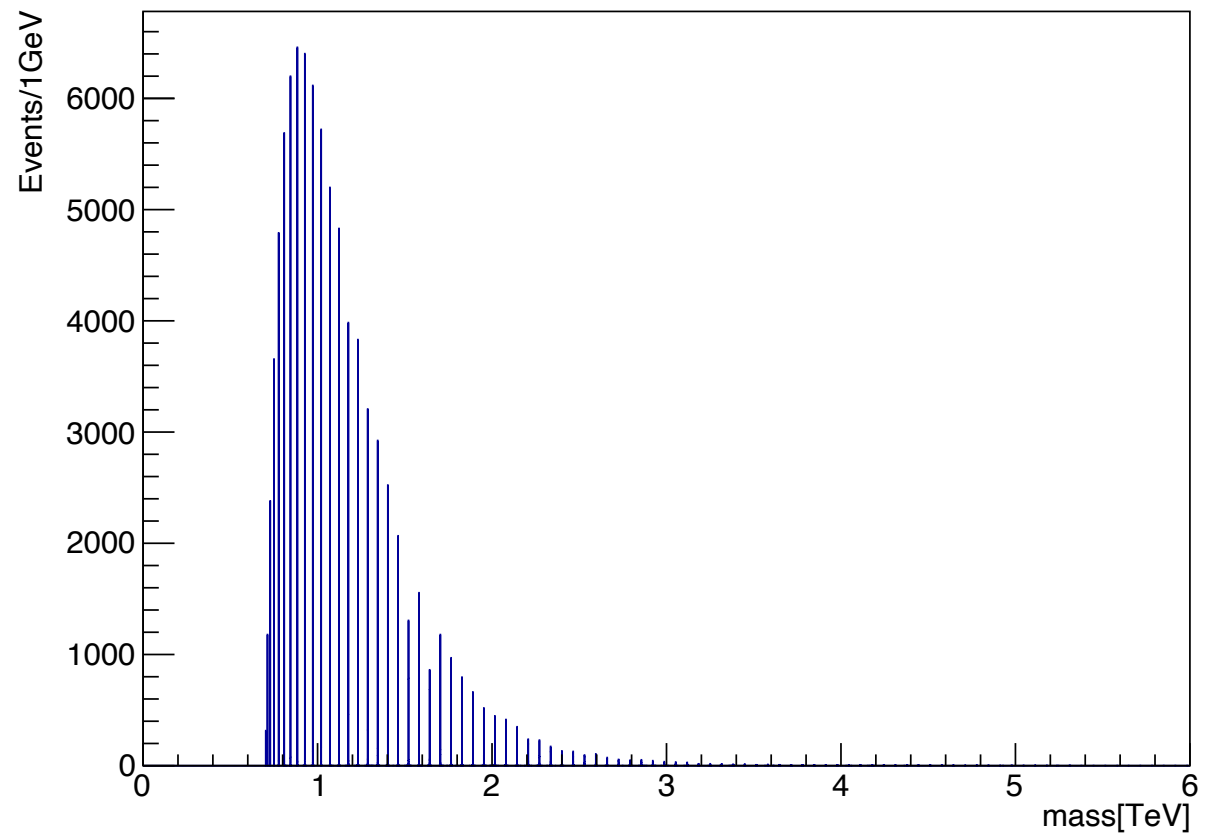
$$m_0 = 0, \quad m_n^2 = k^2 + \frac{n^2}{R^2}, \quad n = 1, 2, 3, \dots$$



Graviton mass distribution $k = 1.2 \text{ TeV}$



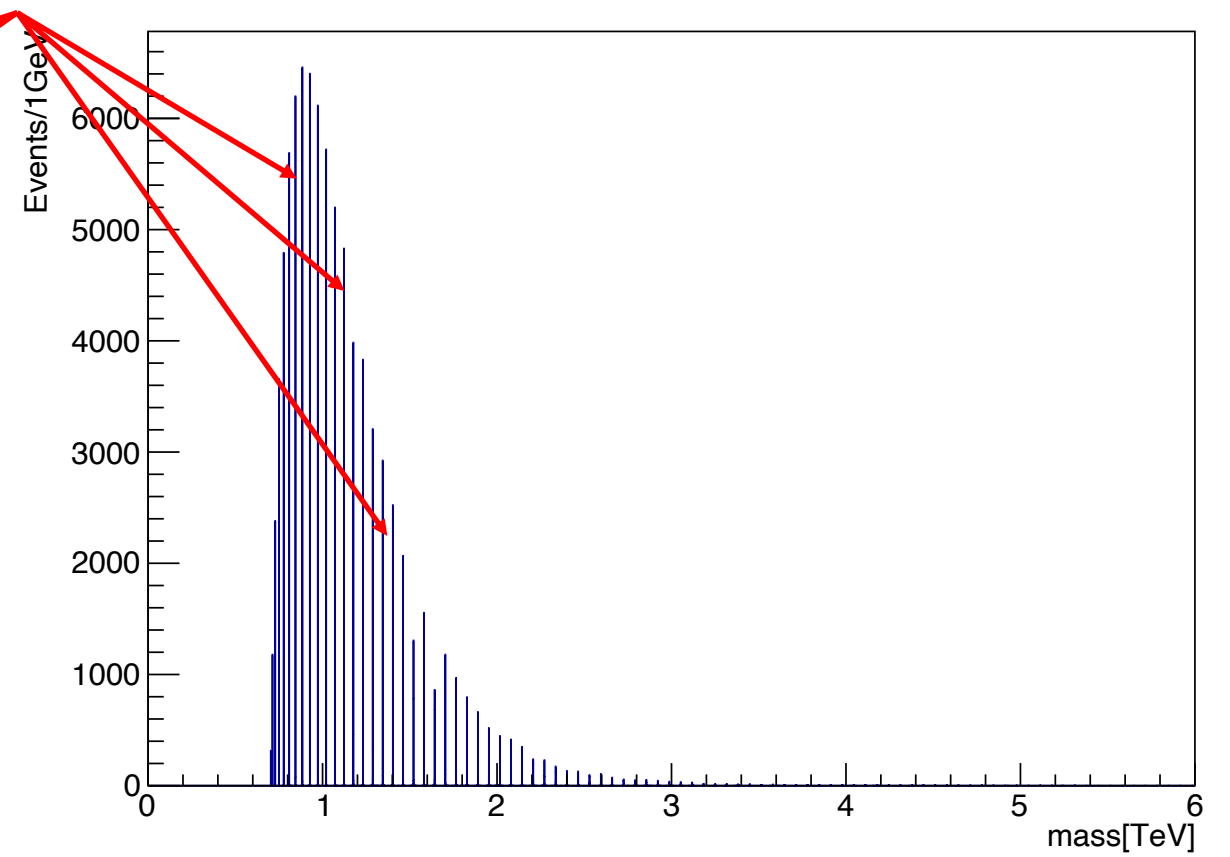
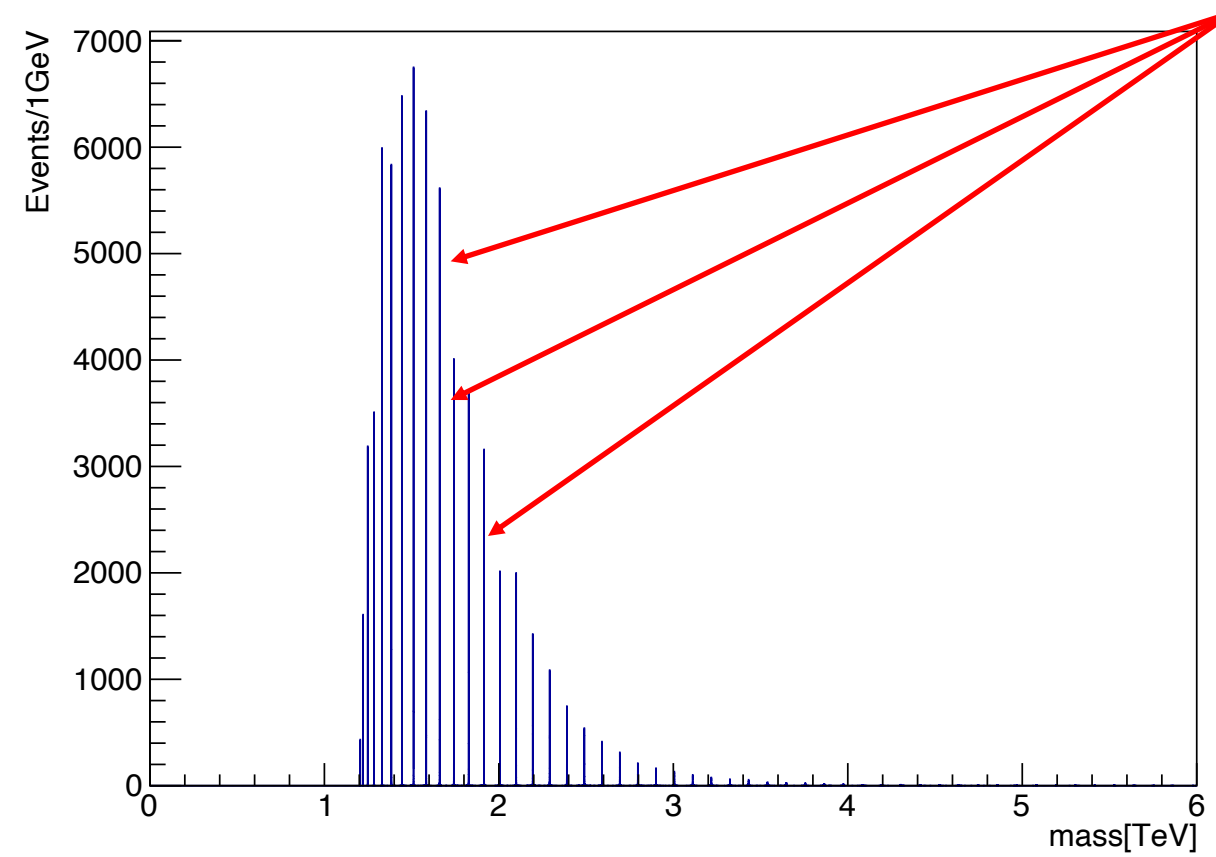
Graviton mass distribution $k=0.7\text{TeV}$



Features	Analysis benefit

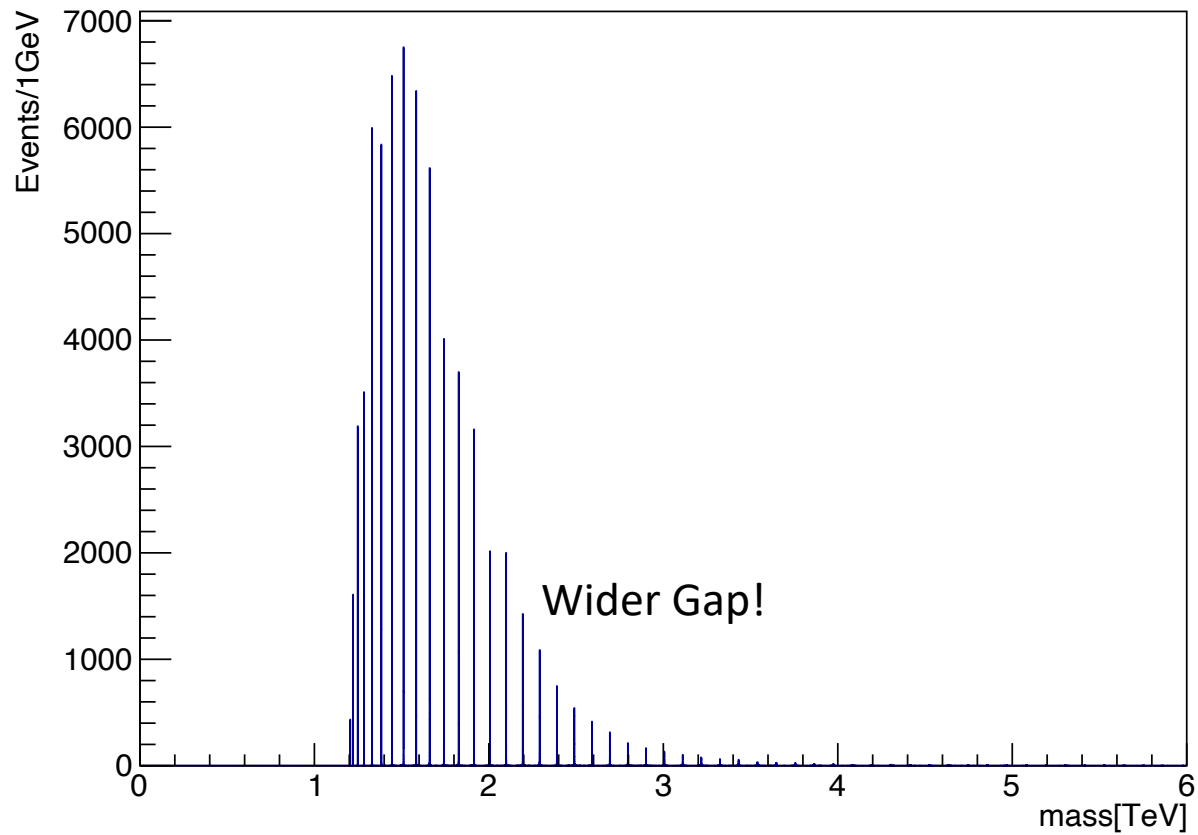
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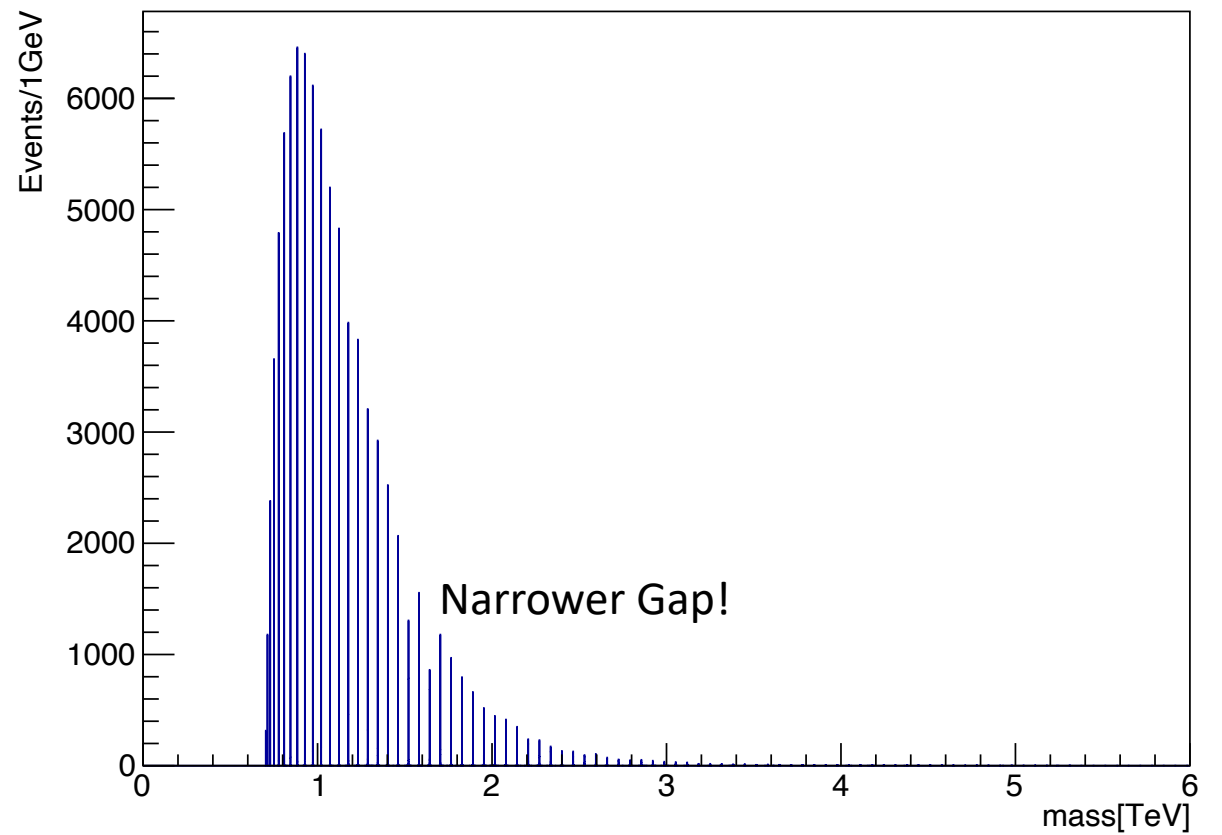


Features	Analysis benefit
Many Peaks!	Oscillation!

Graviton mass distribution $k = 1.2 \text{ TeV}$

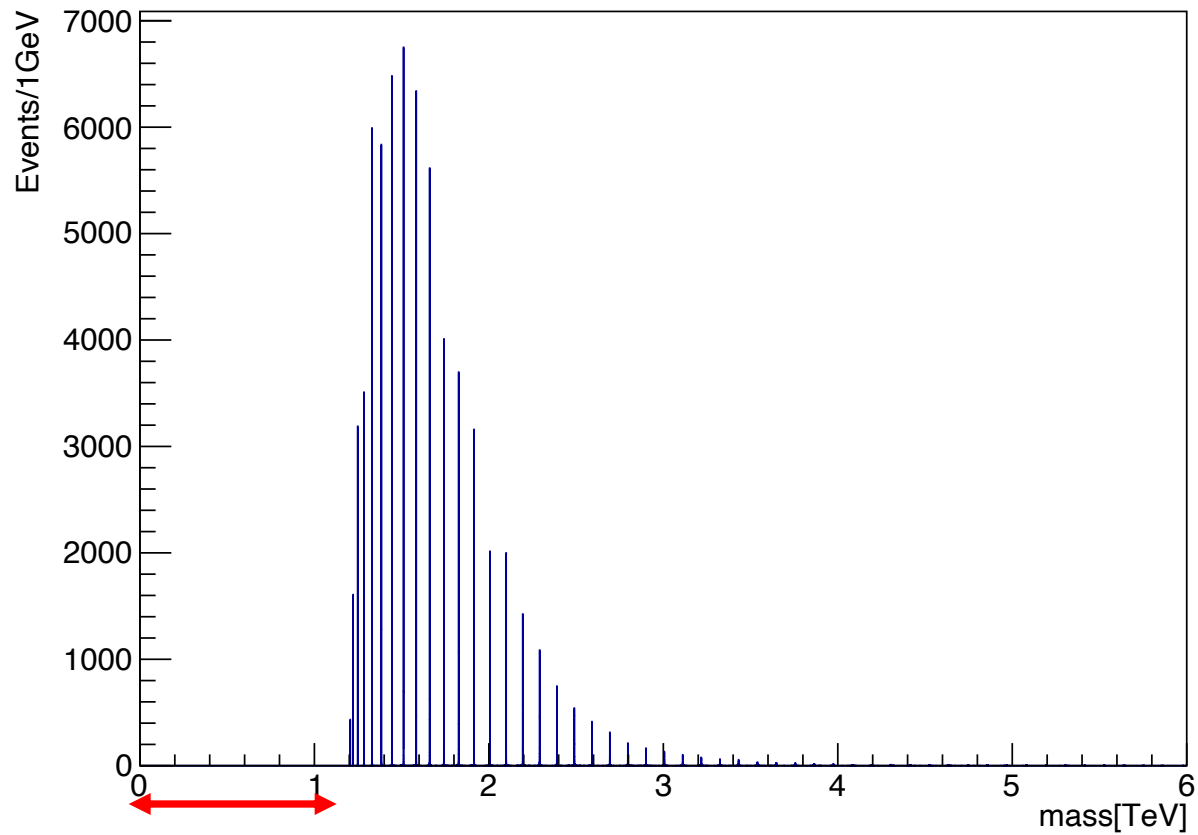


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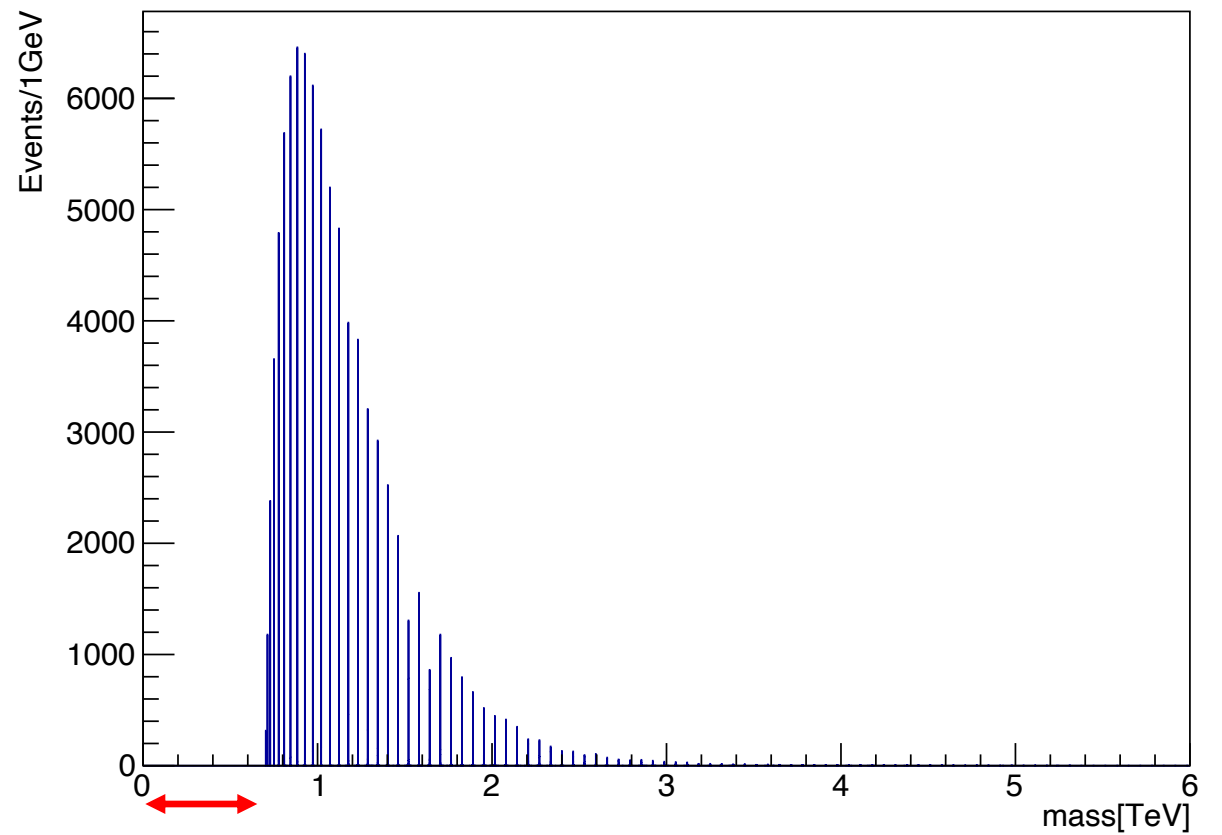


Features	Analysis benefit
Many Peaks!	Oscillation!
Wide/Narrow gap between peaks!	Unique frequency!

Graviton mass distribution $k = 1.2 \text{ TeV}$



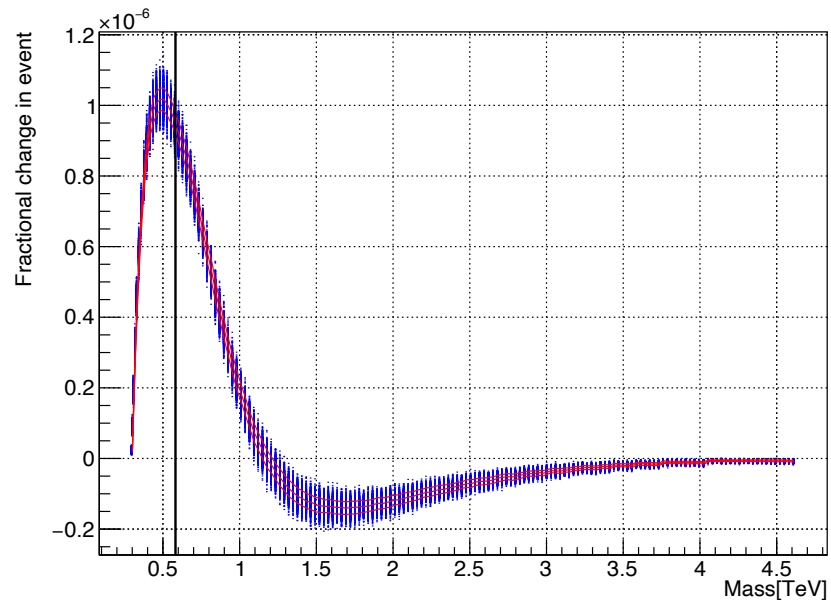
Graviton mass distribution $k=0.7\text{TeV}$



Features	Analysis benefit
Many Peaks!	Oscillation!
Wide/Narrow gap between peaks!	Unique frequency!
Different minimum mass!	Mass range for analysis!

Cascade of decay

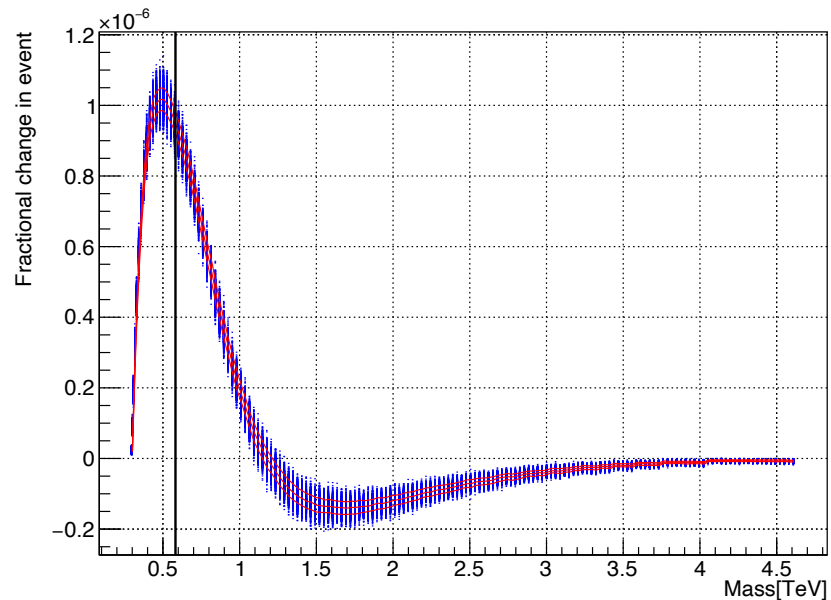
- $G(\text{mass mode } 40) \rightarrow G(26)G(14)$
- But the daughter $G(26)$ may also decay to $G(2)G(1)$: $G(26) \rightarrow G(1)G(2)$



The fractional change after including cascade effect,
 $k=0.3\text{TeV}$

Cascade of decay

- $G(\text{mass mode } 40) \rightarrow G(26)G(14)$
- But the daughter $G(26)$ may also decay to $G(2)G(1)$: $G(26) \rightarrow G(1)G(2)$
- **MORE** lower-mass gravitons & **fewer** higher-mass gravitons



The fractional change after including cascade effect,
 $k=0.3\text{TeV}$

Searching Routine

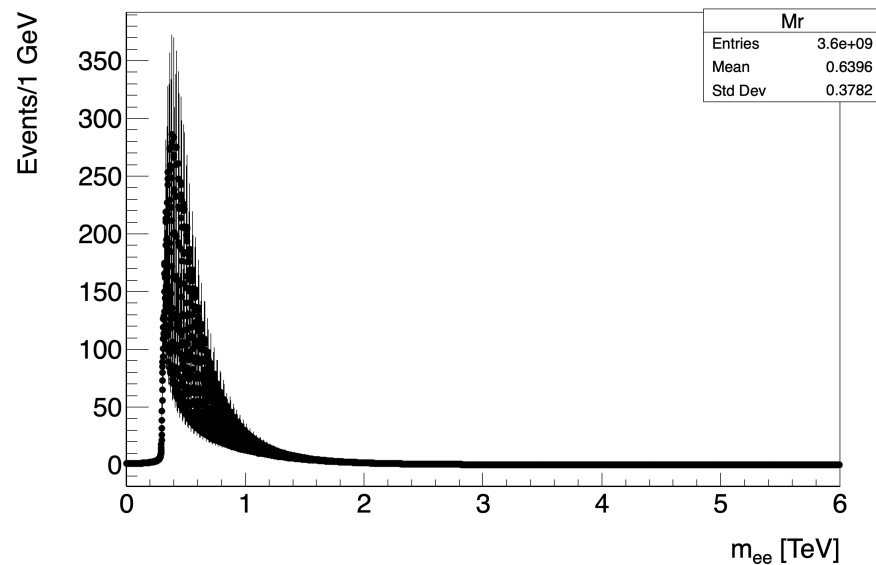
Simulating Physics

Simulating Detector
Responses

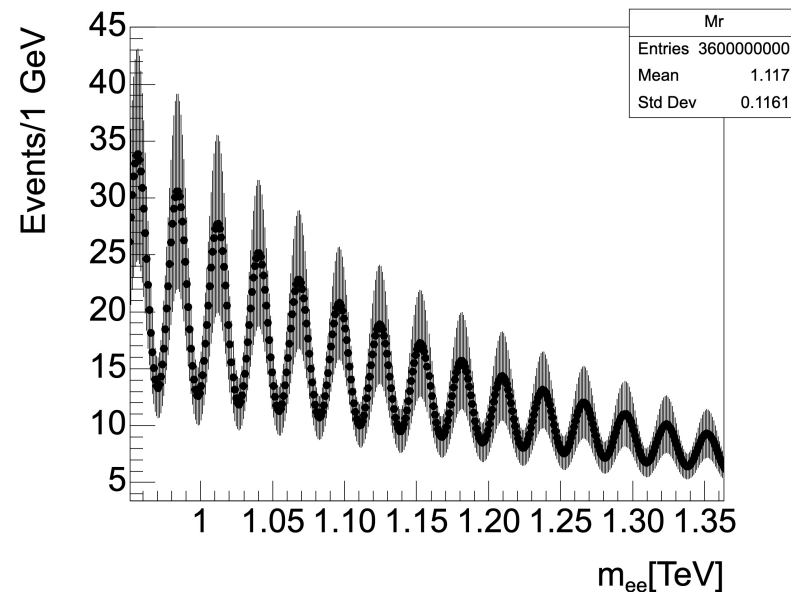
Analyzing responses

From Pythia to Detector responses

- Generating the reconstruction result of the detector.
- Transform/convolution method
- The resolution function for dielectron and diphoton channels are different for ATLAS



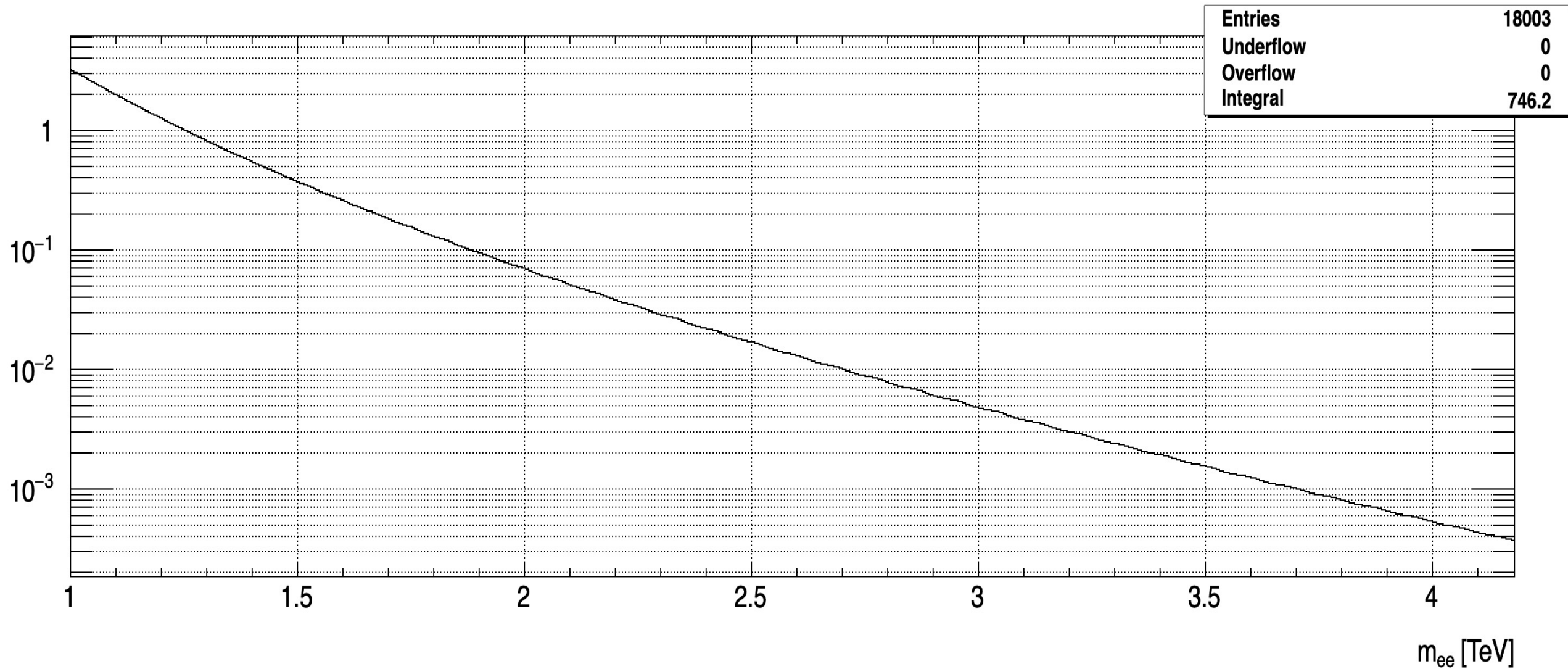
Example plot of transferred result with dielectrons resolution function $k=300\text{GeV}$



An enlarged version of the left plot to show the oscillation

MC Signal+Background example

Eyes exam: can you see the wiggling?



Searching Routine

Simulating Physics

Simulating Detector
Responses

Analyzing Responses

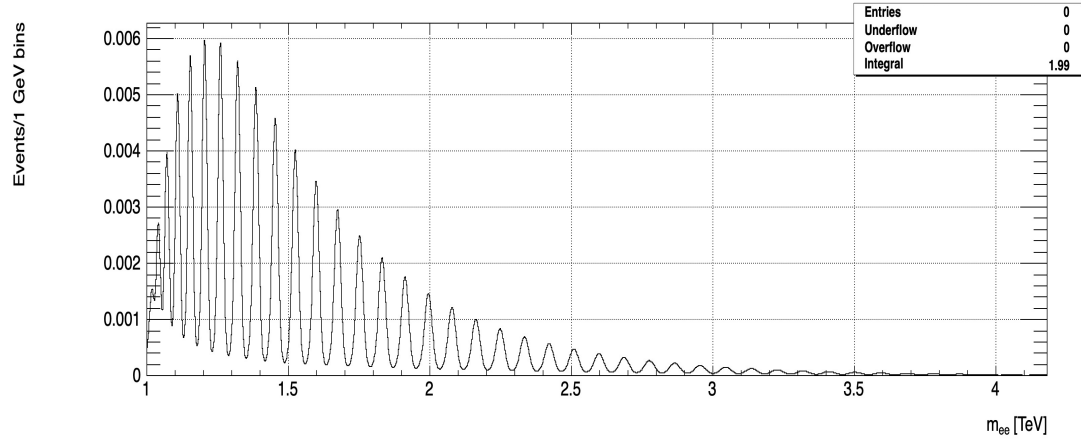
Fourier Transform analysis

- The oscillating spectrum implies the possibility of using Fourier Transform analysis
- We applied **discrete Fourier Transform** and studied **power spectrum P(T)**
- In the power spectrum, we define the peak of the spectrum to be our test statistic for the hypothesis test

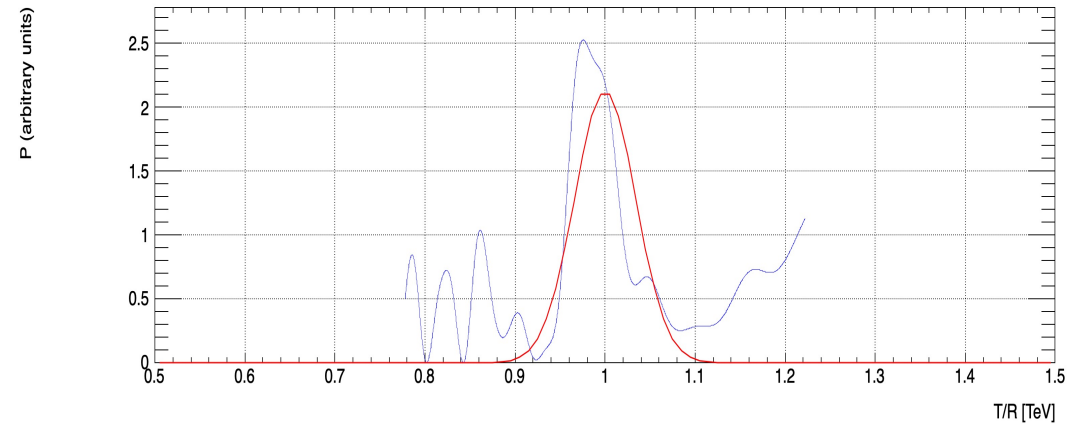
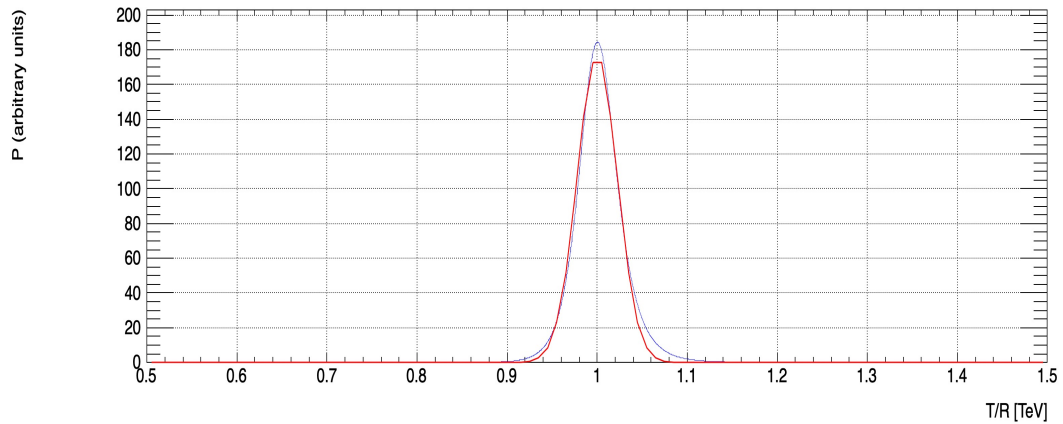
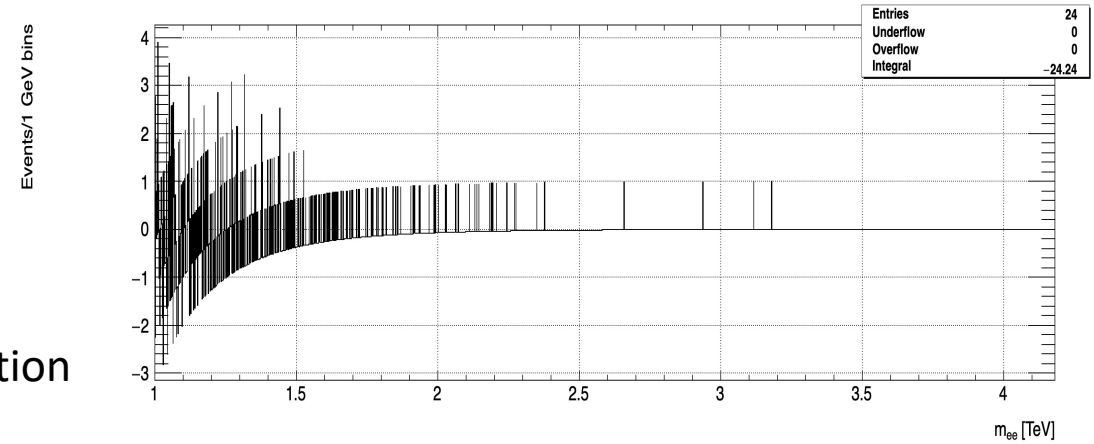
$$P(T) = \left| \frac{1}{\sqrt{2\pi}} \int_{m_{\min}}^{m_{\max}} dm \frac{d\sigma}{dm} \exp\left(i \frac{2\pi\sqrt{m^2 - k^2}}{T}\right) \right|^2$$

- Background is in appendix

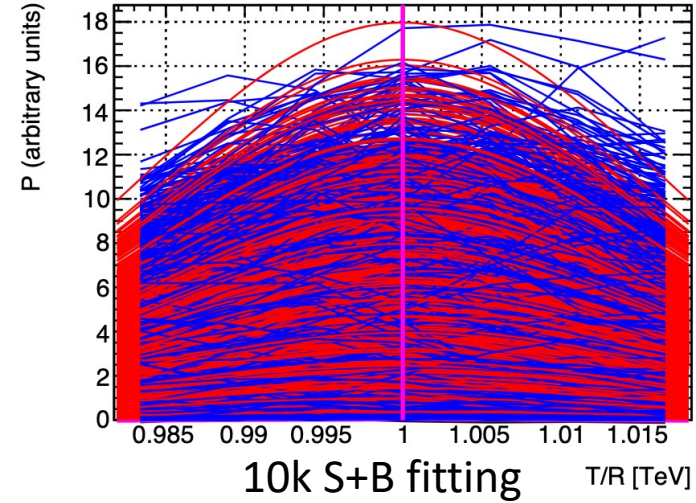
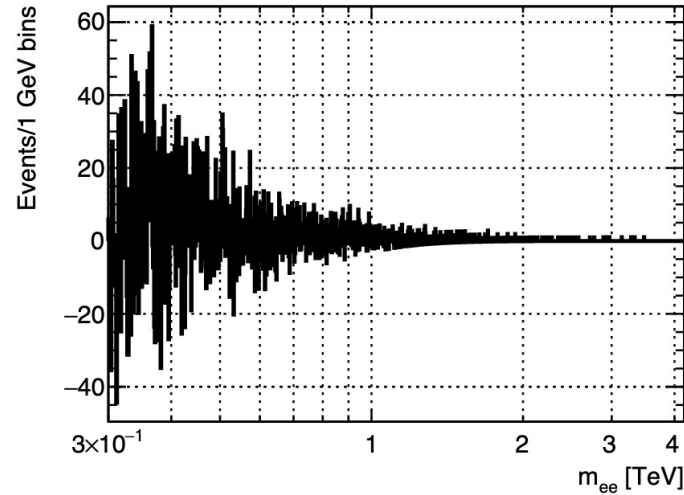
Fourier transform example



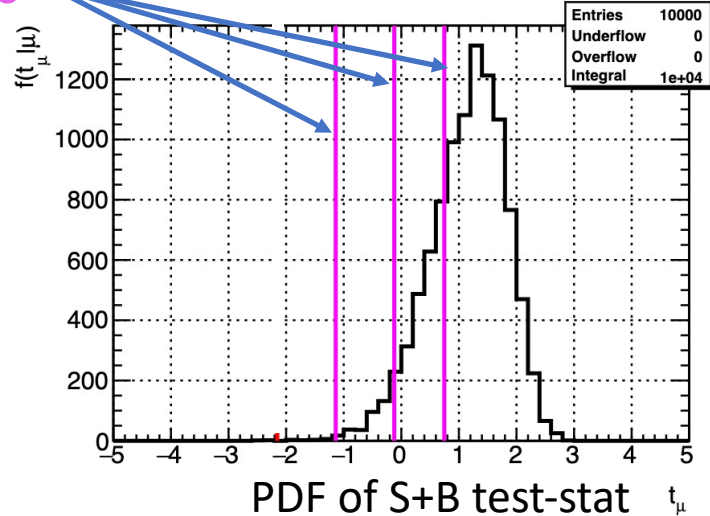
Poisson Fluctuation
→



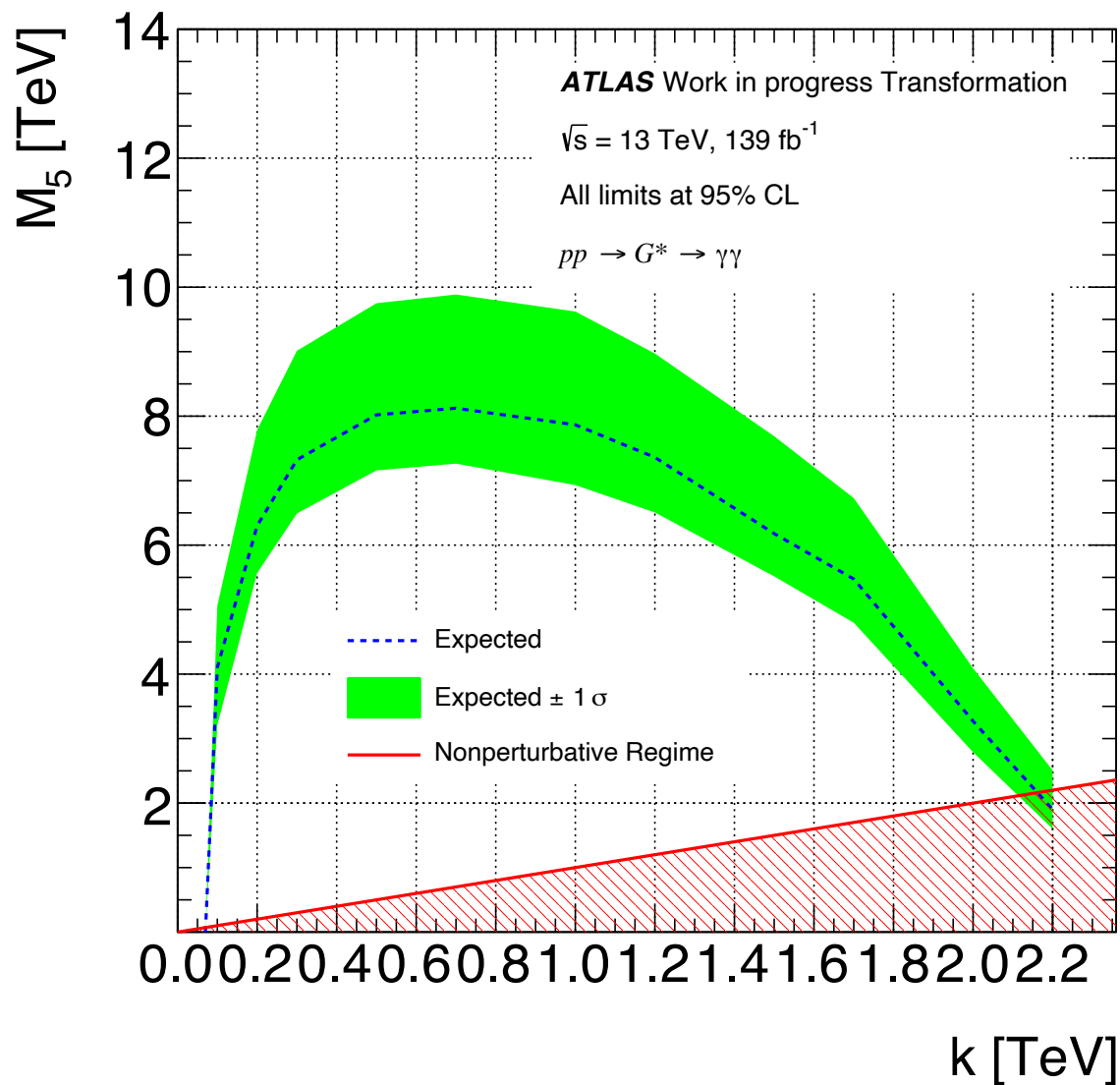
Applying Fourier Transform



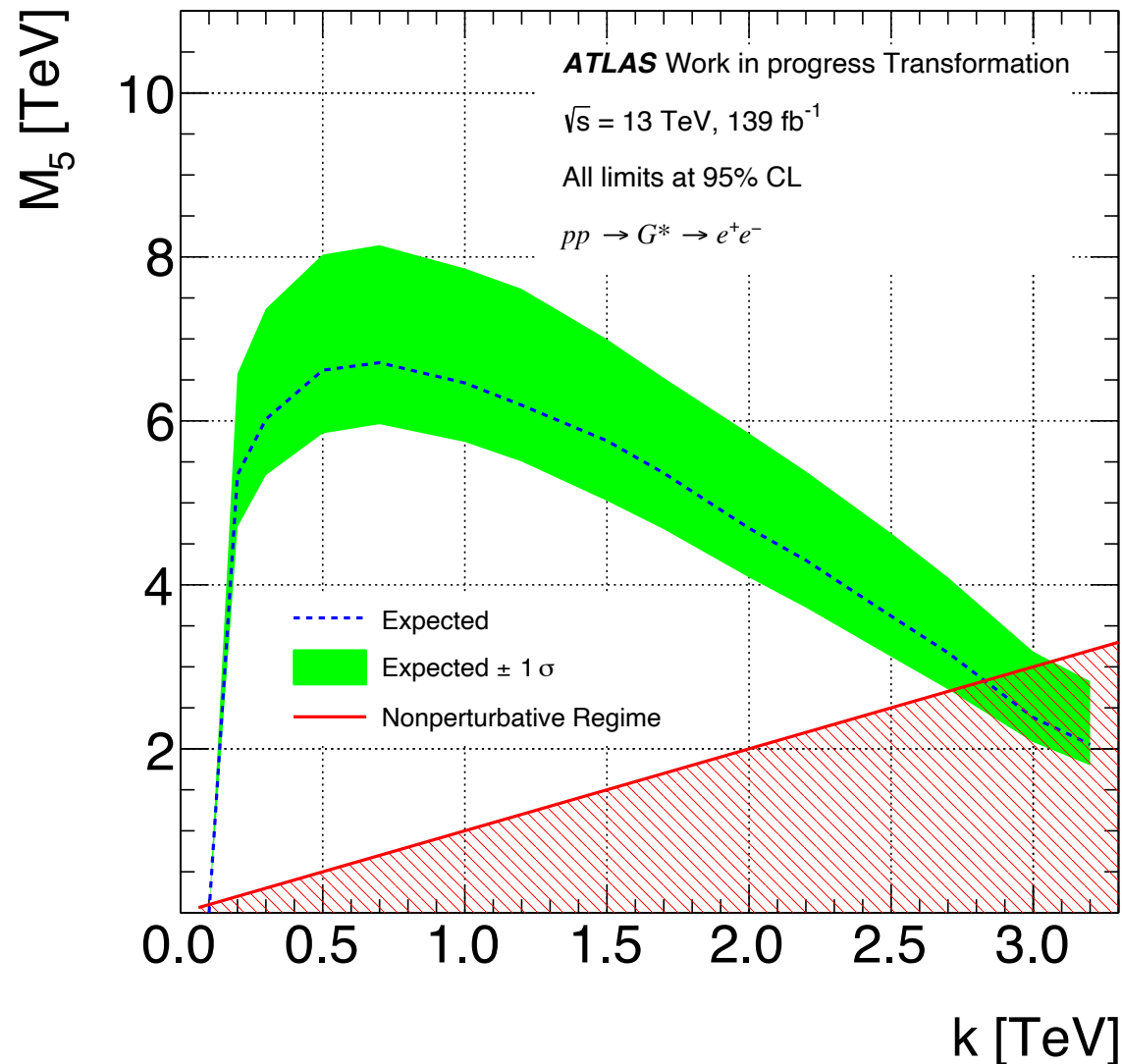
Bkg only test-stat $\mu \pm \sigma$



95% LOWER limit plot



$$M_5 \propto 1/\text{cross-section}$$



Q&A

Thanks for listening

Appendix -- k M₅ R

$$M_P^2 = \frac{M_5^3}{k} (e^{2\pi k R} - 1)$$

- 3D Planck mass M_p can be obtained by rewriting Newtonian Gravitational potential

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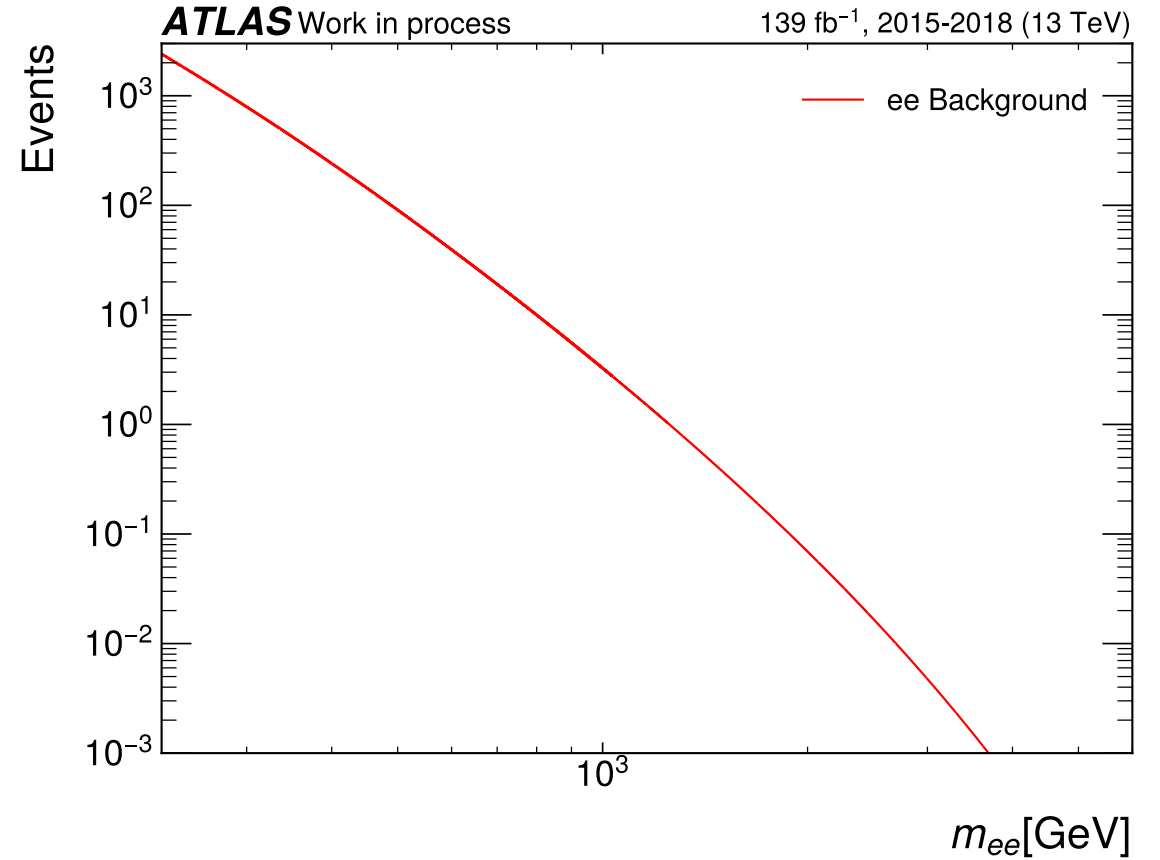
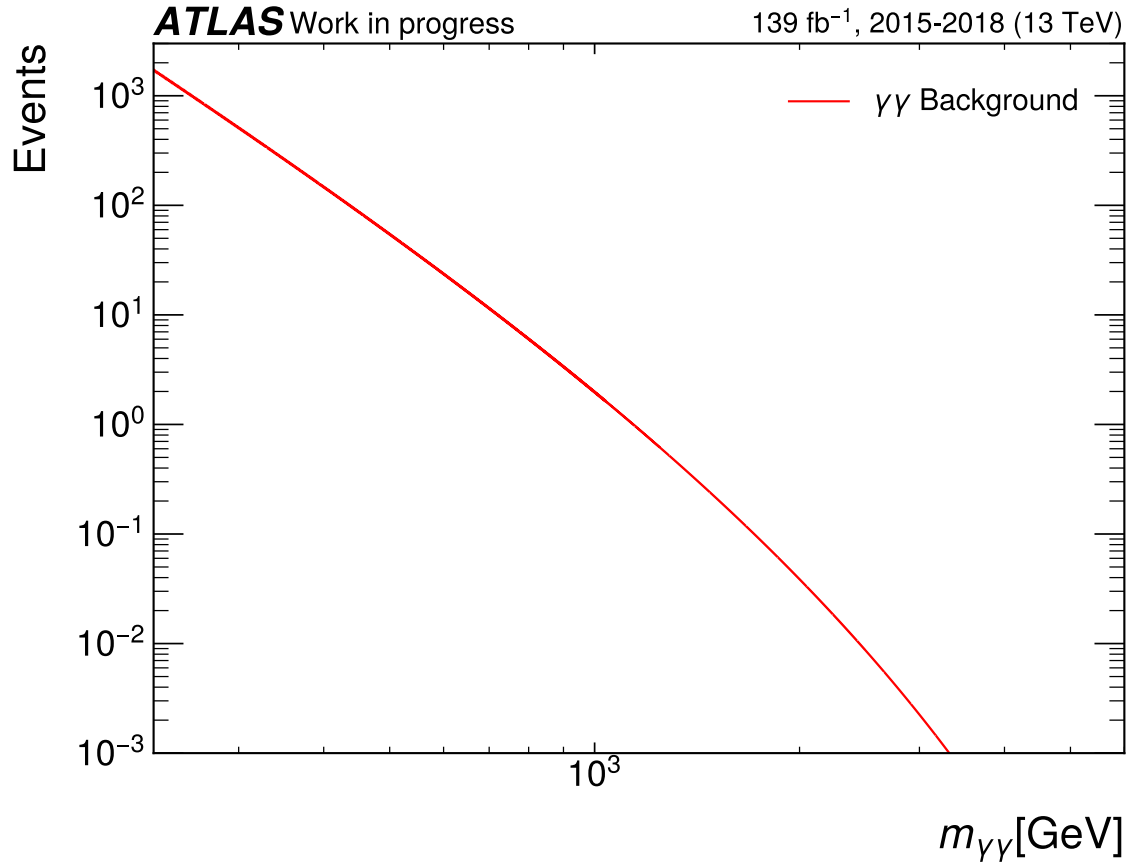
- Fourier transform of 3+n-dimensions gravitational potential

$$V(r) \propto \int d^{3+n}k e^{i\vec{k}\cdot\vec{x}} \frac{1}{\vec{k}^2} \propto \frac{1}{r^{1+n}} \quad V(r) = \frac{m_1m_2}{M_n^{2+n}} \frac{1}{r^{1+n}} \quad (\text{in } 3+n\text{-Dimensions})$$

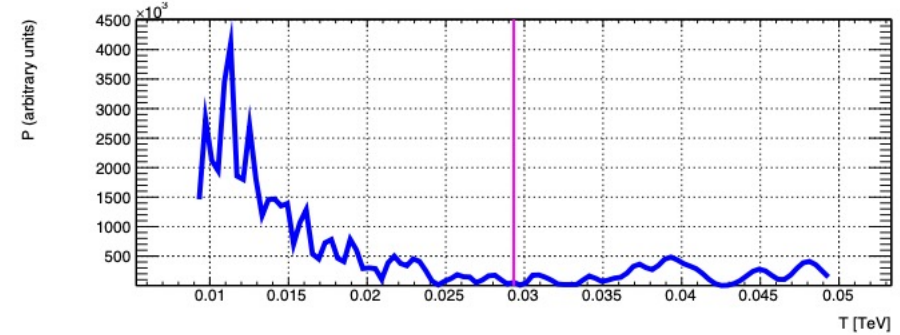
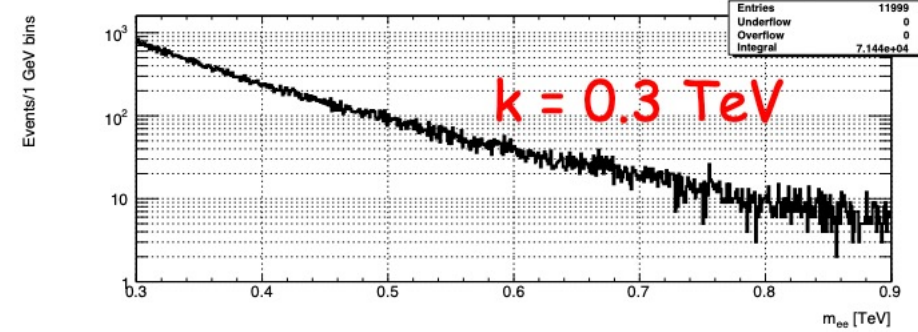
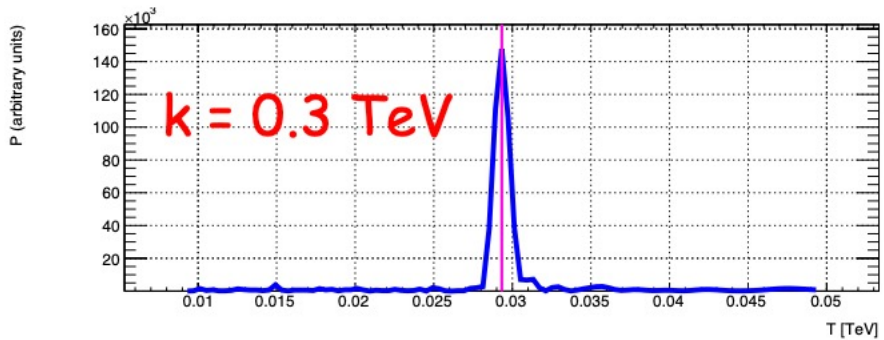
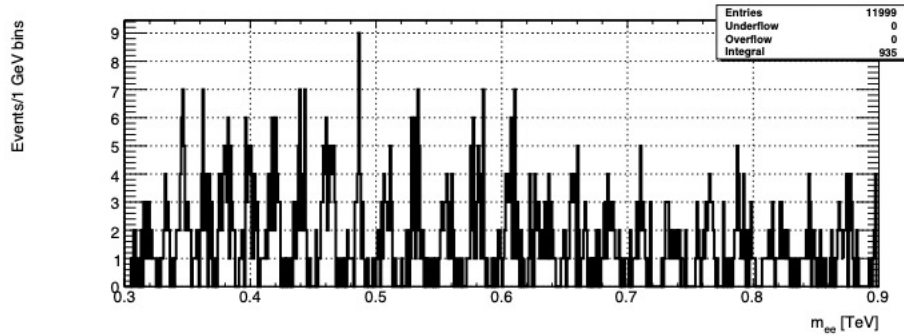
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Appendix-Backgrounds

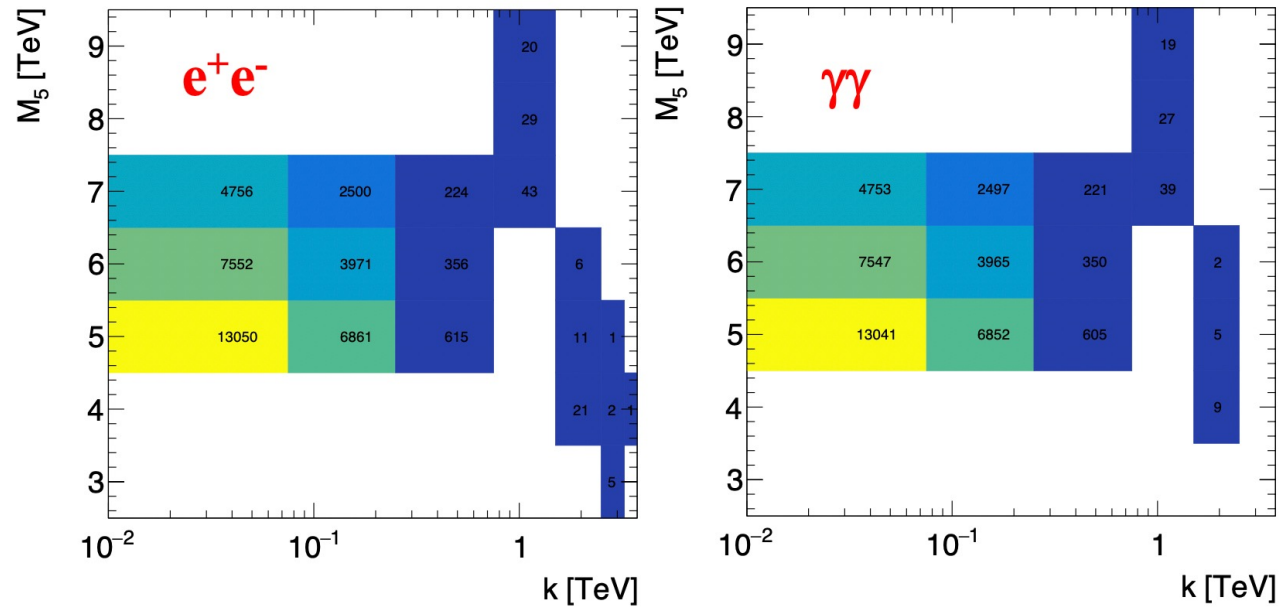


Appendix – FT



$$P(T) = \left| \frac{1}{\sqrt{2\pi}} \int_{m_{\min}}^{m_{\max}} dm \frac{d\sigma}{dm} \exp\left(i \frac{2\pi\sqrt{m^2 - k^2}}{T}\right) \right|^2$$

Appendix – Cross-section



Appendix – Decay Width

