

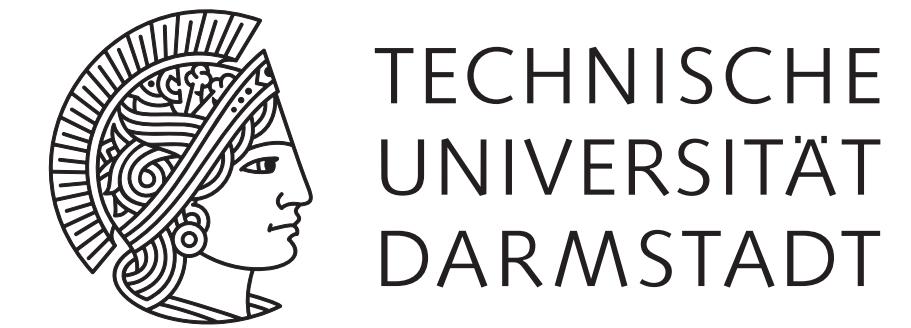
# IMSRG with three-body operators

Matthias Heinz

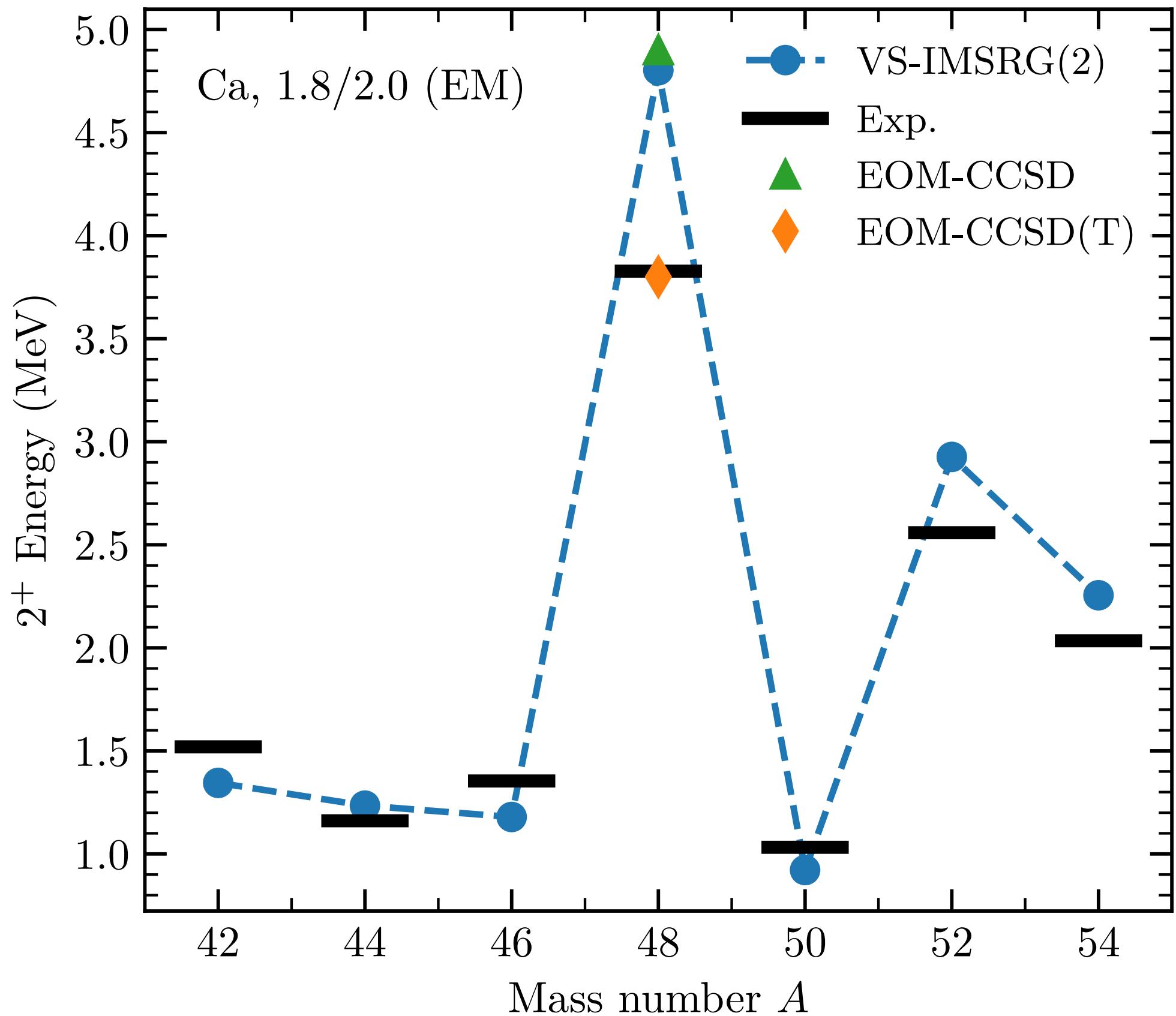
*with Jan Hoppe, Takayuki Miyagi, Alexander Tichai,  
Ragnar Stroberg, Kai Hebeler, Achim Schwenk*



Progress in Ab Initio Nuclear Theory 2023 - Mar. 1, 2023



# Why IMSRG(3)?



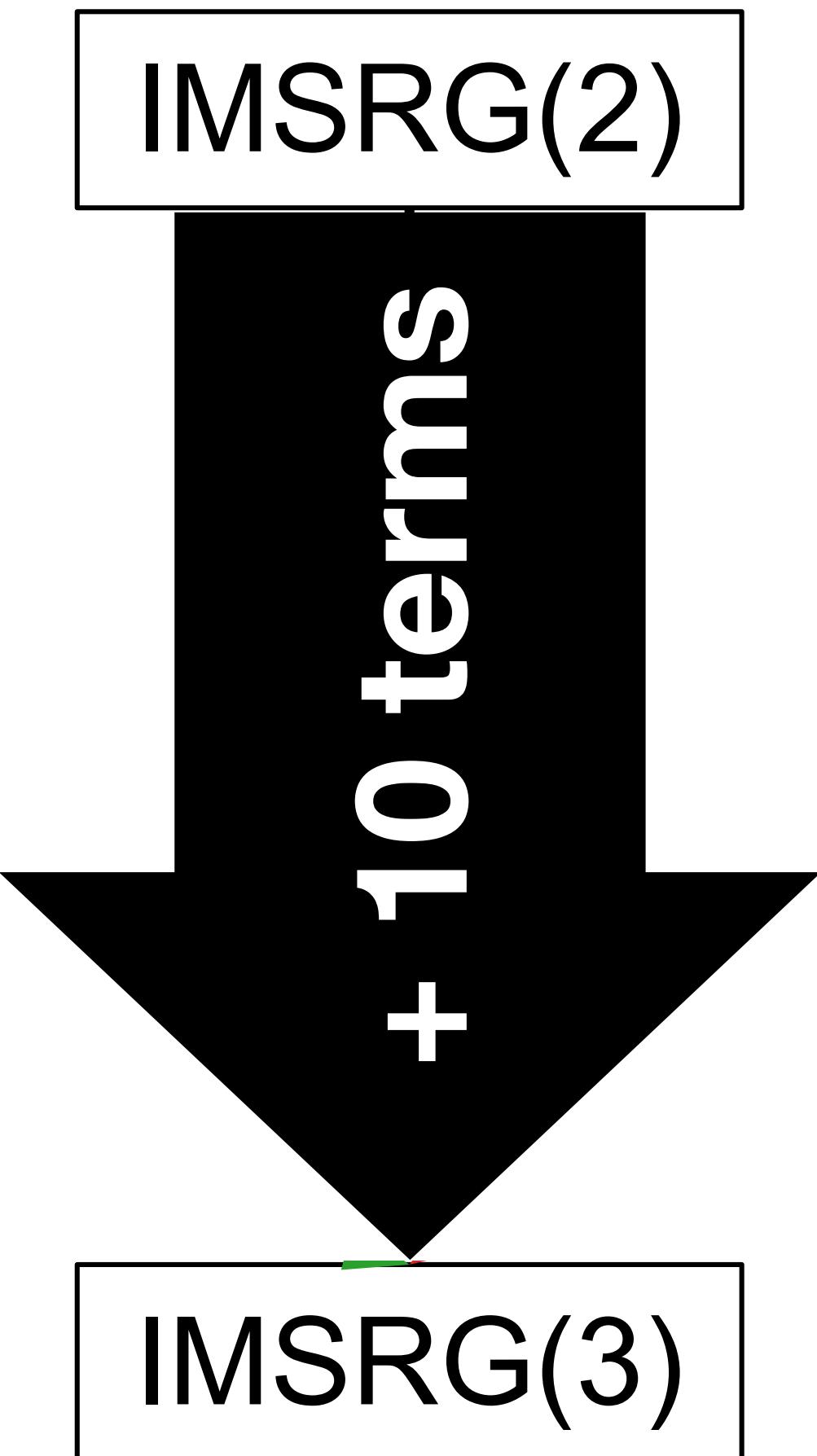
- IMSRG relies on many-body operator expansion
- **IMSRG(2)** = standard, successful truncation
- **IMSRG(3)** is more precise, but more expensive
- Benefits of IMSRG(3):
  - Known IMSRG(2) deficiencies in certain observables
  - Many-body uncertainty quantification within the IMSRG possible

Hagen, Jansen, Papenbrock, PRL 117 (2016)

Simonis, Stroberg, Hebeler, Holt, Schwenk, PRC 96 (2017)

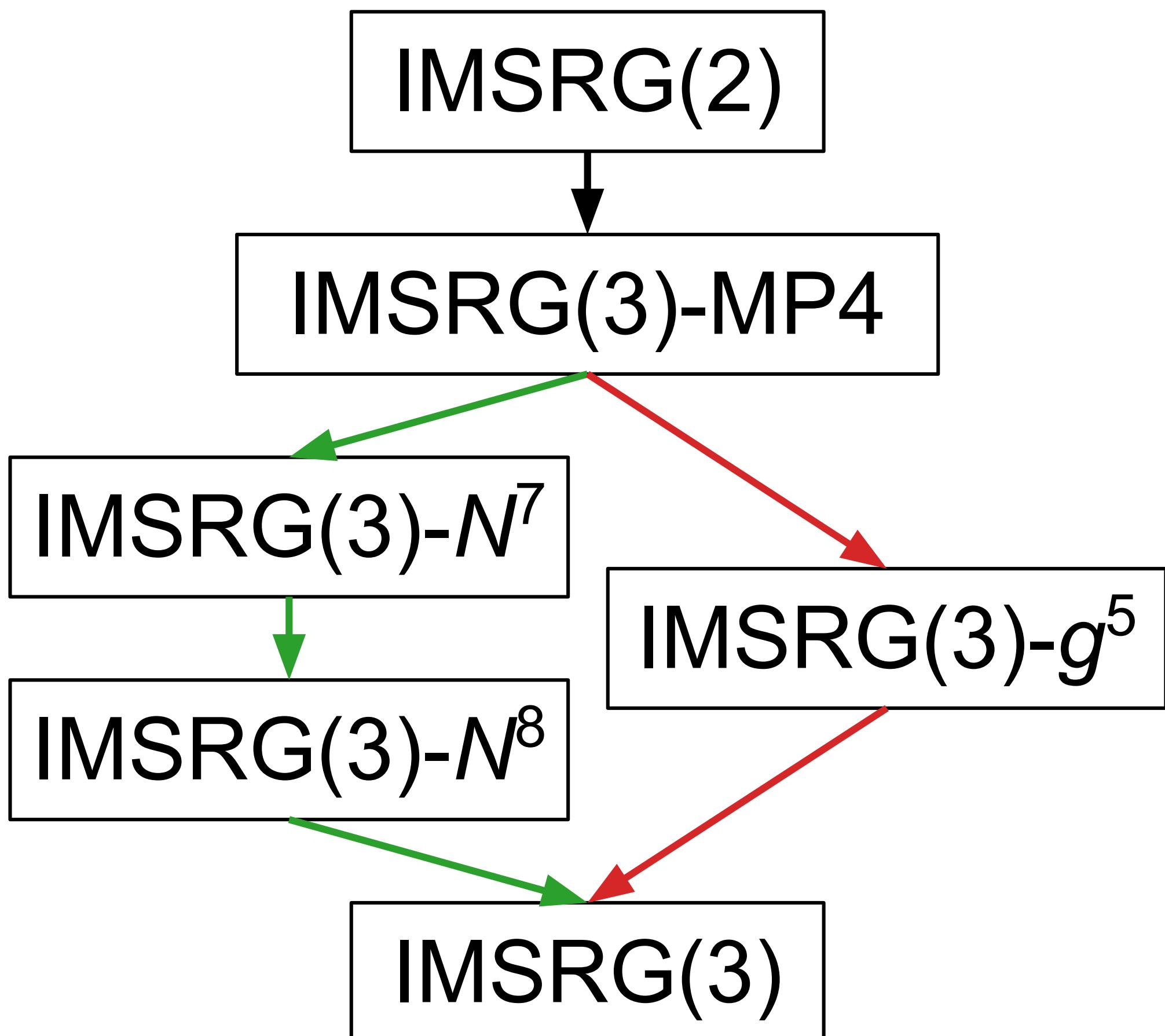
# IMSRG(3) benchmarks

- IMSRG(3) is too expensive
- What can we afford?
- What is actually important?



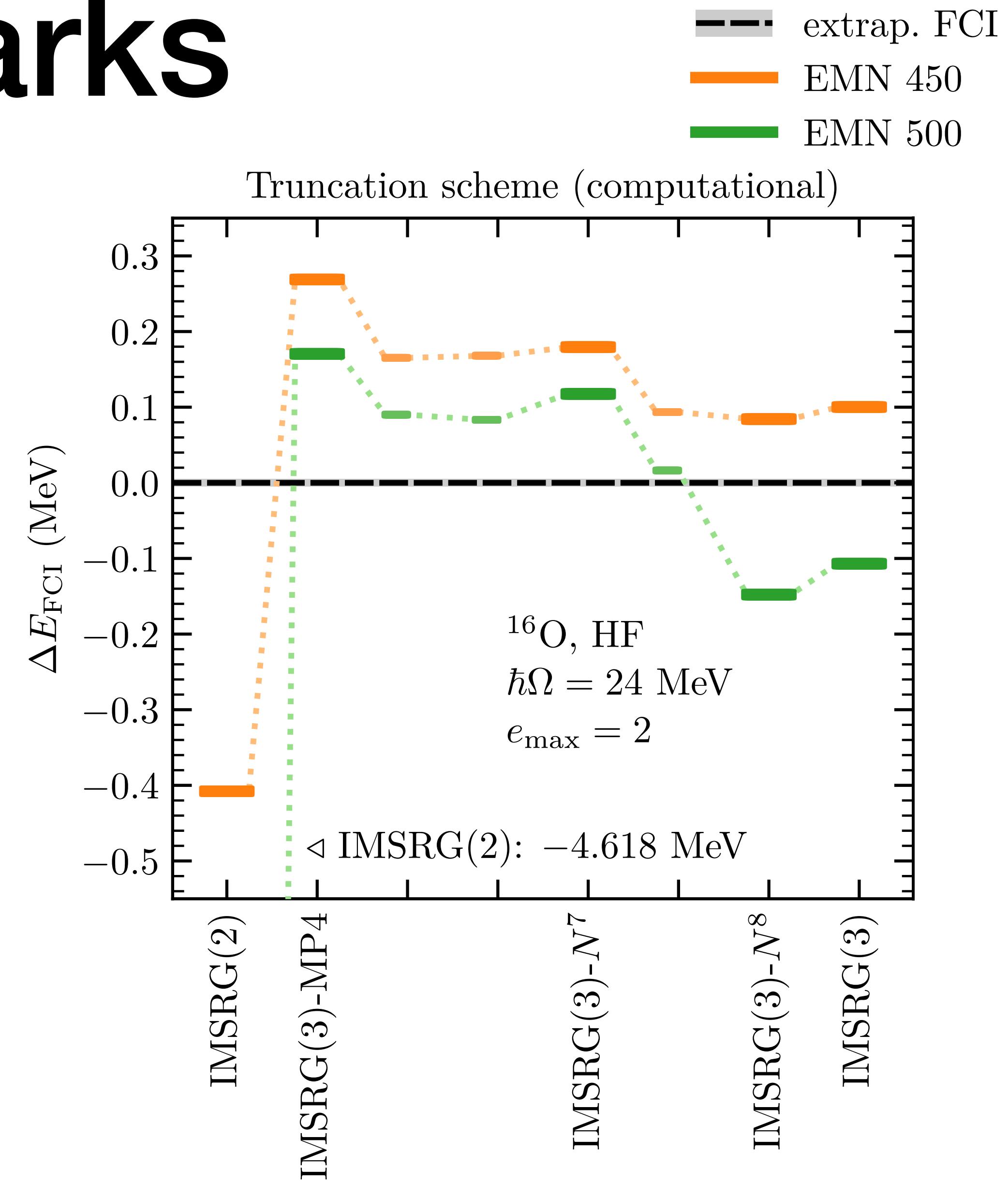
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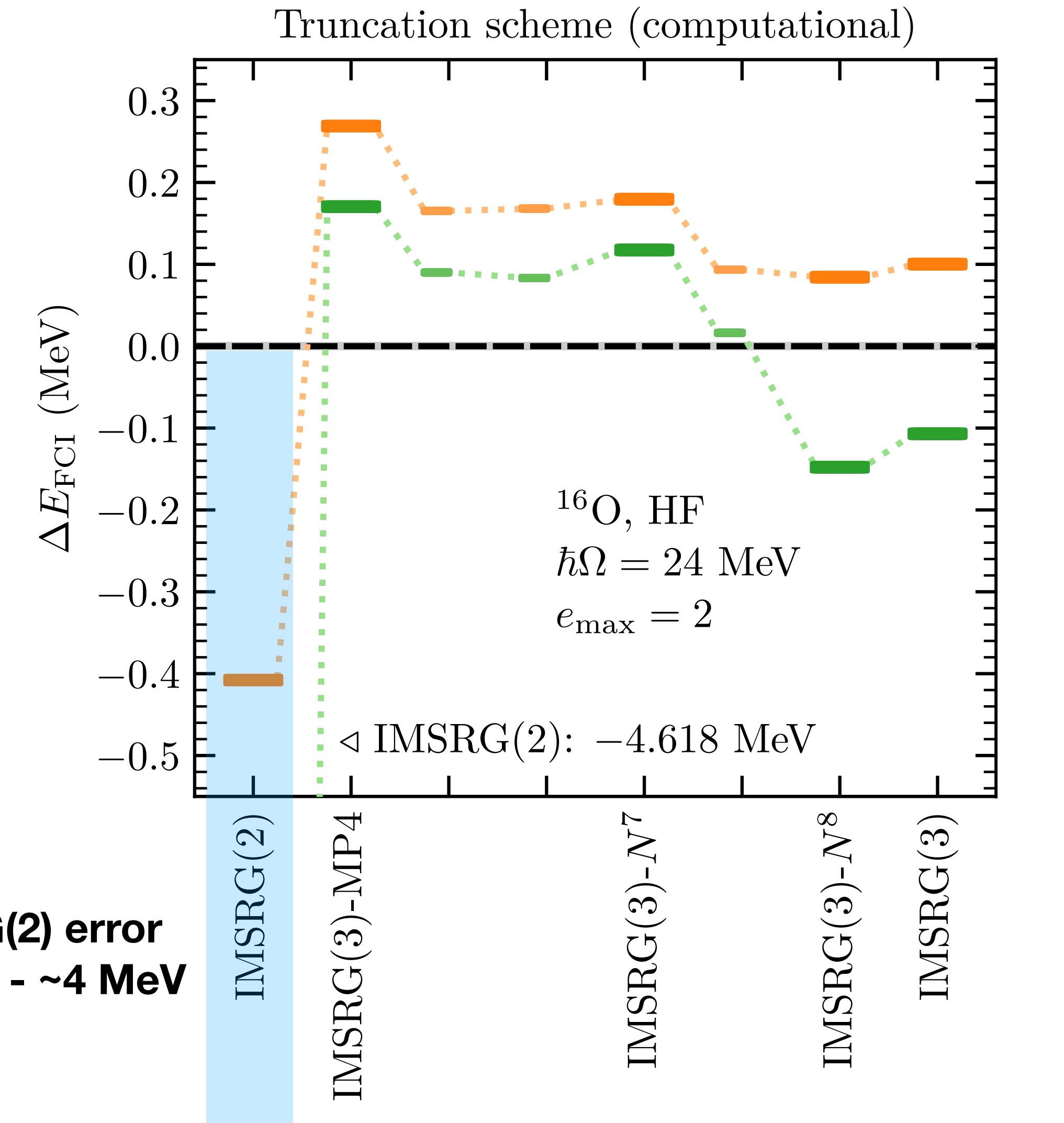
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- What is actually important?
- Systematic study with comparison to exact results
- **IMSRG(3)** gives expected increase in precision
- ... also at lower computational cost



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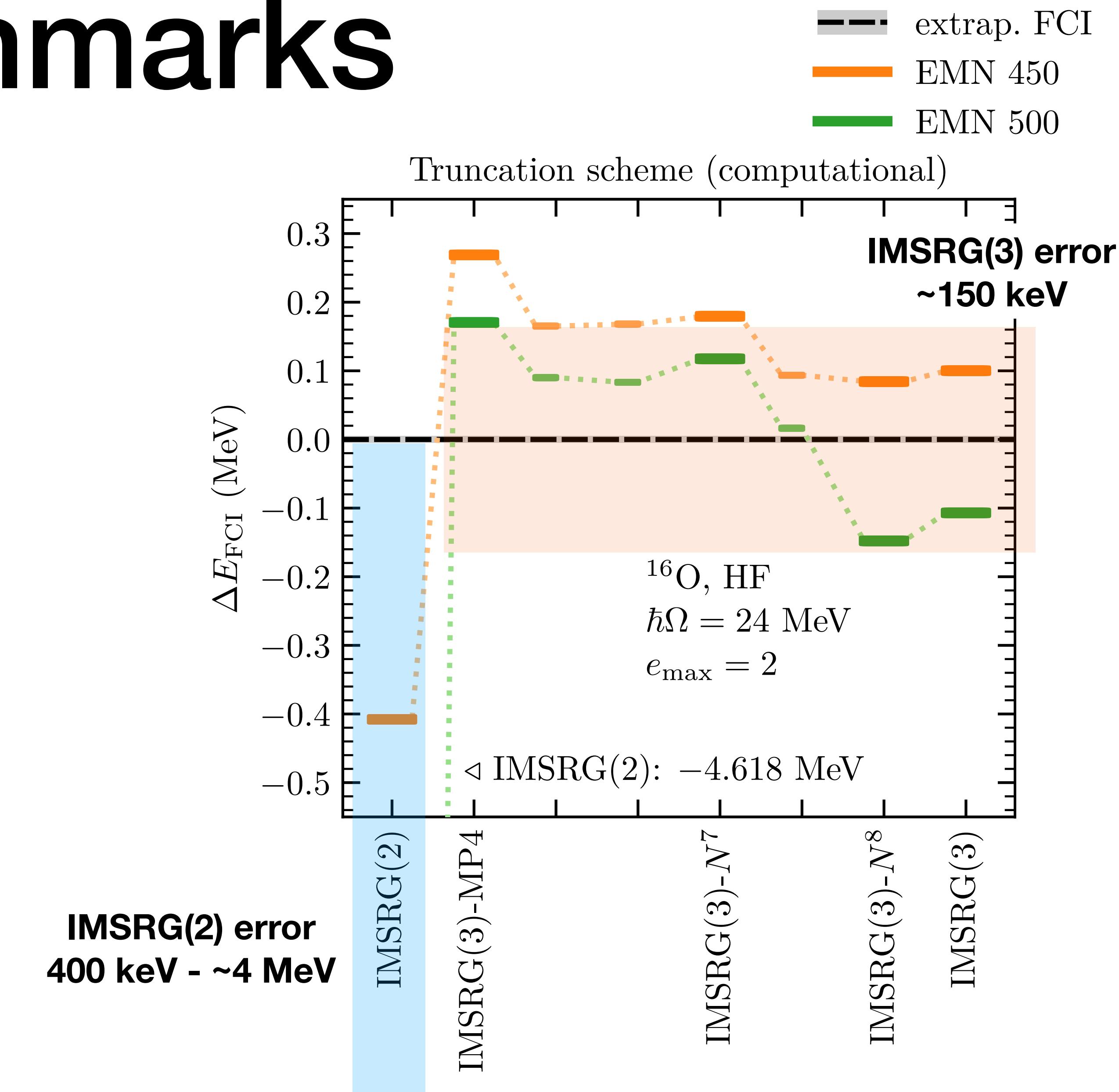
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**IMSRG(2) error**  
400 keV - ~4 MeV

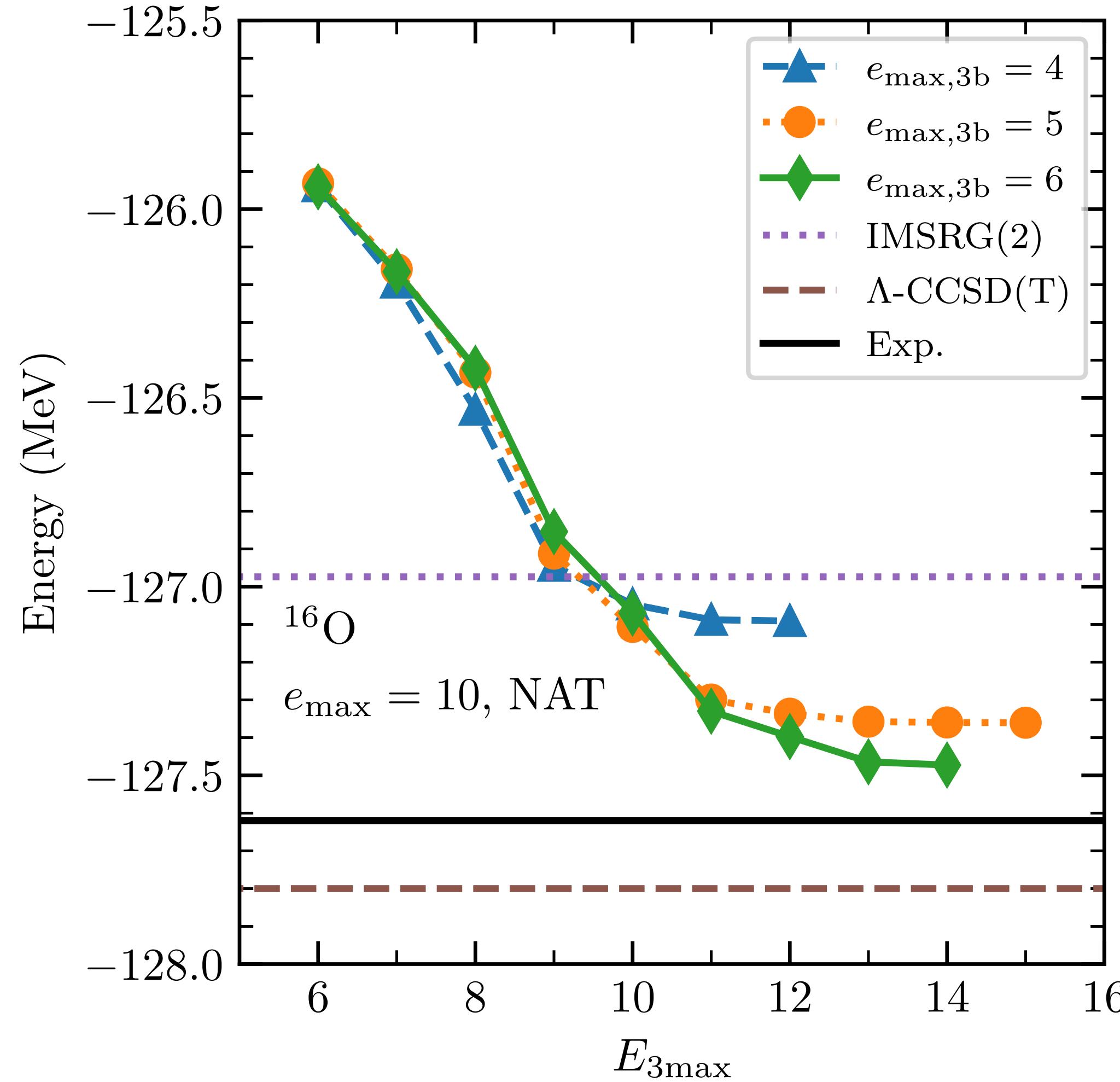


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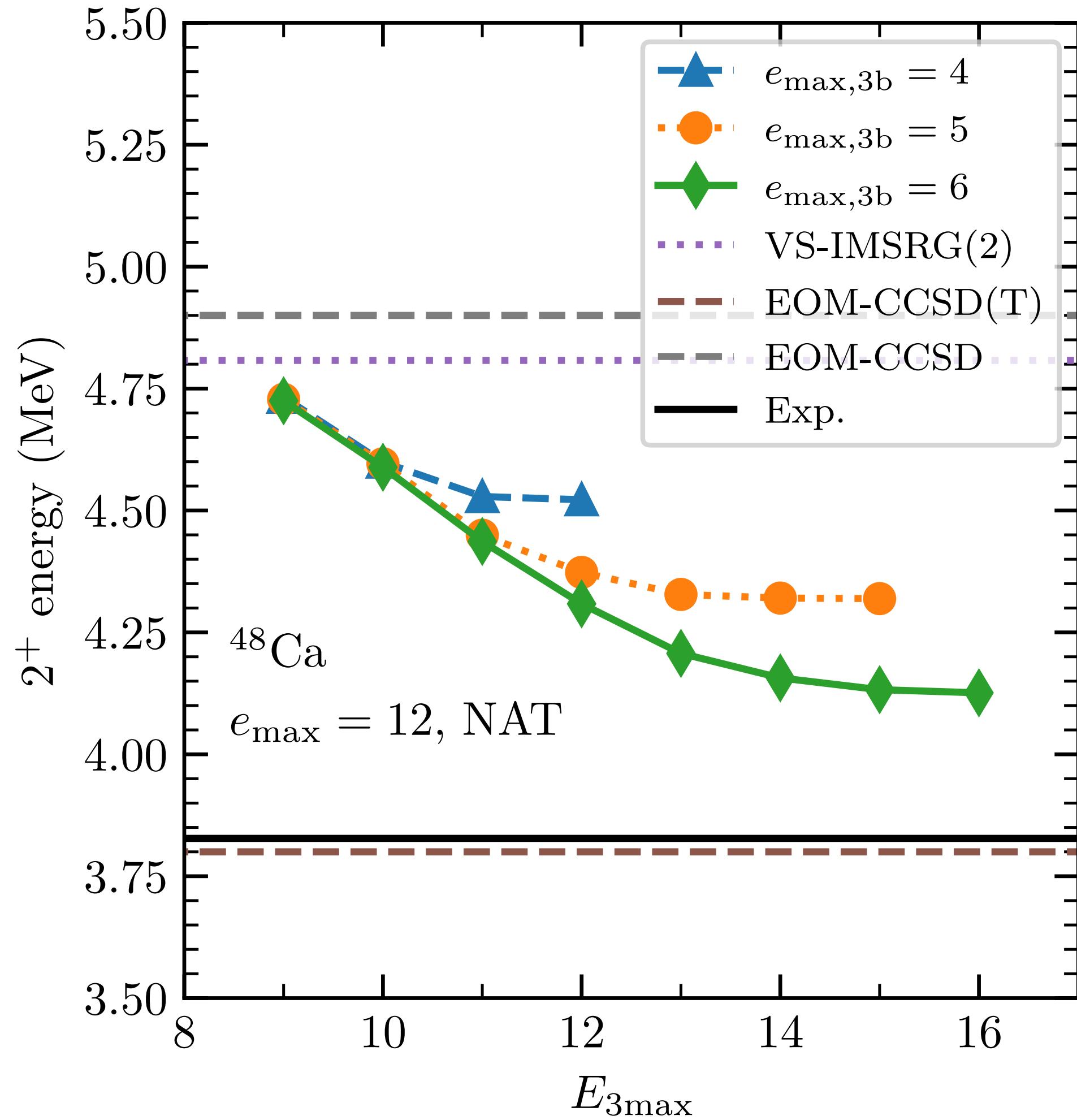


# IMSRG(3) for medium-mass nuclei



- Investigate IMSRG(3) in  $^{16}\text{O}$ ,  $^{48}\text{Ca}$
- Truncations on 3B operator necessary for realistic calculations:  $e_{\text{max},3b}$ ,  $E_{3\text{max}}$
- Nearly converged for ground-state energy

# IMSRG(3) for medium-mass nuclei

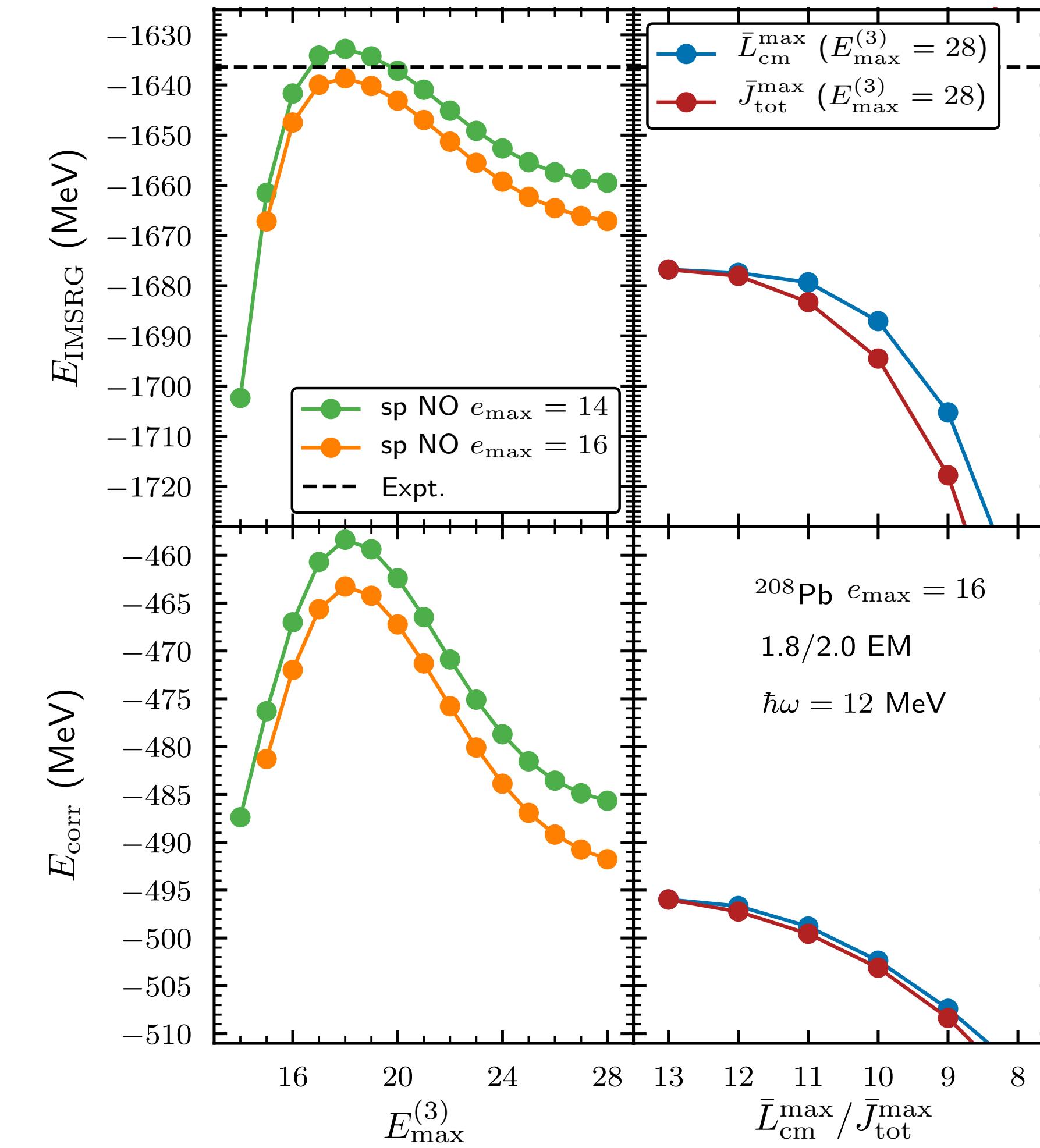


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- Truncations on 3B operator necessary for realistic calculations:  $e_{\text{max},3\text{b}}$ ,  $E_{3\text{max}}$
- Nearly converged for ground-state energy
- Convergence more challenging in Ca
- Substantial corrections to 2<sup>+</sup> energy
- Large model spaces needed for quantitative statements
- Overall qualitative consistency with CC

# Aside: Jacobi normal ordering of 3N forces

Hebeler, Durant, Hoppe, MH, Schwenk, Simonis, Tichai, PRC **107** (2023)

- NO2B three-body force obtained in Jacobi basis
- No  $E_{3,\max}$  truncation required
- Results consistent with Miyagi et al.
- Converged results for  $^{208}\text{Pb}$



# Conclusions and outlook

- Approaching **realistic IMSRG(3) calculations** of medium-mass nuclei
- Small corrections for ground-state energies; **Larger corrections for  $2^+$  energies**
- Further **optimization** needed (basis, numerical implementation)
- Impact of IMSRG(3) in **neutron-rich isotopes?**

Thanks to:

- **Jan Hoppe, Takayuki Miyagi, Alex Tichai**, Ragnar Stroberg, Kai Hebeler, Achim Schwenk
- TU Darmstadt "STRONGINT" group
- ORNL Nuclear Theory



- ... and all of you for your attention

