

The INDRA-FAZIA setup:  
Investigating isospin transport as a signature for  
symmetry energy effects in heavy ion collisions

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*for the INDRA-FAZIA collaboration*

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Probing the symmetry energy of the nuclear Equation of State (nEoS)

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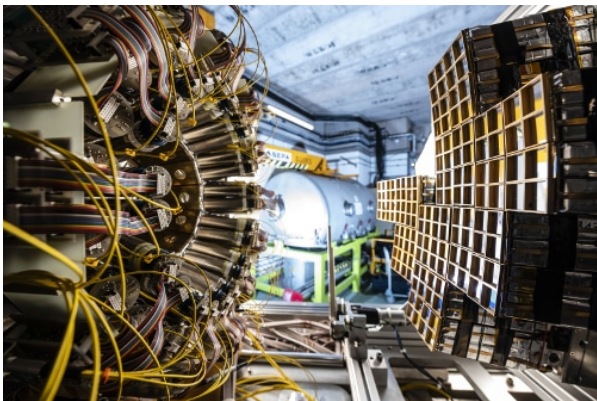
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- **Isospin drift** (or *isospin migration*): driven by density gradient (e.g. neck  $\rho \lesssim \rho_0$ ). Can be isolated by choosing a symmetric system. Sensitive to  $\frac{\partial E_{sym}(\rho)/A}{\partial \rho} \rightarrow$  neutron enrichment of the neck region

# The INDRA-FAZIA apparatus

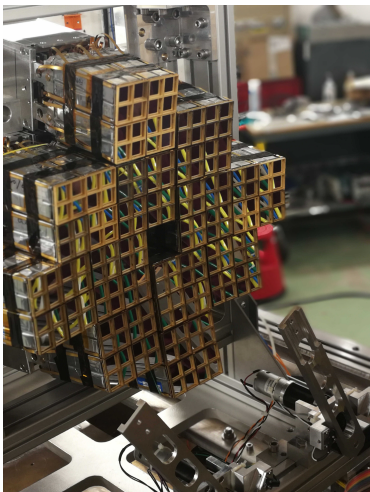
Experimental requirements for isospin transport studies

To study isospin transport, we need the **isotopic identification** ( $Z, A$ ) of the produced fragments, and a **good global event reconstruction**.



The recently coupled INDRA-FAZIA apparatus (GANIL, Caen FR) aims to overcome the most common limitations and to collect the most comprehensive information on the event.



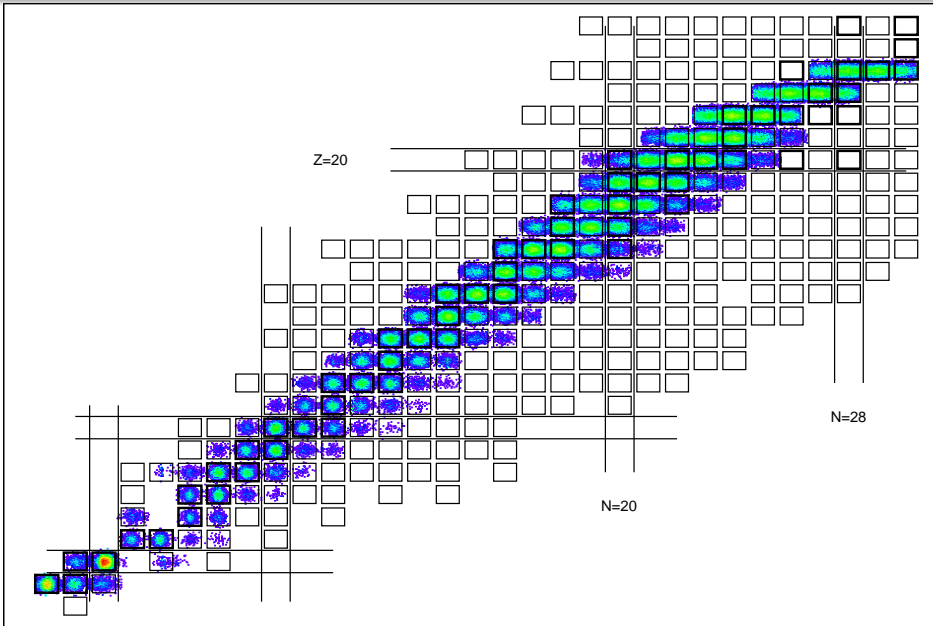


**FAZIA** (*Forward-angle A and Z Identification Array*): optimal ion identification in the Fermi energy domain.

- Result of R&D activities to refine:
  - detector performance
  - digital treatment of signals
- Basic module: **block**, consisting of 16 three stage **telescopes** ( $2 \times 2 \text{ cm}^2$  active area):
  - Si1 300  $\mu\text{m}$  thick
  - Si2 500  $\mu\text{m}$  thick
  - CsI(Tl) 10cm thick
 + read-out electronics for all telescopes.
- Identification techniques:  $\Delta E$ -E / PSA
  - Charge discrimination tested up to  $Z \sim 55$
  - Mass discrimination up to  $Z \sim 25$  /  $Z \sim 22$

R. Bougault et al., *Eur. Phys. J. A* 50, 47 (2014)

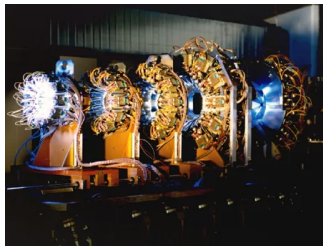
S. Valdré et al., *NIMA* 930, 27 (2019)



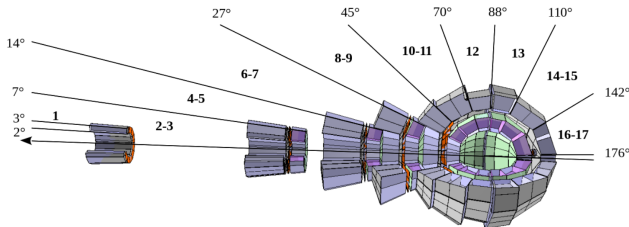


**INDRA** (*Identification de Noyaux et Détection avec Résolutions Accrues*): highly segmented array for detection and identification of charged products of heavy ion collisions at intermediate energies ( $10 < E < 100$  AMeV).

- Original configuration of 17 rings:
  - 1: Phoswich detectors
  - 2-9: Ionisation ch. + Si + CsI(Tl)
  - 10-17: Ionisation ch. + CsI(Tl)
- Charge discrimination up to uranium, mass discrimination up to  $Z \sim 4$   
 → Electronics upgrade (2020): now up to  $Z \sim 10$   
 J. D. Frankland et al., *Nuovo Cim. C* 45, 43 (2022)



- Large solid angle coverage (90%) with high granularity (336 modules)



# INDRA-FAZIA

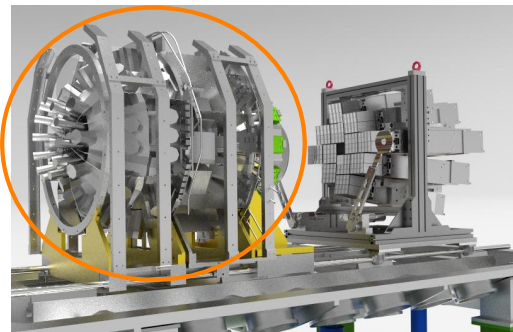
The coupling of the two setups (2019)



- The most forward polar angles ( $1.4^\circ < \theta < 12.6^\circ$ ) have been covered with 12 FAZIA blocks in a wall configuration at 1 m from the target. The first five rings of INDRA have been removed.  
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# Impact parameter reconstruction

A model independent method: basic structure

Centrality-related observable  $X \longleftrightarrow$  deduce the correspondence with  $b$   
(see J. D. Frankland et al., PRC104, 034609 (2021), R. Rogly et al., PRC98, 024902 (2018))  
 $\Rightarrow$  Need to model the conditional probability distribution:  $\mathbf{P}(\mathbf{X}|\mathbf{b})$

## Step 1

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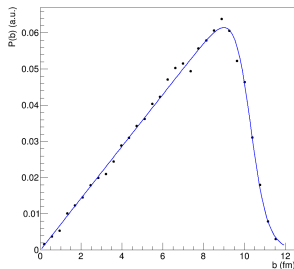
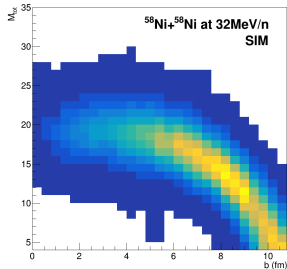
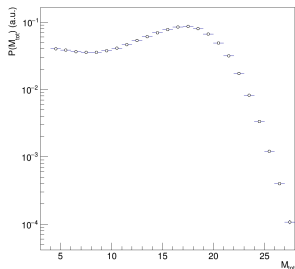
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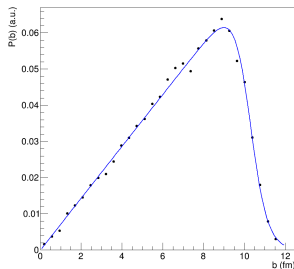
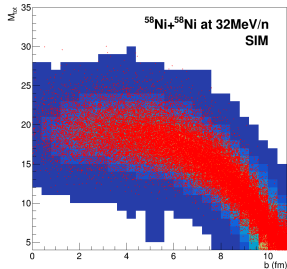
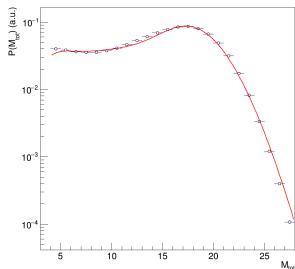
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## Step 3

Having the  $\mathbf{P}(X|\mathbf{b})$ , for each  $X$  selection we can evaluate:

$$P(b|x_1 < X < x_2) = \frac{\int_{x_1}^{x_2} P(b, X) dX}{\int_{x_1}^{x_2} P(X) dX} = \frac{\int_{x_1}^{x_2} P(X) P(b|X) dX}{\int_{x_1}^{x_2} P(X) dX} = \frac{\int_{x_1}^{x_2} P(b) \mathbf{P}(X|\mathbf{b}) dX}{\int_{x_1}^{x_2} P(X) dX}$$



To obtain the impact parameter distribution, it is necessary to perform the fit on the most inclusive  $P(X)$  distribution, for which the  $P(b)$  above can be assumed.



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Some events are discarded in a non-trivial way, especially for semiperipheral collisions. The triangular  $P(b)$  distribution does not well represent the experimental one.

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**INDRA dataset**  $\rightarrow$   $^{58}\text{Ni}+^{58}\text{Ni}$  at 32 MeV/nucl.

- Trigger condition:  $M_{\text{tot}} \geq 4$

Minimum bias, the  $P(b)$  can be well approximated as shown before (with  $\Delta b \approx 0.4\text{fm}$ ). (see J. D. Frankland et al., *Phys. Rev. C* 104, 034609 (2021), E. Vient et al., *Phys. Rev. C* 98, 044612 (2018))

Suitable for the application of the *impact parameter reconstruction method*.

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Procedure for the reaction in common  $^{58}\text{Ni}+^{58}\text{Ni}$  at 32 MeV/nucl.:

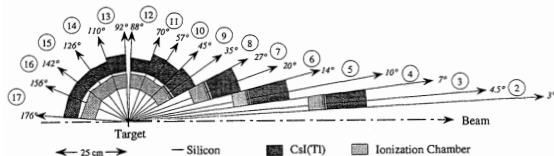
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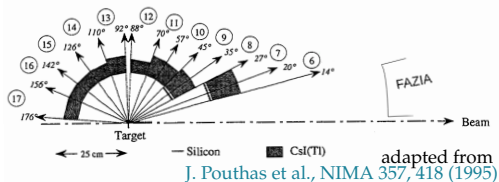


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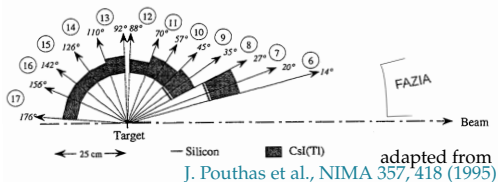


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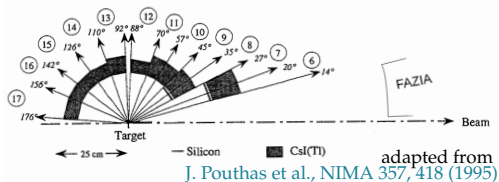


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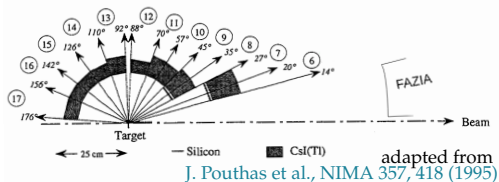
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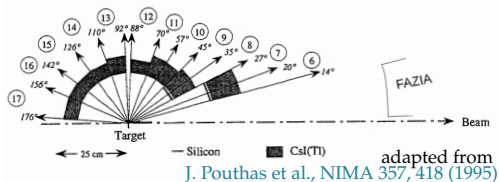
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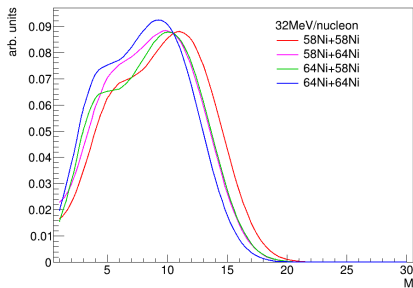
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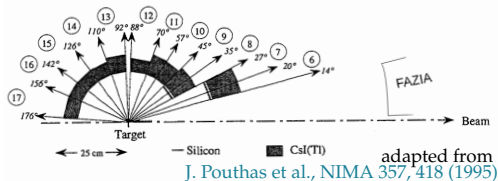


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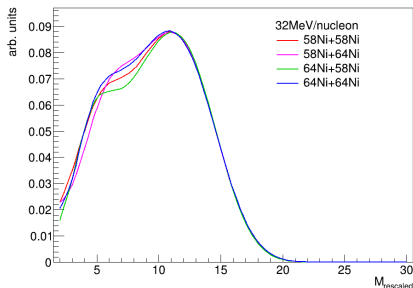
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Procedure for the other systems:

→ rescale the detected multiplicity  $M_{\text{sys}}$  into a corresponding  $M_{\text{resc}}$  value for  $^{58}\text{Ni}+^{58}\text{Ni}$ .

$$M_{\text{resc}} = [\alpha \cdot (M_{\text{sys}} + r) + \beta]$$

where  $r \sim U([0, 1])$  is a uniformly distributed random variable taking values in  $[0, 1]$ .



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Model independent impact parameter distributions

Absolute  $b$  distributions  $\rightarrow$  set  $P(b)$  parameters in a model independent way:

$$P(b) = \frac{2\pi b}{1 + \exp[(b - b_0)/\Delta b]}$$

$\Delta b \approx 0.4 \text{ fm}$  as verified in PRC 104, 034609 (2021)

$b_0$  by inverting  $\sigma_R = -2\pi(\Delta b)^2 \text{Li}_2\left[-\exp\left(\frac{b_0}{\Delta b}\right)\right]$

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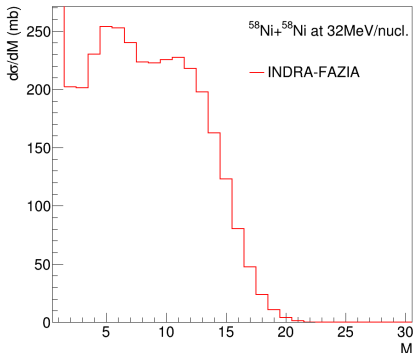
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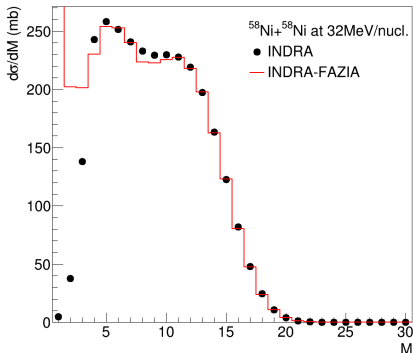
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- Use the elastic scattering events in the INDRA-FAZIA dataset ( $M_{FAZIA} \geq 1$ ) as reference for cross section normalization
- Transfer the normalization to the INDRA dataset using the high multiplicity tail, after correcting for small trigger effect  $\rightarrow \sigma_R$  INDRA dataset  $\Rightarrow b_0 = (9.8 \pm 0.7) \text{ fm}$

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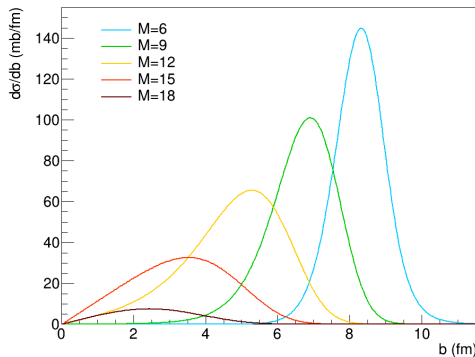
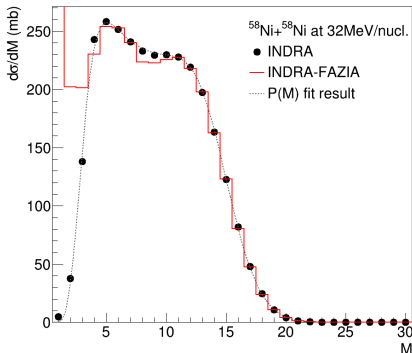
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$b_0$  by inverting  $\sigma_R = -2\pi(\Delta b)^2 \text{Li}_2\left[-\exp\left(\frac{b_0}{\Delta b}\right)\right]$



$\rightarrow$  important role of **intrinsic fluctuations**: relatively different  $M$  selections populate partly (or entirely) superimposed  $b$  intervals

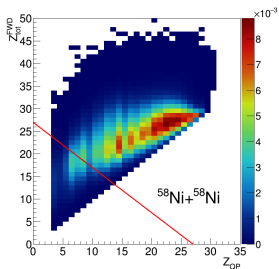
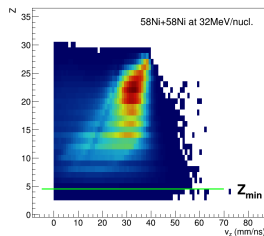


# Isospin analysis

## Selection of the events

In view of producing the most general result, easily comparable with any theoretical prediction, we avoid a strictly exclusive analysis.

- No distinction among different output channels
- QP remnant selected as:
  - 1 fragment with largest  $Z$  in forward hemisphere
  - 2 if more than one with same  $Z$ , select largest  $v_z^{\text{c.m.}}$
- Minimum size to consider a QP remnant:  $Z_{QP} \geq 5$   
→ include light products from very dissipative events



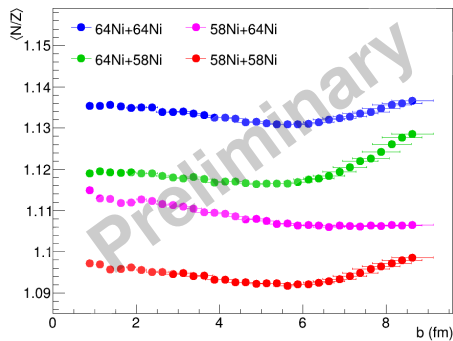
Since we are considering such light QP remnants it is necessary to carefully check the completeness of the event to exclude those in which the heaviest fragment has been lost.

- The total undetected charge in the forward hemisphere should not exceed  $Z_{QP}$
- Accept event if  $Z_{QP} \geq 28 - Z_{tot}^{\text{FWD}}$
- We verified that by removing  $< 13\%$  of events, the final result becomes stable against reasonable variations of  $Z_{QP}^{\text{min}}$

# Isospin analysis

Evolution of isospin equilibration with centrality

From the distributions of  $(Z_{QP}, A_{QP})$  vs  $M_{\text{resc}}$ , the number of counts for each produced nuclear species for each  $M_{\text{resc}}$  value is independently redistributed according to the corresponding  $b$  distribution  $\Rightarrow$  take into account the fluctuations



**Model-independent  $\langle N/Z \rangle$  for the QP remnant as a function of  $b$  for the four systems in the INDRA-FAZIA dataset**

Clear effect of isospin equilibration down to the most central collisions:

- *peripheral*: similar result for reactions with same projectile
- *central*:  $\langle N/Z \rangle$  depends on target, mixed systems tend to each other

The horizontal error bars are associated with the uncertainty on the estimation of  $b_0$  in the  $P(b)$  assumed for the impact parameter reconstruction method, affecting less central collisions to a greater extent.

# Isospin analysis

## Isospin transport ratio

**Isospin transport ratio:** can highlight the isospin diffusion effect, bypassing the effects acting similarly on the four systems (F. Rami et al., Phys. Rev. Lett. 84, 1120 (2000))

$$R(x) = \frac{2x_i - x_{AA} - x_{BB}}{x_{AA} - x_{BB}}$$

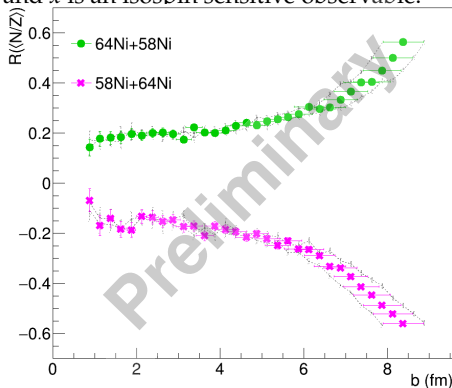
$R(x) = \pm 1 \rightarrow$  non equilibrated

$R(x_{AB}) = R(x_{BA}) \rightarrow$  full equilibration

where  $A = {}^{64}\text{Ni}$ ,  $B = {}^{58}\text{Ni}$ ,  $i = AA, AB, BA, BB$  and  $x$  is an isospin sensitive observable.

**Model-independent isospin transport ratio  $R(\langle N/Z \rangle)$  for the QP remnant as a function of the impact parameter  $b$**

Regular behavior towards equilibration for increasing centralities (full equilibration is not achieved).



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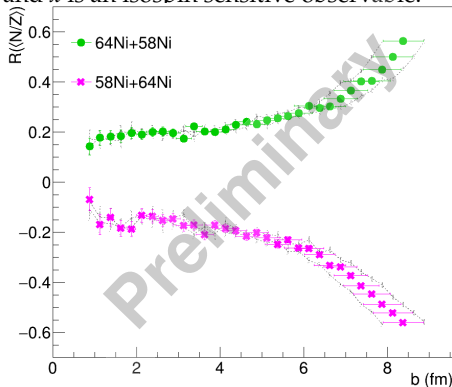
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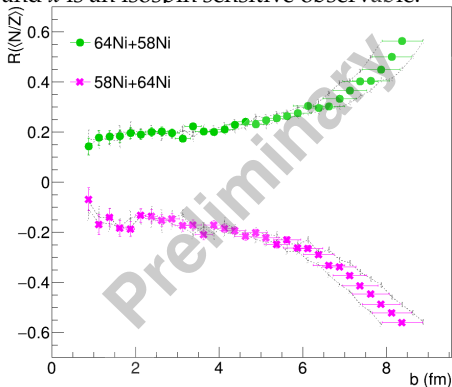
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The isospin transport ratio is also largely unaffected by statistical deexcitation.

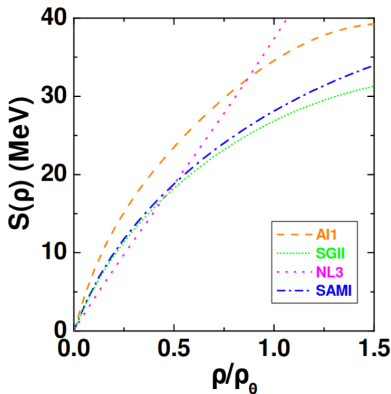
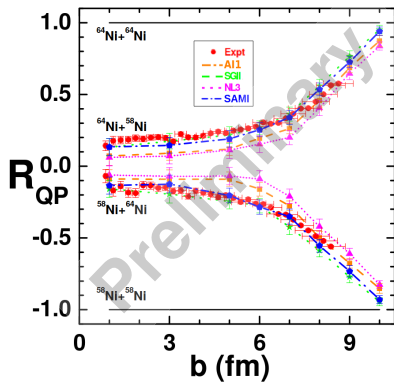
A. Camaiani et al., Phys. Rev. C 102, 044607 (2020),

S. Mallik et al., J. Phys. G 49, 015102 (2021)



# Preliminary comparison with theoretical predictions

BUU@VECC-McGill model predictions for different  $E_{sym}$



**Comparison of experimental  $R(\langle N/Z \rangle)$  vs  $b$  with theoretical predictions from BUU@VECC-McGill transport model for primary QP fragment.**

No afterburner coupled to transport code (S. Mallik et al., J. Phys. G 49, 015102 (2021)).

Some differences arise among model predictions assuming different symmetry energy parametrizations, particularly for semicentral collisions. Multiple  $E_{sym}$  parametrizations are being explored (J. Margueron et al., Phys. Rev. C 97, 025806 (2018)).

## Summary

- First INDRA-FAZIA experiment: isospin diffusion at Fermi energies
- Combined analysis of two datasets (INDRA and INDRA-FAZIA) of Ni-Ni reactions at 32MeV/nucleon
- Model independent reconstruction of the impact parameter
- *Experimental result*: isospin transport ratio calculated on the isospin content of QP remnant, studied as a function of the impact parameter
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## Future perspectives

- Multiple symmetry energy parametrizations are being tested
- The evolution of crucial quantities (e.g. density, currents) in the framework of the BUU model predictions is being studied
- This model independent experimental assessment of the isospin diffusion effect across varying reaction centralities can represent a benchmark to test the performance of transport models and to gain further insight on the N<sub>EoS</sub> behavior for sub- to saturation densities



# *Backup slides*

# Impact parameter reconstruction

## Detailed structure of the method

Given a centrality observable  $X$ , its inclusive distribution  $P(X)$  can be expressed as:

$$P(X) = \int_0^\infty P(X, b) db = \int_0^\infty P(b) P(X|b) db = \int_0^1 P(X|c_b) dc_b$$

where a change of variables is applied, introducing the centrality  $c_b \equiv \int_0^b P(b') db'$  and exploiting that  $P(c_b) = 1$ .

**Key step:** model the  $P(X|c_b)$  and extract its parameters by fitting the experimental  $P(X)$ .  $X$  assumes positive values  $\rightarrow$  non-negative gamma distribution as fluctuation kernel:

$$P(X|c_b) = \frac{1}{\Gamma(k)\theta^k} X^{k-1} e^{-X/\theta} \quad \text{where } \bar{X} = k\theta \text{ and } \sigma_X = \sqrt{k}\theta$$

where  $k$  and  $\theta$  generally evolve with centrality. For them we assume:

- $k(c_b) = k_{\max}[1 - c_b^\alpha]^\gamma + k_{\min}$ , where  $\alpha$ ,  $\gamma$ ,  $k_{\min}$  and  $k_{\max}$  are parameters of the fit
- $\theta$  independent of centrality (problem is underconstrained)  $\rightarrow \theta$  is a fit parameter

Once the  $P(X|c_b)$  is determined, one obtains:

$$P(c_b|x_1 \leq X \leq x_2) = \frac{\int_{x_1}^{x_2} P(c_b, X) dX}{\int_{x_1}^{x_2} P(X) dX} = \frac{\int_{x_1}^{x_2} P(X|c_b) dX}{\int_{x_1}^{x_2} P(X) dX}$$

and by changing back the variable:  $P(b|x_1 \leq X \leq x_2) = P(b) P(c_b(b)|x_1 \leq X \leq x_2)$

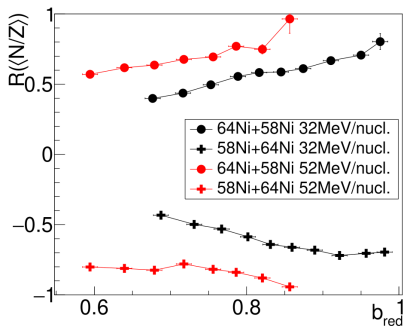
### Scientific production from the first INDRA-FAZIA experiment:

- E789 (2019):  $^{58,64}\text{Ni}+^{58,64}\text{Ni}$  at 32, 52 MeV/nucl.  
C. C. et al. (INDRA-FAZIA coll.), Phys. Rev. C 106, 024603 (2022),  
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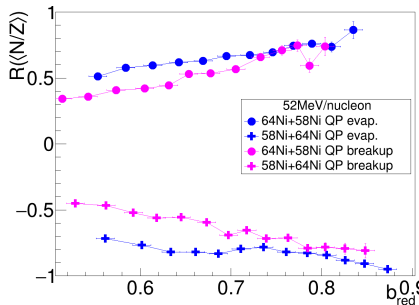
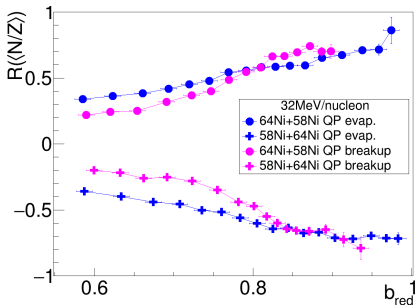
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