

Isospin properties and pair correlations in 88Ru

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Phases of (macroscopic) matter - phase transitions

PHYSICAL REVIEW

Letters to the Editor

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Bound Electron Pairs in a Degenerate Fermi Gas*

LEON N. COOPER

Physics Department, University of Illinois, Urbana, Illinois (Received September 21, 1956)

 \mathbf{T} T has been proposed that a metal would display I superconducting properties at low temperatures if the one-electron energy spectrum had a volume-independent energy gap of order $\Delta \simeq kT_c$, between the ground state and the first excited state.^{1,2} We should like to point out how, primarily as a result of the exclusion principle, such a situation could arise.

Consider a pair of electrons which interact above a quiescent Fermi sphere with an interaction of the kind that might be expected due to the phonon and the screened Coulomb fields. If there is a net attraction between the electrons, it turns out that they can form a bound state, though their total energy is larger than zero. The properties of a noninteracting system of such

 $=(1/V) \exp[i(\mathbf{k}_1 \cdot \mathbf{r}_1 + \mathbf{k}_2 \cdot \mathbf{r}_2)]$ which satisfy periodic boundary conditions in a box of volume V , and where r_1 and r_2 are the coordinates of electron one and electron two. (One can use antisymmetric functions and obtain essentially the same results, but alternatively we can choose the electrons of opposite spin.) Defining relative and center-of-mass coordinates, $\mathbf{R} = \frac{1}{2}(\mathbf{r}_1 + \mathbf{r}_2)$, $\mathbf{r} = (\mathbf{r}_2 - \mathbf{r}_1), \mathbf{K} = (\mathbf{k}_1 + \mathbf{k}_2)$ and $\mathbf{k} = \frac{1}{2}(\mathbf{k}_2 - \mathbf{k}_1)$, and letting $\mathcal{E}_K + \epsilon_k = (\hbar^2/m)(\frac{1}{4}K^2 + k^2)$, the Schrödinger equation can be written

$$
\begin{array}{l}\n(\mathcal{E}_K + \epsilon_k - E) a_k + \sum_{k'} a_{k'}(\mathbf{k} | H_1 | \mathbf{k'}) \\
\times \delta(\mathbf{K} - \mathbf{K'}) / \delta(0) = 0\n\end{array} (1)
$$

where

$$
\Psi(\mathbf{R}, \mathbf{r}) = (1/\sqrt{V})e^{i\mathbf{K} \cdot \mathbf{R}} \chi(\mathbf{r}, K),
$$

\n
$$
\chi(\mathbf{r}, K) = \sum_{k} (a_k/\sqrt{V})e^{i\mathbf{k} \cdot \mathbf{r}},
$$
\n(2)

and

$$
(\mathbf{k} | H_1 | \mathbf{k}') = \left(\frac{1}{V} \int d\mathbf{r} e^{-i\mathbf{k} \cdot \mathbf{r}} H_1 e^{i\mathbf{k}' \cdot \mathbf{r}}\right)_{0 \text{ phonons}}
$$

We have assumed translational invariance in the metal. The summation over k' is limited by the exclusion principle to values of k_1 and k_2 larger than q_0 , and by the delta function, which guarantees the conservation of the total momentum of the pair in a single scattering. The K dependence enters through the latter restriction.

Bardeen and Pines³ and Fröhlich⁴ have derived approximate formulas for the matrix element $(\mathbf{k} | H_1 | \mathbf{k}')$; it is thought that the matrix elements for which the two electrons are confined to a thin energy shell near the Fermi surface, $\epsilon_1 \simeq \epsilon_2 \simeq \epsilon_F$, are the principal ones

Can we observe something similar in atomic nuclei?

THE

PHYSICAL REVIEW

 $\mathcal A$ journal of experimental and theoretical physics established by E. L. Nichols in 1893

SECOND SERIES, VOL. 114, No. 6

JUNE 15, 1959

Possible Superfluidity of a System of Strongly Interacting Fermions*†

L. N. COOPER.[†] R. L. MILLS, AND A. M. SESSLER The Ohio State University, Columbus, Ohio (Received January 30, 1959)

The possible superfluidity of a system of strongly interacting fermions is investigated on the assumption that an adequate description of the system in its "normal" state is given by independent fermions in a momentum-dependent potential. On the basis of this assumption we have investigated whether a correlated wave function of the form used by Bardeen, Cooper, and Schrieffer minimizes the ground-state energy. The nonzero terms in the expectation value of the Hamiltonian contain the modified kinetic energy and the full two-body potential between the fermion pairs. An integral equation is obtained in configuration space for the correlation function between pairs. This integral equation is meaningful even for potentials with hard cores, and a nonzero solution implies the existence of a superfluid state. A variational method is devised which provides a criterion for superfluidity and a lower bound for the transition temperature into the superfluid state. We find that a repulsive hard core does not in principle forbid the existence of a superfluid state, but whereas in the absence of a hard core an attractive two-body potential always leads to a superfluid state at sufficiently low temperatures, in the presence of a repulsive core there appears to be a critical strength of attraction needed to form a superfluid state. When the variational principle is applied to liquid He³ or to nuclear matter, it is found for a wide class of trial functions that the system does not become a superfluid.

I. INTRODUCTION

THE fact that a system of fermions can become a superfluid is demonstrated by the observed behavior of the electron gas in many metals at low temperatures. It seems natural then to inquire whether or not other systems of fermions might display similar properties, and what the criterion for such behavior would be. This question is of particular interest because of recent conjectures¹ that nuclear matter might be superfluid in the sense that for an infinite medium there would be an energy gap between the ground state and the lowest single particle excitations. It has been further conjectured that this might show up for a finite nucleus as the explanation for the abnormally large singleparticle excitation energy of even-even nuclei. Whether or not He³, the other well-known Fermi fluid, has a superfluid phase at low temperatures has been a matter of concern since the discovery of the λ transition in He⁴ and London's conjecture² that Bose statistics are crucial to the formation of the superfluid phase.

We have attempted to treat this question by taking over to an arbitrary system of fermions what appears to have worked very well for the electron gas. There the introduction of pair correlations into the wave function and the approximation that only pairs of given total spin and total momentum are strongly correlated was sufficient to account for the observed properties of the superconducting phase. In making this same assumption for an arbitrary system of fermions we have had to assume that in some sense the "normal" fluid could be described in an uncorrelated approximation. The situation in this regard, for a fermion system such as the nucleus, is much less clear than the corresponding situation in a metal where the lattice plays such a dominant rôle.

This basic conjecture of our procedure, the description of the normal fluid as a Fermi gas in a momentumdependent potential, is discussed in Sec. II. In the third

^{*} Supported in part by the National Science Foundation.

[†] A preliminary account of this work was presented at the Kamerlingh-Onnes Conference on Low-Temperature Physics, Leiden, Netherlands, June, 1958 (Suppl. Physica 24, September, 1958).

İ Present address: Brown University, Providence, Rhode **Island** ¹ Bohr, Mottelson, and Pines, Phys. Rev. 110, 936 (1958);

C. De Dominicis and P. C. Martin, Bull. Am. Phys. Soc. Ser. II, 3, 224 (1958).

² F. London, Nature 163, 694 (1949).

PHYSICAL REVIEW C, VOLUME 63, 044309

Thermal and electromagnetic properties of 166Er and 167Er

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Frank Laboratory of Neutron Physics, Joint Institute of Nuclear Research, RU-141980 Dubna, Moscow region, Russia (Received 30 October 2000; published 6 March 2001)

The primary γ -ray spectra of ¹⁶⁶Er and ¹⁶⁷Er are deduced from the (³He, $\alpha \gamma$) reaction and the (³He,³He' γ) reaction, respectively, enabling a simultaneous extraction of the level density and the γ -ray-strength function. Entropy, temperature, and heat capacity are deduced from the level density within the microcanonical and canonical ensembles, displaying signals of a phaselike transition from the pair-correlated ground state to an uncorrelated state at $T_c \sim 0.5$ MeV. The γ -ray-strength function displays a bump around $E_{\gamma} \sim 3$ MeV, interpreted as the pygmy resonance.

NN2024 Whistler, BC CA / BC t_{M} and α α

PRL 117, 132501 (2016)

 Γ at Γ atomic nuclei Γ Exotic phases of nuclear matter Quartetting and α -particle condensation

P Selected for a Viewpoint in *Physics* PHYSICAL REVIEW LETTERS

week ending
23 SEPTEMBER 2016

\mathcal{G}

Nuclear Binding Near a Quantum Phase Transition

Serdar Elhatisari,¹ Ning Li,² Alexander Rokash,³ Jose Manuel Alarcón,¹ Dechuan Du,² Nico Klein,¹ Bing-nan Lu,² Ulf-G. Meißner,^{1,2,4} Evgeny Epelbaum,³ Hermann Krebs,³ Timo A. Lähde,² Dean Lee,⁵ and Gautam Rupak⁶

Isospin NN pairing modes (a unique possibility for nuclei due to the coupling of two Fermi liquids)

Isoscalar paired phase in 92Pd? B. Cederwall et al., Nature (London) 469, 68 (2011)

Theory predictions for neutron-proton pairing
in the heaviest $N \sim Z$ nuclei

A. L. Goodman , PRC 60, 014311 (1999) – HFB studies of ground states of e-e A = 76-96, N = Z nuclei

"Isocranking": The isoscalar (np) pair gap is predicted to increase sharply as $N \rightarrow Z$

Similarly to a magnetic field on a superconductor, the rotational motion of a deformed nucleus counteracts the isovector-coupled $(I=0)$ superfluid phase by breaking time-reversed nn or pp pairs. (Coriolis anti-pairing effect)

Isospin-generalized HFB theory *J*"*Jmax*"2 *j*, where *j* is the nucleon spin. Figure 9 shows

" $T = 0$ and $T = 1$ pairing in rotational states of the $N = Z$ nucleus ${}^{80}Zr"$ A. L. Goodman, PRC 63, 044325 (2001)

FIG. 1. Energies of the rotational bands versus the spin *I*.

procedure. On each iteration *h* and ! are calculated from the

FIG. 9. Angular momentum components of the pair potential $\Delta_{J,T=0}$ for the *T*=0 pair band.

density matrix " and the pairing tensor *t*, respectively; then " \vert \vert \vert \vert \vert \vert \vert pairing is <u>suppressed</u> by the Coriolis (\vert The T=0 coupling is less affected by the *Coriolis* anti-pairing effect and will still be successive iterations. It is a model space contained space $\frac{1}{2}$ or $\frac{1}{$ active and could become dominant as I increases lated up to spin *I*!26). At high spins, the *T*!1 pair band T=1 pairing is suppressed by the Coriolis effect in high-spin states tween spins *I*!8 and *I*!14. The spin *I*!10,12 states have $\frac{1}{\sqrt{1-\frac{1$ The T=0 coupling is less affected by the Coriolis anti-pairing effect and will still be

 $\overline{1}$

Neutron-proton pairing in $N \approx Z$ nuclei - experimental probes

- Masses binding energies in e-e and o-o nuclei indicate that **T=1** *np* **pairing** is dominant, no evidence for a T=0 (deuteron-like) pair condensate **up to around A≈60. Need for accurate mass measurements in heavier N=Z systems**
- np (deuteron) pair transfer reactions
- GT Beta decay strengths
- Other radioactive decay modes: (alpha) proton???

Probe ground-state or low-spin correlations

- Spectral properties of spherical N=Z nuclei near closed shells –deviations from classical s.p. behavior (e.g. ^{92}Pd – isoscalar spin-aligned coupling scheme*)
- **Rotational properties of deformed nuclei**

We know the isoscalar effective NN interaction is strongly attractive but can it produce a correlated np pairing condensate?

- B. Cederwall et al., Nature (London) 469, 68 (2011)
- S. Frauendorf and A. Macchiavelli, Prog. Part. Nucl. Phys. 78, 24 (2014) NN2024 Whistler, BC CA / BC

Note: The "Backbending" effect (A. Johnson et al., 1971) is not a complete phase transition. In the finite nuclear system the paired and unpaired phases are mixed after the first alignment ("Stockholm, S-band") (F.S. Stephens and R.S. Simon, 1972).

A. Johnson, H. Ryde, and J. Sztarkier, Phys. Lett. B34, 605 (1971)

- A. Johnson, H. Ryde, S. A. Hjorth, Nuc. Phys. A179, 753 (1972)
- F. S. Stephens and R. S. Simon. Nuc. Phys. A183, 257 (1972)
- R. Wyss & M. A. Riley, Fifty Years of Backbending, Nuclear Physics News, 32:2, 16-20 (2022) $_{NN2024}$ Whistler, BC CA / BC

Experiment

Beam: 36Ar (115 MeV, 5 ~ 10 pnA) Target: 54Fe (99.58%, 6 mg/cm2) Main contaminations: 16O from oxidation, 56Fe (0.40%) Fusion-evaporation reactions of interest: 36Ar(54Fe, 2n)88Ru 36Ar(54Fe, 2n1p)87Tc

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Experimental Setup

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AGATA

- 34 AGATA crystals (out of 180)
- $\sim 0.8\pi$ Coverage
- E, T, Position (x, y, z)
- Trigger: YY-n

Basic ingredients of γ-ray tracking

Pulse shape analysis – spatial resolution of 2-5 mm

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C1

Forward Tracking of Compton Scattering Events

Wn contains physics of Compton scattering vertex and empiric factors

Find χ^2 for the N! permutations **of the interaction points 0123 0132 0231 0213 0312 0321** Accept permutation with smallest χ^2 if **this is below a predefined value 0.01 0.1 1 10 100 0 24 48 72 96 120** χ^2 **Permutation number** How it works for two 5-point events

PROBLEMS : **Position resolution, Short range scattering, Compton profile**

DIAMANT charged particle array

- **60 CsI(Tl) Detectors**
- $\sim 2\pi$ Coverage
- **E, T, PID**
- **Slave Mode**
- $\epsilon_p \sim 40\%, \epsilon_{\alpha} \sim 25\%$

NEDA & NWall

- Organic liquid scintillator cells
- 54 NEDA & 14 NWall
- $\sim 1.6 \pi$ Coverage
- Pulse Shape
- Trigger: γγ-*n* (neutron-like)

Volts

Neutron-*γ* **Discrimination**

Results: yrast band in 88Ru

Taken from B. Cederwall et al, PRL 124 062501 (2020)

B. Cederwall et al, PRL 124 062501 (2020)

Strutinsky-type PES calculations * with standard isovector pairing (total Routhian surface (TRS) approach)

Note: do not produce deformed ground-state shape

(but pronounced superdeformed minimum appears already at zero rot. frequency!)

* W. Nazarewicz, R. Wyss, A. Johnson, Nuclear Physics A 503(2), 285 (1989)

LSSM predictions for 88Ru with interaction including an explicit pairing term (PMMU) $H = H_0 + H_P + H_M + H_m^{MU}$.

PMMU: $H = H_0 + H_P + H_M + H_m$:

 $H_o = s.p$, $H_P = pairing$ H_M = multipole, contains $QQ + OO$ components H_m = monopole term

$$
H_0 = \sum_{\alpha} \varepsilon_a c_{\alpha}^{\dagger} c_{\alpha}, \quad H_P = -\sum_{J=0,2} \frac{1}{2} g_J \sum_{MK} P_{JM1\kappa}^{\dagger} P_{JM1\kappa}
$$

components
$$
H_M = -\frac{1}{2} \chi_2 \sum_{M} : Q_{2M}^{\dagger} Q_{2M} : -\frac{1}{2} \chi_3 \sum_{M} : O_{3M}^{\dagger} O_{3M} :
$$

$$
H_m^{MU} = \sum_{a \le b, T} V_m^{MU}(ab, T) \sum_{JMK} A_{JMTK}^{\dagger}(ab) A_{JMTK}(ab),
$$

K. Kaneko, T. Mizusaki, Y. Sun, and S. Tazaki, Phys. Rev. C89, 011302(R) (2014) Kaneko, Sun and de Angelis, Nuclear Physics A957, 144-153 (2017)

F Without the $T = 0$ *np* pairing the sq experiment and $\iota = \nu \eta p$ pairing, the si t and behaviour as for $90,92R_H$ **OO** m_{max} sented m_{max} comparison. a_1 a_2 a_3 a_4 a_5 a_7 a_8 **1**, a_7 a_8 **1**, a_9 oth pattern in ⁸⁶Ku disappears and it rotational behaviour as for $\rm{^{90,92}Ru}$. QQ np T=0 is most important in $\rm{^{88}Ru}$. $F_{\rm 1D}$ online online 88 R₁₁ disame are and it **Note:** Without the $T = 0$ *np* pairing, the smooth pattern in ⁸⁸Ru disappears and it lacks *VM*(*ab,T* = 0) indicates large deviations from the full calculation. The dominant contribution of the multipole *T* = 0 part

LSSM calculations: T=0 correlations drive collectivity

Extension of the ground state $(\pi g_{9/2})$ band and new oblate band in the $T_z=1/2$ nucleus ⁸⁷Tc

Pairing isospin modes in deformed N~Z nuclei at intermediate angular momentum – odd-even vs even-even

B. Cederwall et al, PRL 124 062501 (2020) X. Liu et al, PRC 104 L021302 (2021)

Shell model calculation for ⁸⁷Tc (T_Z=1/2) – effect of spin-aligned np pairs (V_{np})

Odd-mass $N \sim Z$ (T_z=1/2) nuclei:

- Odd valence particle contributes constructively to isoscalr np pairing correlations "spin-dependent effective 3-N" interaction as opposed to "blocking" effect in pure isovector case?
- Increase of structural difference between 1qp and 3qp configuration reduces interaction strength in the band crossing?

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Experiment

54

The Contract of the Contract

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Letter Open Access

Evidence for enhanced neutron-proton correlations from the level
structure of the $N = Z + 1$ nucleus ${}^{87}_{43}\text{Tc}_{44}$

X. Liu et al. Phys. Rev. C 104, L021302 - Published 20 August 2021

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covering nuclear physics

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Evidence for spherical-oblate shape coexistence in ⁸⁷Tc

X. Liu et al. Phys. Rev. C 106, 034304 - Published 9 September 2022

 $|y|$ $|z|$ $<$ More

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PHYSICAL REVIEW LETTERS

Accepted Paper

Isospin properties of nuclear pair correlations from the level structure of the self-conjugate nucleus ⁸⁸Ru Phys. Rev. Lett.

B. Cederwall et al.

Accepted 18 December 2019

- Intermediate-angular momentum states in the heaviest deformed $N \sim Z$ nuclei $88Ru$ and $87Tc$ have been observed with AGATA + ancillary detectors (NEDA/NWALL, DIAMANT)
- In ⁸⁸Ru, the rotational frequency for the configuration change between the ground-state and qp-aligned structures indicates a "delay" wrt standard calculations and expt data in neighboring Tz=1 isotones, in agreement with theoretical predictions for enhanced isoscalar np correlations.
- For, the $T_{Z}=1/2$ isotone, ⁸⁷Tc, we observe an earlier band crossing frequency compared with the neighboring N=44 and N=43 odd-mass nuclei for the yrast band built on the $\pi g_{9/2}$ ground state
- ∴ IV band crossing frequencies show opposite behavior as $T_Z \rightarrow 0$ for ee and oe systems - a new signature for enhanced IS pair correlations in these N~Z systems?

Thanks to AGATA collaboration, GANIL, NEDA, DIAMANT teams!

Thank You

Backup

PHYSICAL REVIEW C 69, 034317 (2004)

Transition from the seniority regime to collective motion

J. J. Ressler,¹ R. F. Casten,¹ N. V. Zamfir,¹ C. W. Beausang,¹ R B. Cakirli,^{1,2} H. Ai,¹ H. Annro,¹ M. A. Caprio,¹ A. A. Hecht,¹ A. Heinz,¹ S. D. Langdown,^{1,3} E. A. McCutchan,¹ D. A. Meyer,¹ C. Pl ¹Wright Nuclear Structure Laboratory, Yale University, New Haven, Connecticut 06520-8124, USA 2 Istanbul University, 34459 Vezneciler-Istanbul, Turkey ³University of Surrey, Guilford, Surrey GU2 7XH, United Kingdom (Received 17 September 2003; published 15 March 2004)

 $B(E2)$ values from isomeric states near closed shells are discussed in the context of the behavior of seniority conserving transitions induced by even tensor operators. This result provides a signature for the transition from the seniority regime to collective motion that can be of use in identifying shell structure in exotic nuclei.

DOI: 10.1103/PhysRevC.69.034317

PACS number(s): 21.10.Pc, 21.60.Cs, 23.20.Lv, 27.80.+w

NEDA energy vs TOF

Ginzburg-Landau theory

 $\overline{1}$

 $\mathbf 0$

1 $\overline{\circ}$

Atomic nuclei are finite systems!

Control parameter is discrete (particle number, excitation energy etc)

T. Faestermann, M. Górska, and H. Grawe, Prog. Part. Nucl.Phys. 69, 85 (2013)

Evidence for *isovector* np pairing from nuclear charge radius

"Proton-Neutron Pairing Correlations in the Self-Conjugate Nucleus ³⁸*K* Probed via a Direct Measurement of the Isomer Shift" M.L. Bissell et al., PRL 113, 052502 (2014)

GT (beta decay) strengths CT_d \mathcal{N} Δ supermultiplet, with Δ ay) strengths

4 3 6

single level $B(GT)$ and accumulated $B(GT)$ values for the ⁶²Ge to ⁶²Ga β decay. Left panels use the ISM approach using the KB3G interaction and right panels use the OBBA approach using the SI v4 interaction and right panels use the QRPA approach using the SLy4 interaction. Experimental uncertainty corridors are indicated in gray. FIG. 4 (color online). Experimental (black) and calculated (red)

"Search for a new kind of superfluidity built on collective proton-neutron pairs with aligned spin is performed studying the Gamow-Teller decay of the $T = 1$, $J^{\pi} = 0^{+}$ ground state of ⁶²Ge into excited states of the odd-odd $N = Z$ nucleus 62 Ga. Individual Gamow-Teller transition strengths agree well with theoretical predictions of the interacting shell model and the quasiparticle random phase approximation. The absence of any sizable low-lying Gamow-Teller strength in the reported betadecay experiment supports the hypothesis of a negligible role of coherent $T = 0$ proton-neutron correlations in ⁶²Ga. " of the levels in bold characters. The levels in the levels in gray. The levels in gray \sim in gray. The levels in gray.

ISSUES:

- 1) Need for (reaction) theory to develop clear predictions
- 2) Will be many years before intense beams of ${}^{80}Zr$, ${}^{84}Mo$, ${}^{88}Ru$, ${}^{92}Pd$ etc are available for such studies
- 3) Only probes ground-state or low-spin correlations

Experimental systematics I vs ω

Upper: Shell model spectra of 92Pd

calculated within the $1p_{3/2}0f_{5/2}1p_{1/2}0g_{9/2}$ space [10] (fpg) and the $1p_{1/2}0g_{9/2}$ space (pg). Lower: B(E2; I \rightarrow I – 2) values in ⁹²Pd calculated within the fpg and pg spaces. The two dashed lines show the predictions of the geometric collective model normalized to the 2^+ ₁ state C.Qi, J.Blomqvist, T.Bäck, B. Cederwall, A. Johnson, R. J. Liotta, and R. Wyss, PRC 84, 021301(R) (2011)

Predictions for 88Ru

"Standard" SM calculations* for ⁸⁸Ru predict similar "alignment" of angular momentum

SM calculations for 87Tc

As yet there is no data that definitively supports the presence of $T=0$ np BCS type pairing condensate, but clear evidence for influence of T=0 np interaction in spherical nuclei.

