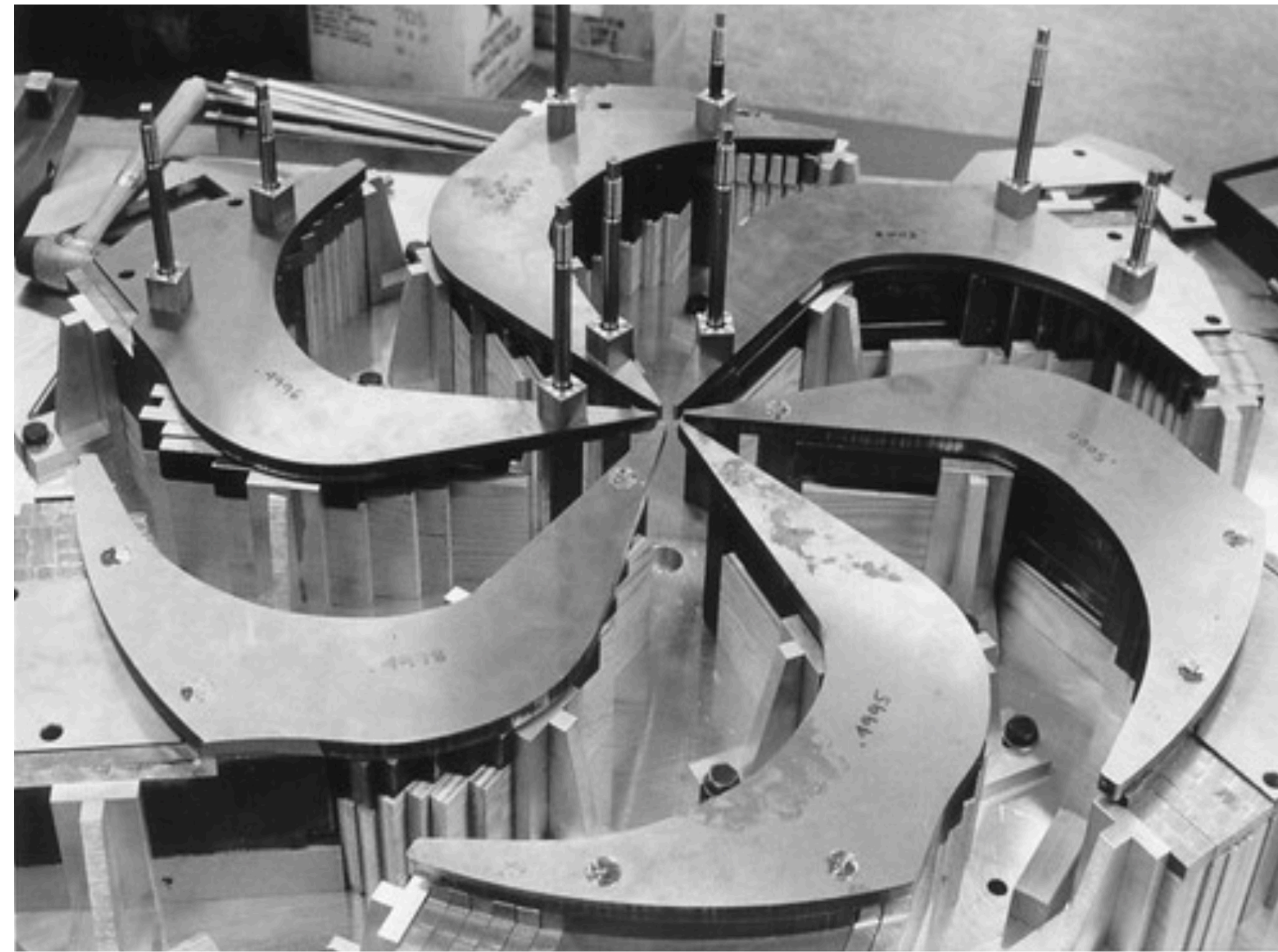


Cosmology of Dirac Neutrino Mass Models



 **TRIUMF**

Canada's particle accelerator centre
Centre canadien d'accélération des particules

Michael Shamma (He/They)
mshamma@triumf.ca

Neutrinos in Astrophysics and Cosmology
March 2024

Outline

- What we don't know about neutrinos
- It's really tough to produce and detect Dirac ν
- Example Dirac ν models which contribute detectably to ΔN_{eff}
- Terrestrial and cosmological ν probes
 - Correlating terrestrial and cosmological ν measurements
- Neutrinos in the bulk

Majorana or Dirac?

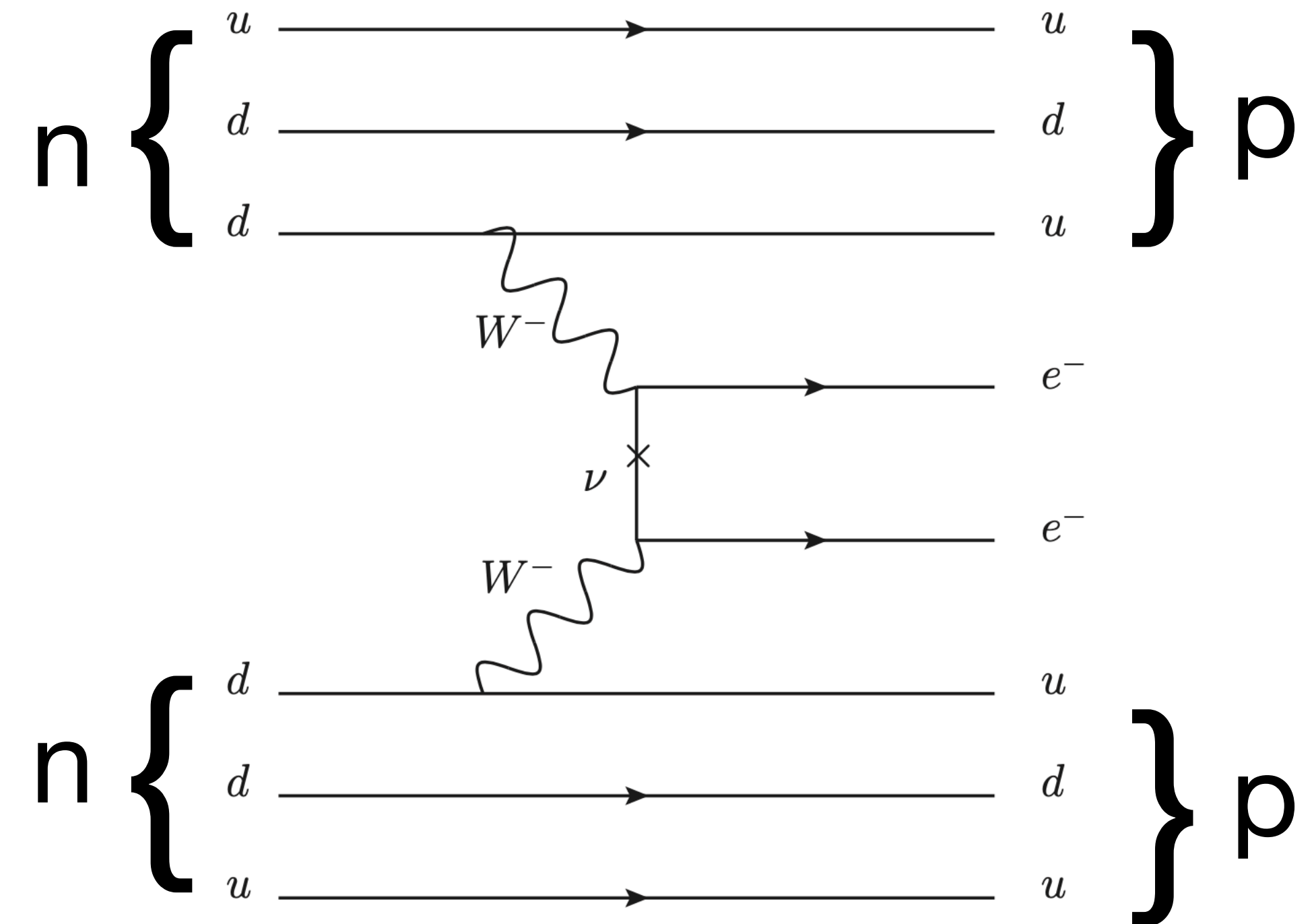
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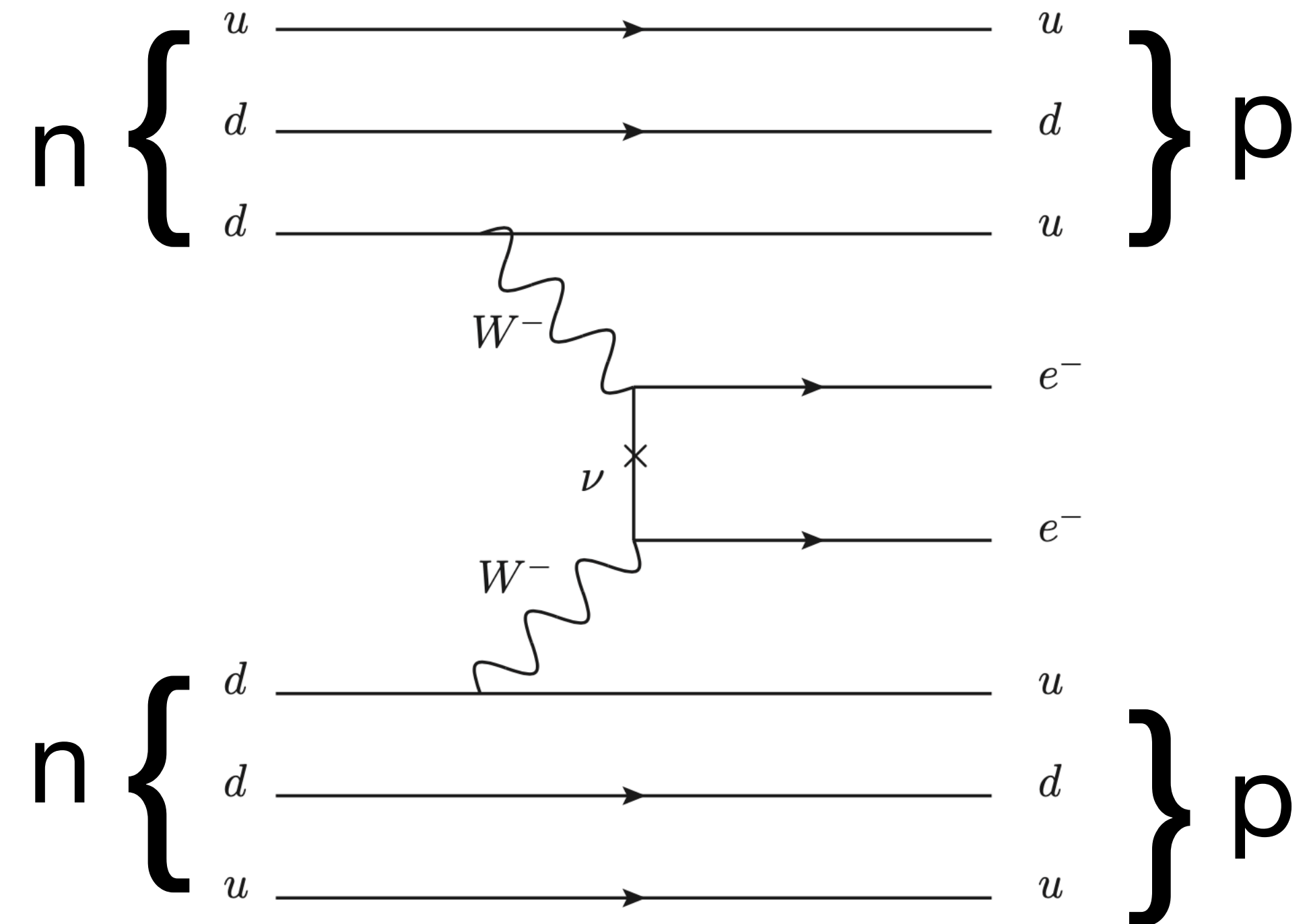
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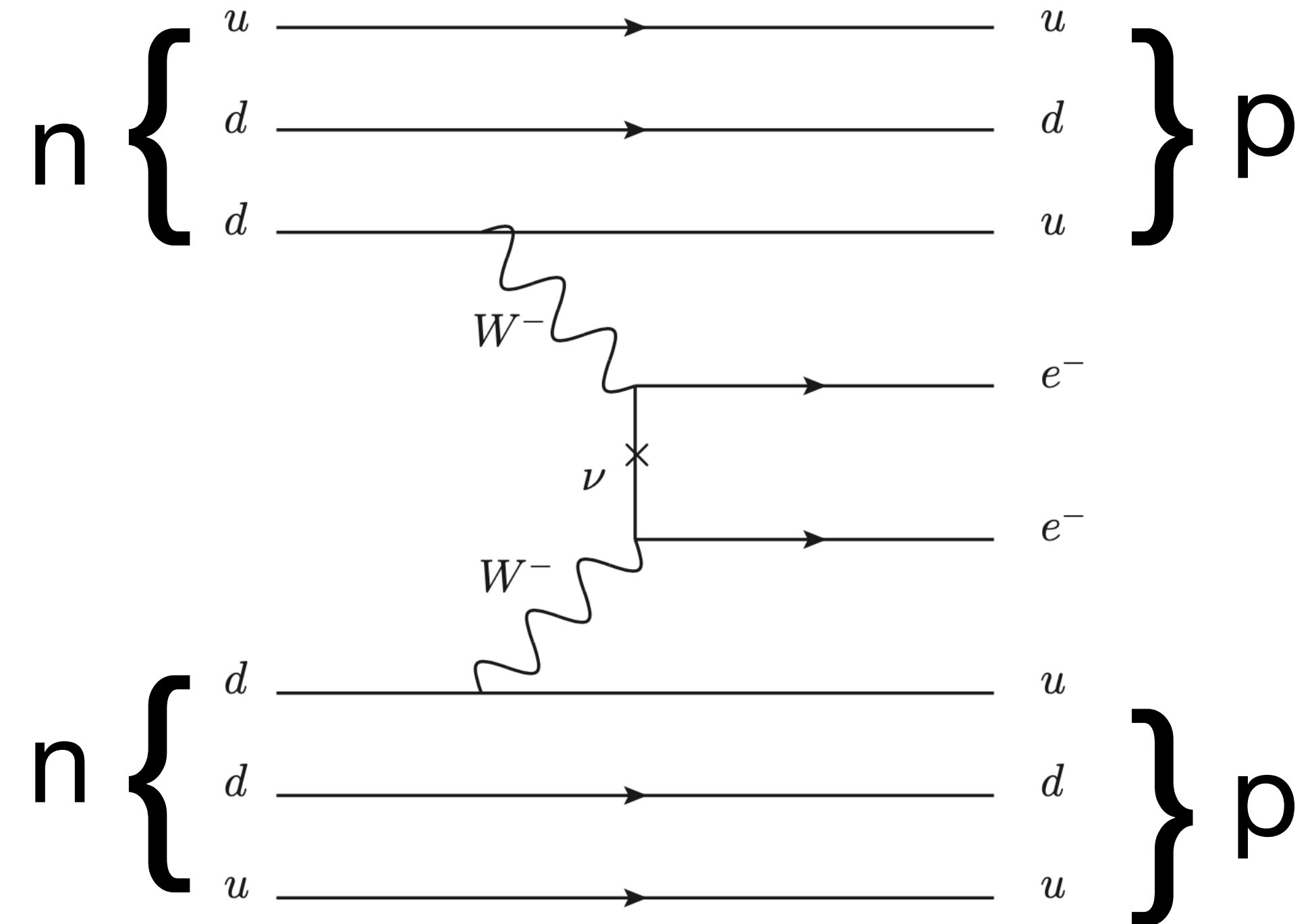
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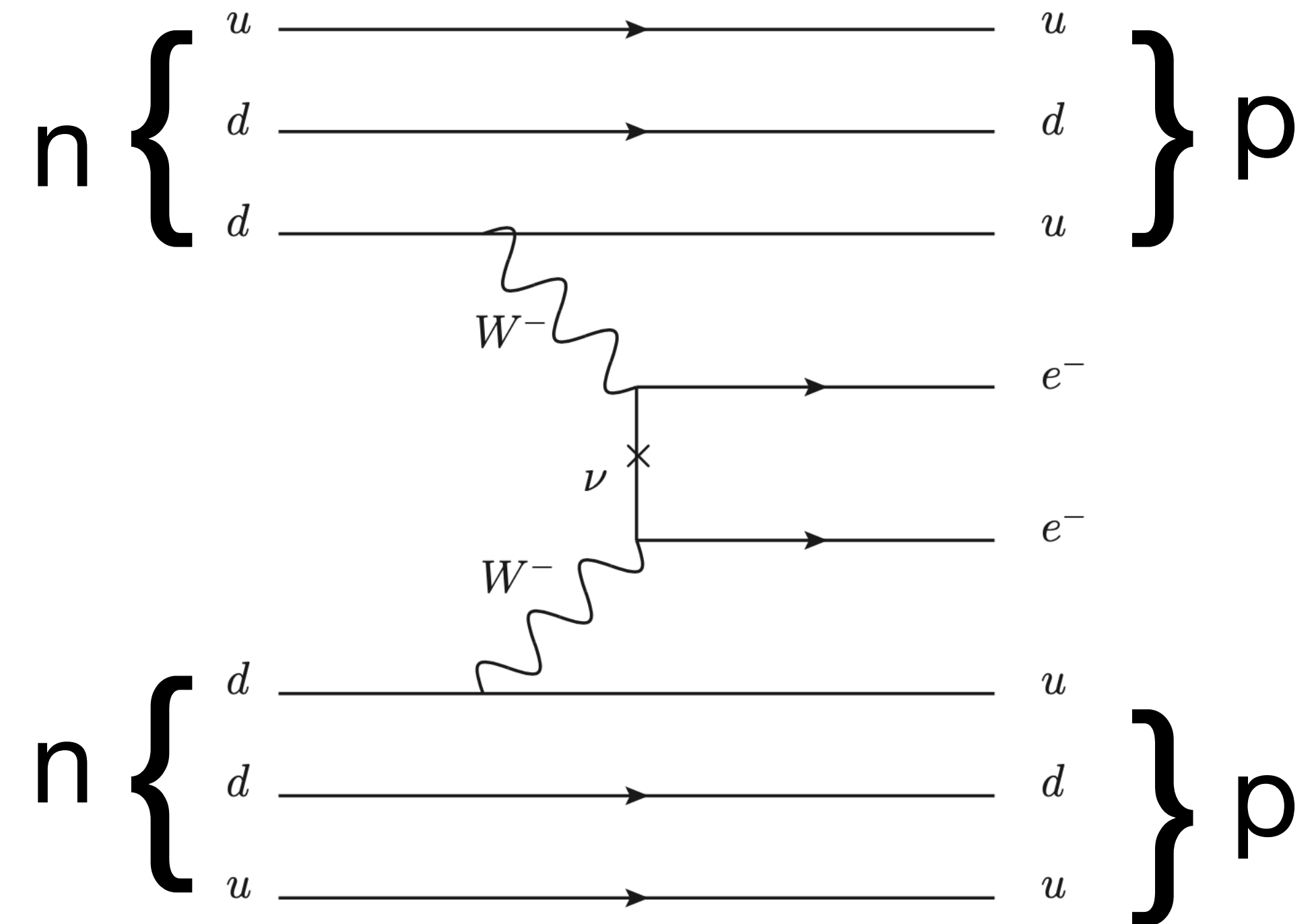
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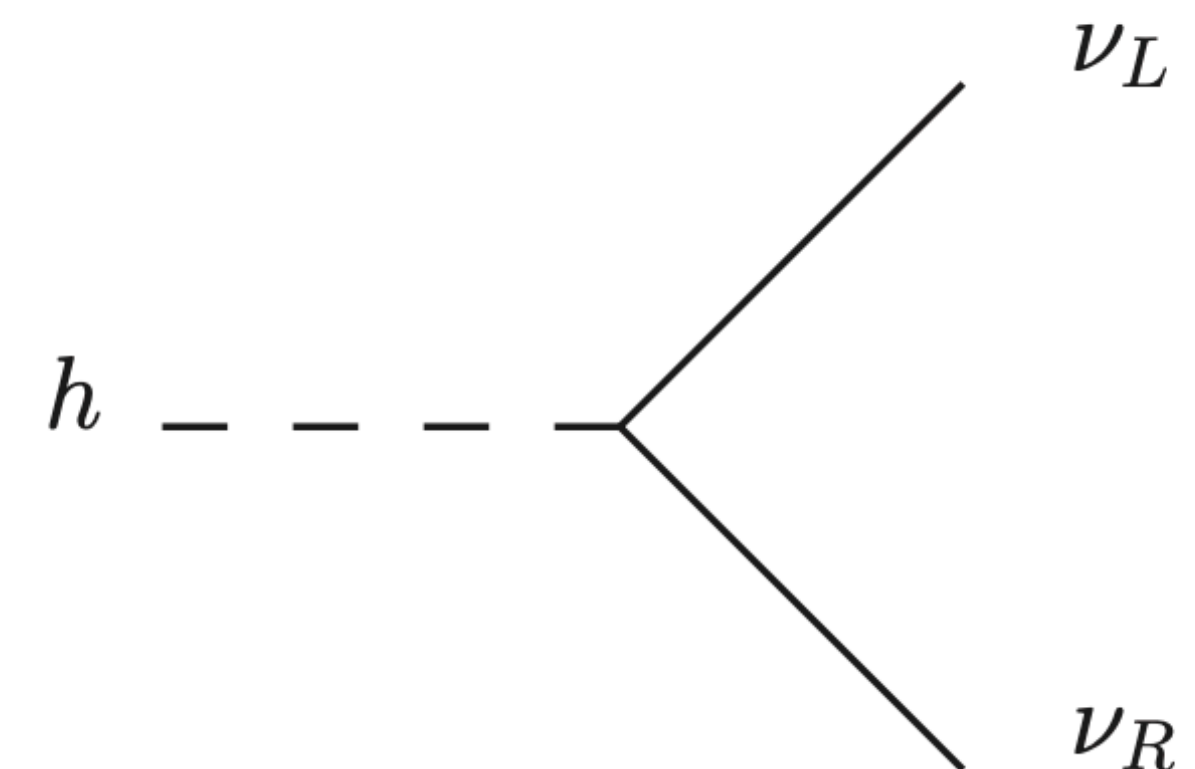
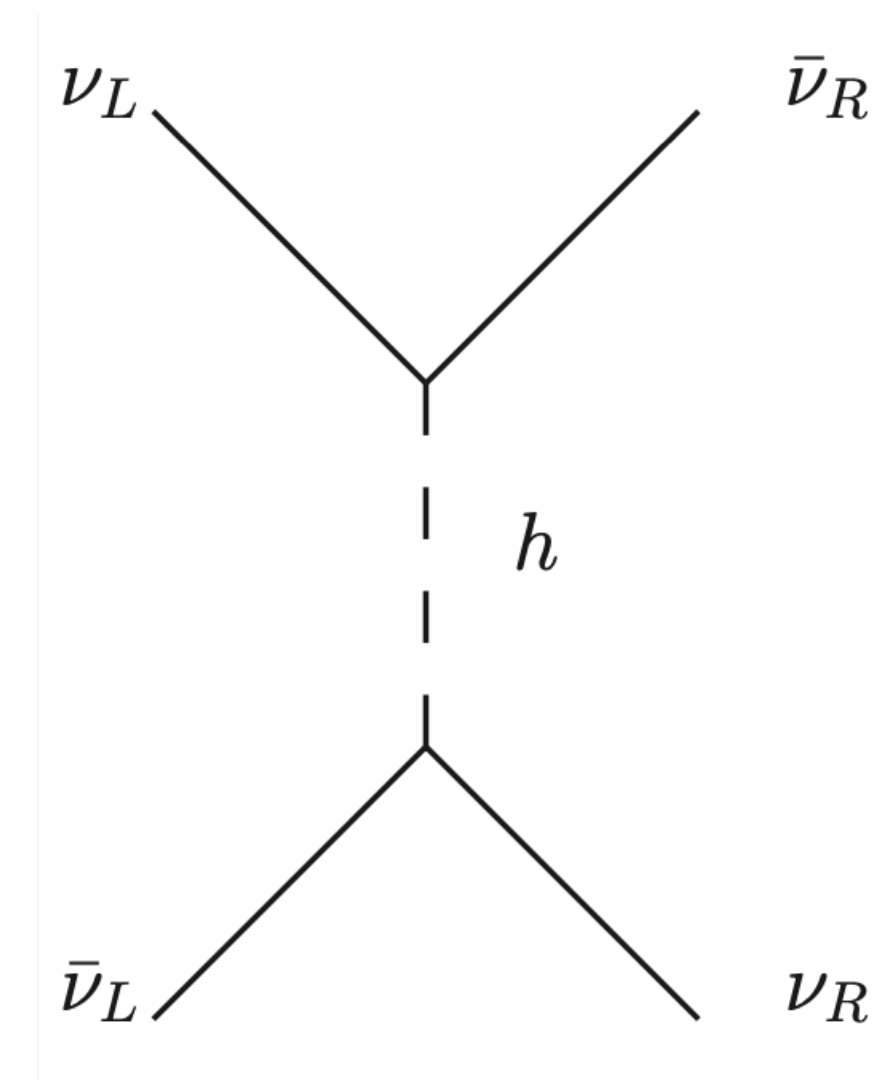
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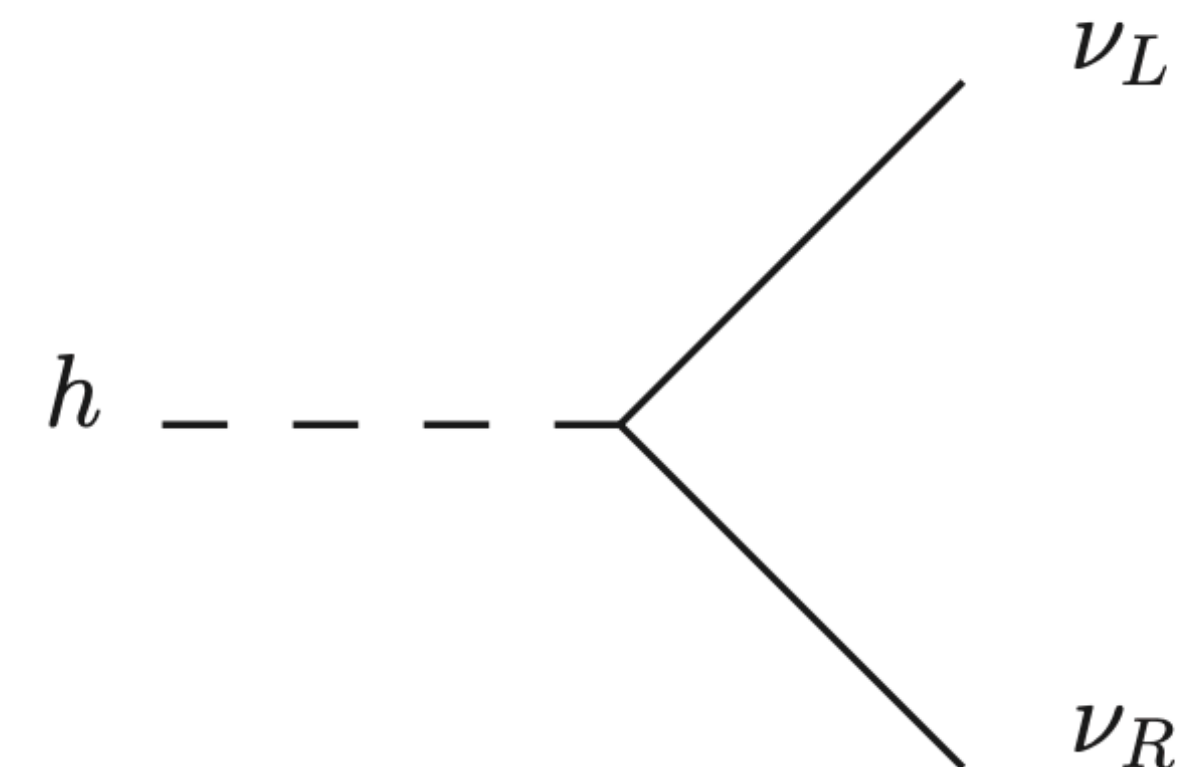
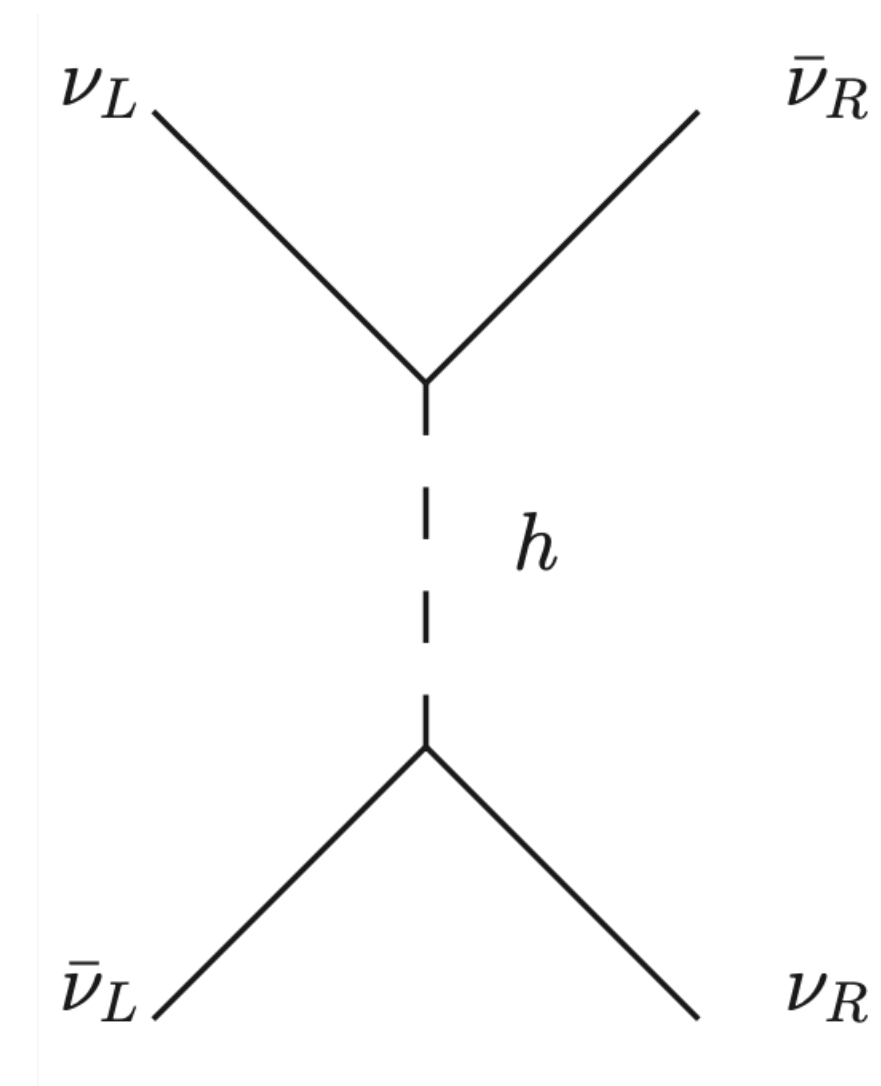
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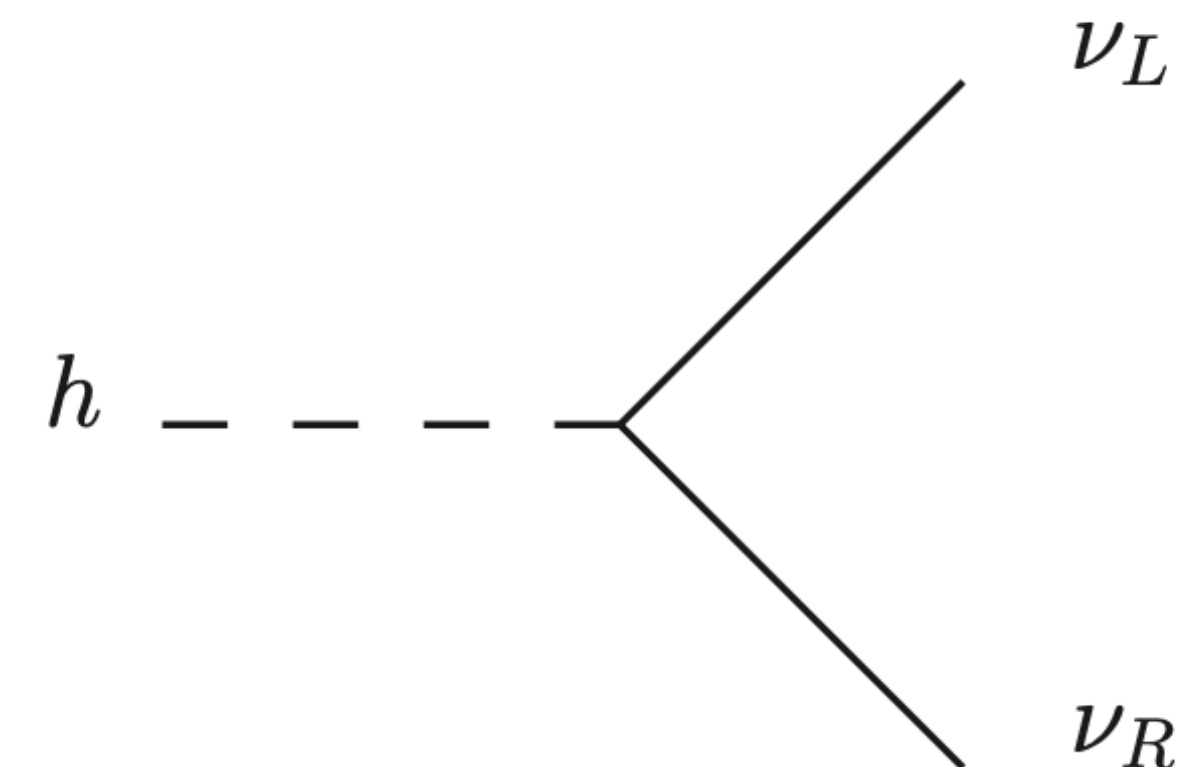
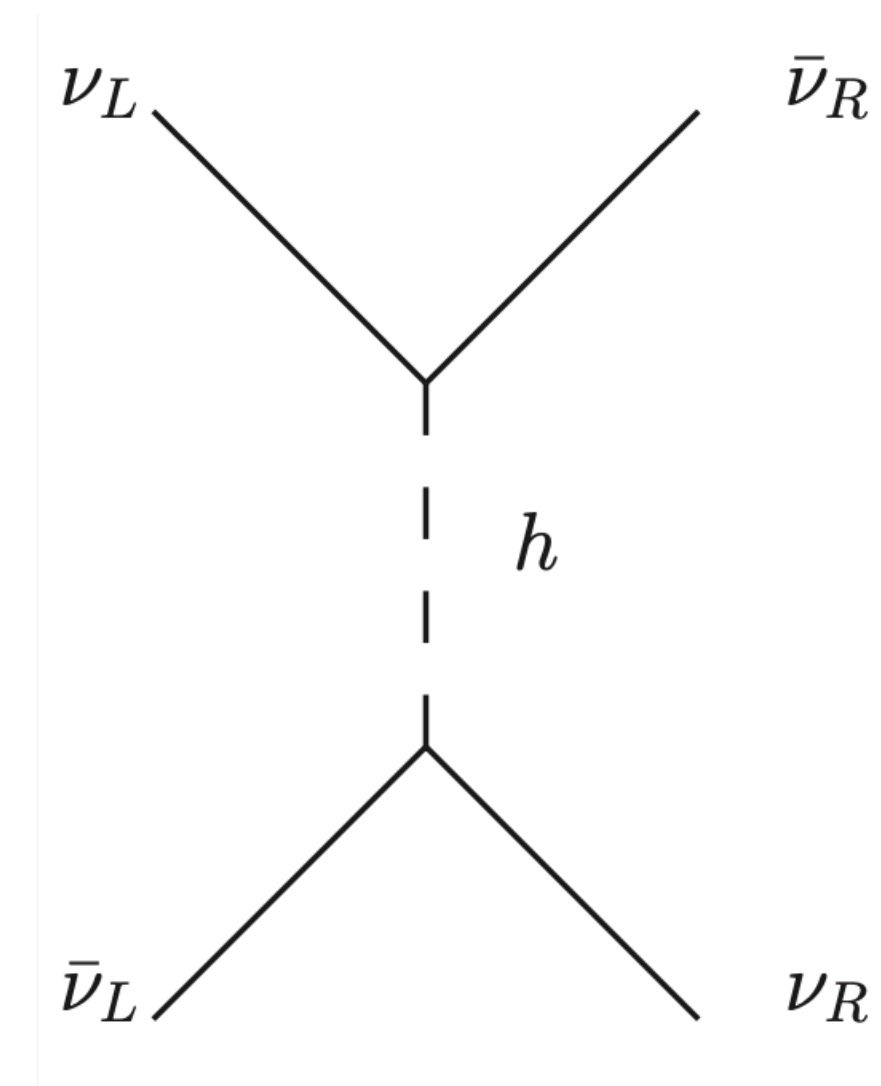
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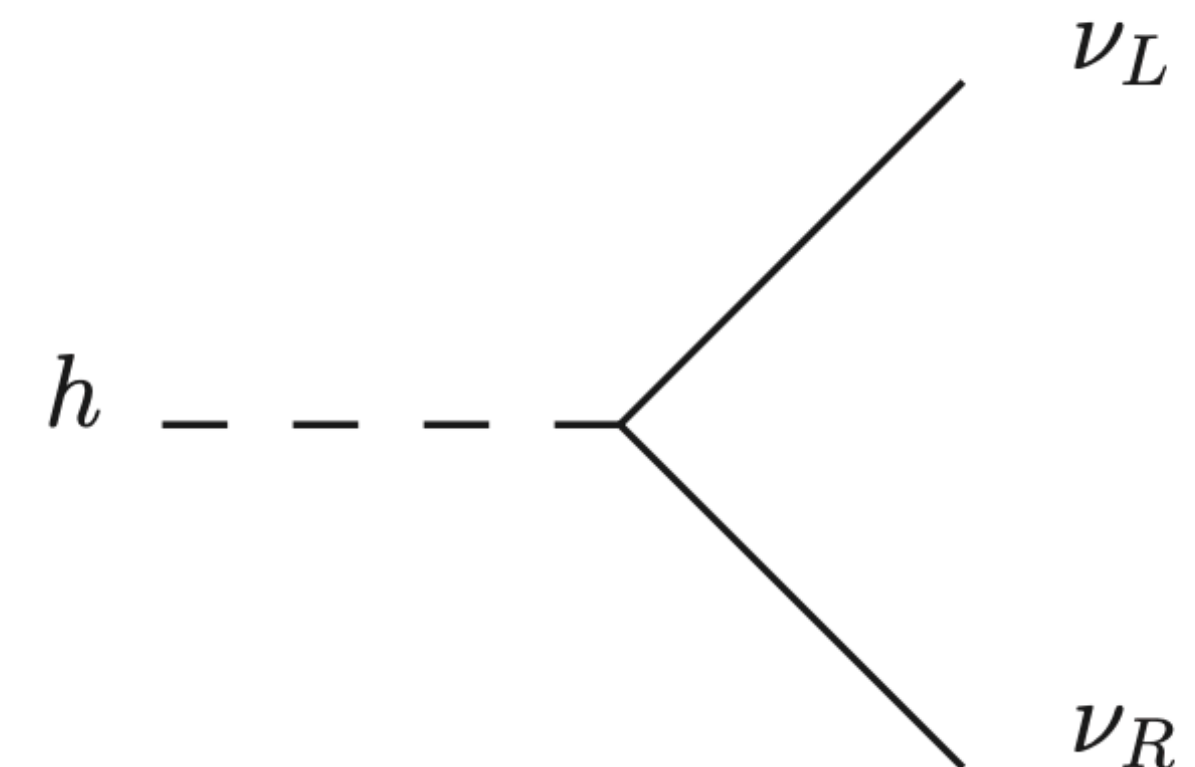
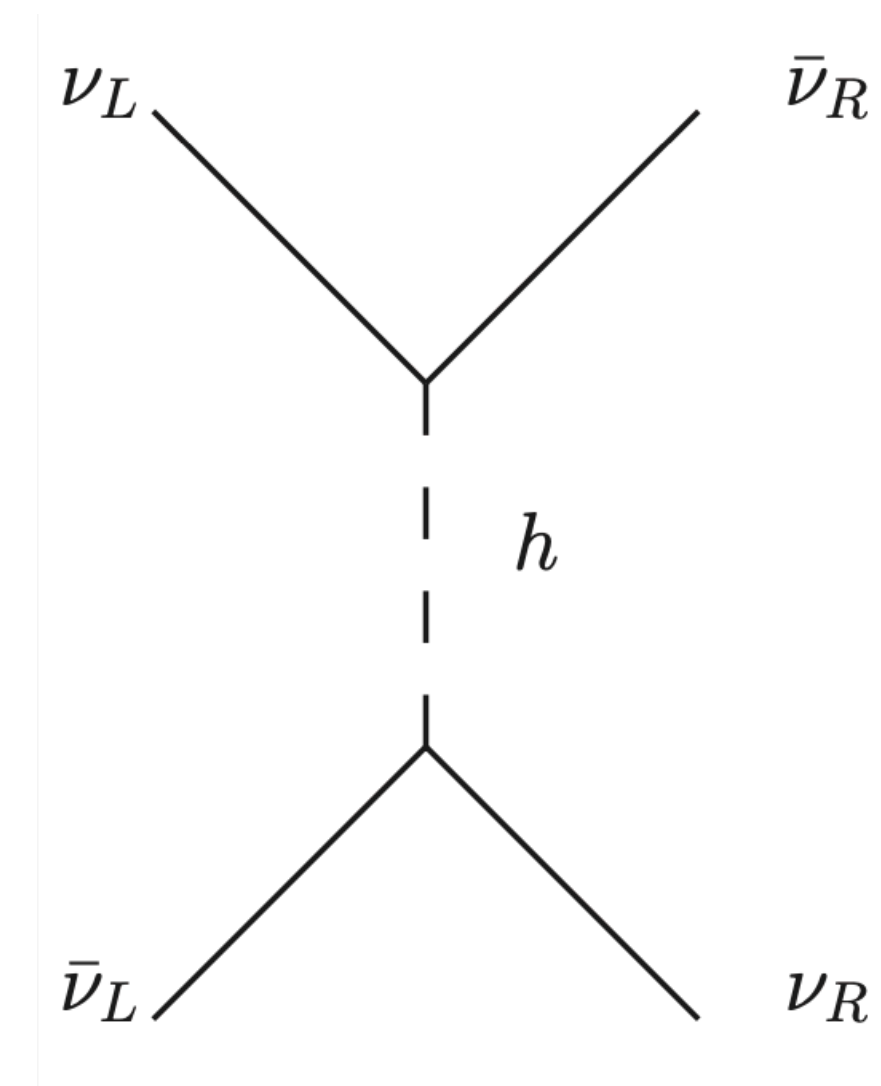
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Predicted abundance is

$$\Omega_{\nu_R} \sim \frac{\rho_{\nu_R}}{T_{\text{ew}}^4} \sim \frac{\Gamma(h \rightarrow \nu_L \nu_R) n_h}{HT_{\text{ew}}^3} \sim 10^{-8} \left(\frac{m_\nu}{0.1 \text{ eV}} \right)^2$$

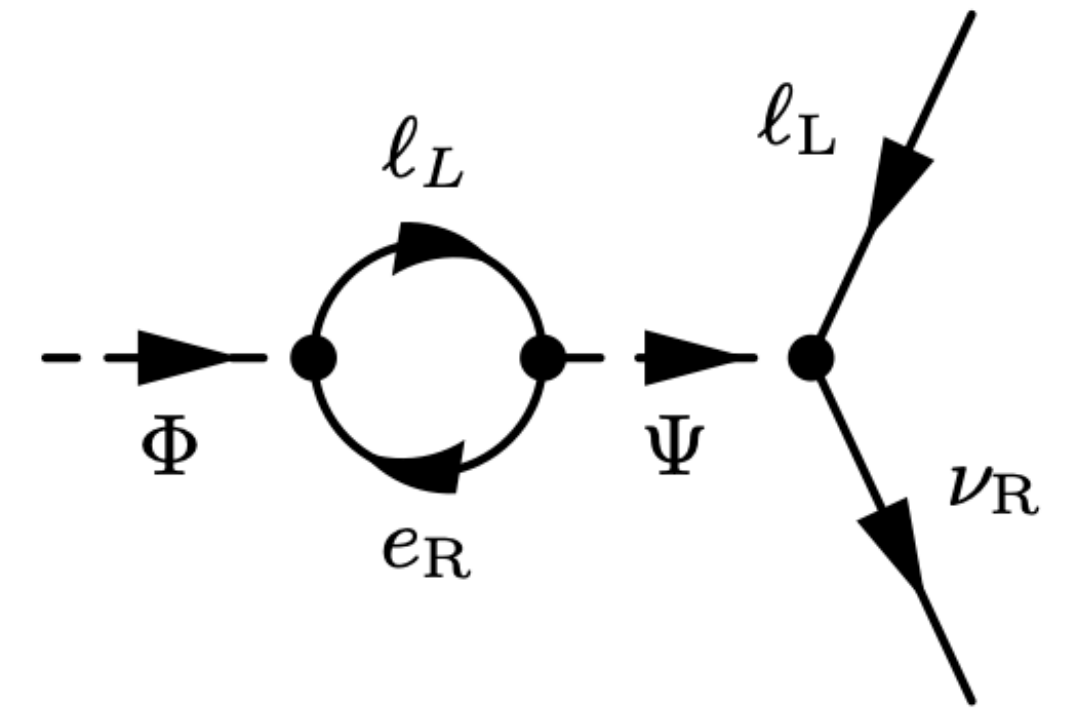
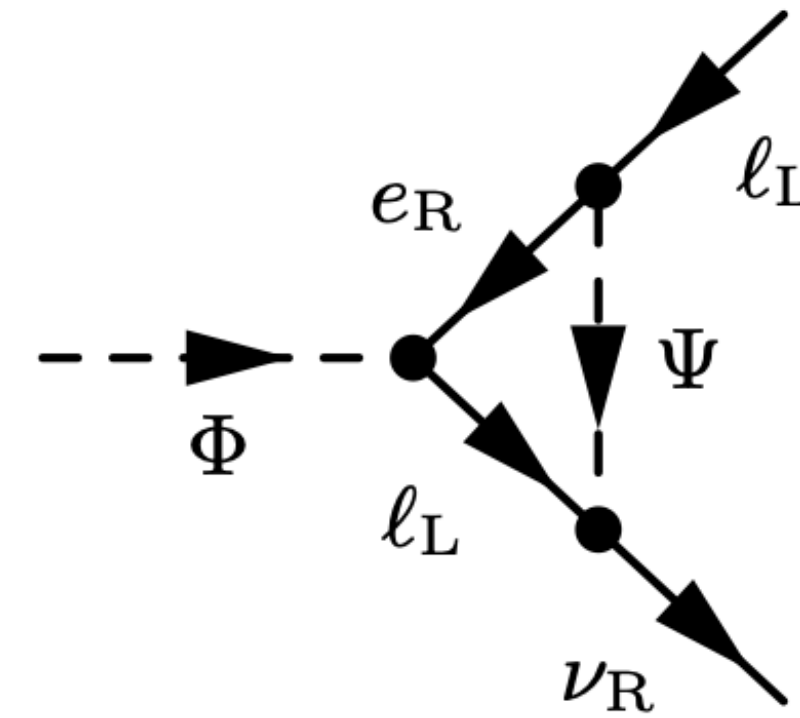
[P. Adshead, Y. Cui, A. Long, **MS**, hep-ph/2009.07852
X. Luo, W. Rodejohann, X. Xu hep-ph/2011.13059]



BSM Dirac Neutrino Masses

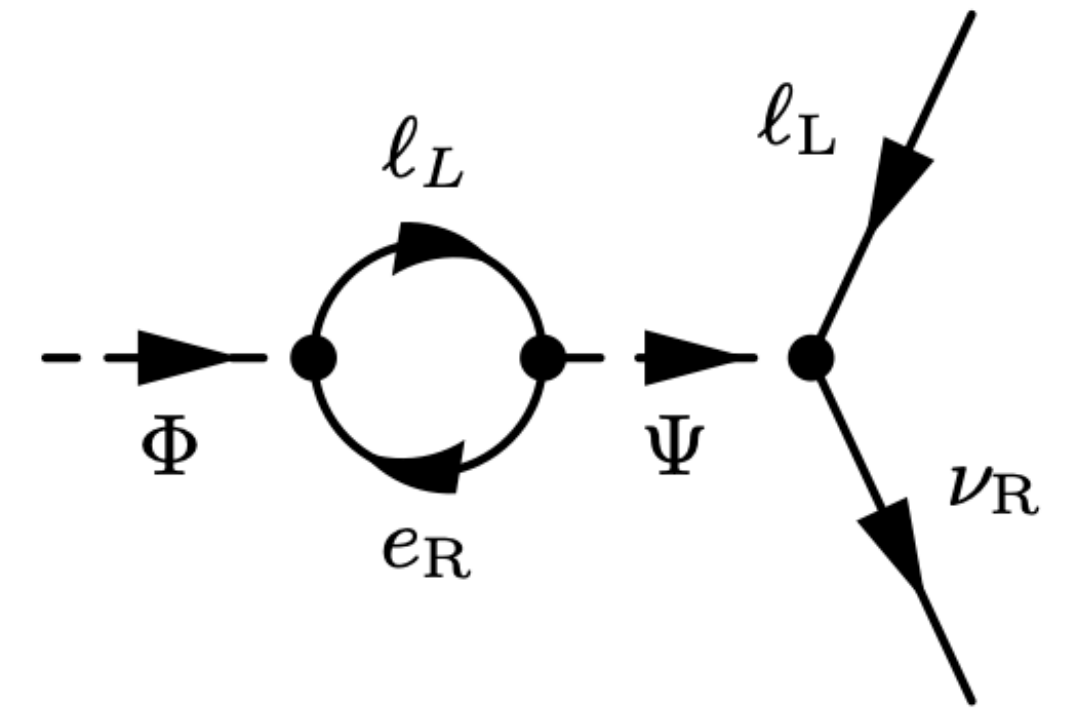
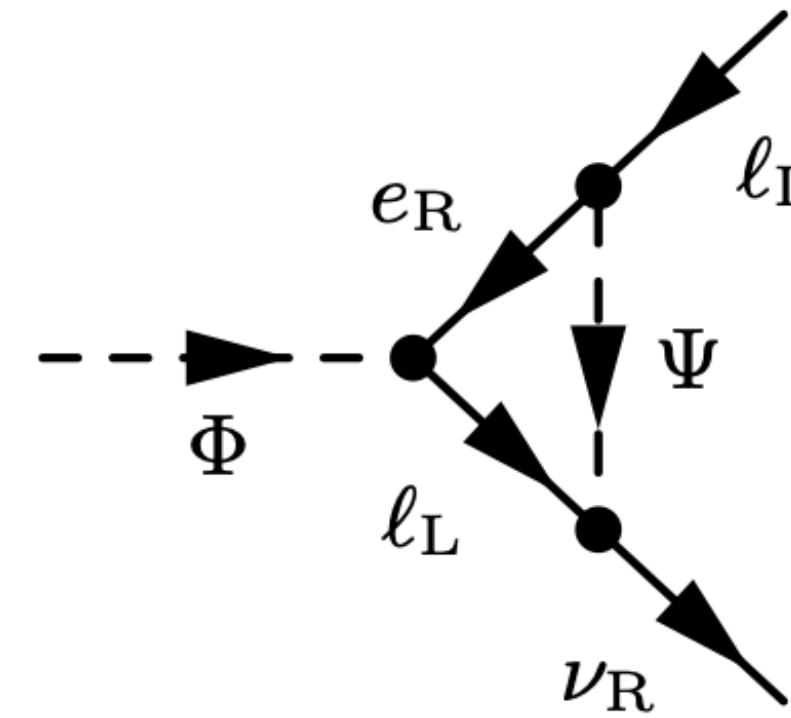
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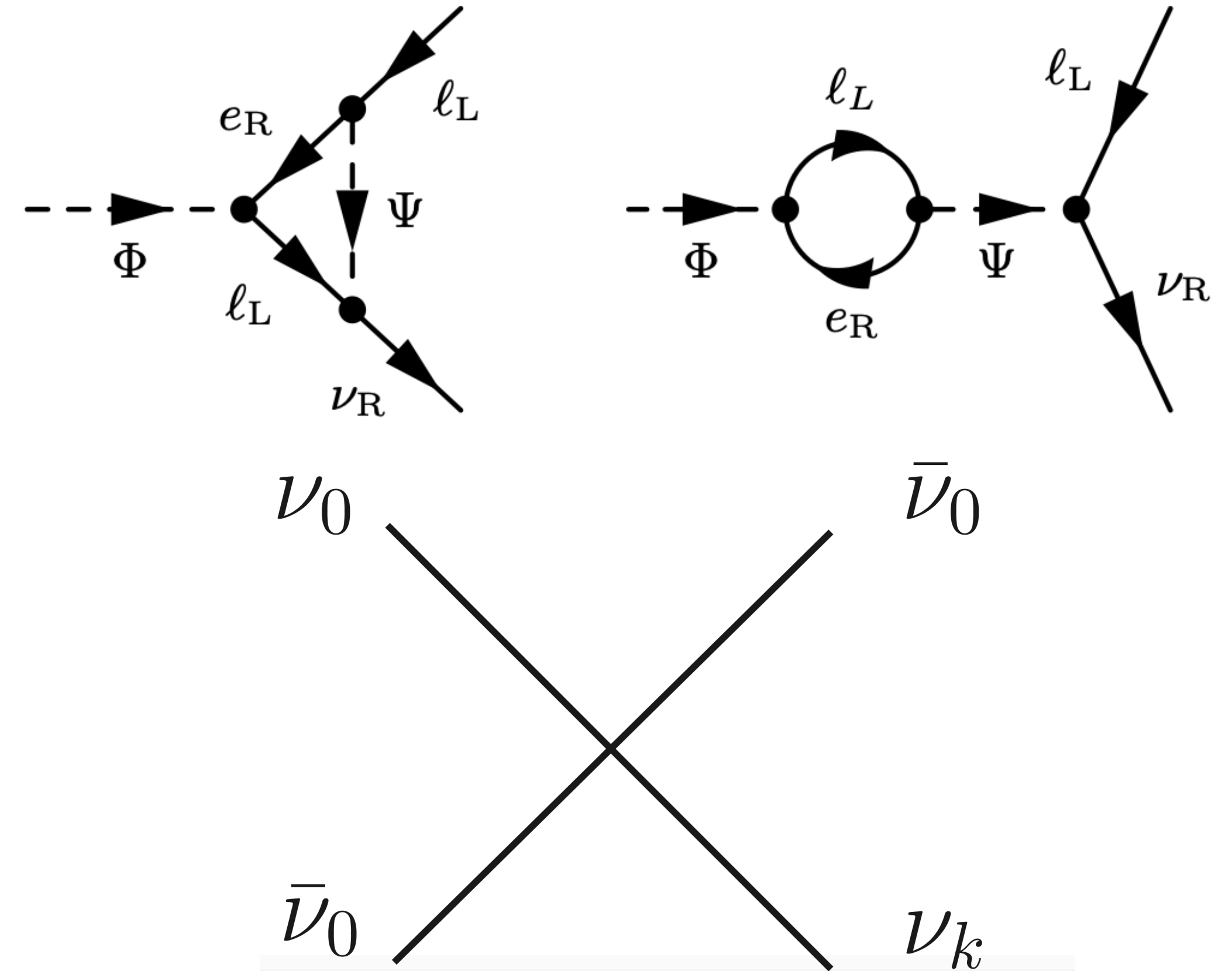
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- Neutrino mass models have a home in an extra dimension [N. Arkani-Hamed, et. al. hep-ph/9811448, K.R. Dienes, et. al. hep-ph/9811428]:
 - Compactification generates Dirac ν mass
 - $\implies \mathcal{L} \supset - \frac{\lambda \nu}{\sqrt{2\pi R_{\text{ED}} M_*}} \bar{\nu}_L \nu_R^{(0)}$
 - ...also generates mixing of the ν_k modes with ν_L
 - And substantial number of relics, strong constraints [K. Abazajian, G. Fuller, M. Patel hep-ph/0011048]

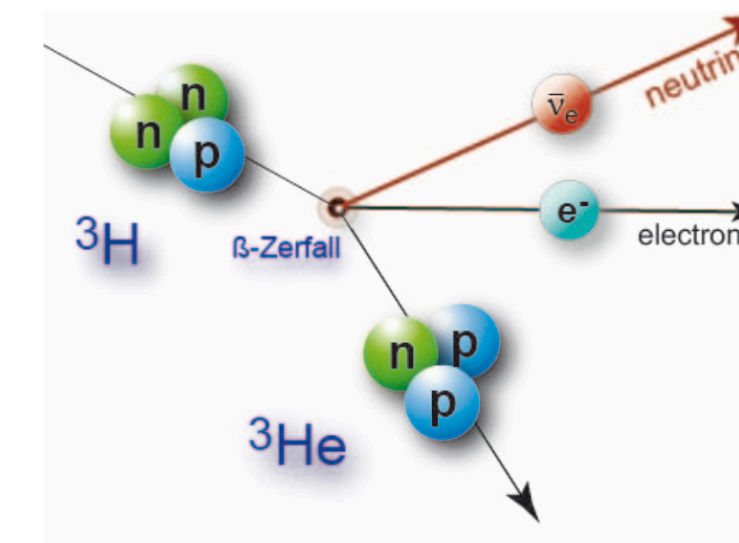


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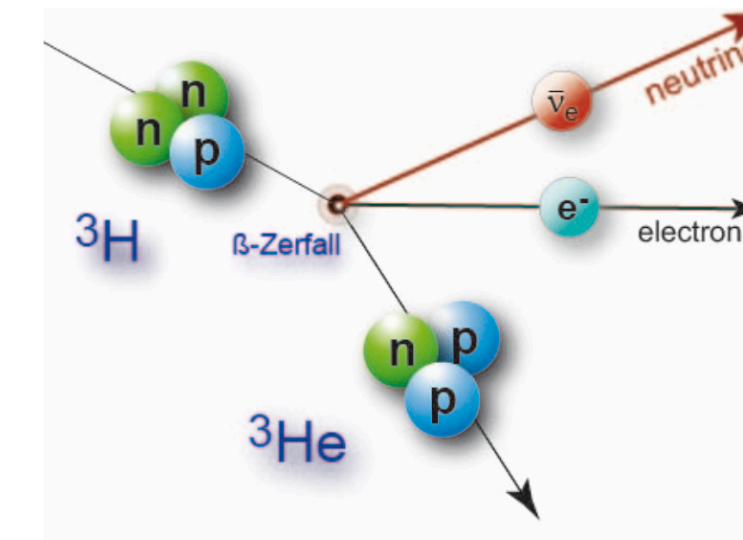
Katrin

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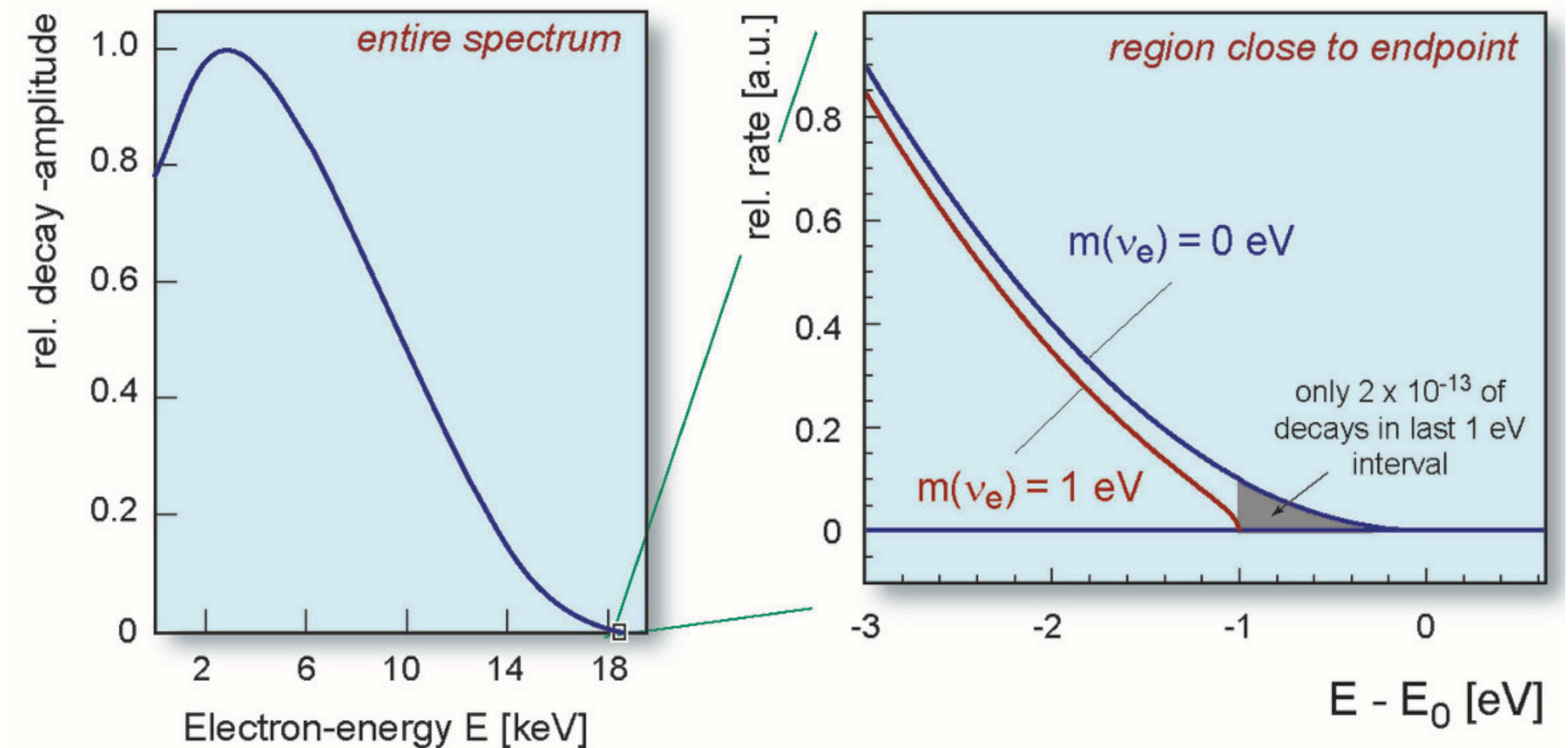
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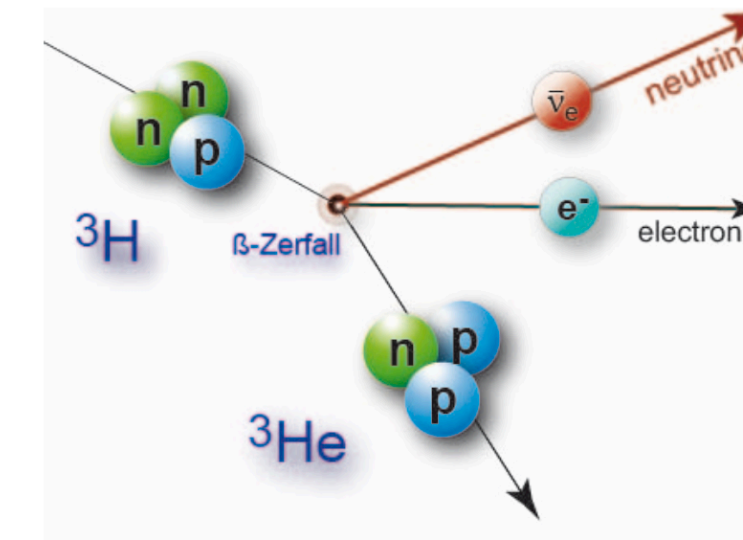
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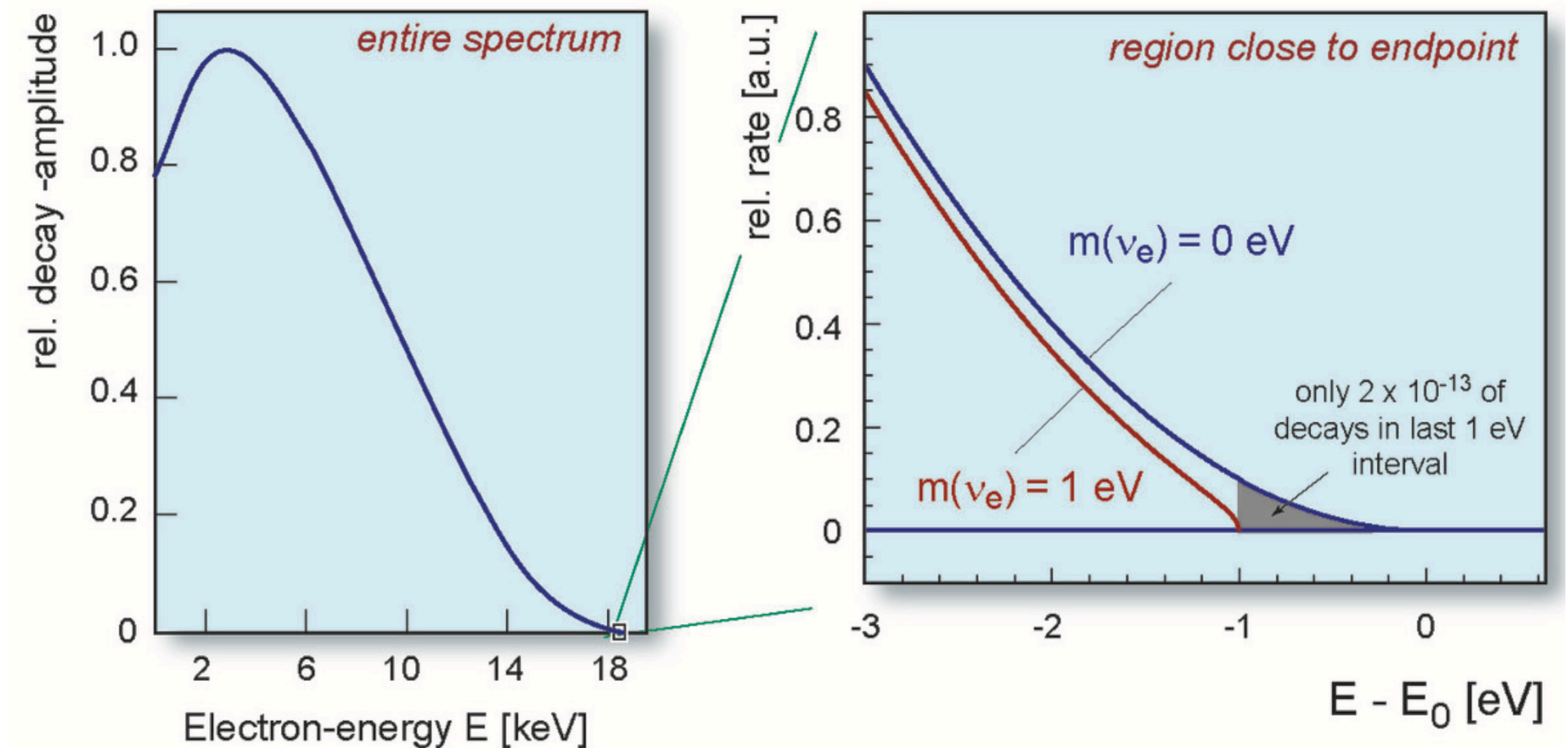
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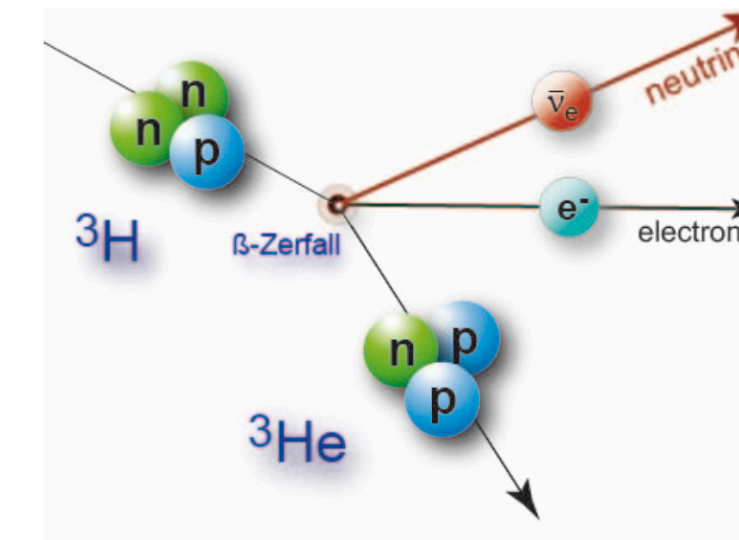
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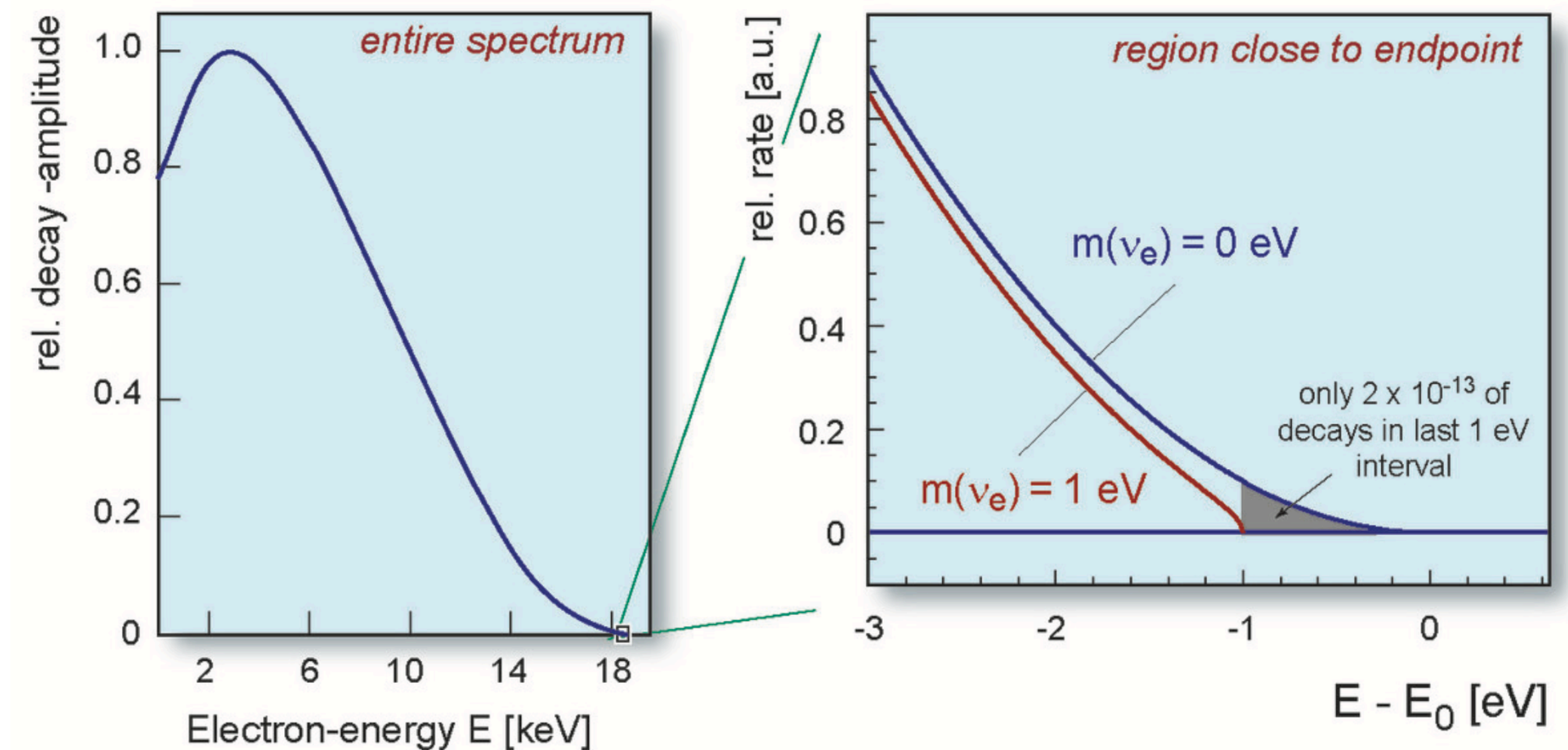
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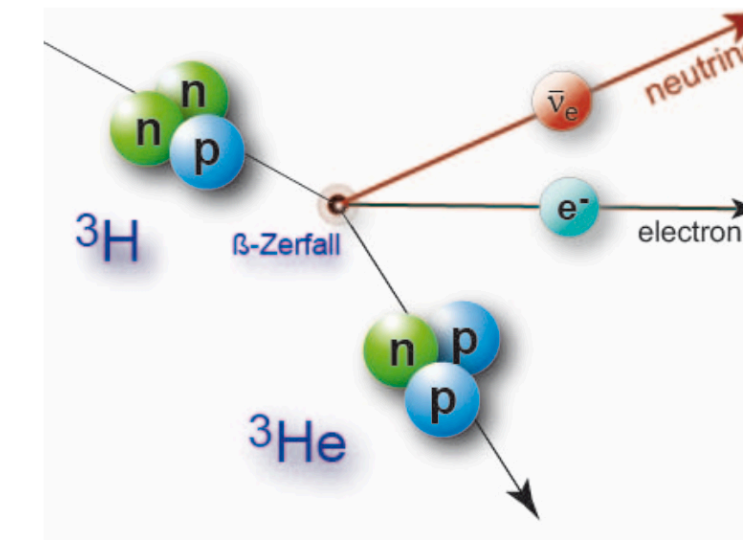


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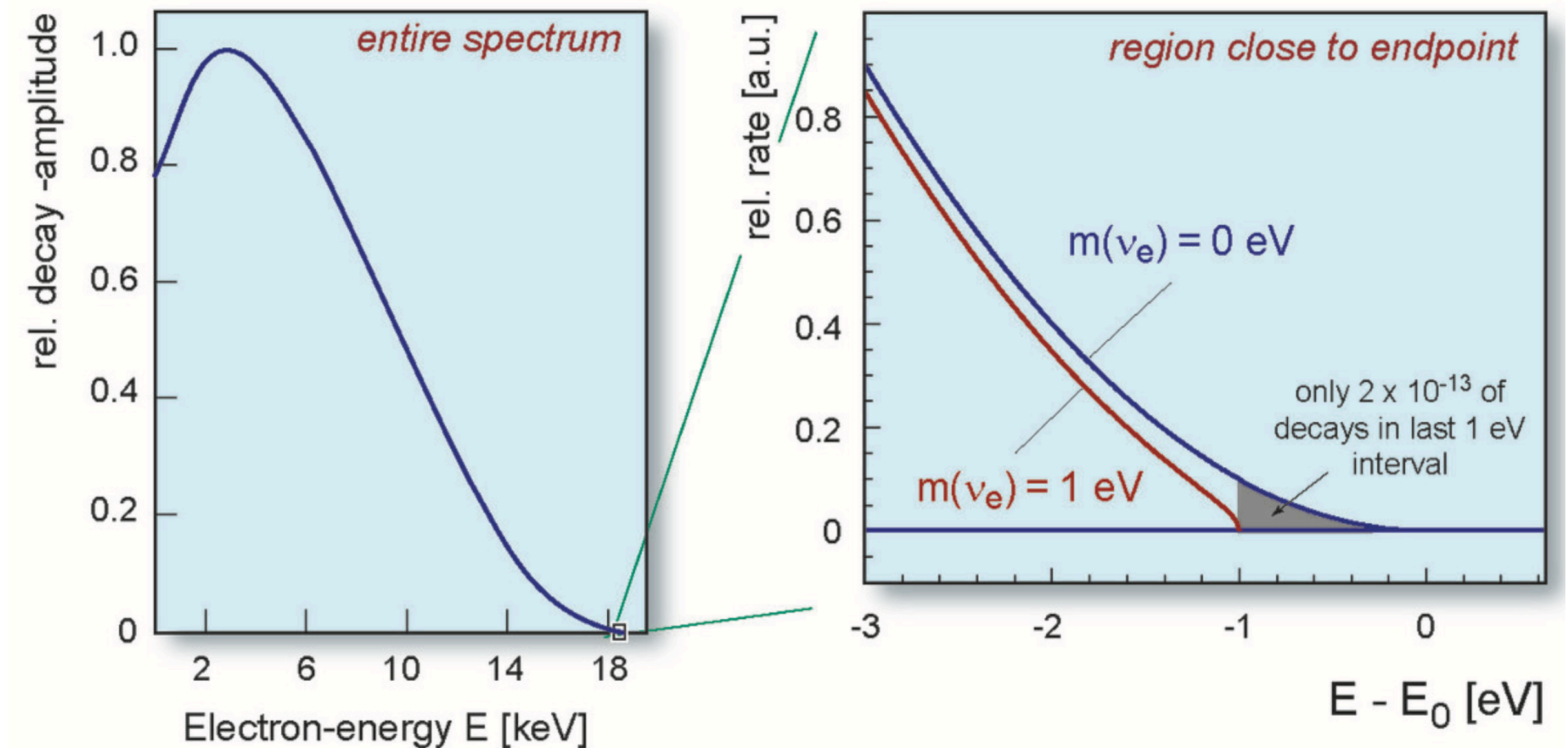
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 $\implies \Sigma m_{\nu} \simeq 3 \text{ eV}$ [J. Angrik, et. al. 2004.22005]



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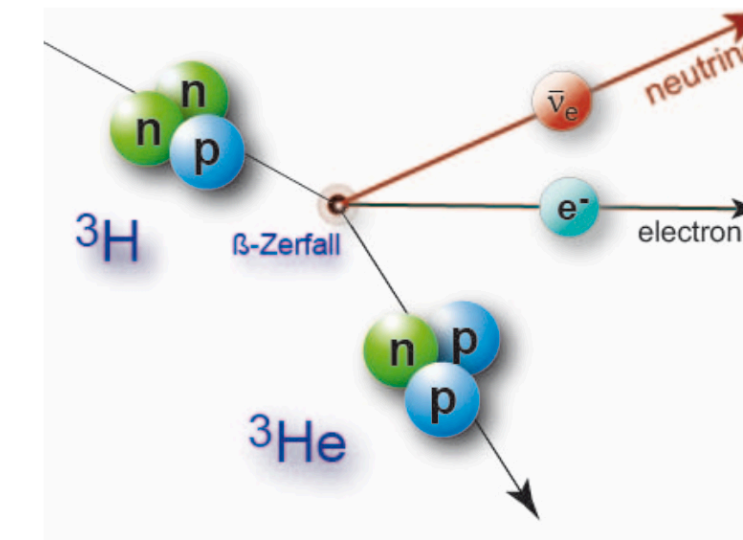
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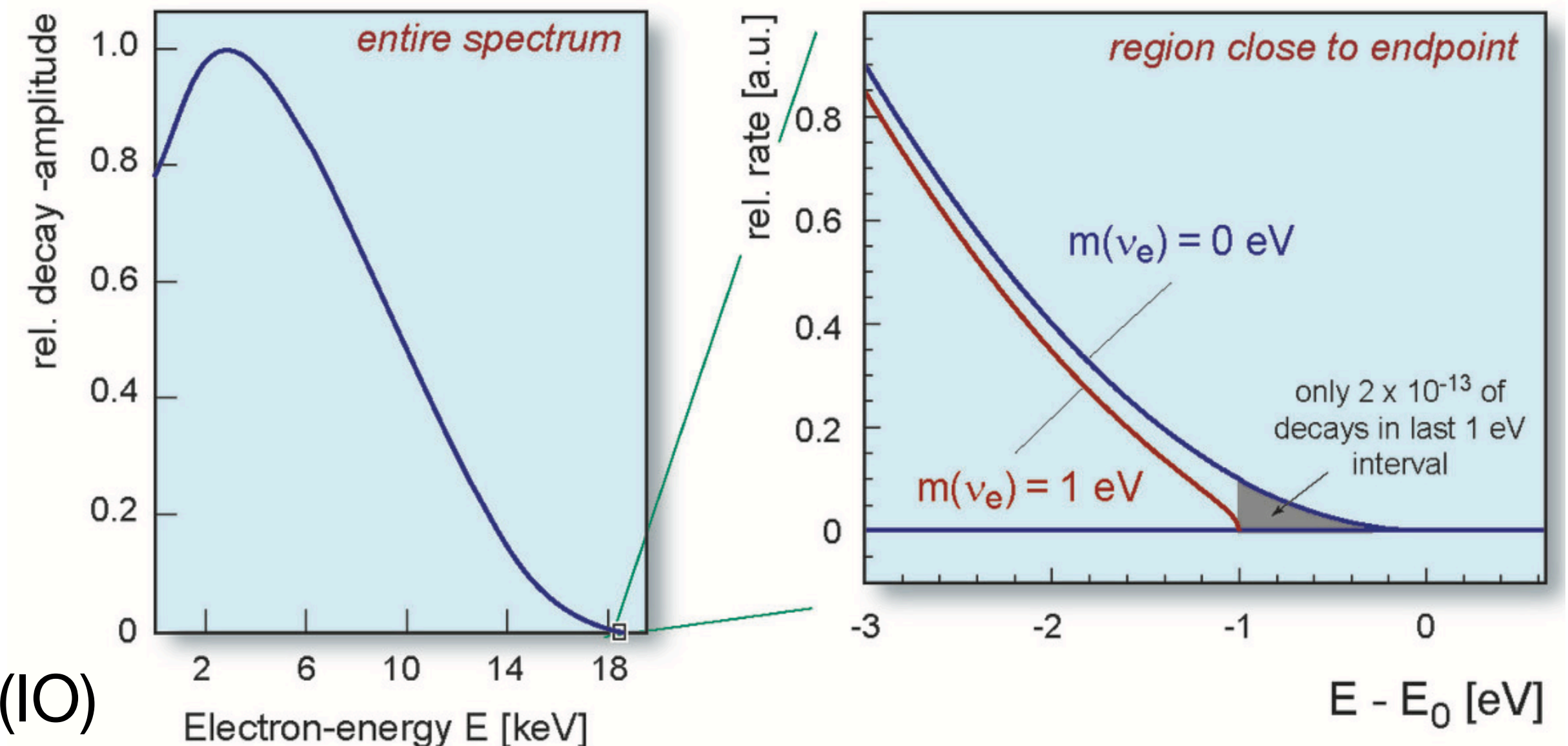
- Project 8 projected sensitivity: $m_{\nu_e} < 0.04 \text{ eV}$

$$\implies \Sigma m_{\nu} \simeq 0.14 \text{ eV (NO)} \text{ and } \Sigma m_{\nu} \simeq 0.099 \text{ eV (IO)}$$

[A.A. Esfahani et al. J. Phys. G, 44(5):054004]



KATRIN



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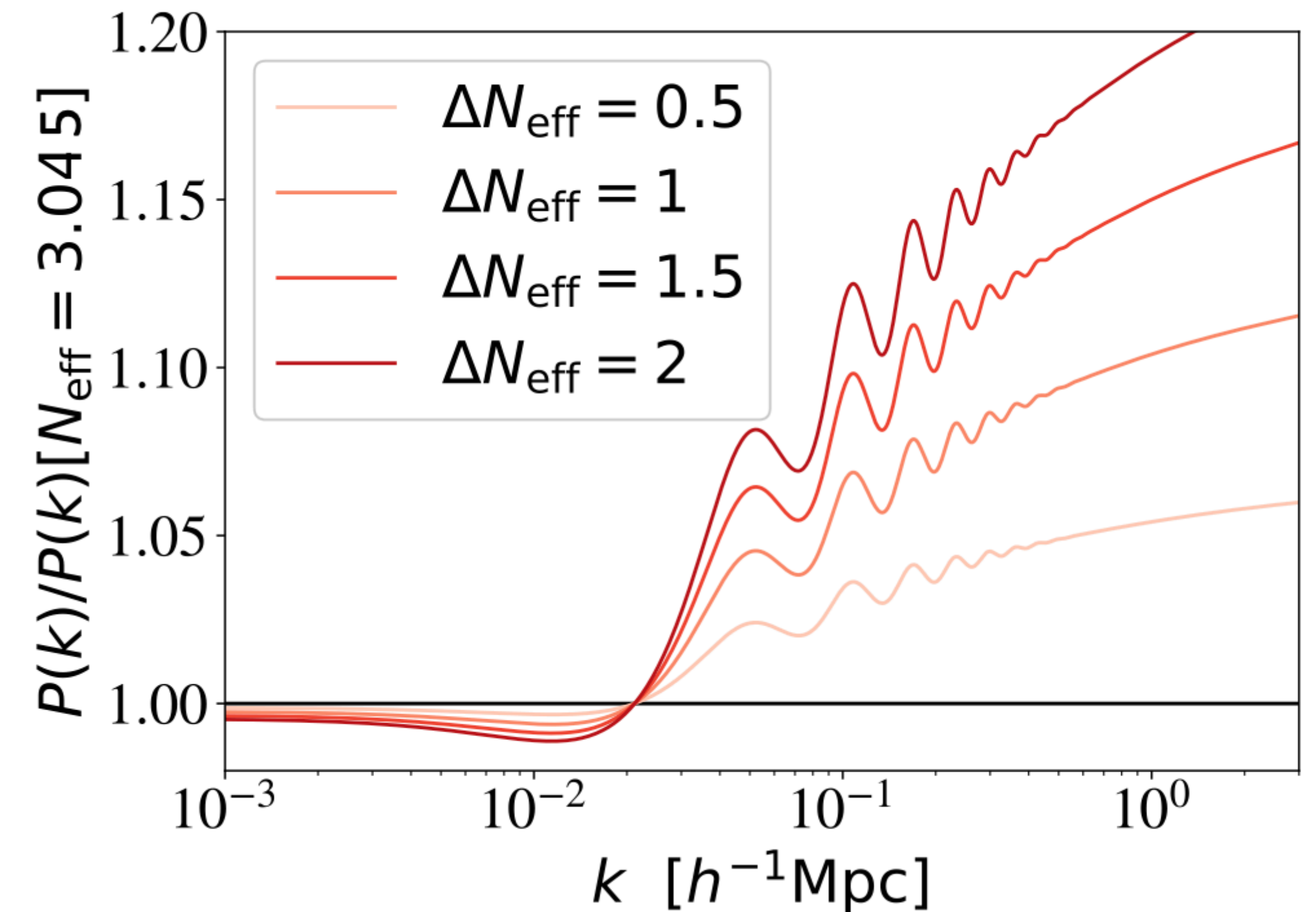
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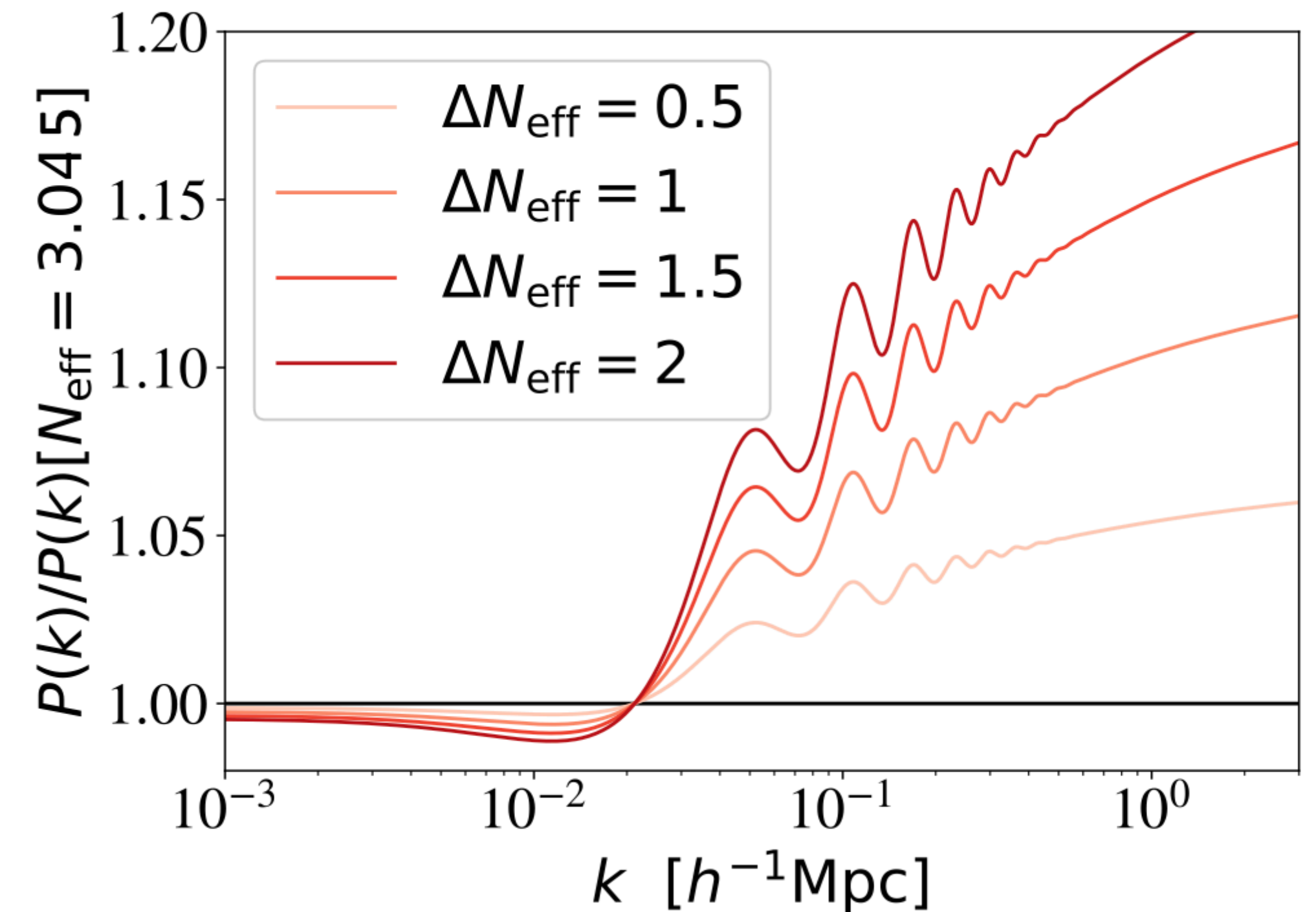
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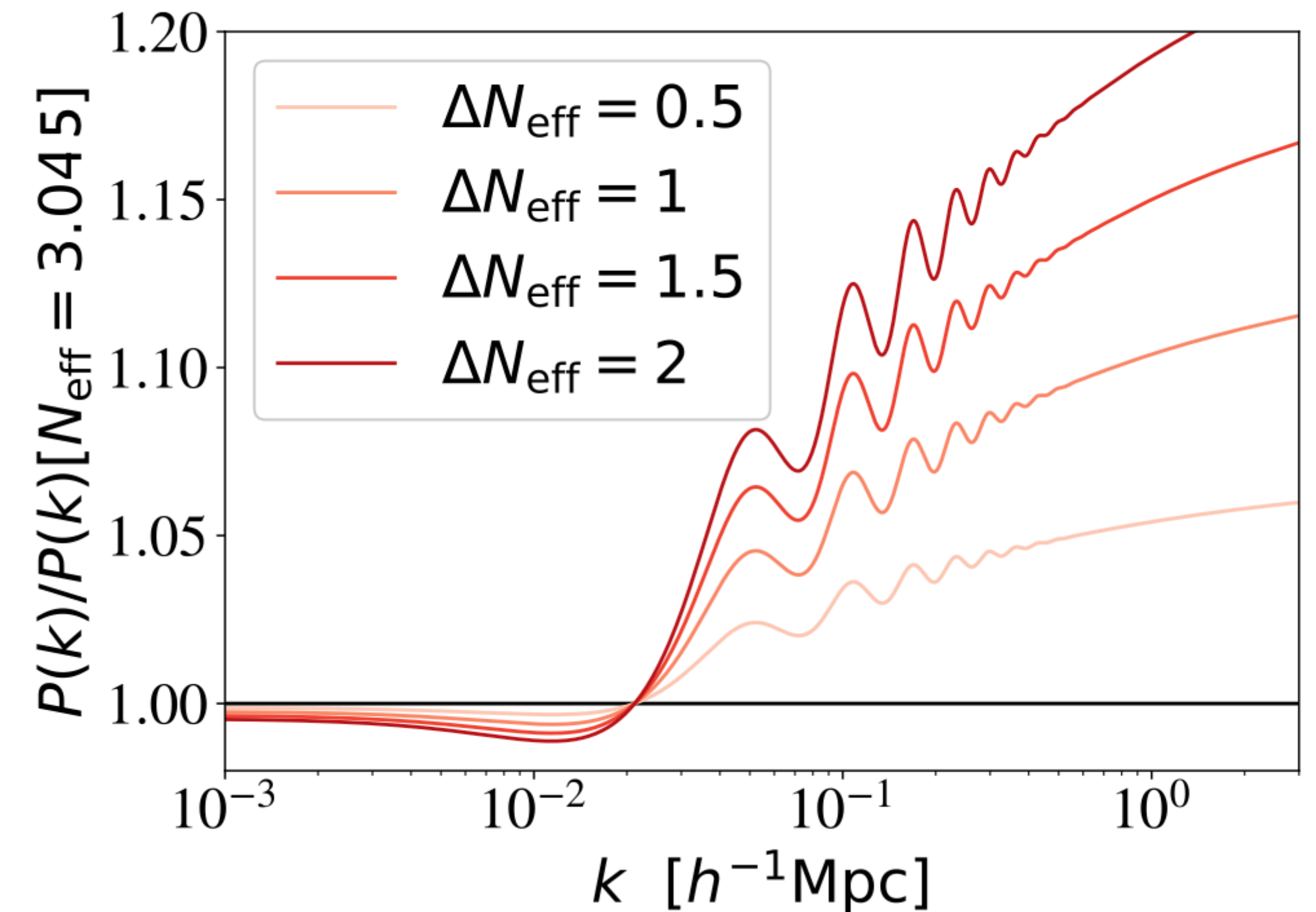
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[K. Abazajian, et. al. astro-ph.IM/1907.04473]



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[E. Di Valentino, A. Melichiorri, J. Silk, astro-ph.CO/1507.06646]
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- Planck+BAO gives joint bound of $m_{\nu,\text{sterile}}^{\text{eff}} < 0.23 \text{ eV}, N_{\text{eff}} < 3.34$

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Internal d.o.f \downarrow g \uparrow Eff. d.o.f just before ν_L decoupling g'_\star

$T_\nu = T_{\text{SM}}$ \uparrow T_ν \uparrow $g_\star(T_d)$ \uparrow **Total** eff. d.o.f at ν_R decoupling

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$$\Delta N_{\text{eff}} = \frac{4g}{7} \left[\frac{43}{4g_\star(T_d)} \right]^{4/3} = 0.027g \left[\frac{106.75}{g_\star(T_d)} \right]^{4/3}$$

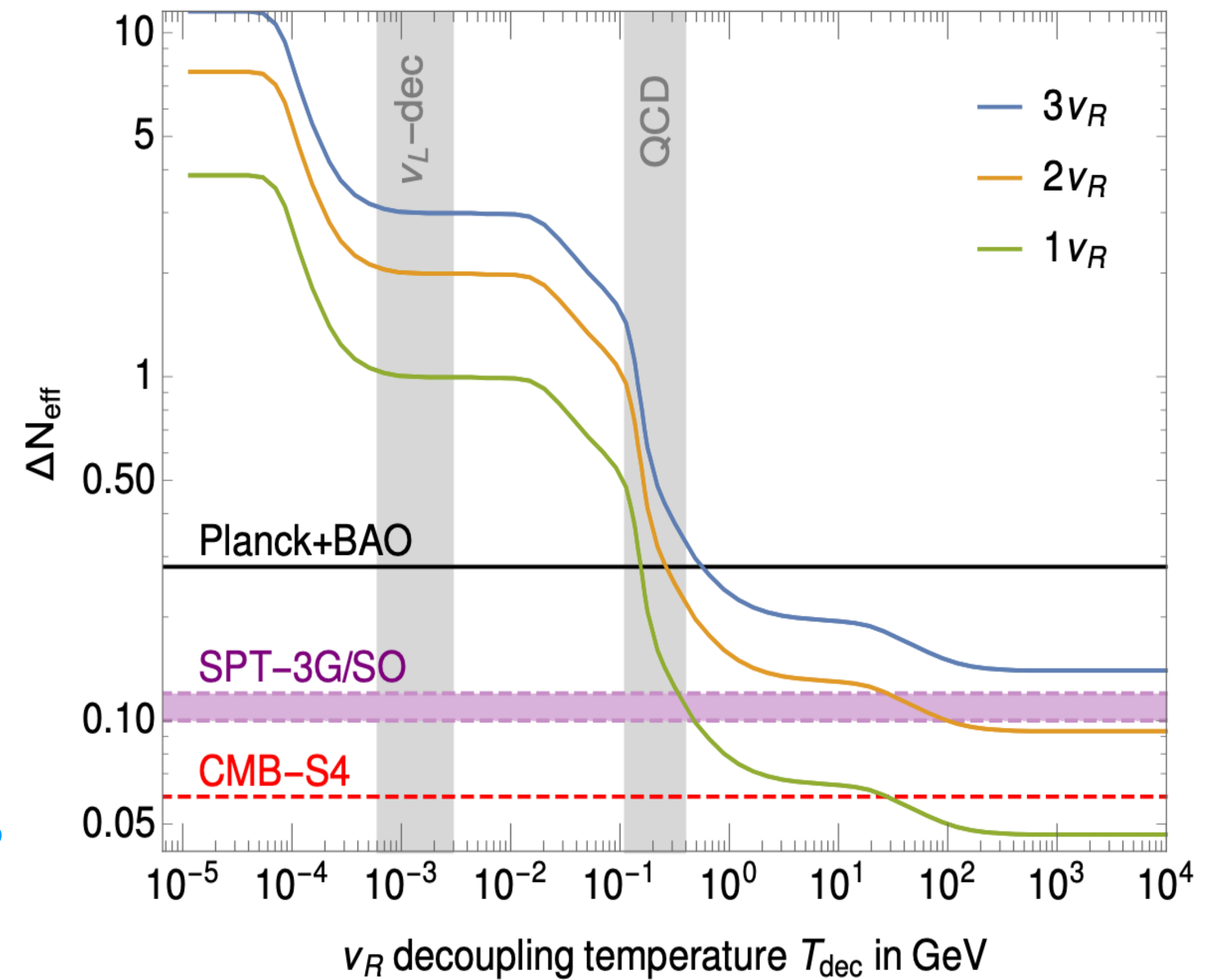
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[K. Abazajian, J. Heeck, hep-ph/1908.03286]

Correlating Terrestrial and Cosmological Probes

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[K. Abazajian, J. Heeck, hep-ph/1908.03286;
P. Adshead, Y. Cui, A. Long, **MS**, hep-ph/2009.07852]

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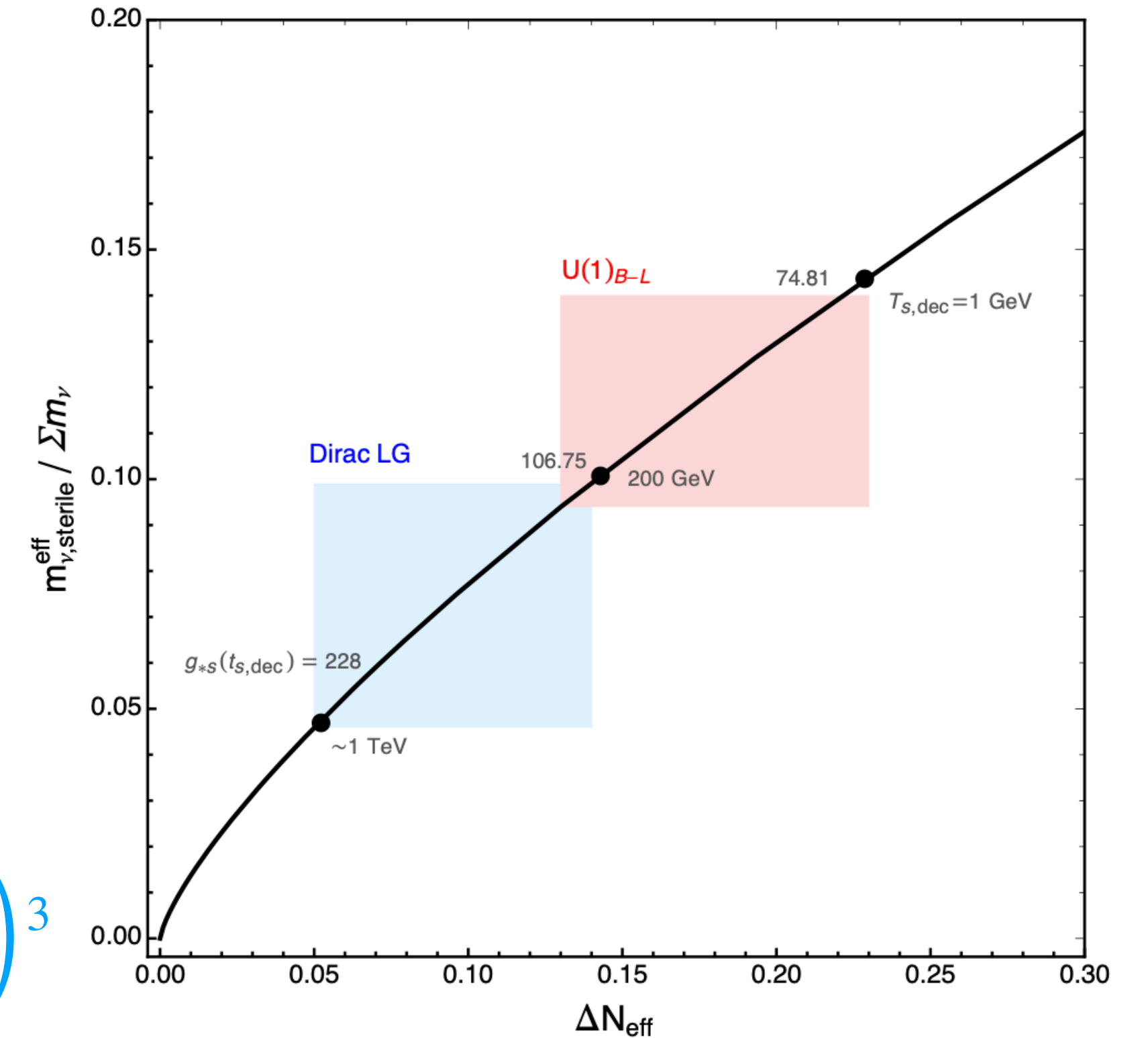
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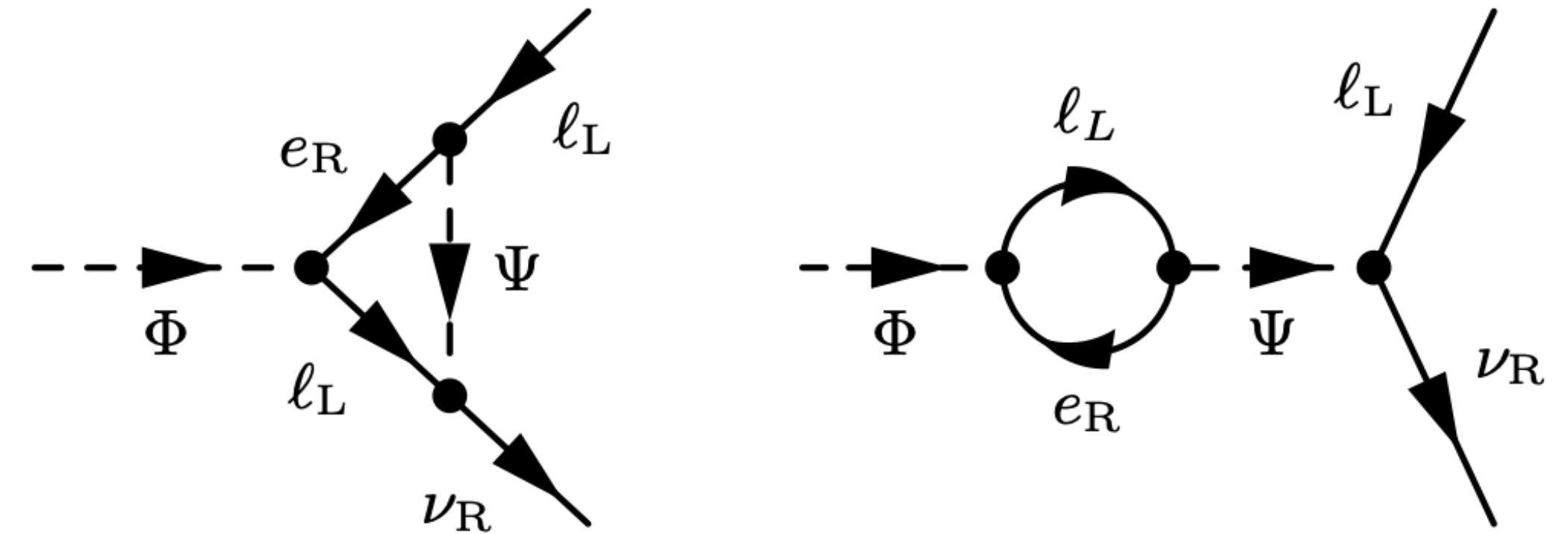
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BSM Dirac Neutrino Masses

- Dirac Leptogenesis [K. Dick, et. al. Phys. Rev. Lett., 84:4039–4042, 2000...]
 - Model dependent $\Delta N_{\text{eff}} \sim 0.05 - 0.14$
- Gauged $U(1)_{B-L}$ [V. Barger, et. al. Phys. Rev. D, 67:075009, 2003...]
 - $T_{\text{dec}} \lesssim (m_Z/g' M_{\text{pl}})^{4/3} M_{\text{pl}} \implies \Delta N_{\text{eff}} \simeq 0.13 - 0.23$



- Neutrino mass models have a home in an extra dimension

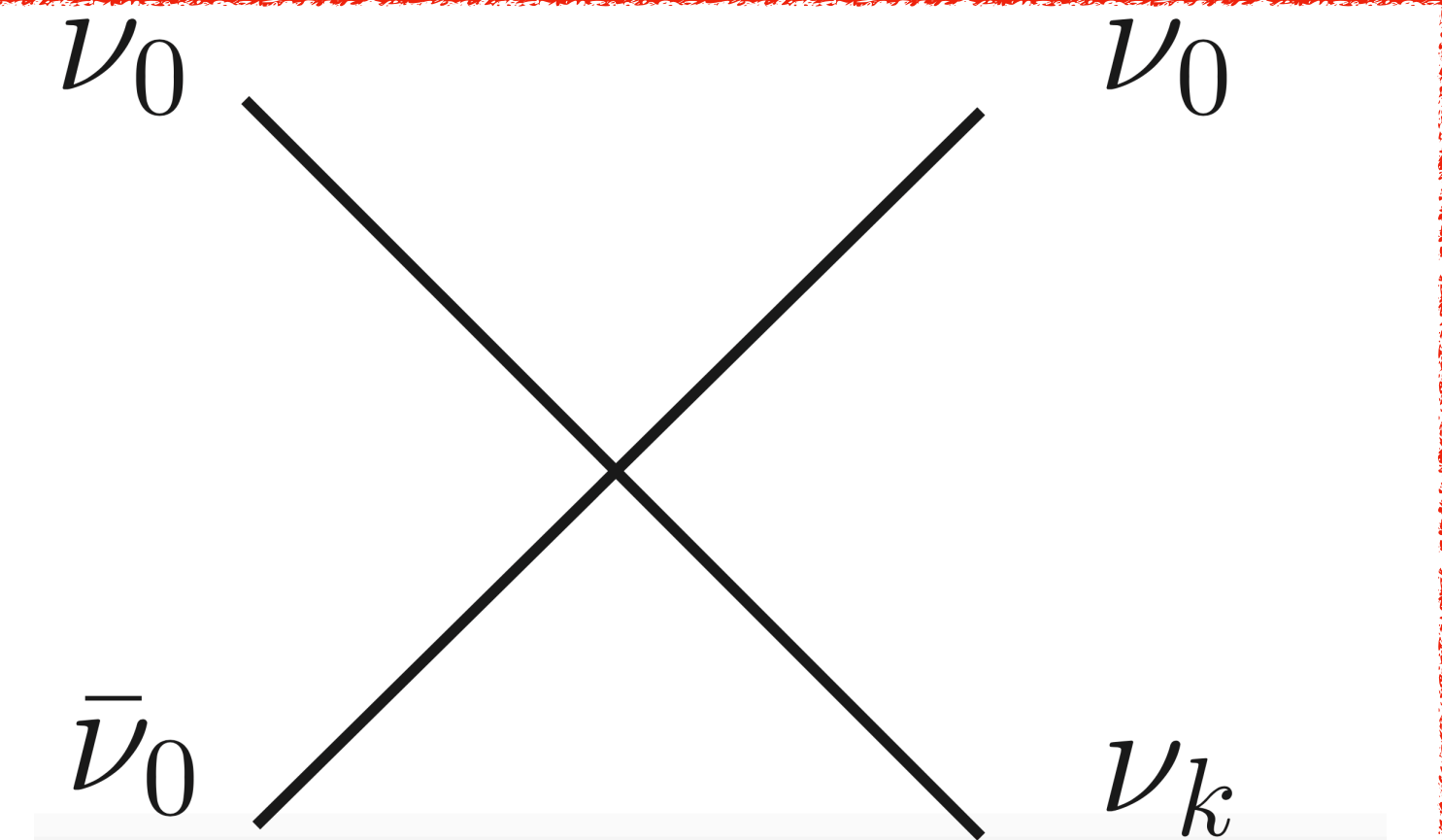
[N. Arkani-Hamed, et. al. hep-ph/9811448, K.R. Dienes, et. al. hep-ph/9811428]:

- Compactification generates Dirac ν mass

$$\implies \mathcal{L} \supset - \frac{\lambda \nu}{\sqrt{2\pi R_{\text{ED}} M_*}} \bar{\nu}_L \nu_R^{(0)}$$

- ...also generates mixing of the ν_k modes with ν_L
- And substantial number of relics, strong constraints

[K. Abazajian, G. Fuller, M. Patel hep-ph/0011048]



Probing Large Extra Dimensions? [D. Mckeen, J. Ng., **MS** in prep]

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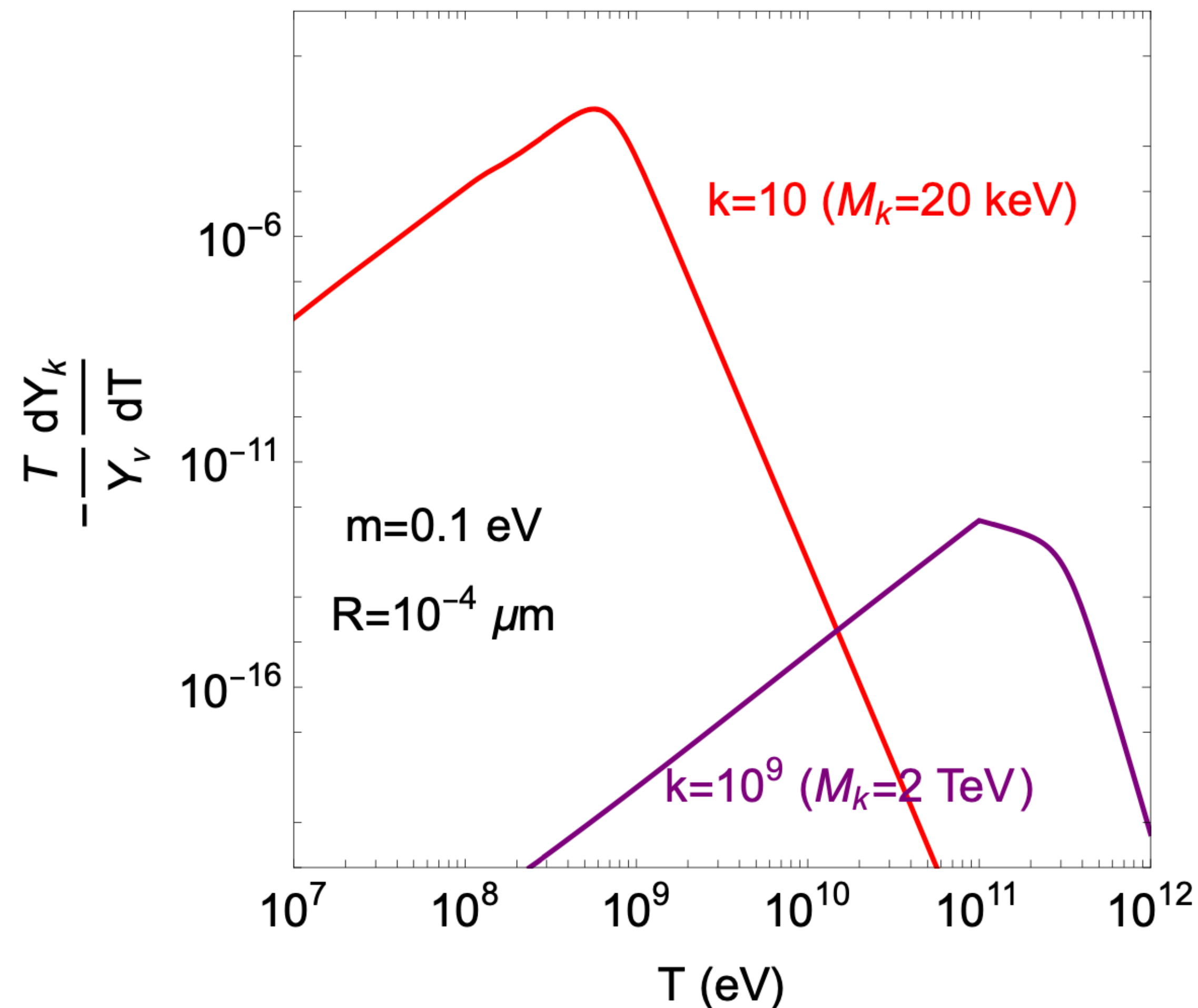
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$$\frac{n_k}{n_\nu} \simeq 2.32 \times 10^{-2} \left(\frac{m}{0.1 \text{ eV}} \right)^2 \left(\frac{R}{10^{-4} \mu\text{m}} \right) \frac{1}{k} \left[\frac{10.75}{g_*(T_V^k)} \right]^{11/6}$$

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Low Reheat Universe, $T_{\text{RH}} \sim \mathcal{O}(10 \text{ MeV})$:

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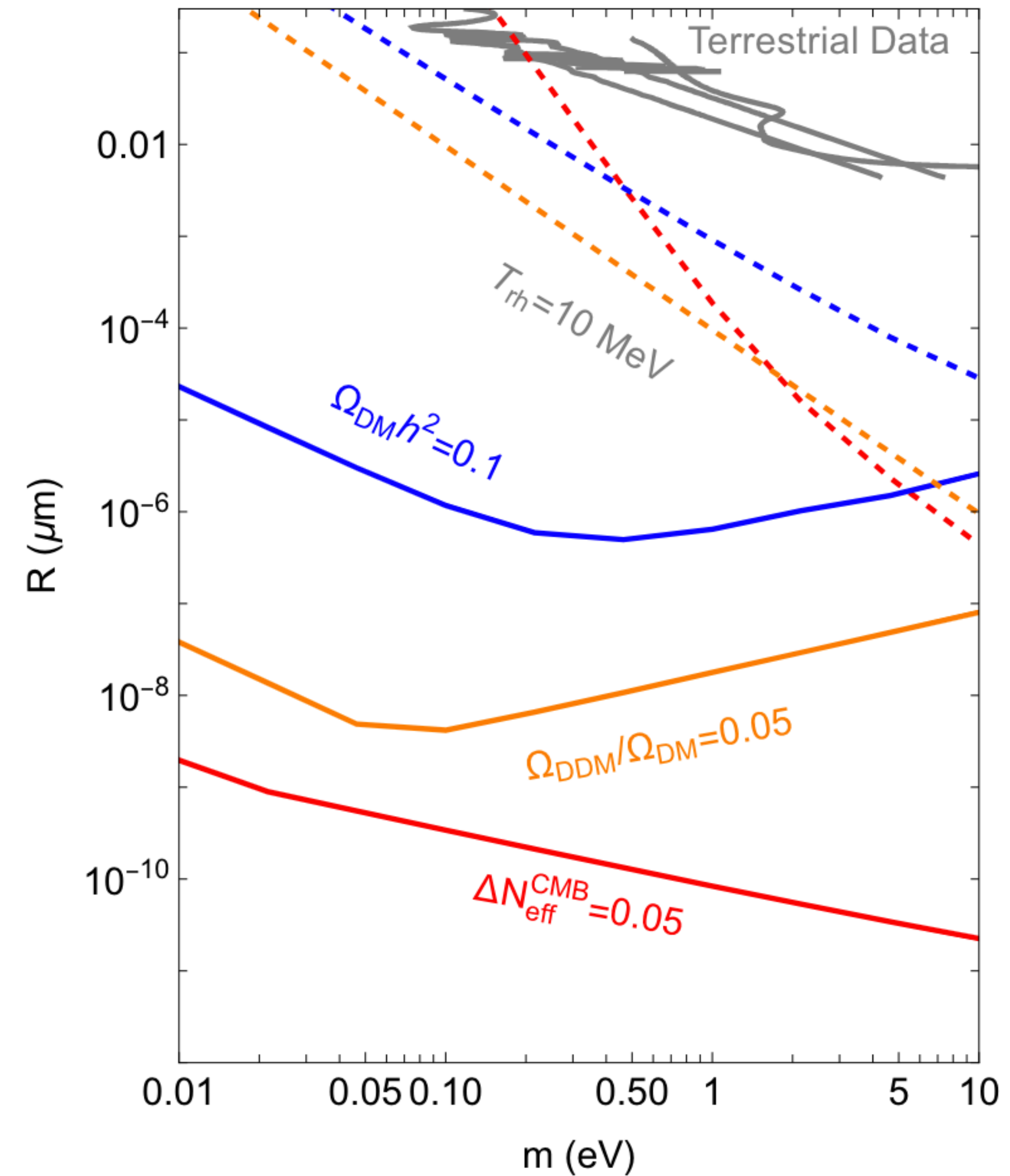
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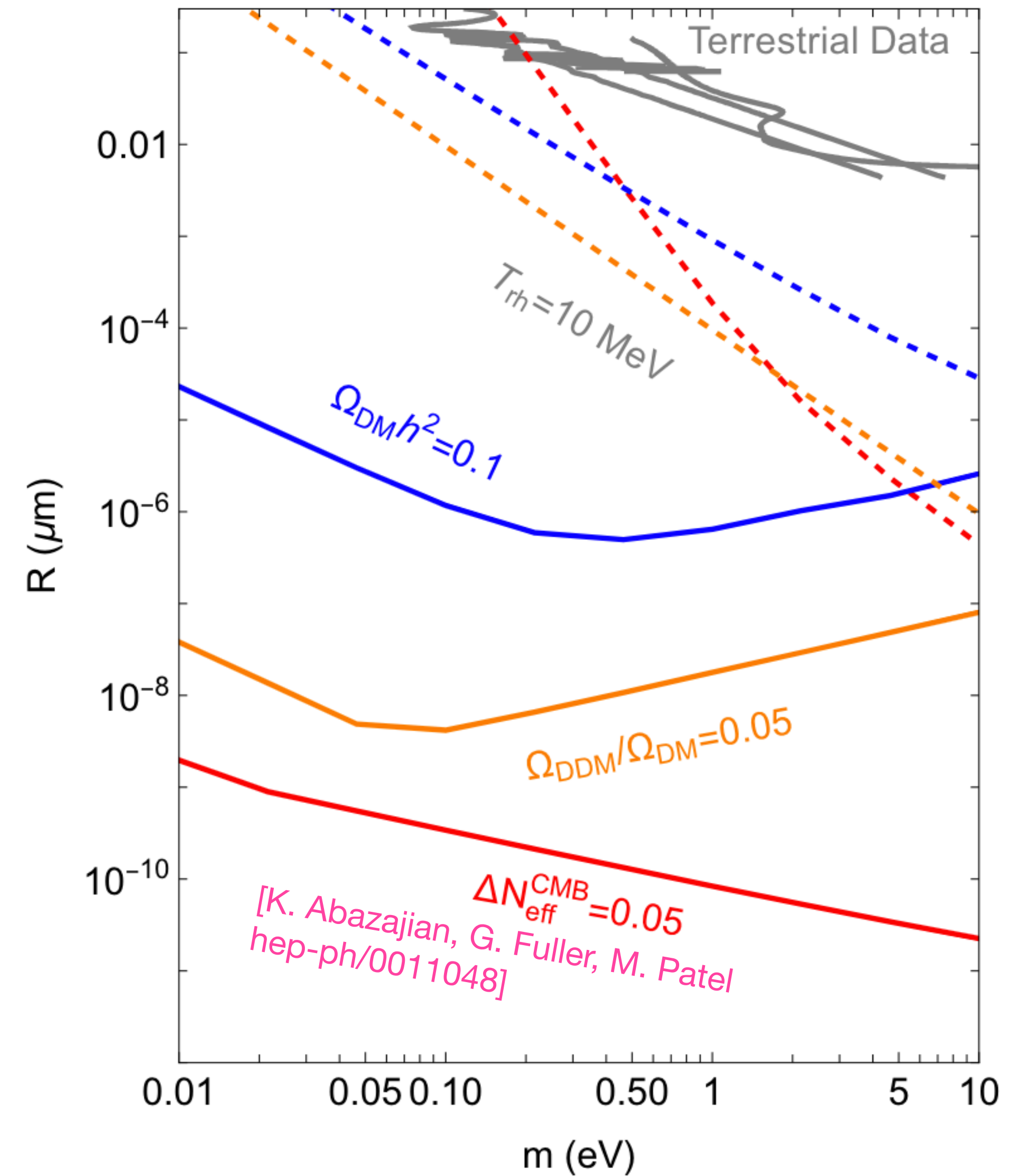


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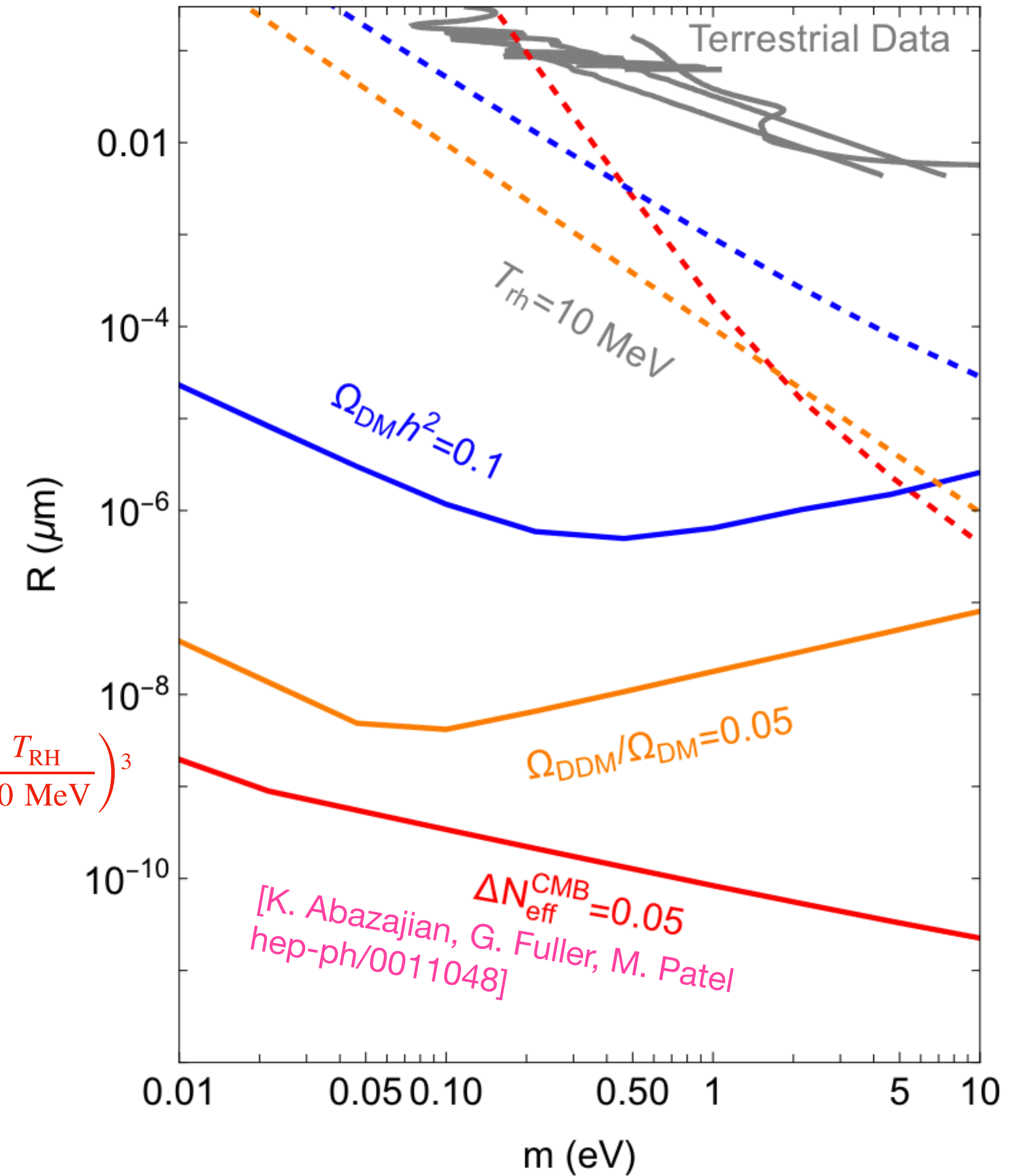
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Summary

- New physics with Dirac ν provide well-motivated explanation of m_ν
- New interactions can produce substantial numbers of ν_R which potentially thermalize
 - Upcoming cosmological surveys can probe Dirac ν !
- Future surveys may probe BSM physics through correlated observables
 - This diagnostic test can distinguish generic eV-scale relics ($m_{\text{relic}} \neq m_{\nu_L}$) from the DNH ($m_{\nu_L} = m_{\nu_R}$)
- Upcoming work explores the scenario in which many possibly non-degenerate eV-keV scale relics are produced alongside the degenerate ν_R
 - E.g. **will provide constraints on the size of dark dimensions, neutrino masses**

Thank you!

