

# Development and application of a dispersion-matched ion-optical mode of the SRC and BigRIPS system for high-resolution missing-mass spectroscopy experiments with primary beams

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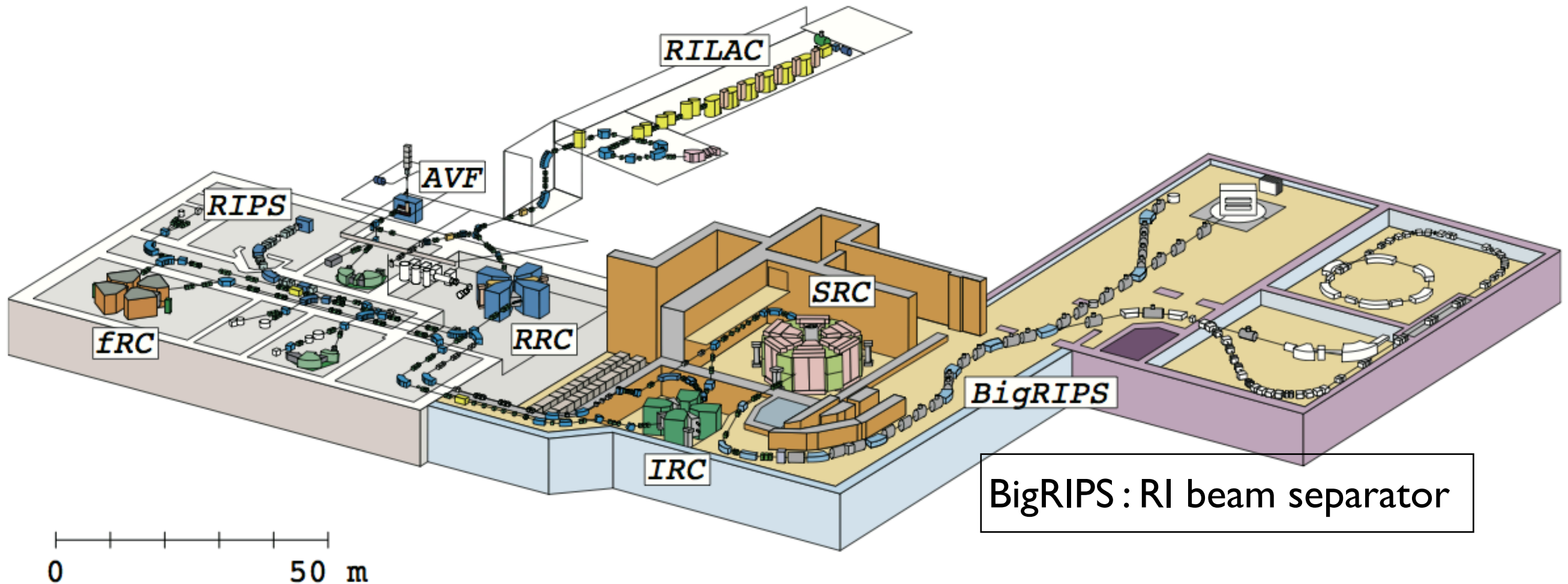
GSI : H. Geissel, E. Haettner, H. Weick

Univ. Notre Dame : G. P. A. Berg

CNS Univ. Tokyo : M. Takaki

# Spectroscopy with primary beams at RIBF

RI Beam Factory (RIBF), RIKEN, Japan



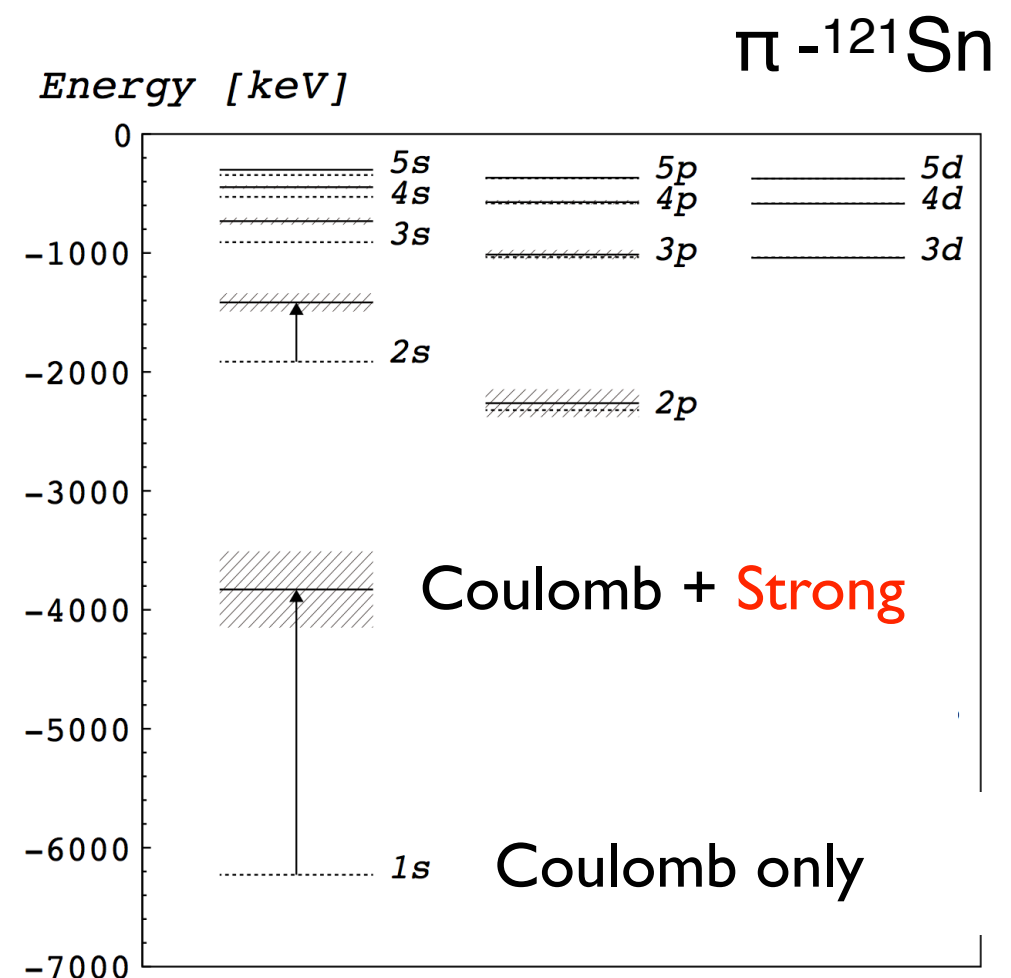
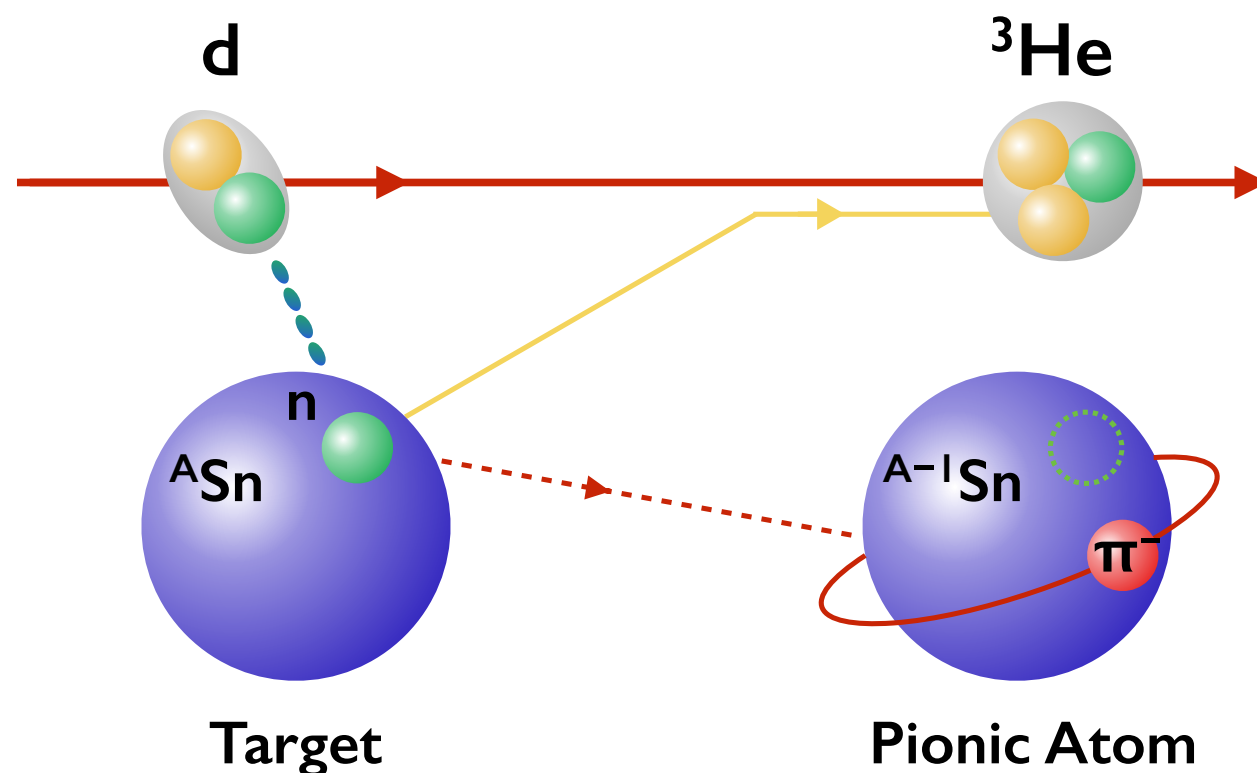
- ◇ High-intensity primary beam from SRC
- ◇ BigRIPS used as a high-resolution and large-acceptance spectrometer with powerful background suppression

Opportunity for precision missing-mass spectroscopy  
with reactions using primary ion beams

# Physics cases

## Precision spectroscopy of deeply-bound $\pi$ -atoms

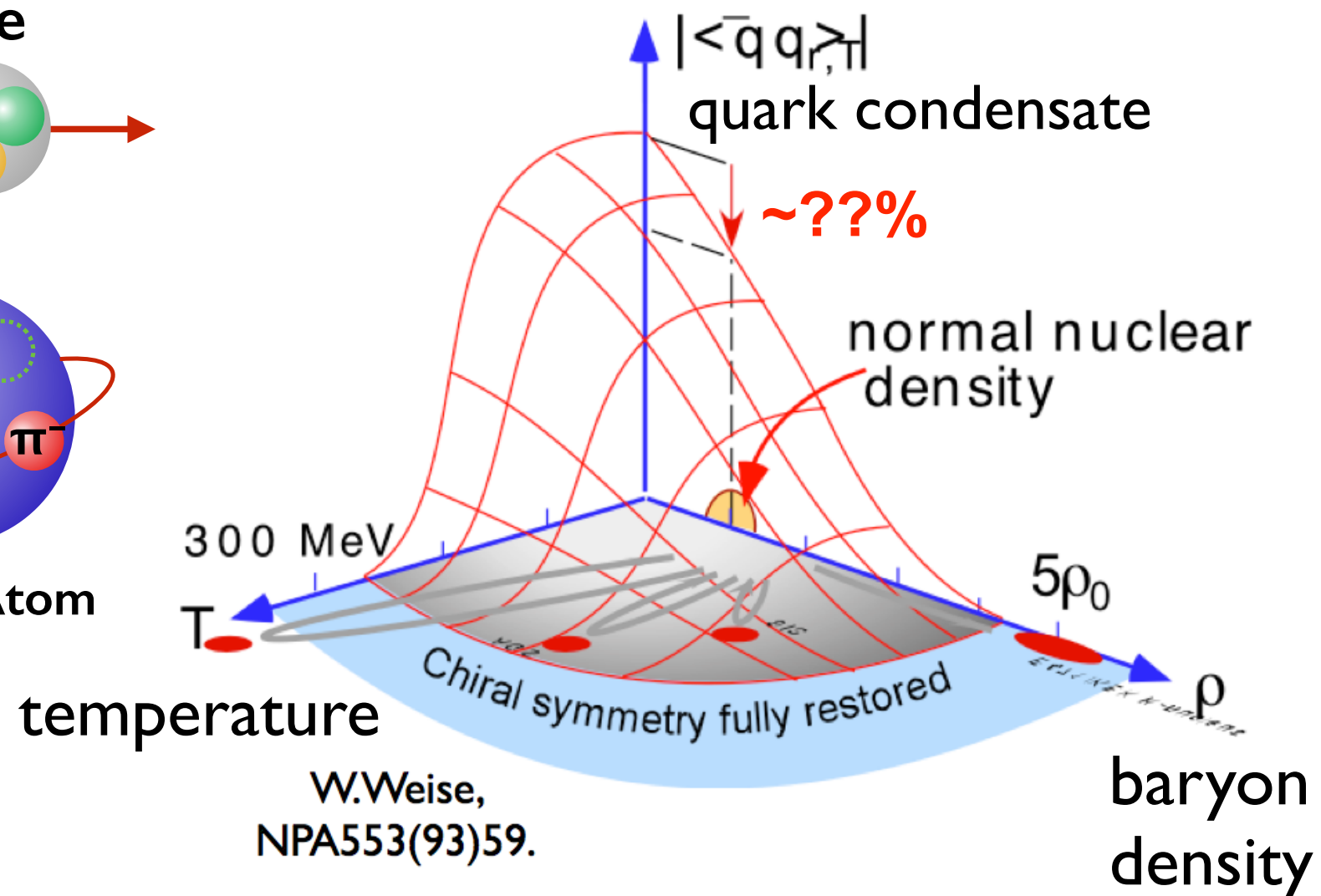
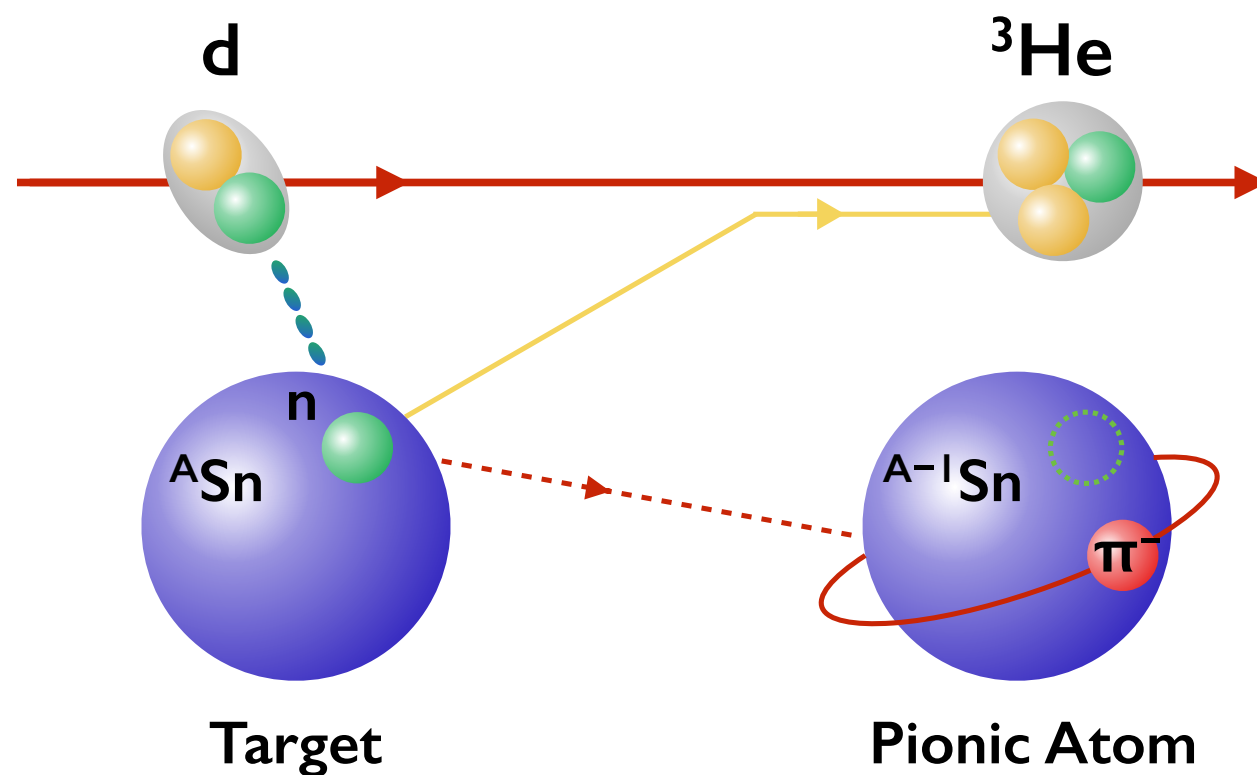
- Missing mass spectroscopy of  $^A\text{Sn}(d, ^3\text{He})$  reaction
- $\pi$ -A strong interaction potential  $\rightarrow$  Chiral symmetry restoration



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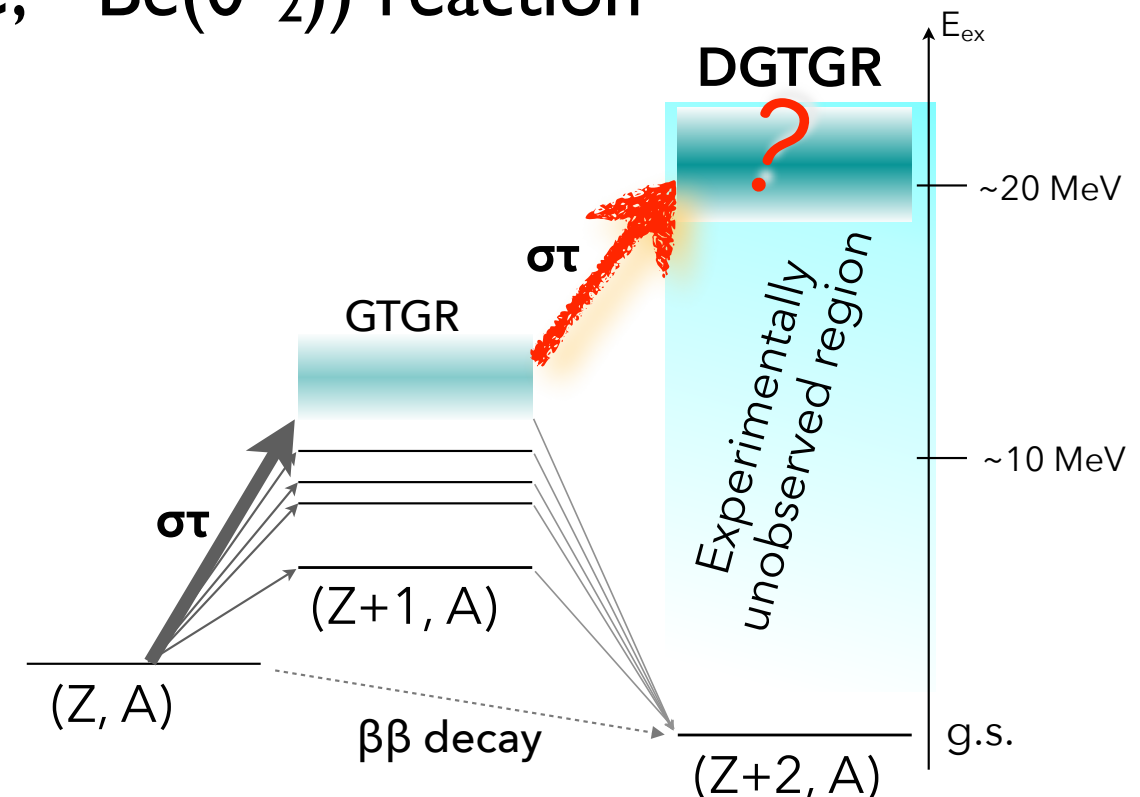
# Physics cases

## Precision spectroscopy of deeply-bound $\pi$ -atoms

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## Search for Double Gamow–Teller Giant Resonance (DGTGR)

- Missing mass spectroscopy of  $^{48}\text{Ca}(^{12}\text{C}, ^{12}\text{Be}(0^+_2))$  reaction
- yet to be established experimentally
- provide information on  $0\nu\beta\beta$  NME



# Physics cases

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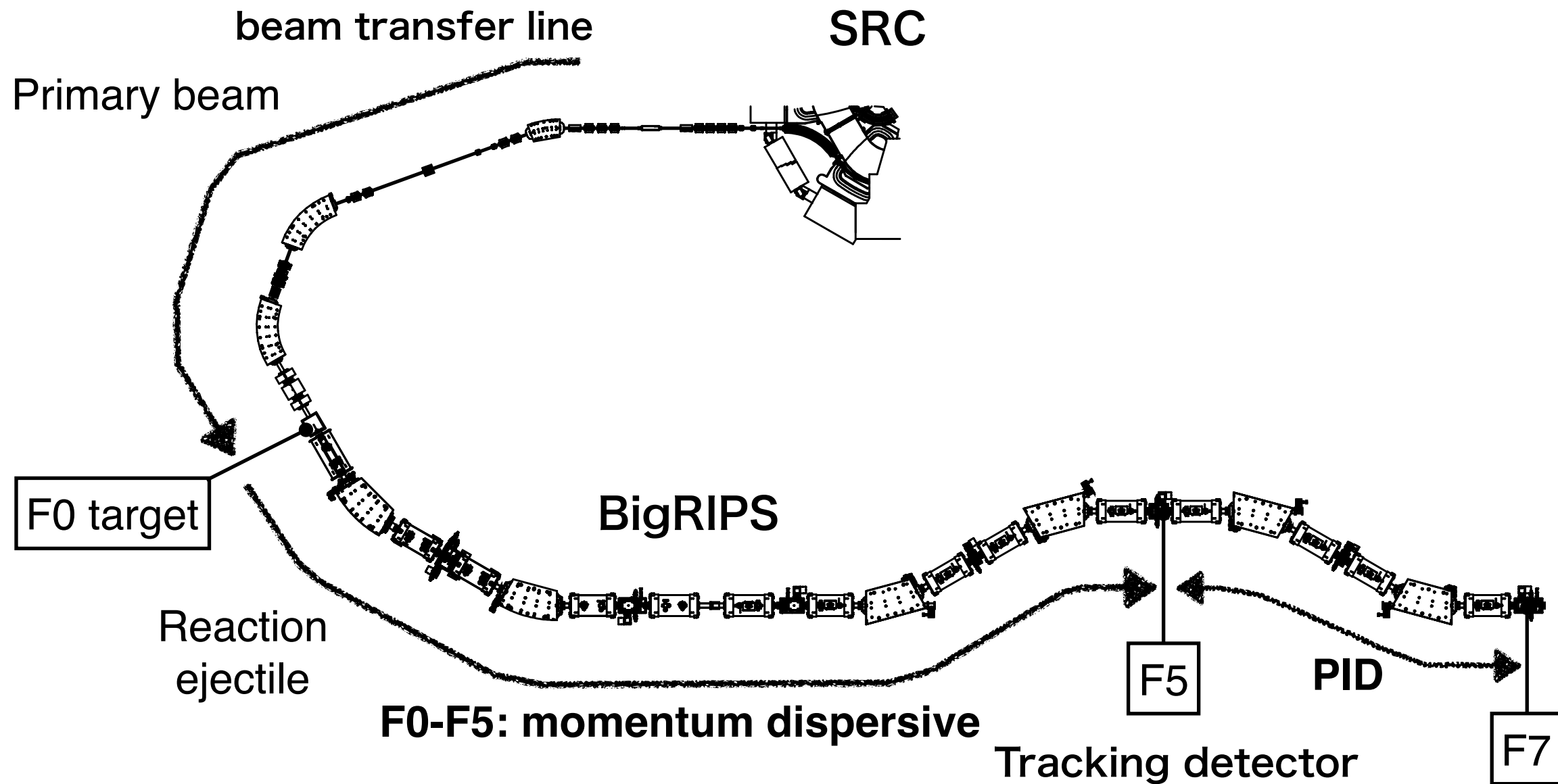
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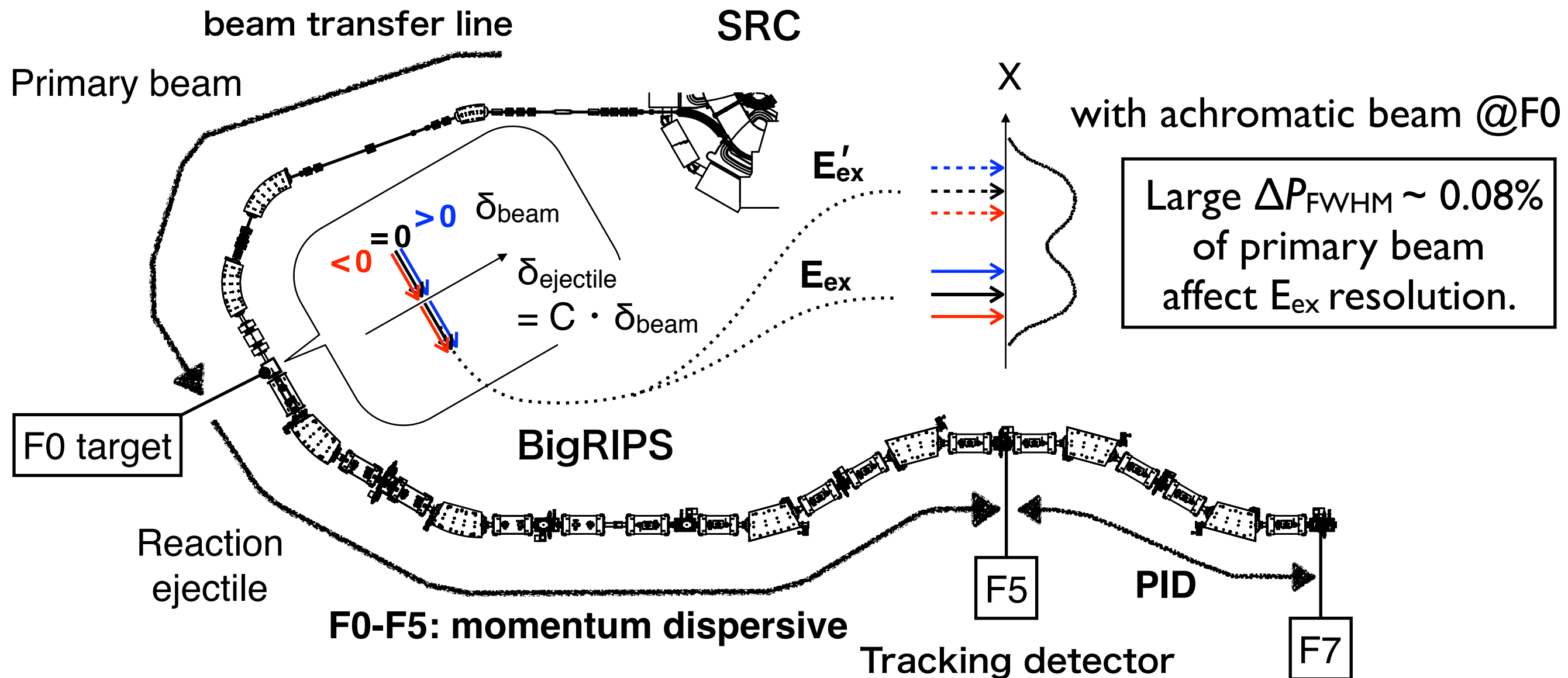
- Missing mass spectroscopy of  $^{48}\text{Ca}(^{12}\text{C}, ^{12}\text{Be}(0^+_2))$  reaction
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High-resolution is a key requirement  
for both experiments

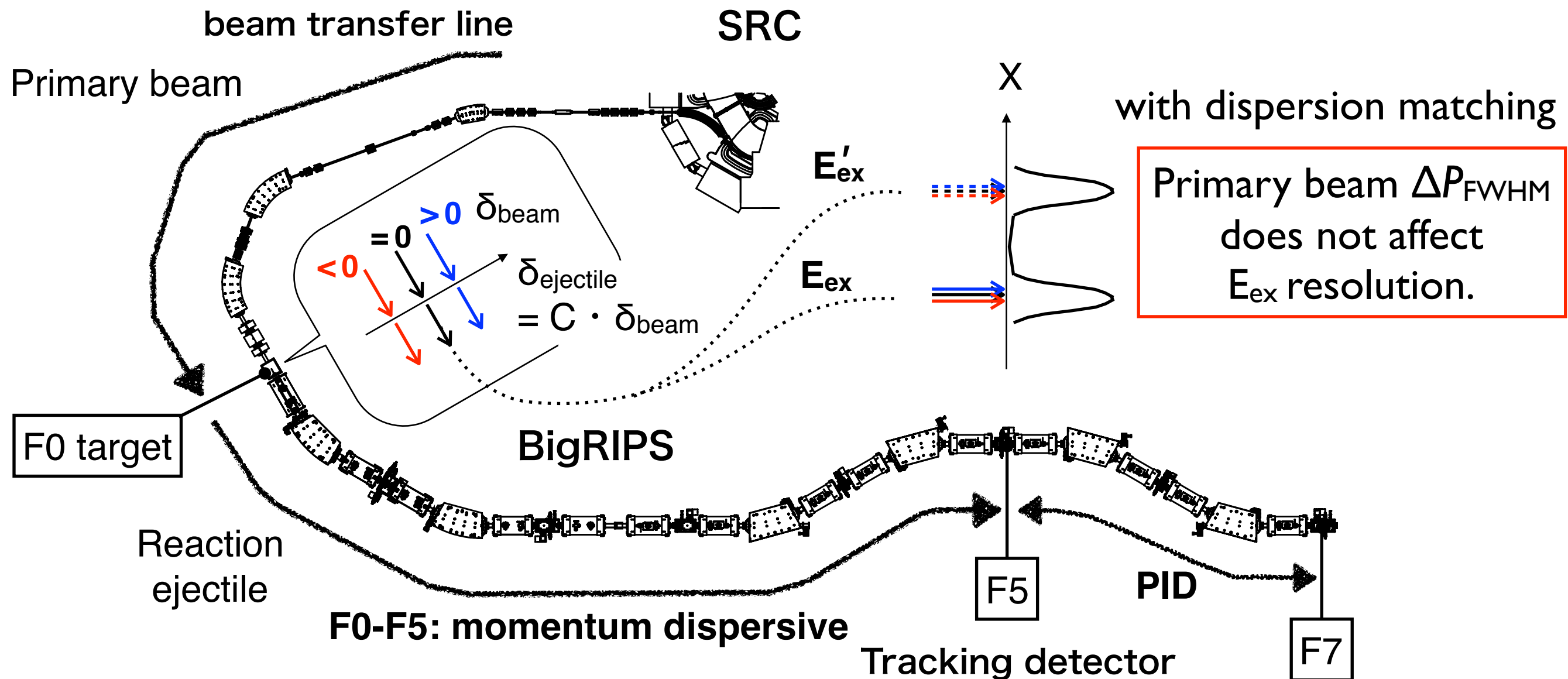
# Dispersion-matched ion optics



# Dispersion-matched ion optics

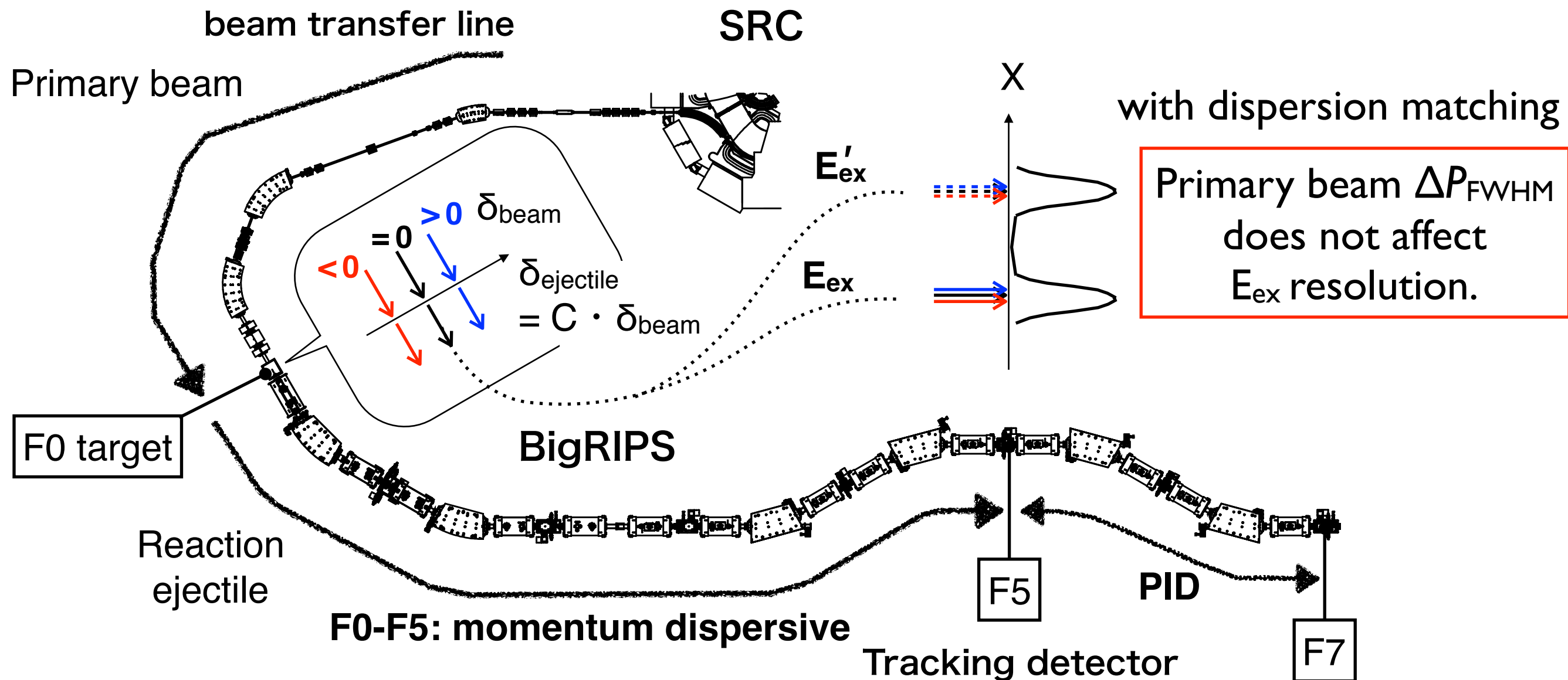


# Dispersion-matched ion optics





# Dispersion-matched ion optics



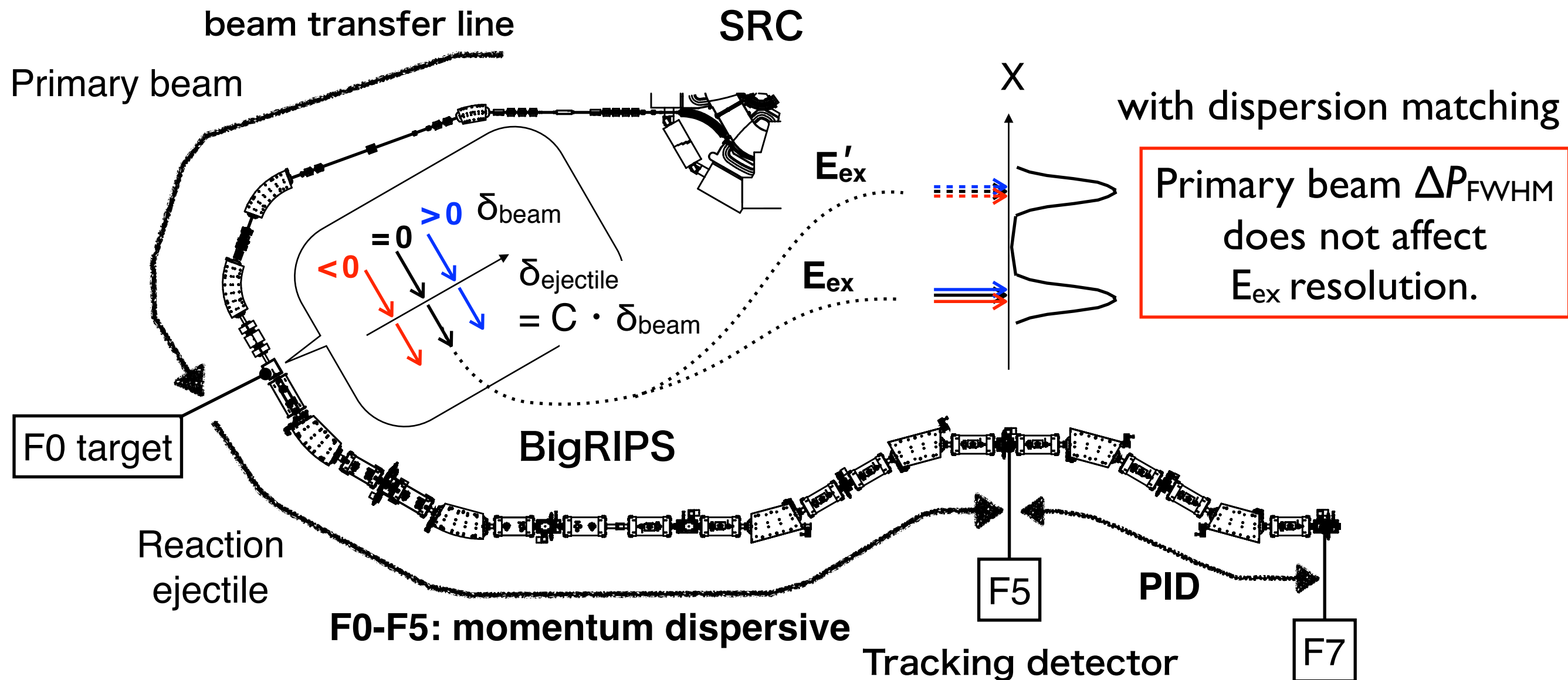
## Dispersion matching condition

$$(X|\delta)_{\text{SRC-F5}} = 0 \longrightarrow$$

$$(X|\delta)_{\text{SRC-F0}} (X|X)_{\text{F0-F5}} + C \cdot (X|\delta)_{\text{F0-F5}} = 0$$

$$\begin{aligned} \pi\text{-atom} : C &= 1.31, & (X|\delta)_{\text{SRC-F0}} &= 44.6 \text{ mm/\%} \\ \text{DGTGR} : C &= 1.0, & (X|\delta)_{\text{SRC-F0}} &= 34.1 \text{ mm/\%} \end{aligned}$$

# Dispersion-matched ion optics



## Dispersion matching condition

$$(X|\delta)_{SRC-F5} = 0 \longrightarrow (X|\delta)_{SRC-F0} (X|X)_{F0-F5} + C \cdot (X|\delta)_{F0-F5} = 0$$

$$\text{Resolving power} = \left| \frac{(X|\delta)_{F0-F5}}{\Delta X_{F0} \cdot (X|X)_{F0-F5}} \right| = \left| \frac{(X|\delta)_{SRC-F0}}{C \cdot \Delta X_{F0}} \right|$$

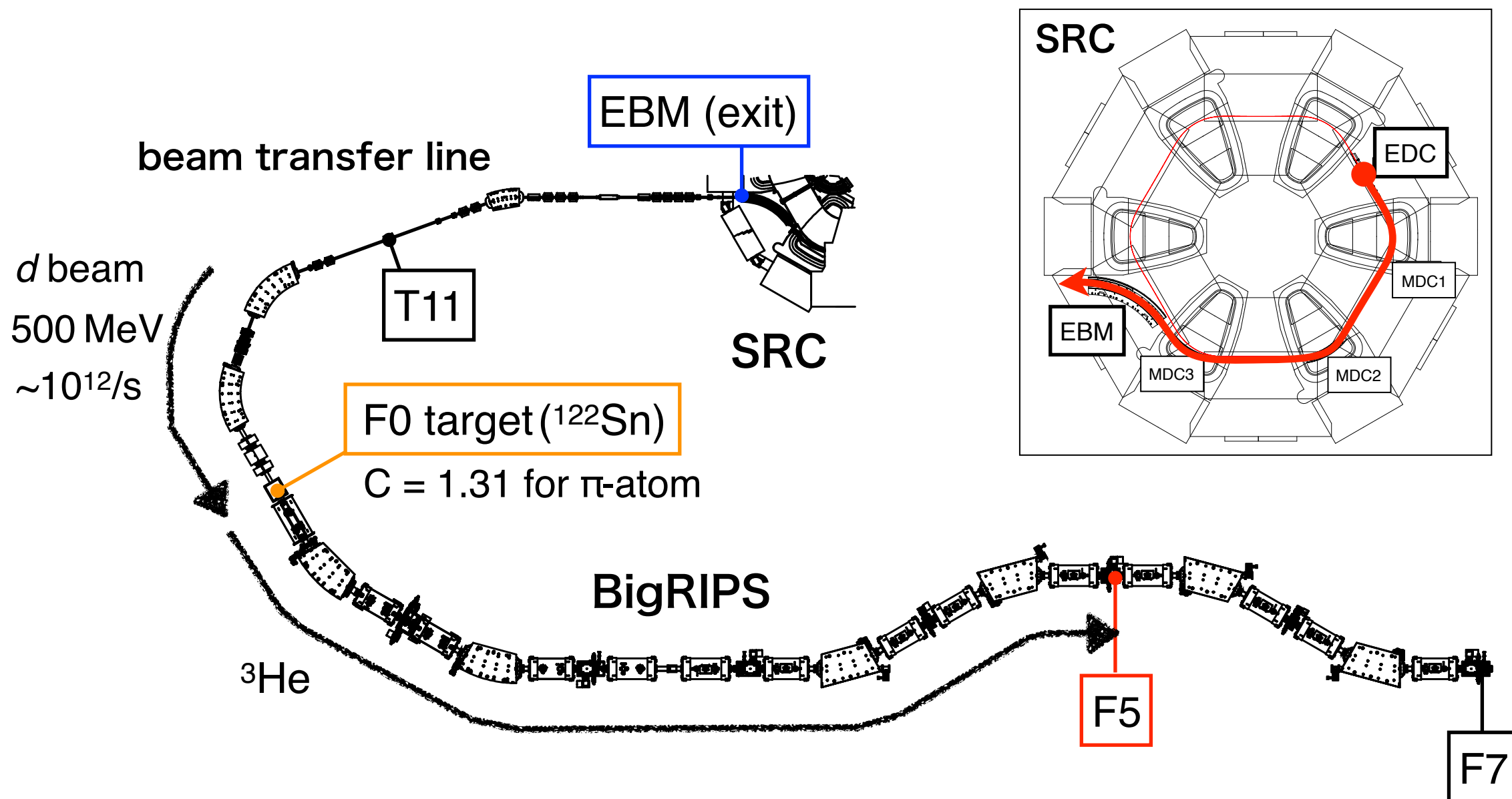
-1.82

62mm/%

# First experiments of $\pi$ -atom in 2010 and 2014

## Simulation-based approach

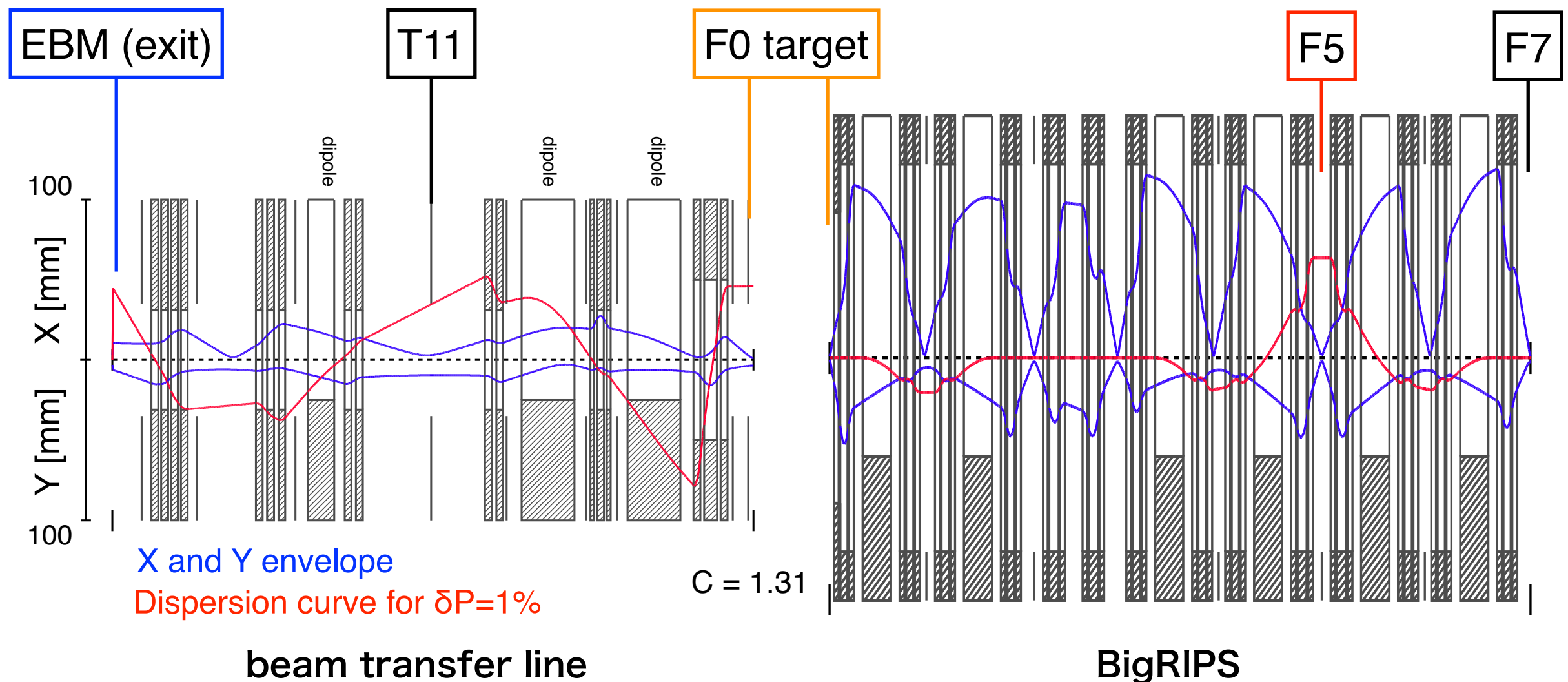
1. Assume achromatic beam waist at EDC (electrostatic deflection channel)
2. EDC to EBM exit (extraction bending magnet) transport by Runge–Kutta calculation
3. Design EBM exit to Target (F0) to fulfill dispersion-matching condition



# First experiments of $\pi$ -atom in 2010 and 2014

## Simulation-based approach

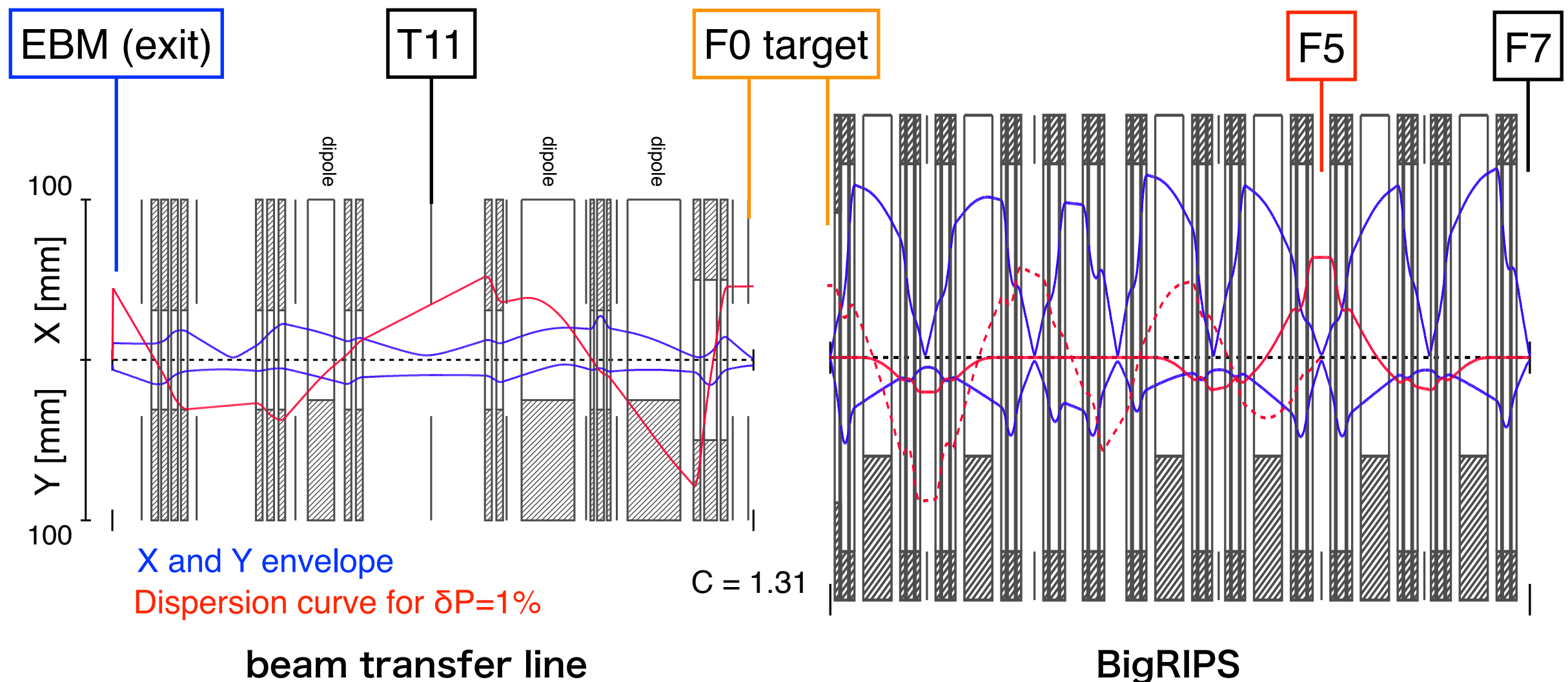
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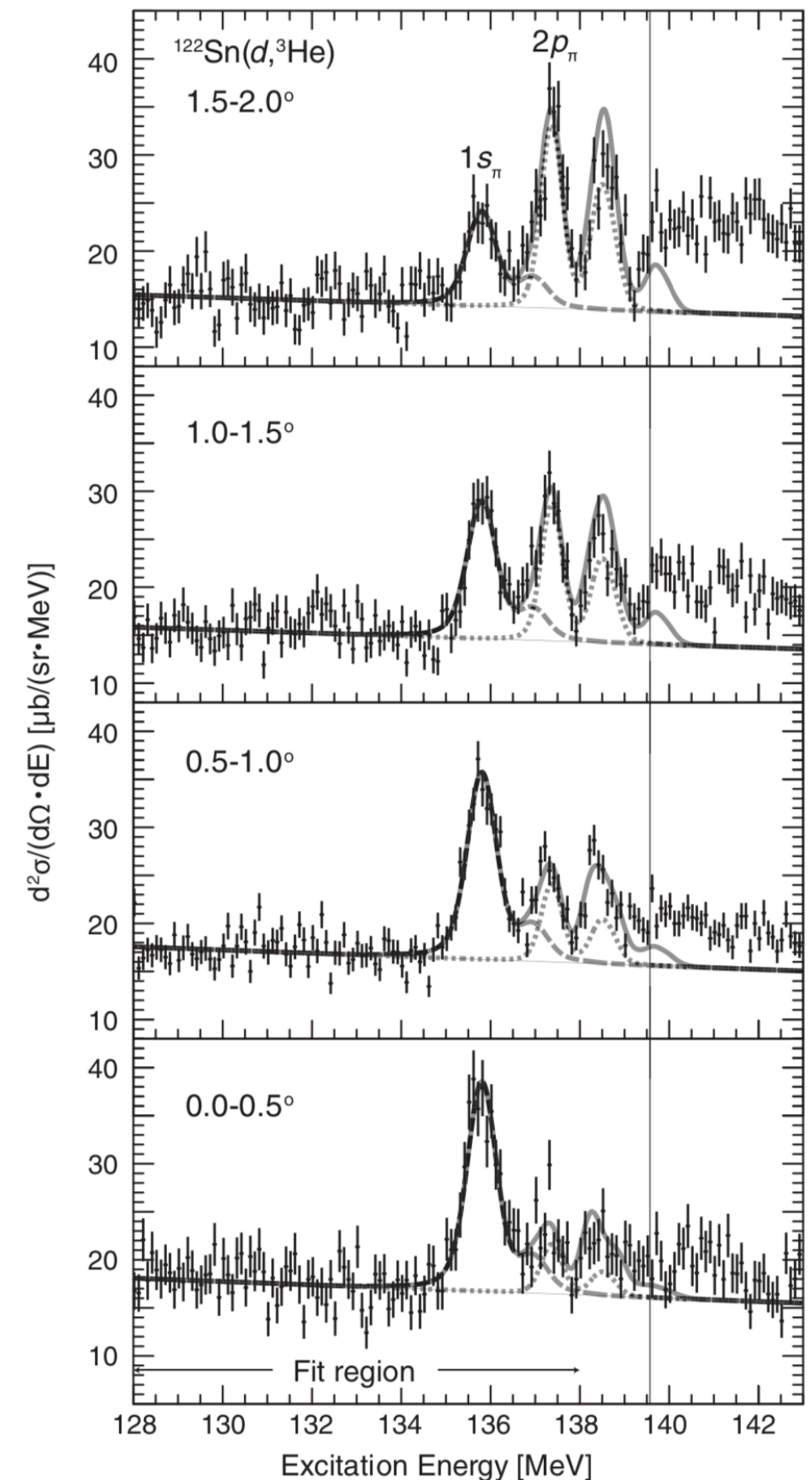


# $\pi$ - $^{121}\text{Sn}$ excitation spectrum – pilot run in 2010 –

only 15 hours DAQ

First observation of angle-dependence  
of  $\pi$ -atom formation cross section

Takahiro Nishi, Kenta Itahashi, et al.,  
Phys. Rev. Lett 120, 152505 (2018)



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Achieved resolution:

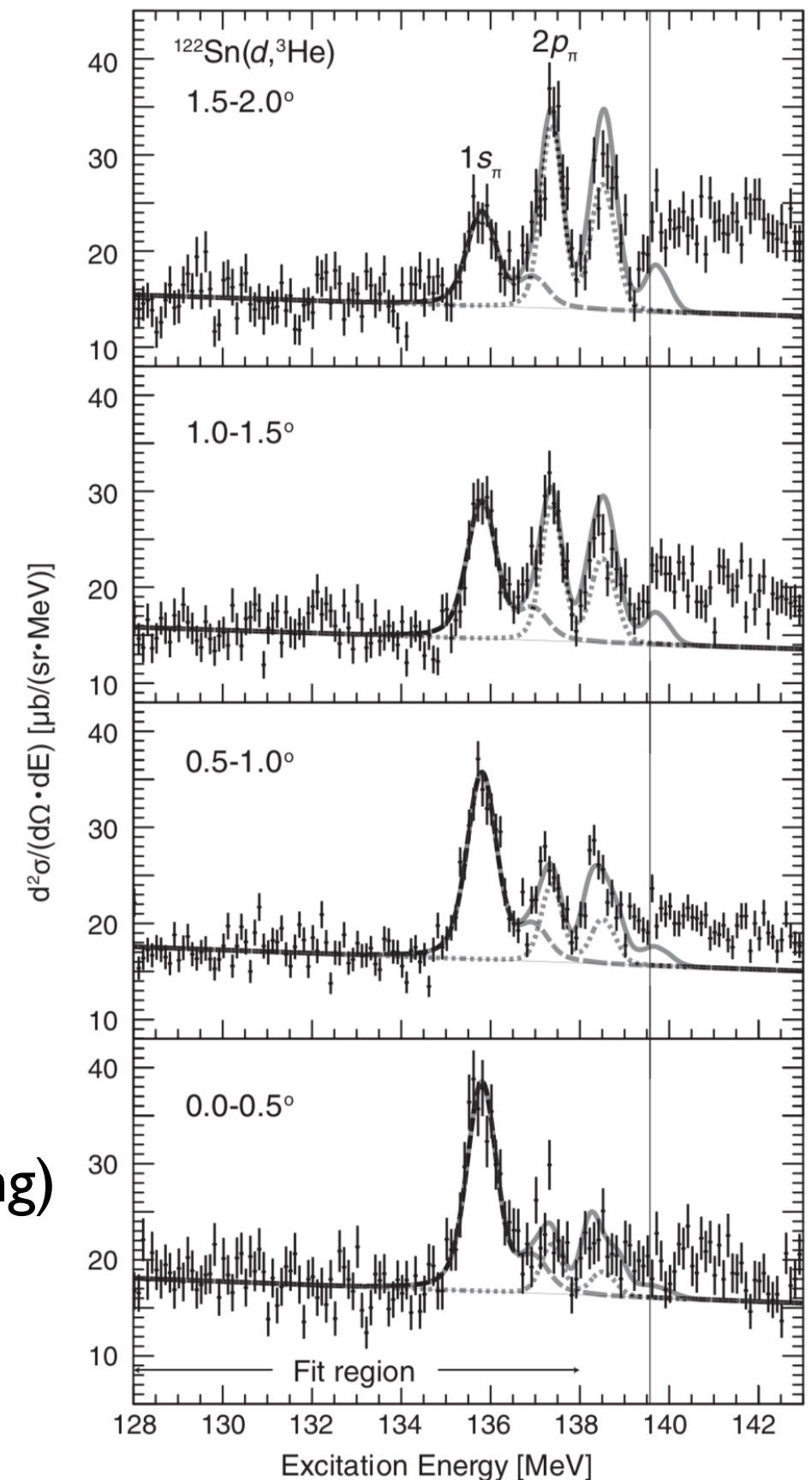
Total (FWHM): 420 keV

$\Delta P_{\text{beam}}$  contribution: 280 keV

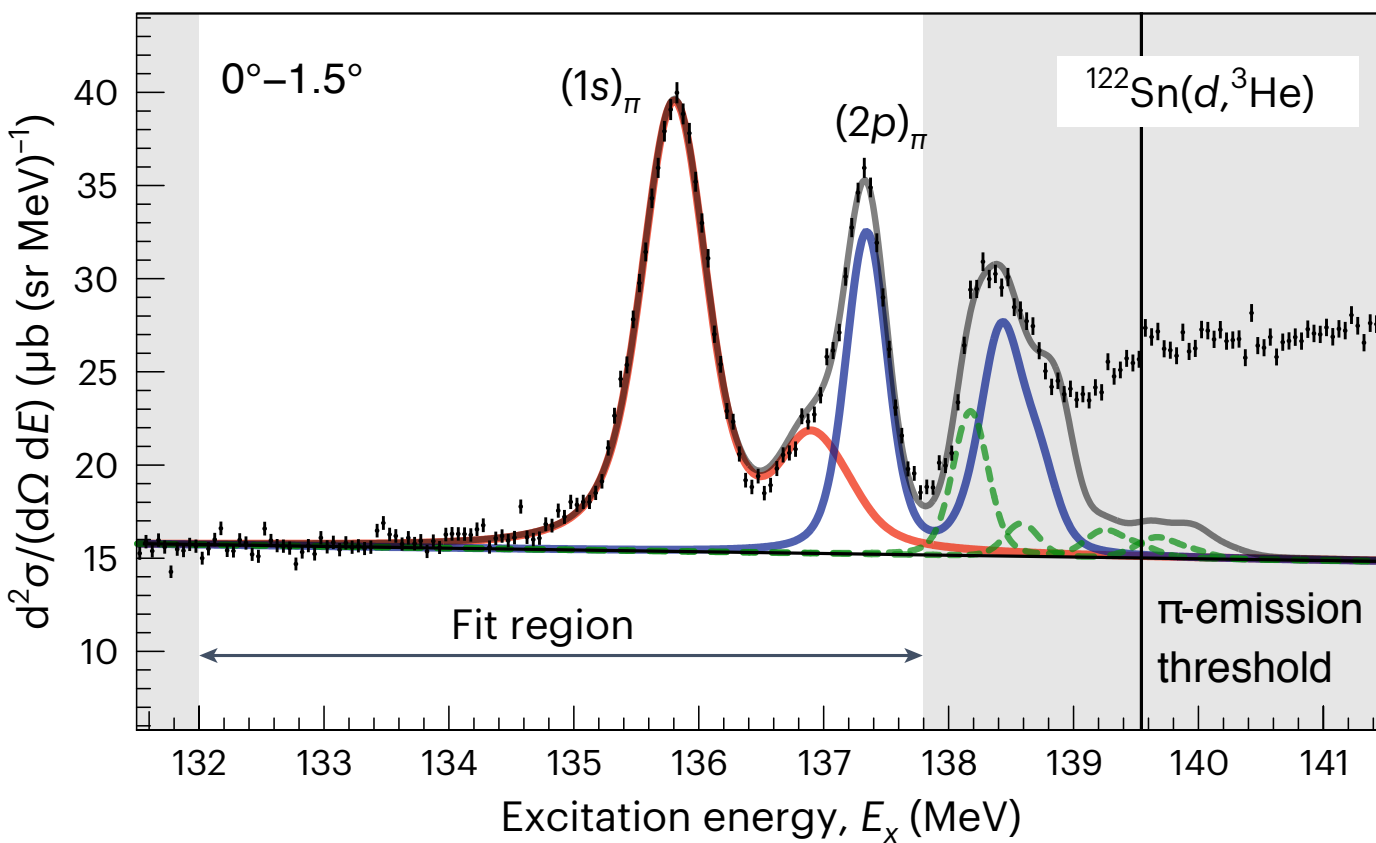
Dispersion matching condition:

$(X|\delta)$  at F0 target  $\sim 24$  mm/% (deduced)

44 mm/% (designed for matching)



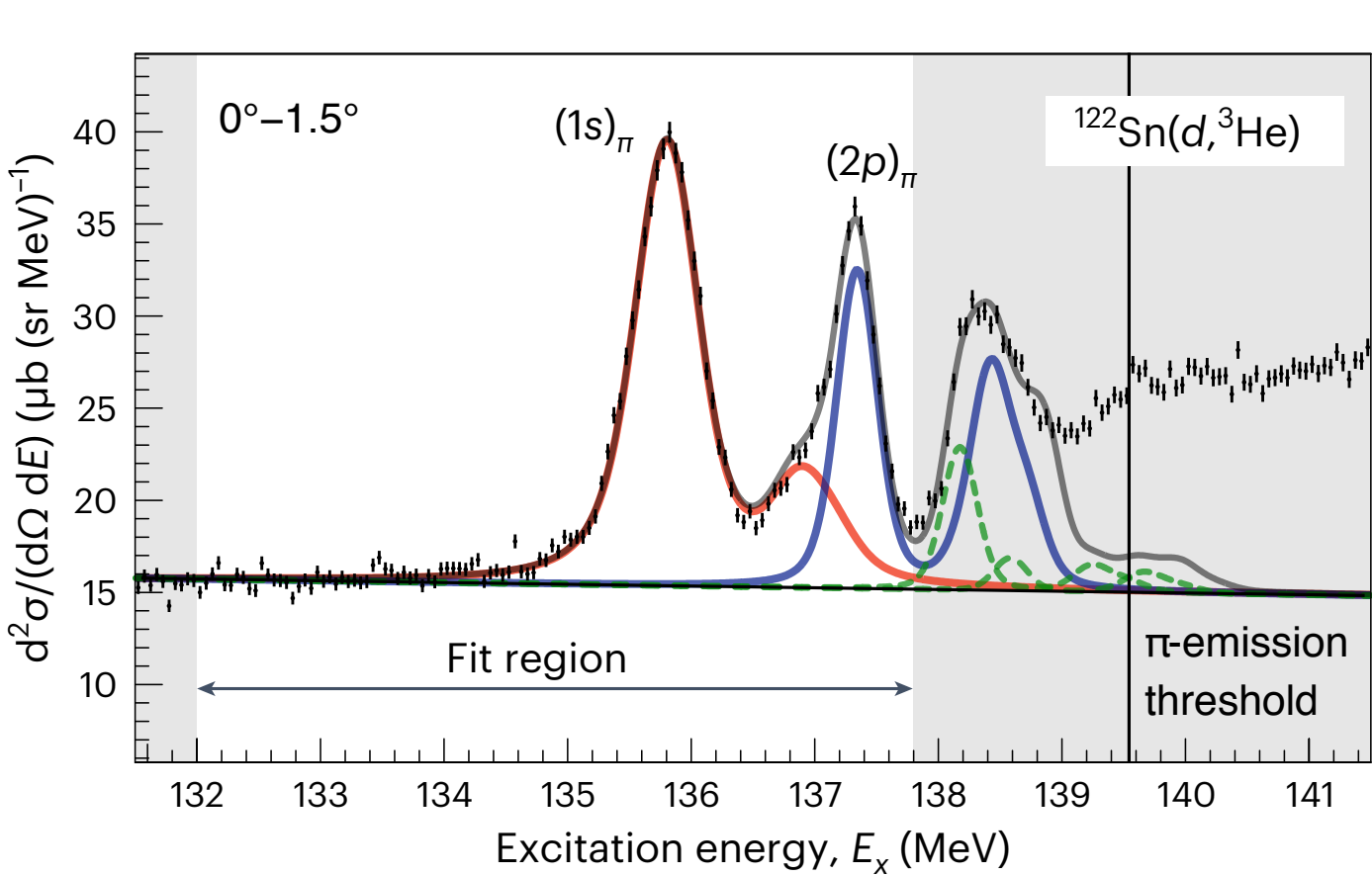
# $\pi$ - $^{121}\text{Sn}$ excitation spectrum – Experiment in 2014 –



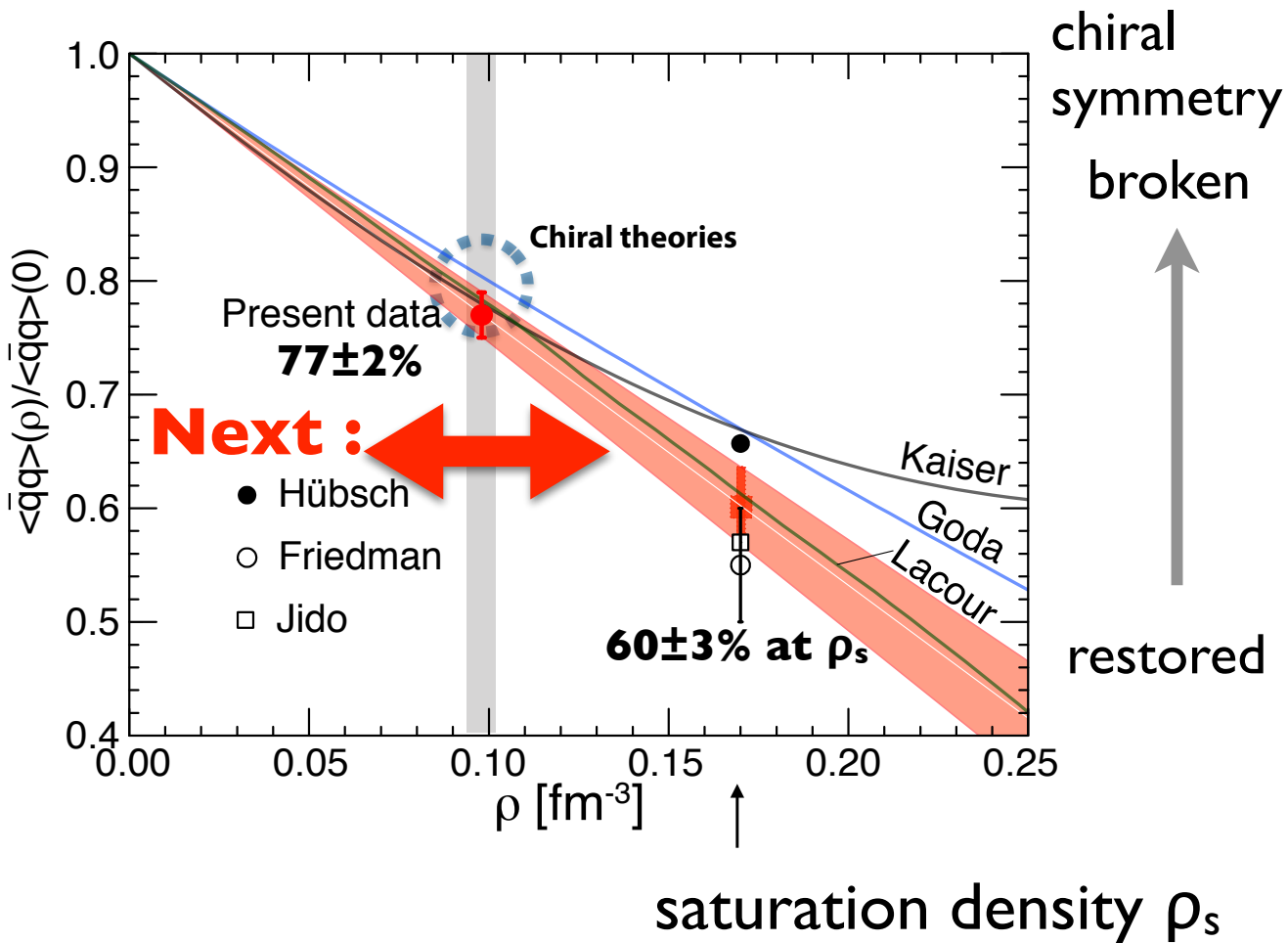
1s and 2p states observed  
simultaneously  
with high-statistics

T. Nishi, K. Itahashi, et al.,  
Nature Phys. 19, 788 (2023).

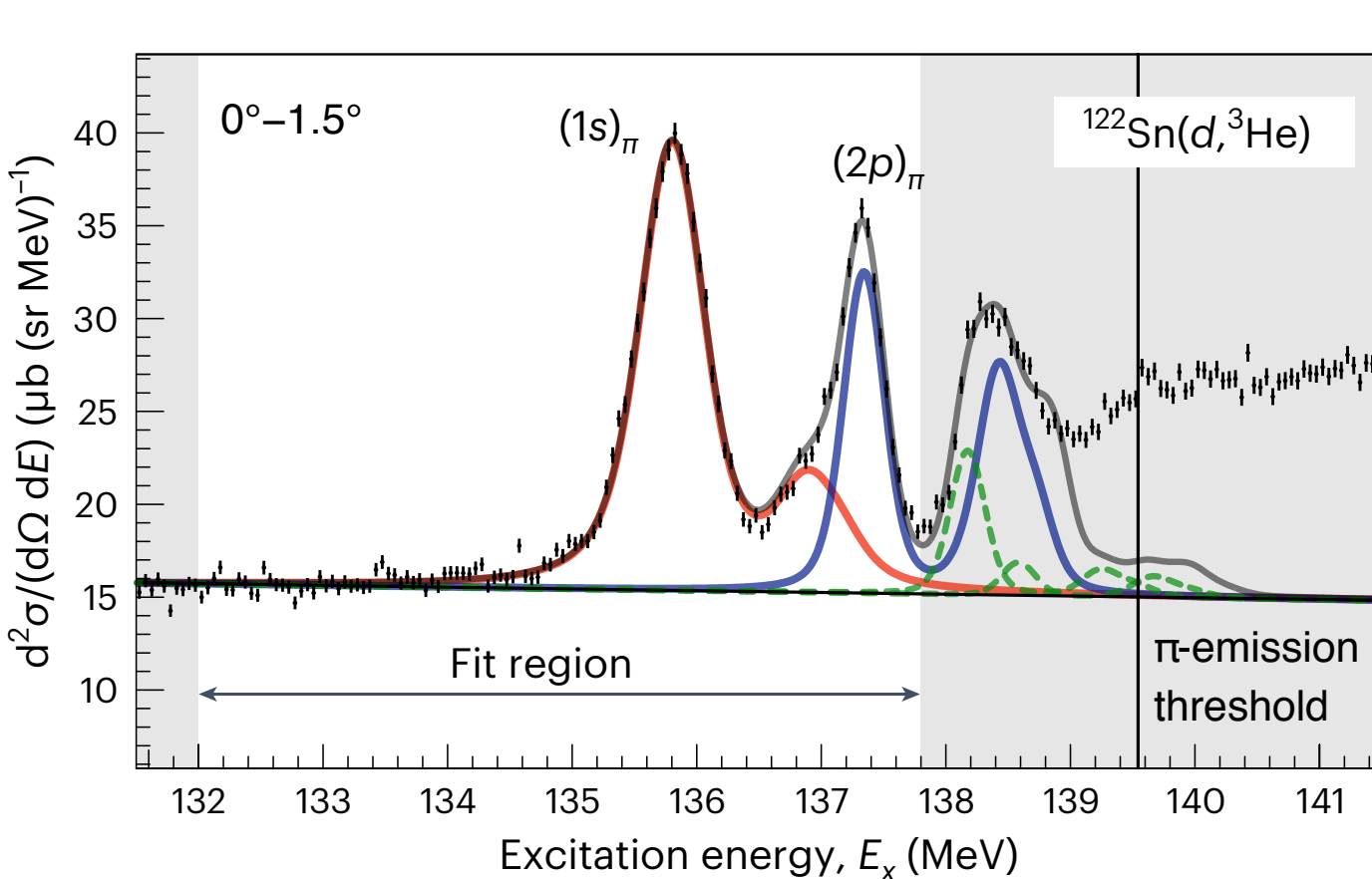
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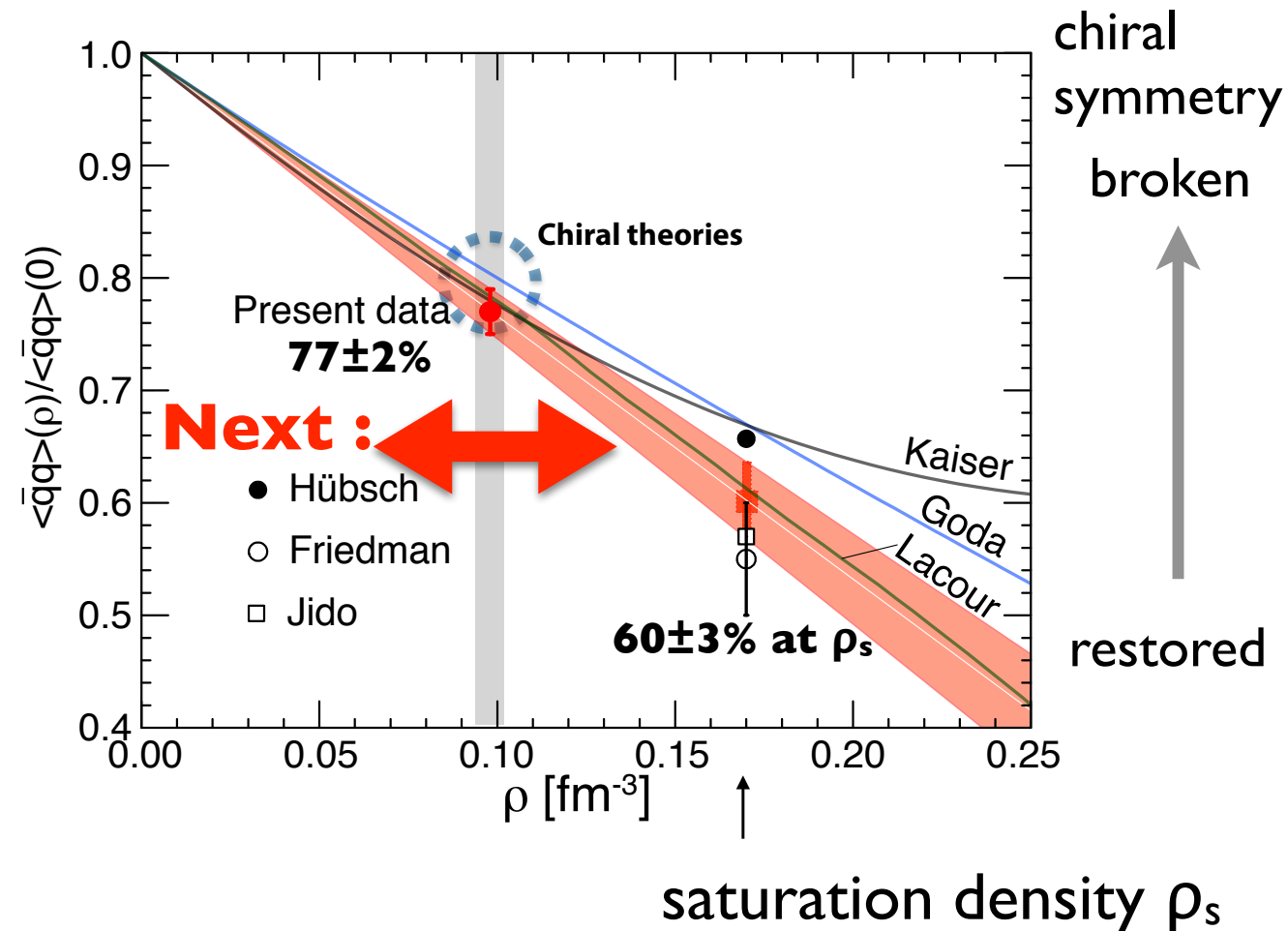
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# $\pi$ - $^{121}\text{Sn}$ excitation spectrum – Experiment in 2014 –



T. Nishi, K. Itahashi, et al.,  
Nature Phys. 19, 788 (2023).



Achieved resolution:

Total (FWHM): 290 keV  
 $\Delta P_{\text{beam}}$  contribution : 220 keV

Dispersion matching condition:

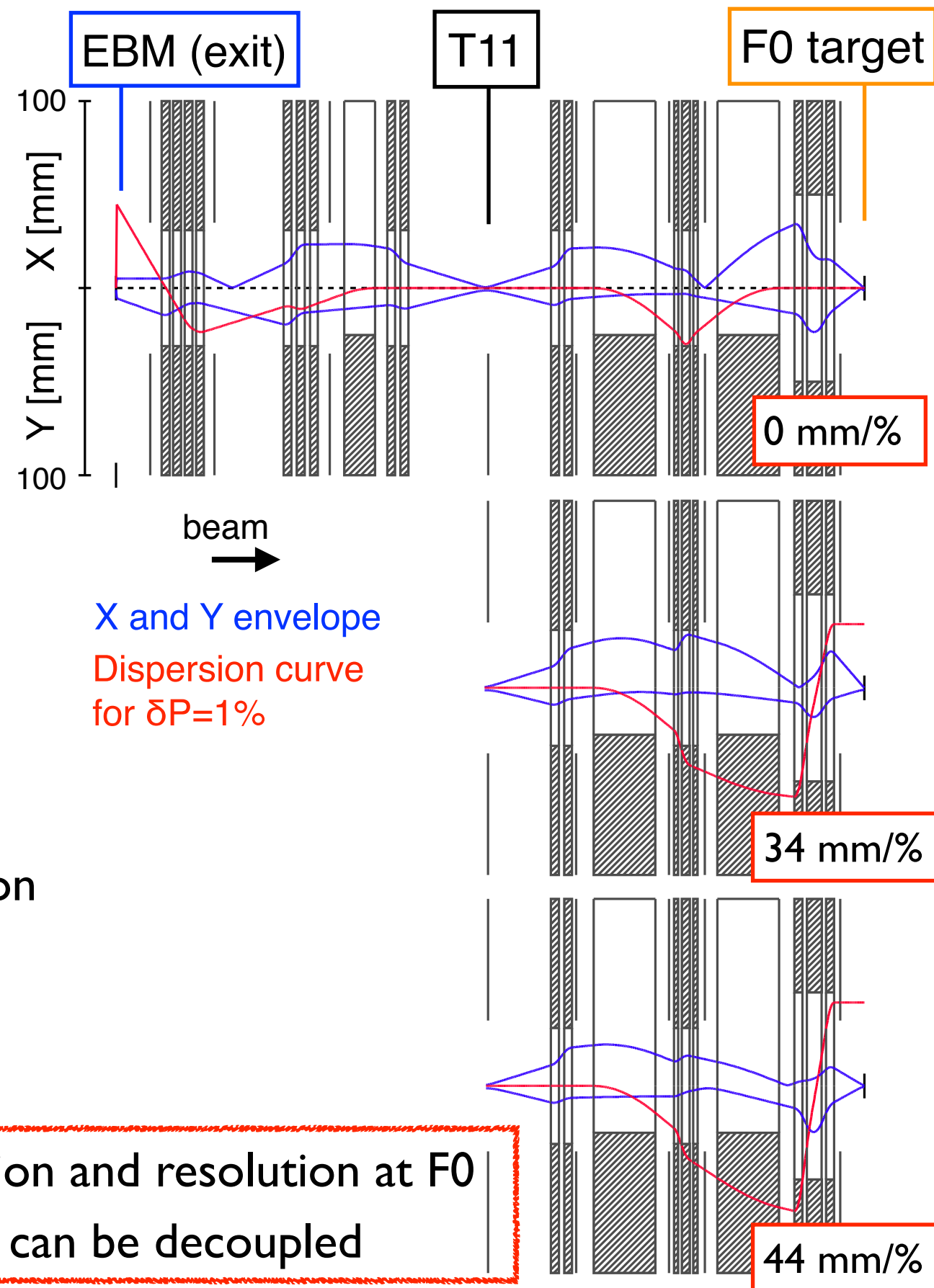
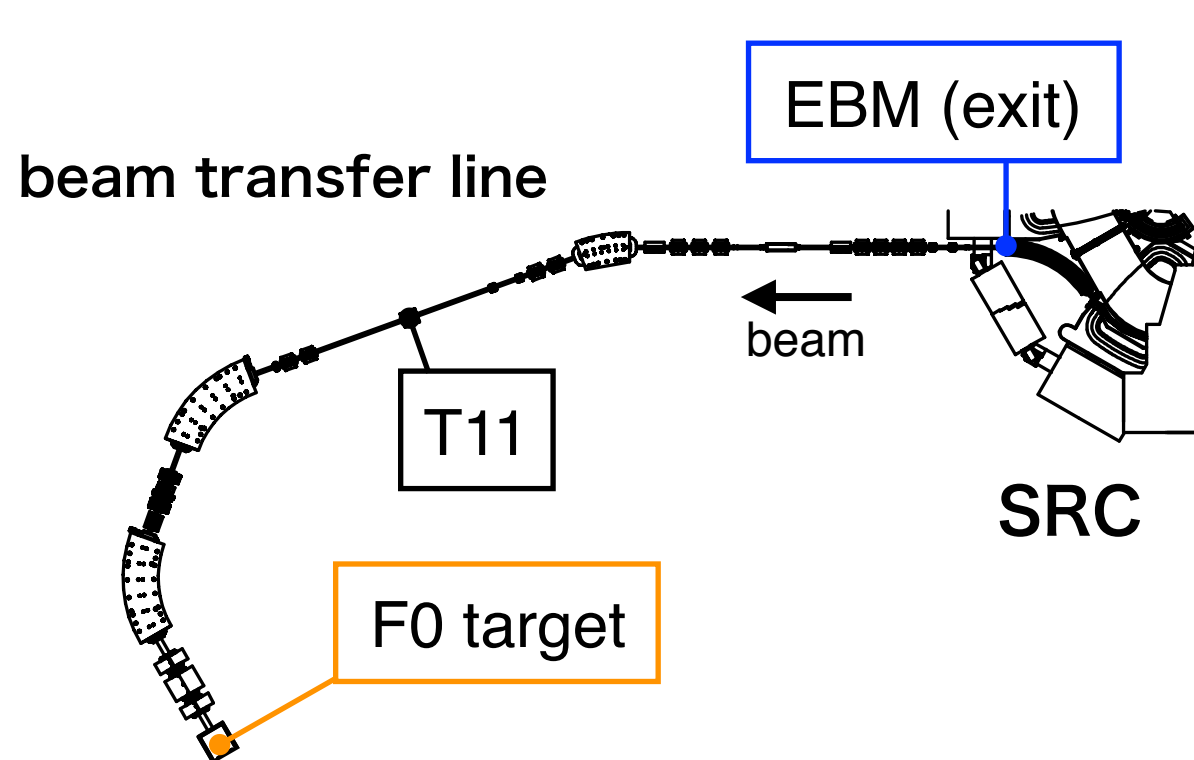
$(X|\delta)$  at F0 target  $\sim 28$  mm/% (deduced)  
44 mm/% (for matching)

→ Dispersion matching partially achieved in the first experiments

Estimation of dispersion from accelerator seems to have uncertainties



# Redesign ion optics of beam transfer line



- ◇ aim at T11 achromatic focus / waist
- ◇ use EBM (exit) - T11 section to compensate uncertainty from SRC beam phase space
- ◇ T11 - F0 section to produce desired dispersion
  - \*  $(X|\delta) = 0$  (for tuning)
  - \*  $(X|\delta) = 34 \text{ mm}/\%$  (for  $C=1.00$ , DGTGR)
  - \*  $(X|\delta) = 44 \text{ mm}/\%$  (for  $C=1.31$ ,  $\pi$ -atom)

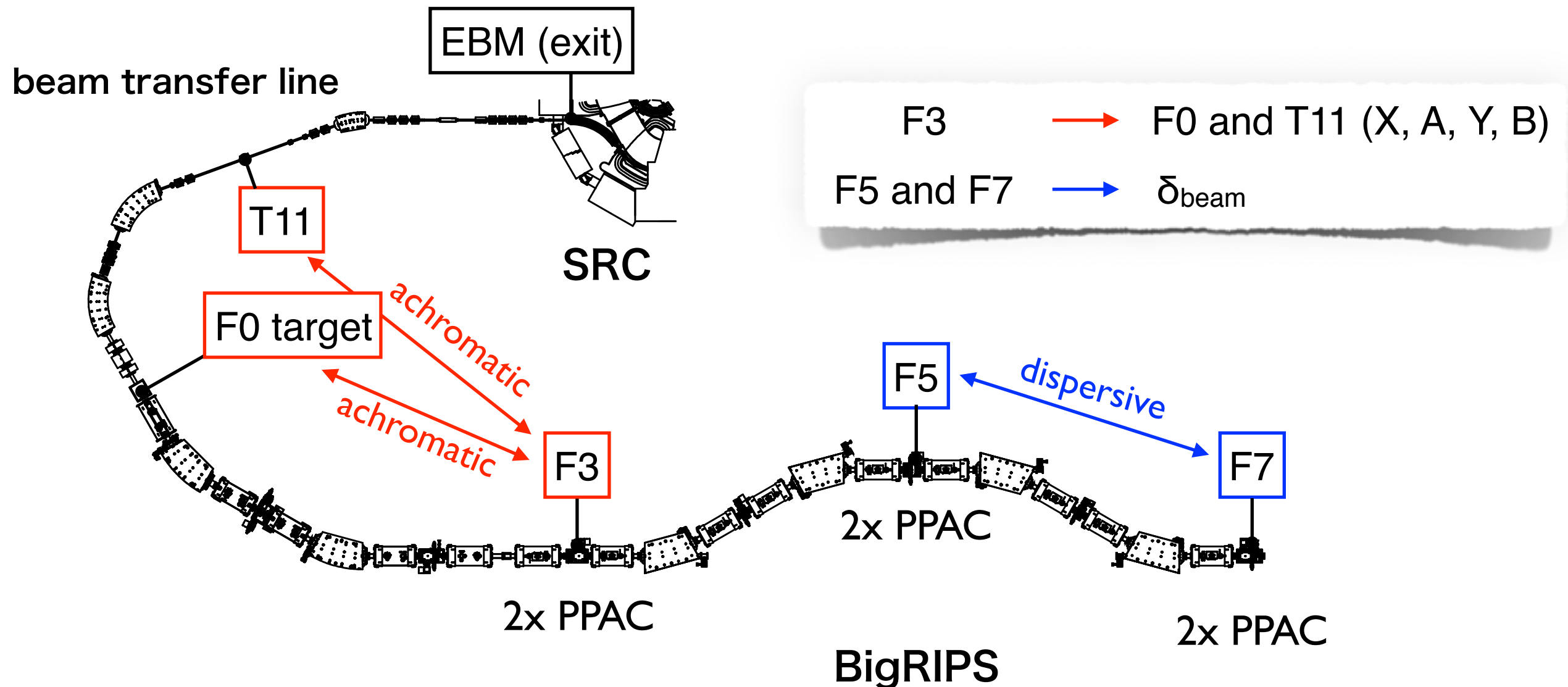


- ◇ Straightforward adjustment of dispersion and resolution at F0
- ◇ Dispersion tuning and (X & Y) tuning can be decoupled

# Next approach : Trace-back method

## Measurement-based approach

- ◇ Measurement and tuning of beam at upstream beam transfer line are needed
- ◇ Use data of downstream focal planes to deduce F0 and T11 phase space



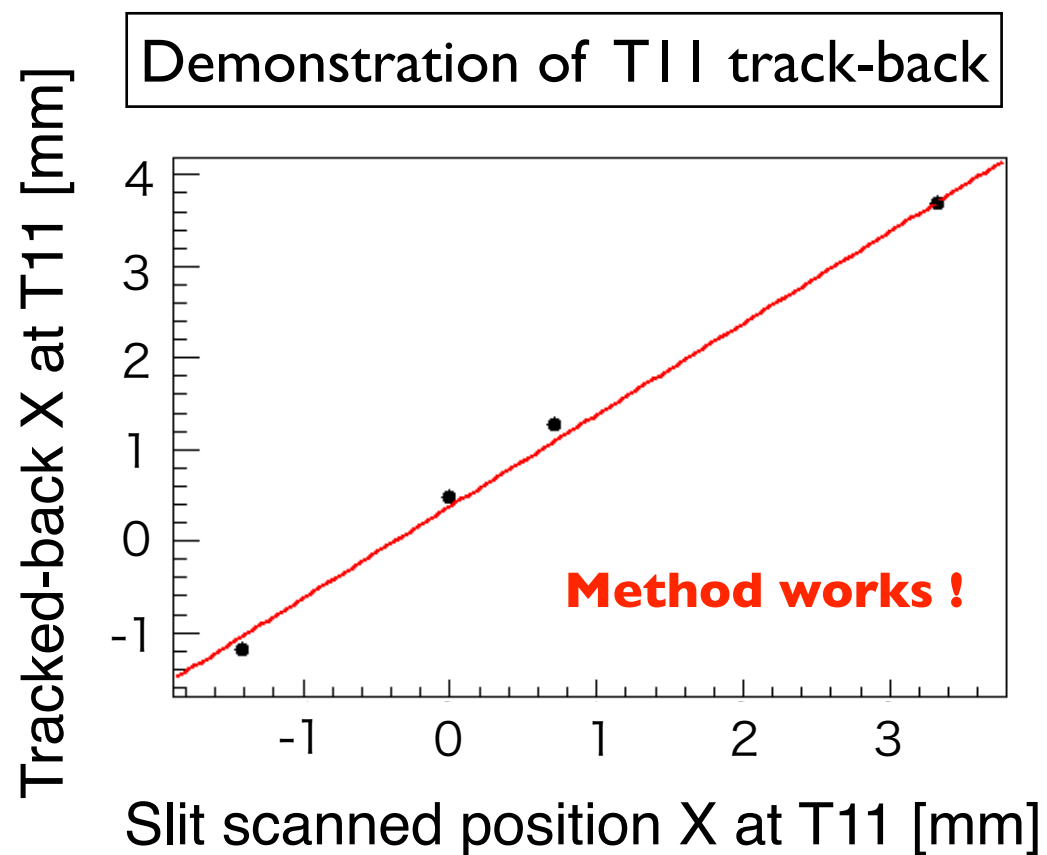
# Test of trace-back method with $^{18}\text{O}$ beam in 2018

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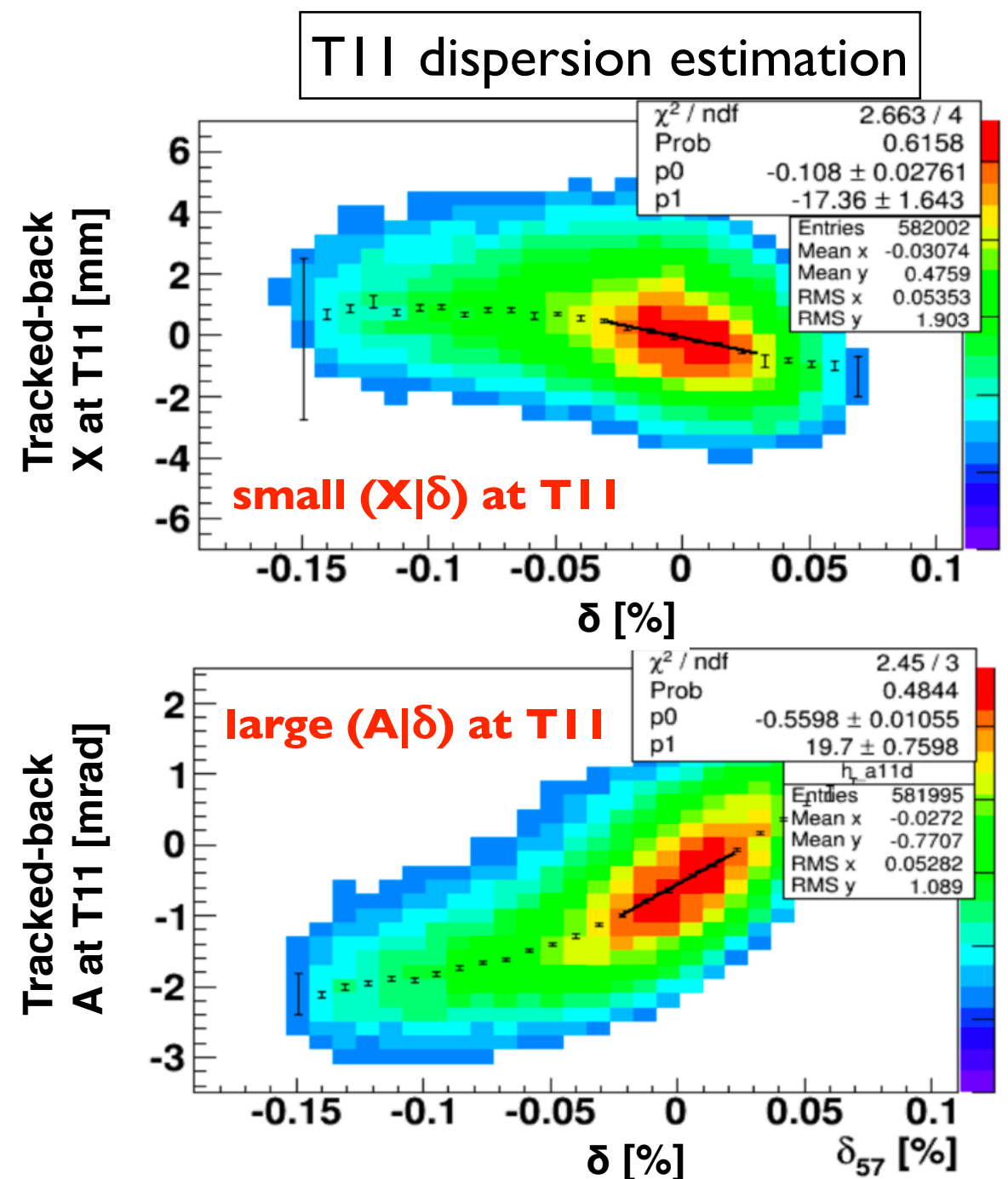
- ◇ BigRIPS optics tuning and matrix measurements
- ◇ T11-F0 achromatic optics tuning and matrix measurements
- ◇ T11-trace-back method to deduce primary beam phase space at T11

# Test of trace-back method with $^{18}\text{O}$ beam in 2018

- ◇ BigRIPS optics tuning and matrix measurements
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- ◇ T11-trace-back method to deduce primary beam phase space at T11



S. Y. Matsumoto

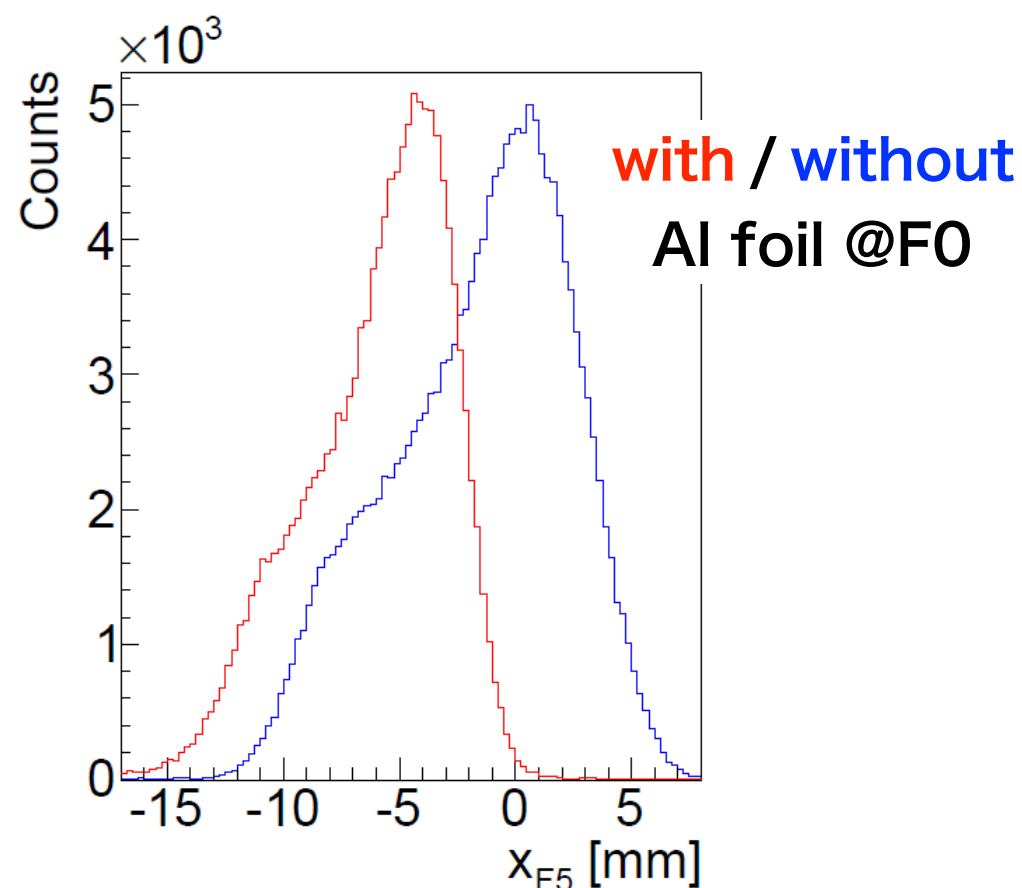


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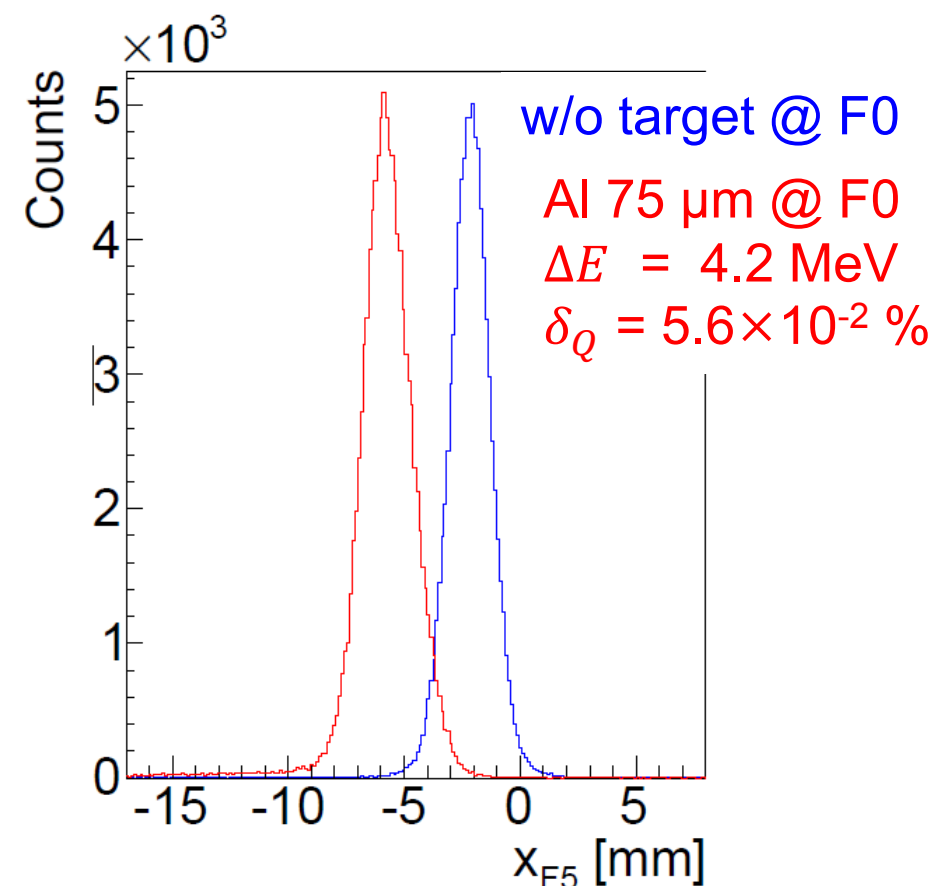
## Demonstration of dispersion matching by $\Delta E$ spectroscopy

- ◇  $\Delta E$  measurement of Al 75  $\mu\text{m}$  at F0 target
- ◇  $C = 1.00 \rightarrow (X|\delta)_{\text{SRC-F0}} = 34 \text{ mm}/\%$  is required

Without dispersion matching  
 $(X|\delta)_{\text{SRC-F0}} = 0$



With dispersion matching  
 $(X|\delta)_{\text{SRC-F0}} \sim 34 \text{ mm}/\%$

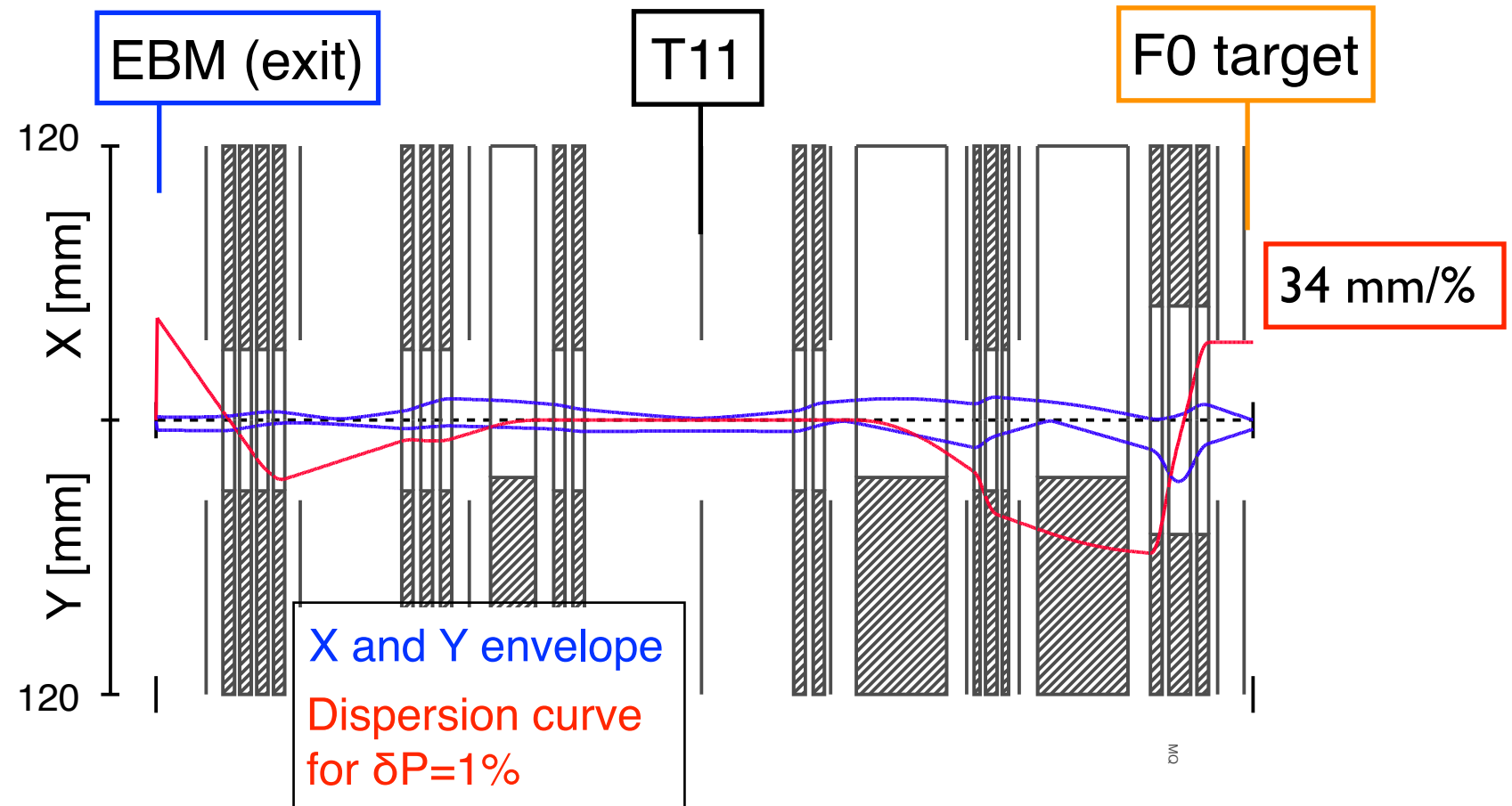
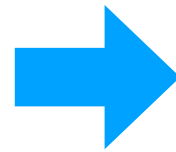




# DGTGR and $\pi$ -atom experiments in 2021

$^{12}\text{C}$  beam @ 250MeV/u  
(DGTGR, 2021 May)

Trace-back +  
T11  $\rightarrow$  EBM matrix

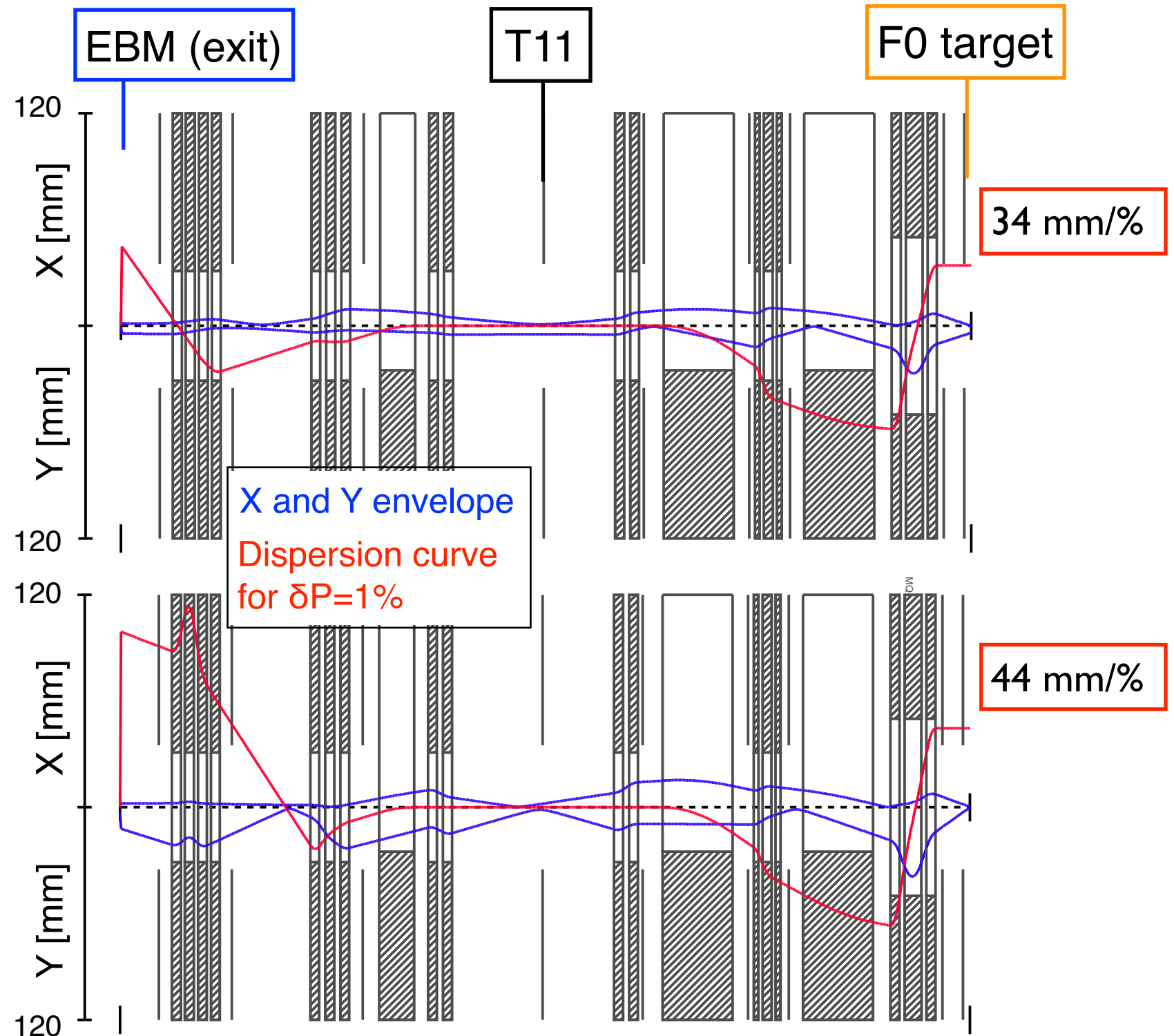


# DGTGR and $\pi$ -atom experiments in 2021

$^{12}\text{C}$  beam @ 250MeV/u  
(DGTGR, 2021 May)

Trace-back +  
TII  $\rightarrow$  EBM matrix

$d$  beam @ 250MeV/u  
( $\pi$ -atom, 2021 June)

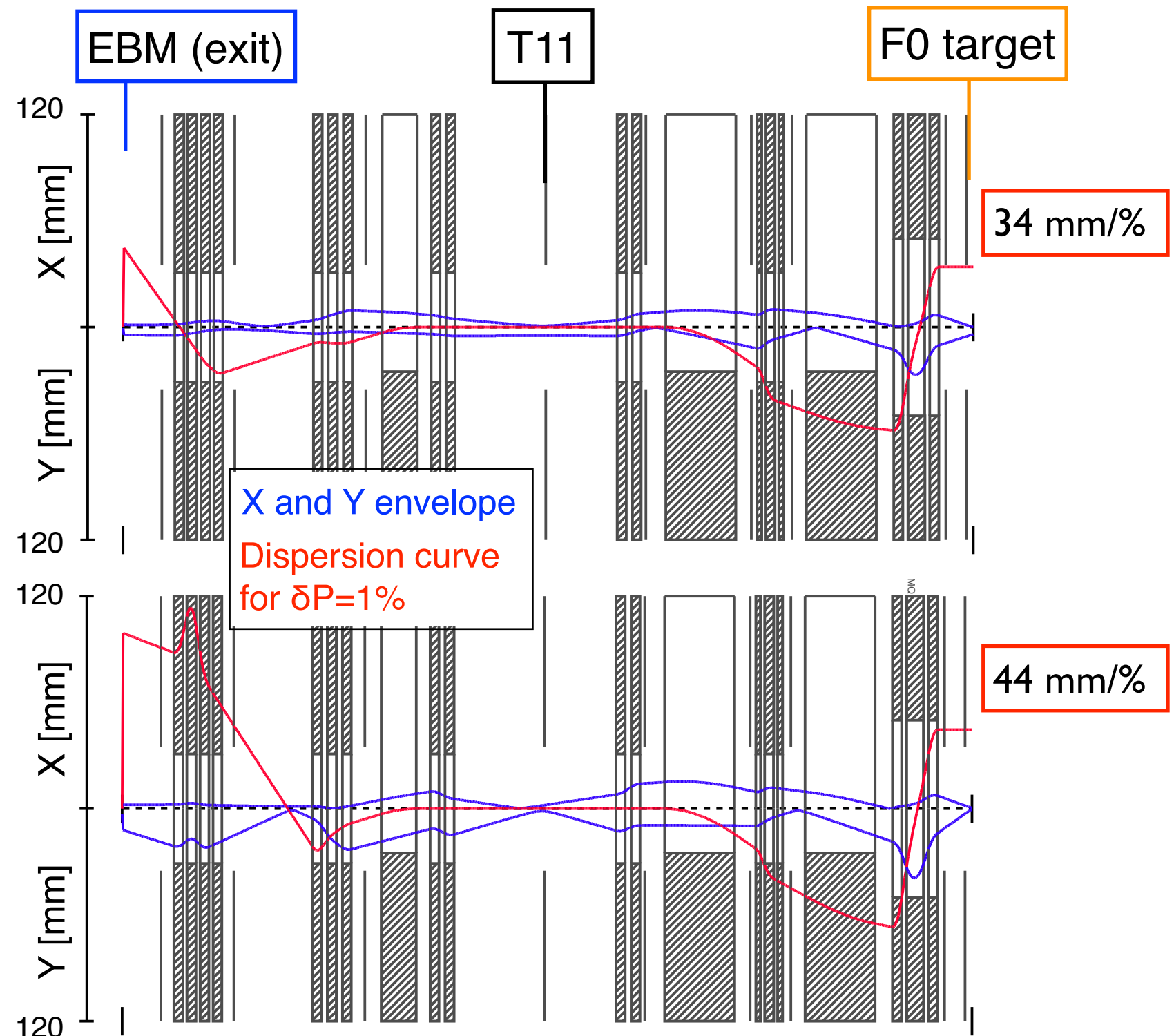


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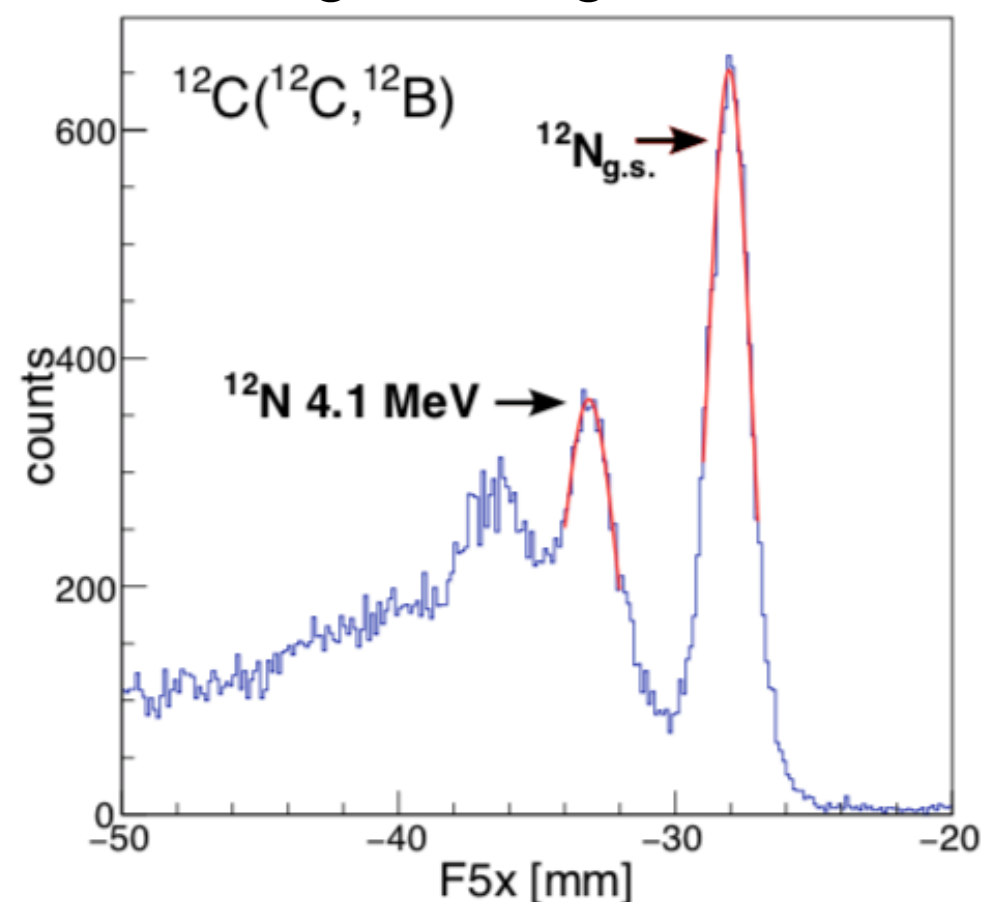


- ◇ Different dispersion curves at SRC exit were observed for different beams !
- ◇ For each experiment, TII was tuned to be achromatic, and F0 with desired dispersion

# DGTGR and $\pi$ -atom experiments in 2021

$^{12}\text{C}$  beam @ 250 MeV/u  
(DGTGR, 2021 May)

Calibration with single-charge exchange reaction



A. Sakaue, PhD thesis,  
Kyoto Univ.(2025)

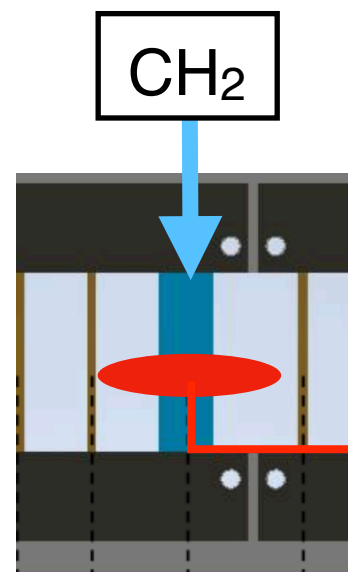
- ◇ Excitation energy resolution (FWHM)  $\sim 1.5$  MeV
- ◇ Corresponding resolving power  $P/\Delta P_{\text{FWHM}} \sim 3600$

# DGTGR and $\pi$ -atom experiments in 2021

$d$  beam @ 250MeV/u  
( $\pi$ -atom, 2021 June)

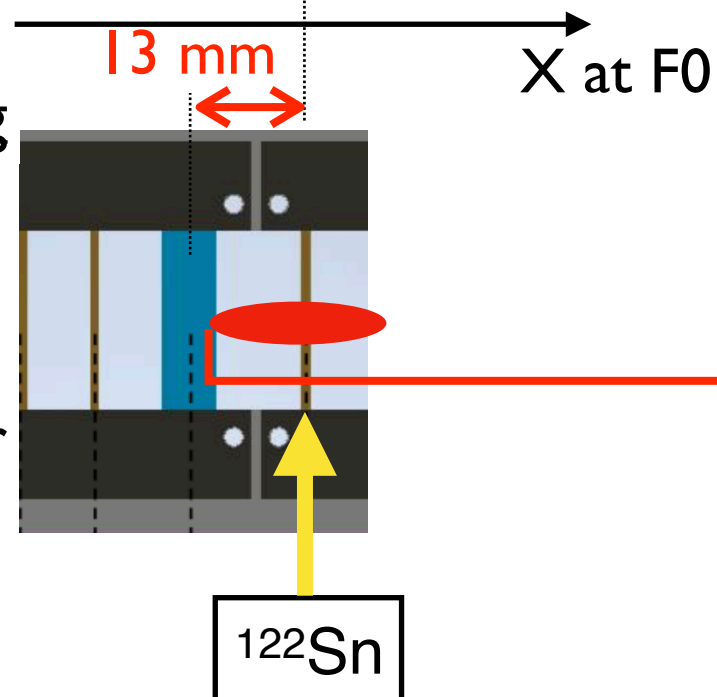
$H(d,^3\text{He})\pi^0$  setting

Target ladder  
 $\text{CH}_2$  at center

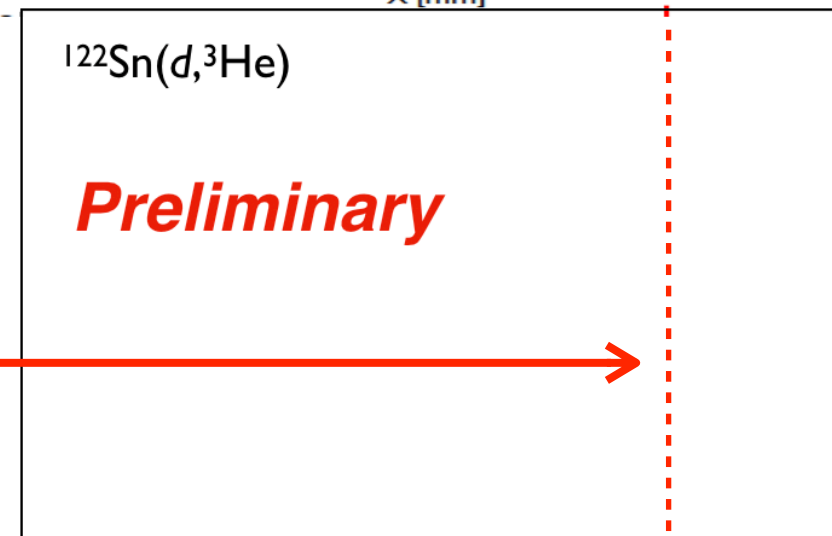
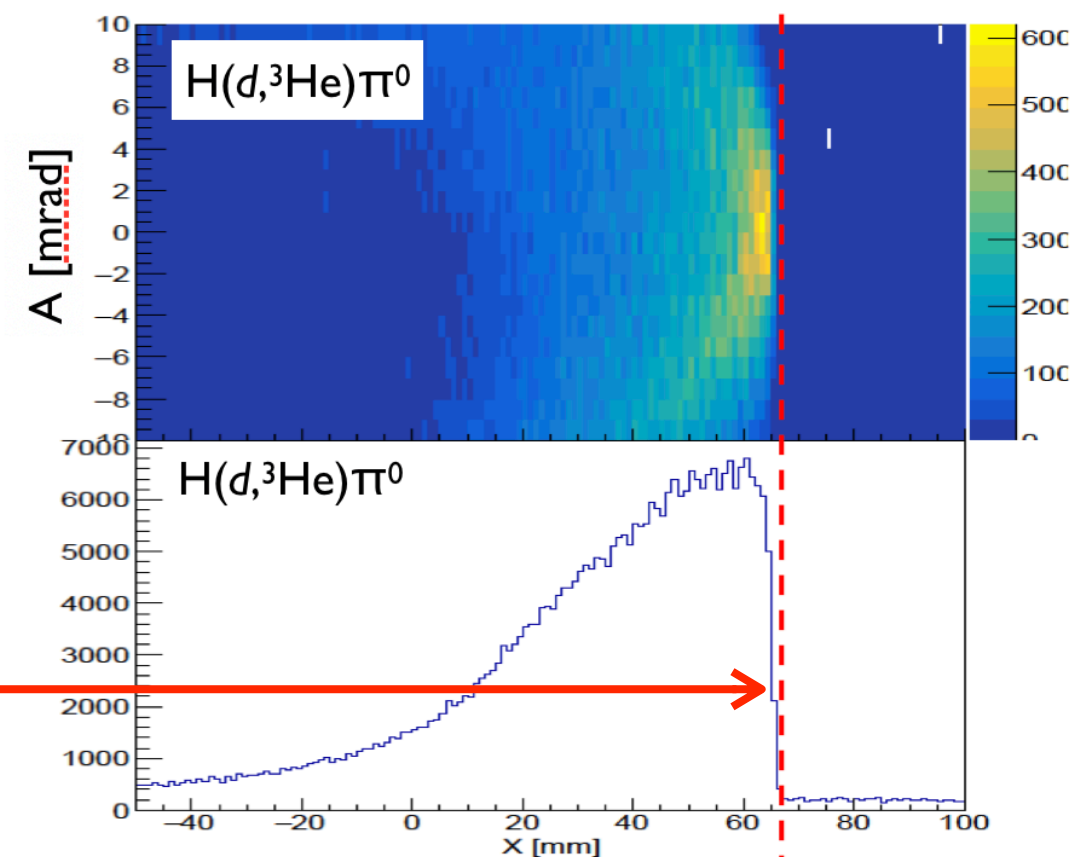


$^{122}\text{Sn}(d,^3\text{He})$  setting

Target ladder  
 $^{122}\text{Sn}$  at center



Evidence of dispersion matching



X at F5 [mm]

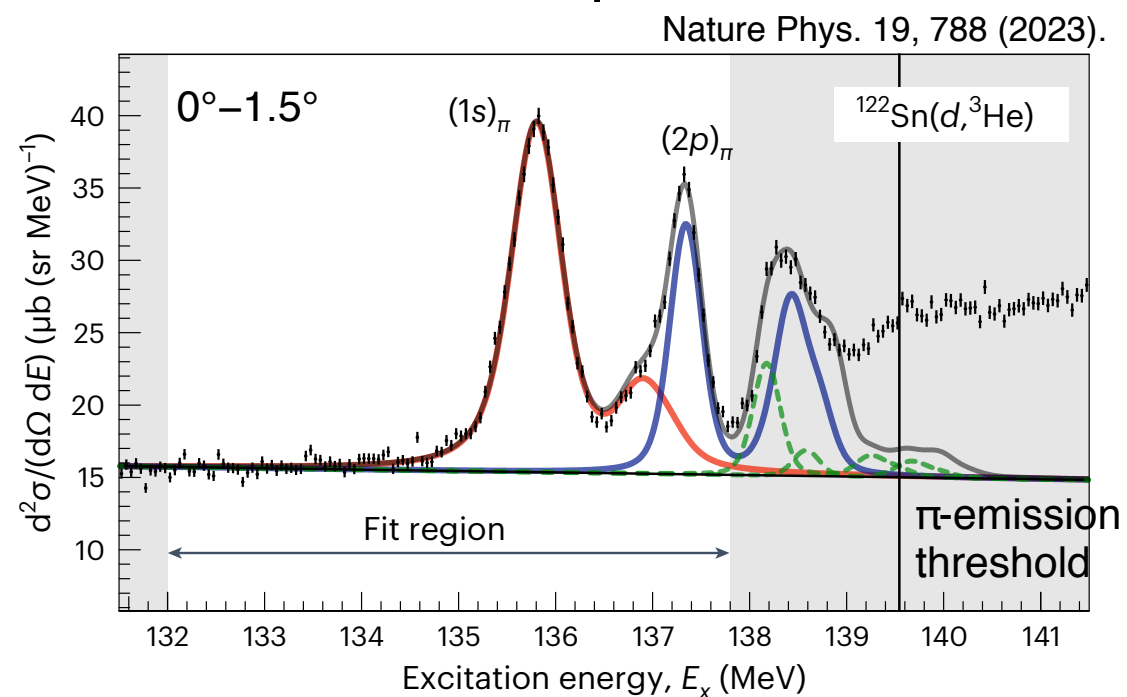
S. Y. Matsumoto  
HIN2025

Effects of shifted X and  $\delta$  of the beam at F0 compensate !

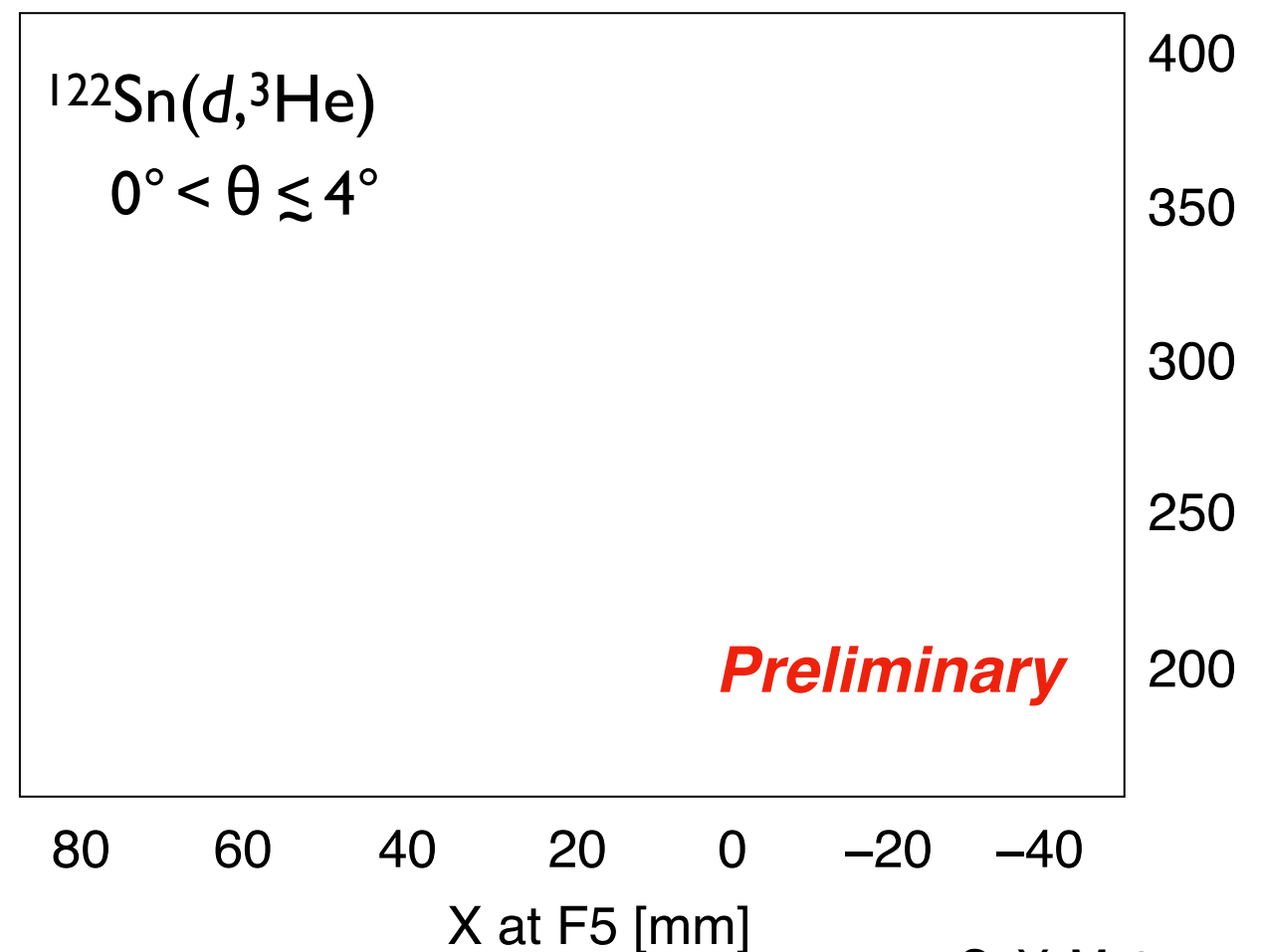
# DGTGR and $\pi$ -atom experiments in 2021

$d$  beam @ 250MeV/u  
( $\pi$ -atom, 2021 June)

2014 experiment



2021 experiment



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- ◇ Narrower peaks and more sub-components are observed !
- ◇ Detailed analysis is in progress

# Summary and future prospects

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- We have developed dispersion-matched SRC + BigRIPS ion optics for precision missing-mass spectroscopy with reactions using primary beams. We established its tuning procedure with a trace-back method.
- Two experiments have been successfully performed in 2021 :
  - Spectroscopy of deeply-bound pionic atoms with  $^A\text{Sn}(d, ^3\text{He})$  reaction
  - Study of double Gamow-Teller giant resonances with  $^{48}\text{Ca}(^{12}\text{C}, ^{12}\text{Be}(0^+_2))$  reaction
- For the future, we will continue application of the dispersion-matching method to further studies of  $\pi$ -atom and DGTGR.
  - e.g., DGTGR with  $^{136}\text{Xe}$  target,
  - $\pi$ -atom with  $Z=50, 54$  isotope,  $N=82$  isotone
- We are also developing  $\pi$ -atom spectroscopy in inverse kinematics
  - $\partial E_{\text{ex}}/\partial P_{\text{beam}} \sim 0$  due to kinematics
  - Explore possibilities of producing variety of pionic atoms