

# Semileptonic B decays - Experimental Status

## FPCP-2019



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(On behalf of Belle Collaboration also including material from LHCb and BaBar)



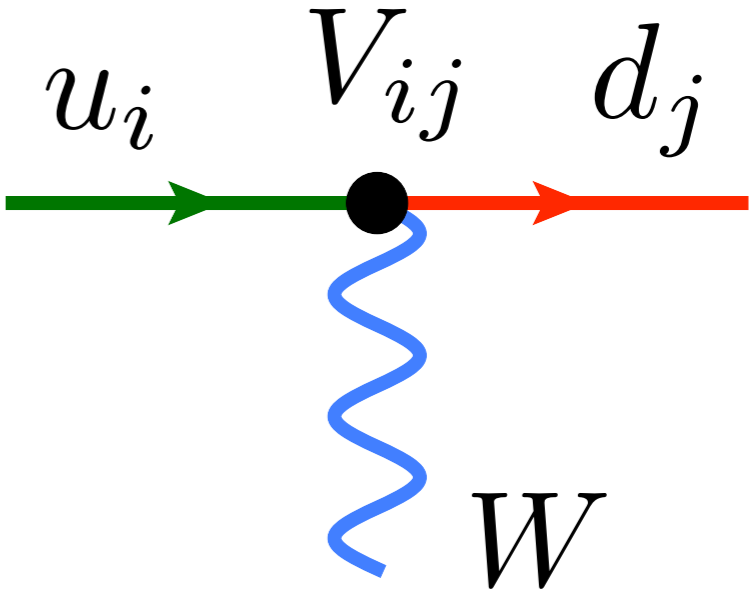
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# CKM Quark Mixing

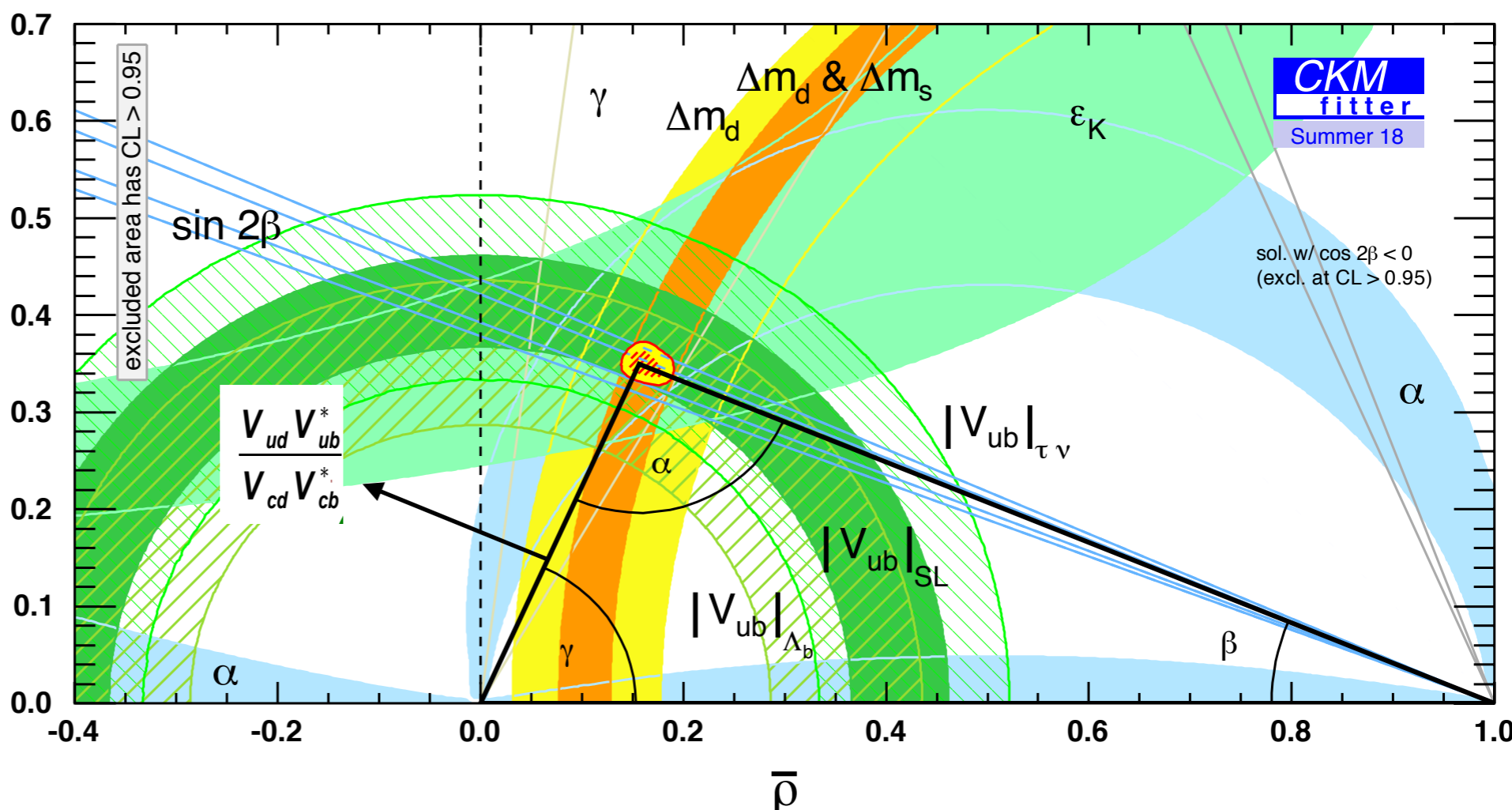
## Importance of $|V_{cb}|$ and $|V_{ub}|$

- Test of CKM sector
- So far huge success for SM
- New Physics still possible within current precision
- $|V_{ub}|$  has largest error among parameters of UT

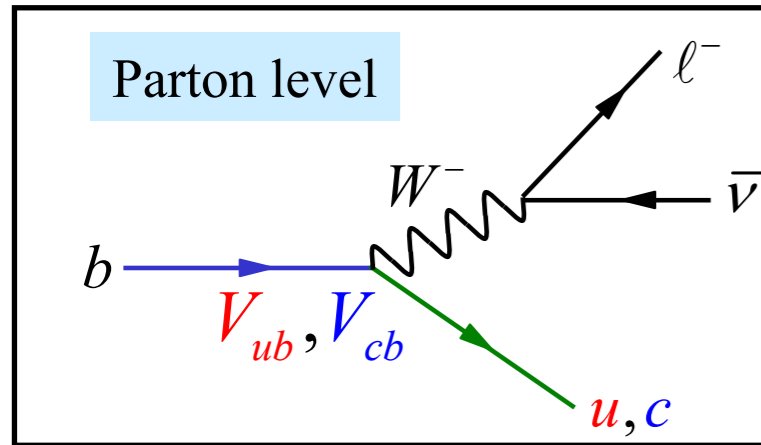


## $|V_{qbl}|$ current precision

$|V_{ub}|$  exlc.  $\sim 4\%$ ,  $|V_{cb}| \sim 2\%$ ,

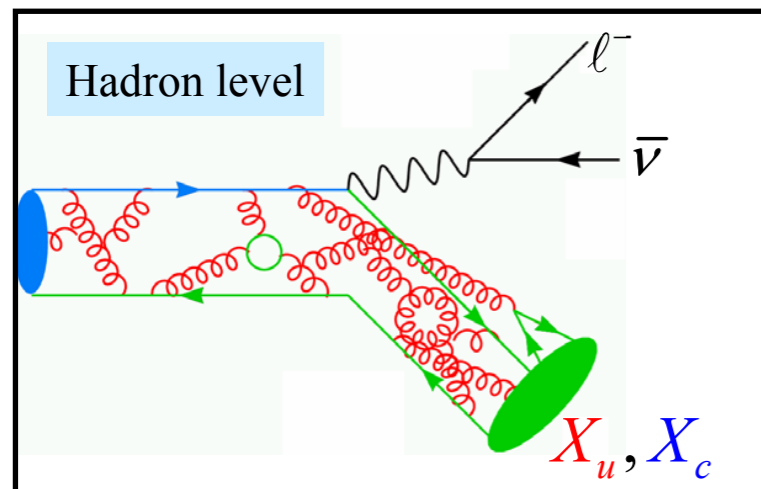


# Semileptonic B decays



Decay properties depend on  $|V_{cb}|$  &  $|V_{ub}|$  and  $m_b$

perturbative regime



But quarks are bounded by soft gluons: non-perturbative

+long distance interactions of b quark with light quark

- Decay rate  $\Gamma_X \equiv \Gamma(b \rightarrow Xl\nu) \propto |V_{xb}|^2$
- $\Gamma_c$  larger than  $\Gamma_u$  by a factor  $\sim 50$
- Extracting  $b \rightarrow \mu l \nu$  signal challenging

## Semileptonic B decays from HFLAV<sup>[1]</sup>

$$B^0 \rightarrow D^{*-} l \nu_\ell = 5.05 \pm 0.02 \pm 0.14$$

$$B^+ \rightarrow \bar{D}^{*0} l \nu_\ell = 5.66 \pm 0.07 \pm 0.21$$

$$B^0 \rightarrow D^- l \nu_\ell = 2.31 \pm 0.04 \pm 0.09$$

$$B^+ \rightarrow \bar{D}^0 l \nu_\ell = 2.35 \pm 0.03 \pm 0.09$$

$$\mathcal{B}(\bar{B} \rightarrow X_c l^- \bar{\nu}_\ell) = (10.65 \pm 0.16)\%$$

$$\mathcal{B}(\bar{B} \rightarrow \pi l^- \bar{\nu}_\ell) = (1.47 \pm 0.06) \times 10^{-4}$$

$$\mathcal{B}(B \rightarrow X_u l \nu) = (1.86 \pm 0.10 \pm 0.14) \times 10^{-3}$$

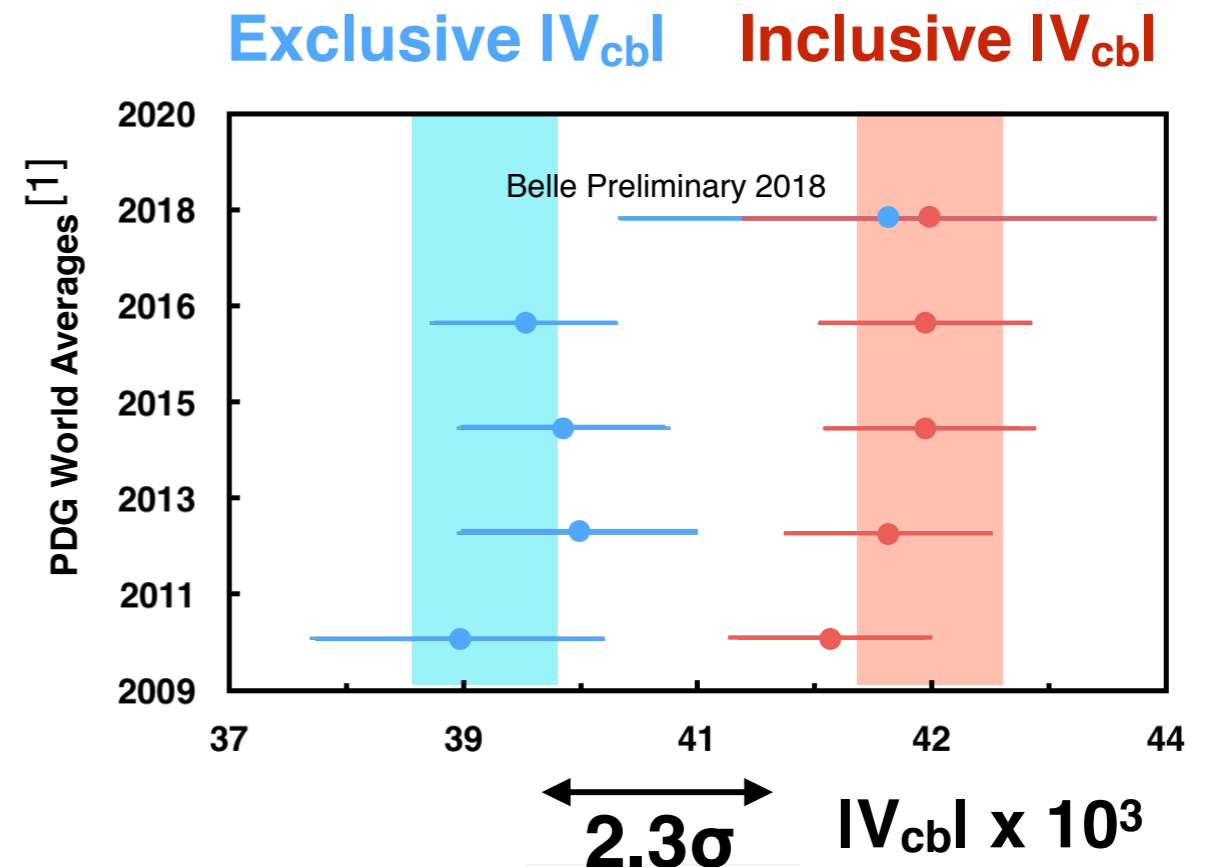
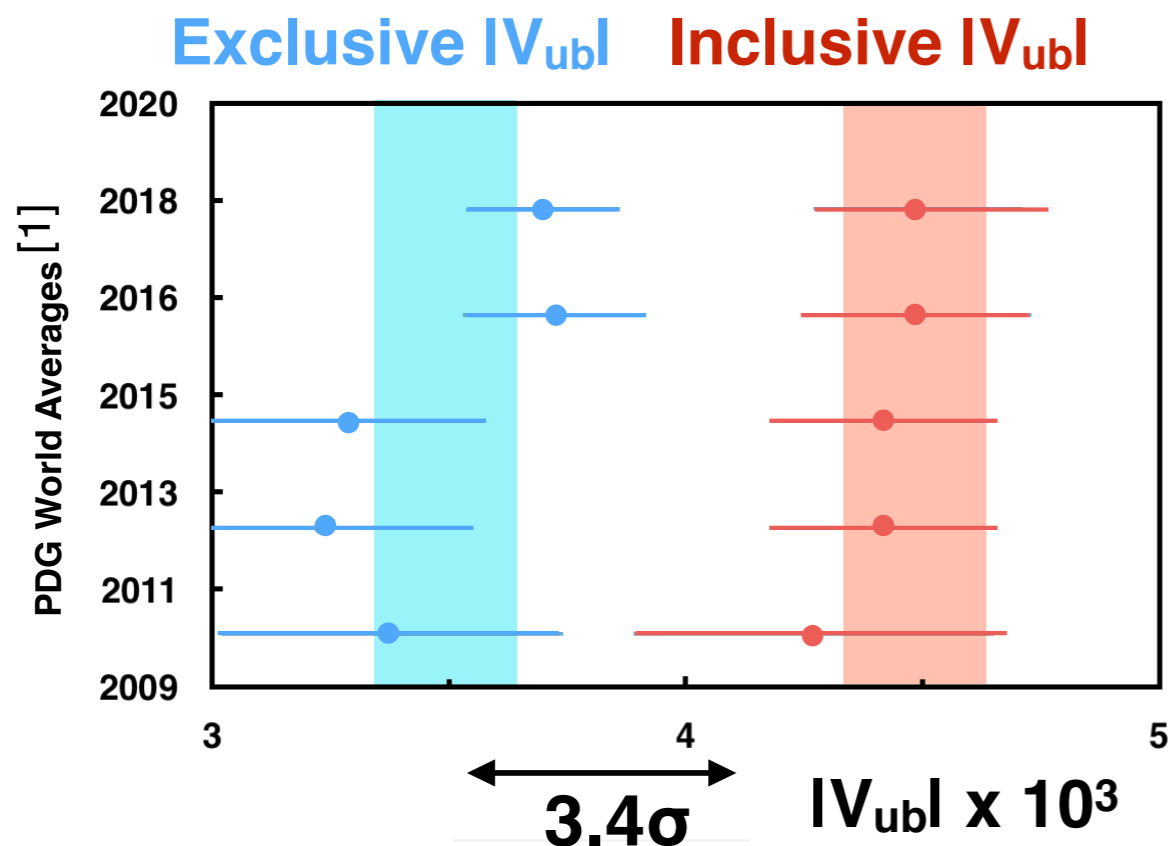
# A persistent puzzle in $IV_{xb}$ determination

## Inclusive Approach ( $B \rightarrow X_c l \nu$ )

- B Meson acts like a b quark which means that the decay can be described as  $b \rightarrow c, u$  quark transition.
- Calculated with Heavy Quark Expansion. (Phys.Rev.Lett. 114 (2015), 061802)

## Exclusive Approach $B \rightarrow D^* l \nu / B \rightarrow \pi l \nu$

- Hadronic transitions for  $B \rightarrow D^*/B \rightarrow \pi$  described with form factors. LQCD and LCSR
  - Theoretically calculable at **kinematical limits**
  - Lattice QCD works if  $D^*$  or  $\pi$  is at rest relative to  $B$  (arXiv:1203.1204)

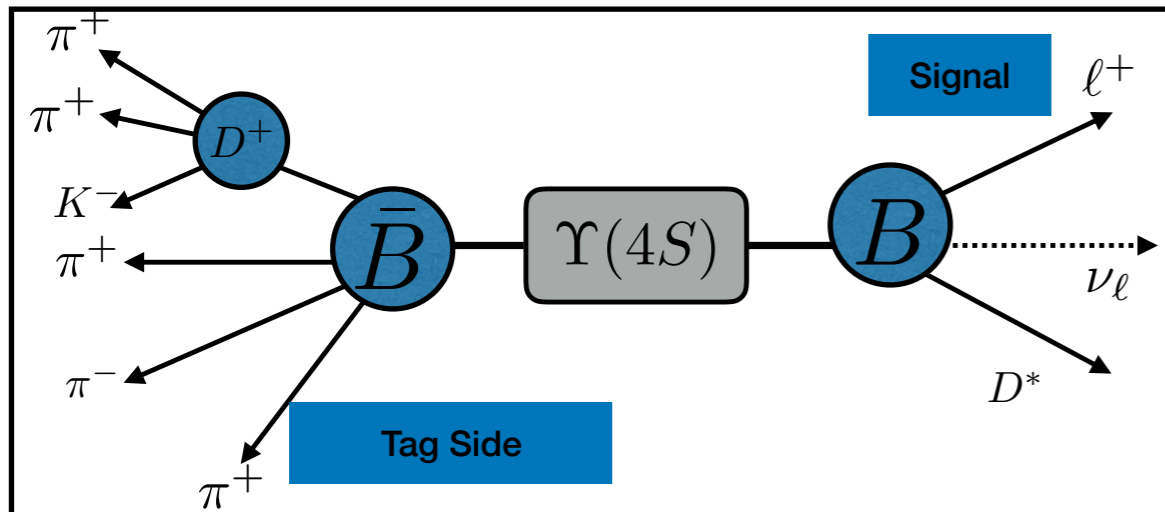


# Experimental Measurements at Belle/BaBar

## Tagged Measurement

One B reconstructed completely in a known  $b \rightarrow c$  mode without  $\nu$ . “B-meson Beam”

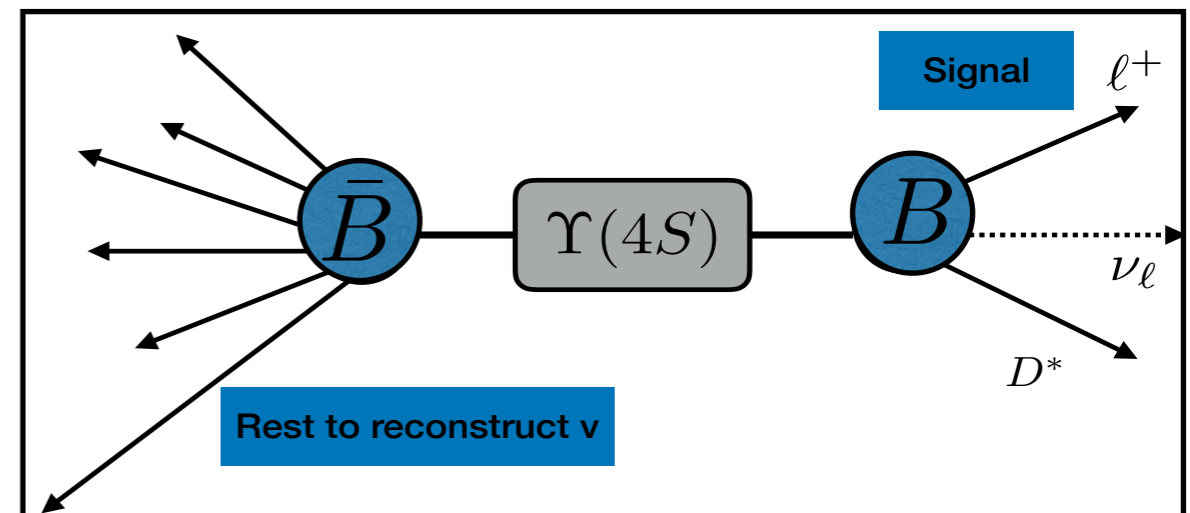
- High purity, very small background
- Low Efficiency, large stat. errors



## Untagged Measurement

Initial 4 momentum known, missing 4-momentum =  $\nu$   
Reconstructed  $B \rightarrow X_q \ell \nu$   
Other side information to constrain signal B flight direction

- High efficiency
- Low purity, large background



## Basic Analysis Steps

- Reconstruction
- Projection into bins of kinematic variables
- Fitting signal yield
- Compare measured events to expected events (Fit to calculate  $IV_{cbl}$  and  $IV_{ubl}$ )

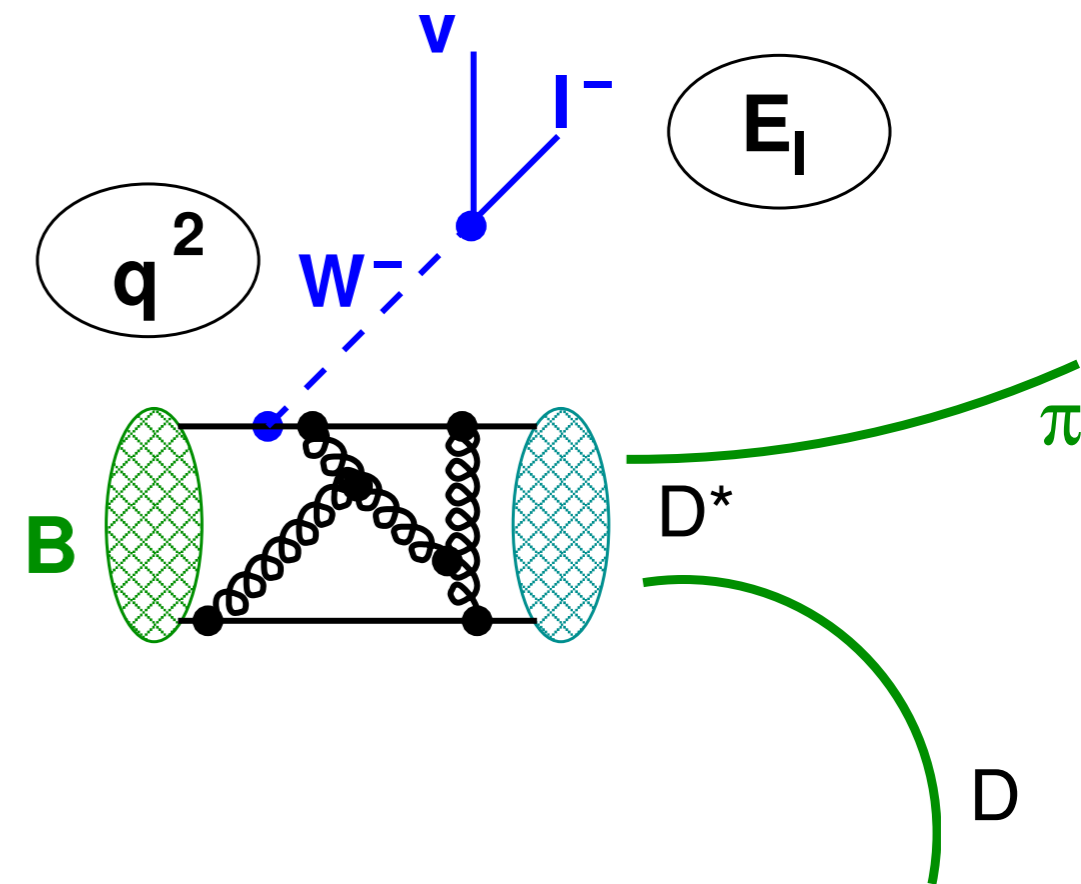
# Recent Semileptonic Measurements at B Factories

- $B \rightarrow D^* \ell \nu$  BaBar tagged 2019 (arXiv:1903.10002, submitted to PRL)
- $B^0 \rightarrow D^{*-} \ell^+ \nu_\ell$  Belle untagged 2018/2019 (arXiv:1809.03290, submitted to PRD)
- Measurement of shape of  $\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}$  differential decay rate (arXiv:1709.01920 Phys. Rev. D 96, 112005 (2017))
- $D^{*-}$  polarisation in  $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$  arXiv:1903.03102
- $B \rightarrow D^* \pi \ell \nu_\ell$  Belle hadronic tagged 2018 (arXiv:1803.06444, Phys. Rev. D 98, 012005 (2018))
- Relative  $B^- \rightarrow D^0 / D^{*0} / D^{**0} \mu^- \nu_\mu$  branching fractions (arXiv:1807.10722, submitted to PRD)
- Inclusive  $|V_{ub}|$  BaBar tagged 2019 (arXiv:1611.05624, Phys. Rev. D 95, 072001(2017))

IVcbl

# Semileptonic Observables

- Four momentum of **charged lepton**
  - Experimentally: good LeptonID to minimise fakes
- Four momentum of **hadronic system**
  - Experimentally: slow pion momentum - important for measurement at low recoil
- Momentum transfer to leptonic system



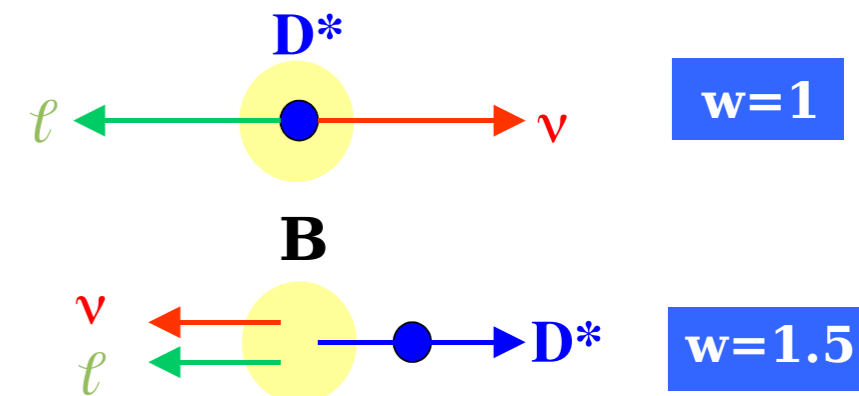
- $q^2 = (p_l + p_\nu)^2$

- Hadronic recoil

- $w \equiv v_B \cdot v_{D^*} = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$

- For  $B^0 \rightarrow D^{*-} \ell^+ \nu$  :  $1 < w < 1.504$

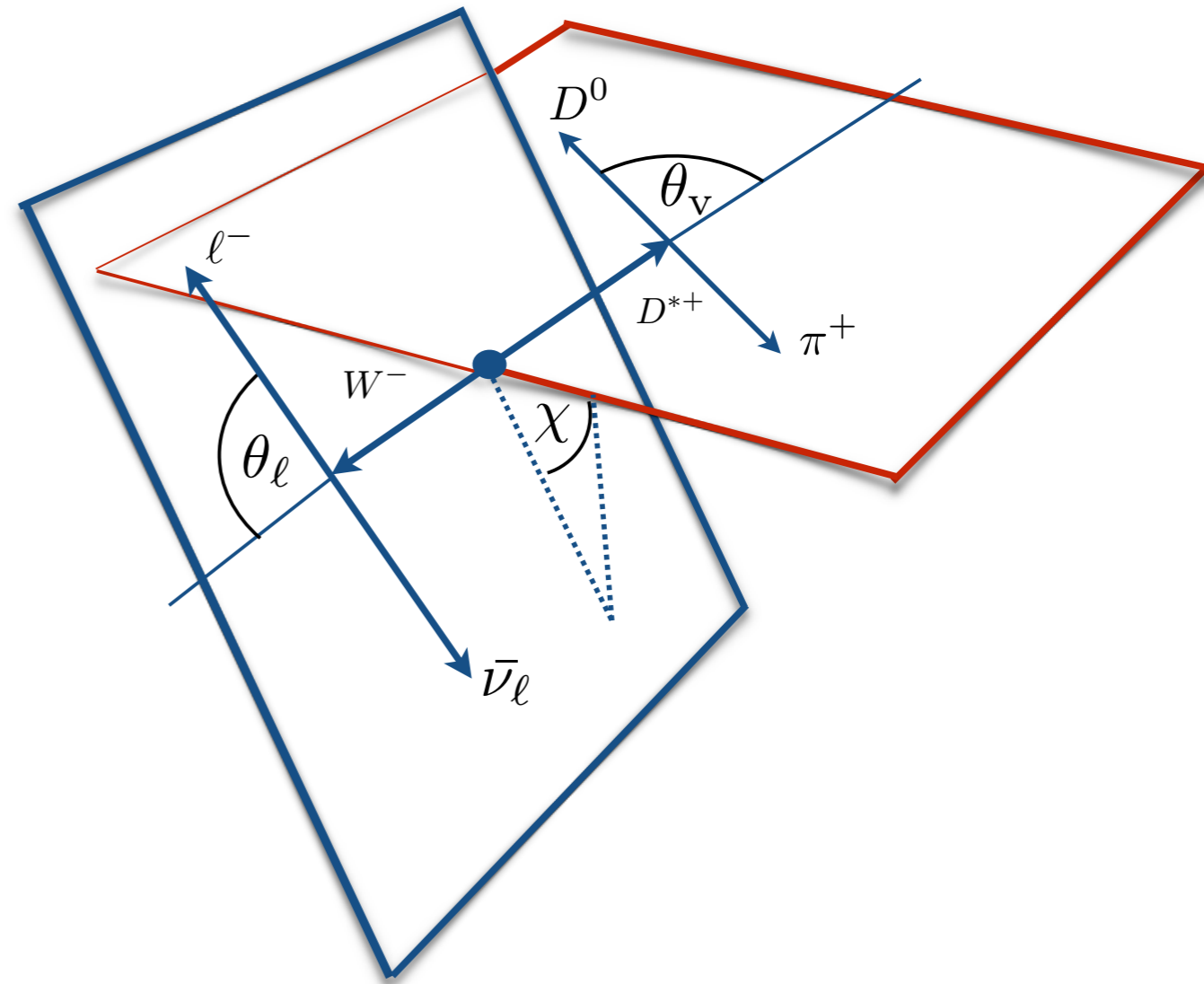
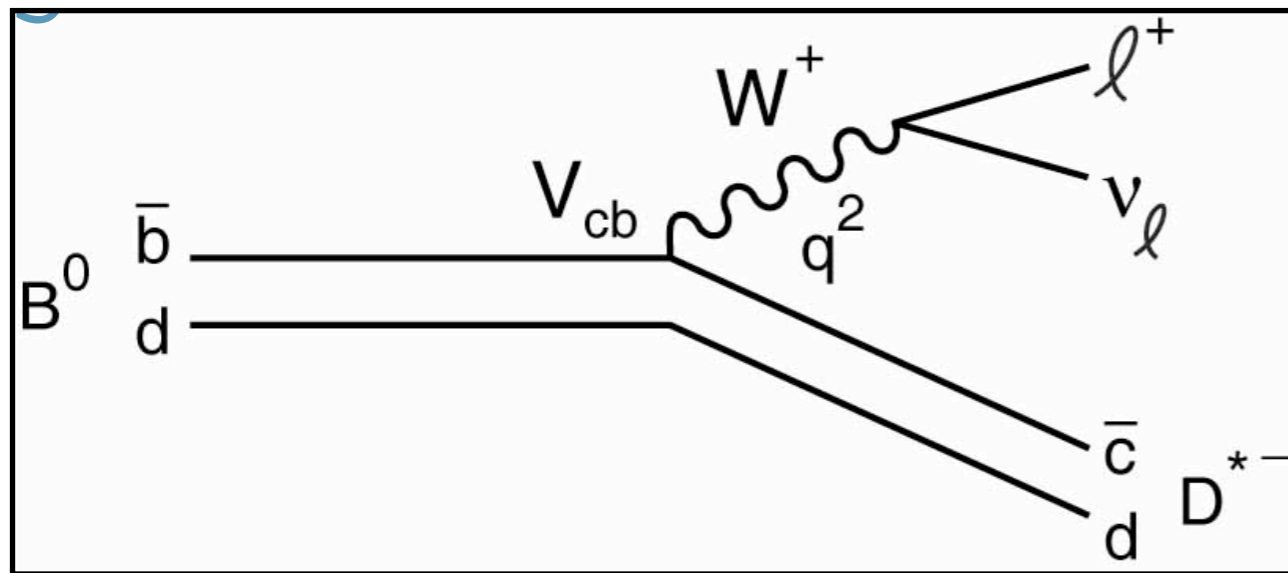
- Normalisation ( $w = 1$ ) = 1 (Heavy quark limit)





# $|V_{cb}|$ and Decay Rate of

$$B^0 \rightarrow D^{*-} \ell^+ \nu_\ell$$



Differential Decay rate

$$\frac{d\Gamma(B^0 \rightarrow D^* \ell^+ \nu_\ell)}{dw d\cos\theta_\ell \cos\theta_V d\chi} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} F(w, \theta_\ell, \theta_V, \chi) G(w)$$

Form factor of  $B \rightarrow D^*$  transition

phase space (known)

In case of  $B \rightarrow D \ell \nu$  decay rate only depend on  $w$ .

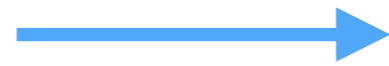
# Form factor parameterisation

Caprini, Lelouch, Neubert (CLN)

arXiv:hep-ph/9712417,  
Nucl.Phys. B530 (1998)

Theoretical assumptions used to reduce the number of free parameters describing form factors: to measure  $|V_{cb}|$  with a smaller data set

$F(w, \theta_\ell, \theta_V, \chi)$



3 non trivial form factors  $A_1(w)$ ,  
 $A_2(w)$  and  $V(w)$

$$R_1(w) = V/A_1$$

$$R_2(w) = A_2/A_1$$

$$\rho^2(w) = -dF/dw|_{w=1}$$

$F(w)$  normalised at zero recoil ( $w=1$ )

Boyd Grinstein Lebed (BGL)

arXiv:hep-ph/9504235,  
Phys.Lett.B353:306-312,1995

$F(w, \theta_\ell, \theta_V, \chi)$  is written as the most generic parameterisation with minimal theory assumptions, the expansion is constrained by unitarity (can have more coefficients than CLN at  $O(3)$ )

# Form factor parameterisation: CLN Vs BGL

- CLN arXiv:hep-ph/9712417,  
Nucl.Phys. B530 (1998)

- HQET relations + corrections  
in powers of  $\Lambda_{\text{QCD}}/m_b$ ,

- For  $B \rightarrow D^* l \nu$

$$h_{A_1}(w) = h_{A_1}(1) \left( -z^3 \left( 231\rho_{D^*}^2 - 91 \right) + z^2 \left( 53\rho_{D^*}^2 - 15 \right) - 8z\rho_{D^*}^2 + 1 \right),$$

$$R_1(w) = R_1(1) + 0.05(w-1)^2 - 0.12(w-1),$$

$$R_2(w) = R_2(1) - 0.06(w-1)^2 + 0.11(w-1)$$

- For  $B \rightarrow D l \nu$

$$\mathcal{G}(w) = \mathcal{G}(1) \left( 1 - 8\rho_D^2 z + (51\rho_D^2 - 10)z^2 - (252\rho_D^2 - 84)z^3 \right)$$

- BGL Phys.Lett. B771 (2017)  
Phys.Lett. B769 (2017)

- No HQET input

- For  $B \rightarrow D^* l \nu$

$$h_{A_1}(w) = \frac{f(w)}{\sqrt{m_B m_{D^*}}(1+w)}$$

$$R_1(w) = (w+1)m_B m_{D^*} \frac{g(w)}{f(w)}$$

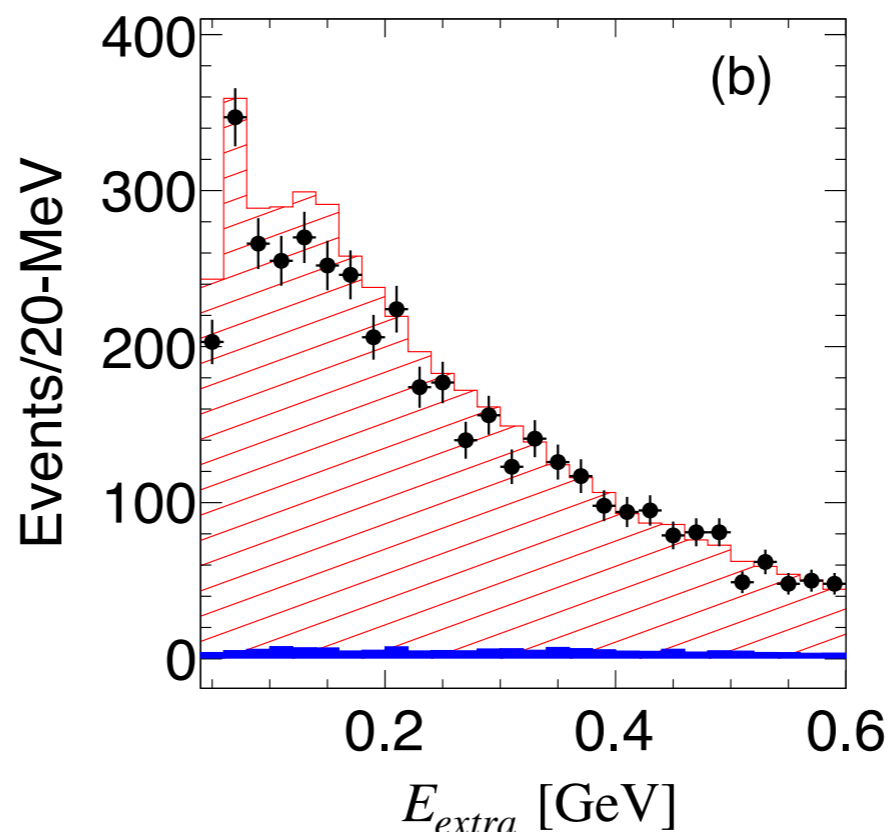
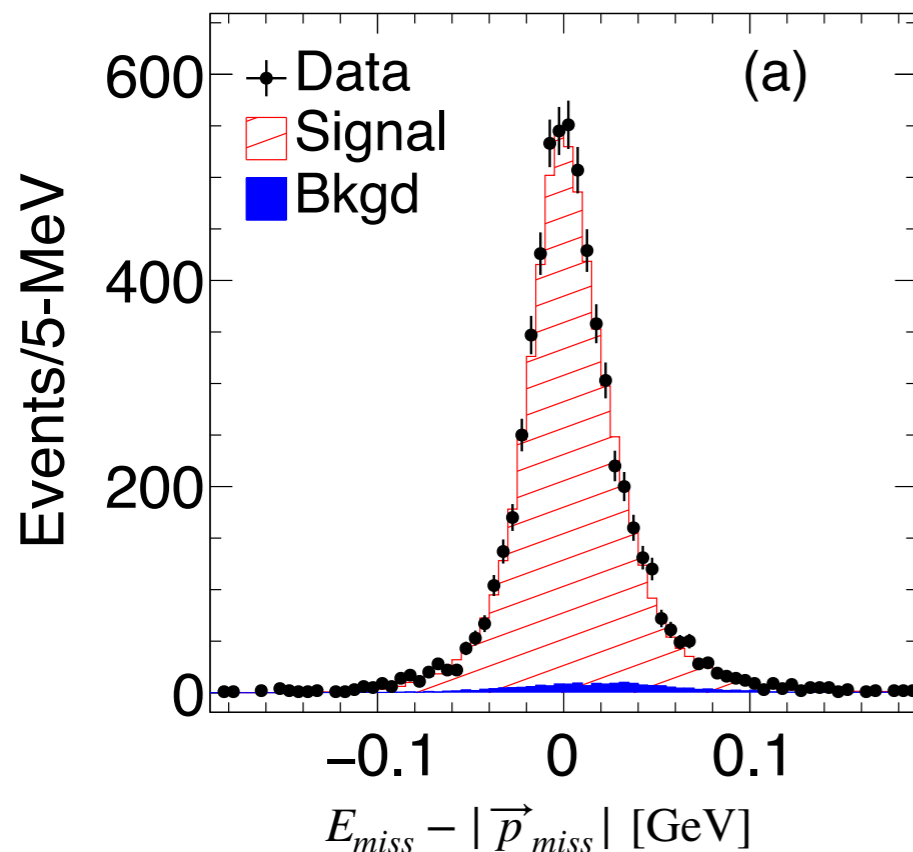
$$R_2(w) = \frac{w-r}{w-1} - \frac{\mathcal{F}_1(w)}{m_B(w-1)f(w)}$$

where  $f$ ,  $g$  and  $\mathcal{F}_1$  are  
parameterised as ....

$$f(z) = \frac{1}{P_i(z)\phi_i(z)} \sum_{n=0}^N a_{i,n} z^n$$

cut off at  $n=1, 2 \dots$

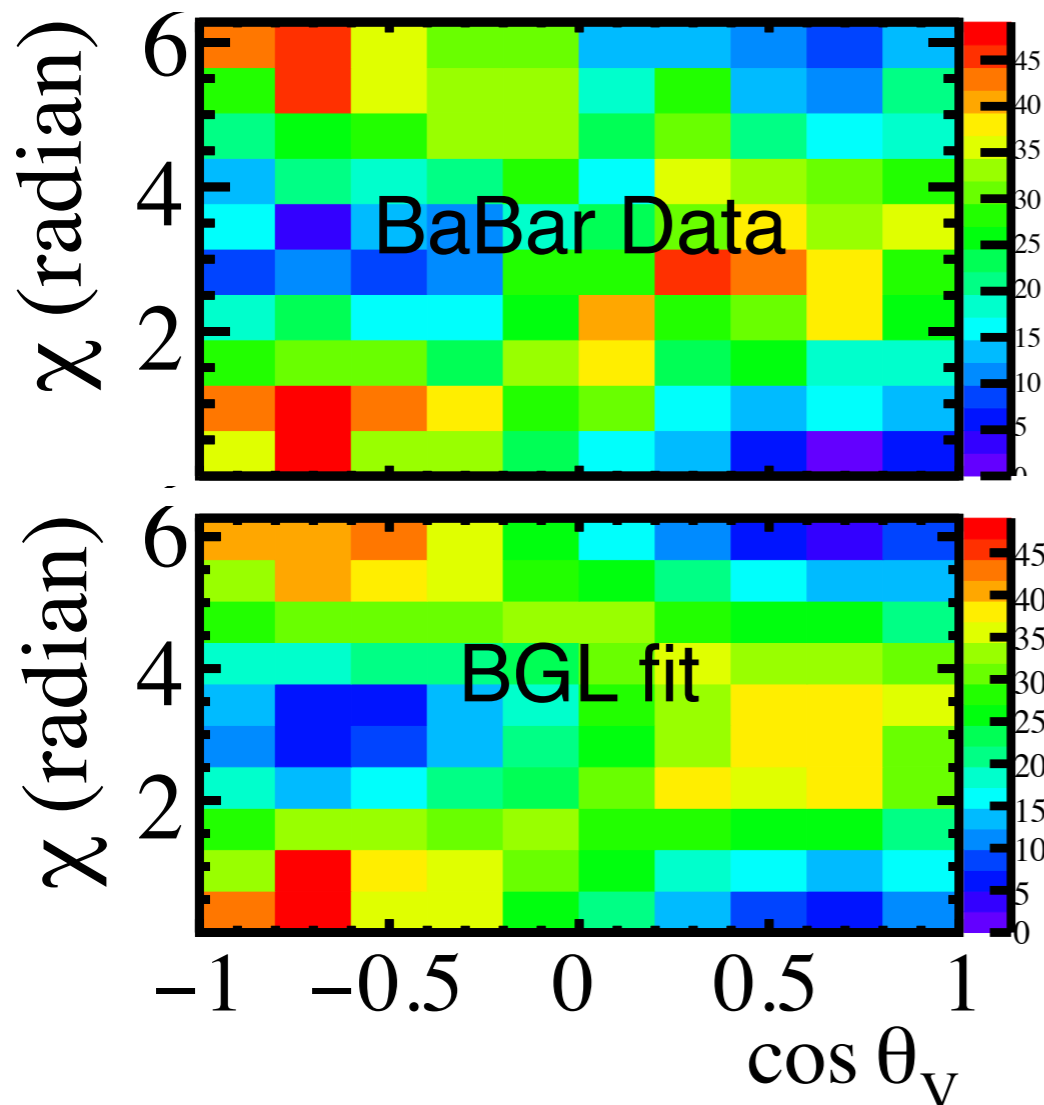
- Tag side B reconstructed (hadronically) to reconstruct unknown neutrino momentum
- Reconstruct Bsignal (comprised of  $D^*e, D^*\mu$  and  $D^{*0}e, D^{*0}\mu$  where  $D^0$  from  $D^{*(0)}$  decays to  $K^-\pi^+, K^-\pi^-\pi^0, K^-\pi^+\pi^-\pi^+$  combined with  $\pi^0$  and  $\pi^+$ )
- Signal selection using  $\Delta m = (m_{D^*} - m_D)$  and  $p_{lep}$
- Kinematic fit to  $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B_{tag}\bar{B}_{sig}(\rightarrow D^*\ell^-\bar{\nu}_l)$



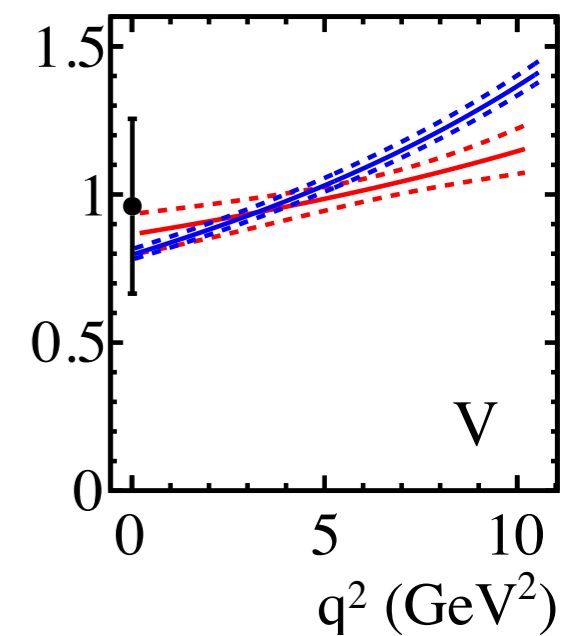
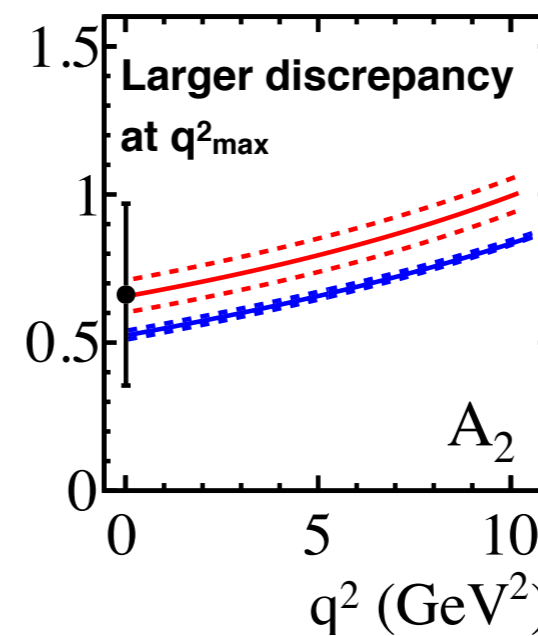
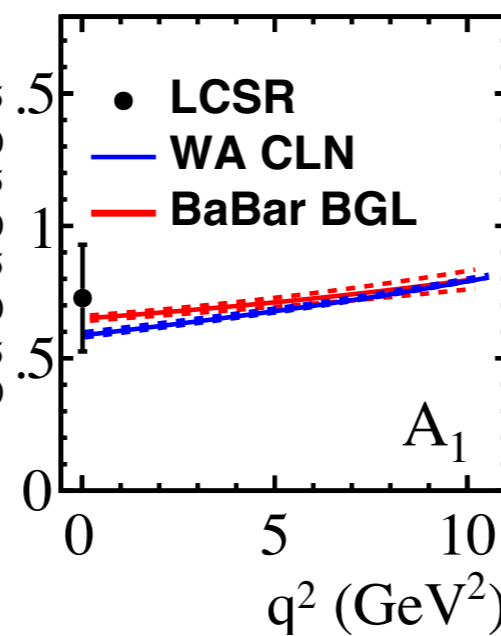
**BaBar** 469 fb<sup>-1</sup>  
N<sub>signals</sub> = 5932

- Measure  $|V_{cb}|$  and form factor parameters
  - First unbinned (ML) fit in 4-D of  $q^2$ ,  $\cos\theta_l$ ,  $\cos\theta_\nu$ ,  $X$  for BGL expansion (N=1)
  - Tension remain between inclusive and exclusive  $|V_{cb}|$
- $|V_{cb}|$  consistent with CLN-WA

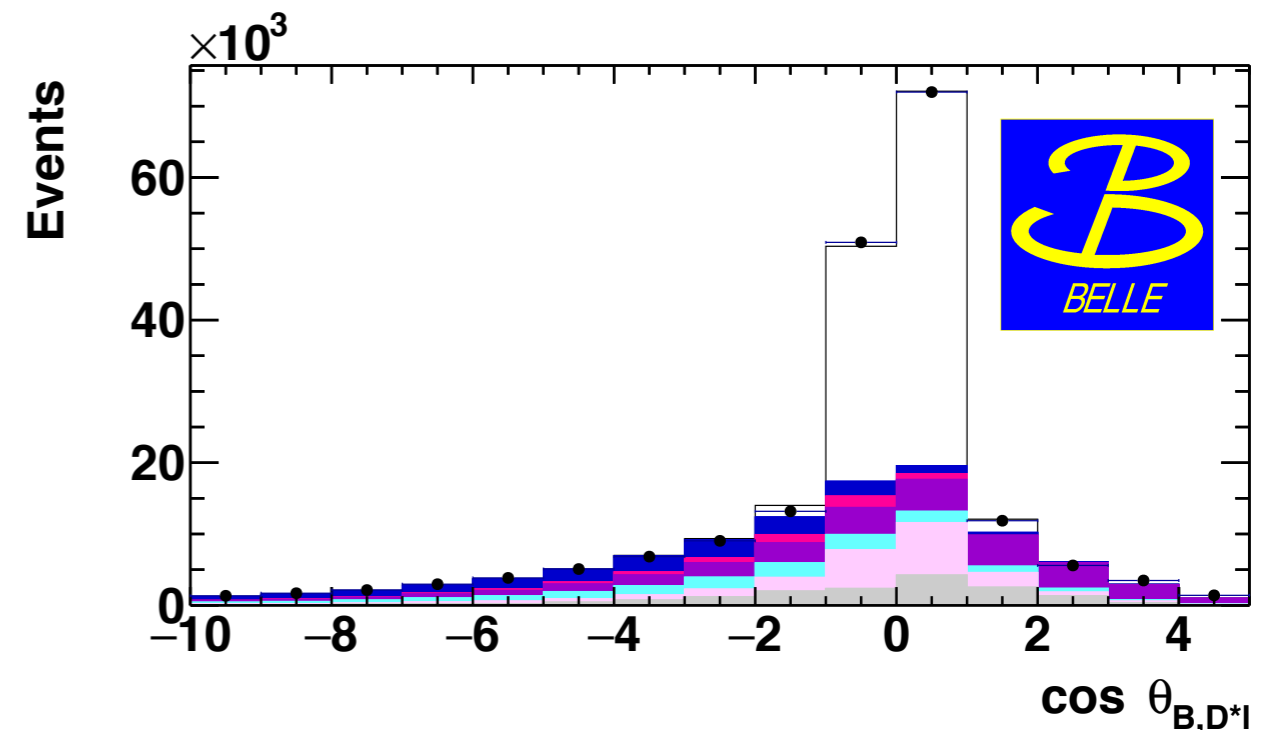
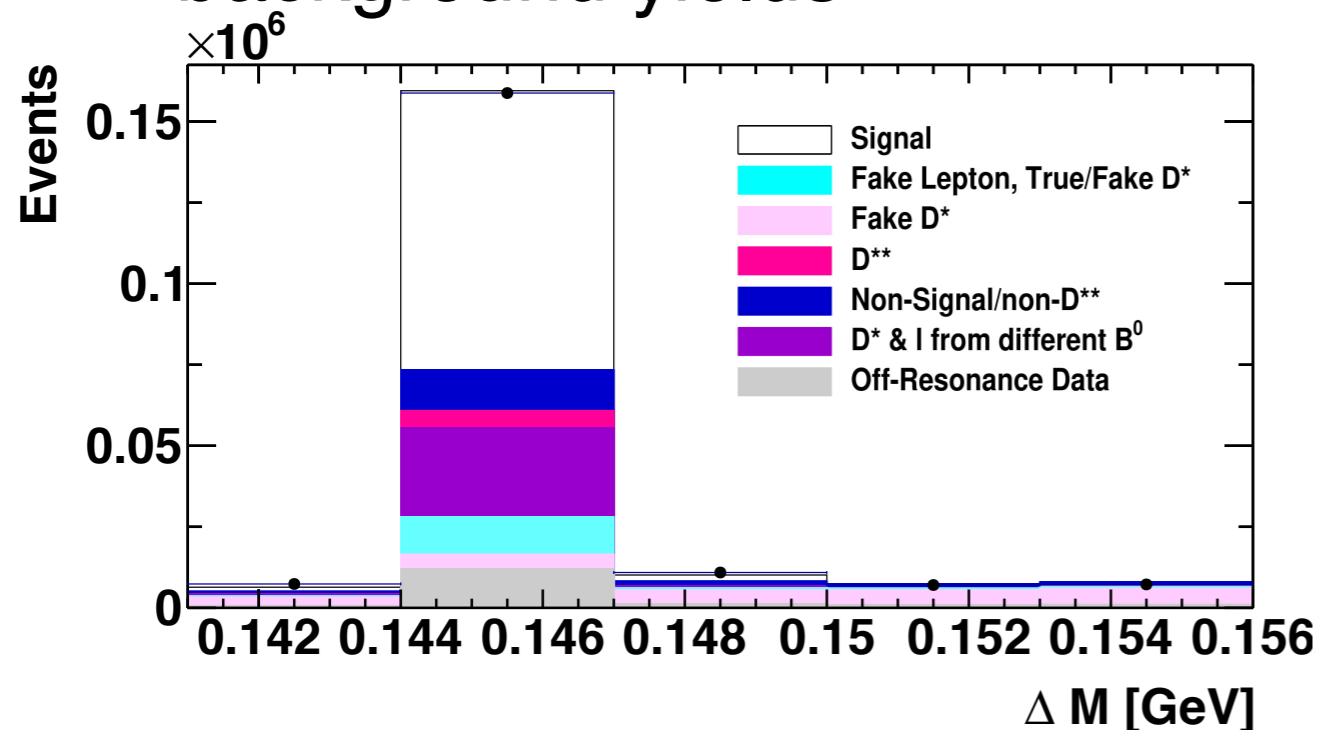
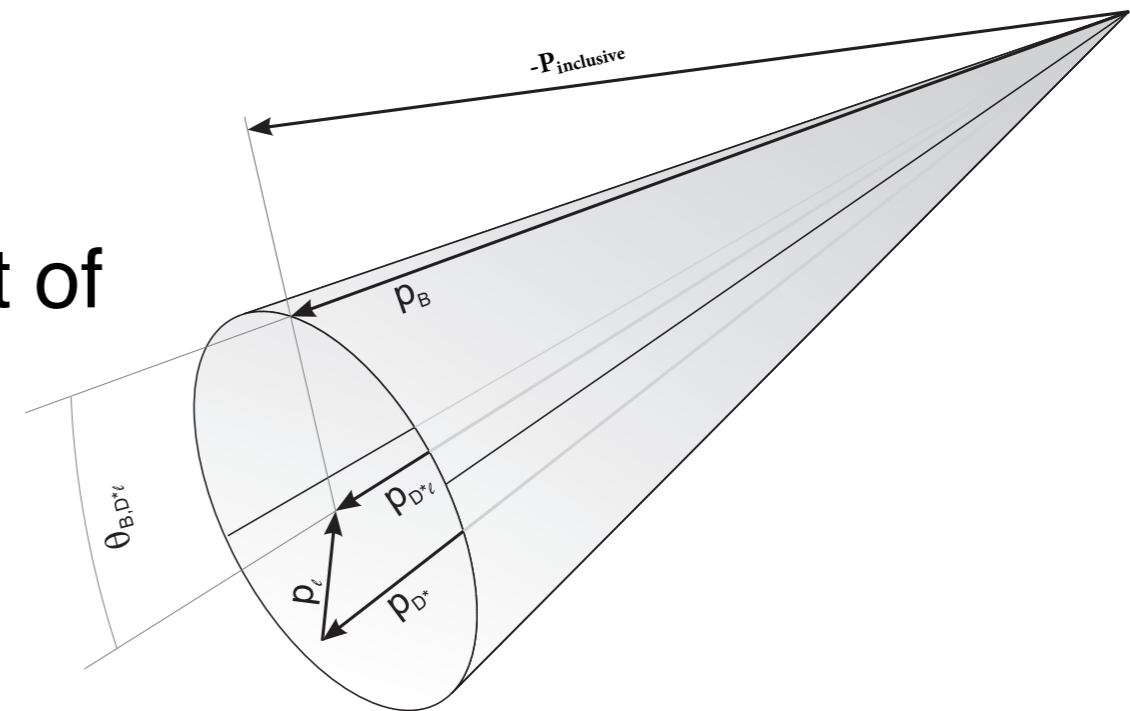
$ V_{cb}  \times 10^3 = 38.03 \pm 1.05$	$(B^- - e)$
$ V_{cb}  \times 10^3 = 38.68 \pm 1.16$	$(B^- - \mu)$
$ V_{cb}  \times 10^3 = 38.59 \pm 1.15$	$(B^0 - e)$
$ V_{cb}  \times 10^3 = 38.24 \pm 1.05$	$(B^0 - \mu)$



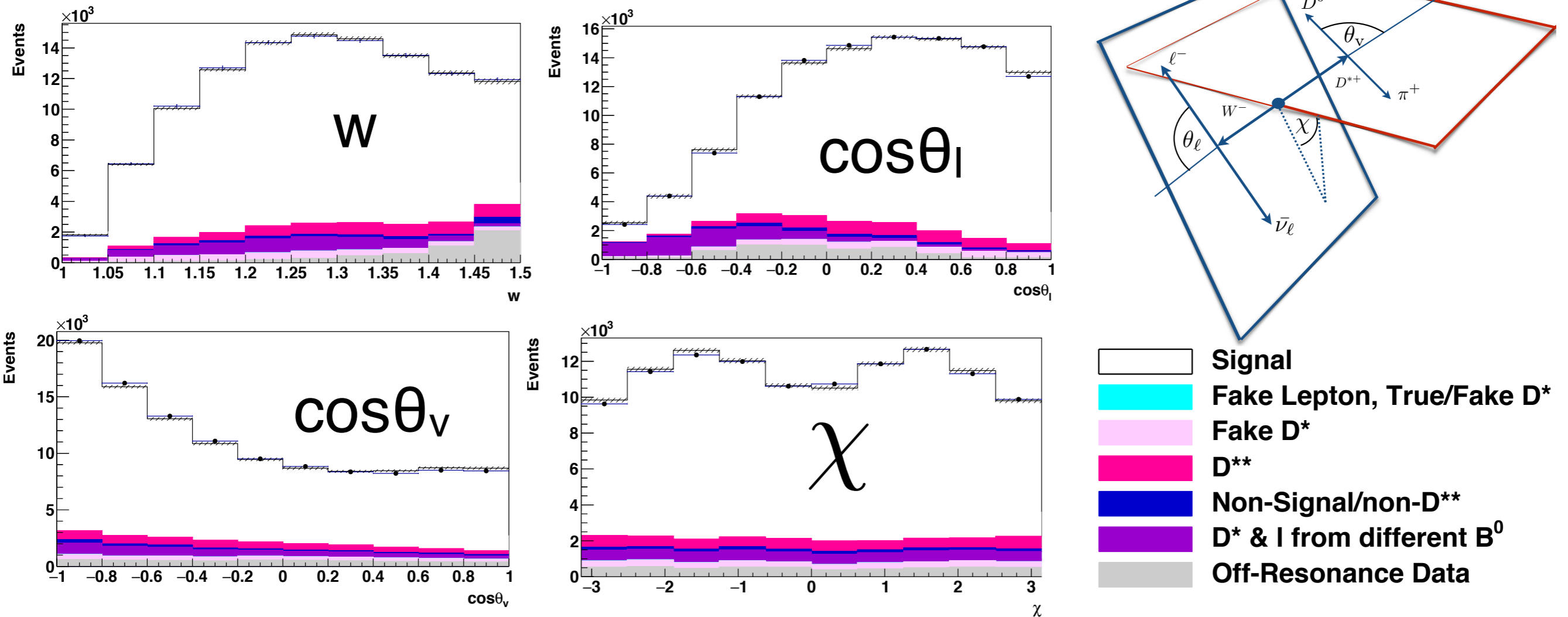
$a_0^f \times 10^2$	$a_1^f \times 10^2$	$a_1^{F_1} \times 10^2$	$a_0^g \times 10^2$	$a_1^g \times 10^2$	$ V_{cb}  \times 10^3$
1.29	1.63	0.03	2.74	8.33	38.36
$\pm 0.03$	$\pm 1.00$	$\pm 0.11$	$\pm 0.11$	$\pm 6.67$	$\pm 0.90$



- Measure  $|V_{cb}|$  using **Belle**  $711\text{fb}^{-1}$ .
- Signal Selection using
  - 3D - Binned Maximum Likelihood fit of
  - $(\cos\theta_{B,D^*l})$
  - $\Delta M = \text{mass}(D^* - D^0)$
  - lepton momentum
- Float Signal & Backgrounds components from MC to extract background yields



Simultaneous fit of 1D projections of  $w$ ,  $\cos\theta_l$ ,  $\cos\theta_v$ ,  $\chi$  to extract  $\rho^2$ ,  $R_1(1)$ ,  $R_2(1)$  and  $F(1)IV_{cb}$



$$\rho^2 = 1.106 \pm 0.031 \pm 0.007$$

$$R_1(1) = 1.229 \pm 0.028 \pm 0.009$$

$$R_2(1) = 0.852 \pm 0.021 \pm 0.006$$

$$F(1)IV_{cb} \eta_{EW} \times 10^3 = 35.1 \pm 0.2 \pm 0.6$$

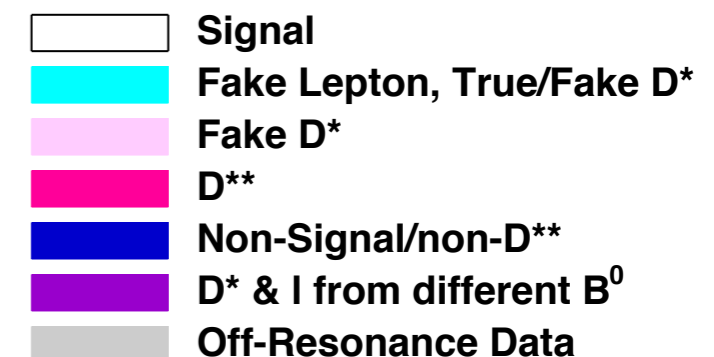
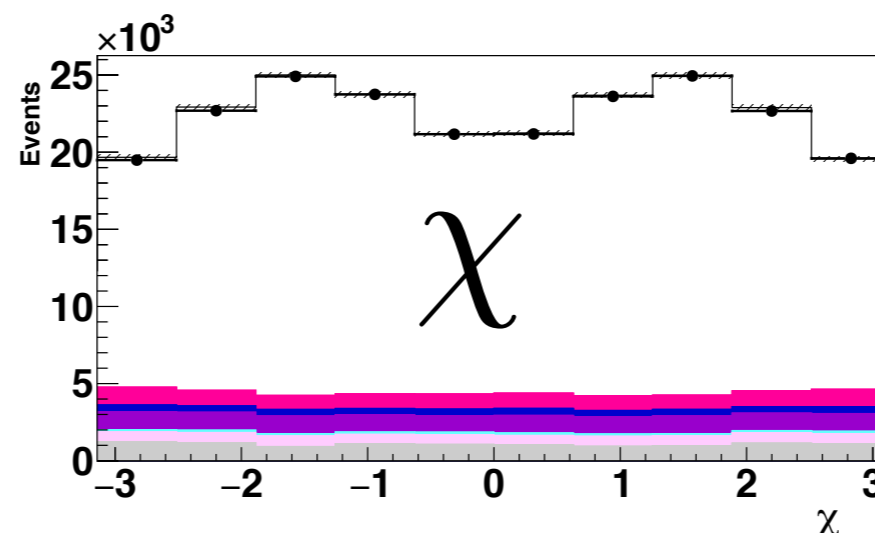
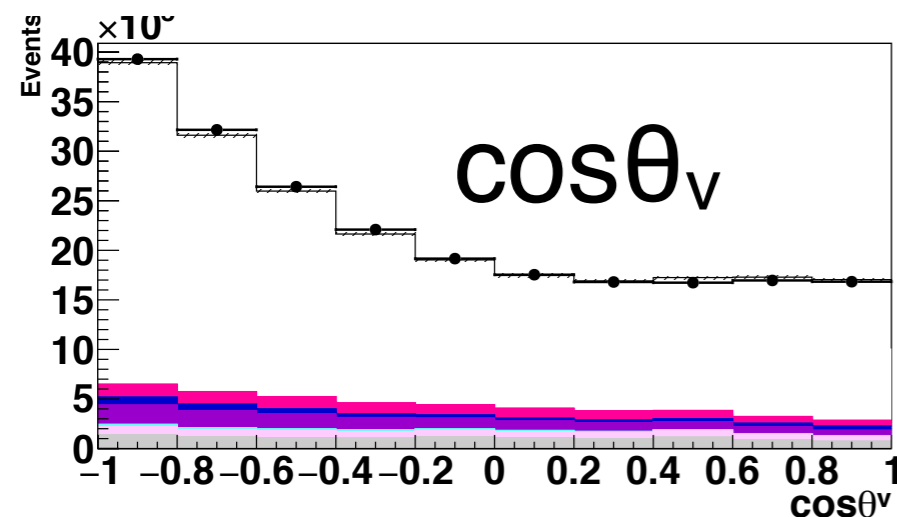
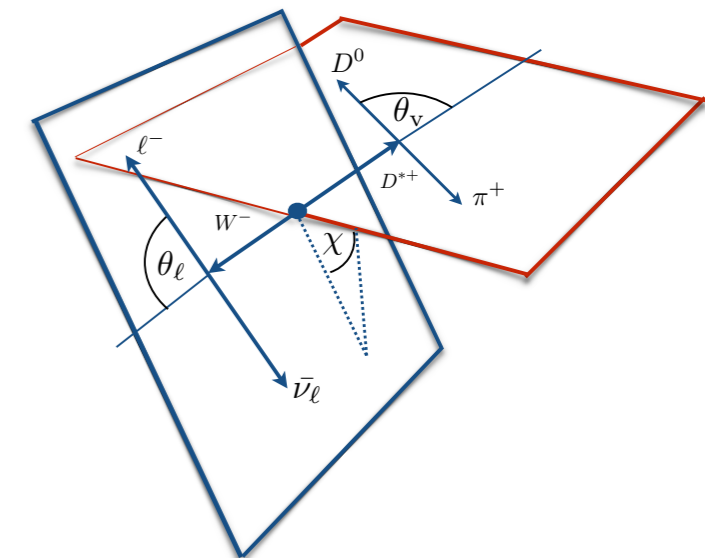
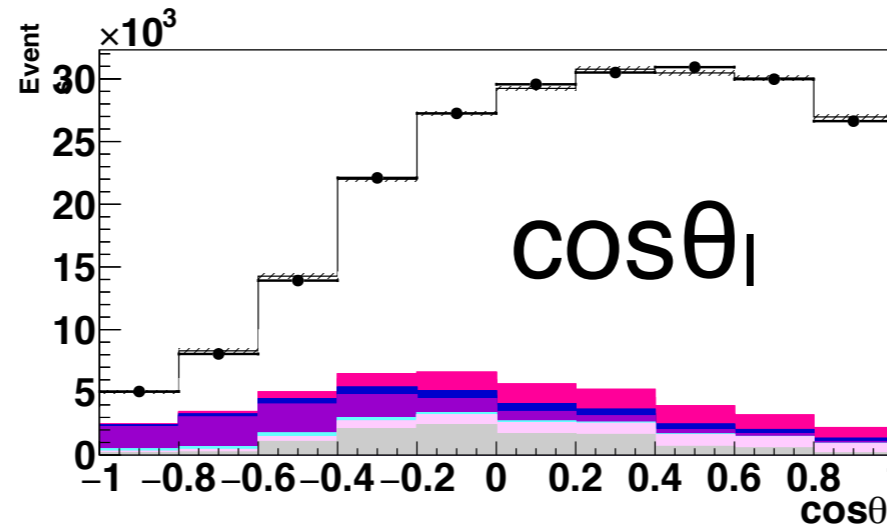
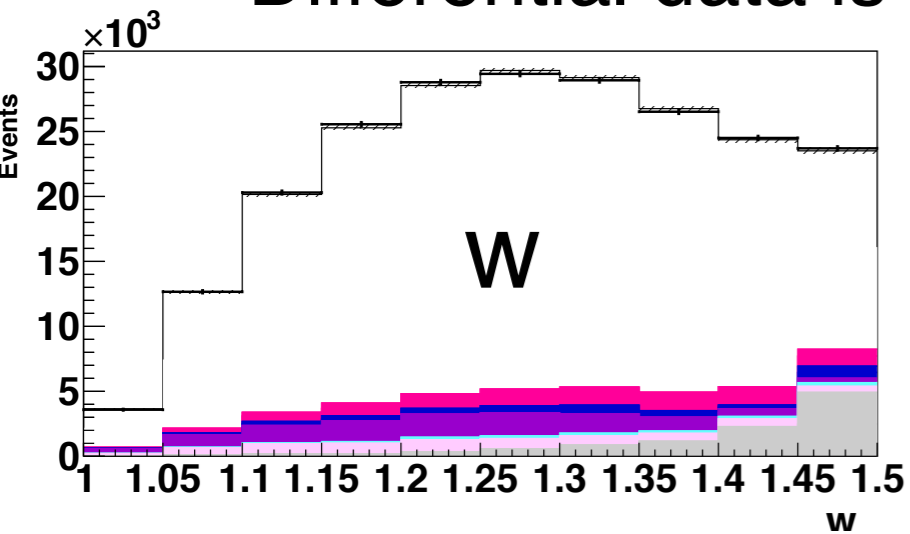


Simultaneous fit of 1D projections of  $w$ ,  $\cos\theta_l$ ,  $\cos\theta_v$ ,  $\chi$  to extract the coefficients of the BGL expansion (up to 3rd order) and  $F(1)|V_{cb}|$

$$F(1)|V_{cb}|\eta_{EW} \times 10^3 = 34.9 \pm 0.2 \pm 0.6$$

- Consistent with CLN
- Differential data is provided

$$\begin{aligned} \tilde{a}_0^f \times 10^3 &= -0.506 \pm 0.004 \pm 0.008, \\ \tilde{a}_1^f \times 10^3 &= -0.65 \pm 0.17 \pm 0.09, \\ \tilde{a}_1^{F_1} \times 10^3 &= -0.270 \pm 0.064 \pm 0.023, \\ \tilde{a}_2^{F_1} \times 10^3 &= +3.27 \pm 1.25 \pm 0.45, \\ \tilde{a}_0^g \times 10^3 &= -0.929 \pm 0.018 \pm 0.013, \end{aligned}$$





# $|V_{cb}|$ from BaBar and Belle From CLN and BGL

## Last 10 years...

$$|V_{cb}| \times 10^3 = 38.4 \pm 0.6 \text{ (CLN-Belle2019) } (B \rightarrow D^* l \nu)^{[1]}$$

$$|V_{cb}| \times 10^3 = 38.3 \pm 0.8 \text{ (BGL-Belle2019) } (B \rightarrow D^* l \nu)^{[1]}$$

$$|V_{cb}| \times 10^3 = 38.4 \pm 0.9 \text{ (BGL-BaBar2019) } (B \rightarrow D^* l \nu)^{[2]}$$

$$|V_{cb}| \times 10^3 = 39.9 \pm 1.3 \text{ (CLN-Belle2016) } (B \rightarrow D l \nu)^{[3]}$$

$$|V_{cb}| \times 10^3 = 40.8 \pm 1.1 \text{ (BCL-Belle2016) } (B \rightarrow D l \nu)^{[3]}$$

$$|V_{cb}| \times 10^3 = 42.2 \pm 0.8 \text{ (Inclusive-HFLAV) }^{[4]}$$

- CLN and BGL agree for both Belle and BaBar
- **Inclusive and Exclusive tension still persistent !!!**
- CLN and BGL form factor differences at zero-recoil (minimum higher order HQET corrections) need to be investigated further.

- Differential decay rate (as function of  $q^2$ ) is compared with expectations from HQET and unquenched lattice QCD predictions.
- $\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu$  described by (6) form factors (FF) corresponding to the vector and axial-vector components.

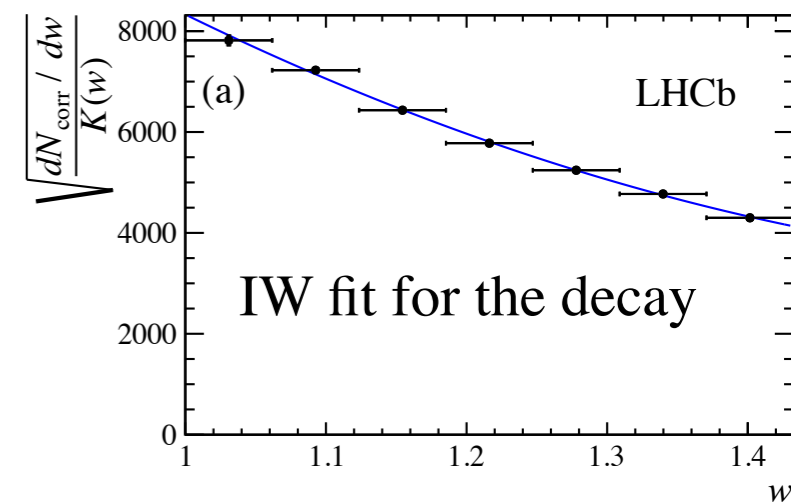
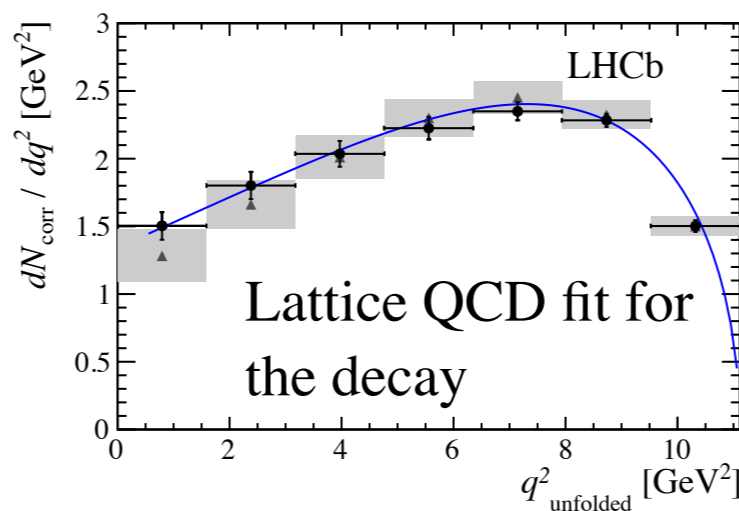
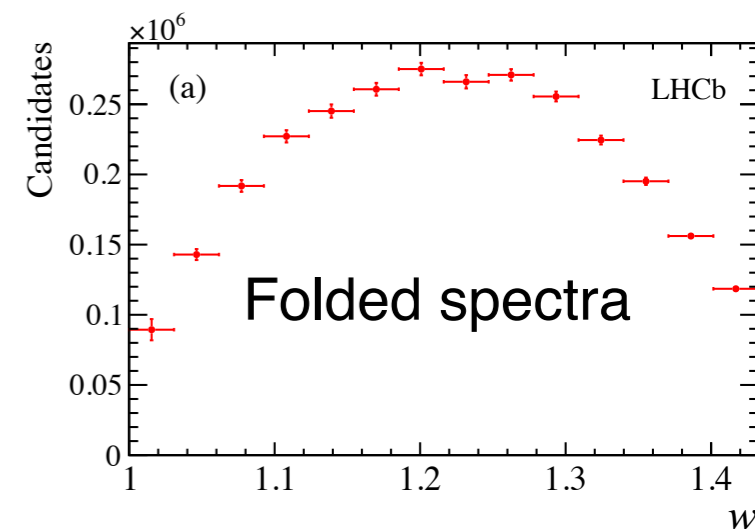
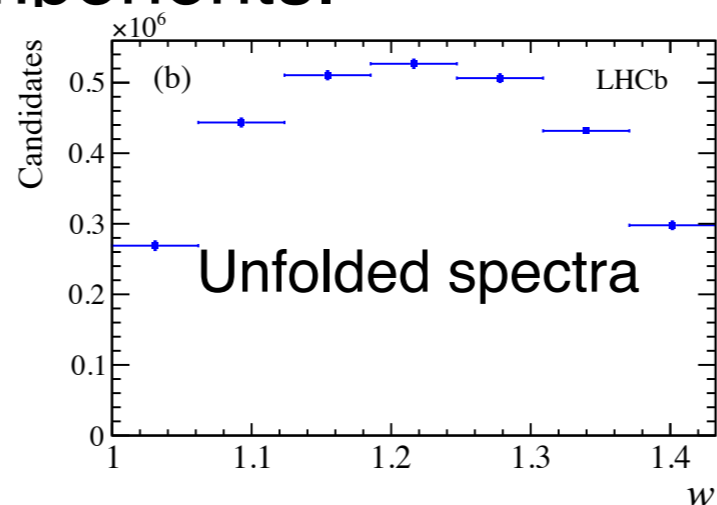
$$\frac{d\Gamma}{dw} = G K(w) \xi_B^2$$

$$G = \frac{2}{3} \frac{G_F^2}{(2\pi)^3} |V_{cb}|^2 (m_{\Lambda_b^0})^4 r^2$$

$$\xi_B(w) = 1 - \rho^2(w-1) + \frac{1}{2}\sigma^2(w-1)^2 + \dots,$$

$$K(w) = m_{\Lambda_c^+} \sqrt{w^2 - 1} [3w(1 - 2rw + r^2) + 2r(w^2 - 1)].$$

**$\rho^2 = 1.63 \pm 0.07 \pm 0.08$ ,**  
 consistent with Lattice<sup>1</sup>, QCD<sup>2</sup>,  
 and relativistic quark model<sup>3</sup>



Further studies with a suitable normalisation channel will lead to a precise independent determination of the CKM parameter  $|V_{cb}|$ .



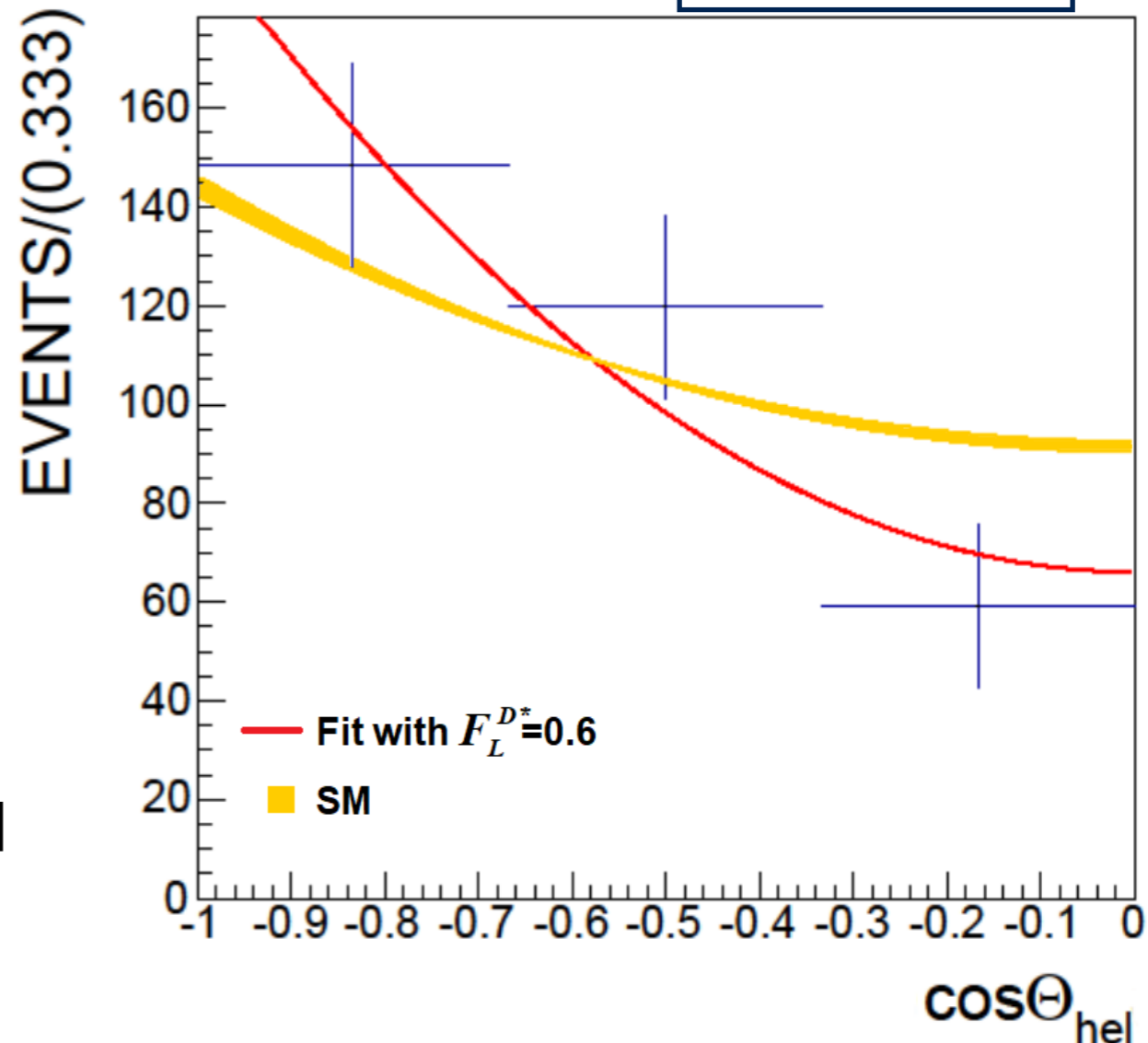
- $F_L^{D^*}$  is fraction of  $D^*$  polarisation in  $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$  decay from angular distribution in  $D^{*-} \rightarrow \bar{D}^0 \pi^-$
- SM prediction<sup>1</sup>:  $F_L^{D^*} = 0.45$

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{3}{4} (2F_L^{D^*} \cos^2 \theta_{\text{hel}} + (1 - F_L^{D^*}) \sin^2 \theta_{\text{hel}})$$

- $\theta_{\text{hel}}$  is angle between  $D^0$  and direction opposite to  $B^0$  in  $D^{*-}$  rest frame

- Rest of event information to reconstruct  $B_{\text{tag}}$
- Calculate helicity angle in 3 bins
- Signal yield in bins of  $\cos \theta_{\text{hel}}$  is extracted from extended unbinned ML fit to  $M_{\text{tag}}$

**Belle 711fb<sup>-1</sup>**



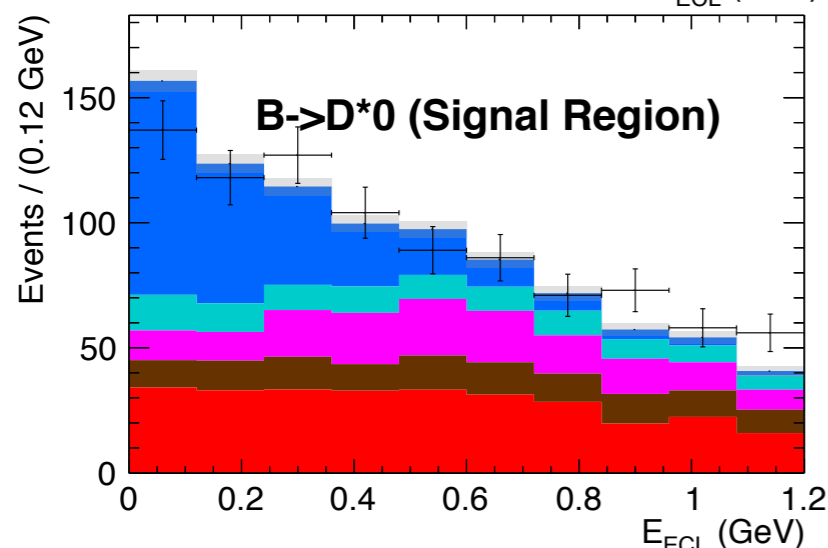
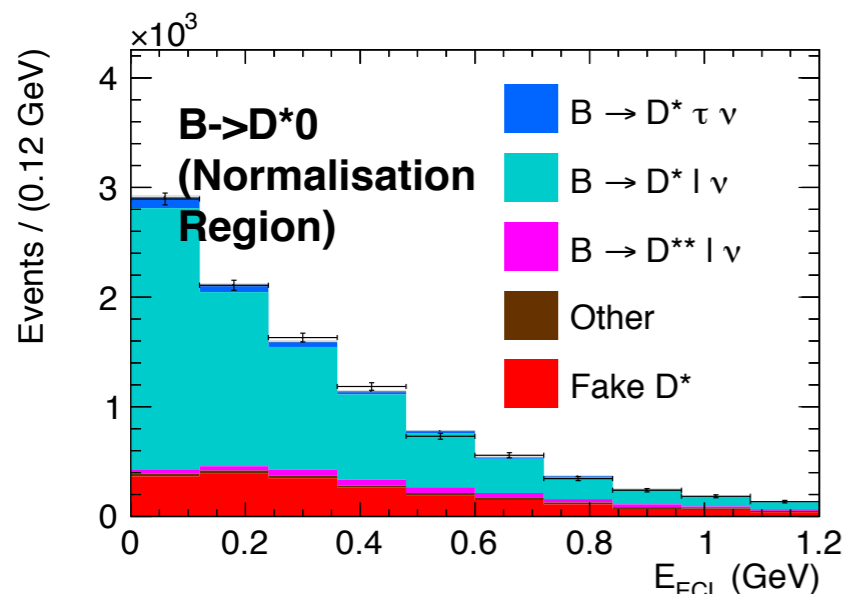
$$F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{sys})$$

agrees within about  $1.7\sigma$  with SM

# Importance of $B \rightarrow D^{**} l \nu$ Measurement

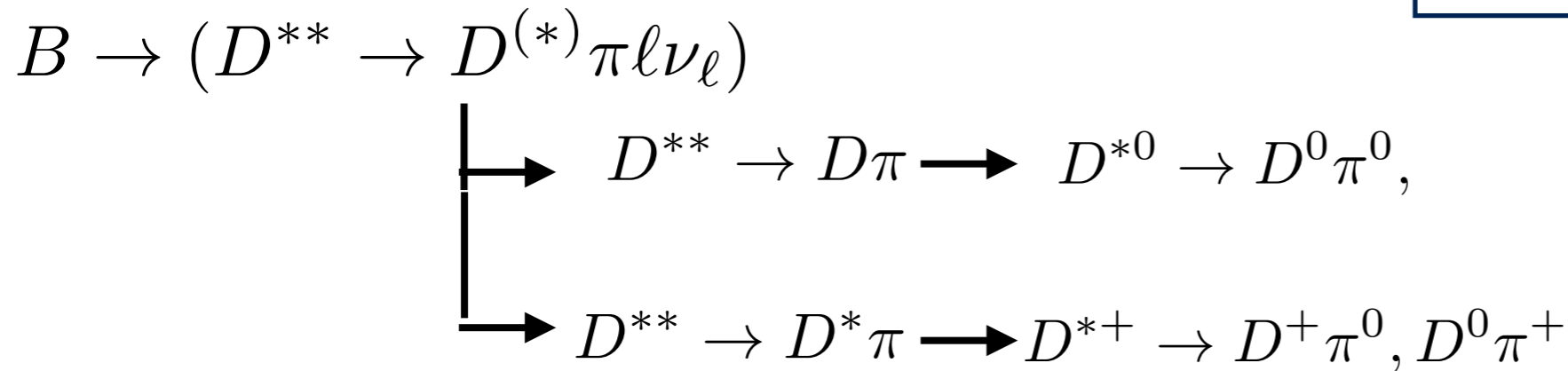
- $D^{**}$  is important background for both semileptonic ( $B \rightarrow D^* l \nu$ ) and semitonic ( $B \rightarrow D^* \tau \nu$ ) measurements
- $D^{**}$  is leading systematic error for both measurement
- Can mimic signal while measuring  $R(D)$  and  $R(D^*)$

arXiv:1904.08794

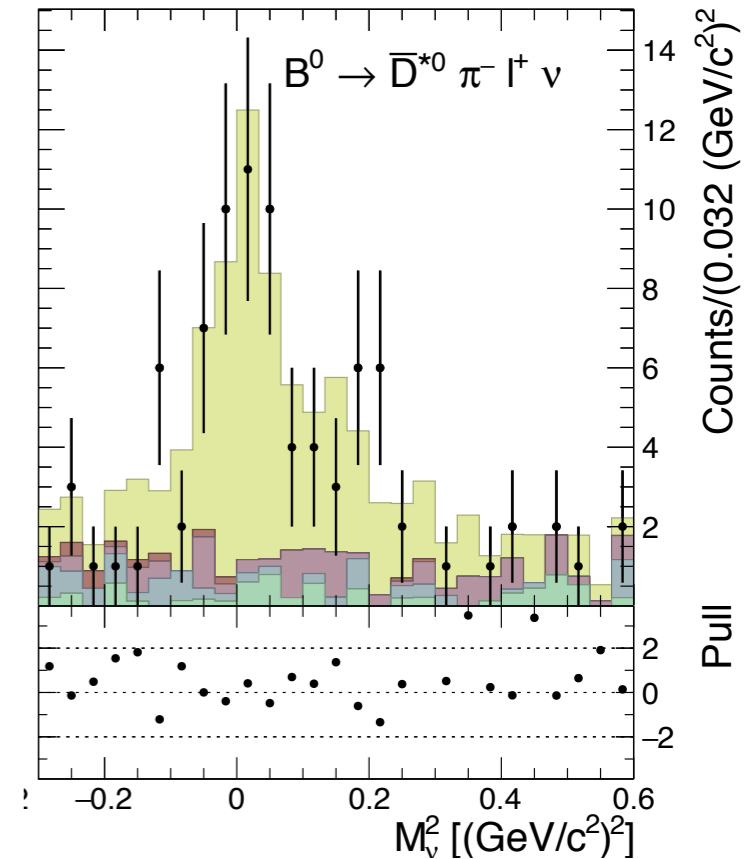


Source	$\Delta R(D)$ (%)	$\Delta R(D^*)$ (%)
$D^{**}$ composition	0.76	1.41
Fake $D^{(*)}$ calibration	0.19	0.11
$B_{\text{tag}}$ calibration	0.07	0.05
Feed-down factors	1.69	0.44
Efficiency factors	1.93	4.12
Lepton efficiency and fake rate	0.36	0.33
Slow pion efficiency	0.08	0.08
MC statistics	4.39	2.25
$B$ decay form factors	0.55	0.28
Luminosity	0.10	0.04
$\mathcal{B}(B \rightarrow D^{(*)} l \nu)$	0.05	0.02
$\mathcal{B}(D)$	0.35	0.13
$\mathcal{B}(D^*)$	0.04	0.02
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.15	0.14
Total	5.21	4.94

Important background for  $B \rightarrow D^* \tau \nu$  and  $R(D^*)$  measurement



Belle 711fb<sup>-1</sup>



$$\mathcal{B}(B^+ \rightarrow D^- \pi^+ \ell^+ \nu)$$

$$= [4.55 \pm 0.27 \text{ (stat.)} \pm 0.39 \text{ (syst.)}] \times 10^{-3},$$

$$\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^- \ell^+ \nu)$$

$$= [4.05 \pm 0.36 \text{ (stat.)} \pm 0.41 \text{ (syst.)}] \times 10^{-3},$$

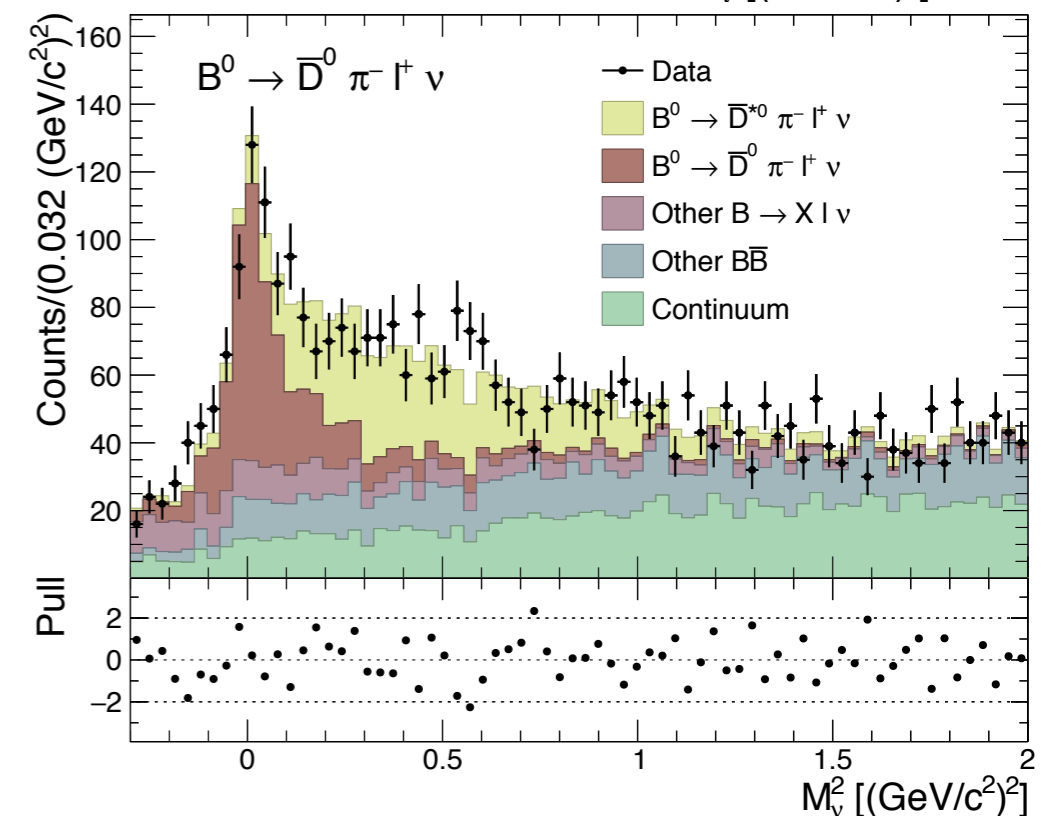
$$\mathcal{B}(B^+ \rightarrow D^{*-} \pi^+ \ell^+ \nu)$$

$$= [6.03 \pm 0.43 \text{ (stat.)} \pm 0.38 \text{ (syst.)}] \times 10^{-3},$$

$$\mathcal{B}(B^0 \rightarrow \bar{D}^{*0} \pi^- \ell^+ \nu)$$

$$= [6.46 \pm 0.53 \text{ (stat.)} \pm 0.52 \text{ (syst.)}] \times 10^{-3}.$$

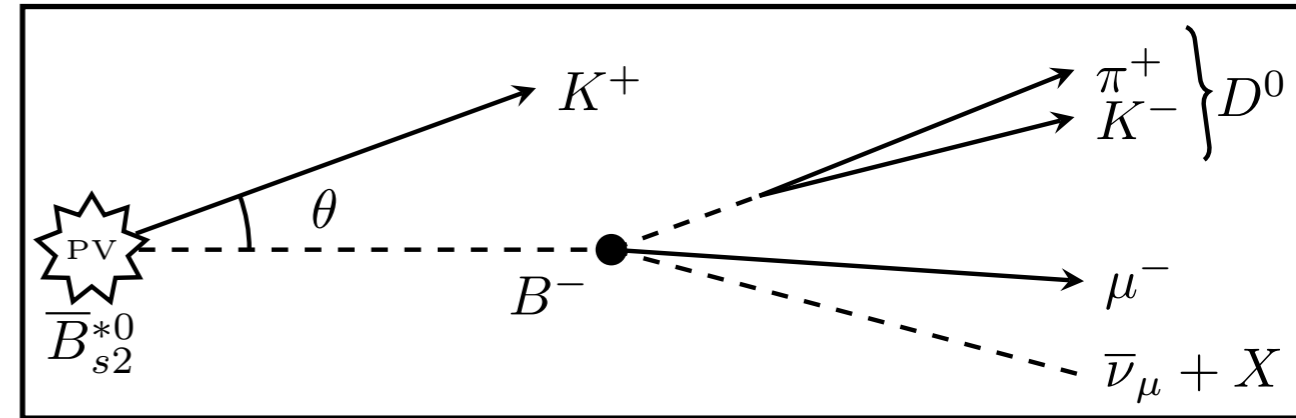
within  $1\sigma$  of WA



# Relative $B^- \rightarrow D^0/D^{*0}/D^{**0} \mu^- \bar{\nu}_\mu$ branching fractions using $B^-$ from $B_{s2}^{*0}$ decays

arXiv:1807.10722, submitted to PRD

- First LHCb measurement of  $f(D^0/D^{*0}/D^{**0}) \rightarrow$  distinguishes  $D^0/D^{*0}/D^{**0}$  in semileptonic B decay
- Useful input for B production rate at LHCb.
- $B_{s2}^{*0}$  decay used to separate the three components
- B.F relative to the inclusive



$$B^- \rightarrow D^0 X \mu^- \bar{\nu}_\mu$$

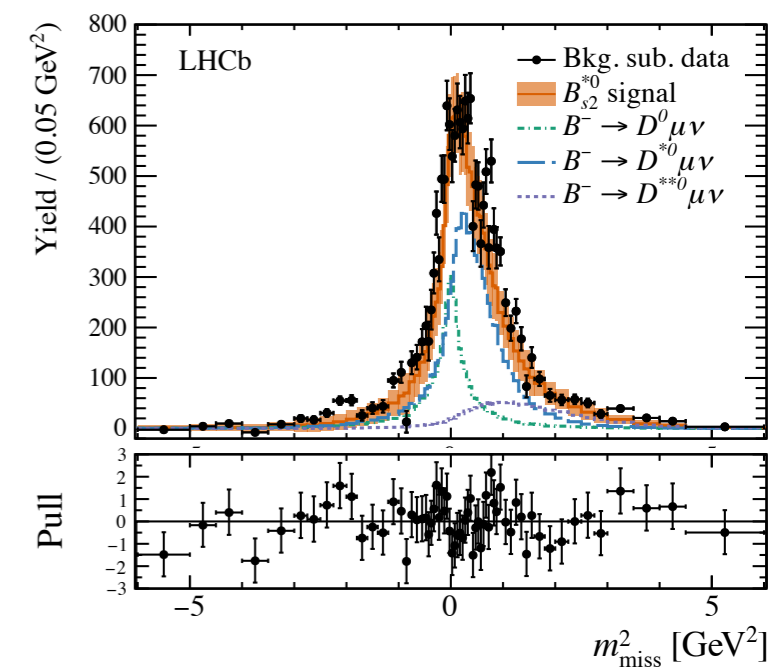
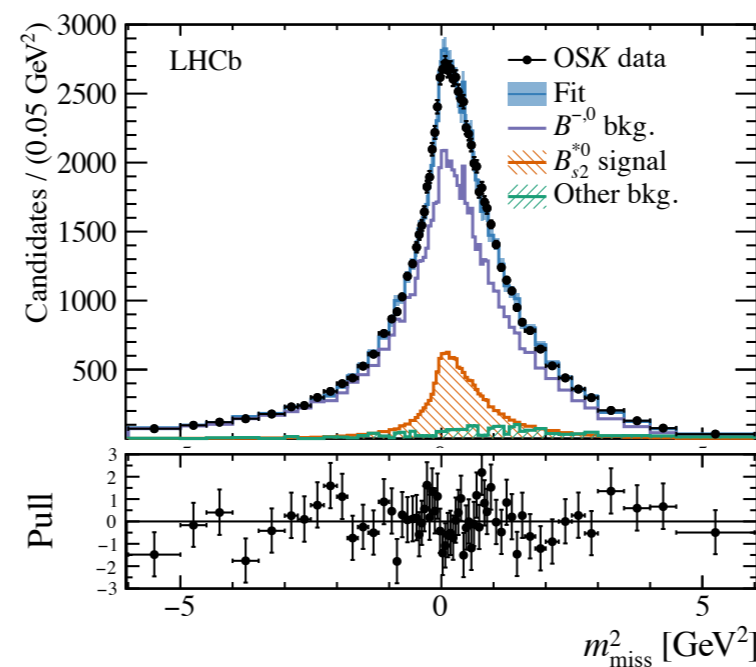


Data 3 fb<sup>-1</sup> collected at 7-8 TeV

$$f_{D^{**0}} = \frac{\mathcal{B}(B^- \rightarrow (D^{**0} \rightarrow D^0 X) \mu^- \bar{\nu}_\mu)}{\mathcal{B}(B^- \rightarrow D^0 X \mu^- \bar{\nu}_\mu)} = 0.21 \pm 0.07.$$

$$f_{D^0} = \frac{\mathcal{B}(B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu)}{\mathcal{B}(B^- \rightarrow D^0 X \mu^- \bar{\nu}_\mu)} = 0.25 \pm 0.06.$$

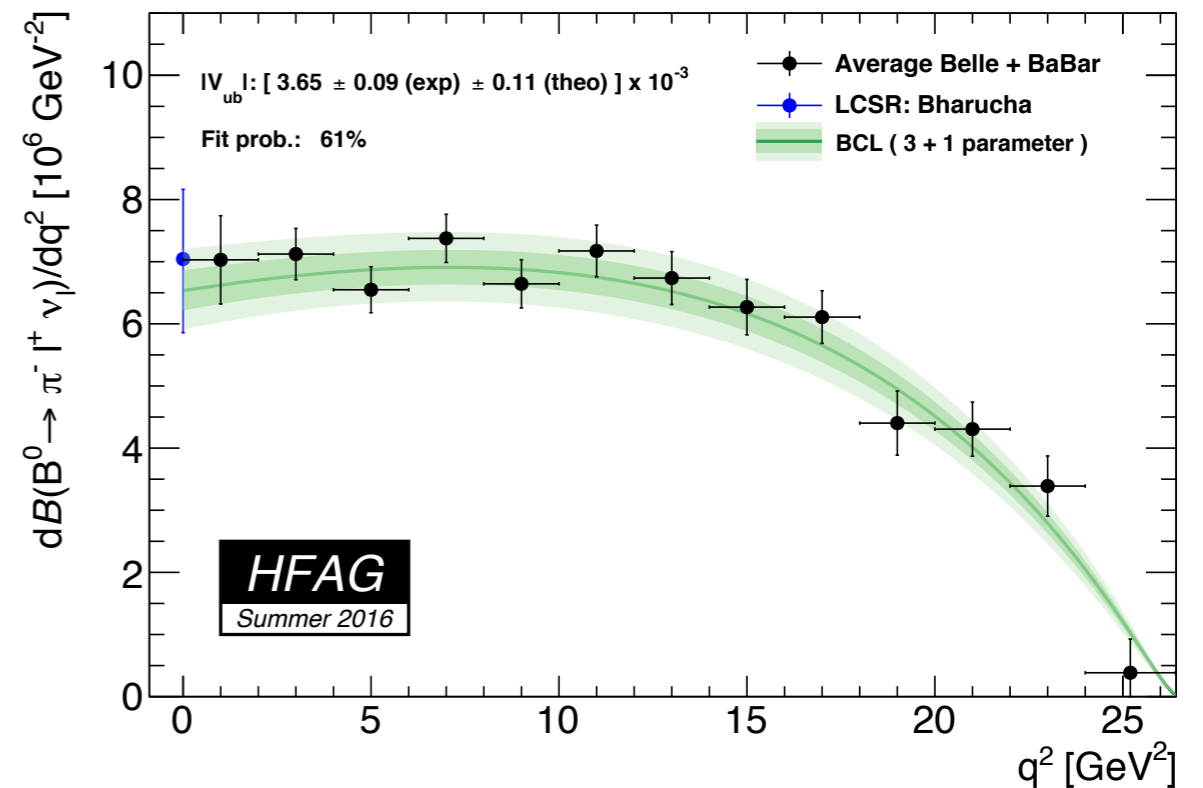
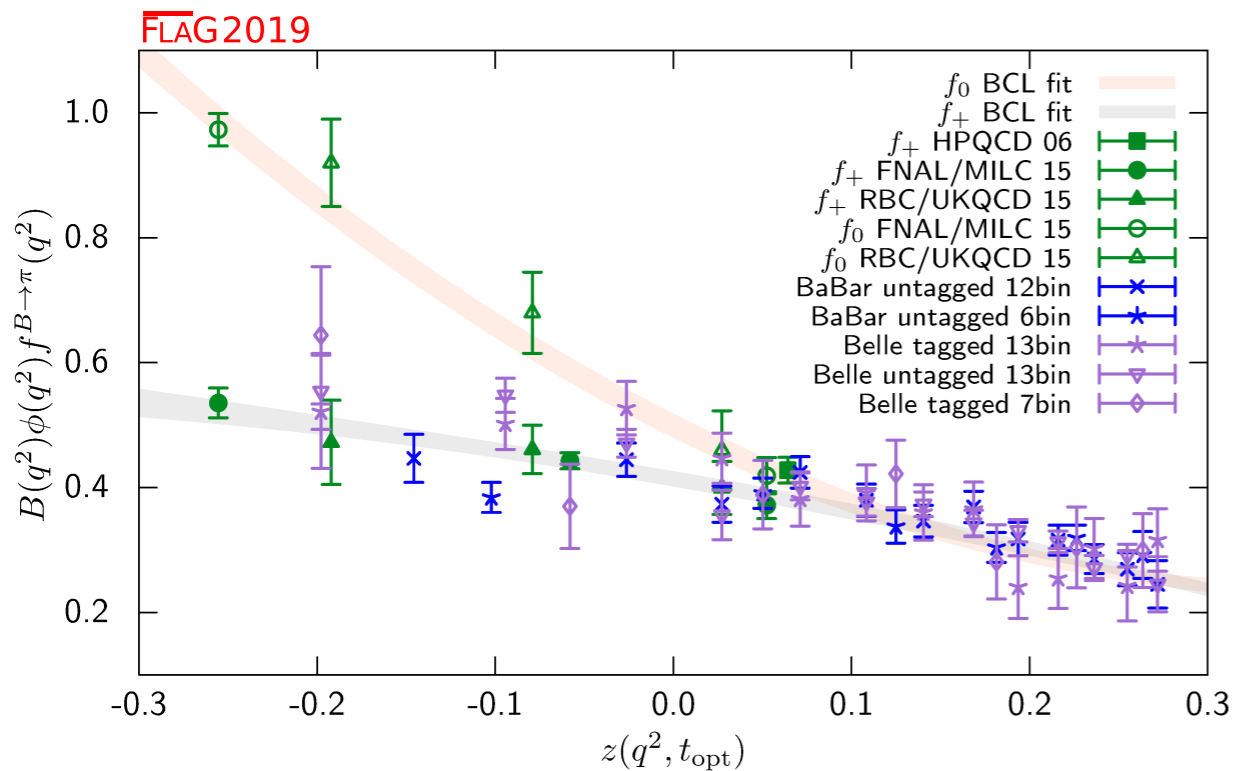
$$\longrightarrow f_{D^{*0}} = 1 - f_{D^0} - f_{D^{**0}}$$



$IV_{ubl}$

# $|V_{ub}|$ Status

- Clean signal in missing mass for exclusive modes to measure  $|V_{ub}|$
- **Form factors  $f_i(q^2)$**  computed with Light Cone Sum Rules or LQCD
- $b \rightarrow u \ell \nu$  signal enhanced w.r.t.  $b \rightarrow c$  backgrounds in low  $M_X$  and high  $q^2$
- systematics effects the charm background composition and u quark fragmentation

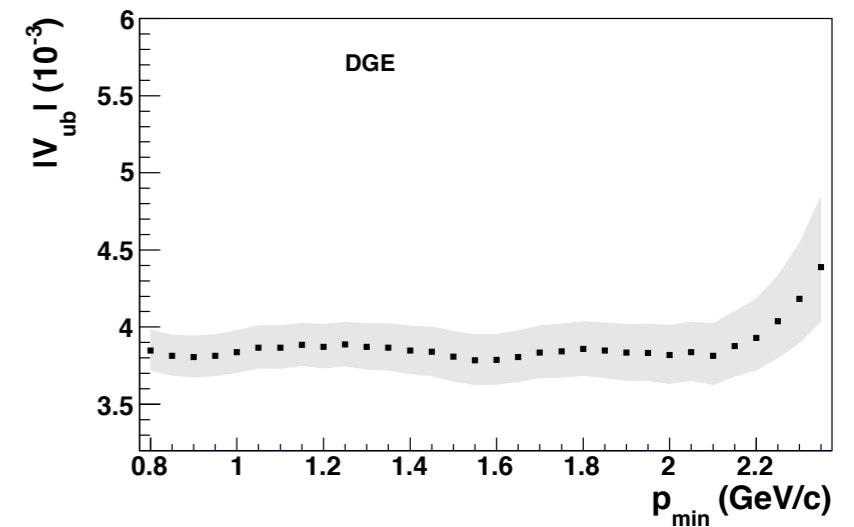
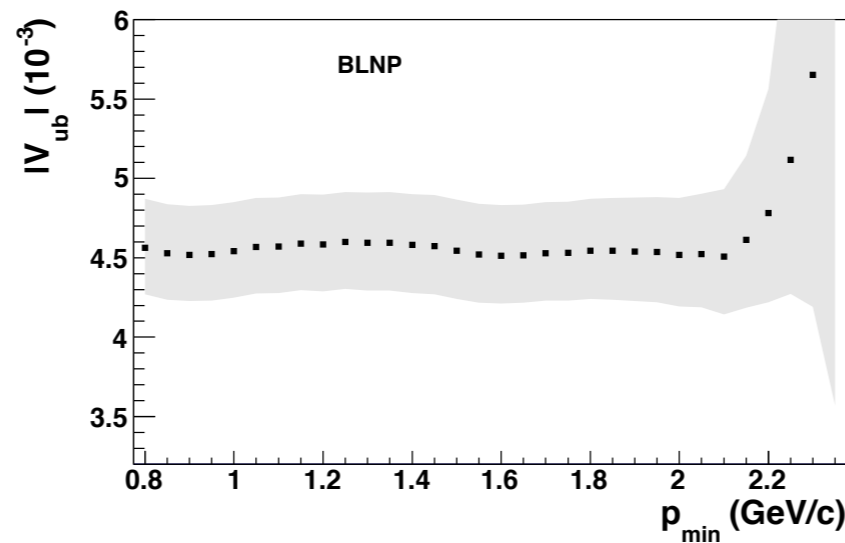
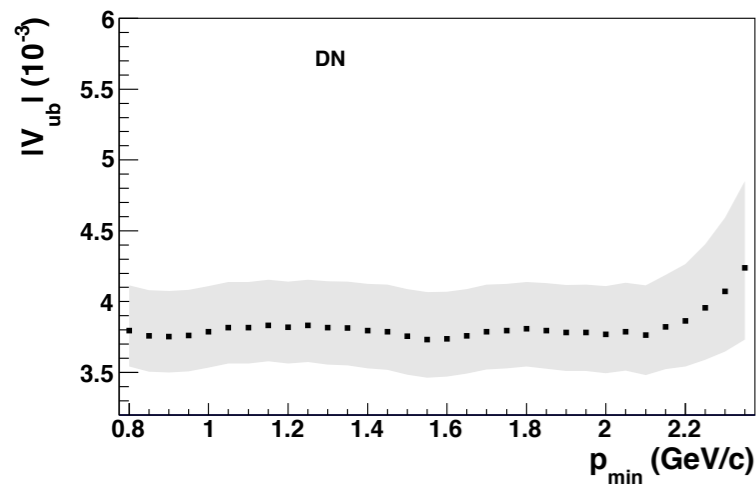


Summary of  $|V_{ub}|$  determined from leptonic decay, exclusive modes compared with lattice QCD





- Inclusive  $B \rightarrow X_{ev}$  measurement from full BaBar data set of  $424 \text{ fb}^{-1}$
- Cut applied to electron momentum to separate signal  $B \rightarrow X_{uev}$  ( $\sim 2.6 \text{ GeV}/c$ ) to background  $B \rightarrow X_{cev}$  ( $\sim 2.3 \text{ GeV}/c$ )
- Perform fit to the inclusive electron momentum spectrum averaged over charged and neutral B meson.



- $IV_{ubl}$  is extracted as a function of plep.
- $IV_{ubl} = (3.794 \pm 0.107_{\text{exp}} \begin{matrix} +0.292 \\ -0.219 \end{matrix} \text{SF} \begin{matrix} +0.078 \\ -0.068 \end{matrix} \text{theory}) \times 10^{-3}$  (DeFazio and Neubert)
- $IV_{ubl} = (4.563 \pm 0.126_{\text{exp}} \begin{matrix} +0.230 \\ -0.208 \end{matrix} \text{SF} \begin{matrix} +0.162 \\ -0.163 \end{matrix} \text{theory}) \times 10^{-3}$  (Bosch, Lange, Neubert, Paz)
- $IV_{ubl} = (3.959 \pm 0.104_{\text{exp}} \begin{matrix} +0.164 \\ -0.154 \end{matrix} \text{SF} \begin{matrix} +0.042 \\ -0.079 \end{matrix} \text{theory}) \times 10^{-3}$  (DGE)

- Improvement of experimental uncertainties expected in both inclusive and exclusive determination

Mode and dataset	Uncertainty (%) EXP. ONLY
<b><math> V_{ub} </math> exclusive (tagged)</b>	
Belle	3.8
Belle II 5 $ab^{-1}$	1.8
Belle II 50 $ab^{-1}$	1.2
<b><math> V_{ub} </math> exclusive (untagged)</b>	
Belle	2.7
Belle II 5 $ab^{-1}$	1.2
Belle II 50 $ab^{-1}$	0.9
<b><math> V_{ub} </math> inclusive (tagged)</b>	
Belle	6.0
Belle II 5 $ab^{-1}$	2.6
Belle II 50 $ab^{-1}$	1.7

- Expect theory error to decrease to 1% for exclusive and 2-4% for inclusive
- Exclusive analyses (hadronic tags) → perform clean and detailed exploration of exclusive  $b \rightarrow u$  modes spectra
- Untagged  $B \rightarrow \pi l \nu$  competitive for  $|V_{ub}|$
- Exploit at maximum the differential distributions for a global  $V_{ub}$  fit (inclusive measurement)

# Summary

- New  $B \rightarrow D^* l \nu$  tagged measurement from BaBar 2019 (BGL)
  - $|V_{cb}| \times 10^3 = 38.4 \pm 0.6$  (BGL)
- $B^0 \rightarrow D^* l \nu$  untagged measurement from Belle, 2018/2019 (BGL and CLN)
  - $|V_{cb}| \times 10^3 = 38.4 \pm 0.6$  (CLN)
  - $|V_{cb}| \times 10^3 = 38.3 \pm 0.8$  (BGL)
- Shape parameters of  $d\Gamma(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \nu_\mu)/dq^2$
- $D^*$  polarisation  $F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{sys})$
- $f(D^0/D^{*0}/D^{**0})$  by LHCb
- Result of inclusive  $B \rightarrow X_u l \nu$  from BaBar
- Measurements are coming up from Belle on inclusive  $|V_{ub}|$
- Belle II will collect  $\sim 5 \text{ab}^{-1}$  data by 2020, enough to look for NP
- Precise model independent measurement of  $|V_{cb}|$  and  $|V_{ub}|$

# Thank you



# References

- Slide 3
  1. Eur. Phys. J. C77 (2017) 895
- Slide 4
  1. M. Tanabashi et al. (Particle Data Group), Phys. Rev. D 98, 030001 (2018).
- Slide 8
  1. Phys. Rev. D57 (1998) 6948, arXiv:hep-lat/9709028.
  2. Phys. Lett. B629 (2005) 27, arXiv:hep-ph/0502004.
  3. Phys. Rev. D73 (2006) 094002, arXiv:hep-ph/0604017
- Slide 17
  4. arXiv:1809.03290
  5. arXiv:1903.10002
  6. Phys. Rev. D 93, 032006
  7. Eur. Phys. J. C77 (2017) 895
- Slide 19
  1. Phys. Rev. D 87, 034028 (2013).

# BACKUP

# Exclusive $|V_{cb}|$ from $B \rightarrow D^* \ell \nu$ untagged

Source	$\rho^2$	$R_1(1)$	$R_2(1)$	$\mathcal{F}(1) V_{cb} $ [%]	$\mathcal{B}(B^0 \rightarrow D^{*-} \ell^+ \nu_\ell)$ [%]
Slow pion efficiency	0.005	0.002	0.001	0.65	1.29
Lepton ID combined	0.001	0.006	0.004	0.68	1.38
$\mathcal{B}(B \rightarrow D^{**} \ell \nu)$	0.002	0.001	0.002	0.26	0.52
$B \rightarrow D^{**} \ell \nu$ form factors	0.003	0.001	0.004	0.11	0.22
$f_{+-}/f_{00}$	0.001	0.002	0.002	0.52	1.06
Fake $e/\mu$	0.004	0.006	0.001	0.11	0.21
Continuum norm.	0.002	0.002	0.001	0.03	0.06
K/ $\pi$ ID	< 0.001	< 0.001	< 0.001	0.39	0.77
Fast track efficiency	-	-	-	0.53	1.05
$N\Upsilon(4S)$	-	-	-	0.68	1.37
$B^0$ lifetime	-	-	-	0.13	0.26
$\mathcal{B}(D^{*+} \rightarrow D^0 \pi_s^+)$	-	-	-	0.37	0.74
$\mathcal{B}(D^0 \rightarrow K\pi)$	-	-	-	0.51	1.02
Total systematic error	0.008	0.009	0.007	1.60	3.21

CLN systematic

Source	$\tilde{a}_0^f$ [%]	$\tilde{a}_1^f$ [%]	$\tilde{a}_1^{F1}$ [%]	$\tilde{a}_2^{F1}$ [%]	$\tilde{a}_0^g$ [%]	$\eta_{EW}\mathcal{F}(1) V_{cb} $ [%]	$\mathcal{B}(B^0 \rightarrow D^{*-} \ell^+ \nu_\ell)$ [%]
Slow pion efficiency	0.79	9.59	5.61	4.46	0.18	0.79	1.57
Lepton ID combined	0.67	5.45	1.35	0.73	0.38	0.67	1.33
$\mathcal{B}(B \rightarrow D^{**} \ell \nu)$	0.05	5.02	4.34	9.31	0.37	0.05	0.10
$B \rightarrow D^{**} \ell \nu$ form factors	0.08	2.08	3.56	6.78	0.12	0.08	0.16
$f_{+-}/f_{00}$	0.56	0.46	0.50	0.48	0.56	0.56	1.05
Fake $e/\mu$	0.07	6.43	3.03	5.92	0.14	0.07	0.11
K/ $\pi$ ID	0.39	0.39	0.39	0.39	0.39	0.39	0.77
Fast track efficiency	0.53	0.53	0.53	0.53	0.53	0.53	1.05
$N(\Upsilon(4S))$	0.69	0.69	0.69	0.69	0.69	0.69	1.37
$B^0$ lifetime	0.13	0.13	0.13	0.13	0.13	0.13	0.26
$\mathcal{B}(D^{*+} \rightarrow D^0 \pi_s^+)$	0.37	0.37	0.37	0.37	0.37	0.37	0.74
$\mathcal{B}(D^0 \rightarrow K\pi)$	0.51	0.51	0.51	0.51	0.51	0.51	1.02
Total systematic error	1.65	13.93	8.69	13.77	1.40	1.65	3.26

BGL systematic

# $B \rightarrow D^{(*)} \pi \ell \nu$ hadronic tagged

arXiv:1803.06444

	$B^+ \rightarrow D^- \pi^+ \ell^+ \nu$	$B^0 \rightarrow \bar{D}^0 \pi^- \ell^+ \nu$
Charged PID	4.8	6.9
$\pi^0$ PID	1.2	6.0
Tracking efficiency	2.6	3.6
$D^{**}$ form factors	0.3	0.2
$D$ meson BRs	1.7	1.6
$B$ meson BRs	0.0	0.1
Number of $B\bar{B}$	1.4	1.4
Tag efficiency	4.6	3.2
$\Upsilon(4S)$ BR	1.2	1.2
<b>Combined</b>	<b>8.3</b>	<b>9.7</b>

	$B^+ \rightarrow D^{*-} \pi^+ \ell^+ \nu$	$B^0 \rightarrow \bar{D}^{*0} \pi^- \ell^+ \nu$
Charged PID	2.1	6.5
$\pi^0$ PID	2.0	5.2
Tracking efficiency	2.9	3.2
$D^{**}$ form factors	0.2	0.1
$D$ meson BRs	1.8	1.1
$B$ meson BRs	0.0	0.1
Number of $B\bar{B}$	1.4	1.4
Tag efficiency	4.2	2.8
$\Upsilon(4S)$ BR	1.2	1.2
<b>Combined</b>	<b>5.8</b>	<b>7.2</b>

The table lists the relative uncertainties in the branching fractions in percent for each channel for the combined fits. The last row gives the combined variation of all sources.



Source		$\Delta F_L^{D^*}$
Monte Carlo statistics	AR shape and peaking background	$\pm 0.032$
	CB shape	$\pm 0.010$
	Background scale factors	$\pm 0.001$
Background modeling	$B \rightarrow D^{**} \ell \nu$	$\pm 0.003$
	$B \rightarrow D^{**} \tau \nu$	$\pm 0.011$
	$B \rightarrow$ hadrons	$\pm 0.005$
	$B \rightarrow \bar{D}^* M$	$\pm 0.004$
Signal modeling	Form factors	$\pm 0.002$
	$\cos \theta_{\text{hel}}$ resolution	$\pm 0.003$
	Acceptance non-uniformity	+0.015 -0.005
Total		+0.039 -0.037

# Measurement of the relative $B^- \rightarrow D^0/D^{*0}/D^{**0} \mu^- \nu_\mu$ branching fractions using $B^-$ mesons from $B_{s2}^{*0}$ decays

arXiv:1807.10722

	Source of uncertainty	$f_{D^0}$	$f_{D^{**0}}$
Statistical	OSK sample	0.025	0.027
	Templates	0.047	0.052
Floating syst.	Signal form-factors	0.006	0.004
	Non- $B^-$ , $\bar{B}^0$ backgrounds	0.004	0.004
	$B^-$ , $\bar{B}^0$ background normalization	0.003	0.015
	$\bar{B}^0$ fraction and $m_{\text{miss}}^2$ shape	0.004	0.030
Fixed syst.	$D^{**0}$ branching fractions	0.025	0.044
	Relative signal efficiency	0.003	0.003
Total uncertainty		0.056	+0.070 -0.074

TABLE I. Systematic uncertainties contributing to the  $\mathcal{R}(D^{(*)})$  results.

Source	$\Delta R(D)$ (%)	$\Delta R(D^*)$ (%)
$D^{**}$ composition	0.76	1.41
Fake $D^{(*)}$ calibration	0.19	0.11
$B_{\text{tag}}$ calibration	0.07	0.05
Feed-down factors	1.69	0.44
Efficiency factors	1.93	4.12
Lepton efficiency and fake rate	0.36	0.33
Slow pion efficiency	0.08	0.08
MC statistics	4.39	2.25
$B$ decay form factors	0.55	0.28
Luminosity	0.10	0.04
$\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)$	0.05	0.02
$\mathcal{B}(D)$	0.35	0.13
$\mathcal{B}(D^*)$	0.04	0.02
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.15	0.14
Total	5.21	4.94

Source	Uncertainty (%)
$\bar{B} \rightarrow \pi\ell^- \bar{\nu}_\ell$ form-factor	0.9
$\bar{B} \rightarrow \rho\ell^- \bar{\nu}_\ell$ form-factor	12
$B^- \rightarrow K_L^0 \pi^-$	5.5
$B^- \rightarrow \mu^- \bar{\nu}_\mu \gamma$	6
Continuum shape	15
Signal peak shape	11
Trigger	8
$\mathcal{B}(\bar{B} \rightarrow \pi\ell^- \bar{\nu}_\ell)$	3.4
Total	24.6

# $B \rightarrow \eta \ell \nu$ and $B \rightarrow \eta' \ell \nu$ hadronic tagged

Phys. Rev. D 96, 091102(R) 2017

Mode $q^2$ [GeV <sup>2</sup> ]	$\eta \rightarrow \gamma\gamma$			$\eta \rightarrow \pi^+\pi^-\pi^0$			Both $\eta$ modes			$\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$ All
	All	< 12	> 12	All	< 12	> 12	All	< 12	> 12	
Track finding	$\pm 0.35$	$\pm 0.35$	$\pm 0.35$	$\pm 1.05$	$\pm 1.05$	$\pm 1.05$	$\pm 0.5$	$\pm 0.5$	$\pm 0.5$	$\pm 1.05$
Photon finding	$\pm 4.0$	$\pm 4.0$	$\pm 4.0$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 3.1$	$\pm 3.1$	$\pm 3.1$	$\pm 4.0$
$\pi^0$ reconstruction	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 2.5$	$\pm 2.5$	$\pm 2.5$	$\pm 0.5$	$\pm 0.5$	$\pm 0.5$	$\pm 0.0$
$\pi^0$ veto	$\pm 2.5$	$\pm 2.5$	$\pm 2.5$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 0.0$
Pion ID	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 1.0$	$\pm 1.0$	$\pm 1.0$	$\pm 0.20$	$\pm 0.20$	$\pm 0.20$	$\pm 1.0$
Lepton ID	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$	$\pm 2.0$
Lepton fake rate	$\pm 0.36$	$^{+0.19}_{-0.13}$	$\pm 0.11$	$^{+0.46}_{-0.50}$	$^{+0.42}_{-0.47}$	$^{+0.18}_{-0.16}$	$^{+0.47}_{-0.44}$	$\pm 0.51$	$^{+0.02}_{-0.07}$	$^{+1.6}_{-1.8}$
Signal model	$\pm 0.83$	$\pm 0.75$	$\pm 1.0$	$\pm 0.50$	$\pm 0.70$	$\pm 0.46$	$\pm 0.88$	$\pm 0.71$	$\pm 2.0$	$\pm 0.28$
$b \rightarrow ul\nu_\ell$ form factors	$\pm 1.1$	$\pm 0.49$	$\pm 0.72$	$^{+1.8}_{-2.6}$	$^{+0.14}_{-0.16}$	$^{+0.82}_{-1.4}$	$^{+0.31}_{-0.43}$	$^{+0.73}_{-1.1}$	$^{+0.77}_{-0.70}$	$^{+0.92}_{-0.56}$
$b \rightarrow ul\nu_\ell$ branching fractions	$^{+0.26}_{-0.20}$	$\pm 1.0$	$^{+1.4}_{-1.3}$	$^{+0.04}_{-0.05}$	$\pm 0.05$	$^{+0.85}_{-0.95}$	$^{+0.50}_{-0.45}$	$^{+1.5}_{-1.8}$	$^{+0.86}_{-1.2}$	$^{+1.9}_{-2.4}$
$b \rightarrow cl\nu_\ell$ form factors	$^{+1.0}_{-0.15}$	$^{+2.3}_{-0.60}$	$\pm 0.0$	$^{+0.21}_{-0.06}$	$^{+0.70}_{-0.22}$	$\pm 0.0$	$^{+1.1}_{-0.10}$	$^{+1.3}_{-0.24}$	$\pm 0.0$	$^{+0.18}_{-0.23}$
$b \rightarrow cl\nu_\ell$ branching fractions	$\pm 0.14$	$\pm 0.80$	$\pm 0.29$	$\pm 0.28$	$^{+0.43}_{-0.45}$	$^{+0.18}_{-0.28}$	$\pm 0.13$	$\pm 0.64$	$^{+0.21}_{-0.27}$	$\pm 0.62$
Secondary leptons	$^{+0.00}_{-0.06}$	$\pm 0.12$	$^{+0.01}_{-0.03}$	$^{+0.07}_{-0.04}$	$^{+0.15}_{-0.13}$	$^{+0.02}_{-0.12}$	$^{+0.03}_{-0.01}$	$\pm 0.08$	$^{+0.06}_{-0.04}$	$^{+0.01}_{-0.00}$
$\mathcal{B}(\eta^{(\prime)})$ [29]	$\pm 0.50$	$\pm 0.50$	$\pm 0.50$	$\pm 1.2$	$\pm 1.2$	$\pm 1.2$	$\pm 0.50$	$\pm 0.50$	$\pm 0.50$	$\pm 1.7$
Hadronic tag	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$	$\pm 4.2$
$N(B\bar{B})$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$	$\pm 1.4$
Continuum	$^{+0.77}_{-0.80}$	$^{+0.98}_{-0.96}$	$^{+0.24}_{-0.30}$	$^{+0.66}_{-0.64}$	$^{+1.1}_{-1.2}$	$^{+0.71}_{-0.62}$	$\pm 0.47$	$\pm 0.83$	$^{+1.2}_{-1.3}$	$\pm 3.9$
Fit procedure	$\pm 2.9$	$\pm 9.8$	$\pm 2.0$	$\pm 6.3$	$\pm 8.7$	$\pm 9.6$	$\pm 2.2$	$\pm 5.6$	$\pm 3.2$	$\pm 5.2$
Total	$\pm 7.6$	$^{+12.3}_{-12.1}$	$\pm 7.3$	$^{+8.8}_{-9.0}$	$\pm 10.6$	$^{+11.3}_{-11.4}$	$\pm 6.7$	$\pm 8.7$	$^{+7.4}_{-7.5}$	$^{+9.7}_{-9.8}$

# Measurement of $R(D)$ and $R(D^*)$ with a semileptonic tag

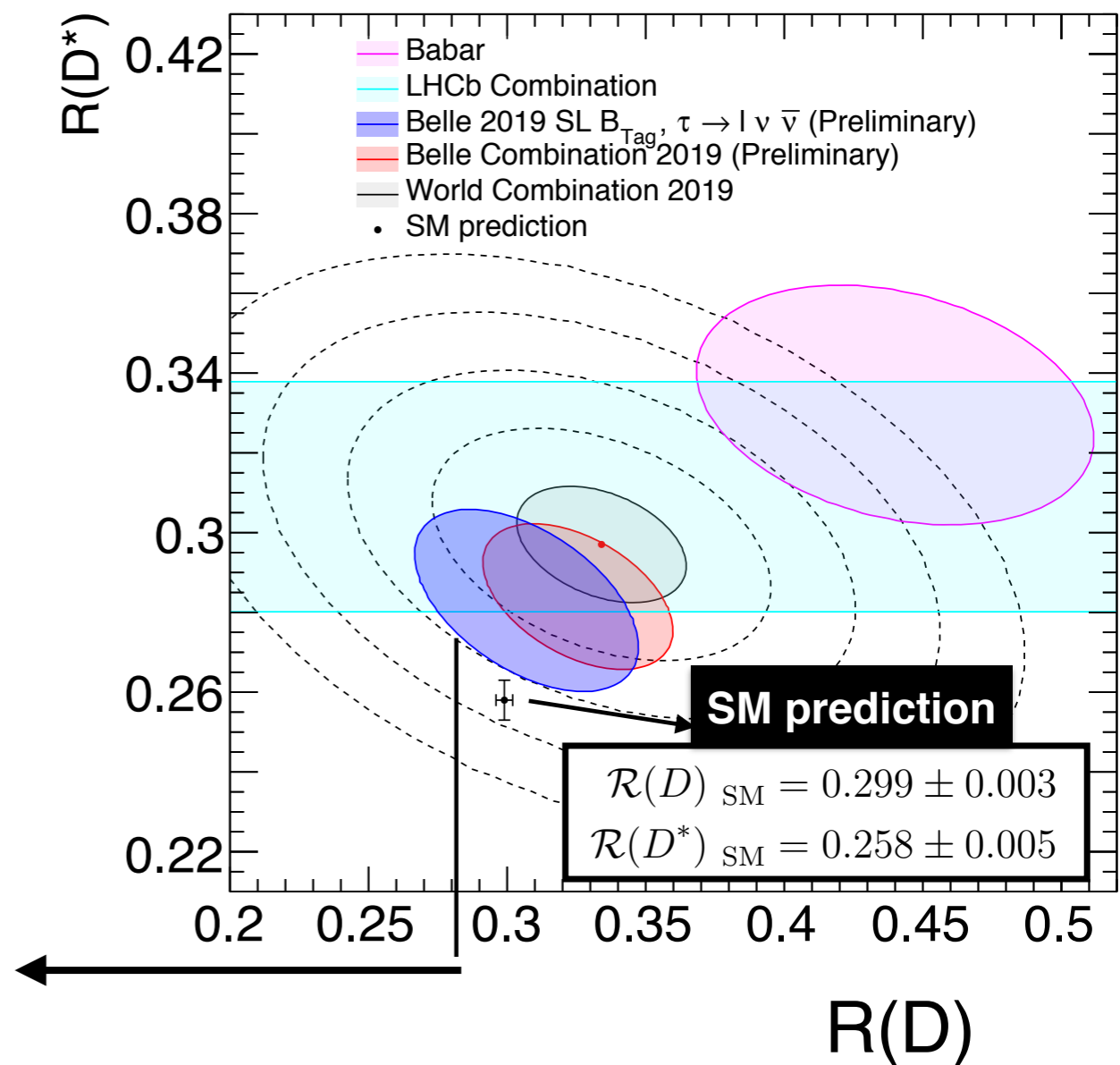
$$R(D) \equiv \frac{\mathcal{B}(\bar{B} \rightarrow D^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^+ \ell^- \bar{\nu}_\ell)} \quad R(D^*) \equiv \frac{\mathcal{B}(\bar{B} \rightarrow D^{*+} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{*+} \ell^- \bar{\nu}_\ell)} \quad \text{where } \ell = e, \mu$$

**Signal:**  $B^{0/\pm} \rightarrow D^{(*)} \tau^- \nu$     **Normalisation:**  $B^{0/\pm} \rightarrow D^{(*)} \ell^- \nu$     **B-tag:**  $B^{0/\pm} \rightarrow D^{(*)} \ell^- \nu$

- First  $R(D)$  and  $R(D^*)$  measurement with semileptonic tag
- Most Precise Measurement till date !!!
- Results compatible with SM expectations within 1.2 sigma
- $R(D)$  and  $R(D^*)$  WA tension reduces to 3.1 sigma

$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014$$

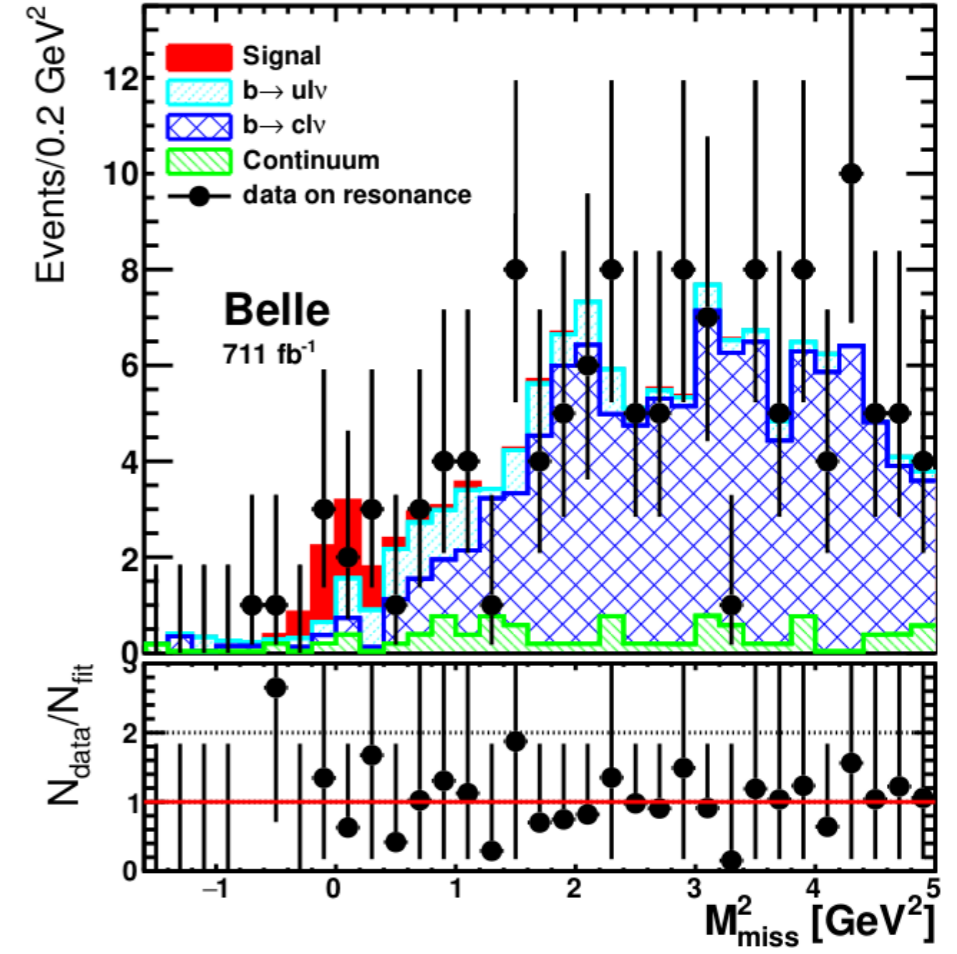
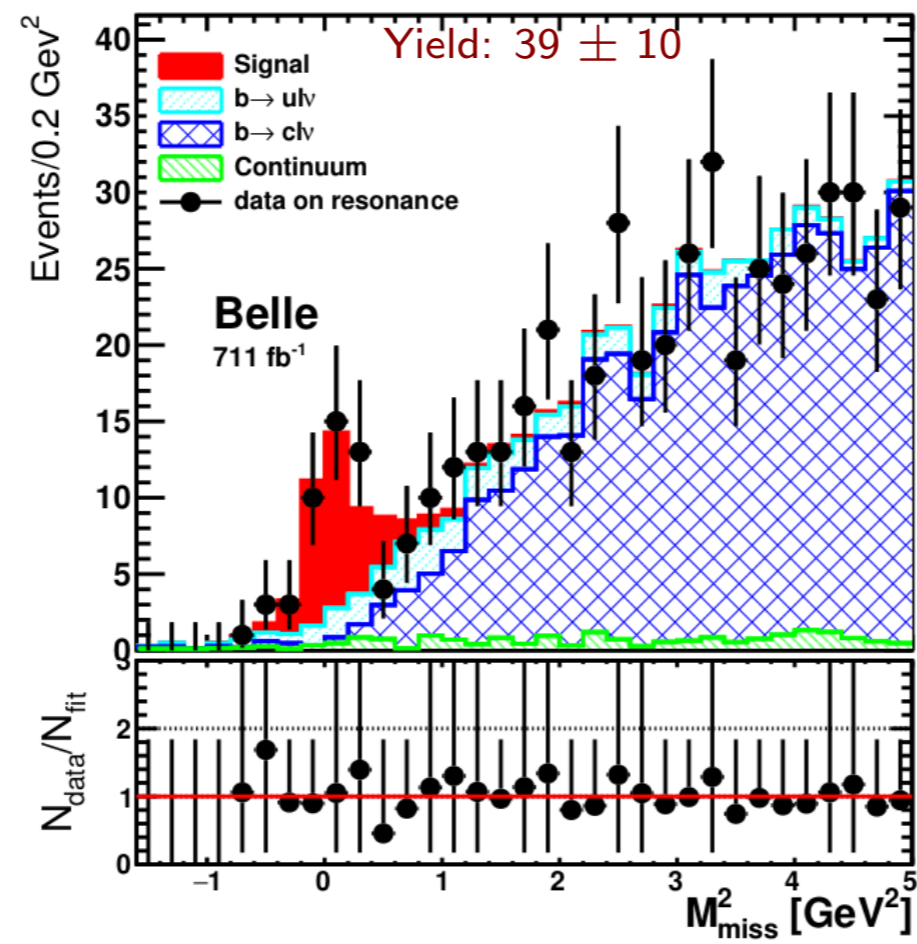


To measure the inclusive  $b \rightarrow ul \nu$  rate we must understand exclusive components.

$\eta \rightarrow \gamma \gamma, \pi^+ \pi^- \pi^0$   
 $\eta' \rightarrow \pi^+ \pi^- \gamma, \eta \gamma$

$B \rightarrow \eta l \nu_e$

$B \rightarrow \eta' l \nu_e$



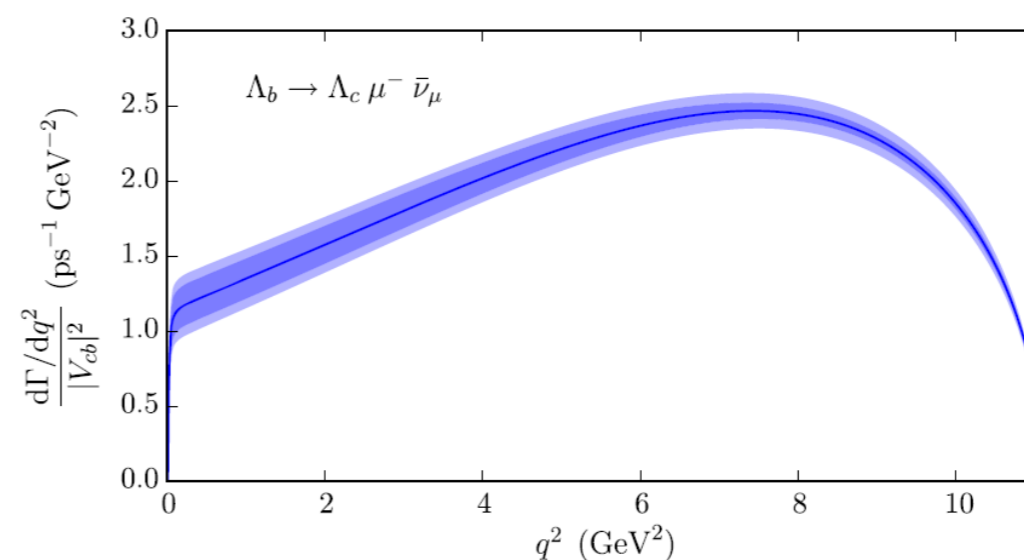
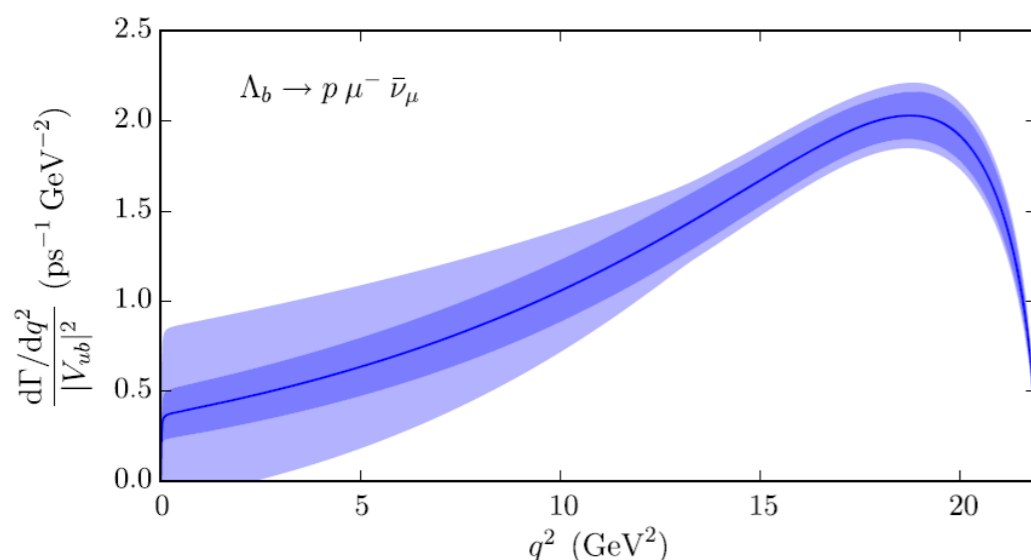
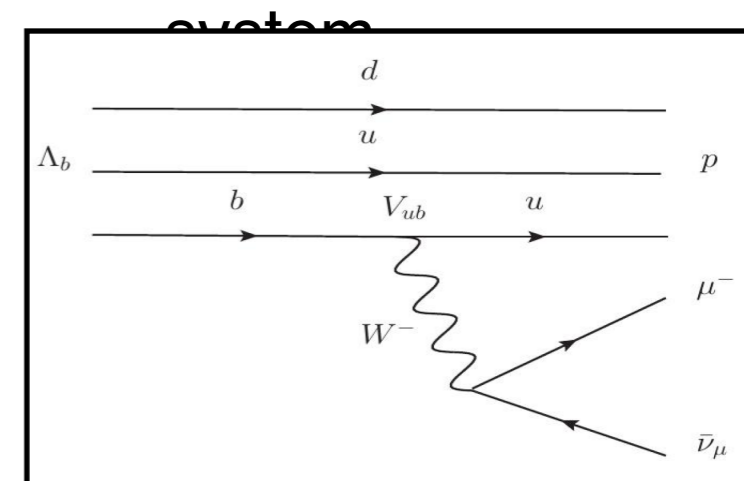
BACKUP

$$\mathcal{B}(B^+ \rightarrow \eta l^+ \nu) = (4.2 \pm 1.1_{stat} \pm 0.3_{syst}) \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow \eta' l^+ \nu) < 0.72 \times 10^{-4} \quad 90\% \text{ C.L.}$$

$$|V_{ub}| = (3.59 \pm 0.58_{stat} \pm 0.13_{syst}^{+0.29}_{-0.32_{theo}}) \times 10^{-3}$$

- Missing neutrino momentum  $\rightarrow$  B not fully reconstructed
- Generally affected by much higher (x10)  $X_b \rightarrow X_c \mu \nu$  backgrounds
- Excellent  $\mu$  and  $p$  PID LHCb from RICH/Muon
- precision vertexing and tracking used
  - displaced  $p_\mu$  vertex as signature in detector
- High production fraction of  $\Lambda_b$  :  $\sim 20\%$  of b-hadron
- Normalise signal yield to a  $|V_{cb}|$  decay  $\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu$ 
  - cancels many systematic uncertainties  $\rightarrow$  the production rate of  $\Lambda_b$
- Improved FF calculations from theory for  $\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu$  and  $\Lambda_b \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu$  in high  $q^2$  region  $\rightarrow$  there FF calculations from theory are most precise





# Analysis Strategy $\Lambda_b \rightarrow p\mu^-\nu_\mu$

- Determine yields of  $\Lambda_b \rightarrow p\mu^-\nu_\mu$  and  $\Lambda_b \rightarrow (\Lambda_c^+ \rightarrow pK^-\pi^+)\mu^-\nu_\mu$
- Estimate relative experimental efficiency with high precision
  - Measuring B.F:

$$\frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^-\nu_\mu)_{q^2 > 15 \text{ GeV}^2}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \mu^-\nu_\mu)_{q^2 > 7 \text{ GeV}^2}} = (1.00 \pm 0.04(\text{stat}) \pm 0.08(\text{syst})) \times 10^{-2}$$

with

$$\frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^-\nu_\mu)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c^+ \mu^-\nu_\mu)} = R_{\text{FF}} \times \frac{|V_{ub}|^2}{|V_{cb}|^2} \text{ with } R_{\text{FF}} = 0.68 \pm 0.07$$

implies

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004(\text{exp.}) \pm 0.004(\text{theo.})$$

using WA  $|V_{cb}| = (39.5 \pm 0.8) \times 10^{-3}$  gives

$$|V_{ub}| = (3.27 \pm 0.15(\text{exp.}) \pm 0.16(\text{theo.}) \pm 0.06(|V_{cb}|)) \times 10^{-3}$$