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# First Measurements of the Quadrupole Moment of the $2_1^+$ State and B(E2) Value of the $4^+$ State in $^{110}\text{Sn}$ from Coulomb Excitation

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14<sup>th</sup> International Conference on Nucleus-Nucleus Collisions

Aug. 21, 2024



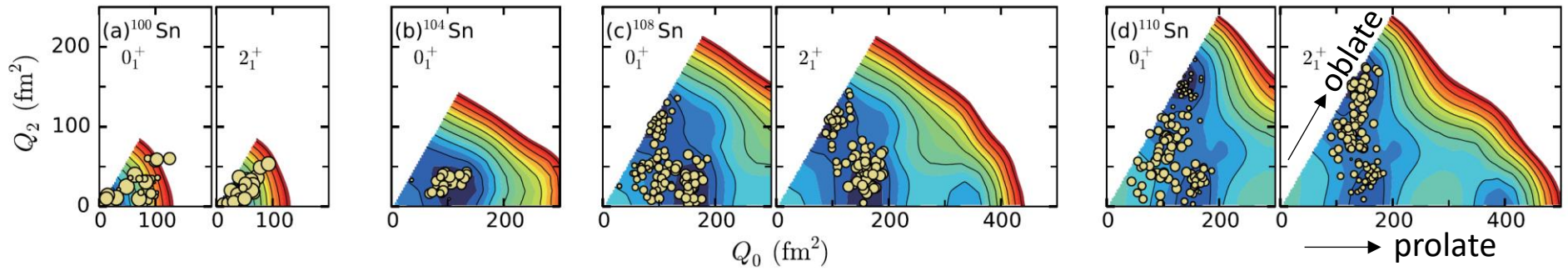
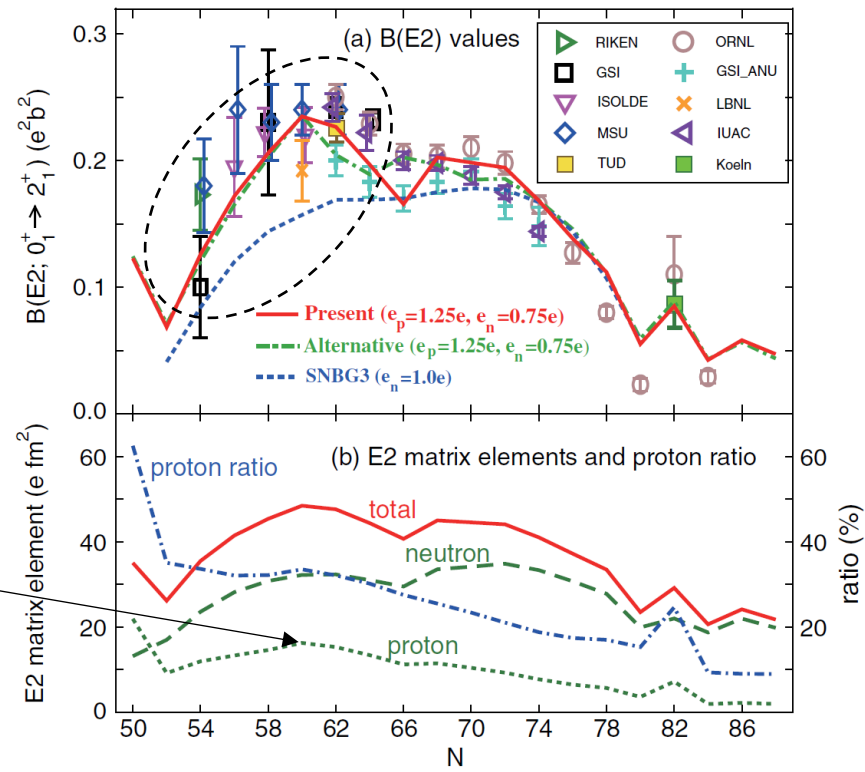
# Physics motivation

Enhanced B(E2) values in light Sn isotopes towards  $^{100}\text{Sn}$ , compared to expectations based on simple seniority scheme

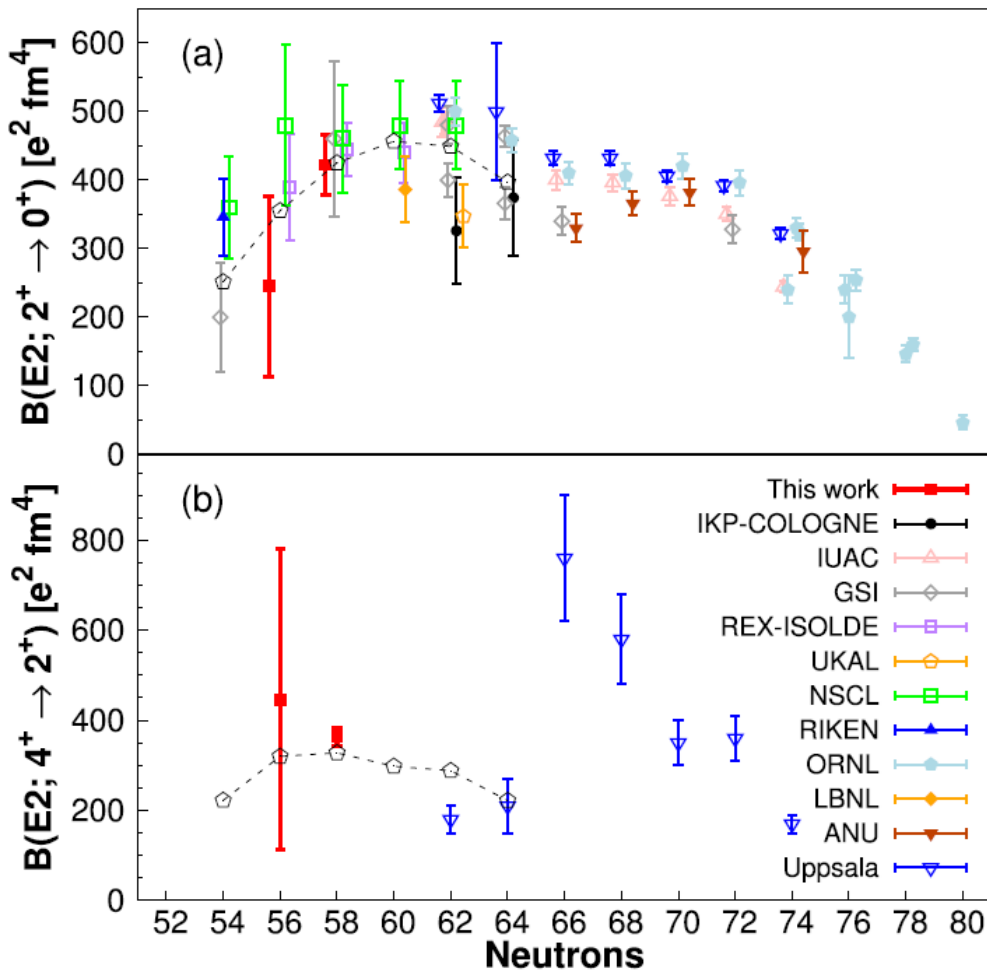
- Isospin-dependent effective charges?
- Quasiparticle phonon model?
- Proton core excitation?

MCSM: huge model space for proton and neutron  $g_{9/2}, g_{7/2}, d_{5/2}, d_{3/2}, s_{1/2}, h_{11/2}, f_{7/2}, p_{3/2}$  orbitals above  $^{80}\text{Zr}$  ( $e_{\pi}, e_{\nu}$ ) = (1.25, 0.75), TBME's from JUN45/SNMG3

MCSM reproduces B(E2) trend via strong proton core excitation which peaks at  $^{110}\text{Sn}$ , with oblate deformation predicted for  $2_1^+$



# Pairing-quadrupole interplay in Sn?

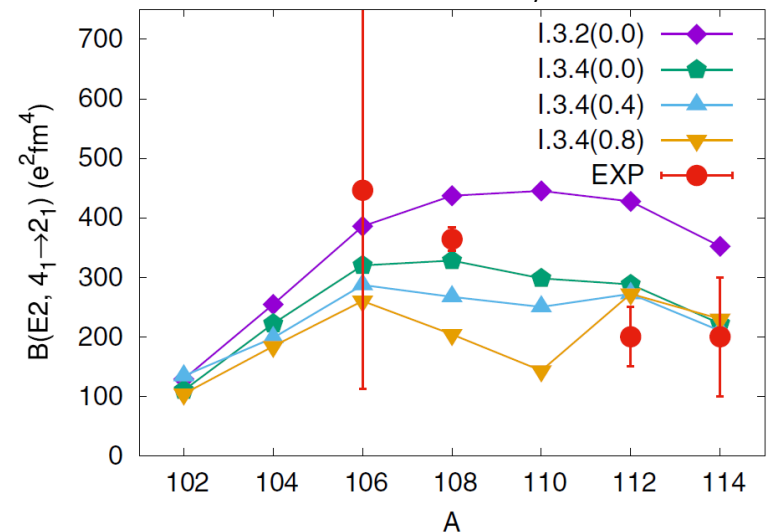


M. Siciliano *et al.*, PLB 806, 135474 (2020)

First  $B(E2)$  measurements of  $4_1^+$  states in  $^{106,108}\text{Sn}$  via RDDS at GANIL,  $^{110}\text{Sn}$  missing in systematics

Realistic SM interaction with limited model space to describe  $B(E2)$  trends in light Cd/Sn isotopes, including  $4_1^+$   
 $(e_\pi, e_\nu) = (1.4, 0.72)$ , neutron  $gds$  orbitals

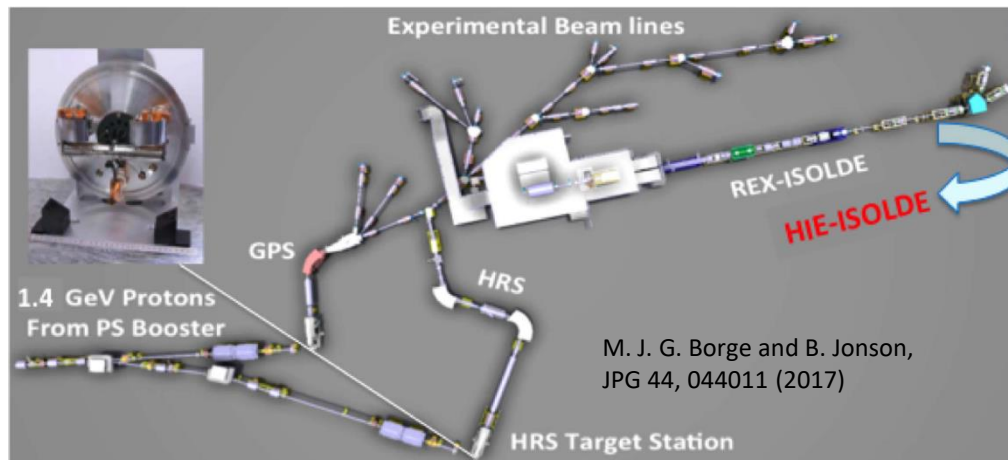
“ $l.q.p$ ”: pairing-quadrupole enhancements  
 $E2$  component  $q \times 10\%$   
 $J = 0, T = 1$  pairing  $p \times 10\%$   
 $(0.k)$ : shift in neutron  $E(s_{1/2})$  by  $0.k$  MeV



A. P. Zuker, PRC 103, 024322 (2021)

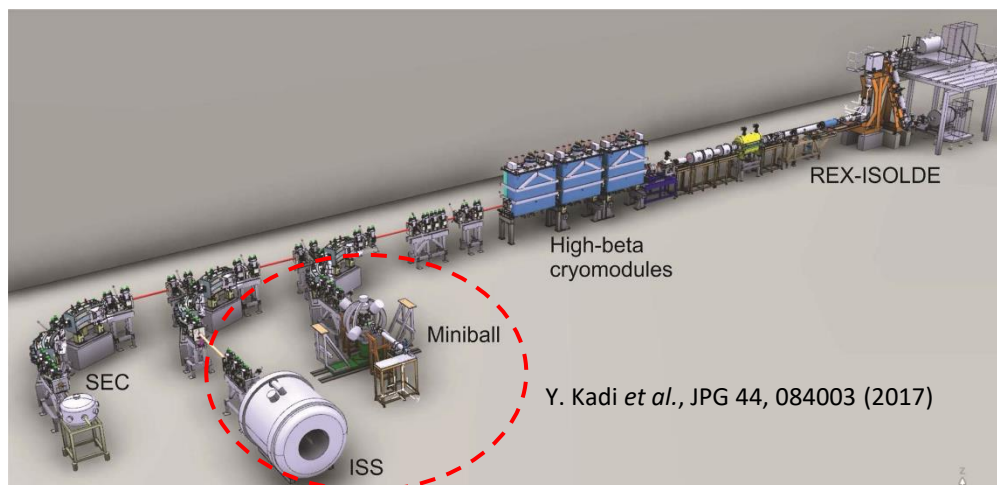
# Experiments at CERN-ISOLDE

Spallation of 1.4-GeV protons from PS booster on  $\text{LaC}_x$  target, transport through GPS  
Isobaric contamination ( $^{106,108,110}\text{In}$ ) suppressed with Resonance Ionization Laser Ion Source (RILIS)



Final isobaric contamination level:  
 $R(^{110}\text{In}/^{110}\text{Sn}) \sim 1\text{-}2\%$   
 $R(^{108}\text{In}/^{108}\text{Sn}) \sim 10\%$   
 $R(^{106}\text{In}/^{106}\text{Sn}) \sim 50\%$

Post-acceleration at HIE-ISOLDE: 4.4-4.5 MeV/u for Coulex and 8.0 MeV/u for (d,p) transfer experiments



2 dedicated campaigns

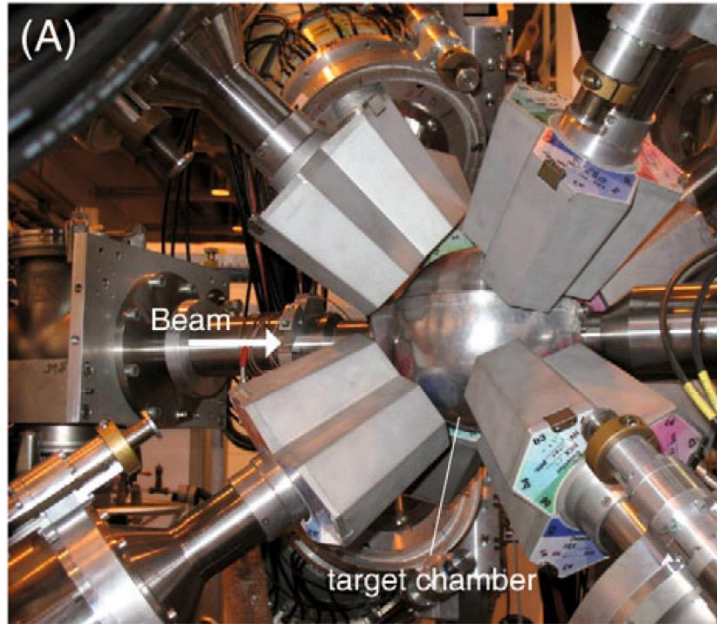
IS562: Coulex of  $^{106,108,110}\text{Sn}$   
with Miniball (completed)

IS686: (d,p) transfers on  $^{106,108,110}\text{Sn}$   
with ISOLDE Solenoidal Spectrometer  
(ongoing)

# The Miniball spectrometer setup

Segmented HPGe detectors for Doppler correction following Coulex reactions

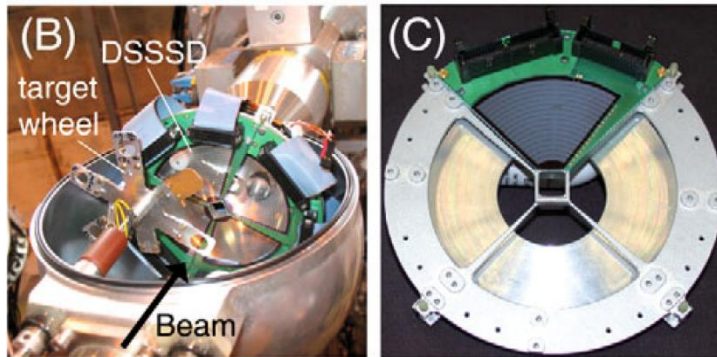
24 HPGe crystals  $\times$   
6 segments =  
144 unique  $\gamma$ -ray  
detection angles



$E_{\text{beam}} = 4.4\text{-}4.5 \text{ MeV/u}$

Just below safe-energy threshold for  
 $^{106,108,110}\text{Sn} + ^{206}\text{Pb}$  combination

$^{206}\text{Pb}$  target,  
4.2-4.7 mg/cm<sup>2</sup>



4-quadrant DSSSD with  $16 \times 16$   
rings and sectors for beam/particle  
scattering angles

N. Warr *et al.*, EPJA 49, 40 (2013)

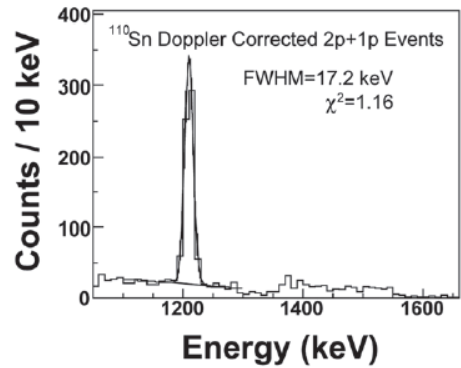
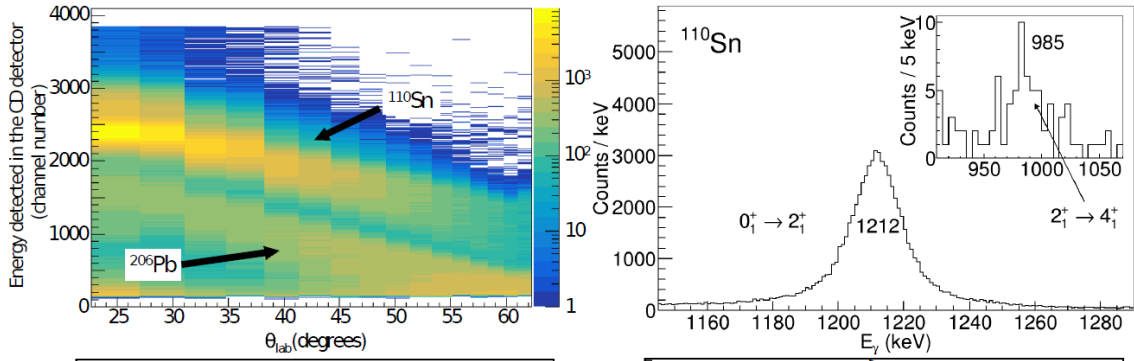
# New Coulex statistics for $^{106,108,110}\text{Sn}$

3 experiments for  $^{110}\text{Sn}$  (2016),  $^{108}\text{Sn}$  (2017), and  $^{106}\text{Sn}$  (2018)

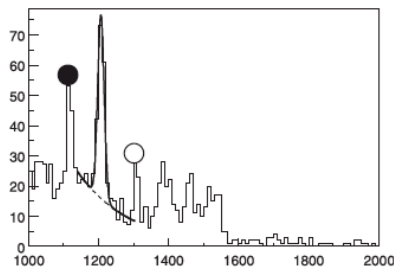
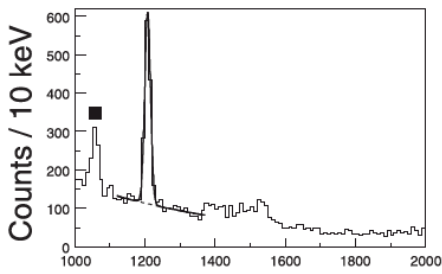
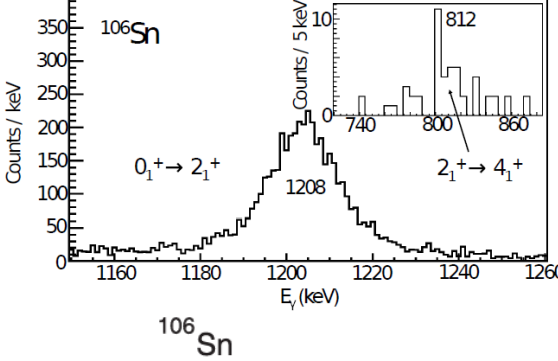
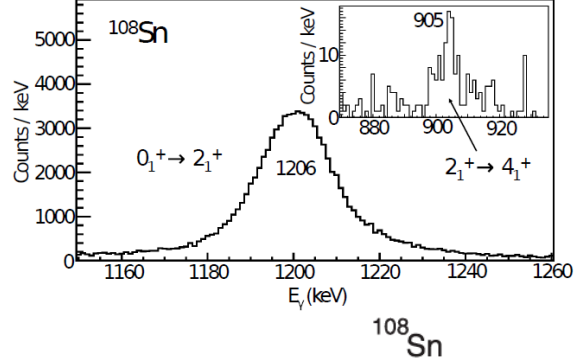
**20-50** increase in statistics with heavier target and  $E_{\text{beam}}$ :  $^{58}\text{Ni}$  (2.8 MeV/u)  $\rightarrow$   $^{206}\text{Pb}$  (4.4 MeV/u)

Excitations to  $4_1^+$  states observed for the first time in safe-energy Coulex

JP *et al.*, JPS Conf. Proc. 32, 010036 (2020)



J. Cederkäll *et al.*, PRL 98, 172501 (2007)



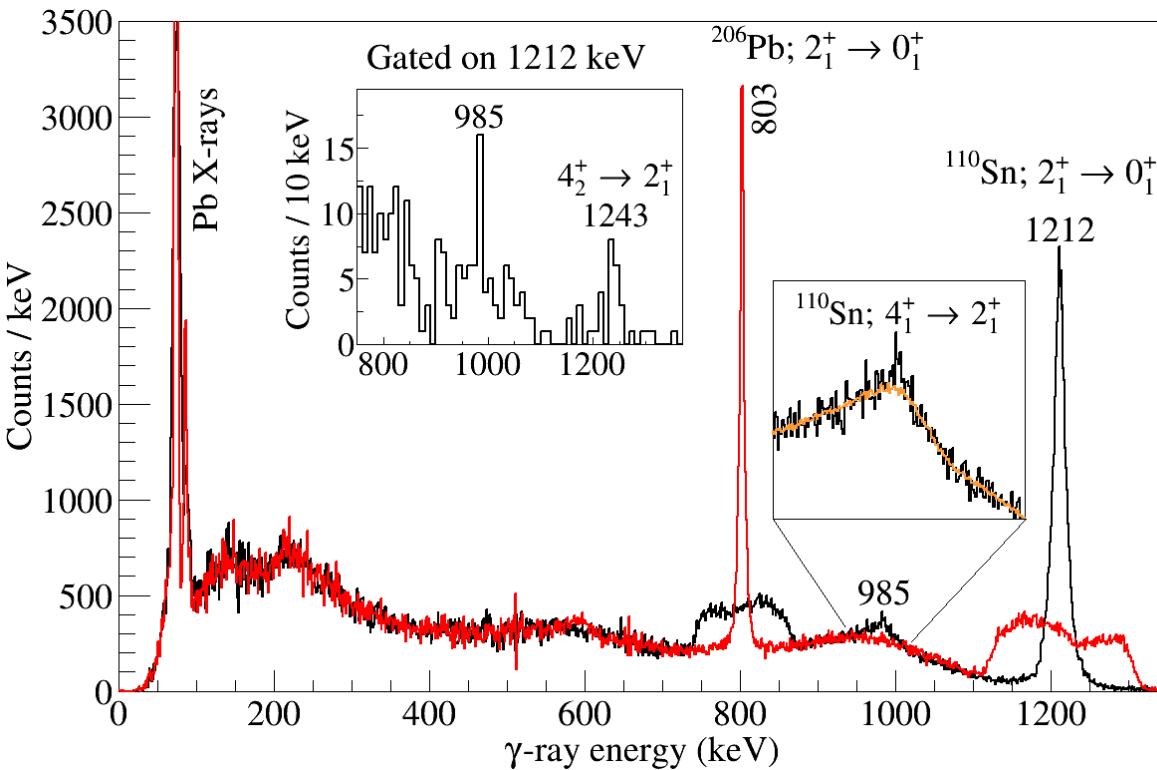
A. Ekström *et al.*, PRL 101, 012502 (2008)



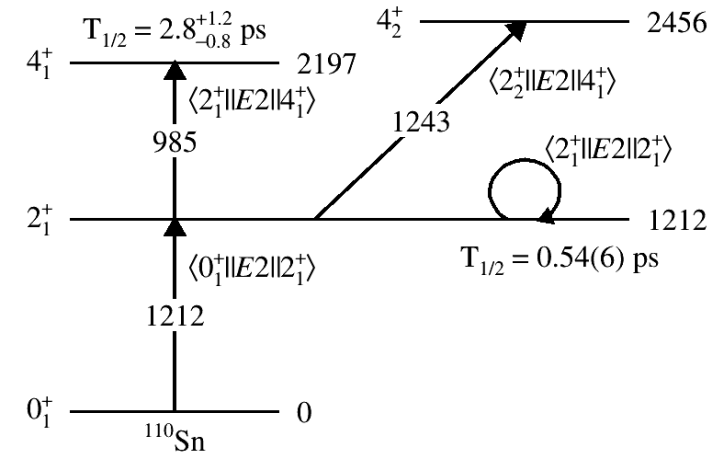
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# Total gamma-ray spectrum for $^{110}\text{Sn}$

Record  $\gamma$ -ray statistics for  $^{110}\text{Sn}$ , additional  $\gamma$ - $\gamma$  coincidence at 1243 keV to  $4_2^+$  state observed



$E2$  matrix elements determined from this experiment

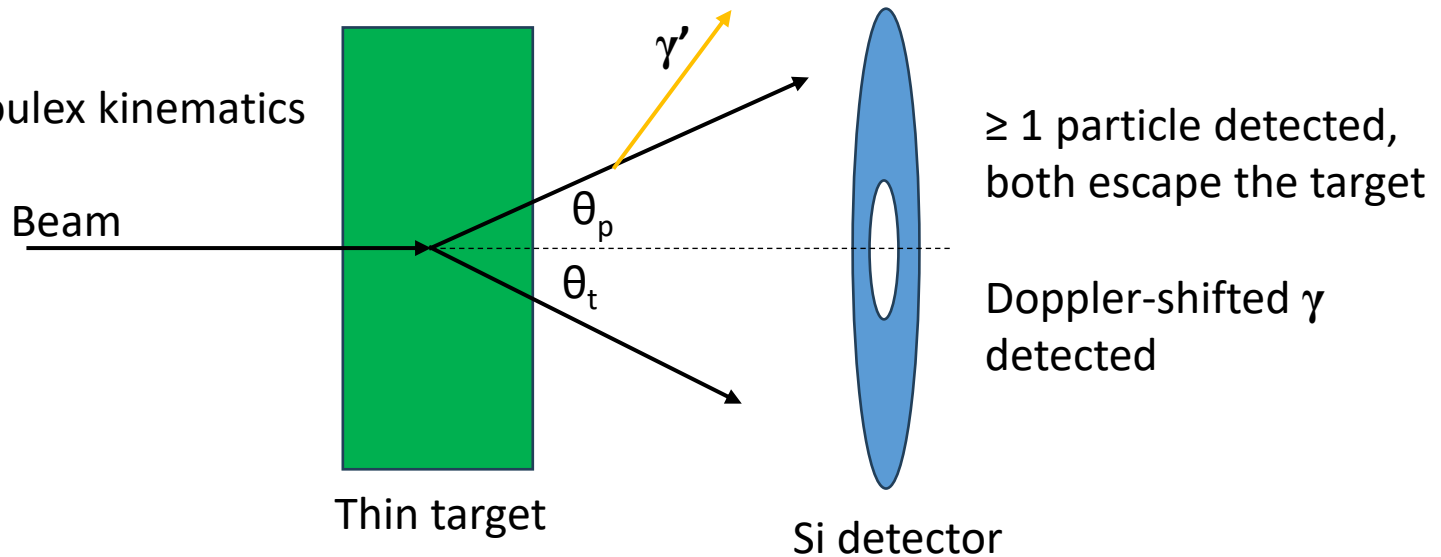


Little evidence of excitations to other states in  $^{110}\text{Sn}$ ,  $^{206}\text{Pb}$

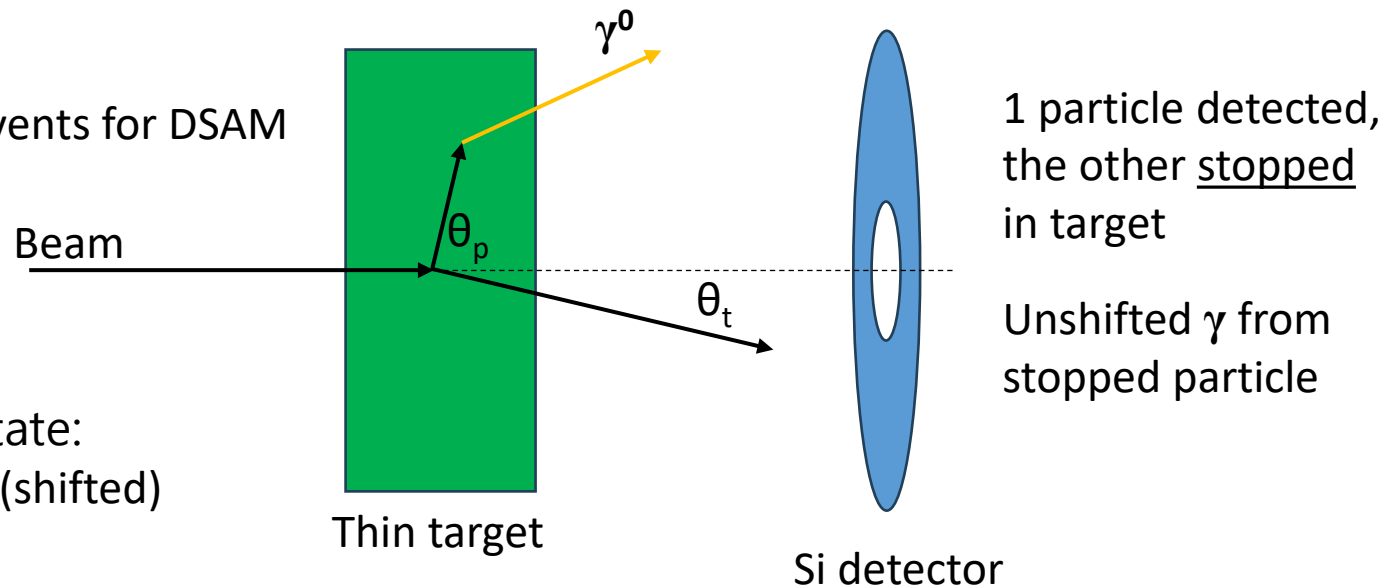
1246-keV  $\gamma$  from  $3_1^-$  state in  $^{110}\text{Sn}$  ruled out; 262-keV side branch unobserved

# Combined Coulex-DSAM analysis for B(E2)

Usual safe-energy Coulex kinematics



Subset of Coulex events for DSAM

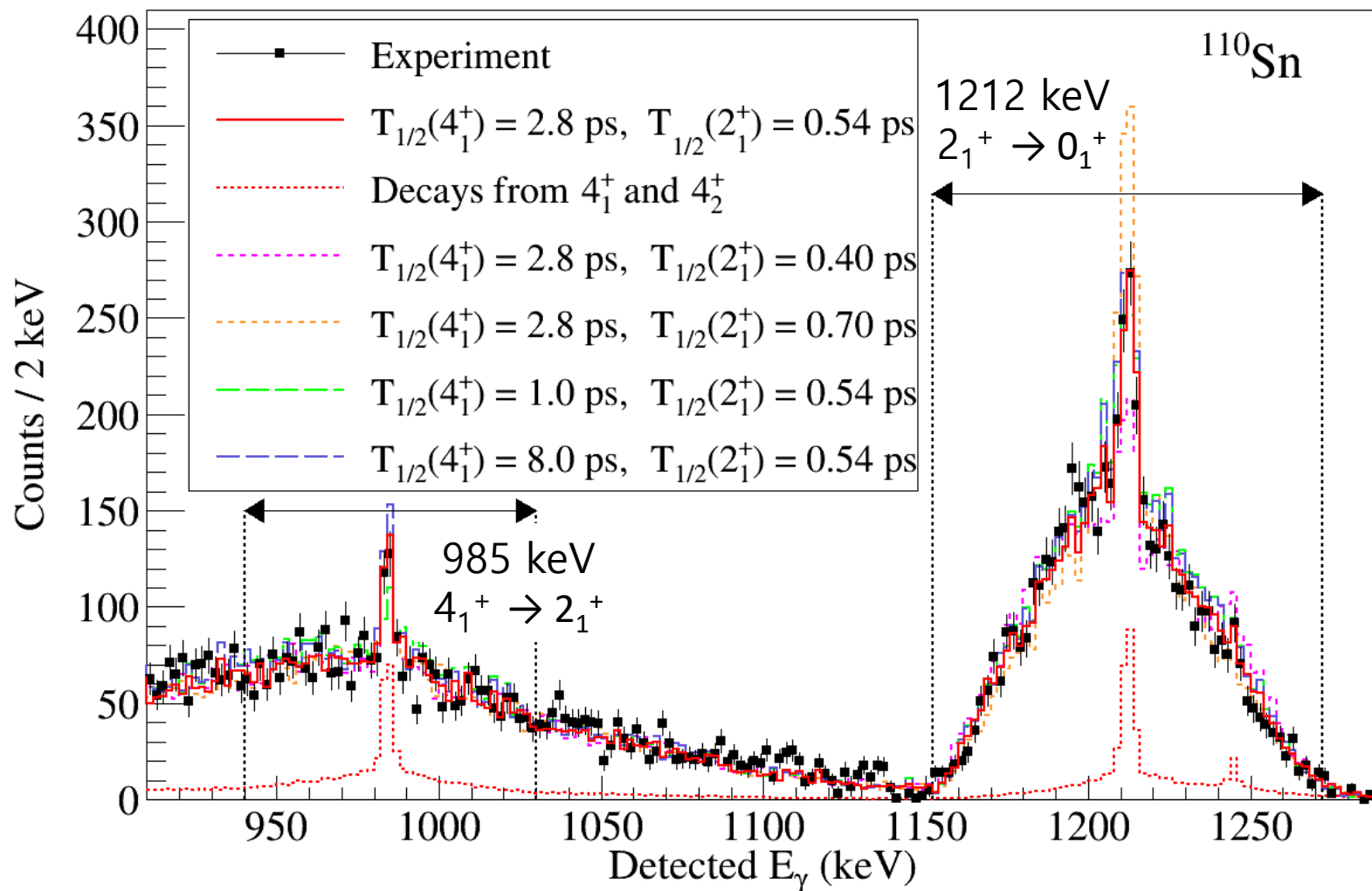


Longer  $T_{1/2}$  of state:  
 $N_\gamma(\text{unshifted}) > N_\gamma(\text{shifted})$



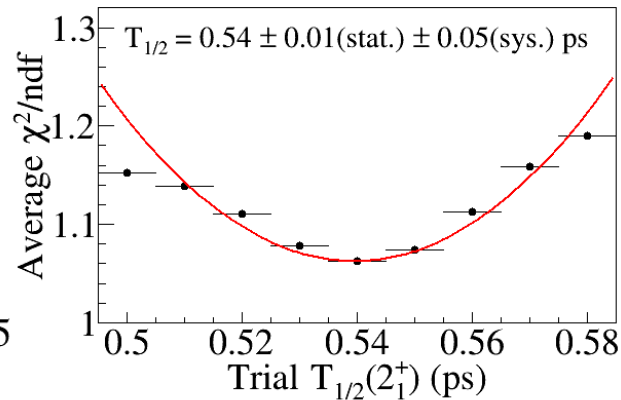
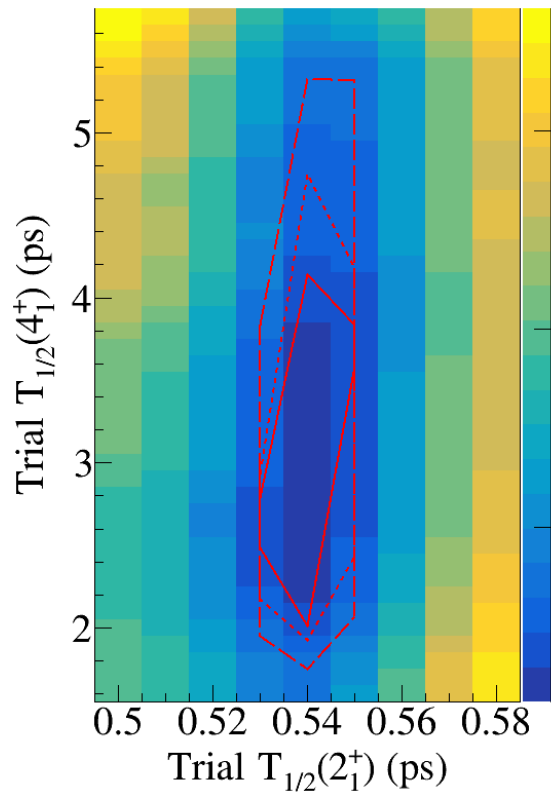
# $T_{1/2}$ analysis with DSAM simulation including cascade decays

Feeding from long-lived  $4_1^+$  state taken into account, minor contribution from  $4_2^+$  also



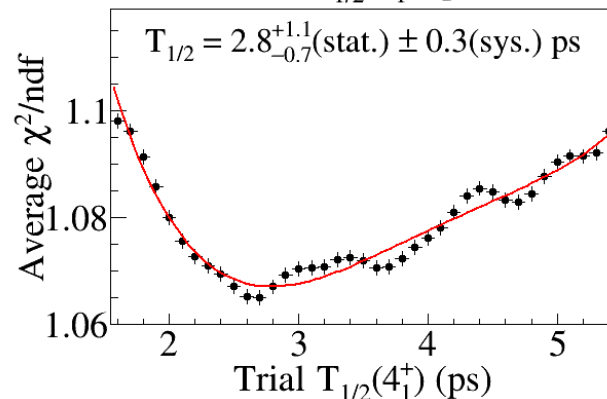
Simulated spectra normalized to experiment within  $\chi^2$  evaluation ranges

# Correlated $T_{1/2}$ analysis of $4_1^+$ and $2_1^+$ states

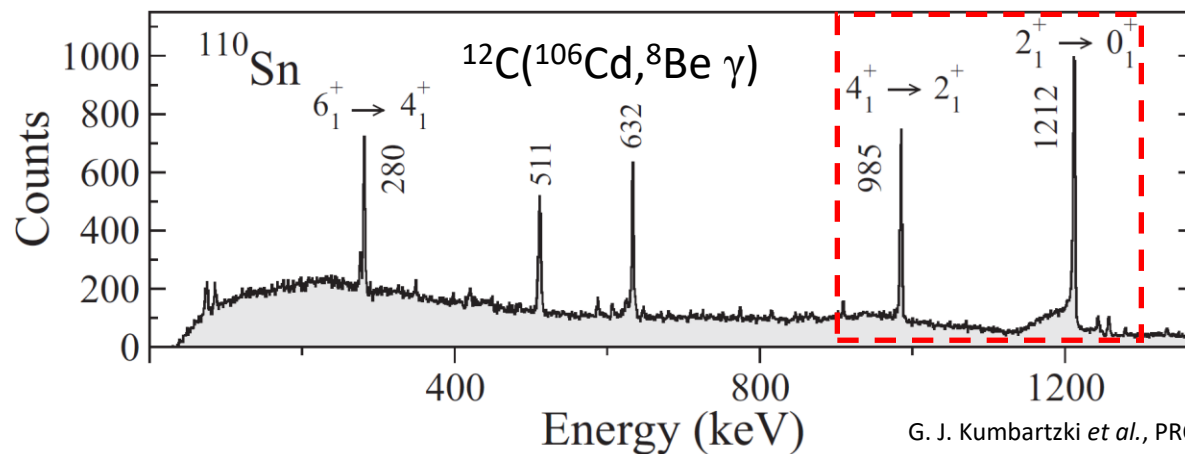


Small correlation in  $\chi^2$  between  $T_{1/2}(2_1^+)$  and  $T_{1/2}(4_1^+)$

$T_{1/2}(2_1^+) = \mathbf{0.54(6) \text{ ps}}$



$T_{1/2}(4_1^+) = \mathbf{2.8^{+1.2}_{-0.8} \text{ ps}}$

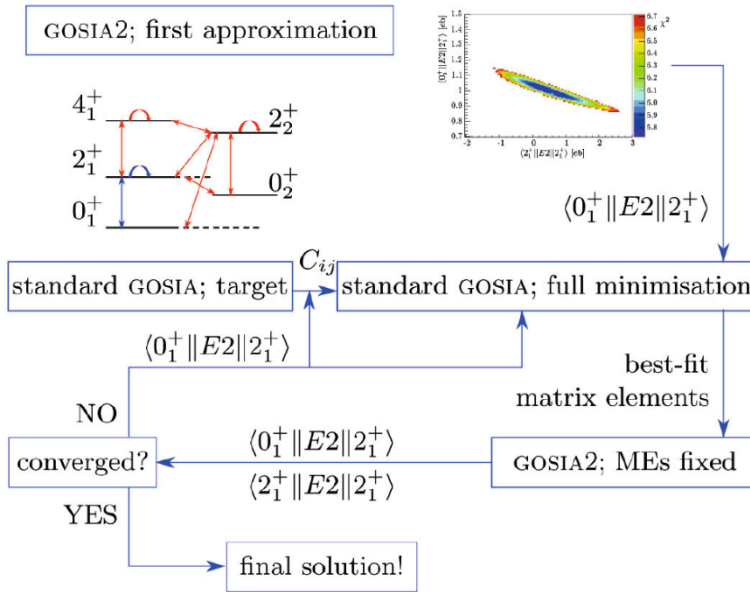


DSAM literature:

$T_{1/2}(2_1^+) = \mathbf{0.56(7) \text{ ps}}$

$T_{1/2}(4_1^+) > \mathbf{2.77 \text{ ps}}$

# Combined GOSIA-GOSIA2 analysis



M. Zielińska *et al.*, EPJA 52, 99 (2016)

$$\langle 0_1^+ || E2 || 2_1^+ \rangle = 0.486(10) \text{ eb}$$

$$B(E2; 2_1^+ \rightarrow 0_1^+) = \begin{cases} 472(20) \text{ e}^2\text{fm}^4 \text{ (Coulex)} \\ 400^{+50}_{-40} \text{ e}^2\text{fm}^4 \text{ (T}_{1/2}) \end{cases}$$

$$\langle 2_1^+ || E2 || 2_1^+ \rangle = 0.25^{+0.10}_{-0.09} \text{ eb}$$

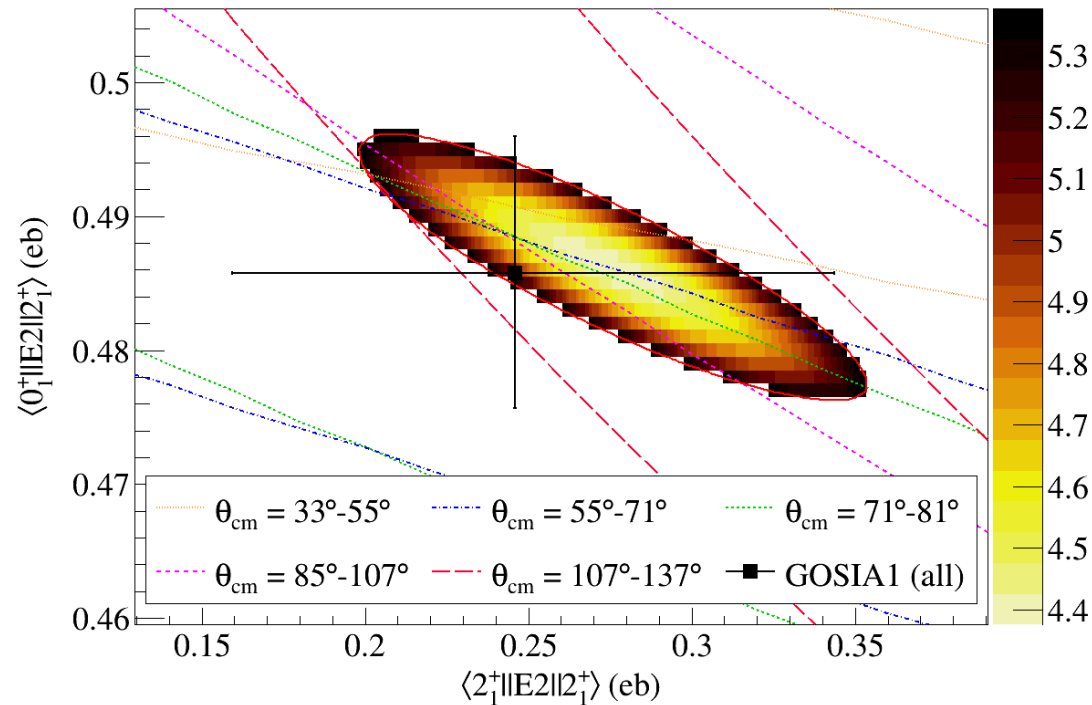
$$Q(2_1^+) = +0.19(7) \text{ eb}$$

$Q > 0$ , oblate deformation by  $> 2\sigma$

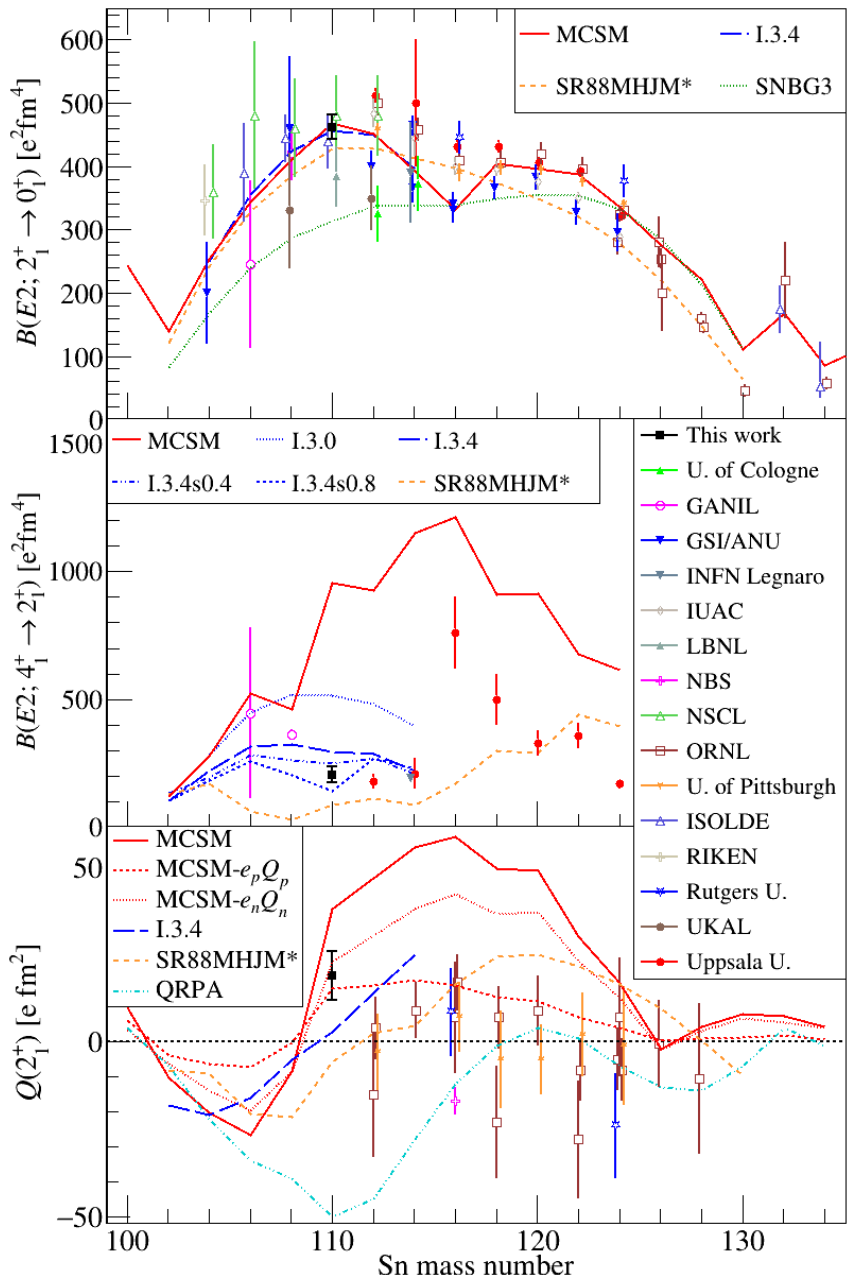
Standalone GOSIA2 analysis not applicable due to multi-step Coulex to higher states in  $^{110}\text{Sn}$

Iterative GOSIA-GOSIA2 approach applied

5 subdivisions of  $\gamma$ -ray yield data for  $B(E2)$  vs  $Q(2_1^+)$



# Comparisons with shell model calculations



$\Delta B(E2)/B(E2) \approx 4\%$  for  $2_1^+$ , down from 10%  
 Little discrepancy with different SM's

$$B(E2; 4_1^+ \rightarrow 2_1^+) = \begin{cases} 203(33) \text{ e}^2\text{fm}^4 \text{ (Coulex)} \\ 218_{-65}^{+87} \text{ e}^2\text{fm}^4 \text{ (T}_{1/2}) \end{cases}$$

$$B(E2; 4_2^+ \rightarrow 2_1^+) = 237(59) \text{ e}^2\text{fm}^4$$

Small  $B(E2; 4_1^+ \rightarrow 2_1^+)$  for  $^{110}\text{Sn}$ , closer to  $^{112,114}\text{Sn}$  than  $^{106,108}\text{Sn}$

Pairing effects quenching  $B(E2)$  of  $B(E2; 4_1^+ \rightarrow 2_1^+)$ ?

$Q(2_1^+)$  of  $^{110}\text{Sn}$  the largest among known isotopes, oblate shape consistent with MCSM and I.3.4

Q magnitudes overestimated by MCSM, large contributions from  $e_p Q_p$  and  $e_n Q_n$

Important to measure  $Q(2_1^+)$  of lighter Sn, shape change to prolate predicted for  $A \leq 108$

Data analysis for  $^{106,108}\text{Sn}$  underway

## Coulomb excitation of $^{110}\text{Sn}$ on $^{206}\text{Pb}$ at HIE-ISOLDE

- Most precise  $B(E2)$  for  $2_1^+$
- New  $B(E2)$  measurements for  $4_1^+$  and  $4_2^+$ , pairing effects eroding quadrupole collectivity
- First determination of  $Q(2_1^+)$  in the light unstable Sn, oblate shape in agreement with MCSM and SM predictions
- To be submitted soon!

## Follow-up studies of $B(E2)$ and $Q(2_1^+)$ systematics with $^{106,108}\text{Sn}$

- Improved precision on  $B(E2)$ , new  $Q(2_1^+)$  and  $B(E2; 4_1^+ \rightarrow 2_1^+)$  expected
- DSAM simulations for independent  $B(E2)$  measurements and comparisons

## IS562 experiment campaign and Miniball collaborators:

J. Park<sup>a,b</sup>, J. Cederkäll<sup>a,\*</sup>, C. Fahlander<sup>a</sup>, P. Golubev<sup>a</sup>, A. Knyazev<sup>a</sup>, A. Lopez<sup>a</sup>,  
E. Rickert<sup>a</sup>, J. Snäll<sup>a</sup>, A. N. Andreyev<sup>c,d</sup>, J. Konki<sup>c</sup>, A. Welker<sup>c</sup>,  
K. Wrzosek-Lipska<sup>e</sup>, A. Gawinek<sup>e</sup>, J. Iwanicki<sup>e</sup>, M. Saxena<sup>e</sup>, G. de Angelis<sup>f</sup>,  
L. P. Gaffney<sup>g</sup>, Th. Kröll<sup>h</sup>, C. Henrich<sup>h</sup>, T. Habermann<sup>h</sup>, M. Schilling<sup>h</sup>,  
M. Seidlitz<sup>h</sup>, C. Stahl<sup>h</sup>, K. Arnswald<sup>i</sup>, A. Blazhev<sup>i</sup>, P. Reiter<sup>i</sup>, D. Rosiak<sup>i</sup>,  
N. Warr<sup>i</sup>, S. Saha<sup>j</sup>, G. Rainovski<sup>k</sup>, R. Zidarova<sup>k</sup>, C. Raison<sup>d</sup>, A. Boukhari<sup>c,l</sup>,  
L. Barber<sup>m</sup>, D. M. Cullen<sup>m</sup>, B. S. Nara Singh<sup>m</sup>, C. Berger<sup>n</sup>, C. Berner<sup>n</sup>,  
R. Gernhäuser<sup>n</sup>, L. Werner<sup>n</sup>, M. J. G. Borge<sup>c,o</sup>, J. Díaz Ovejás<sup>o</sup>, O. Tengblad<sup>o</sup>,  
S. Viñals<sup>o</sup>, T. Berry<sup>p</sup>, D. M. Cox<sup>q,r</sup>, A. Görgen<sup>s</sup>, T. W. Johansen<sup>s</sup>, G. Tveten<sup>s</sup>,  
A. Illana<sup>f,q,t</sup>, M. Stryjczyk<sup>t</sup>, P. Van Duppen<sup>t</sup>, H. De Witte<sup>t</sup>, J. J. Valiente-Dobón<sup>u</sup>



# INPC 2025

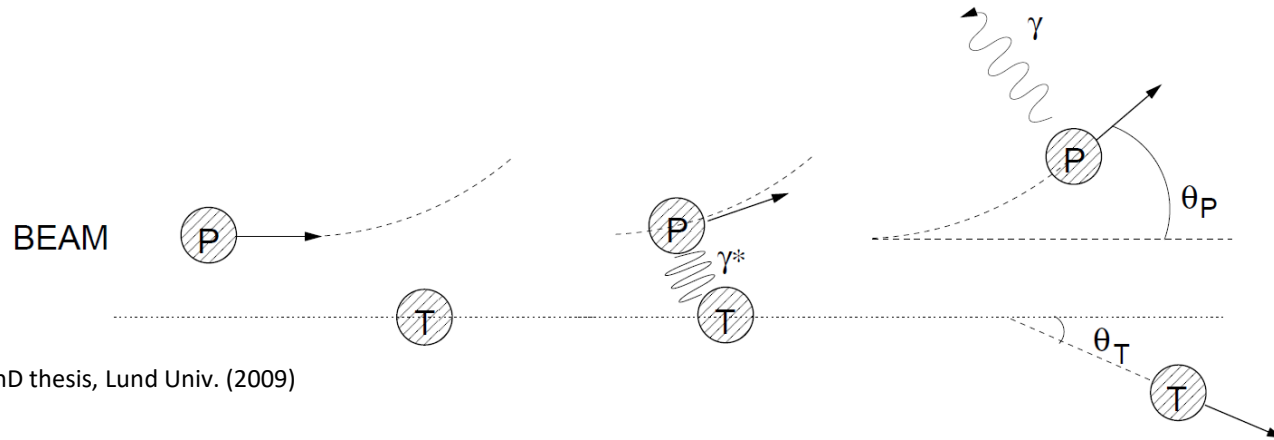
International Nuclear Physics Conference

May 25-30

Daejeon, Republic of Korea

STAY TUNED and WELCOME!

# Safe-energy Coulex experiment design details



A. Ekström, PhD thesis, Lund Univ. (2009)

- Electromagnetic excitation between projectile (beam) and target nucleus through Coulomb field
- Detection of  $\gamma$  rays and Doppler correction using kinematics ( $\beta = v/c$ ),  $\theta_\gamma$ ,  $\theta_p$  and  $\theta_t$
- Nuclear excitation can be separated from pure electromagnetic interaction at “safe” Coulex energy:

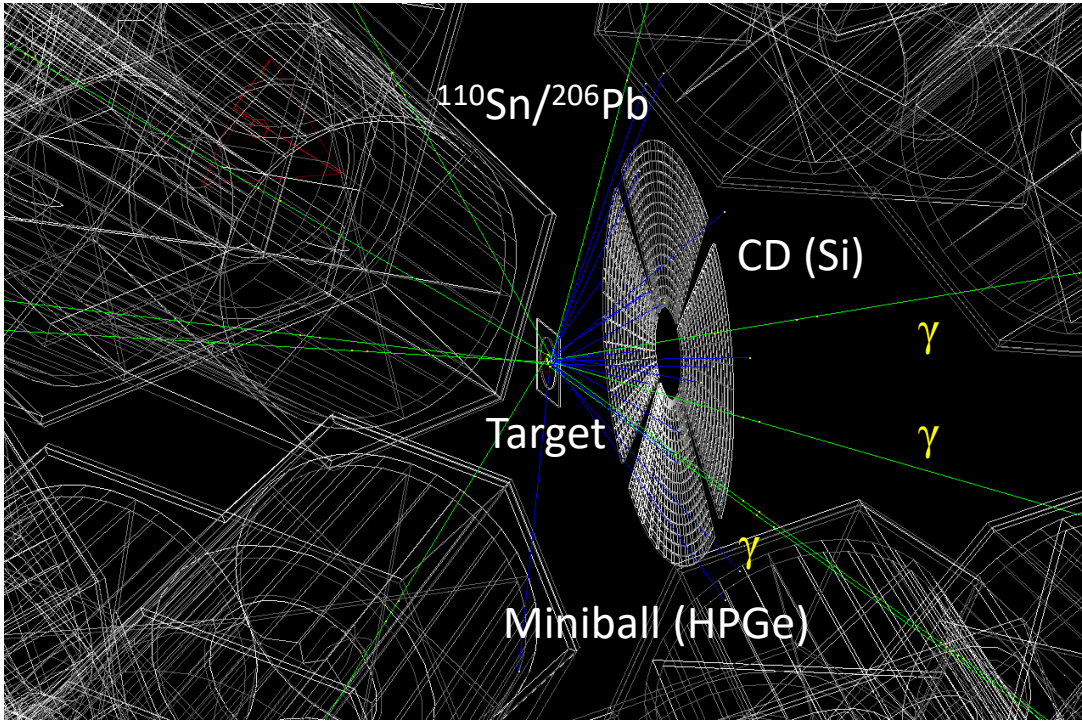
$$E_{\text{safe}} = 1.44 \frac{A_p + A_t}{A_t} \frac{Z_p \cdot Z_t}{1.25(A_p^{1/3} + A_t^{1/3}) + 5} \text{MeV}$$

K. Alder and A. Winther,  
*Electromagnetic Excitation* (1975)

Coulex experiments performed at HIE-ISOLDE using  $^{206}\text{Pb}$  target ( $Z_t = 82$ ,  $A_t = 206$ )

$Z_p$	$A_p$	$E_{\text{safe}}$ (MeV)	$E_{\text{safe}}/A_p$ (MeV)	$E_{\text{exp}}/A_p$ (MeV), year
50	110	493	4.48	4.40 (2016)
50	108	491	4.54	4.50 (2017)
50	106	489	4.61	4.40 (2018)

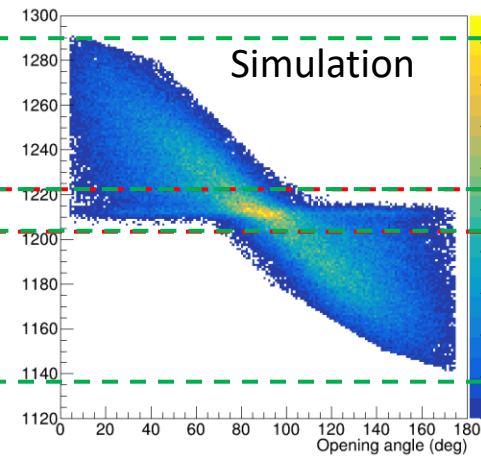
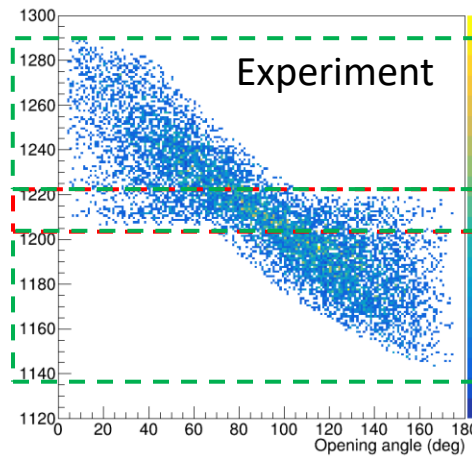
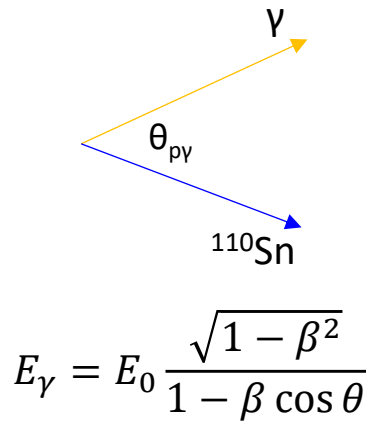
# DSAM simulation with Geant4



Event selection cut:  
 Low  $\theta_{lab}$  for  $^{206}\text{Pb}$ ,  
 more  $^{110}\text{Sn}$  stopped inside target  
 → better sensitivity for DSAM

Stopping power of  $^{206}\text{Pb}$  calculated  
 with SRIM

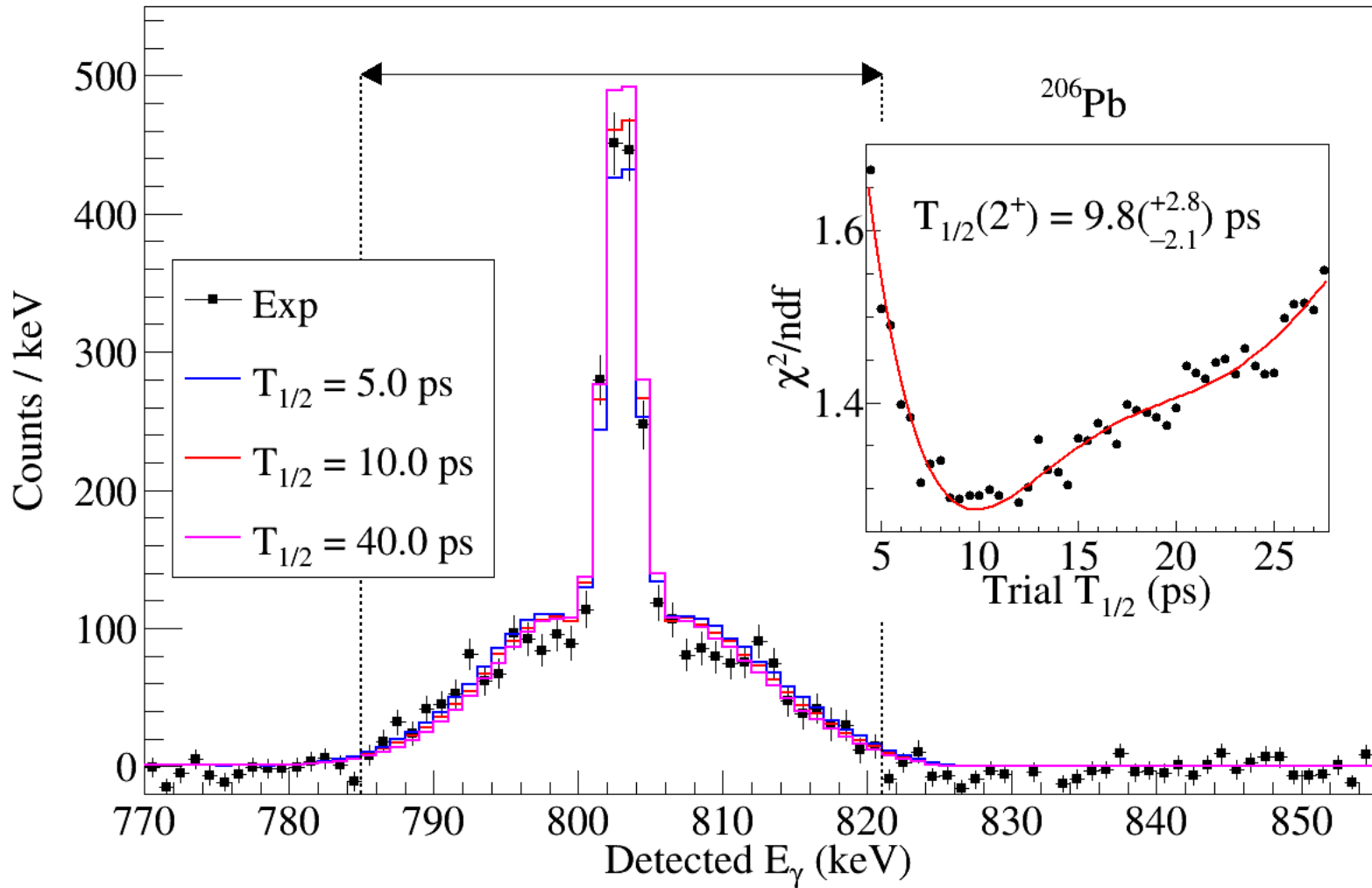
10% systematic uncertainty in  $T_{1/2}$



110Sn stopped  
 110Sn in flight



# DSAM simulation for $T_{1/2}$ of $^{206}\text{Pb}$



Literature  $T_{1/2}$ :

9.1(6) ps: J. L. Quebert *et al.*, Nucl. Phys. A 150 (1970) 68

12(3) ps: D. Ralet *et al.*, Phys. Lett. B 797 (2019) 134797