

Ruprecht Machleidt



1. [arXiv:1202.2839](#) [pdf, other] [nucl-th](#) [nucl-ex](#) [doi](#) [10.1103/PhysRevLett.108.242501](#)

Continuum effects and three-nucleon forces in neutron-rich oxygen isotopes

Authors: G. Hagen, M. Hjorth-Jensen, G. R. Jansen, R. Machleidt, T. Papenbrock

Abstract: We employ interactions from chiral effective field theory and compute binding energies, excited states, and radii for isotopes of oxygen with the coupled-cluster method. Our calculation includes the effects of three-nucleon forces and of the particle continuum, both of which are important for the description of neutron-rich isotopes in the vicinity of the nucleus O-24. Our main results are the pla... [▽ More](#)

Submitted 11 June, 2012; **v1** submitted 13 February, 2012; **originally announced** February 2012.

Comments: 4 pages, 3 figures; small correction of effective 3NF and slight change of the corresponding parameters; updated figures and table; main results and conclusions unchanged

Journal ref: Phys. Rev. Lett. 108, 242501 (2012)

2. [arXiv:1204.3612](#) [pdf, other] [nucl-th](#) [doi](#) [10.1103/PhysRevLett.109.032502](#)

Evolution of shell structure in neutron-rich calcium isotopes

Authors: G. Hagen, M. Hjorth-Jensen, G. R. Jansen, R. Machleidt, T. Papenbrock

Abstract: We employ interactions from chiral effective field theory and compute the binding energies and low-lying excitations of calcium isotopes with the coupled-cluster method. Effects of three-nucleon forces are included phenomenologically as in-medium two-nucleon interactions, and the coupling to the particle continuum is taken into account using a Berggren basis. The computed ground-state energies and... [▽ More](#)

Submitted 15 June, 2012; **v1** submitted 16 April, 2012; **originally announced** April 2012.

Comments: 5 pages, 4 figures; small correction of effective 3NF and slight change of the corresponding parameters; updated figures and tables; main results and conclusions unchanged

Journal ref: Phys. Rev. Lett. 109, 032502 (2012)

3. [arXiv:1303.4674](#) [pdf, other] [nucl-th](#) [doi](#) [10.1103/PhysRevLett.110.192502](#)

An optimized chiral nucleon-nucleon interaction at next-to-next-to-leading order

Authors: A. Ekström, G. Baardsen, C. Forssén, G. Hagen, M. Hjorth-Jensen, G. R. Jansen, R. Machleidt, W. Nazarewicz, T. Papenbrock, J. Sarich, S. M. Wild

Abstract: We optimize the nucleon-nucleon interaction from chiral effective field theory at next-to-next-to-leading order. The resulting new chiral force NNLOopt yields $\chi^2 \approx 1$ per degree of freedom for laboratory energies below approximately 125 MeV. In the $A = 3, 4$ nucleon systems, the contributions of three-nucleon forces are smaller than for previous parametrizations of chiral interactions. We us... [▽ More](#)

Submitted 19 March, 2013; **originally announced** March 2013.

Comments: 6 pages, 4 figures

Journal ref: Phys. Rev. Lett. 110, 192502 (2013)

Error to report

- Our coupled-cluster computations with 3NFs in nuclear matter were wrong.
- Impact:
 - NNLO_{sat} has more accurate nuclear matter properties than previously reported
 - $\Delta\text{NNLO}_{\text{GO}}$ (which was fit to nuclear matter saturation) is overbound and saturates at too high density
- Errata have been published / are being prepared

Thanks to Weiguang Jiang, Francesco Marino , and Sam Novario for identifying this problem.

The magnetic dipole transition in ^{48}Ca – a mystery



Thomas Papenbrock

University of Tennessee & Oak Ridge National Laboratory

TRIUMF workshop on *Progress in Ab Initio Nuclear Theory*, 2/28/2024

Collaborators

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Sonia Bacca (Mainz)

Petr Navratil (TRIUMF)

Bijaya Acharya, Baishan Hu, S. Bacca, G. Hagen, P. Navratil, TP,
“The magnetic dipole transition in ^{48}Ca ,” arXiv:2311.11438

Why do people care about M1 transitions?

Supernova 1987A



February 24, 1987
Las Campanas Observatory

M1 spin excitations are dominated by isovector contributions.

The isovector-0 component of the Gamow-Teller operator translates to inelastic neutral-current neutrino-nucleus reactions at energies relevant for supernovae.

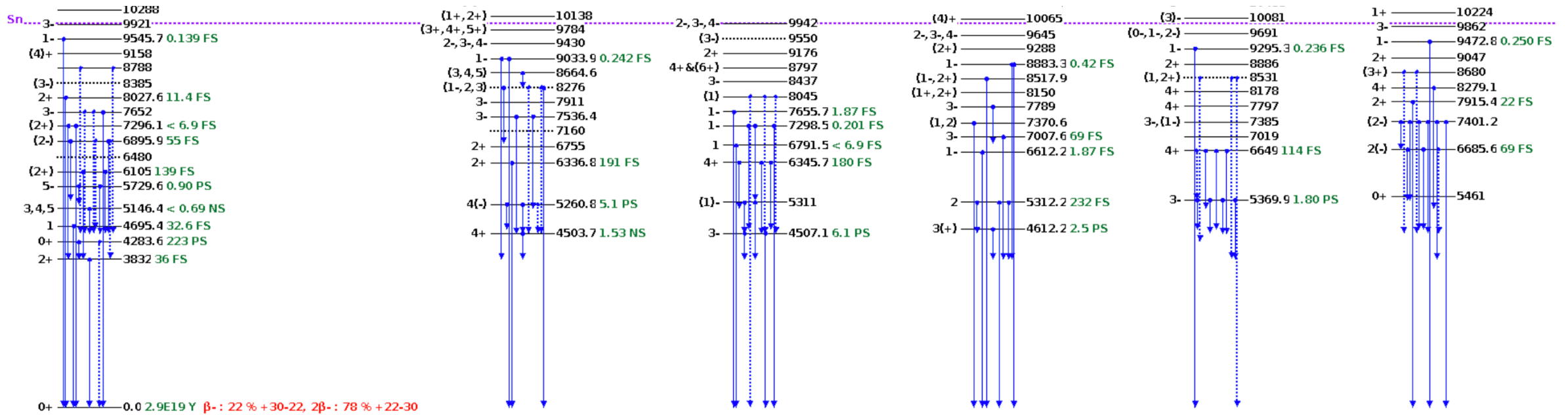
Our understanding of M1 impacts supernovae signals and dynamics.

Lüttge, von Neumann-Cosel, Neumeyer, Richter, Nucl Phys A (1996);
Langanke, Martinez-Pinedo, von Neumann-Cosel, Richter, Phys Rev Lett (2004);
Loens, Langanke, Martinez-Pinedo, Sieja, EPJA (2012);
Tornow et al, Phys Letts B (2022).

Review on *M1*:

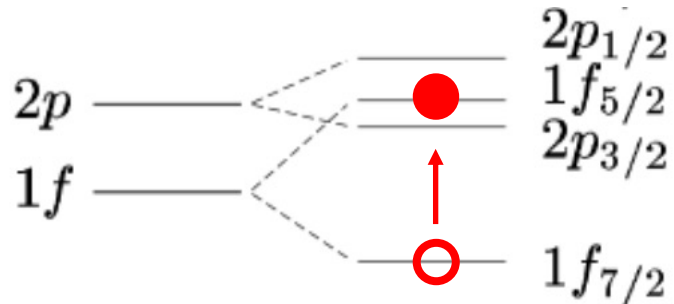
K. Heyde, P. von Neumann-Cosel, A. Richter, Rev. Mod. Phys. 82, 2365 (2010).

The resonant 1^+ state in ^{48}Ca at 10.224 MeV

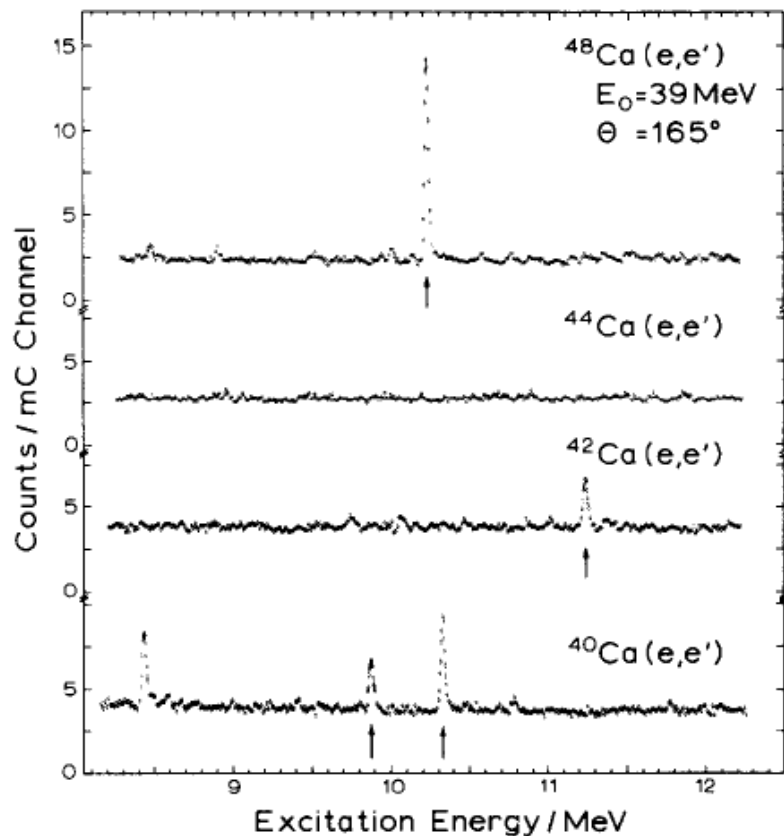


Scattering / reactions that probe the 1^+ state: (e, e') , (p, p') , (p, n) , or (γ, n)

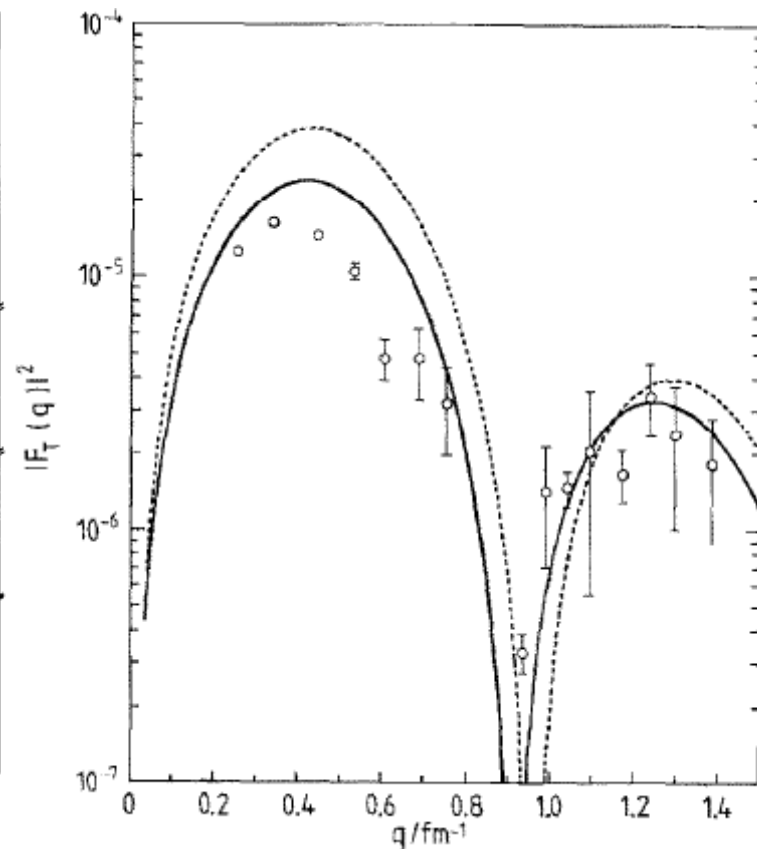
Simple picture of the 1^+ state: neutron 1p-1h excitation; extreme single-particle model: $B(M1) = 12 \mu_N^2$



The mystery

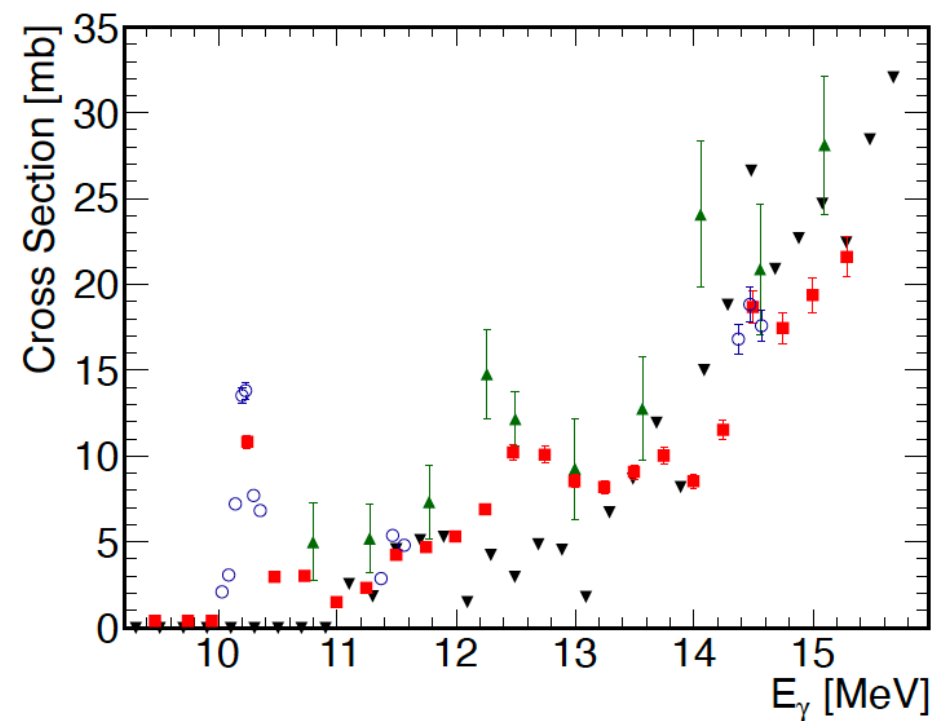


Steffen et al., Phys. Letts. B (1980)
 (e, e') scattering sees a peak,
 interpreted as M1 resonance



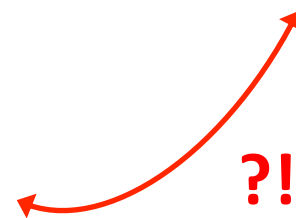
Steffen et al., Nucl. Phys. A (1983)
 form factor compared to shell
 model and quenched shell model

$B(M1) = 4.0 \pm 0.3 \mu_N^2$



Tompkins et al, Phys Rev C (2011)
 $^{48}\text{Ca}(\gamma, n)$ experiment yields

$B(M1) = 6.8 \pm 0.5 \mu_N^2$



The plot thickens

(e, e') scattering: $B(M1) = 4.0 \pm 0.3 \mu_N^2$ [Steffen et al 1980; 1983]

(γ, n) scattering: $B(M1) = 6.8 \pm 0.5 \mu_N^2$ [Tompkin et al 2011]

(p, p') scattering: $B(M1) = 3.85(32) - 4.63(38) \mu_N^2$ [Birkhan et al 2016]

Extreme s.p. model: $B(M1) = 12 \mu_N^2$

Theory has a hard time to reproduce a large amount of quenching

A. Harting, W. Weise, H. Toki, and A. Richter, Physics Letters B 104, 261 (1981).

J. B. McGrory and B. H. Wildenthal, Phys. Lett. B 103, 173 (1981).

Toru Suzuki, S. Krewald, and J. Speth, Physics Letters B 107, 9 (1981).

G. F. Bertsch, Nuclear Physics A 354, 157 (1981).

M. Kohno and D. W. L. Sprung, Phys. Rev. C 26, 297 (1982).

K. Takayanagi, K. Shimizu, and A. Arima, Nuclear Physics A 481, 313 (1988).

M. G. E. Brand, K. Allaart, and W. H. Dickhoff, Nuclear Physics A 509, 1 (1990).

B. A. Brown and W. A. Richter, Phys. Rev. C 58, 2099 (1998).

J. D. Holt, J. Menendez, J. Simonis, and A. Schwenk, Phys. Rev. C 90, 024312 (2014).

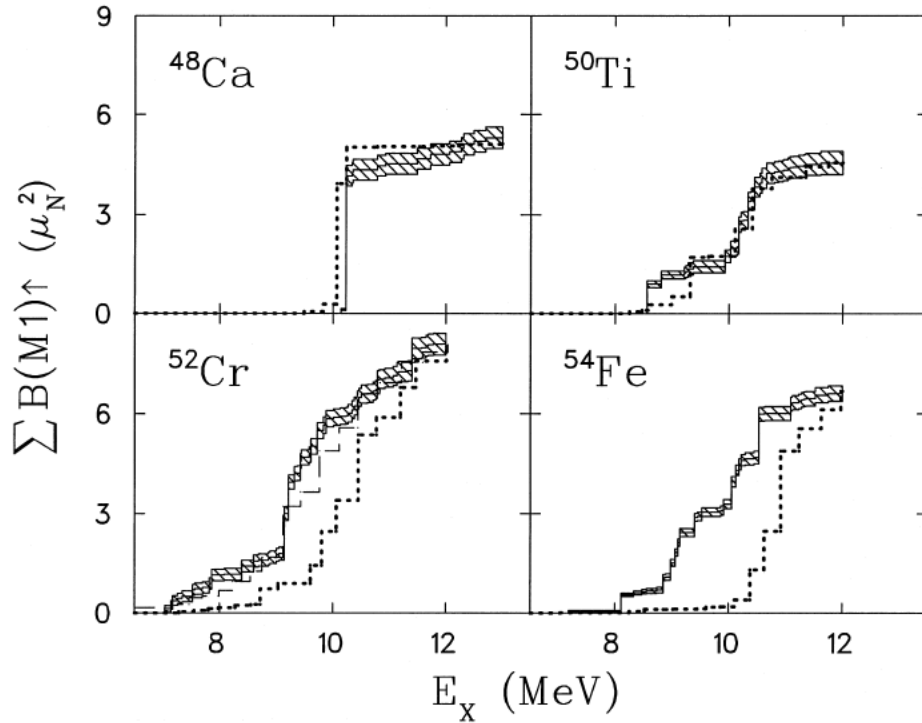
J. Wilhelmy, et al., Phys. Rev. C 98, 034315 (2018).

} Meson-exchange currents explain small $B(M1)$

} All too high $B(M1)$;
 $B(M1) = 7 - 8 \mu_N^2$;
 $B(M1) > 5.1 \mu_N^2$;

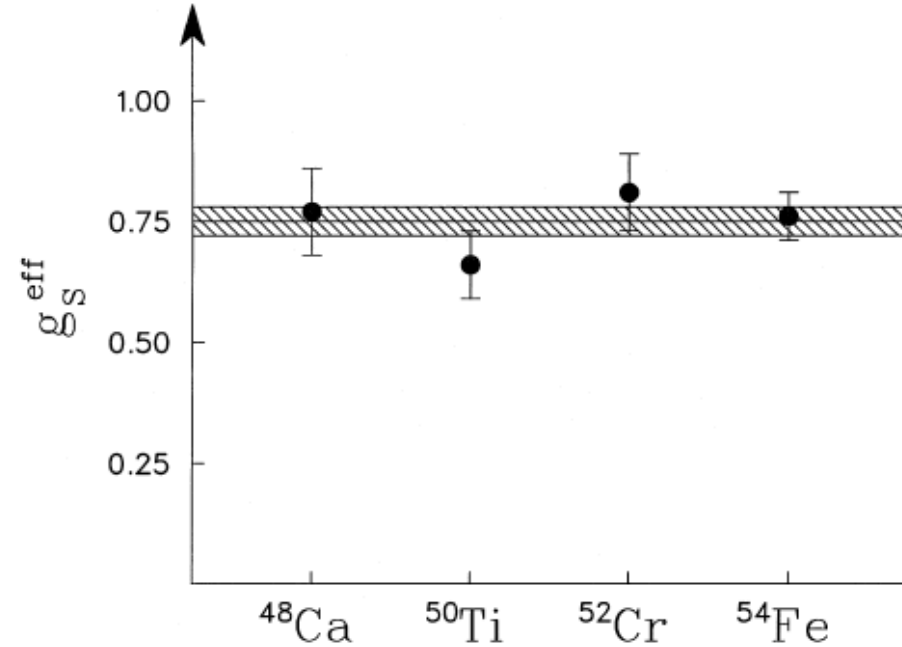
} Reproduce (e, e') $B(M1)$ if quenched

Why could/should there be quenching?



Results from (e, e') scattering match quenched shell-model results

Von Neumann-Cosel, Poves, Retamosa, Richter, Phys Letts B (1998)



Proposed: $B(M1)$ is quenched similarly to $B(GT)$ in pf shell nuclei

→ Impacts (re)analyses of (p, p') experiments using the “unit cross section” method

Two-body currents do not quench M1 transitions in light nuclei

$J_i^\pi \rightarrow J_f^\pi$	Method	IA	MEC				Total
			$\pi + \rho$	MS	MD	Δ	
${}^6\text{Li}(0^+; 1) \rightarrow {}^6\text{Li}(1^+; 0)$	VMC	3.683(14)	0.307	0.003	0.010	-0.053	3.950(14)
${}^6\text{Li}(0^+; 1) \rightarrow {}^6\text{Li}(1^+; 0)$	GFMC	3.587(16)	0.323	0.002	0.012	-0.048	3.876(14)
${}^7\text{Li}(\frac{1}{2}^-) \rightarrow {}^7\text{Li}(\frac{3}{2}^-)$	VMC	2.743(17)	0.396	0.006	-0.017	-0.034	3.162(22)
${}^7\text{Li}(\frac{1}{2}^-) \rightarrow {}^7\text{Li}(\frac{3}{2}^-)$	GFMC	2.677(19)	0.395	0.011	-0.017	0.072	3.138(22)
${}^7\text{Be}(\frac{1}{2}^-) \rightarrow {}^7\text{Be}(\frac{3}{2}^-)$	VMC	2.420(30)	0.390	-0.005	0.010	-0.024	2.791(36)
${}^7\text{Be}(\frac{1}{2}^-) \rightarrow {}^7\text{Be}(\frac{3}{2}^-)$	GFMC	2.374(31)	0.394	-0.010	0.010	-0.002	2.766(36)

Marcucci, Muslema Pervin, Pieper, Schiavilla,
Wiringa, Phys Rev C 78, 065501 (2008)

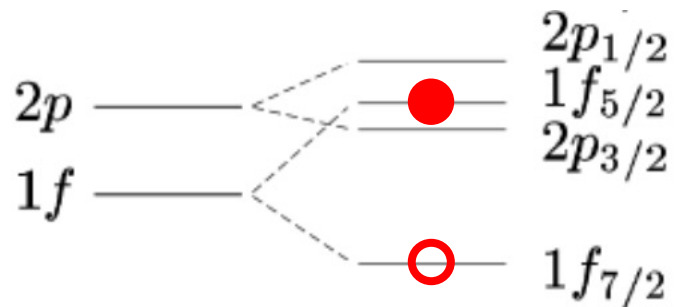
This is similar to
what we will use

This is perhaps
similar to what
people used in
the 1980s

Two-body currents for $M1$ transitions differ from those for Gamow-Teller transitions

An interesting and challenging problem... ...for *Ab Initio*

Conceptually simple:
neutron 1p-1h excitation
 $(a_{5/2}^+ \times a_{7/2})^{(1)} |^{48}\text{Ca}\rangle$



→ Coupled-cluster method
seems attractive for this

However: The excited 1^+ state
at $E_{1^+} = 10.224$ MeV is just
above the threshold for
neutron emission, and we
have $S_n = 9.952$ MeV

(It seems all previous
computations considered only
bound states)

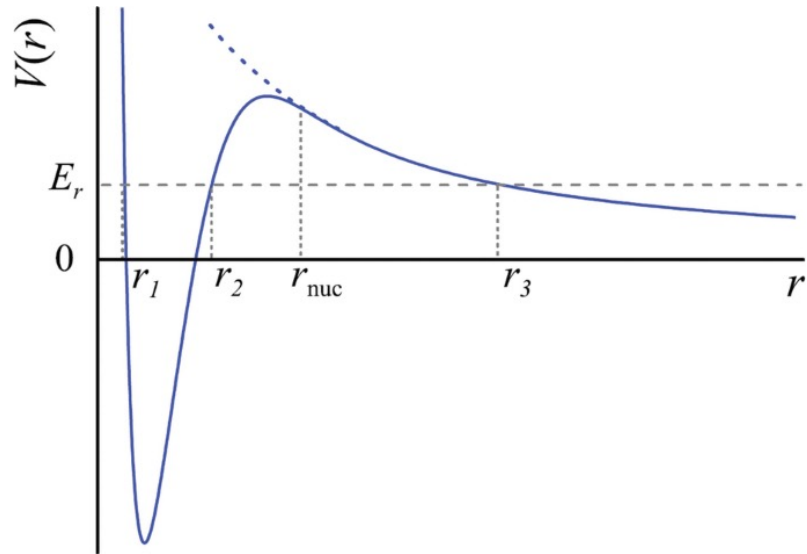
→ Need to use Gamow basis
that includes resonances and
continuum effects

...and: (e, e') and (p, p')
experiments indicated that a
lot of quenching is going on.

Where does this come from?

→ Need to include two-body
currents

The resonant 1^+ state in ^{48}Ca at 10.224 MeV

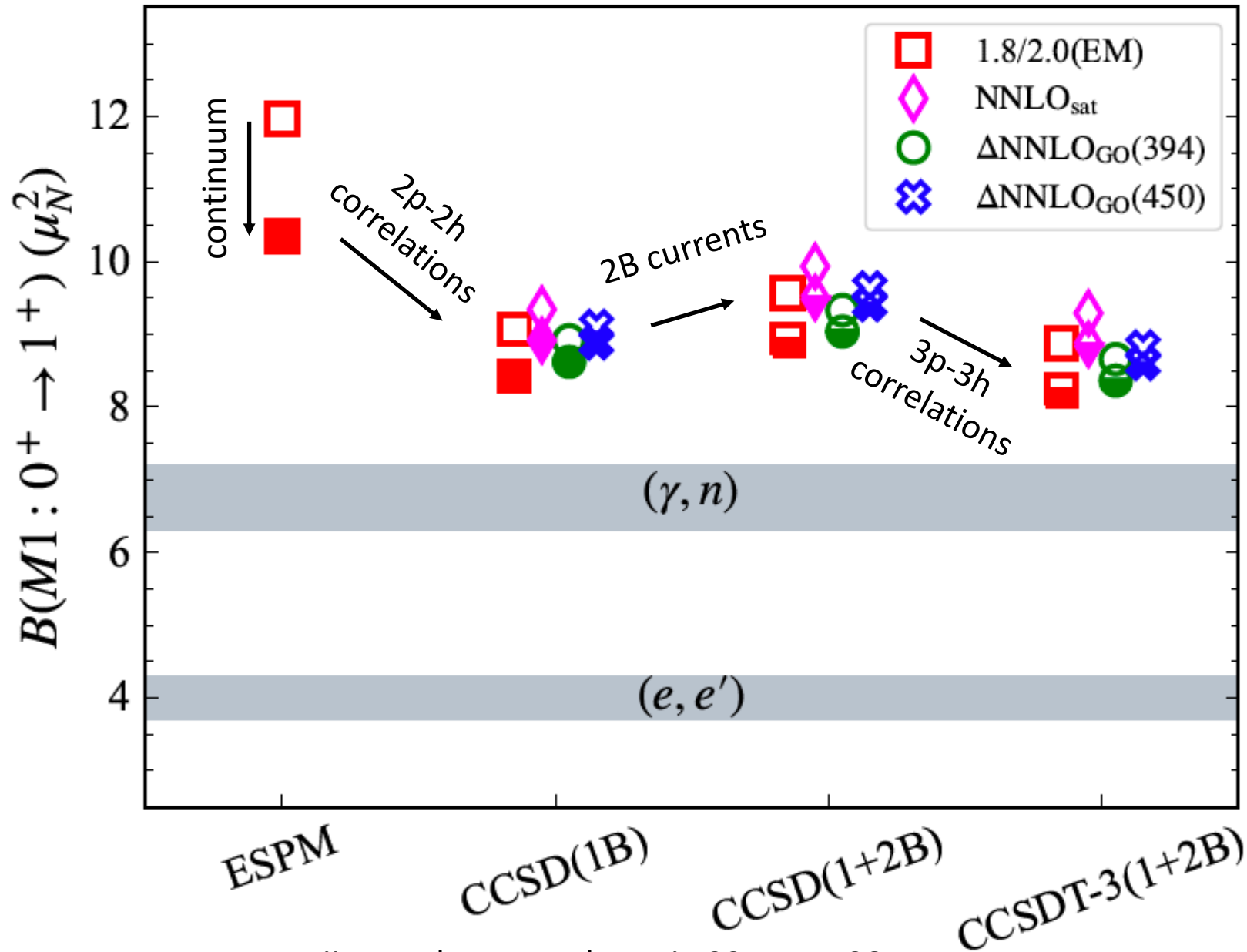


The $l = 3$ orbital angular-momentum barrier permits a neutron resonant state

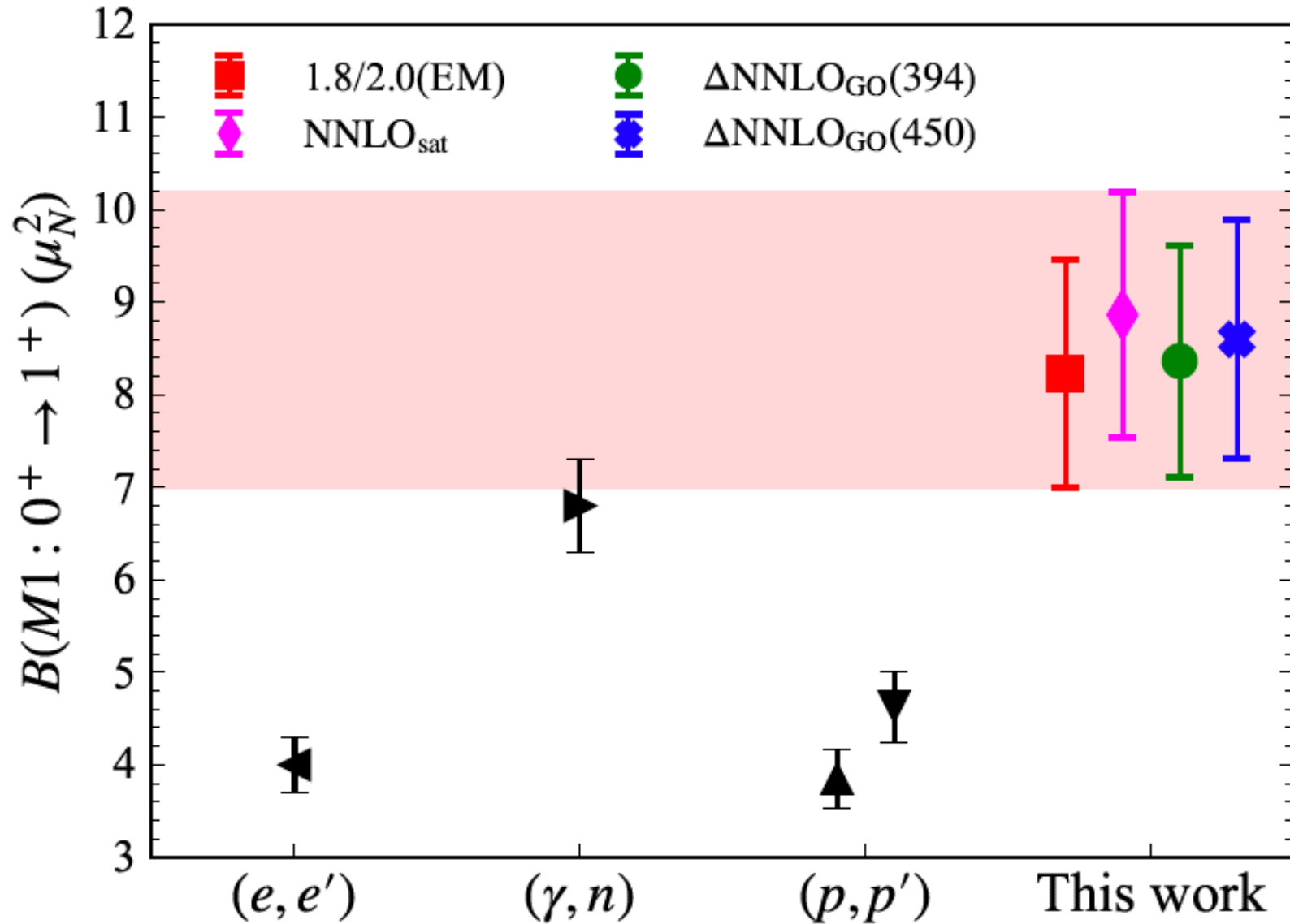
Interaction	S_n (MeV)	ΔE (MeV)	Γ (keV)	$1p-1h$
$\Delta\text{NNLO}_{\text{GO}}(394)$	9.74	-0.44	0	91%
$\Delta\text{NNLO}_{\text{GO}}(450)$	9.38	-1.26	0	91%
NNLO_{sat}	9.34	-0.23	0	91%
1.8/2.0(EM)	10.00	0.55	4	92%
Experiment	9.95	0.28	≤ 17	

Bijaya Acharya et al., arXiv:2311.11438

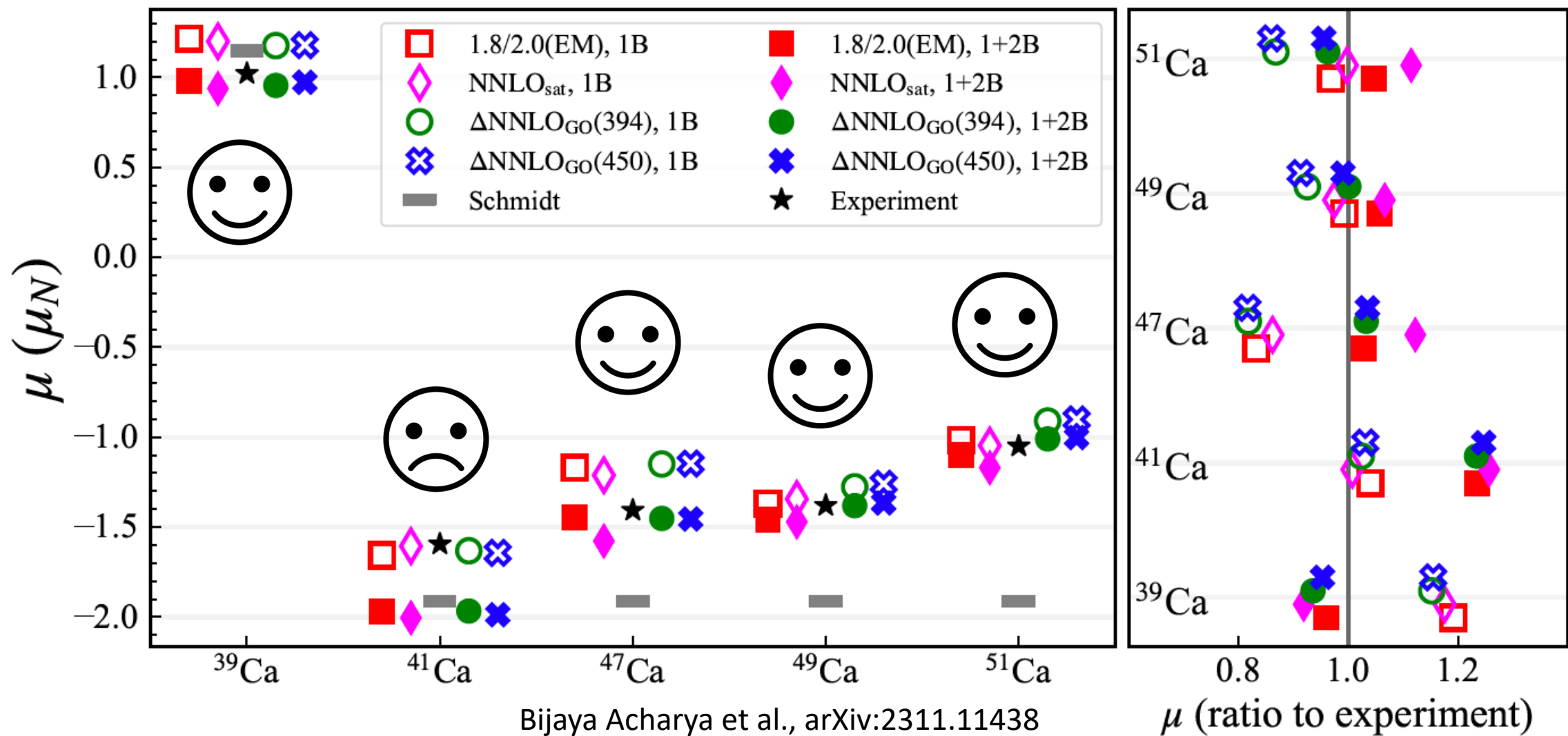
Contributions to $B(M1)$



Final result



Magnetic moments



Takayuki Miyagi et al., arXiv:2311.14383, propose that multi-shell VS-IMSRG calculation yields accurate results for ^{41}Ca .

Almost Summary

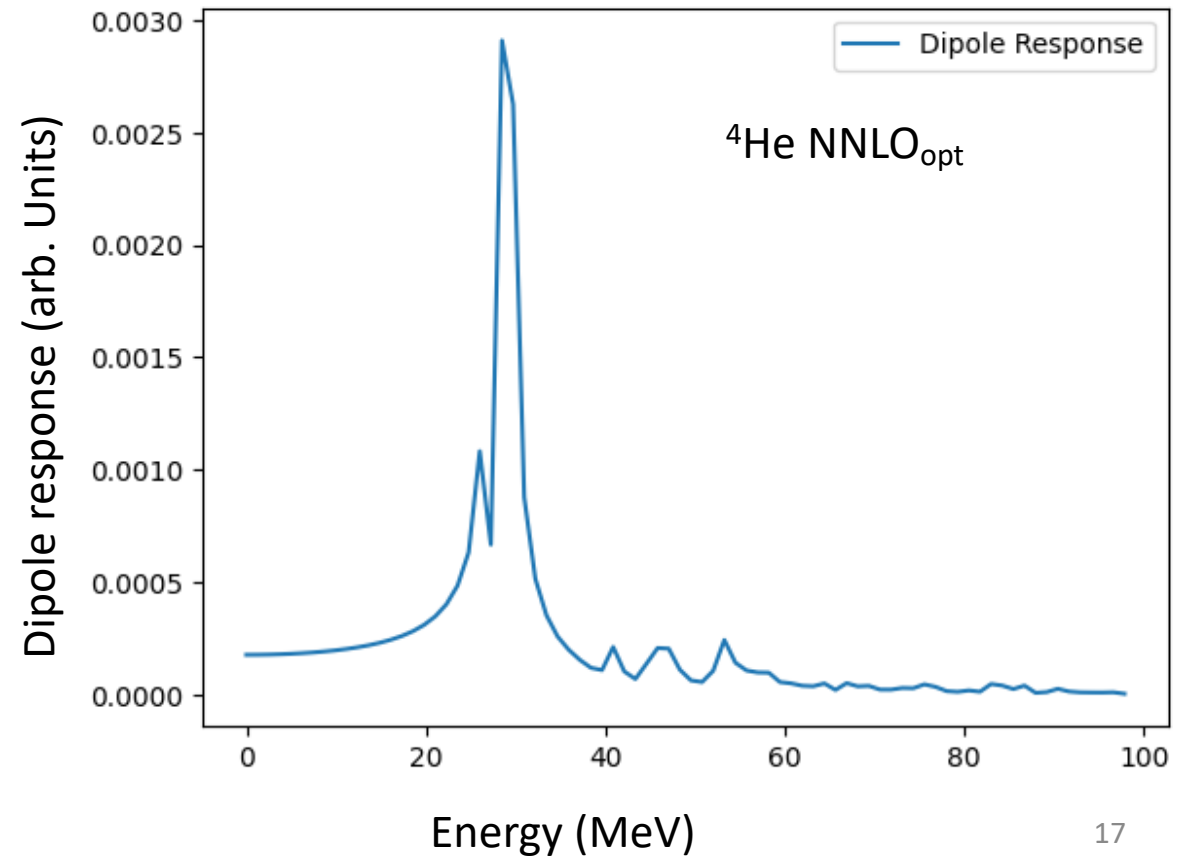
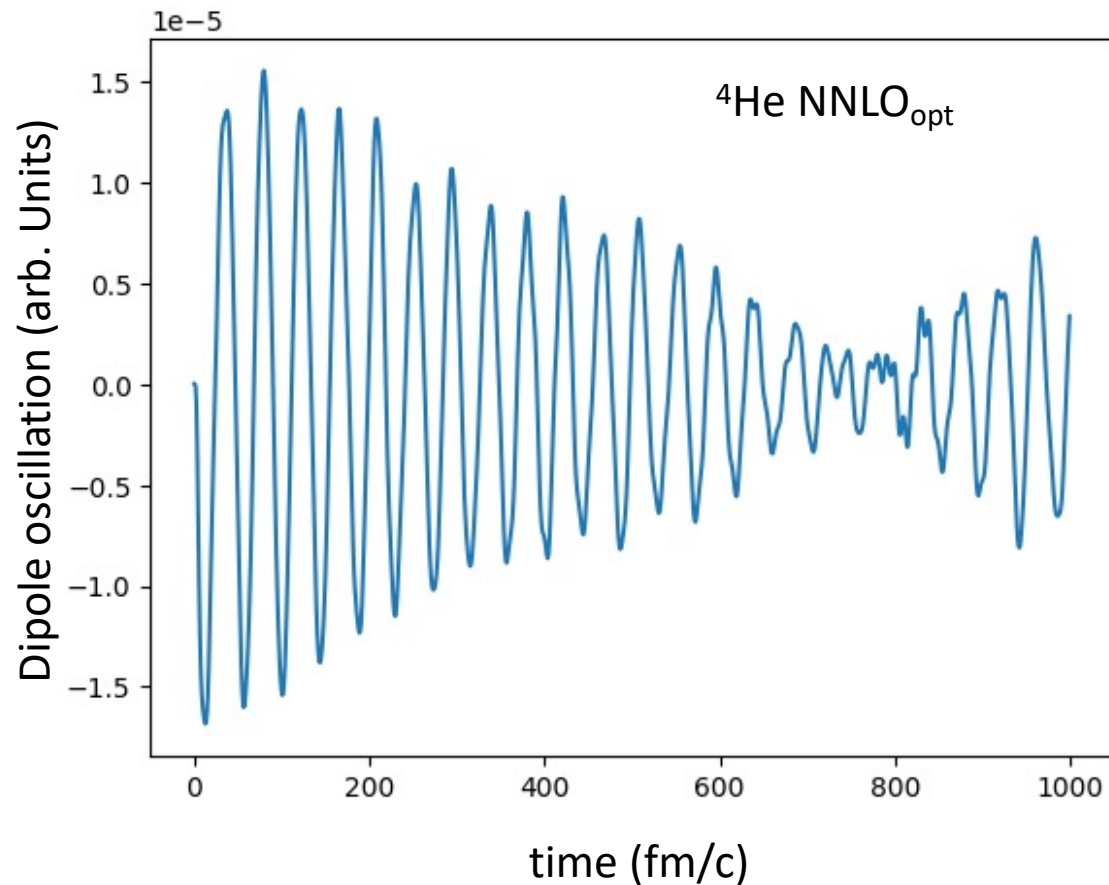
- The discrepancy between (e, e') and (γ, n) experiments regarding $B(M1)$ in ^{48}Ca is puzzling
- Our ab initio computations based on chiral effective field theory, including treatment of the state as a resonance, yield $7\mu_N^2 < B(M1) < 10\mu_N^2$
 - Two-body currents do not yield quenching of $B(M1)$
 - Similar to what was found in light nuclei
- Resolution of this puzzle will impact ab initio computations and/or theory of neutrino-nucleus reactions relevant for supernova signals and dynamics

Time-dependent coupled-cluster method

Dusted off (and updated!) time-dependent coupled cluster code [Pigg, Hagen, Nam, TP, Phys Rev C 2012].

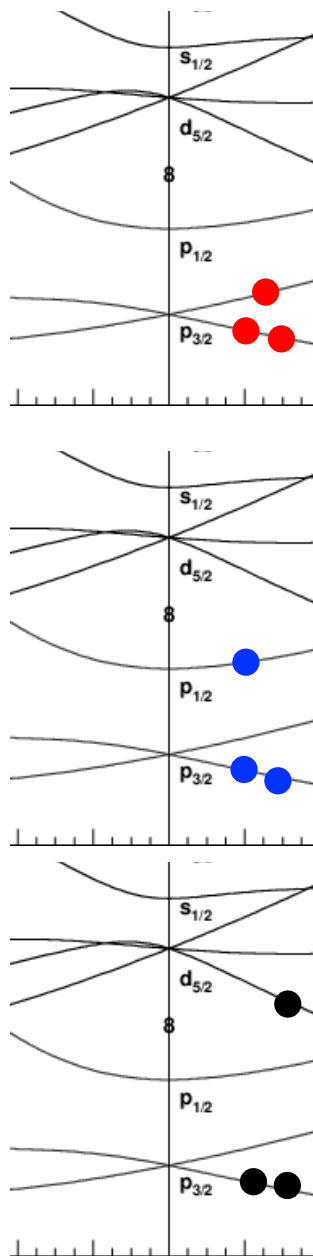
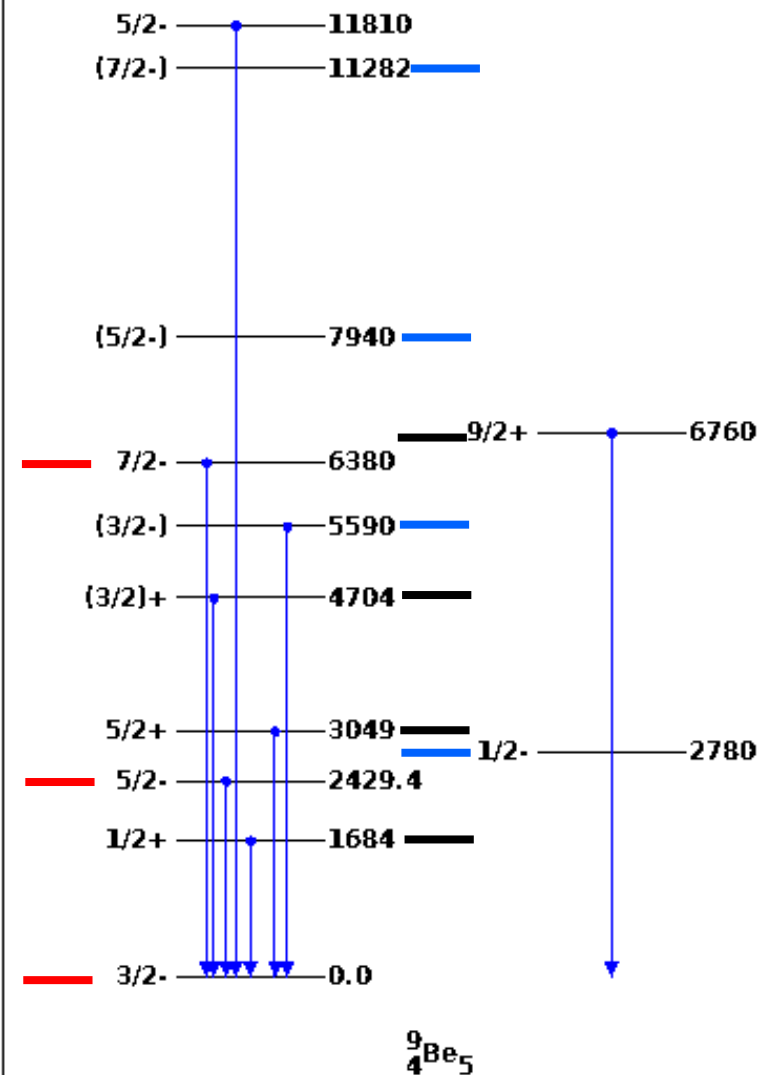
$$\overline{H}|\Phi\rangle = i\hbar e^{-S} \partial_t e^S |\Phi\rangle \qquad \overline{H} \equiv e^{-S} H e^S$$

Work in progress: Kyle Godbey, Gaute Hagen, TP preliminary

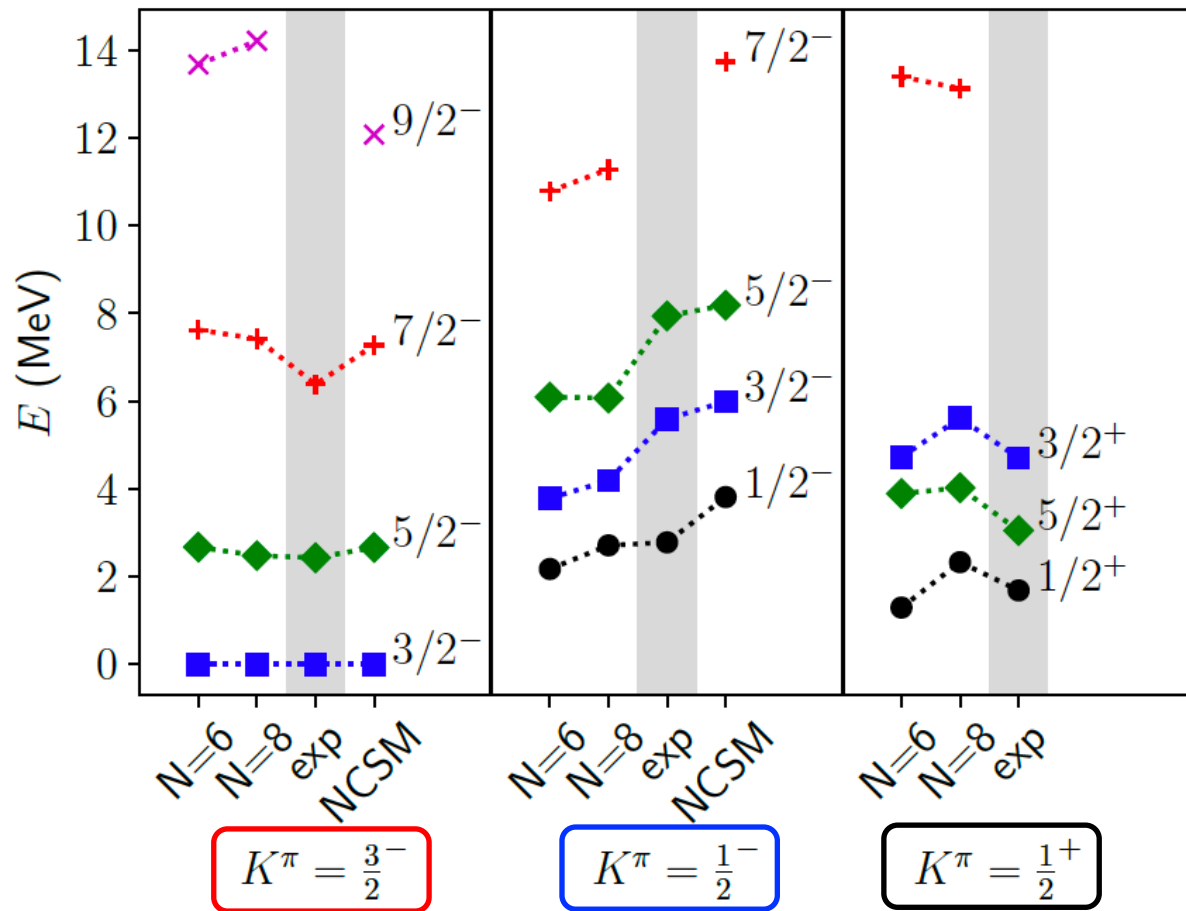


Making sense of spectra in odd-mass nuclei

Looks complicated;
shown data lacks understanding



Zhonghao Sun et al., in preparation
Hartree-Fock computations yield deformed reference
Coupled-cluster + projection yields bands



NCSM from Caprio, Maris, Vary & Smith,
Int. J. Mod. Phys. E 24, 1541002 (2015)

Summary

- The discrepancy between (e, e') and (γ, n) experiments regarding $B(M1)$ in ^{48}Ca is puzzling
- Our ab initio computations based on chiral effective field theory, including treatment of the state as a resonance, yield $7\mu_N^2 < B(M1) < 10\mu_N^2$
 - Two-body currents do not yield quenching of $B(M1)$
 - Similar to what was found in light nuclei
- Resolution of this puzzle will impact ab initio computations and/or theory of neutrino-nucleus reactions relevant for supernova signals and dynamics
- Dusted off time-dependent coupled-cluster code; response functions soon; want to join the movie-making business later
- Odd mass deformed nuclei

Thank you!