



**Nuclear Incompressibility, K_∞ ,
and
the Asymmetry Term, K_τ ,
from
Measurements of the Giant Monopole Resonance
in Neutron-Rich Nuclei**

U. Garg
University of Notre Dame

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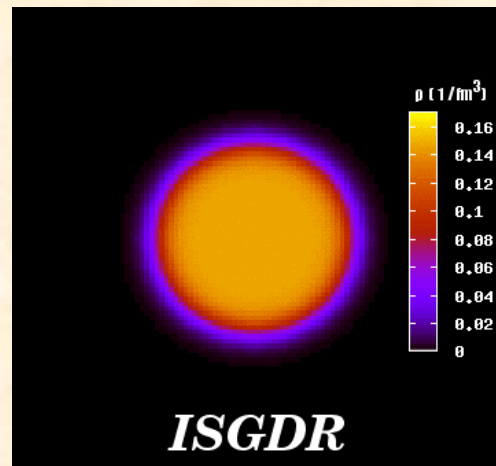
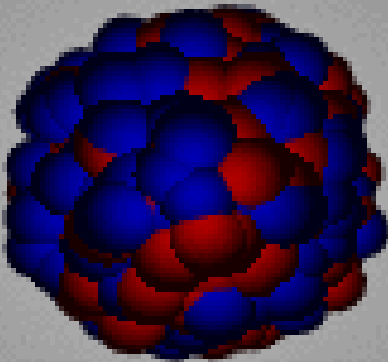
The Compressional Mode Giant Resonances

GMR

ISGDR

$l = 0$

$l = 1$



"Breathing Mode"

"Squeezing Mode"

$$\ddot{a} r_i^2$$

$$2 \square W$$

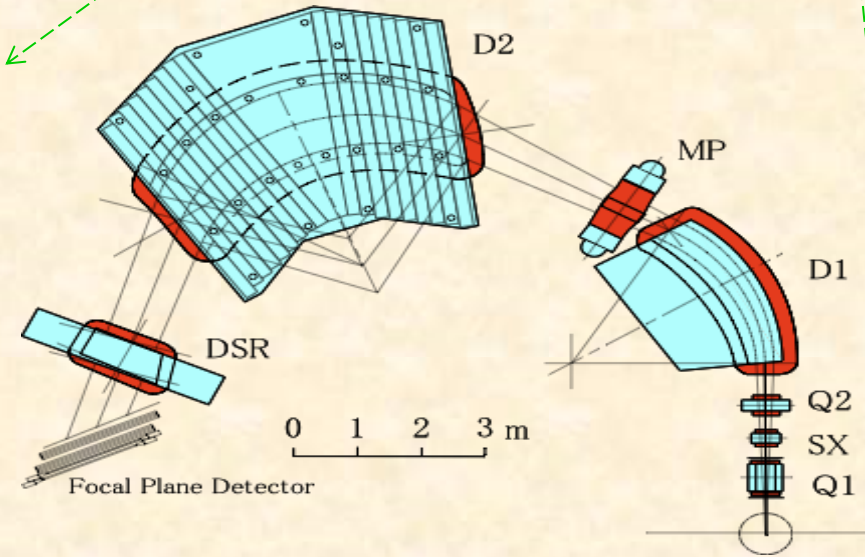
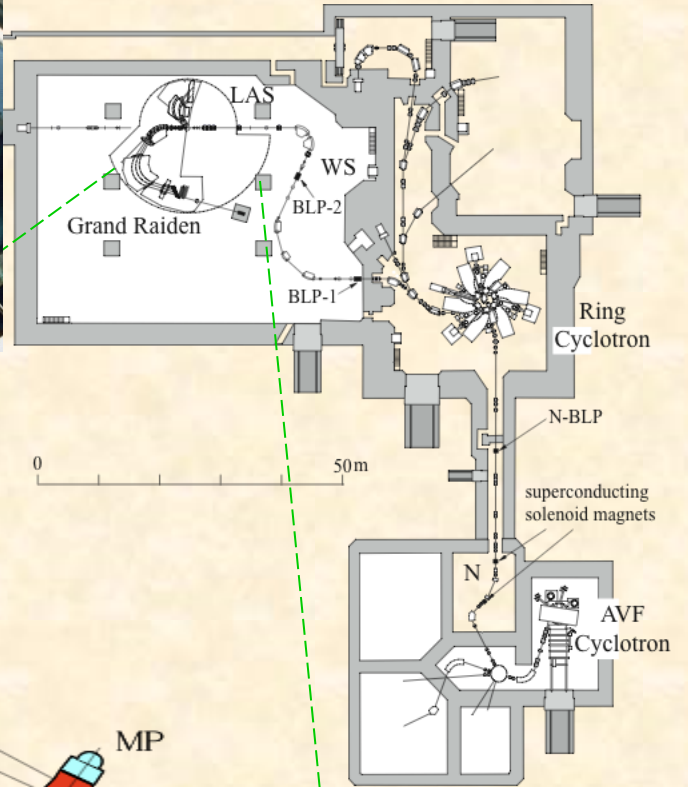
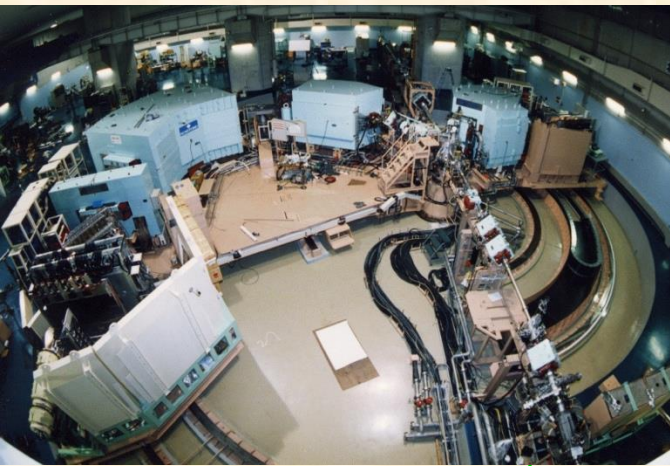
$$\ddot{a} r_i^3 Y_1$$

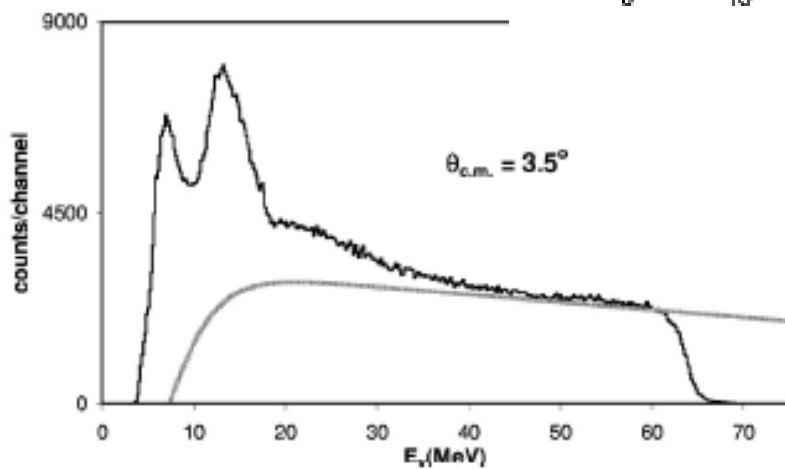
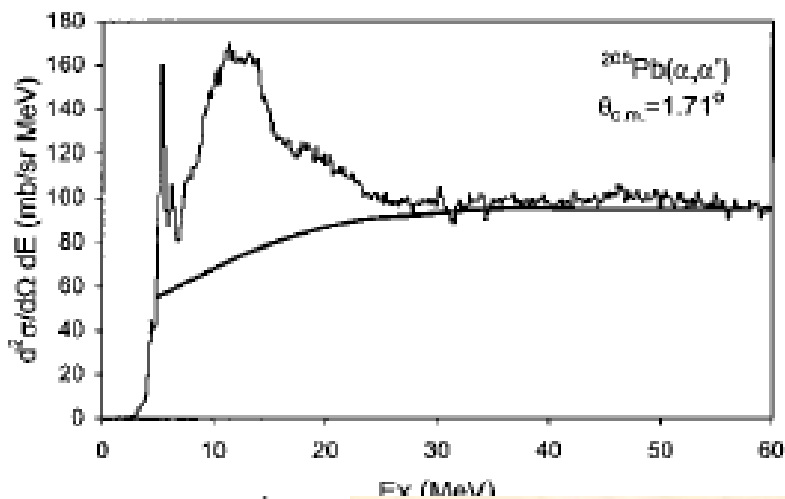
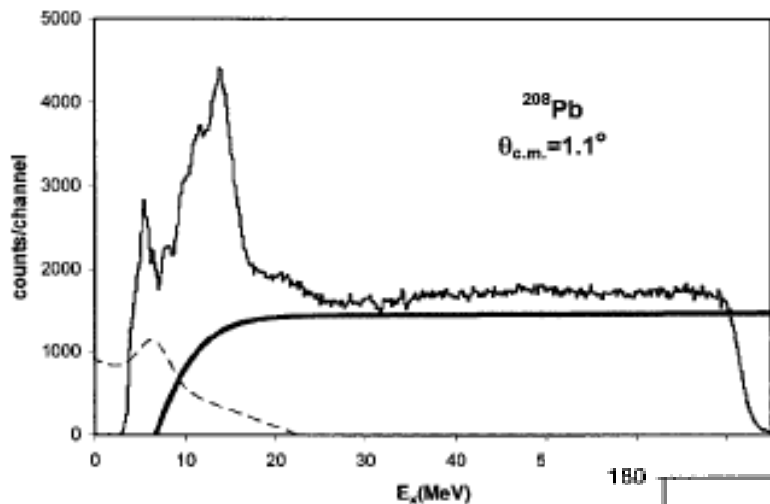
$$3 \square W$$

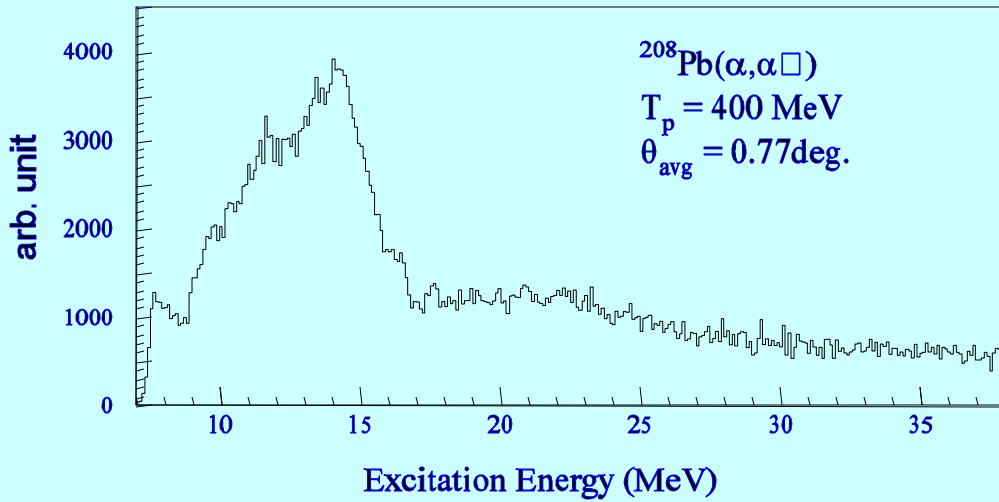
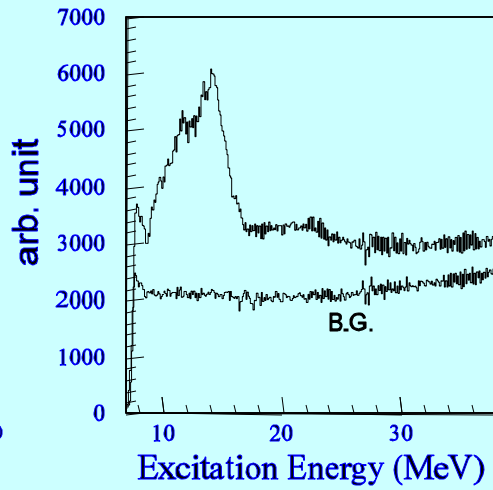
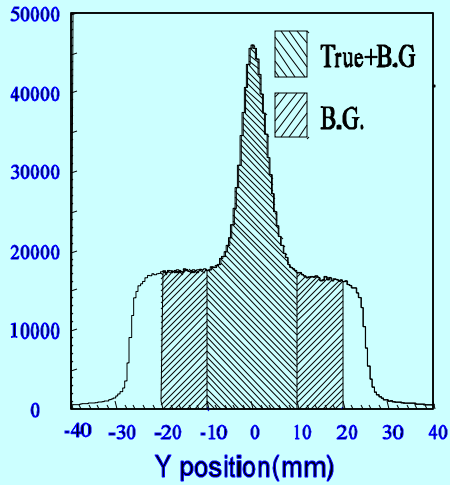
The energies of both these resonances are directly related to Nuclear Incompressibility.

$$E_{GMR} = \square \sqrt{\frac{K_A}{m \langle r^2 \rangle}}$$

$$E_{ISGDR} = \square \sqrt{\frac{7 K_A + \frac{27}{25} e_F}{3 m \langle r^2 \rangle}}$$









From GMR data on ^{208}Pb and ^{90}Zr
 $K_{\infty} = 240 \pm 20 \text{ MeV}$

This number is consistent with both GMR and ISGDR data and with non-relativistic and relativistic calculations



We know K_A from E_{GMR} :

$$E_{GMR} = \hbar \sqrt{\frac{K_A}{m \langle r^2 \rangle}}$$

In an approximate way, K_A may be expressed as:

$$K_A \sim K_\infty (1 + cA^{-1/3}) + K_\tau ((N - Z)/A)^2 + K_{Coul} Z^2 A^{-4/3}$$

$$c \sim -1$$

K_{Coul} is, basically, model independent

$$K_\tau ??$$

Measurements over a series of isotopes gives K_τ

$$K_\tau = K_{sym} - 6L - Q_0 L / K_\infty$$

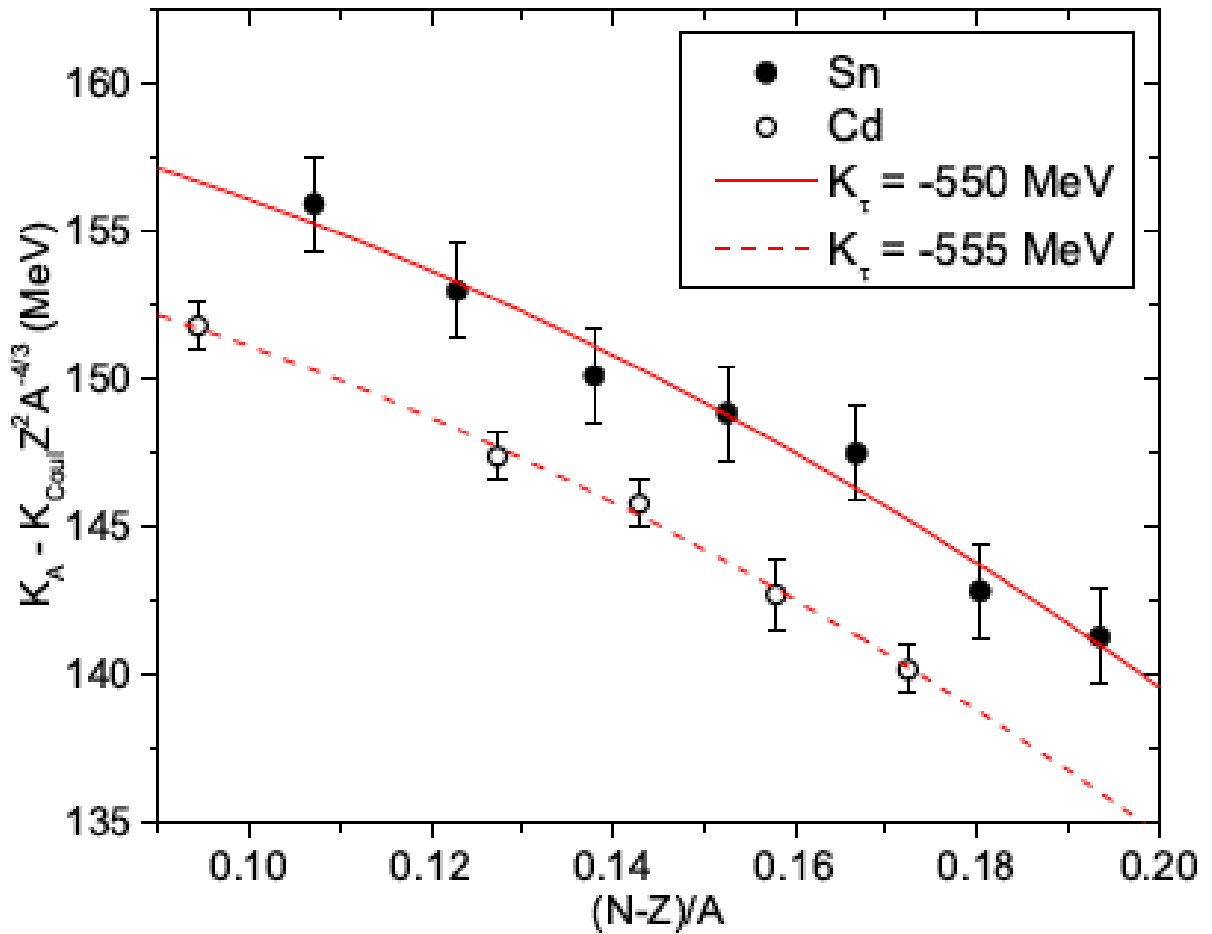


$$K_A \sim K_{\text{vol}} (1 + cA^{-1/3}) + K_{\tau} ((N - Z)/A)^2 + K_{\text{Coul}} Z^2 A^{-4/3}$$

$$K_A - K_{\text{Coul}} Z^2 A^{-4/3} \sim K_{\text{vol}} (1 + cA^{-1/3}) + K_{\tau} ((N - Z)/A)^2$$

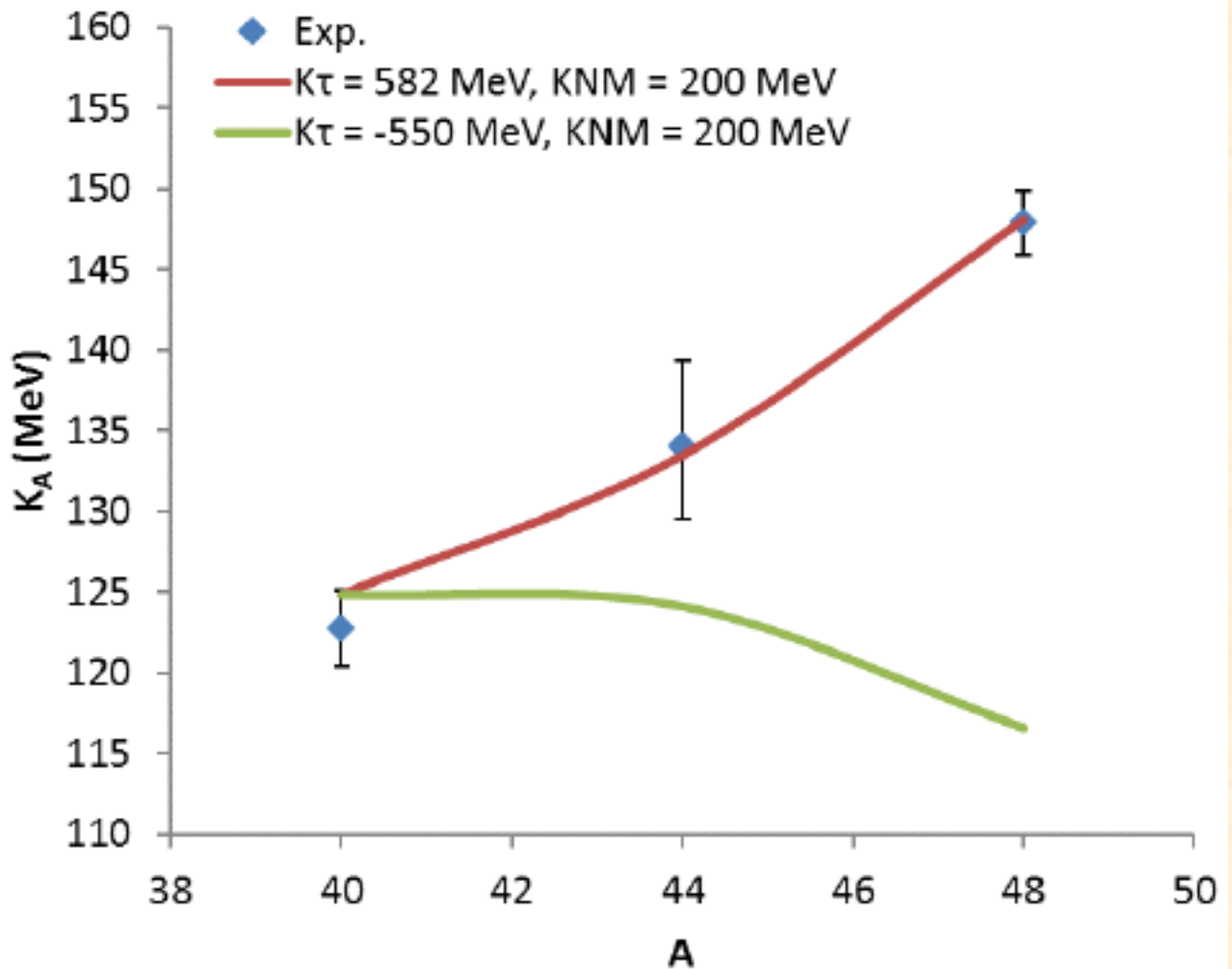
$$\sim \text{Constant} + K_{\tau} ((N - Z)/A)^2$$

We use $K_{\text{Coul}} = - 5.2 \text{ MeV}$ (from Sagawa)

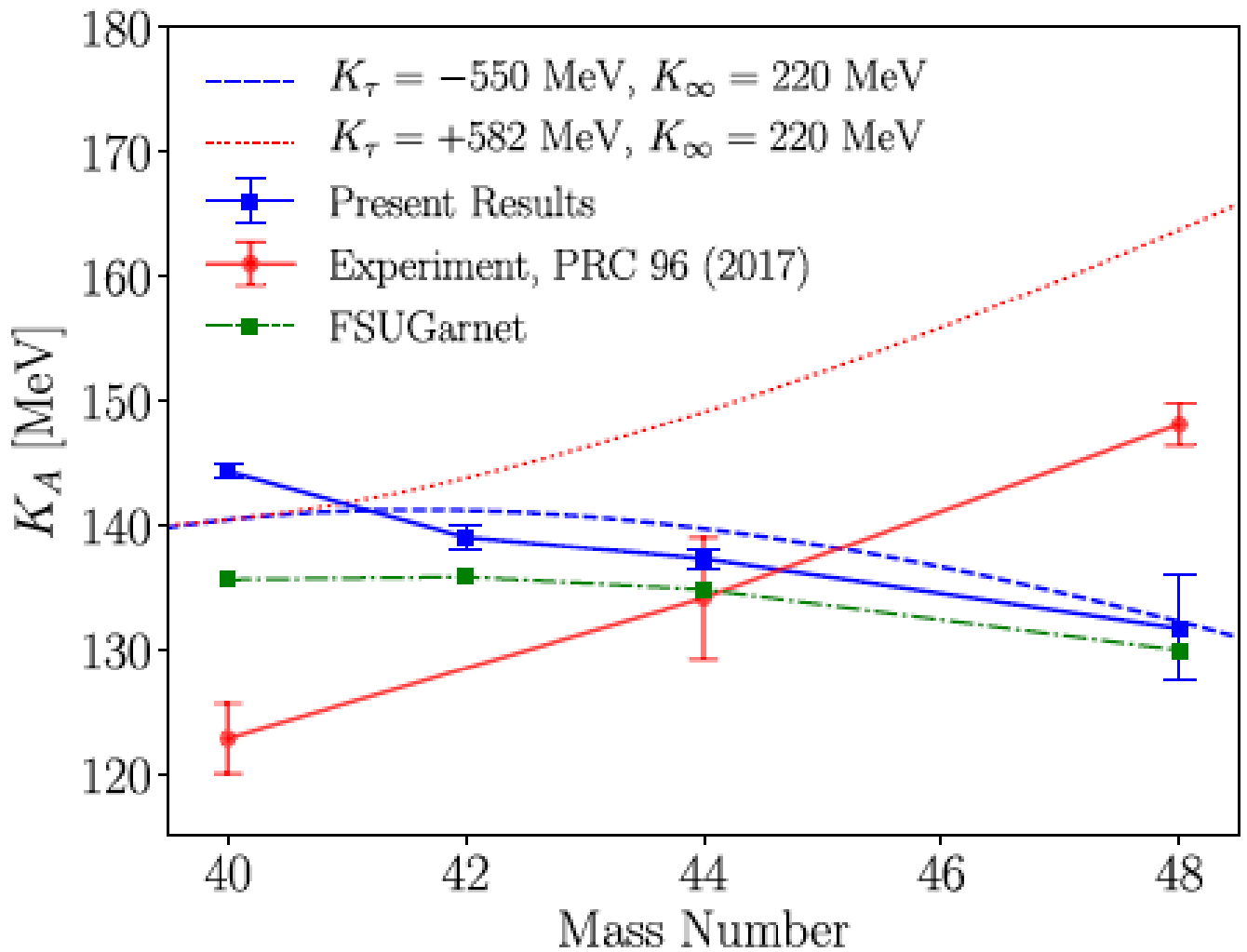


$$K_\tau = -550 \pm 100 \text{ MeV}$$

$$K_\tau = K_{\text{sym}} - 6L - Q_0 L / K_\infty$$



J. Button et al., Phys. Rev. C 96, 054330 (2017)



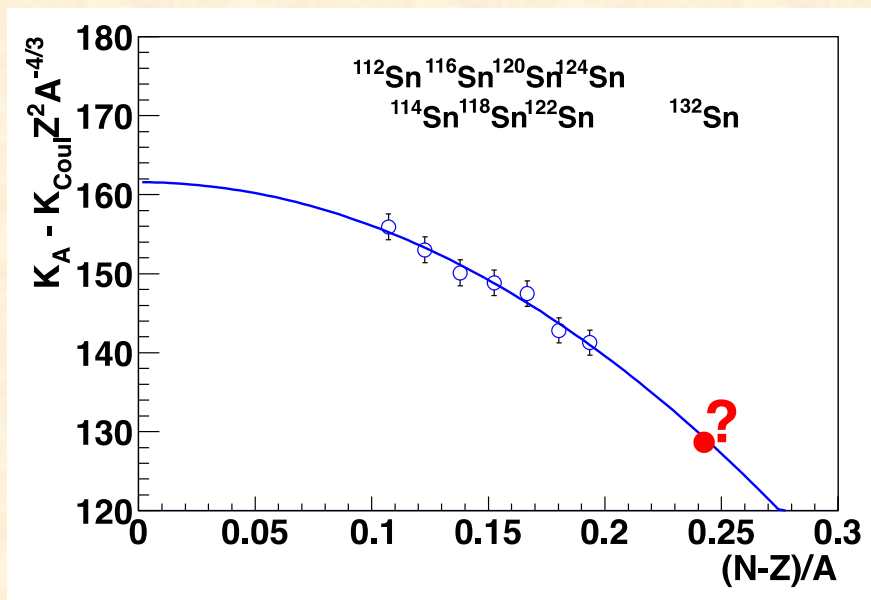
K. B. Howard et al., Phys. Lett. B **801**, 135185 (2020)



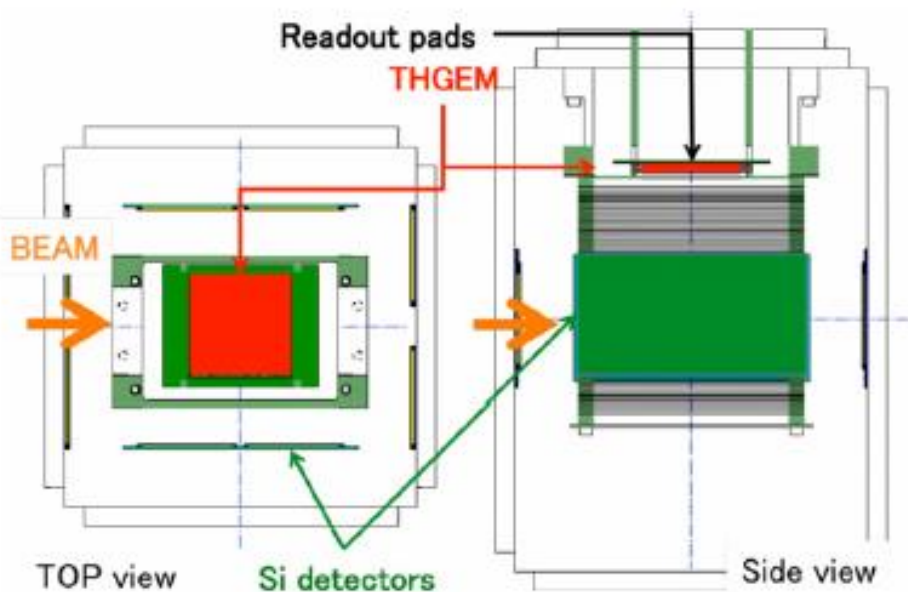
Can we do any better on K_∞ and K_τ ?

-- Not much, I think, on K_∞

-- Can hope for improvement in K_τ



± 50 MeV, perhaps



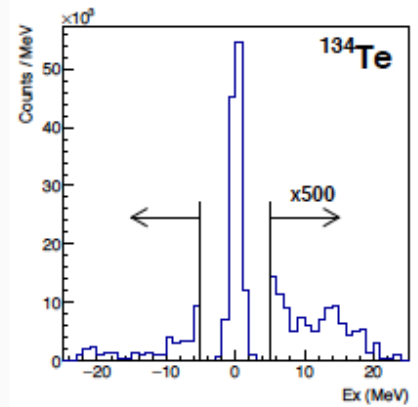
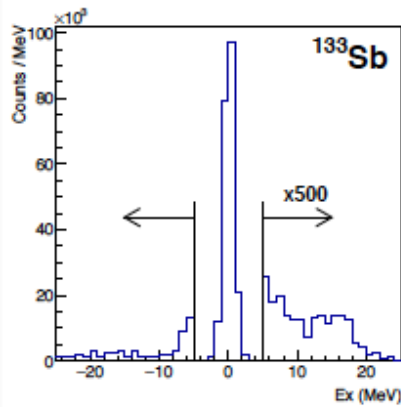
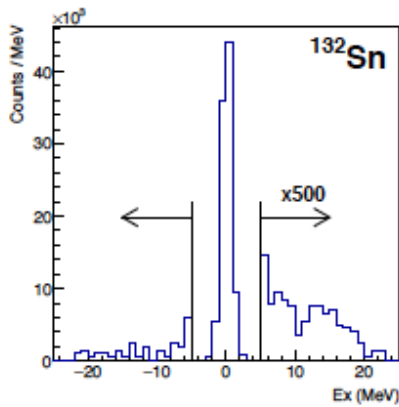
RIBF 113

$^{132}\text{Sn} + ^2\text{H}$
100 MeV/A
>50 kHz ^{132}Sn



Preliminary uncorrected energy spectra for ^{132}Sn , ^{133}Sb , and ^{134}Te .

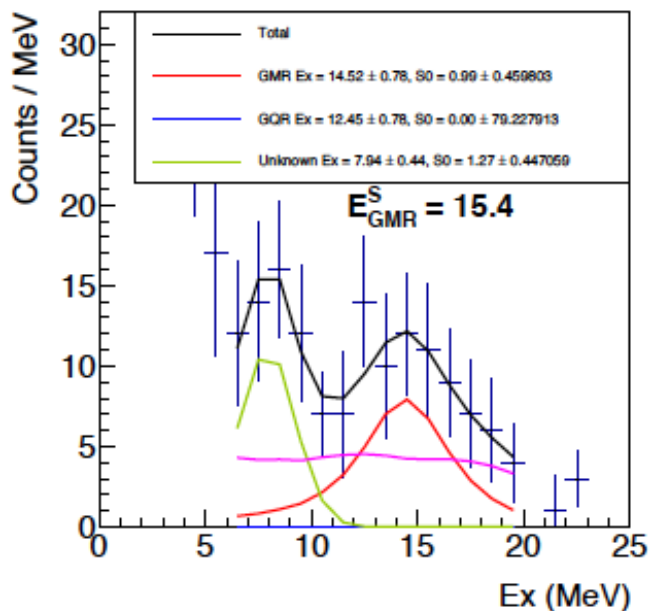
Particle identifications of beam and recoil particles have been done.



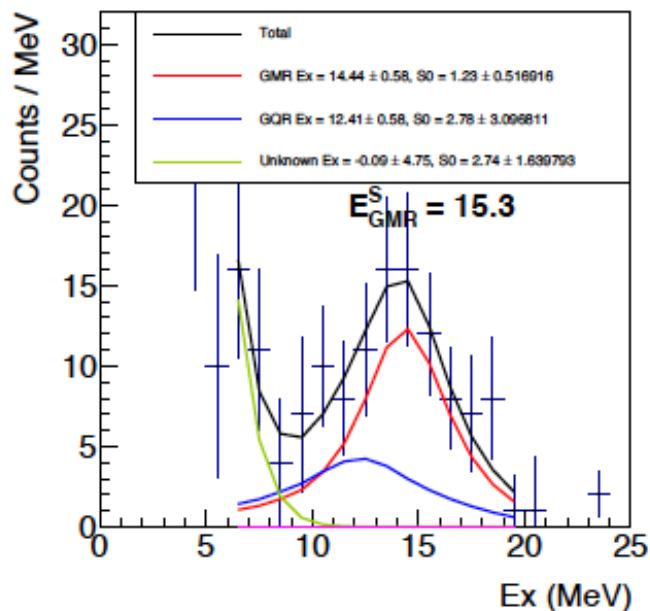
Preliminary results from RIKEN $d(^{132}\text{Sn}, ^{132}\text{Sn}')d$ experiment



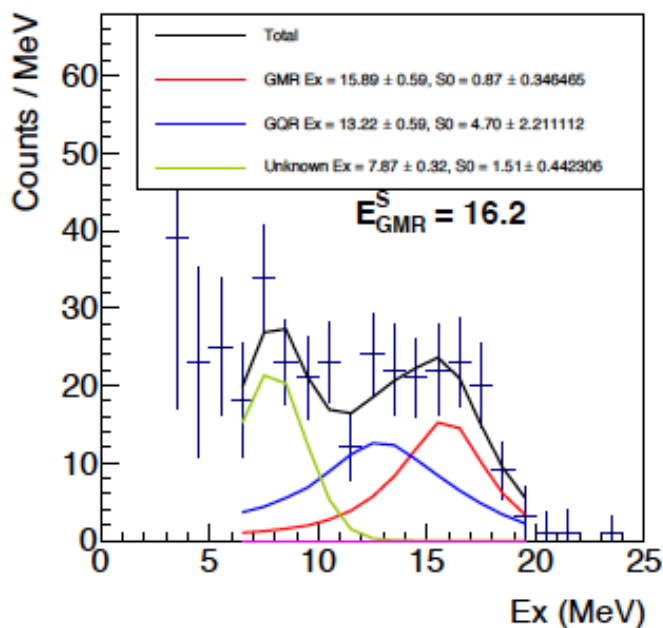
^{132}Sn

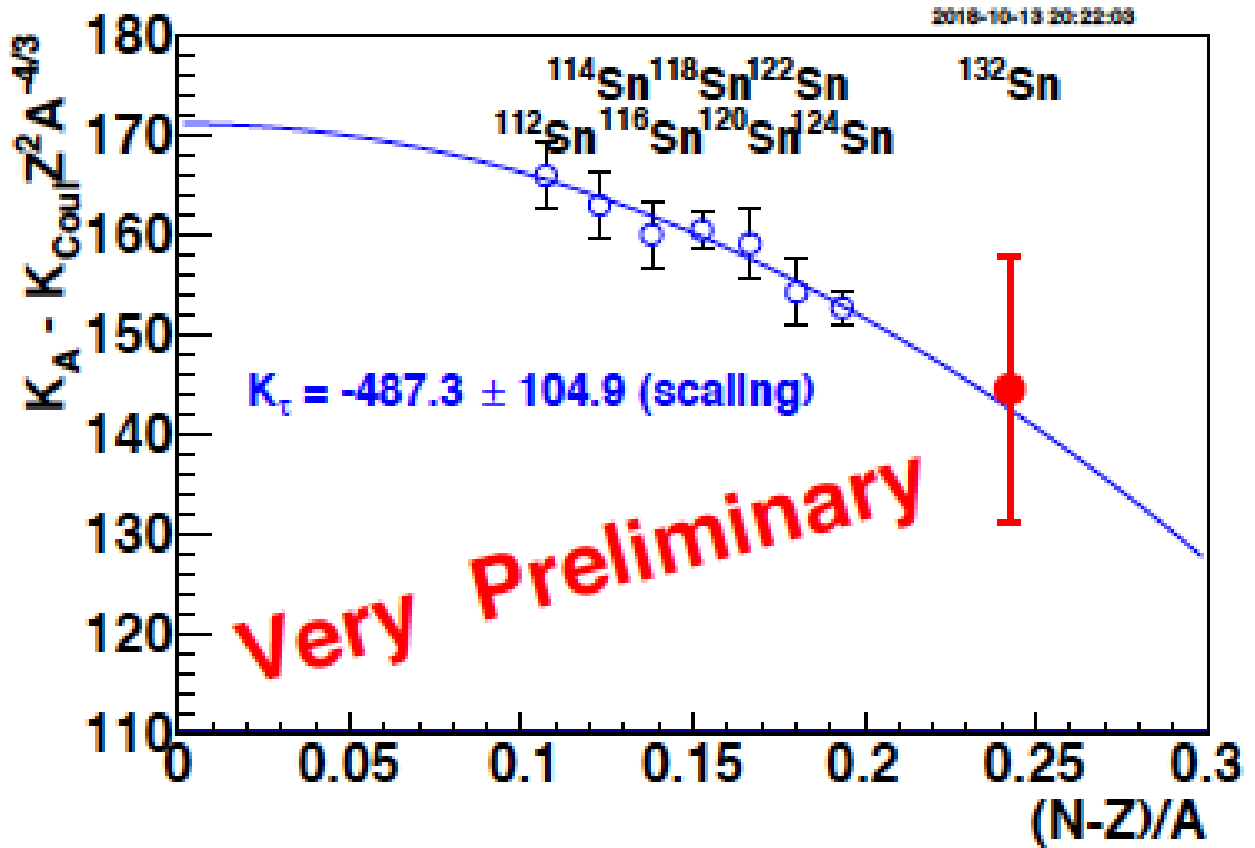


^{134}Te

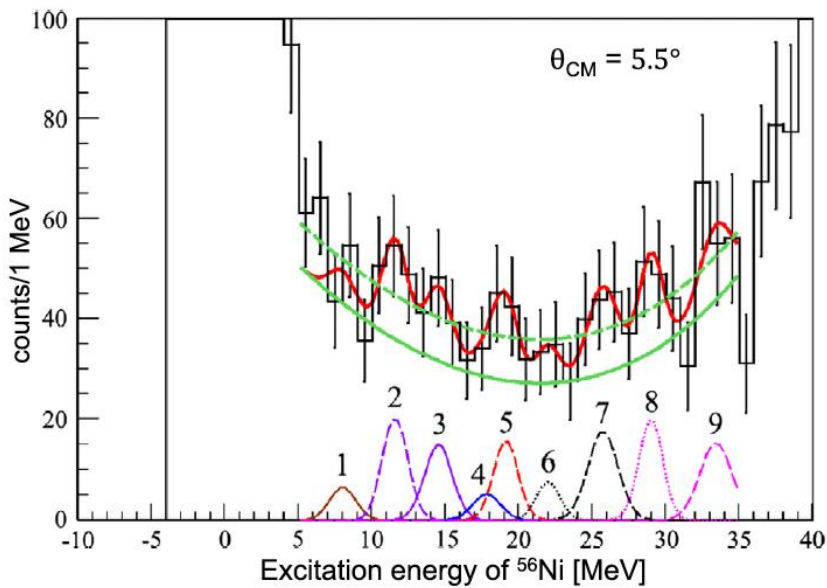


^{133}Sb



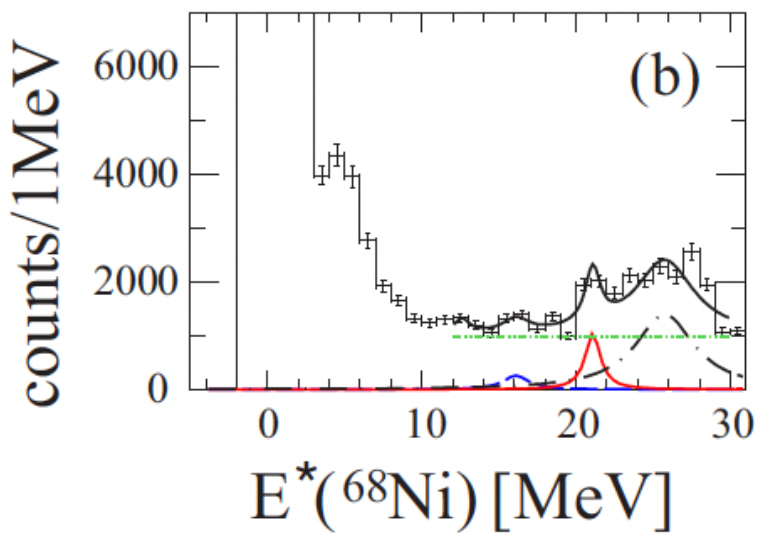


Preliminary results from RIKEN $d(^{132}\text{Sn}, ^{132}\text{Sn}')d$ experiment



^{56}Ni
GANIL

^{68}Ni
GANIL



50 MeV/A (α, α'); He with 5% CF_4



${}^4\text{He}({}^{70}\text{Ni}, {}^{70}\text{Ni}'){}^4\text{He}$ @ NSCL

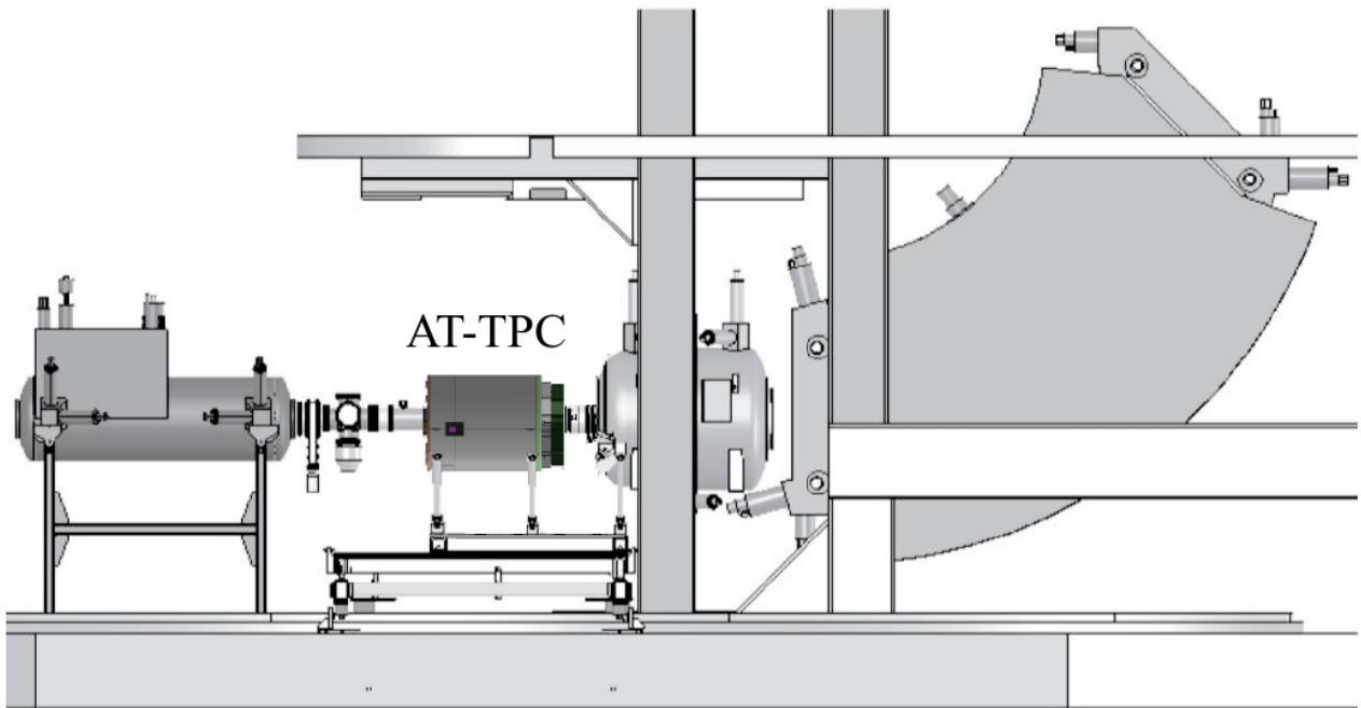


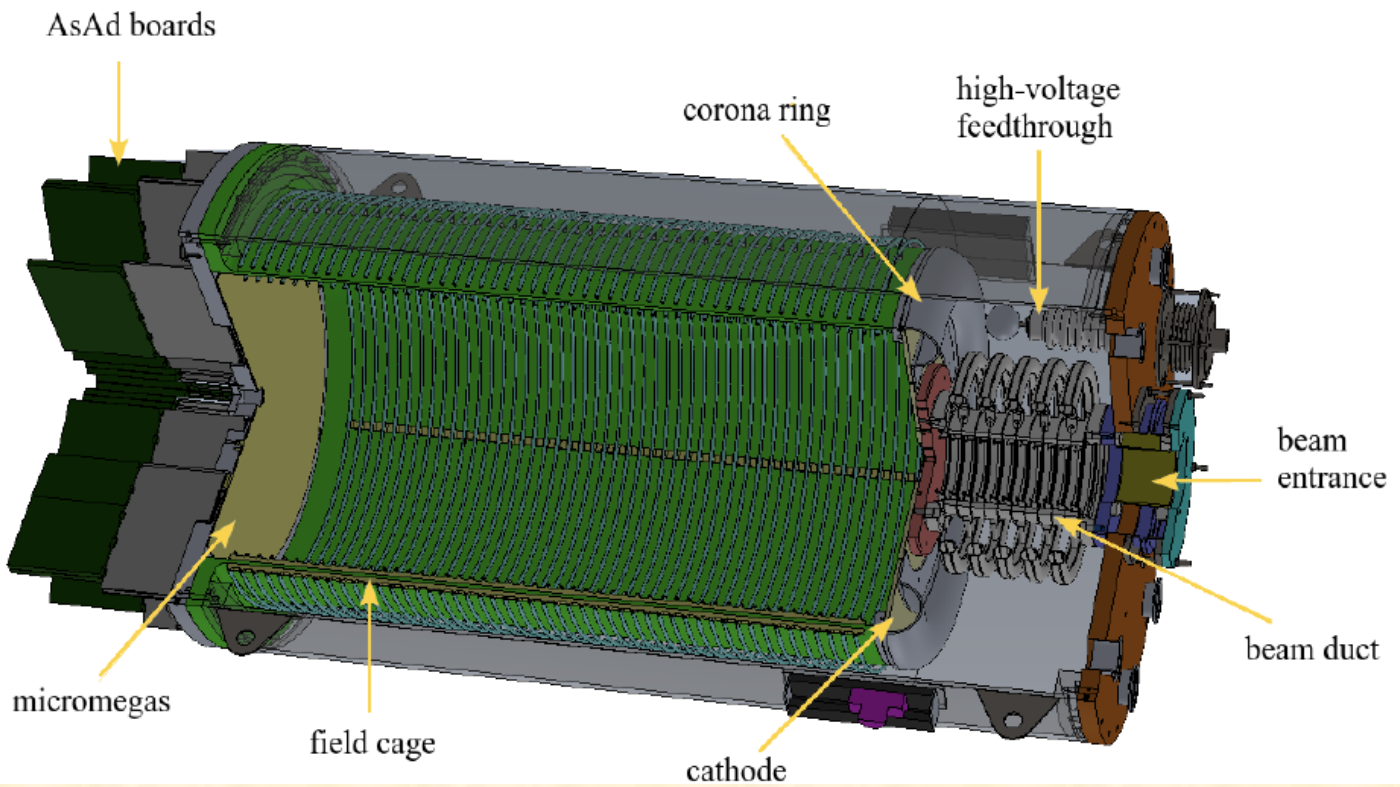
82 MeV/A; ~20k pps

e18207

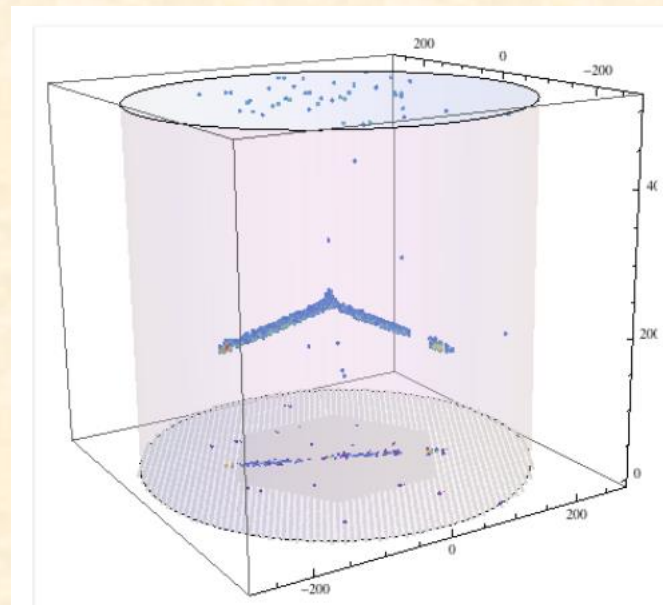


${}^4\text{He}({}^{70}\text{Ni}, {}^{70}\text{Ni}'){}^4\text{He}$ @ NSCL





150 torr of
pure ^4He gas

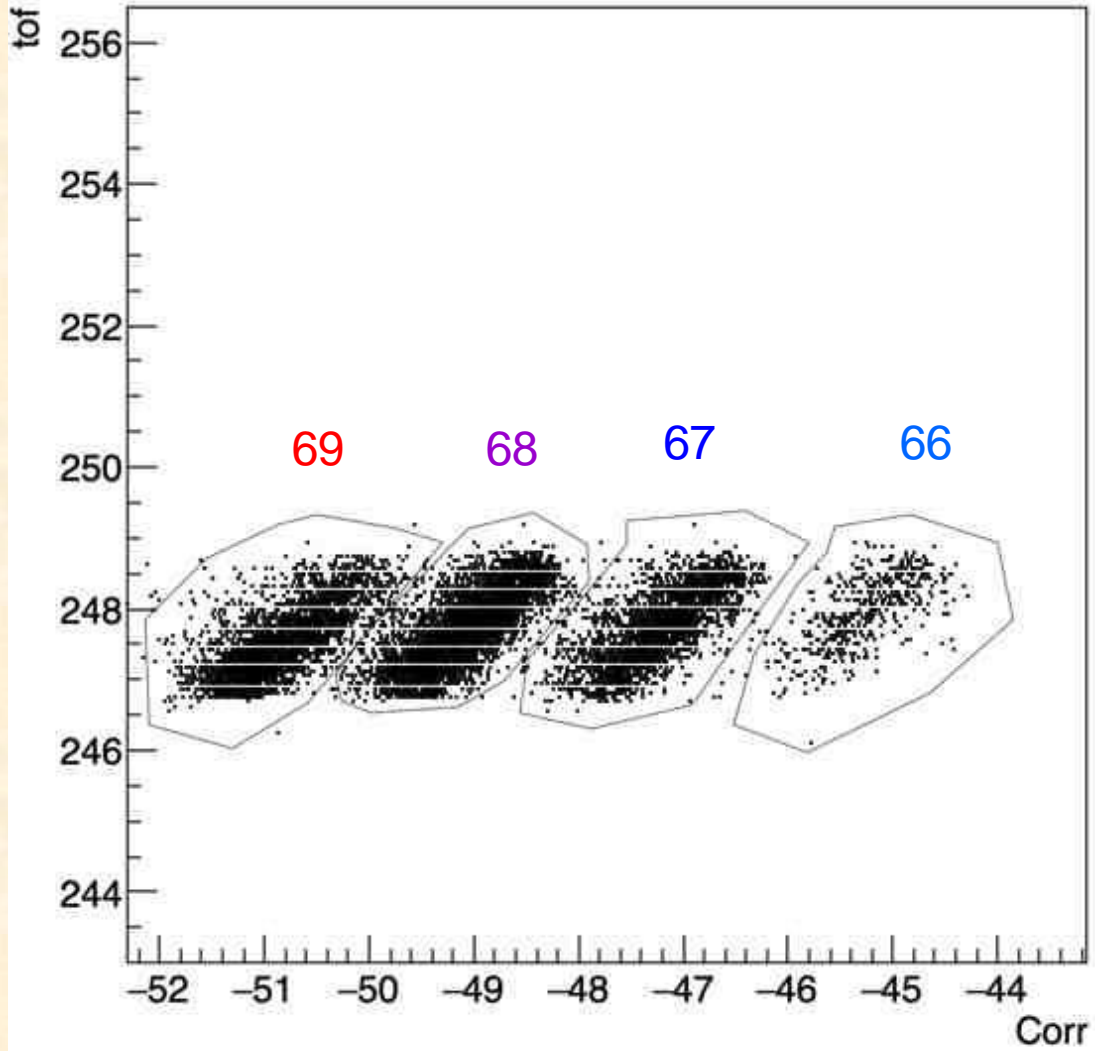


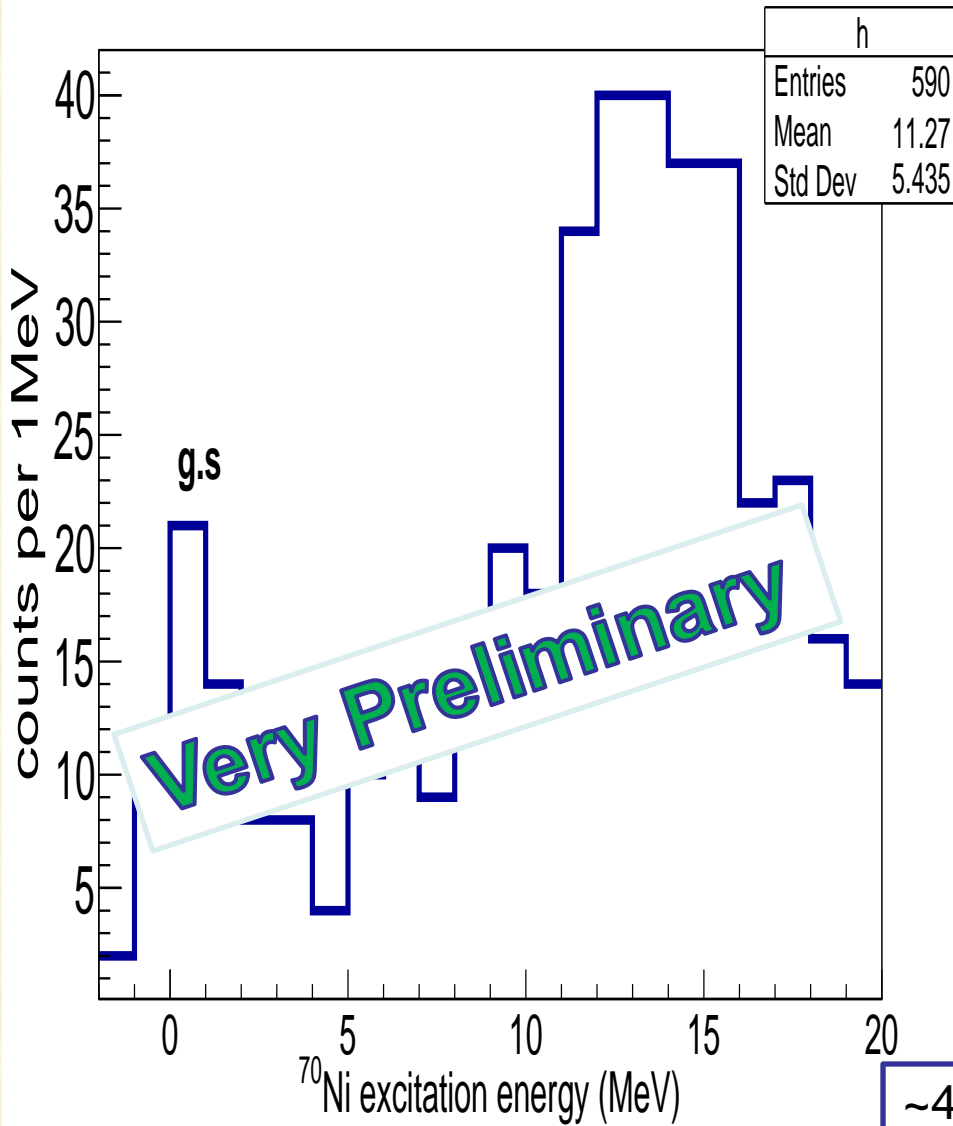
J. Bradt et al., Nucl. Inst. Meth. Phys. Res. A **875**, 65 (2017)

Giraud et al., Nucl. Inst. Meth. Phys. Res. A **1051**, 168213 (2023)

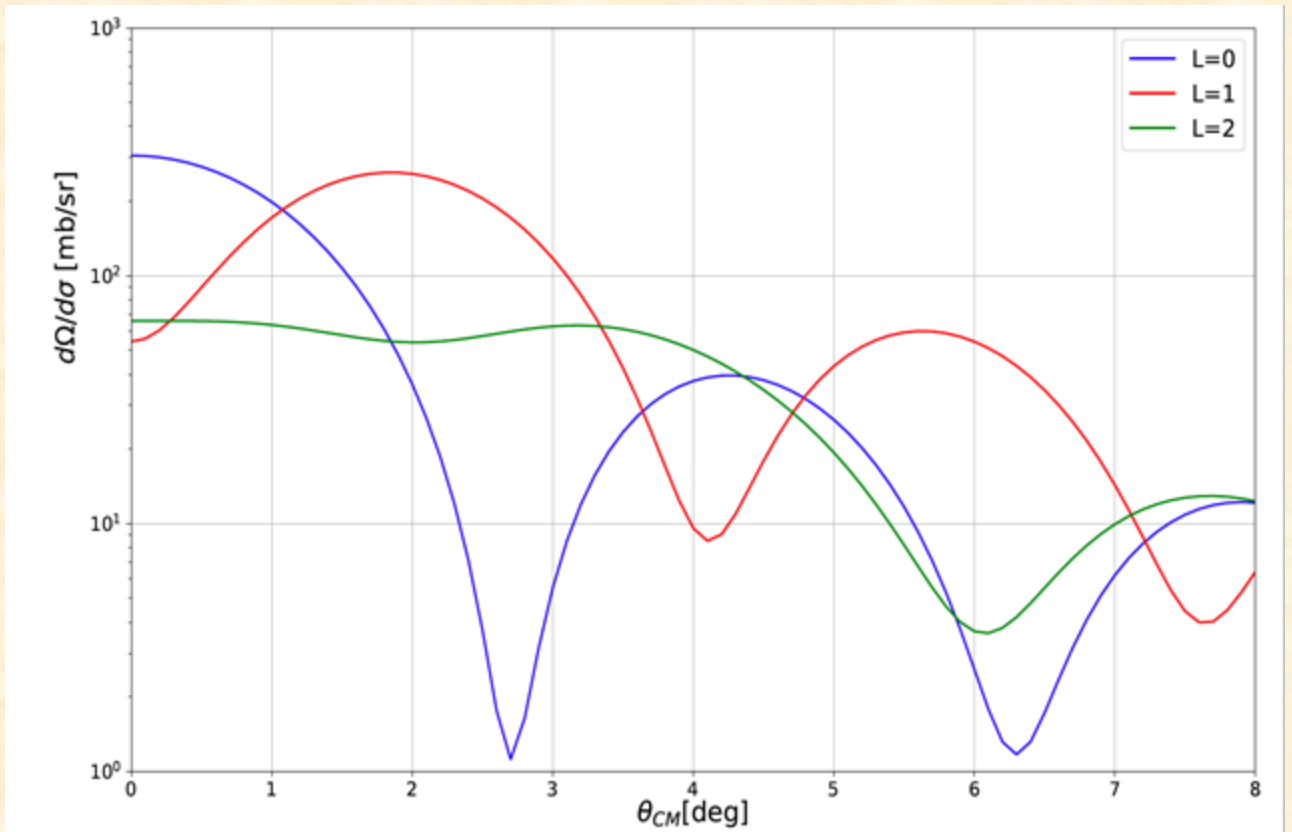


tof:Corr

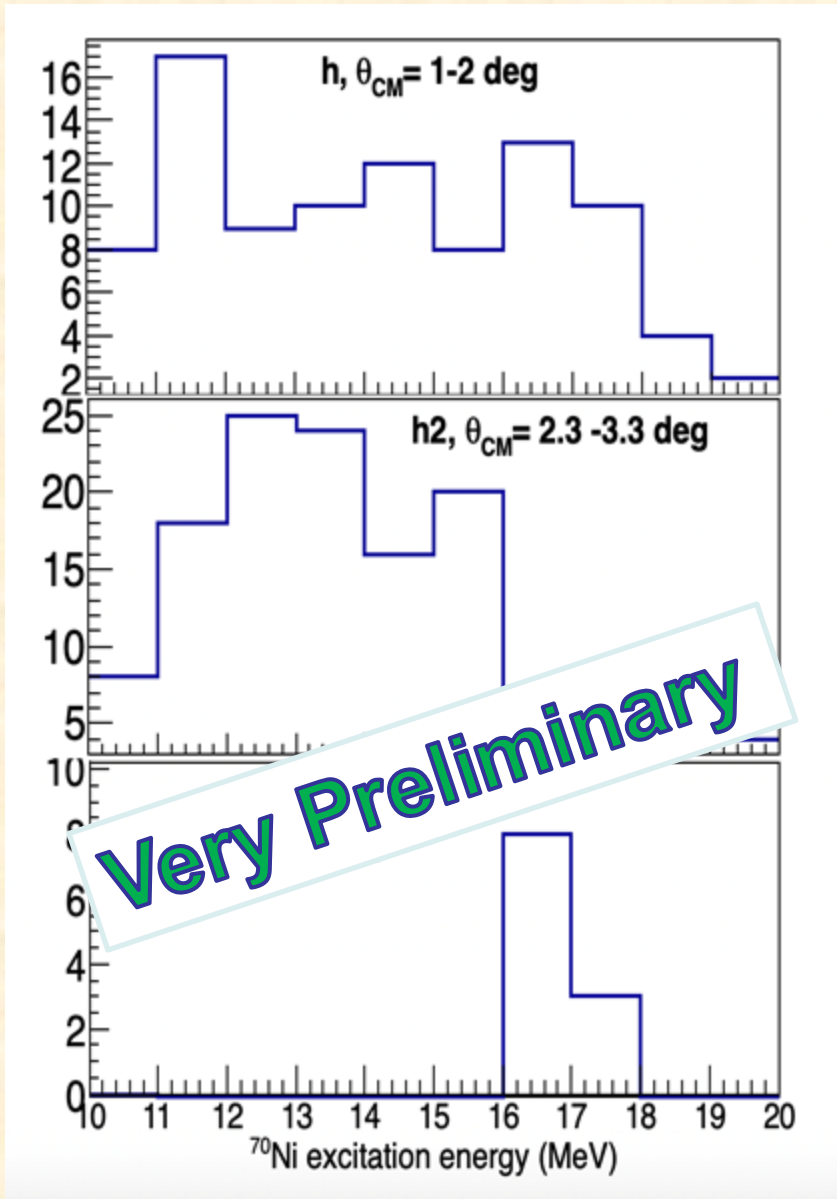




Preliminary results from J.S. Randhawa et al.



- L=0 : Minima at ~ 2.7 degrees
- L=2 : nearly flat in 1-4 degrees

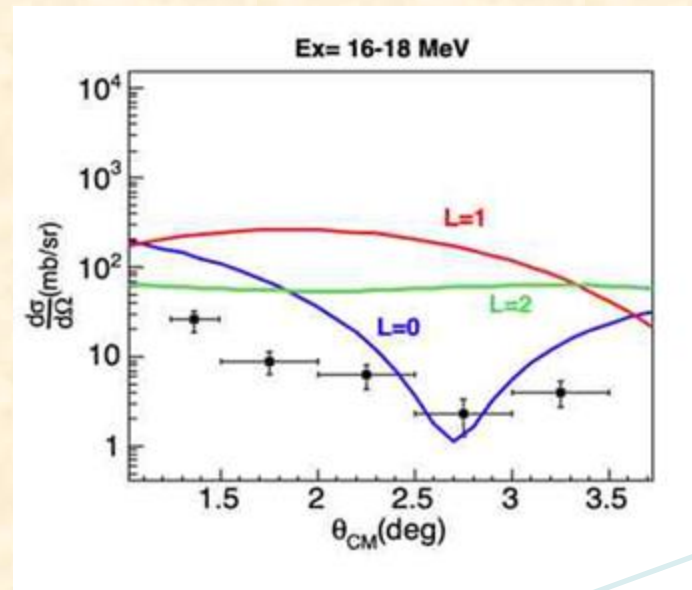


$1^\circ - 2^\circ$

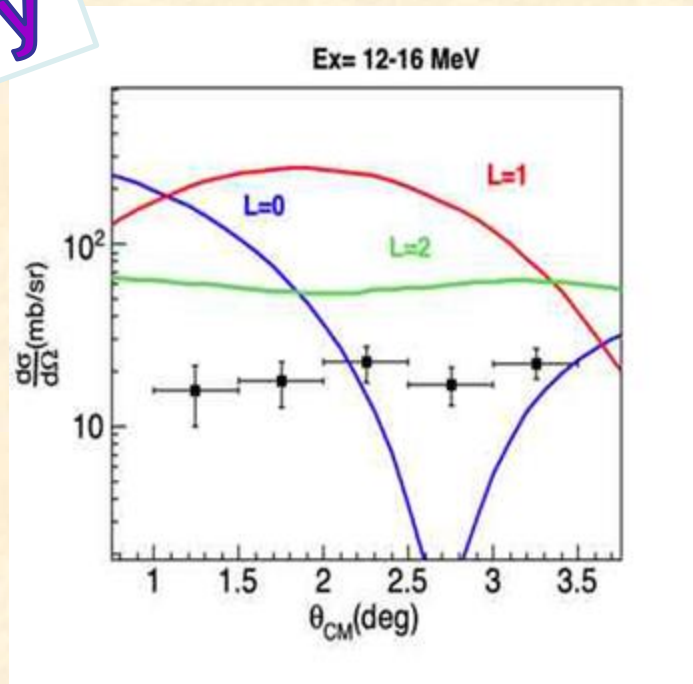
$2.3^\circ - 3.3^\circ$

In ^{70}Ni GMR expected at ~ 17 MeV

Preliminary results from J.S. Randhawa et al.



Very Preliminary





${}^4\text{He}({}^{132}\text{Sn}, {}^{132}\text{Sn}'){}^4\text{He}$ @ FRIB

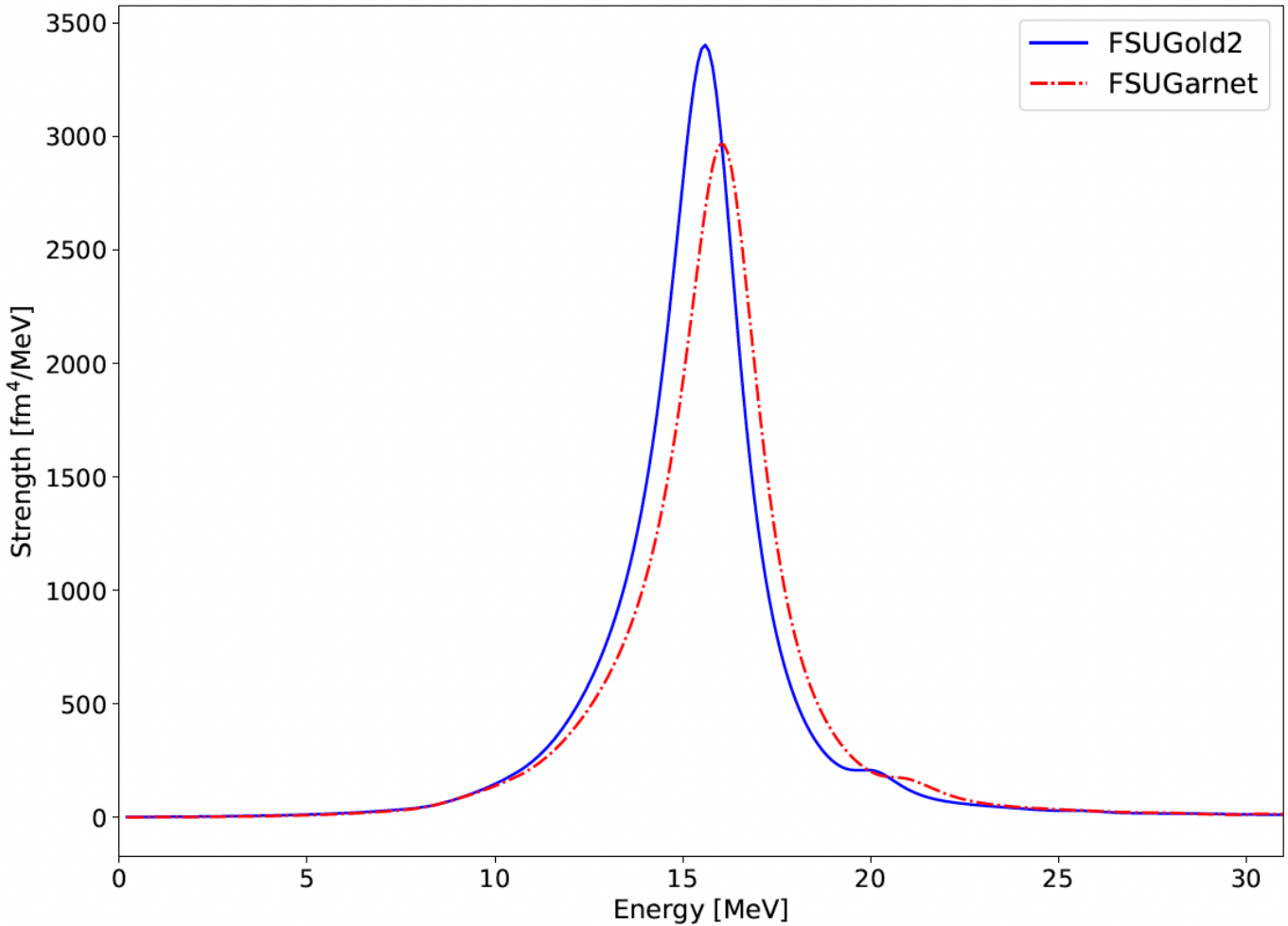
Aims

To investigate:

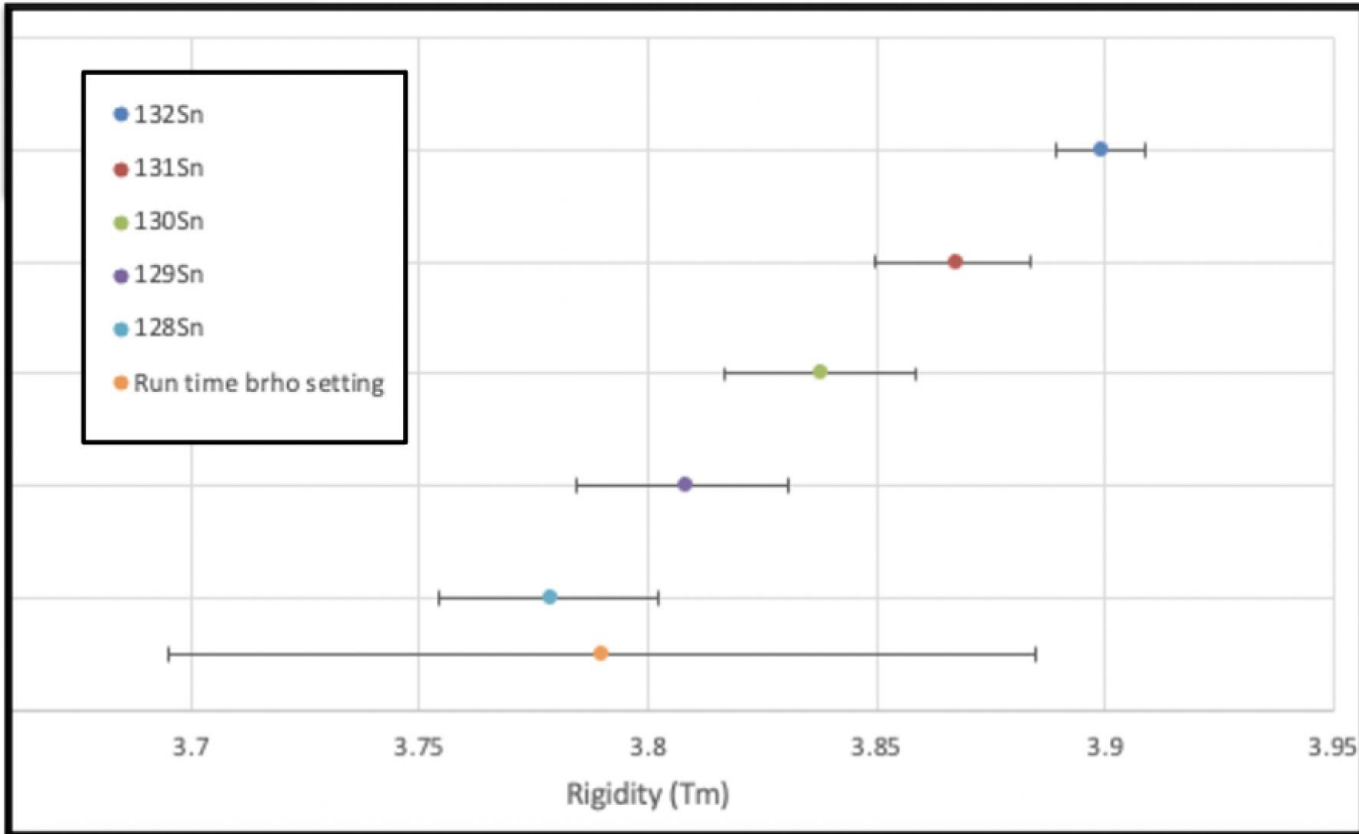
- i) the asymmetry term in the nuclear incompressibility;
- ii) the phenomenon of “softness” of open-shell nuclei as observed in the ISGMR strength distributions in the Sn and Cd nuclei; and,
- iii) to directly test the impact of the recent results from PREX-II on the observed ISGMR strengths in very neutron-rich nuclei.



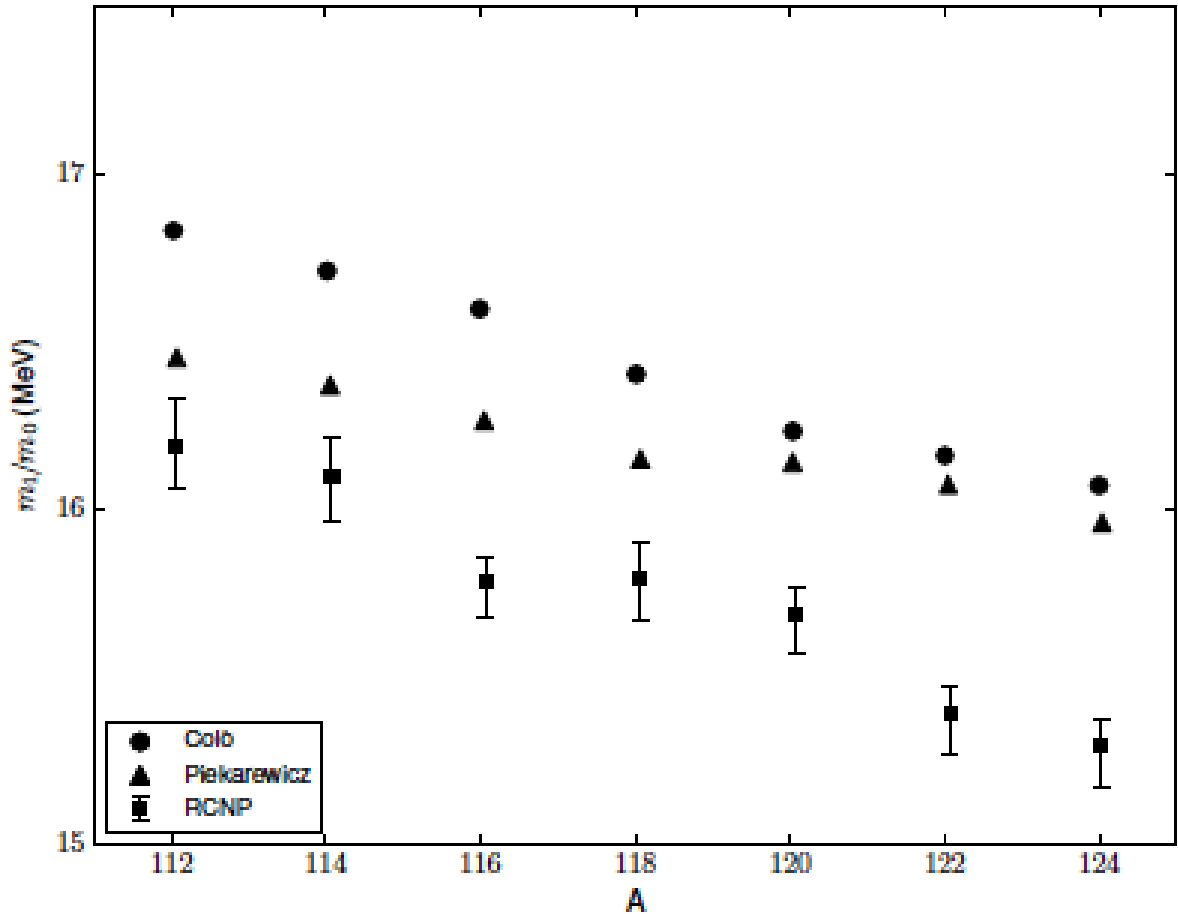
${}^4\text{He}({}^{132}\text{Sn}, {}^{132}\text{Sn}'){}^4\text{He}$ @ FRIB



Calculations courtesy Prof. J. Piekarewicz.



Rigidities of Sn-isotopes and S800 acceptance are shown. The bars for the Sn isotope points represent their expected momentum spread



Why are tins so “Fluffy” ?

T. Li *et al.*, Phys. Rev. Lett. **99**, 162503 (2007)

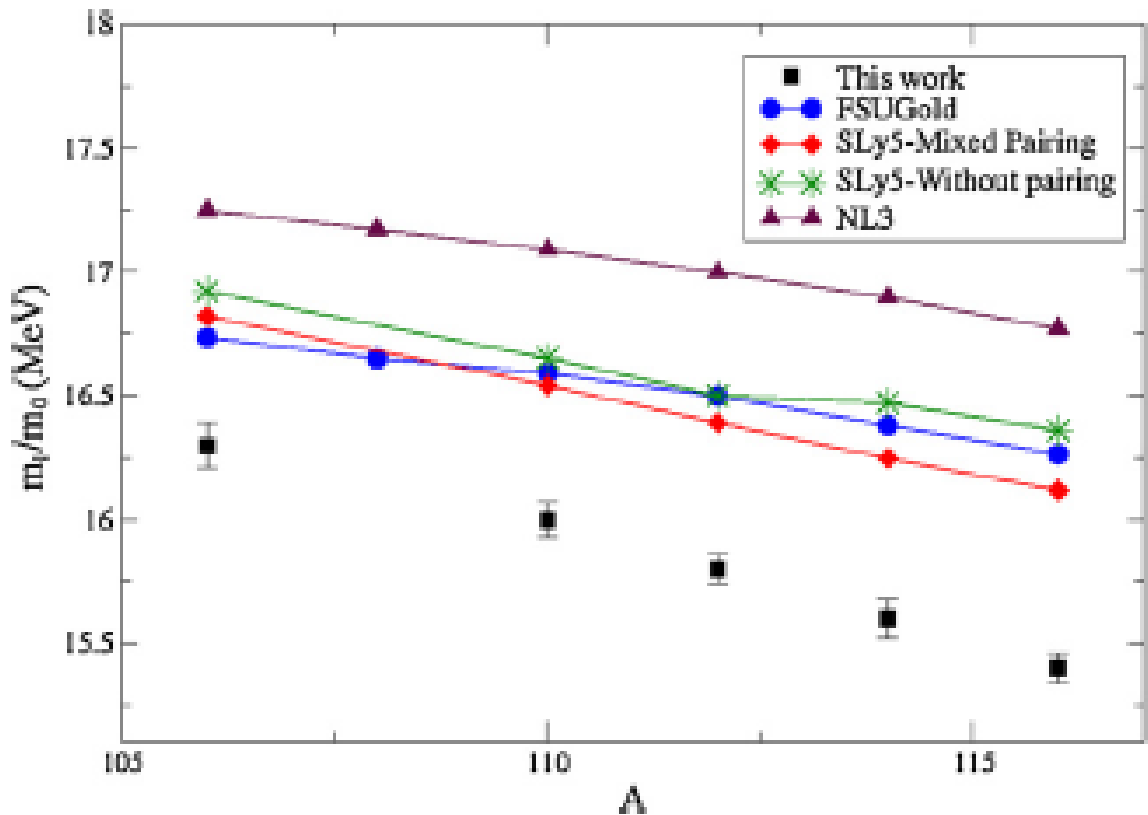
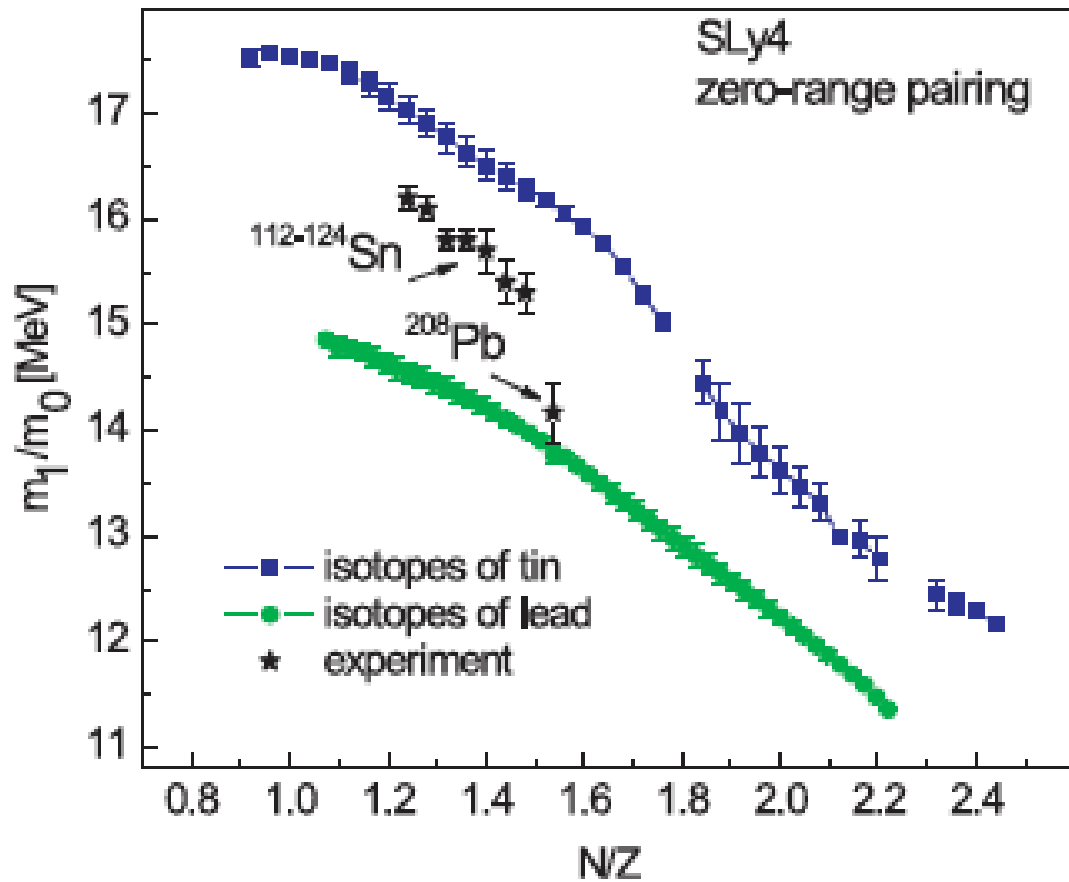
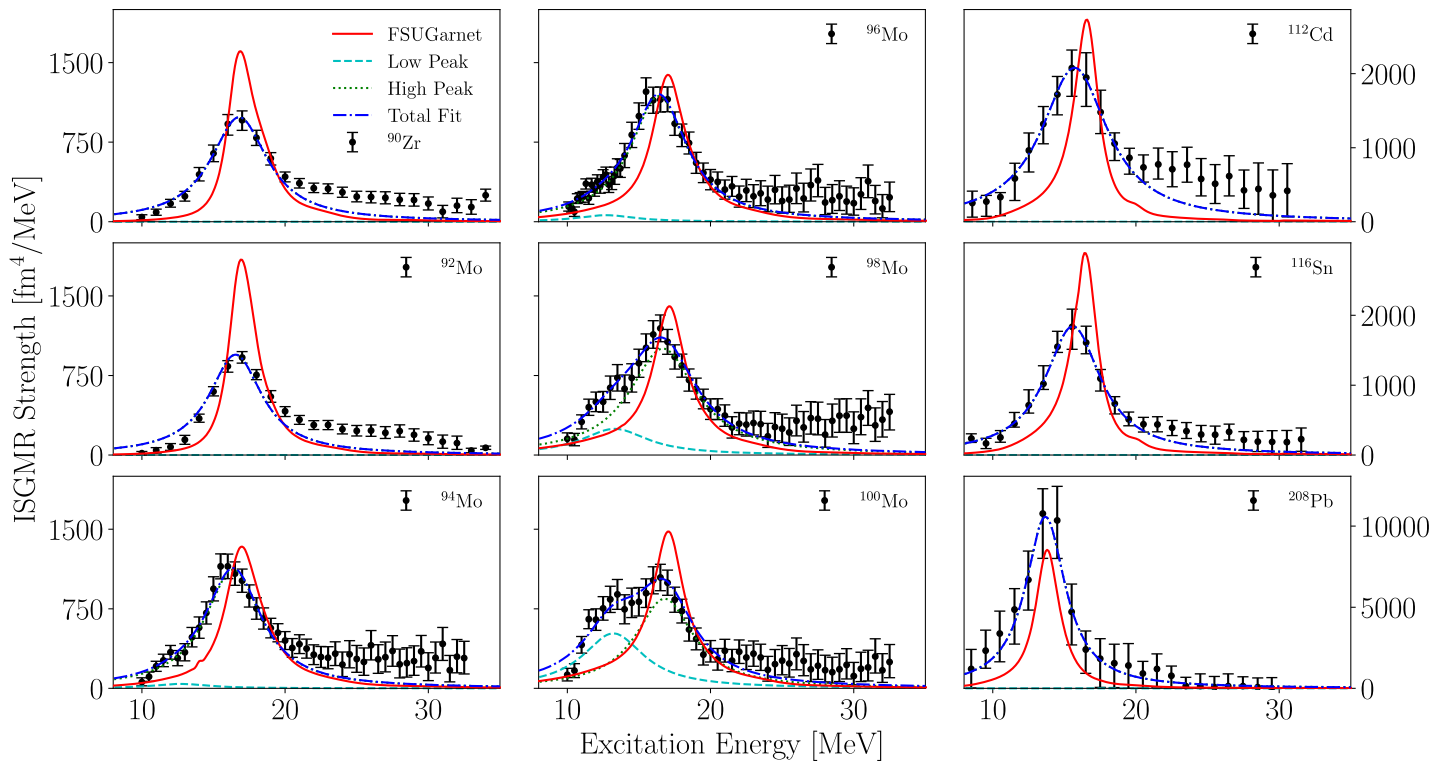
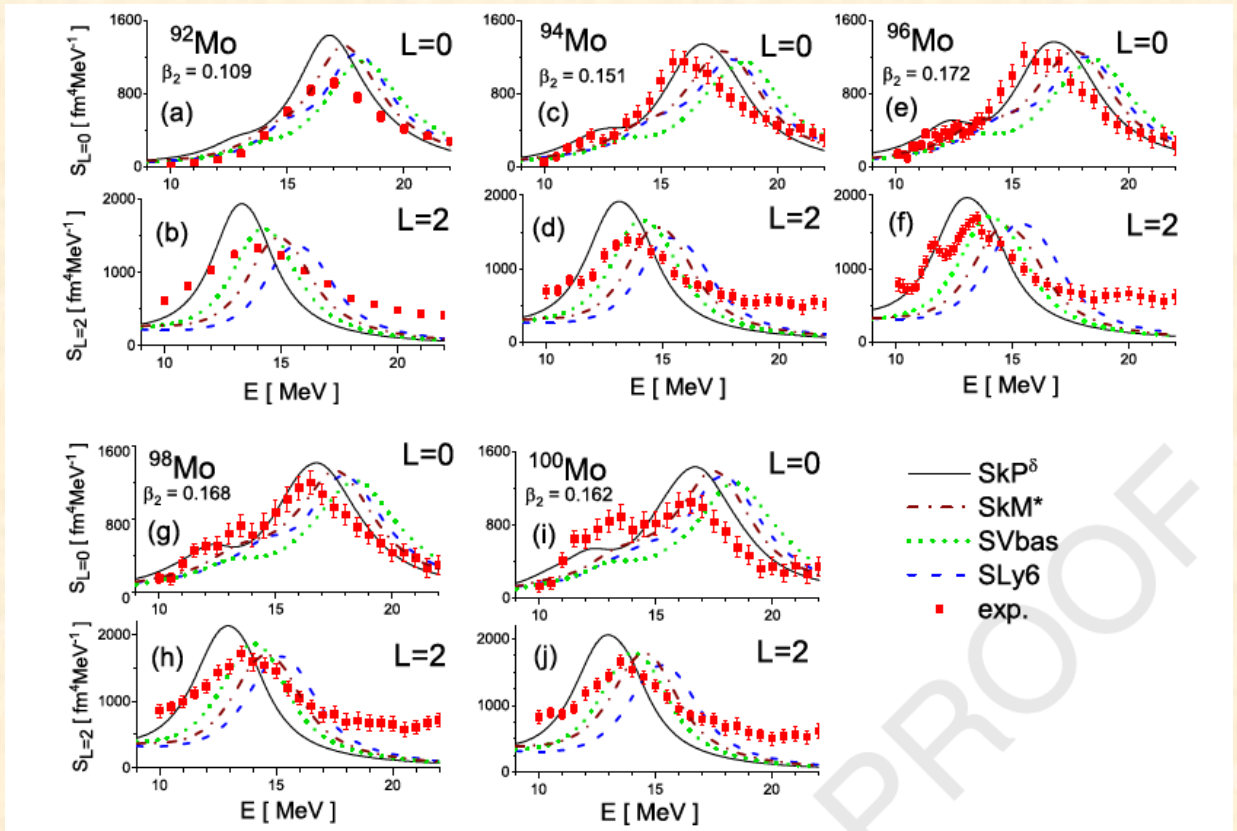


Fig. 3. (Color online.) Systematics of the moment ratio, m_1/m_0 for the ISGMR strength distributions in the Cd isotopes investigated in this work. The experimental results (squares) are compared with relativistic calculations performed using the FSUGold (circles) and NL3 (triangles) effective interactions. Also presented are results from non-relativistic calculations performed using the Sly5 parameter set in the HF-BCS + QRPA formalism with and without the mixed pairing interaction (diamonds and stars, respectively) [36]. The solid lines are to guide the eye.

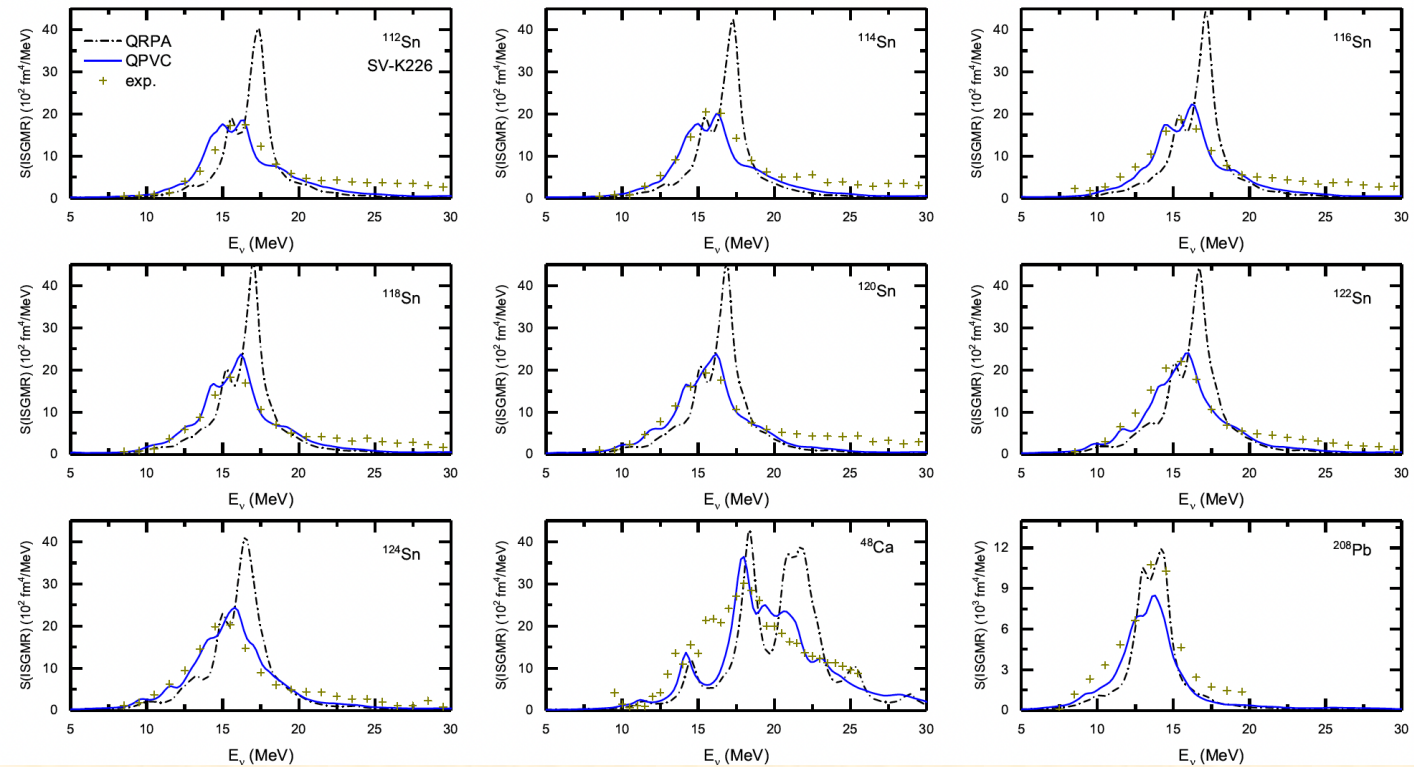




K. B. Howard et al., Phys. Lett. B **807**, 135608 (2020)



the connection between the line shape of the monopole strength ISGMR and the deformation-induced coupling between the ISGMR and the $K = 0$ branch of the ISGQR. The ISGMR is best described by the force SkP^δ , having a low incompressibility $K_\infty = 202$ MeV.



Z. Z. Li, Y. F. Niu, and G. Colo, arXiv:2211.01264v1

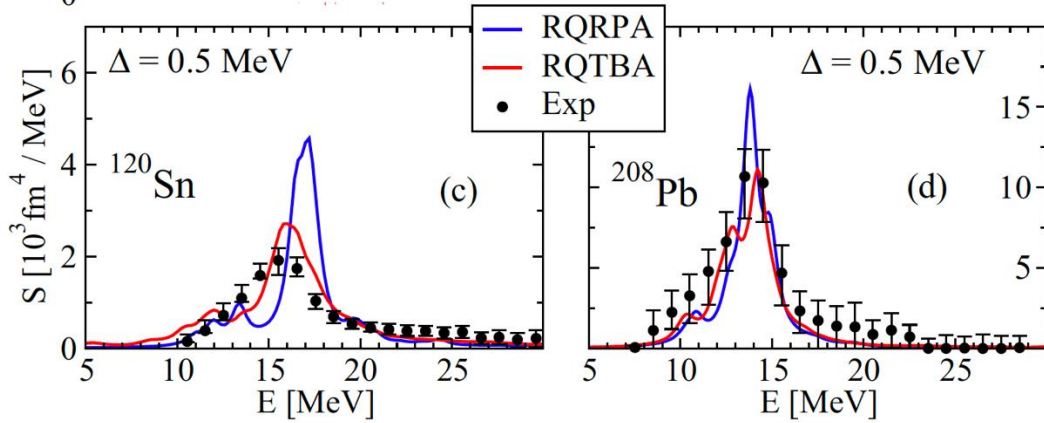
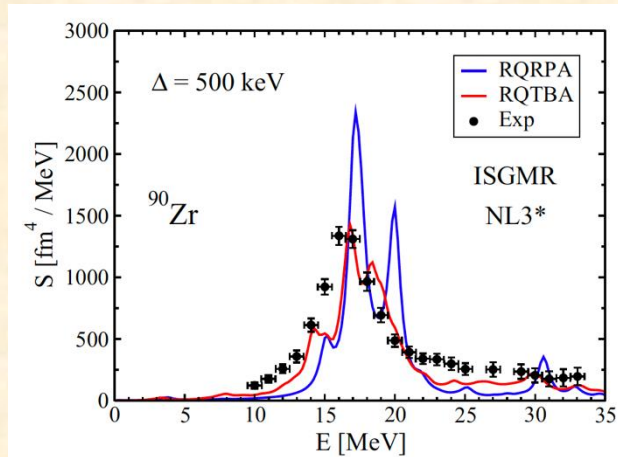


FIG. 1. ISGMR in ^{120}Sn and ^{208}Pb : RQRPA and RQTBA strength distributions compared to experimental data [35] (^{120}Sn) and [1] (^{208}Pb).



Elena Litvinova, Phys. Rev. C **107**, L041302 (2023).



- ◆ We have “experimental” values now for K_{∞} and K_{τ} . There is a lot of room for “improvement” in the latter.
- ◆ We have completed a measurement at NSCL on ^{70}Ni using pure ^4He gas and trigger with S800. Very clean spectra have been observed with a “peak” at ~ 17 MeV consistent with GMR.
- ◆ An experiment to measure ISGMR in ^{132}Sn was approved in the “first round” proposals for FRIB.
- ◆ In the Cd and Sn isotopes, the ISGMR energy was significantly lower than that expected from the accepted value of K_{∞} .
- ◆ The “fluffiness” appears in the Mo isotopes, beginning with ^{92}Mo , just two nucleons out of the “doubly-closed” nucleus ^{90}Zr .
- ◆ Until very recently, there had been no satisfactory theoretical explanation of this “fluffiness” of open-shell nuclei.

MAYBE, Now there is!



Merci

धन्यवाद

Thanks!





The Question Kitten