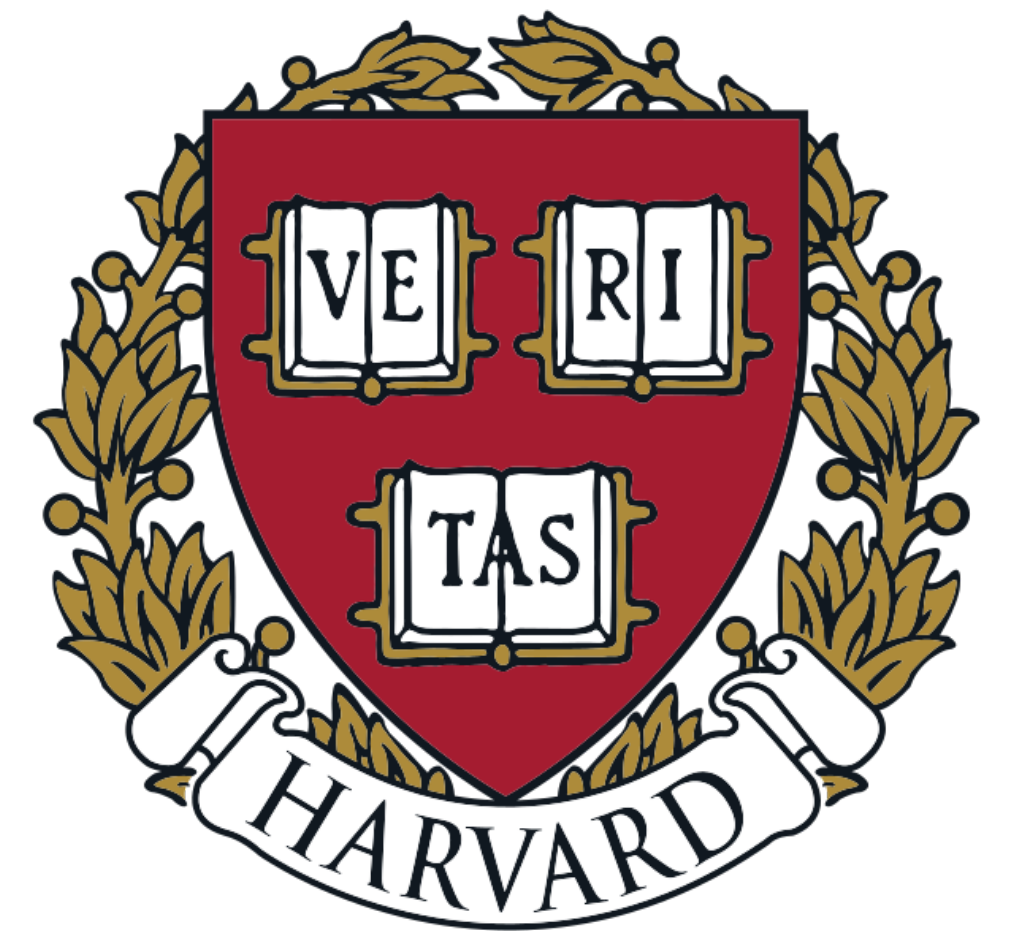


Ultralight Scalars and Vectors

Dark Interactions 2024, Vancouver

Akshay Ghalsasi

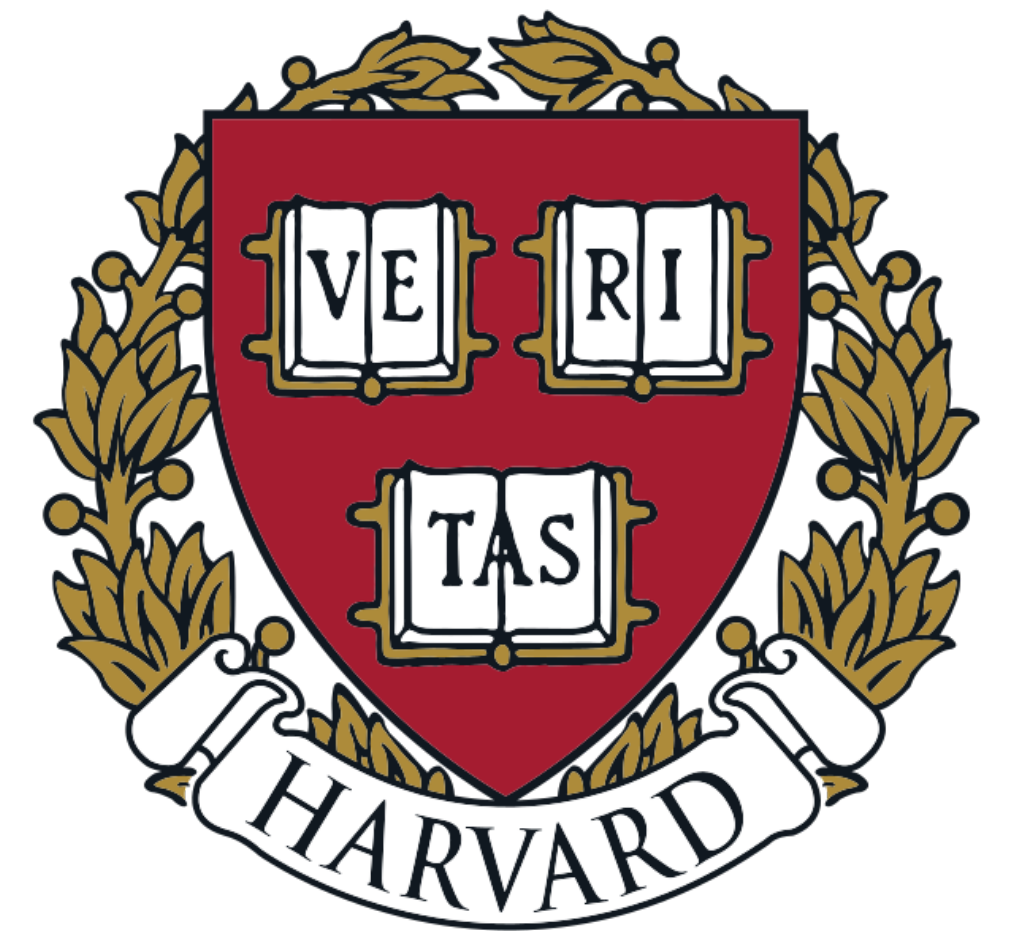


Ultralight Scalars and Vectors

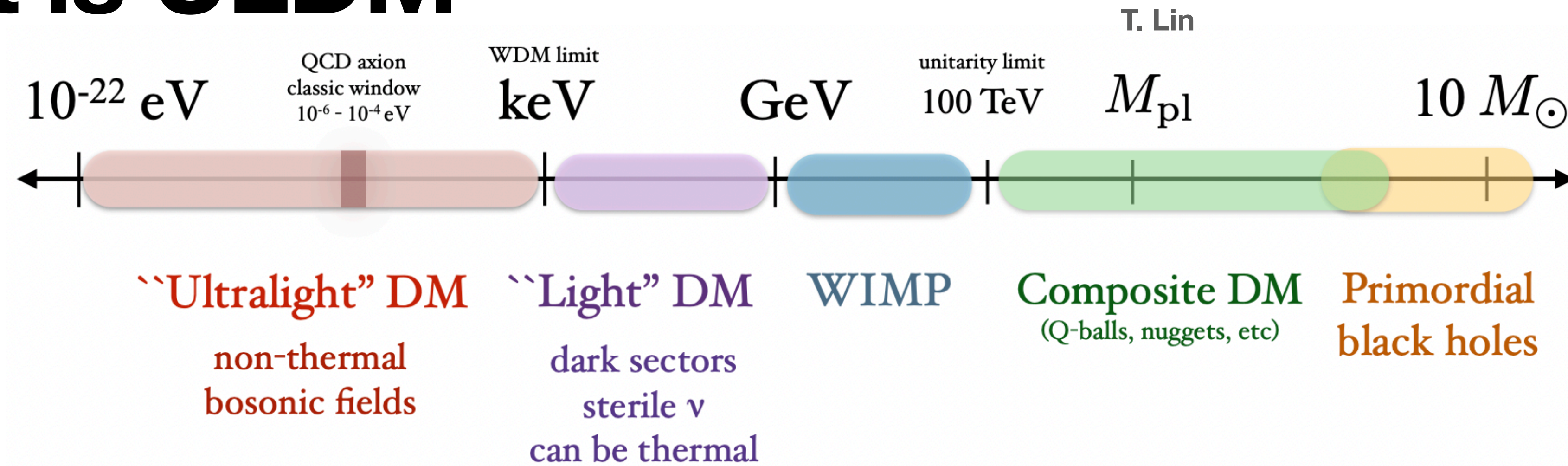
Dark Interactions 2024, Vancouver

The B Team

Akshay Ghalsasi



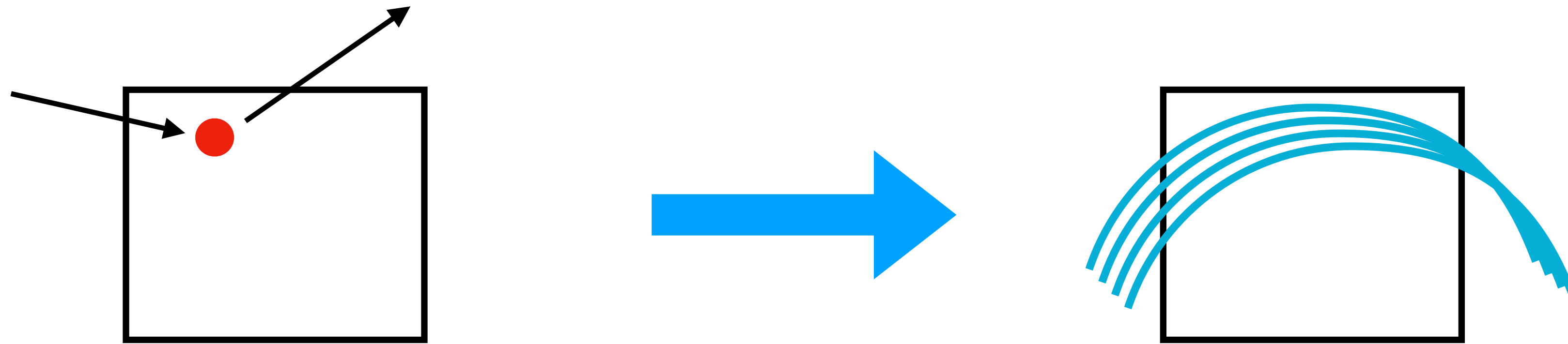
What is ULDM



- Local DM density is known $\sim 0.4 \text{ GeV cm}^{-3}$
- The de Broglie wavelength of a particle is given by $\lambda_{db} = \frac{2\pi}{mv}$
- For local DM density we get $N \simeq \left(\frac{30\text{eV}}{m} \right)^3$ within one dB wavelength

What is ULDM

- In this limit we can approximate DM as classical wave
- Presence of ULDM can be modeled by solving the classical EOM



- Production of boson DM can typically be modeled by classical EOM for $m \gg 30\text{eV}$

ULDM Snowmass Whitepaper

Submitted to the Proceedings of the US Community Study
on the Future of Particle Physics (Snowmass 2021)

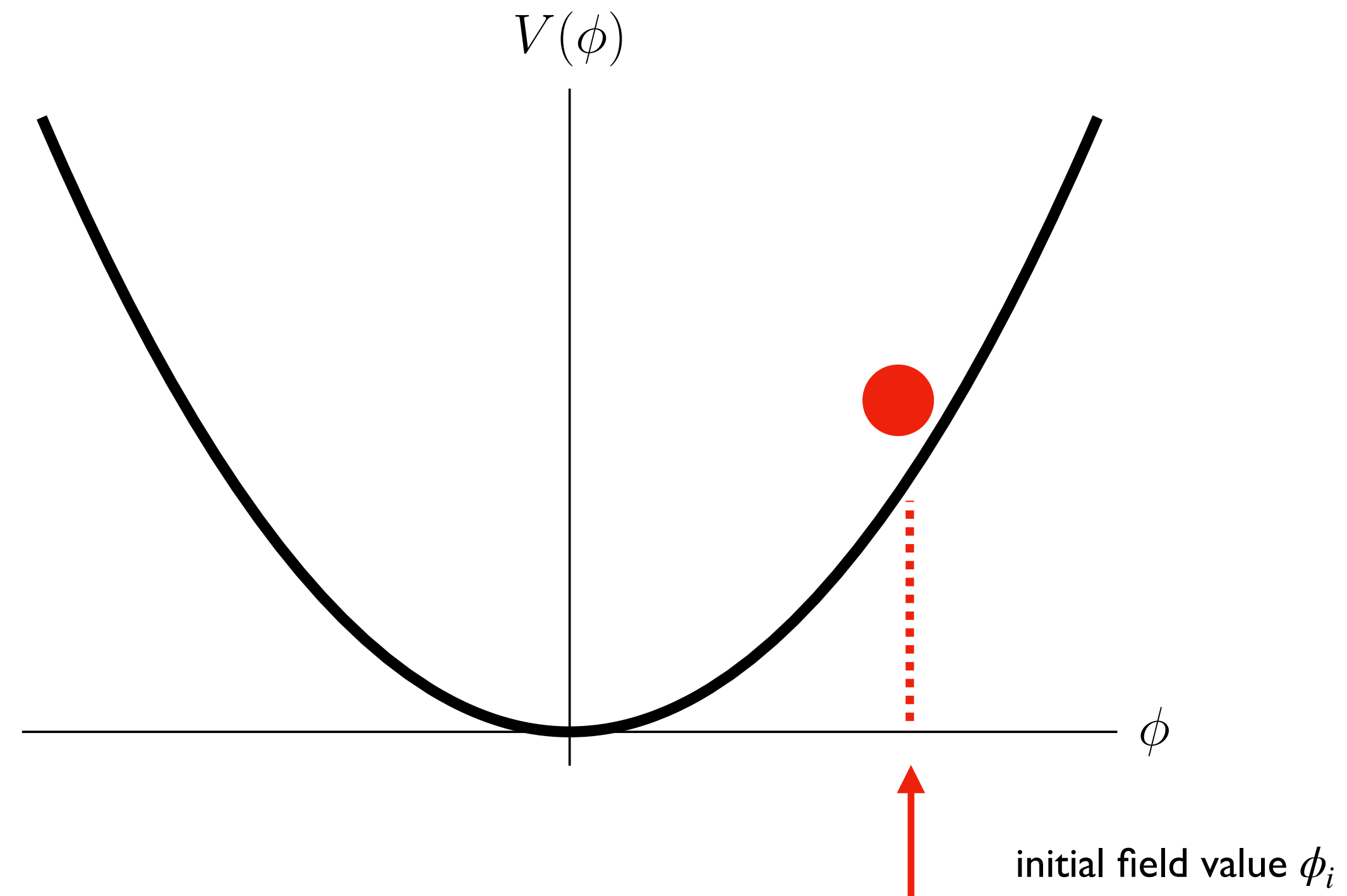
Snowmass 2021 White Paper New Horizons: Scalar and Vector Ultralight Dark Matter

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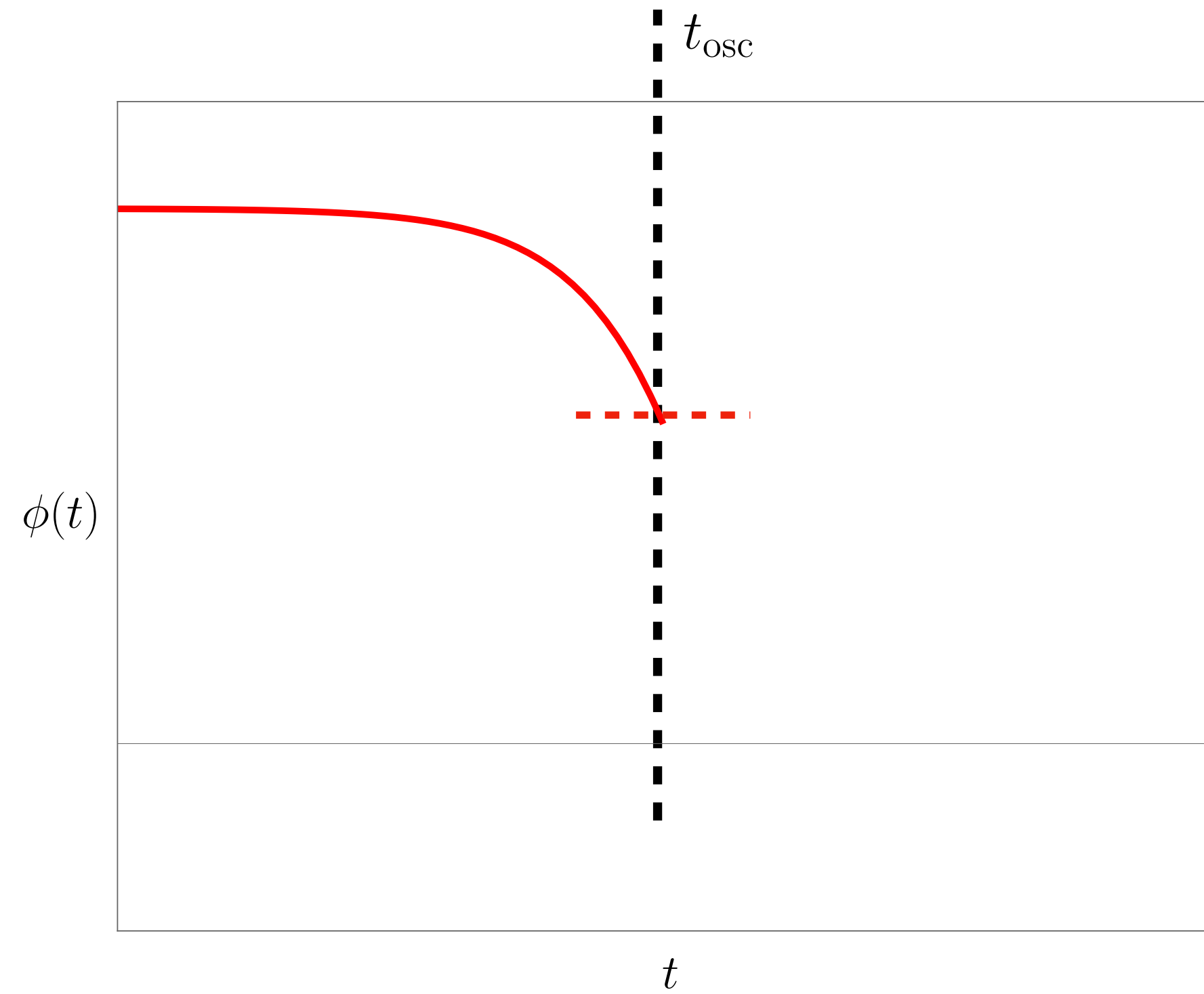
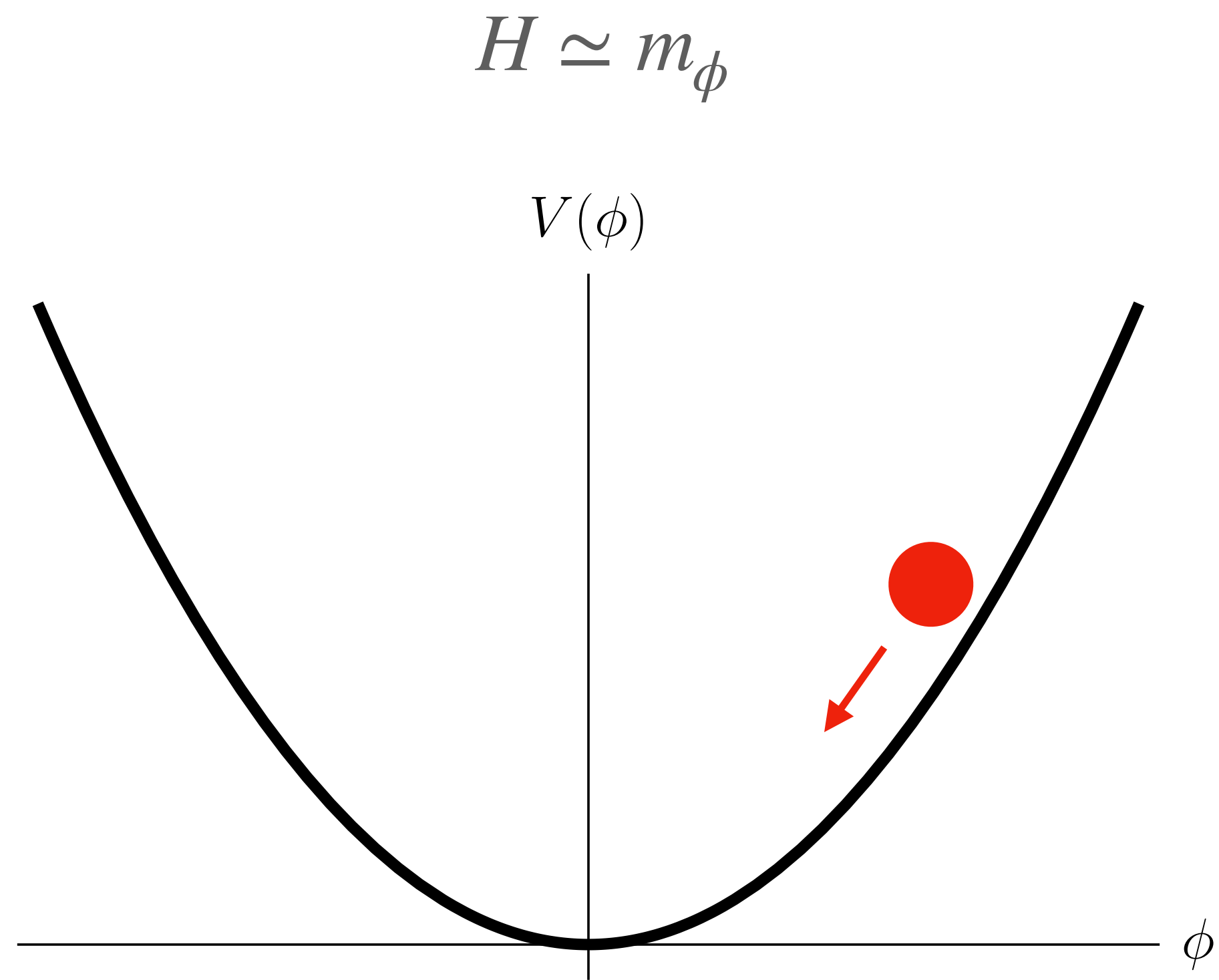
Standard Misalignment

$$\ddot{\phi} + 3H\dot{\phi} + m_\phi^2\phi = 0$$

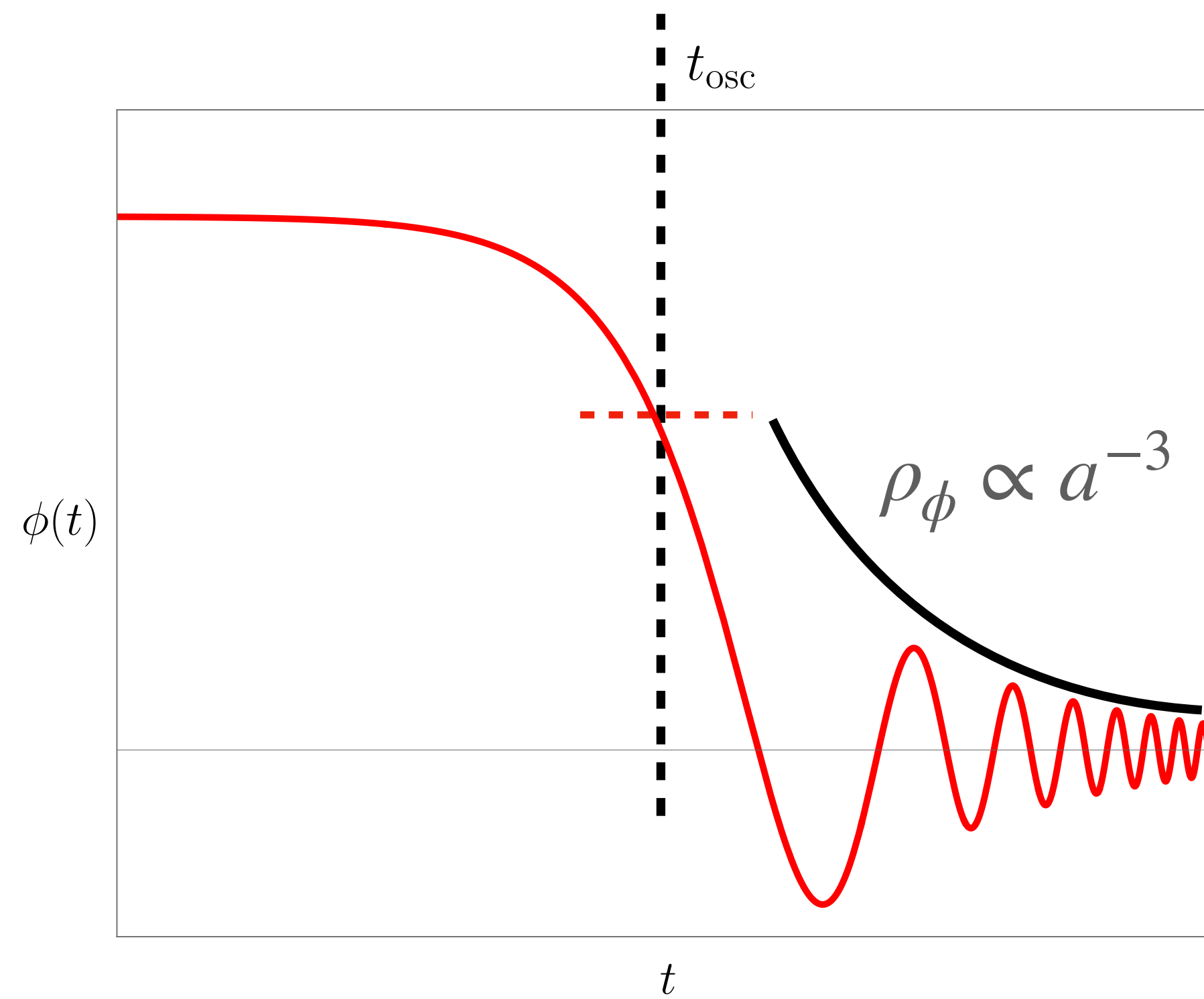
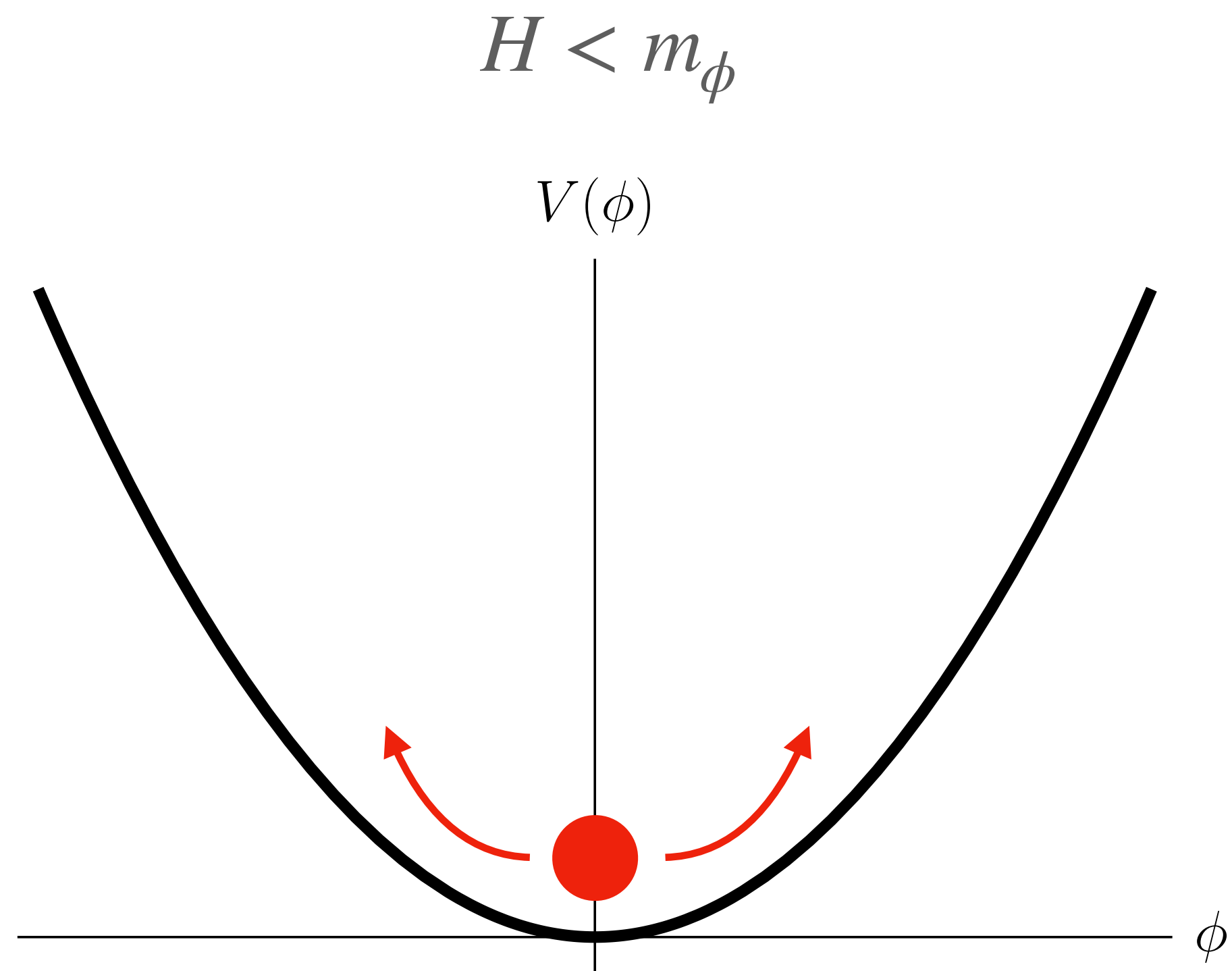
$$H \gg m_\phi$$



Standard Misalignment



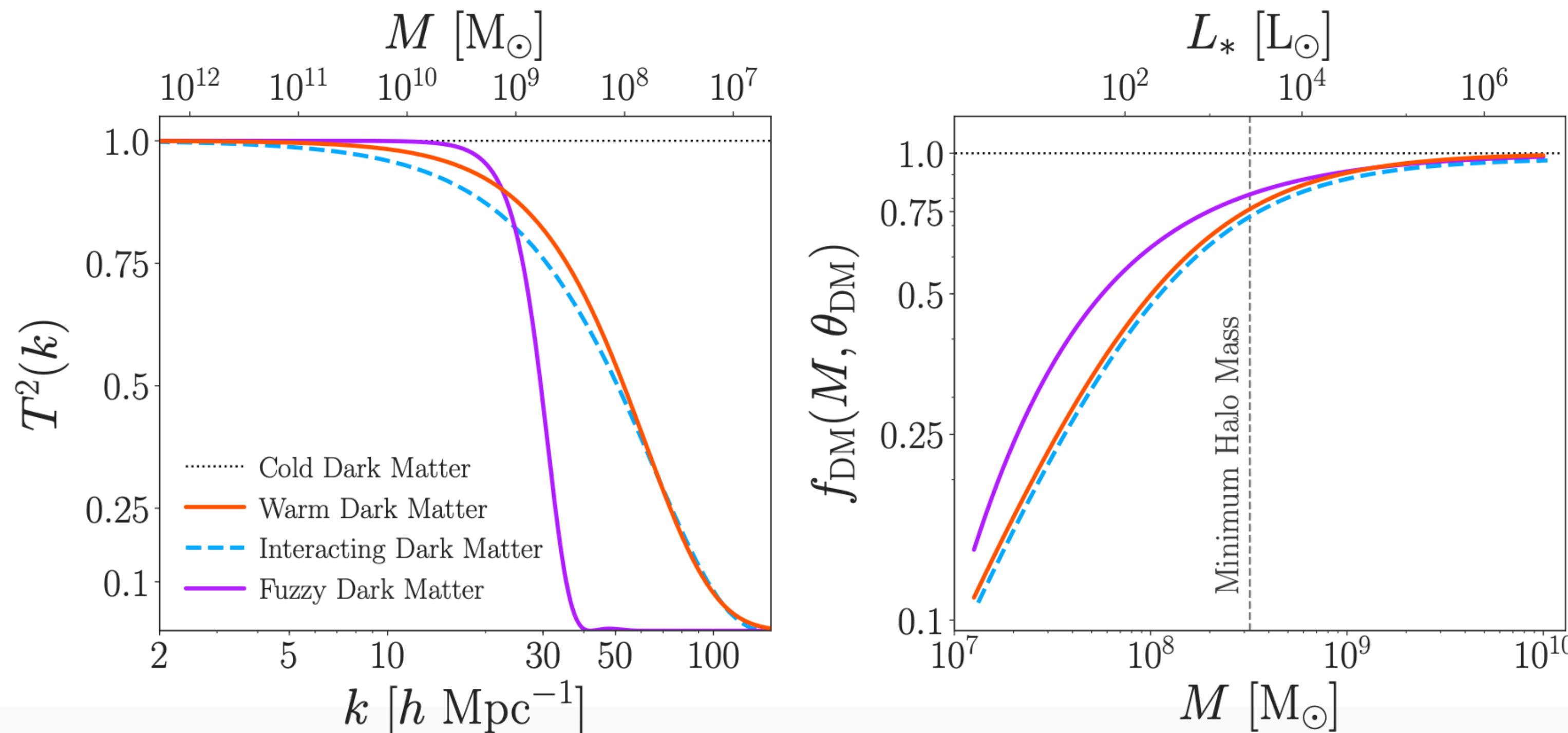
Standard Misalignment



ULDM “Nightmare Scenario”

What if ULDM interacts only gravitationally?

- Lyman α constraints the matter power spectrum $k \simeq 1 - 10 \text{ Mpc}^{-1}$
- MW Satellite counts also constraint the linear matter power spectrum



Nadler et. al.

See talk by Vera, Renee

MW Galaxy count

Ly α

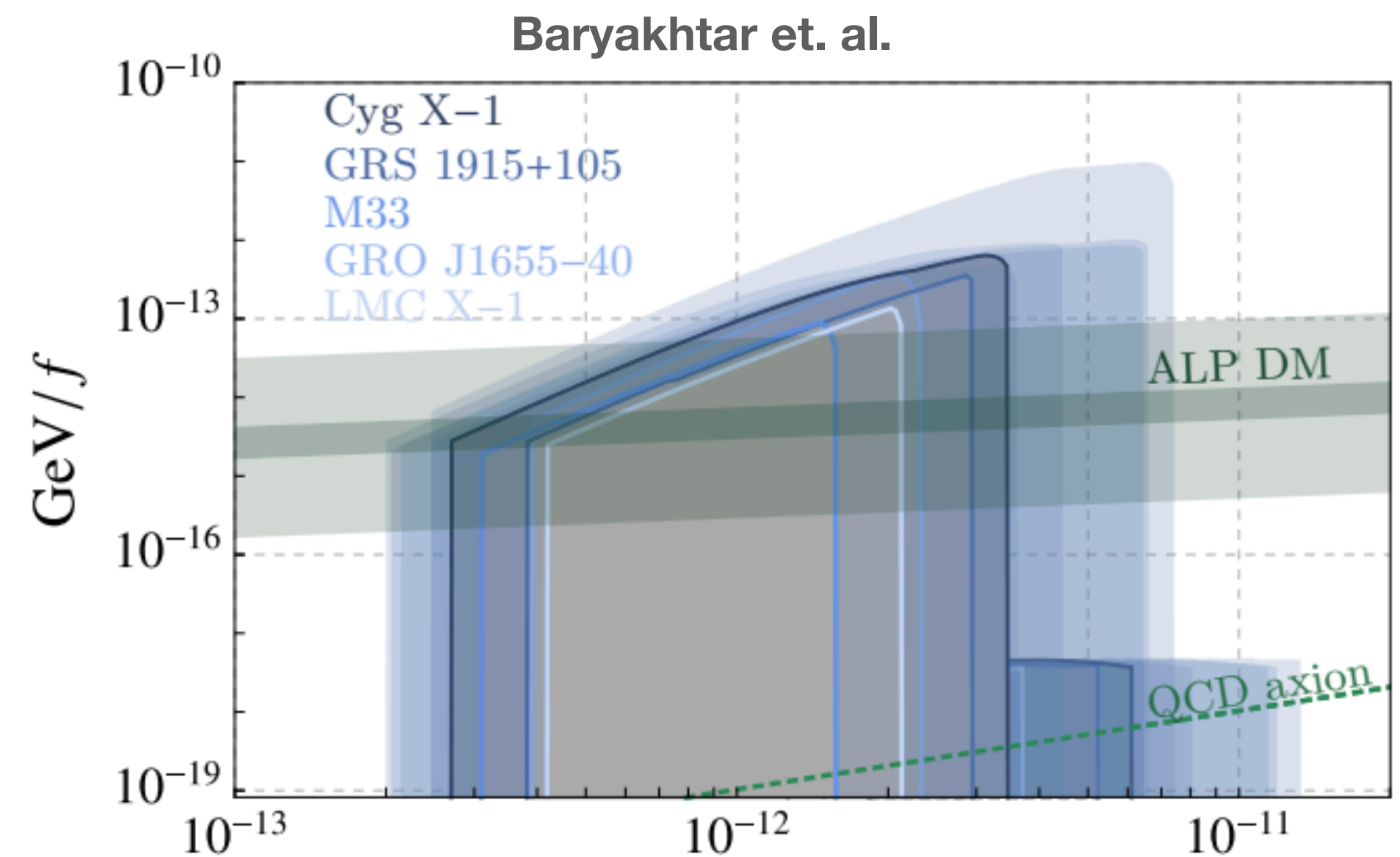
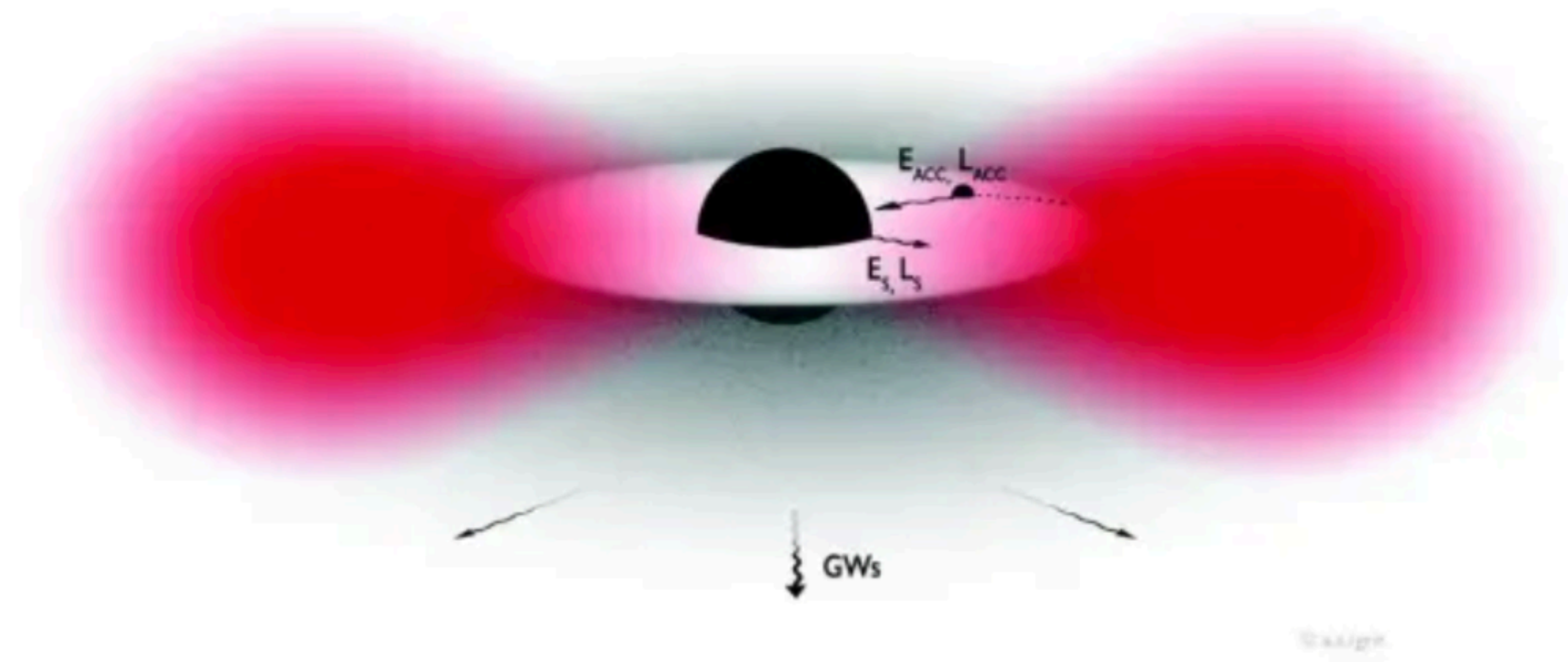


ULDM “Nightmare Scenario”

What if ULDM interacts only gravitationally?

Arvanitaki et. al.

- A massive boson $m_\phi^{-1} \simeq R_{\text{sch}}$ can extract angular momentum from BH

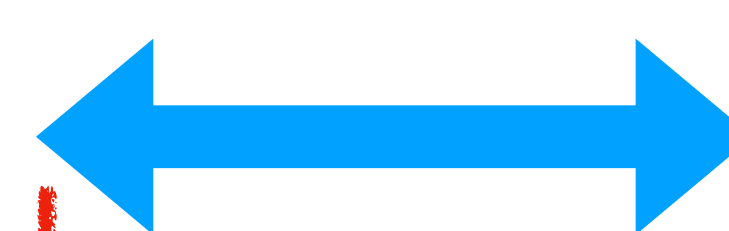


MW Galaxy count

Superradiance

Superradiance

μ/eV



10^{-20} eV

10^{-18} eV

10^{-13} eV

10^{-11} eV

ULDM-SM Interactions

ULDM can interact with standard model particles

- Coupling to photons

$$\frac{1}{4\sqrt{2}} \frac{d_e}{M_{\text{pl}}} \phi F^{\mu\nu} F_{\mu\nu} ; \alpha \rightarrow \alpha \left(1 + \frac{d_e}{\sqrt{2} M_{\text{pl}}} \phi \right)$$

- Coupling to fermions (leptons or quarks)

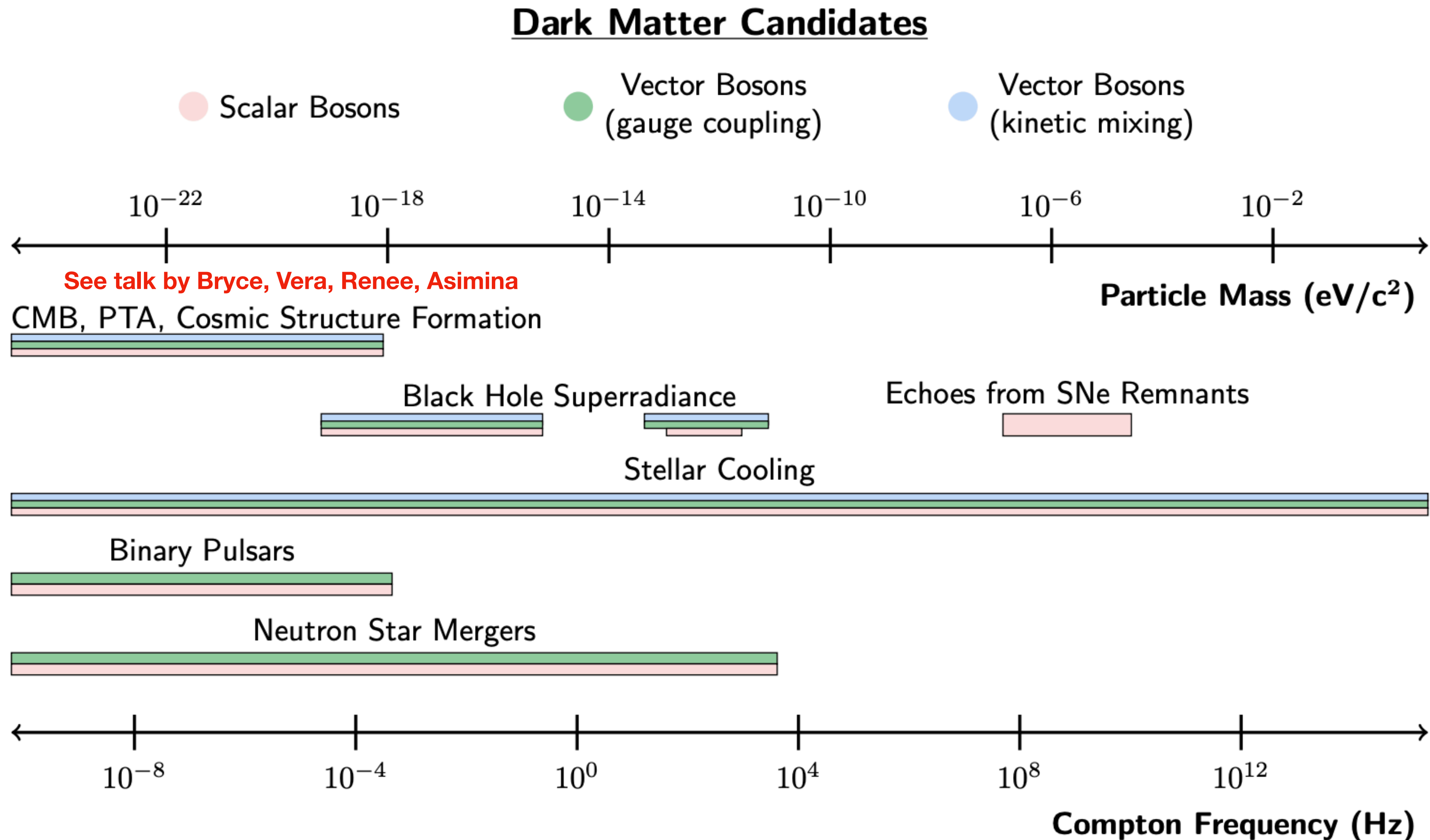
$$\frac{d_{m_f}}{\sqrt{2} M_{\text{pl}}} \phi m_f \bar{f} f ; m_f \rightarrow m_f \left(1 + \frac{d_{m_f} \phi}{\sqrt{2} M_{\text{pl}}} \right)$$

- Coupling to Higgs

$$A\phi H^2 ; v \rightarrow v \left(1 + \frac{A\phi}{m_H^2} \right)$$

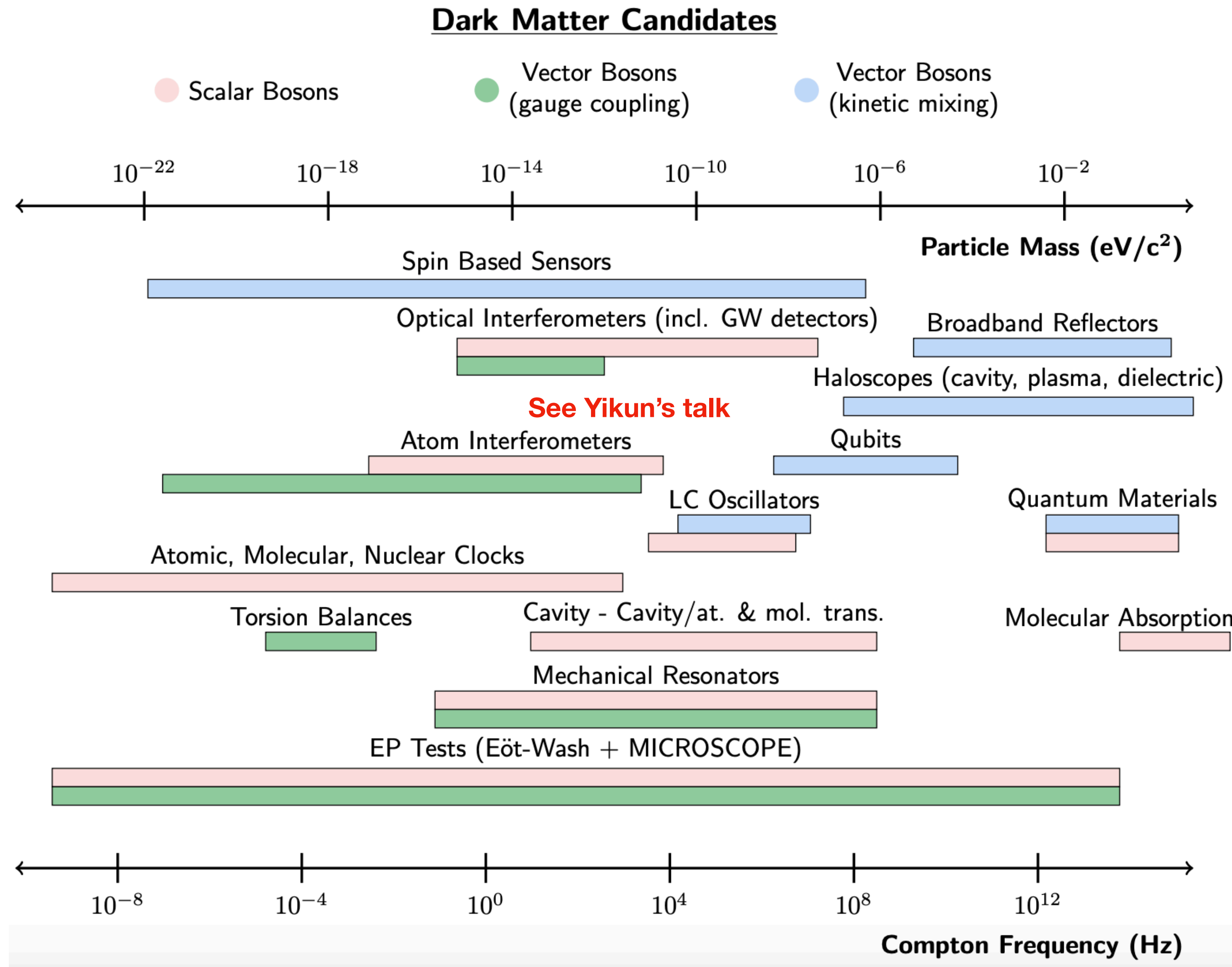
ULDM SM Interactions

Astrophysical Constraints



ULDM SM Interactions

Experimental constraints



Experimental Constraints

Long Range Forces

$$V(r) = -\frac{Gm_A m_B}{r} \left(1 + \alpha_A \alpha_B e^{-m_\phi r} \right) ; \alpha_A \propto \frac{1}{m_A} \frac{\partial m_A}{\partial \phi}$$

- Equivalence principle (acceleration due to gravity is independent of mass)
- EP tests dominate for for $m_\phi \lesssim 10^{-6}$ eV
- For $m_\phi \gtrsim 10^{-6}$ eV Inverse Square Law tests dominate

Experimental Constraints

Atomic/Nuclear Clocks

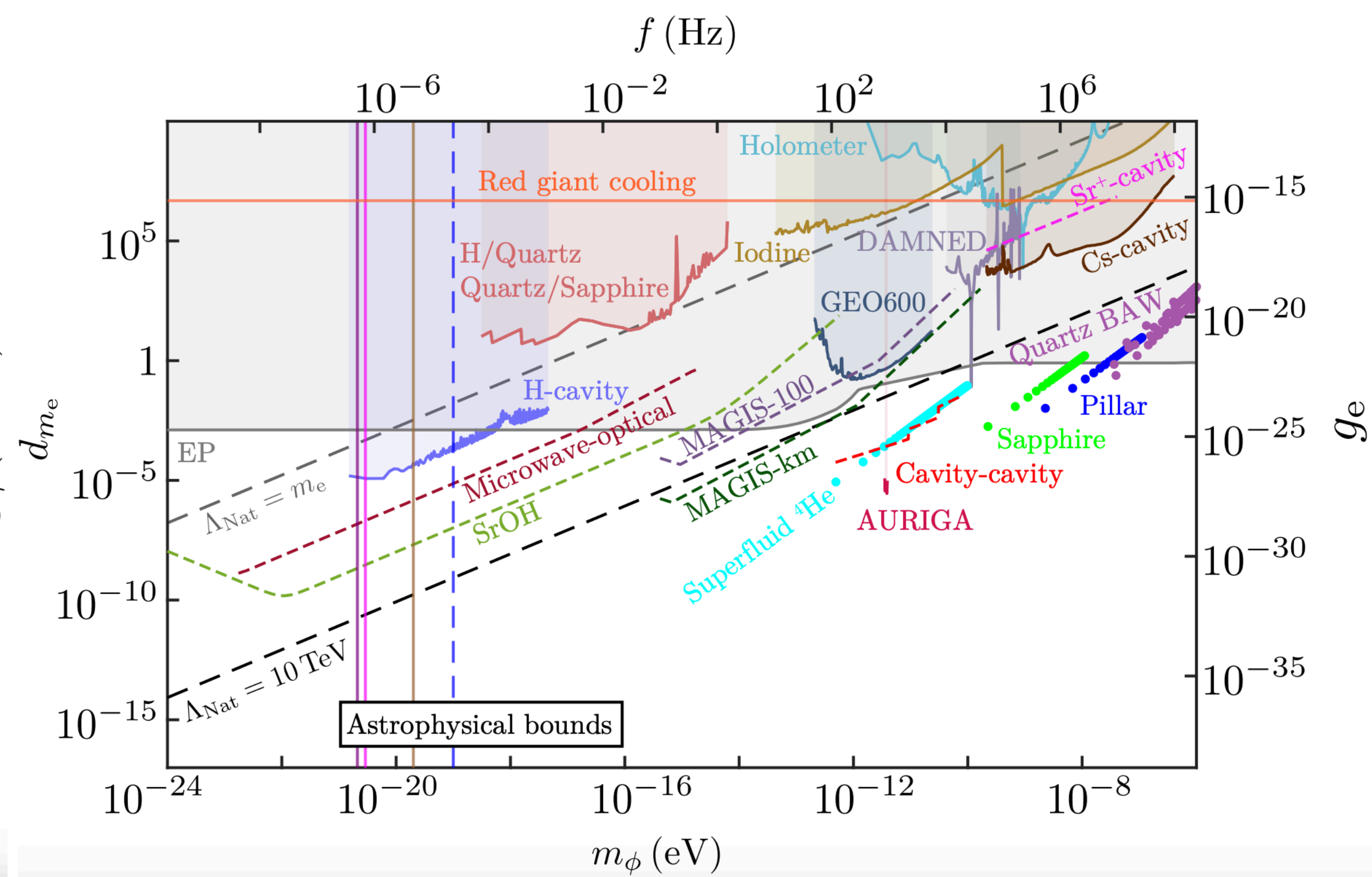
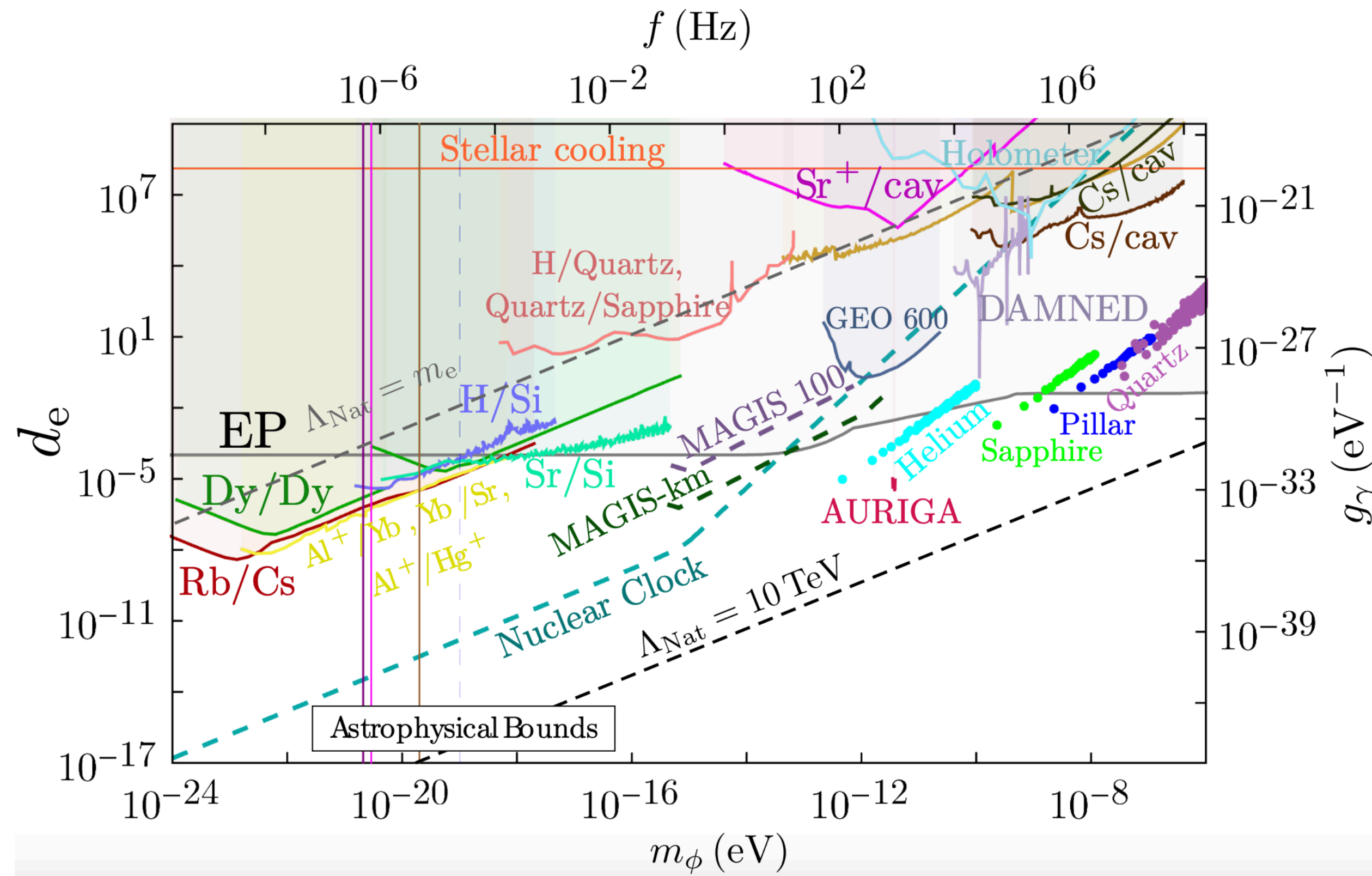
Arvanitaki, Huang, Tilburg

$$\phi(t) \simeq 10^9 \text{GeV} \left(\frac{10^{-20} \text{eV}}{m_\phi} \right) \cos(m_\phi t) \rightarrow \frac{\delta\alpha}{\alpha} \simeq 10^{-9} d_e \left(\frac{10^{-20} \text{eV}}{m_\phi} \right)$$

- Atomic clocks are tuned to specific transitions of atoms
- Compare two frequencies that have different dependences on α

$$\frac{d}{dt} \left(\frac{\nu_2}{\nu_1} \right) = (K_2 - K_1) \frac{1}{\alpha} \frac{d\alpha}{dt}$$

All Constraints



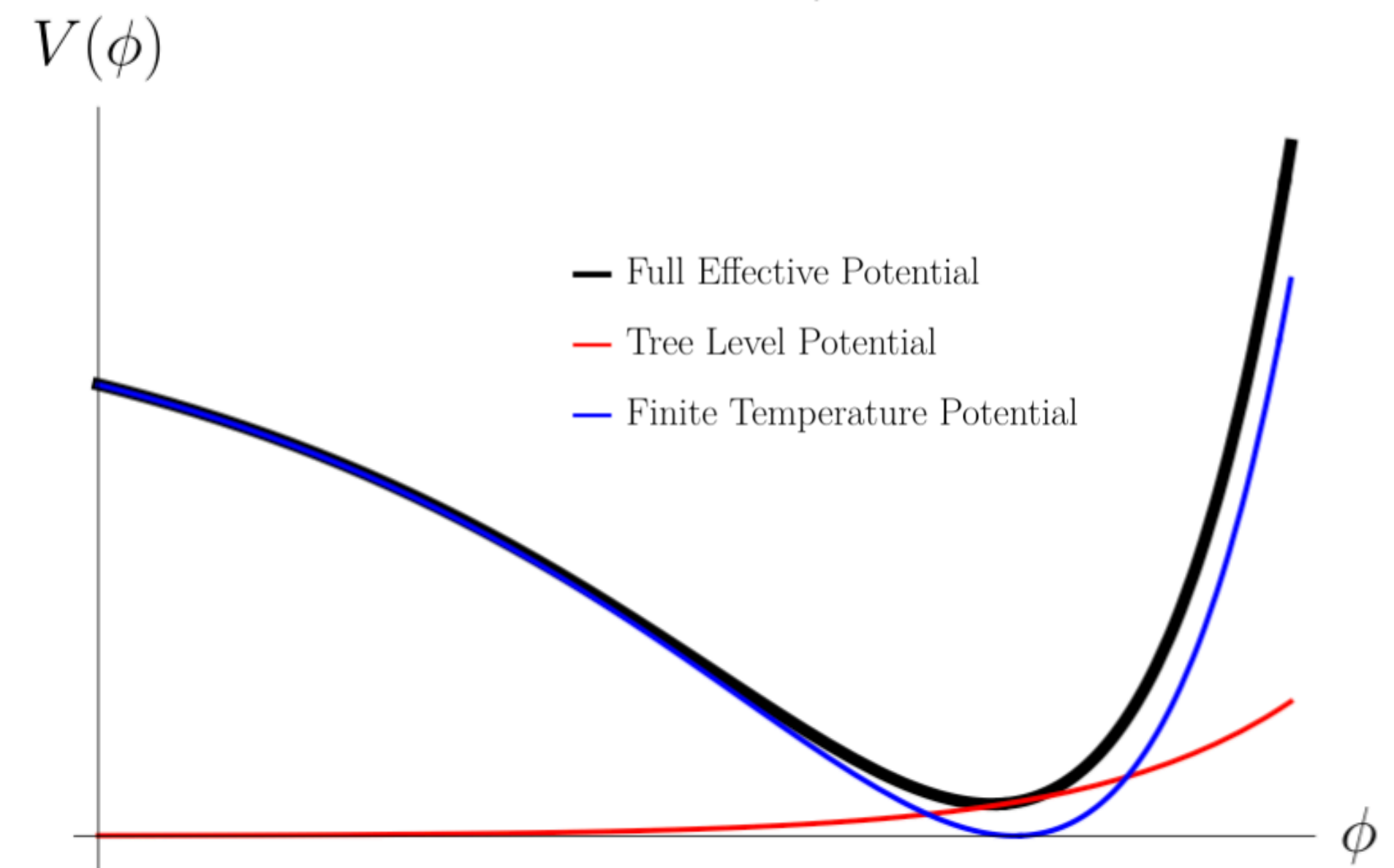
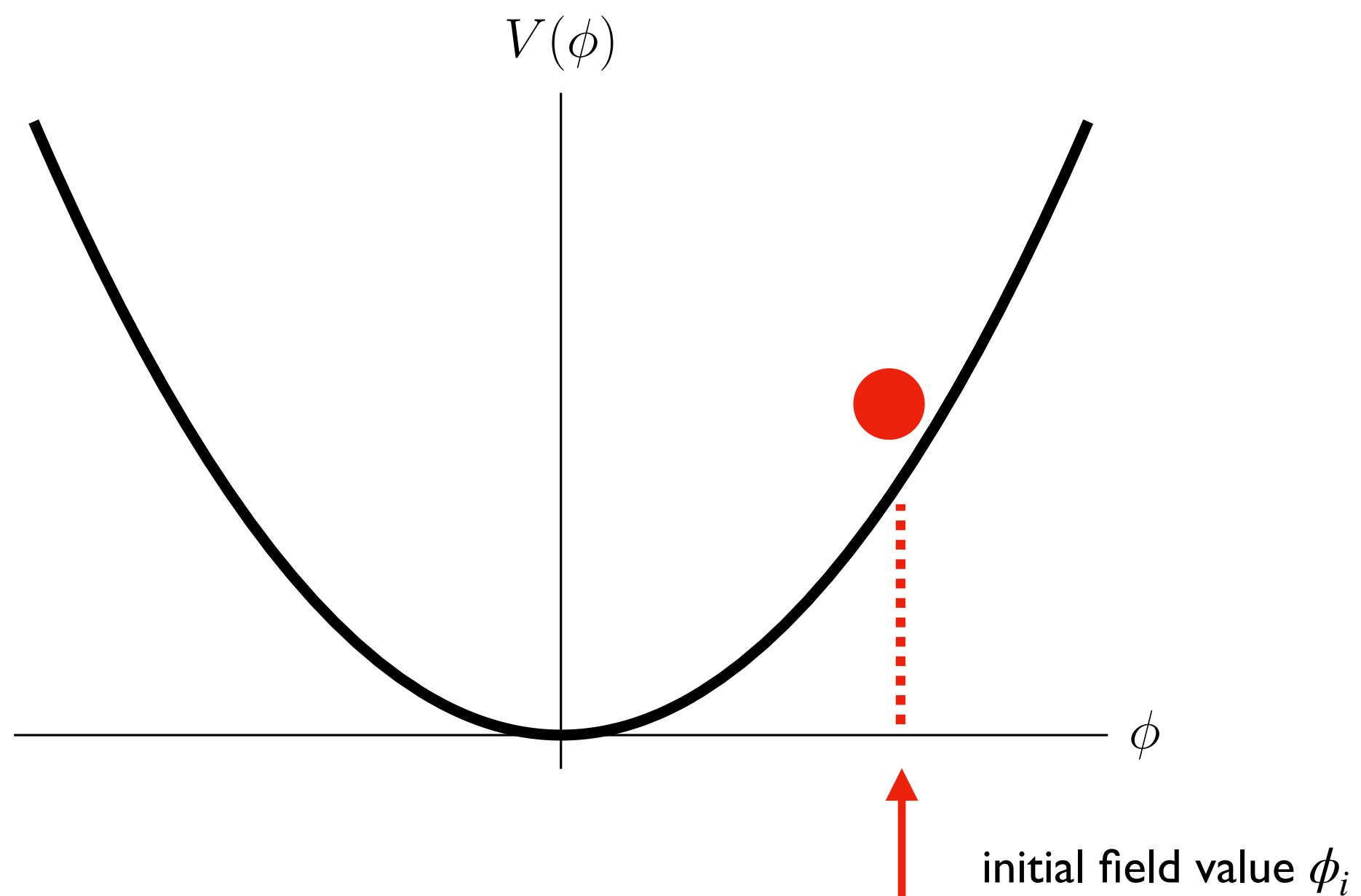
Effects in early universe cosmology

$$\mathcal{L} \supset - \left[m_f \left(1 - \frac{\beta\phi}{M_{\text{pl}}} \right) \bar{\mu}\mu + \text{h.c.} \right] + \frac{1}{2} m_\phi^2 \phi^2$$

$$\ddot{\phi} + 3H\dot{\phi} + m_\phi^2 \phi = 0$$

$$\ddot{\phi} + 3H\dot{\phi} + m_\phi^2 \phi + \frac{\partial V_T(m_\mu(\phi))}{\partial \phi}$$

$T = 10 m_\psi$



Evolution of potential with increasing temperature

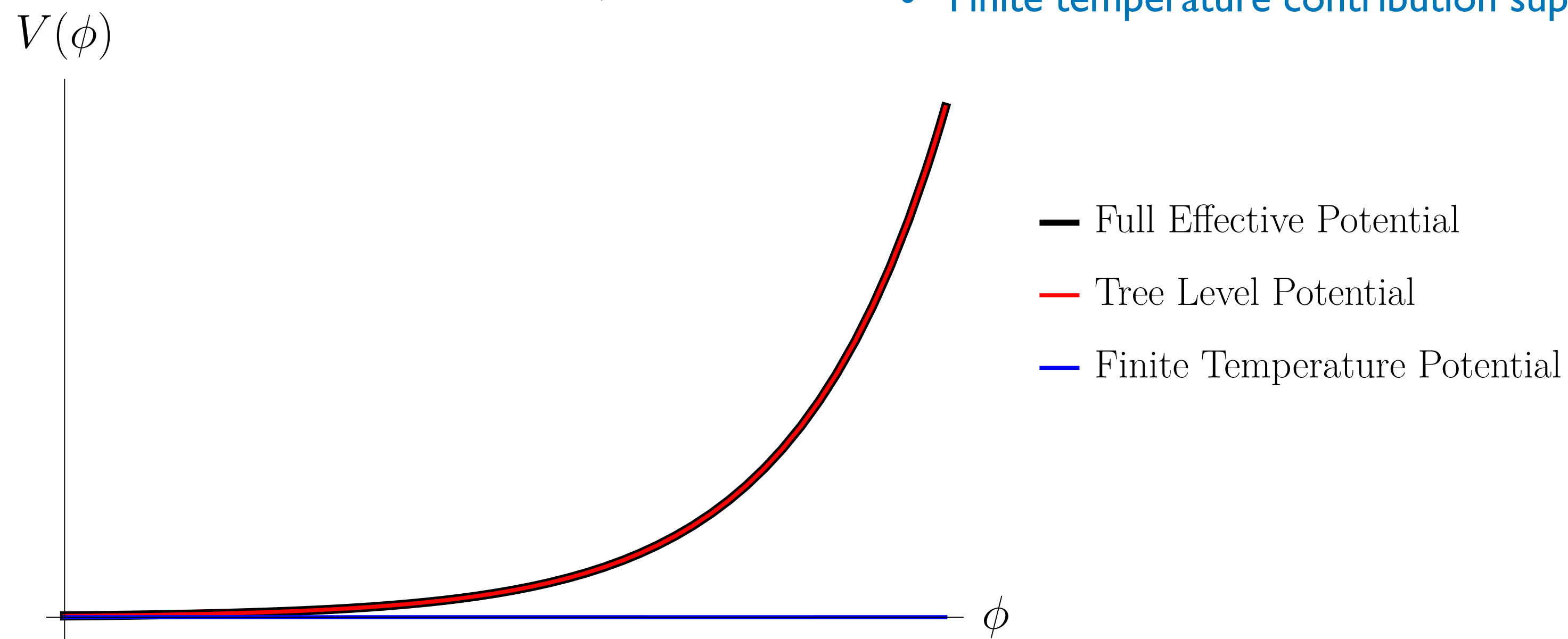
$$V_{\text{eff}}(\phi, T) \simeq V_0(\phi) + V_1^T(\phi) \quad \longrightarrow \quad V_0(\phi) = \frac{1}{2} m_\phi^2 \phi^2$$

$$V_1^T(\phi) = -\frac{g_\psi}{2\pi^2} T^4 \int_0^\infty dx x^2 \log \left[1 + \exp \left(-\sqrt{x^2 + \frac{m_\psi(\phi)^2}{T^2}} \right) \right]$$

$$\sim e^{-m_\psi/T} \quad \text{for } T \ll m_\psi \quad \text{Boltzmann suppressed}$$

Low temperature

$$T = 0.1 m_\psi$$



- Tree level dominates at low temperature
- Finite temperature contribution suppressed

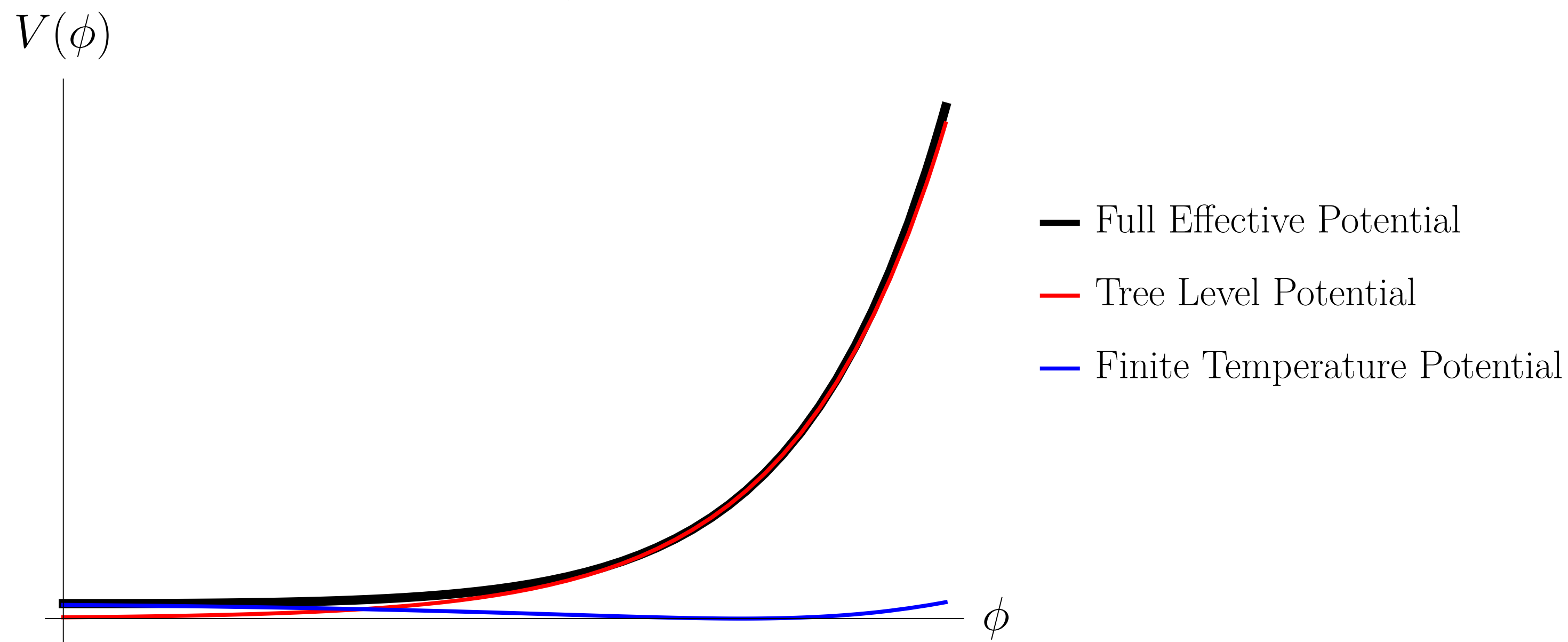
Evolution of potential with increasing temperature

$$V_{\text{eff}}(\phi, T) \simeq V_0(\phi) + V_1^T(\phi) \quad \longrightarrow \quad \begin{aligned} V_0(\phi) &= \frac{1}{2} m_\phi^2 \phi^2 \\ V_1^T(\phi) &= -\frac{g_\psi}{2\pi^2} T^4 \int_0^\infty dx x^2 \log \left[1 + \exp \left(-\sqrt{x^2 + \frac{m_\psi(\phi)^2}{T^2}} \right) \right] \end{aligned}$$

Intermediate temperature

$$T = m_\psi$$

- Finite temperature contribution grows at intermediate temperatures



Evolution of potential with increasing temperature

$$V_{\text{eff}}(\phi, T) \simeq V_0(\phi) + V_1^T(\phi) \quad \longrightarrow \quad V_0(\phi) = \frac{1}{2} m_\psi^2 \phi^2$$

$$V_1^T(\phi) = -\frac{g_\psi}{2\pi^2} T^4 \int_0^\infty dx x^2 \log \left[1 + \exp \left(-\sqrt{x^2 + \frac{m_\psi(\phi)^2}{T^2}} \right) \right]$$

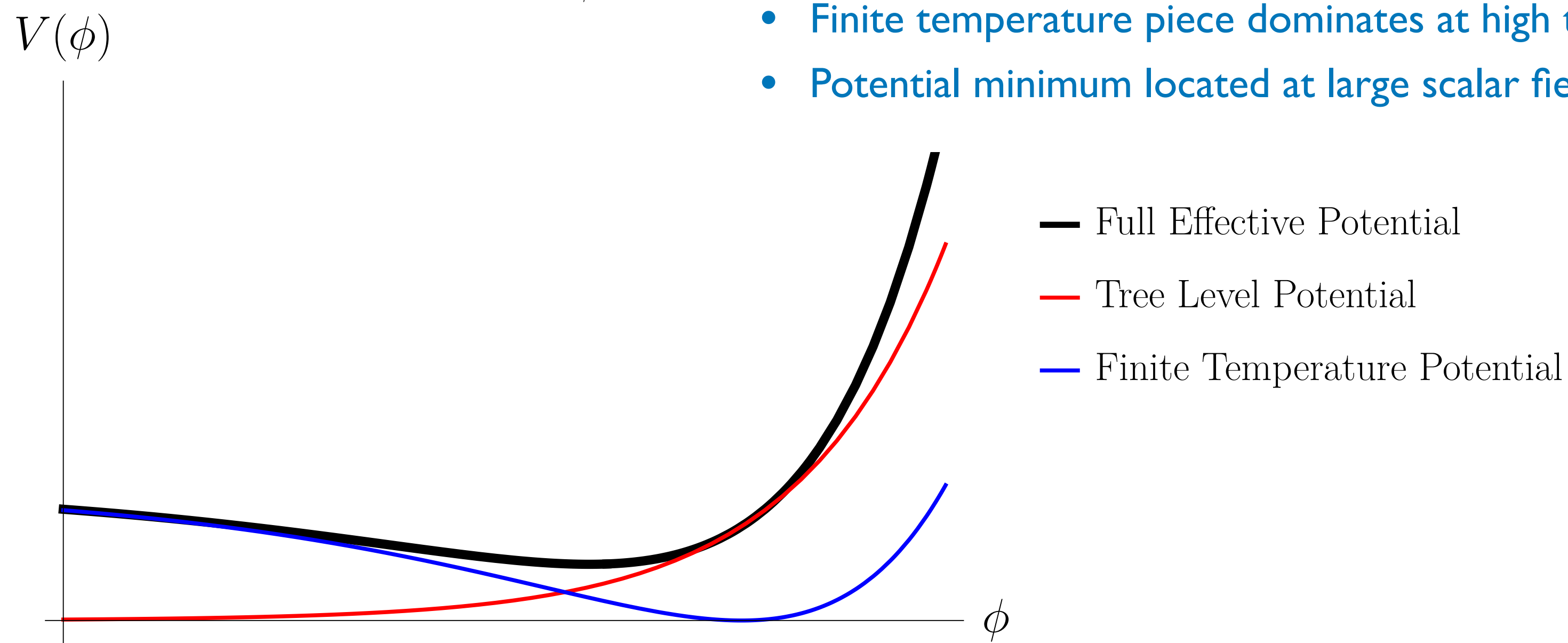
$$\sim \frac{T^2 m_\psi^2}{12} \left(1 - \frac{\beta \phi}{M_{\text{pl}}} \right)^2 \quad \text{for } T \gg m_\psi$$

High temperature

Minimum at $\phi \sim M_{\text{pl}}/\beta$

$$T = 3 m_\psi$$

- Finite temperature piece dominates at high temperatures
- Potential minimum located at large scalar field values



Evolution of potential with increasing temperature

$$V_{\text{eff}}(\phi, T) \simeq V_0(\phi) + V_1^T(\phi) \quad \longrightarrow \quad V_0(\phi) = \frac{1}{2} m_\phi^2 \phi^2$$

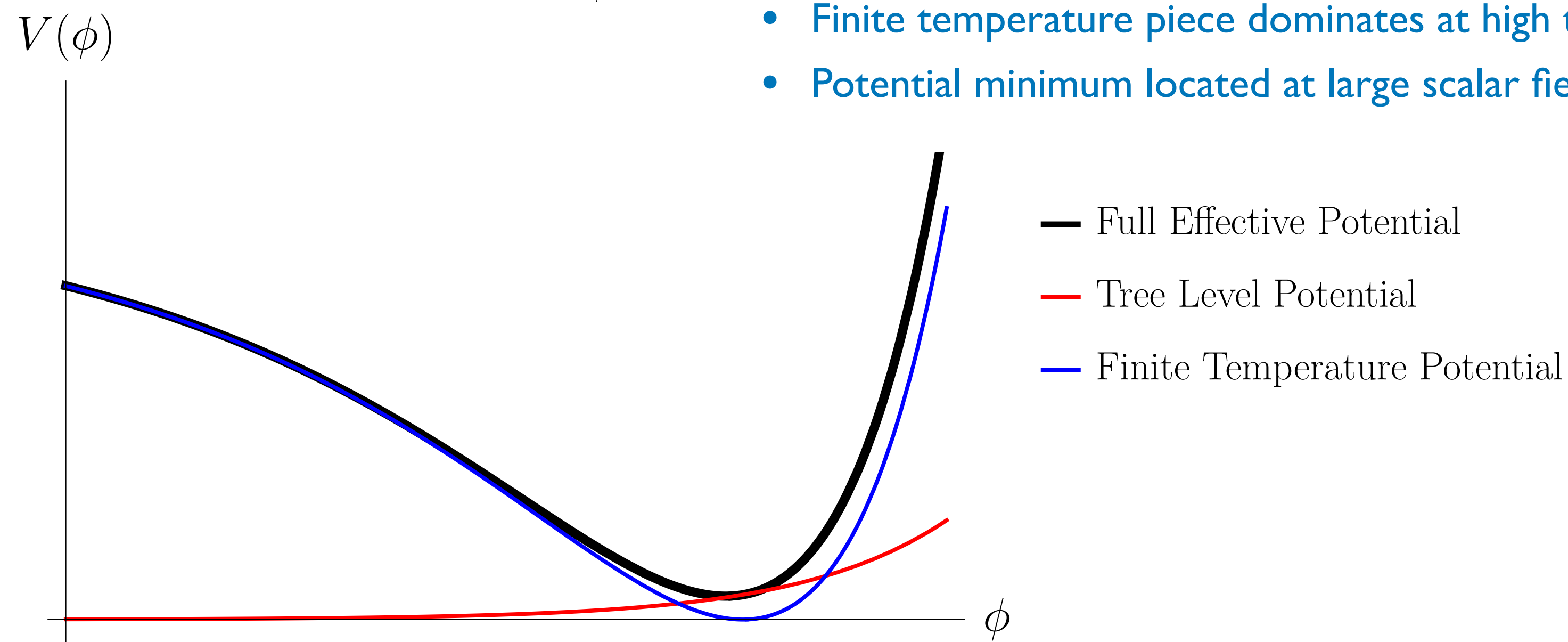
$$V_1^T(\phi) = -\frac{g_\psi}{2\pi^2} T^4 \int_0^\infty dx x^2 \log \left[1 + \exp \left(-\sqrt{x^2 + \frac{m_\psi(\phi)^2}{T^2}} \right) \right]$$

$$\sim \frac{T^2 m_\psi^2}{12} \left(1 - \frac{\beta \phi}{M_{\text{pl}}} \right)^2 \quad \text{for } T \gg m_\psi$$

High temperature

Minimum at $\phi \sim M_{\text{pl}}/\beta$

$$T = 10 m_\psi$$



- Finite temperature piece dominates at high temperatures
- Potential minimum located at large scalar field values

Cartoon sketch of the mechanism

- Assume nonzero homogeneous scalar field with arbitrary* initial condition after inflation
- In the case of a Standard Model fermion, initial condition set after electroweak phase transition



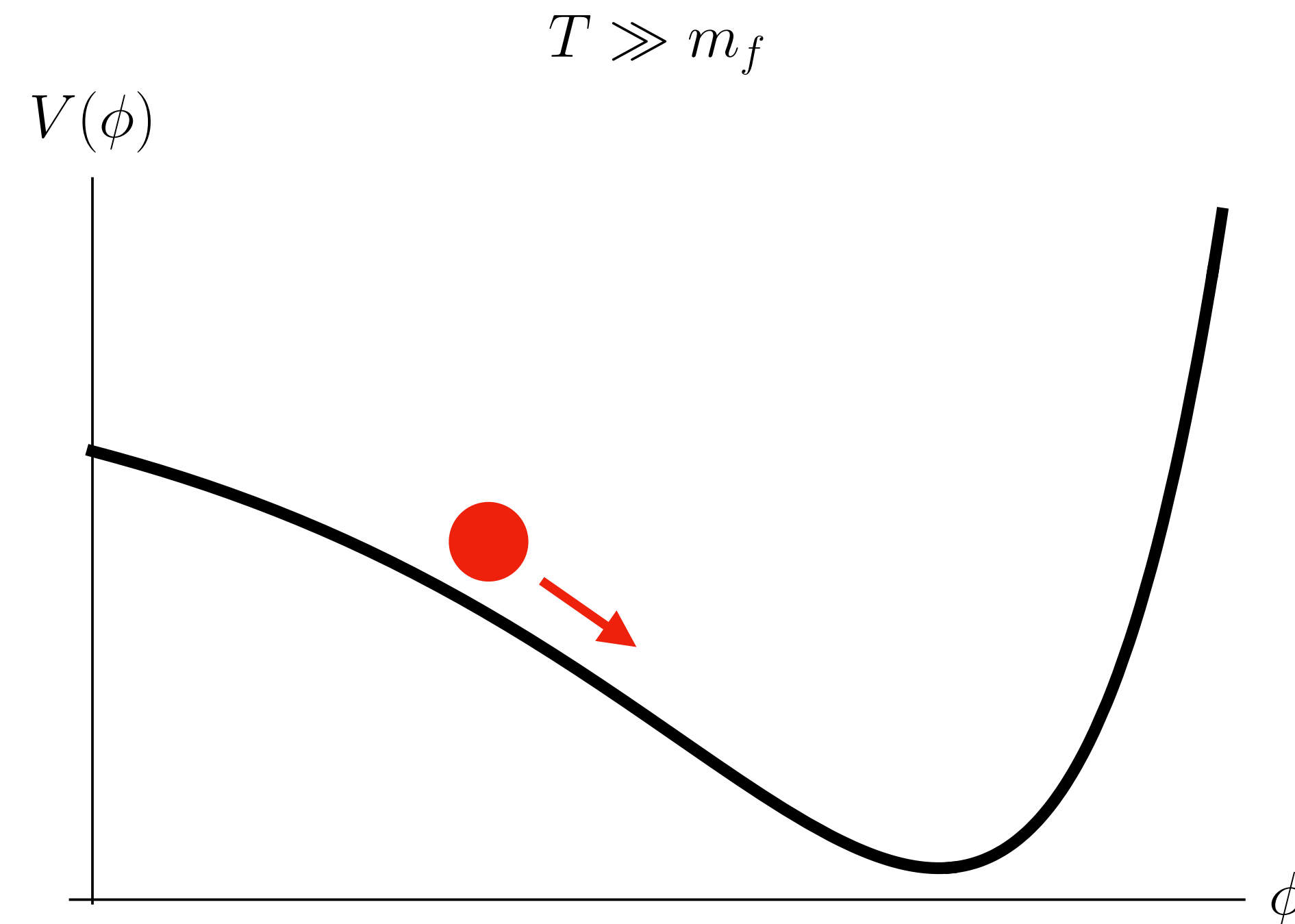
* Caveats will be discussed below

Cartoon sketch of the mechanism

Slide by BB

- Inflation ends and reheating occurs, creating the thermal plasma.
- The finite temperature potential dominates at this stage.
- ϕ rolls toward the minimum at large field values, generating misalignment

High temperature

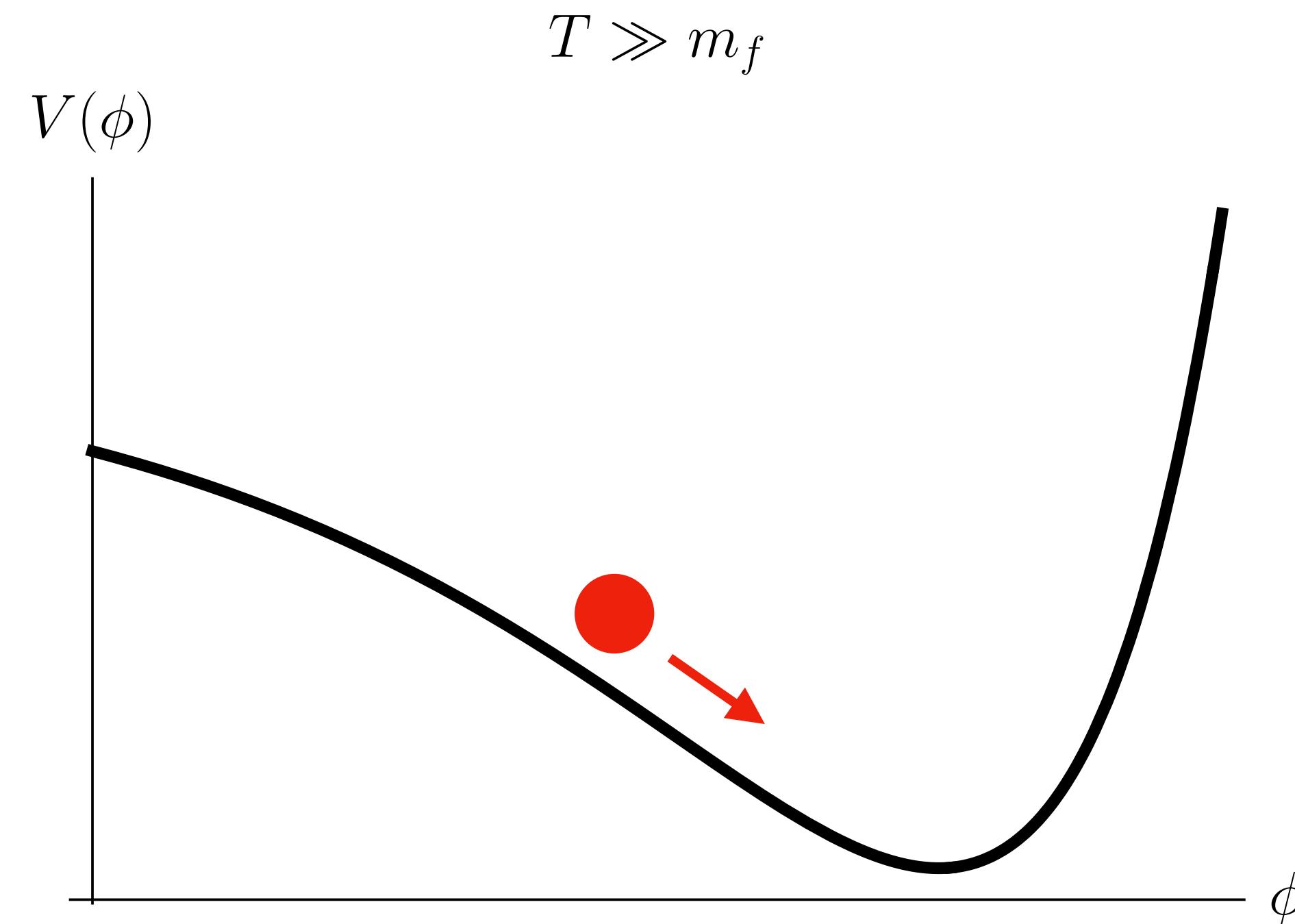


Cartoon sketch of the mechanism

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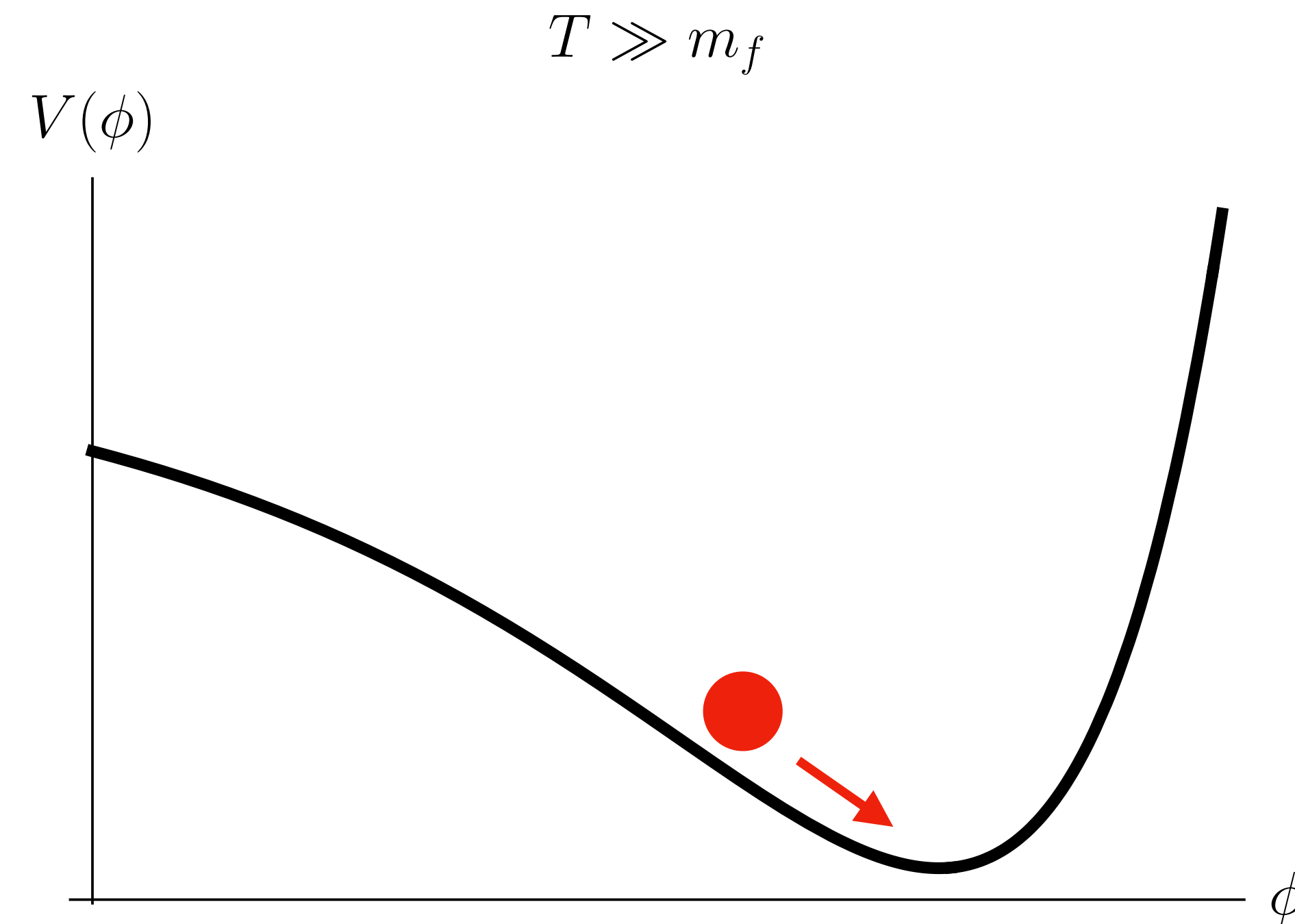


Cartoon sketch of the mechanism

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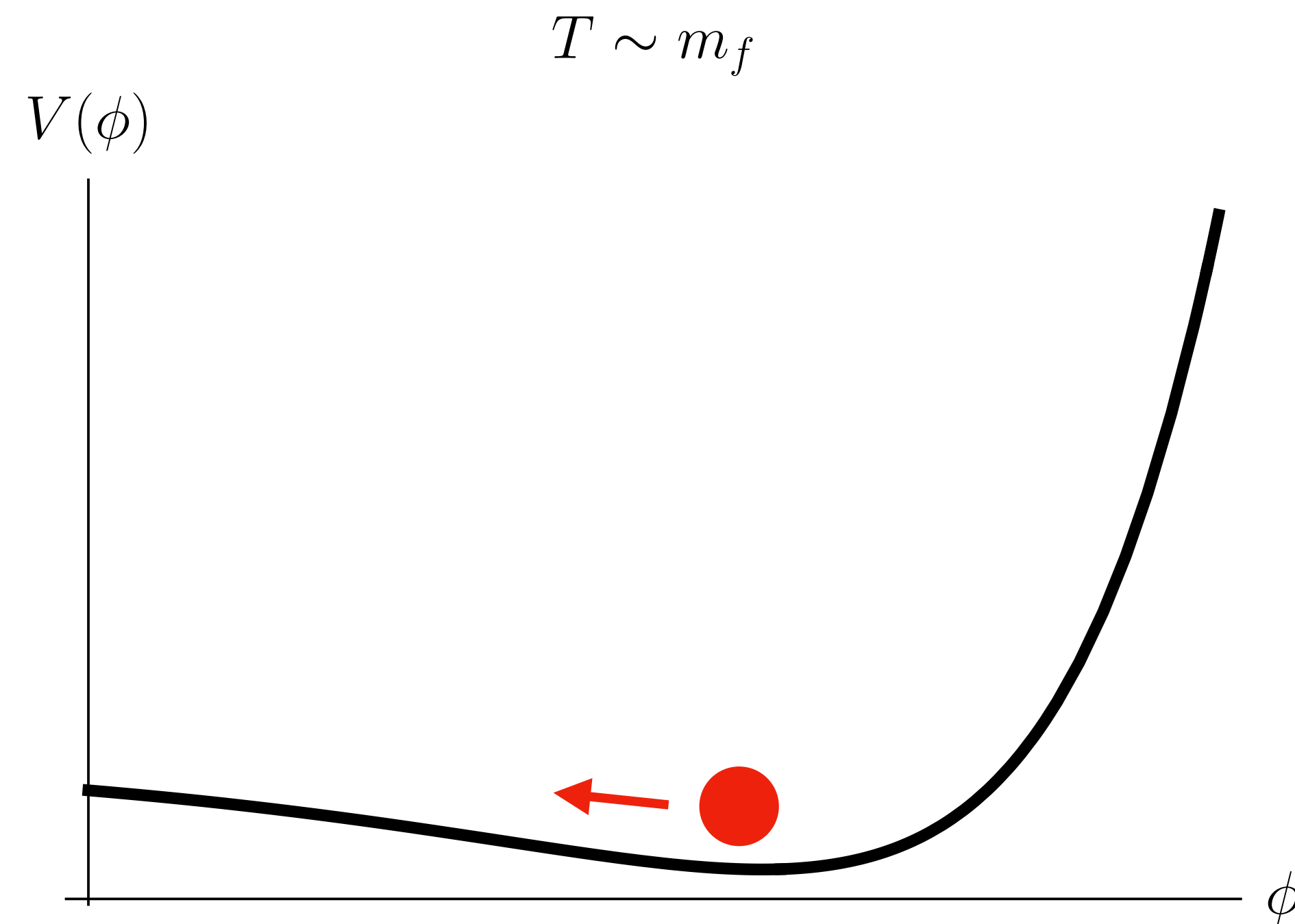


Cartoon sketch of the mechanism

Slide by BB

- At intermediate temperatures of order the fermion mass, the finite temperature pieces becomes smaller.
- The minimum moves toward the origin

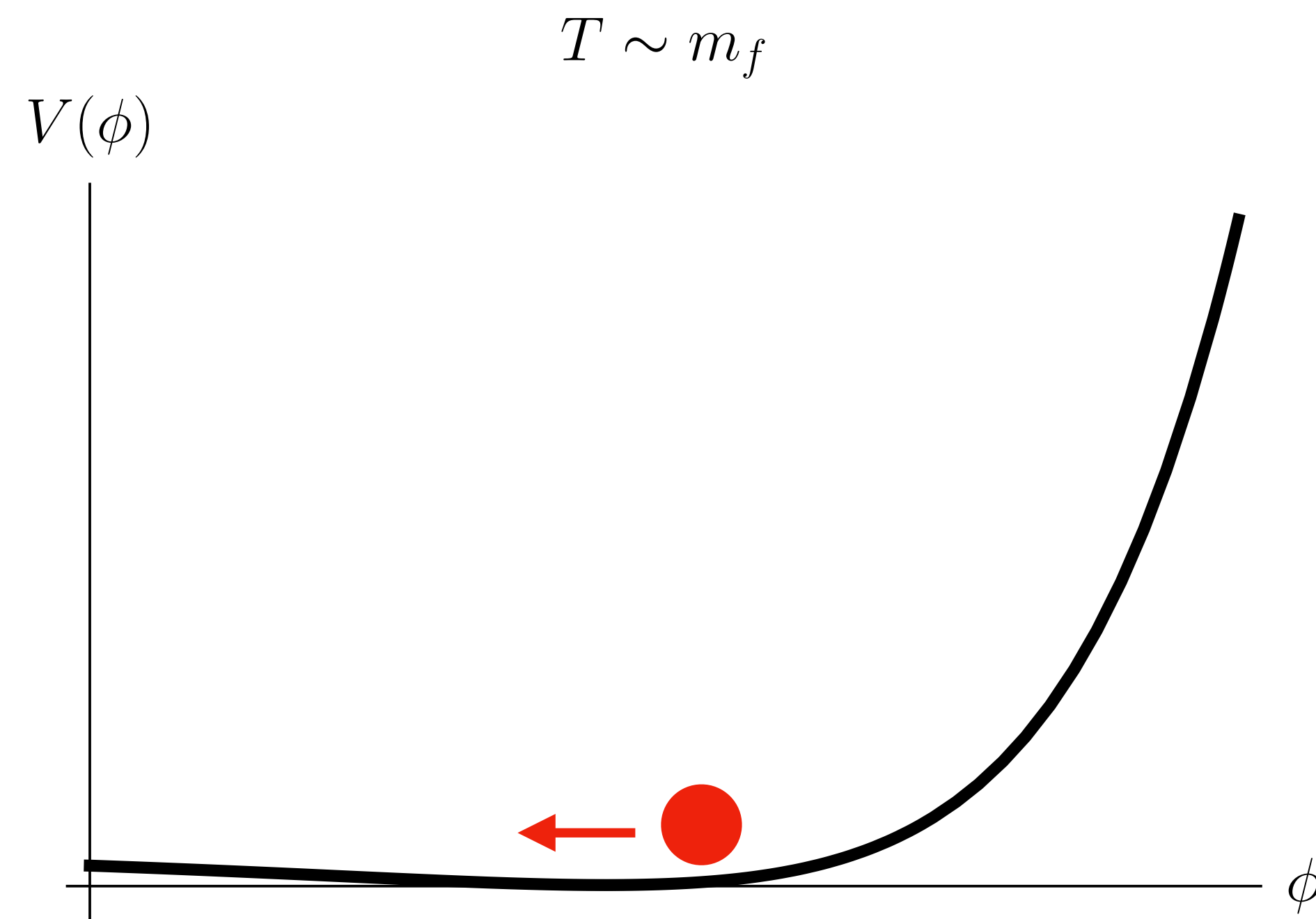
Intermediate temperature



Cartoon sketch of the mechanism

Slide by BB

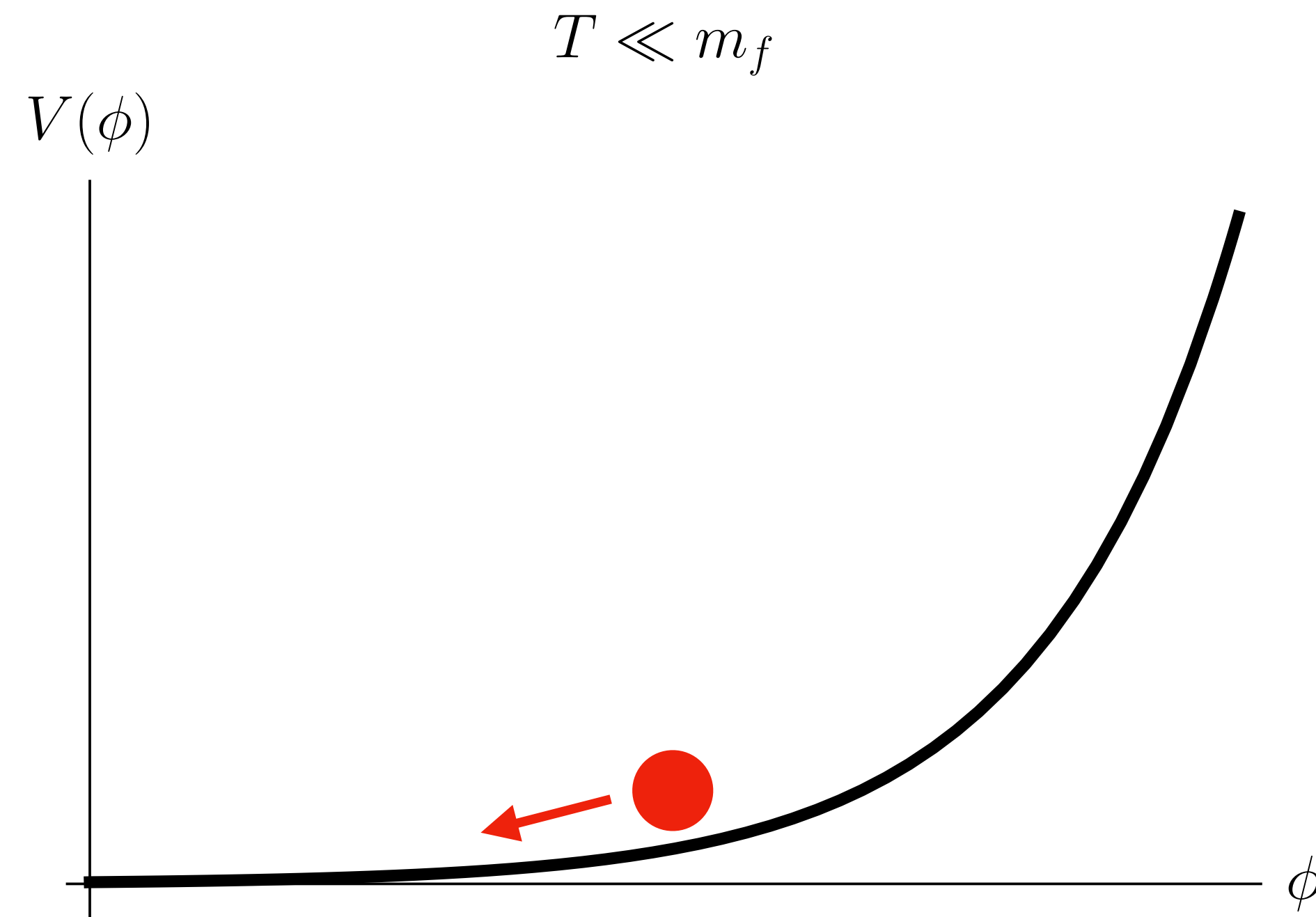
- At intermediate temperatures of order the fermion mass, the finite temperature pieces becomes smaller.
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Cartoon sketch of the mechanism

Slide by BB

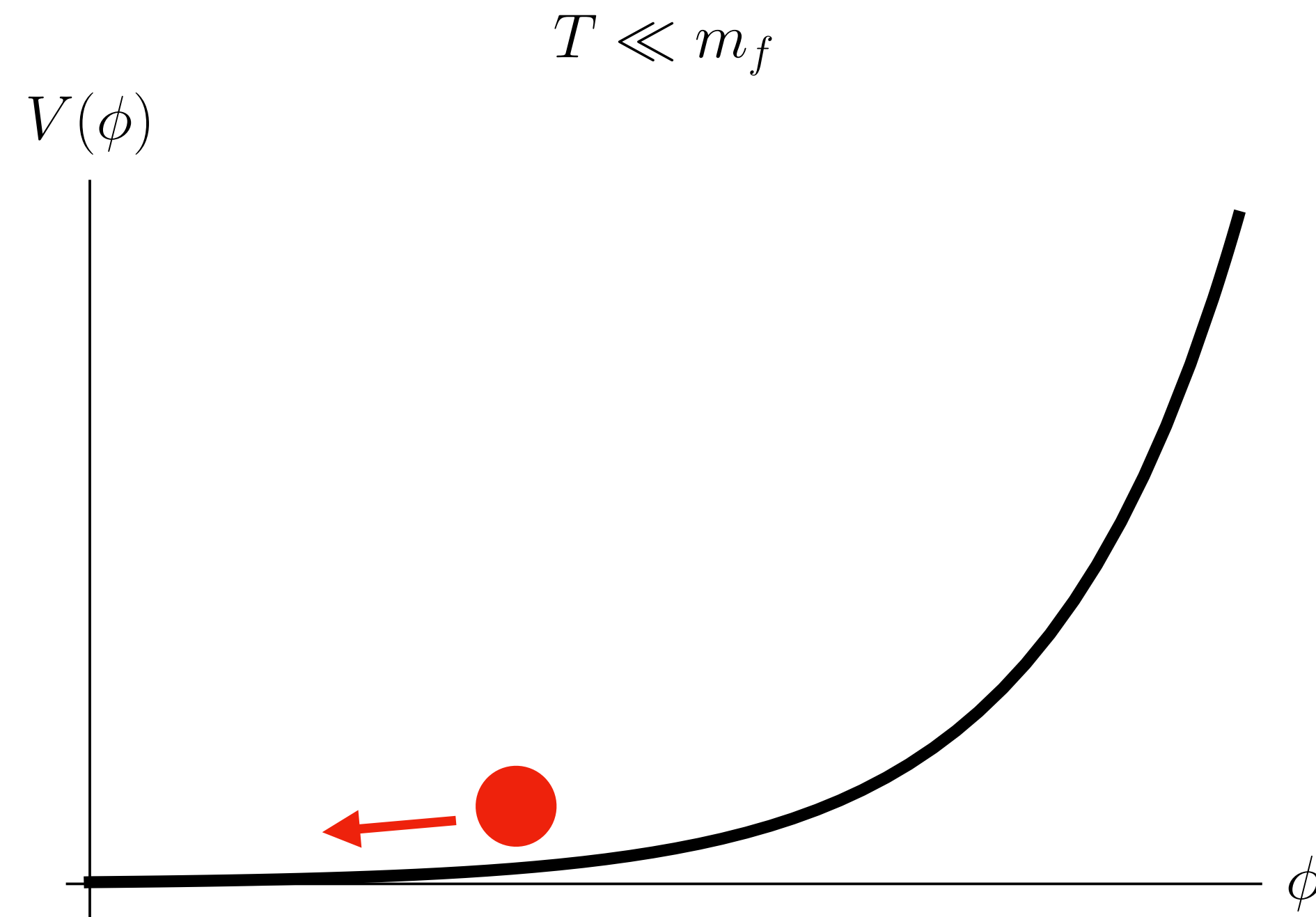
- At low temperatures the tree level potential dominates
- The minimum is located at the origin
- Eventually ϕ oscillates and behaves as dark matter



Cartoon sketch of the mechanism

Slide by BB

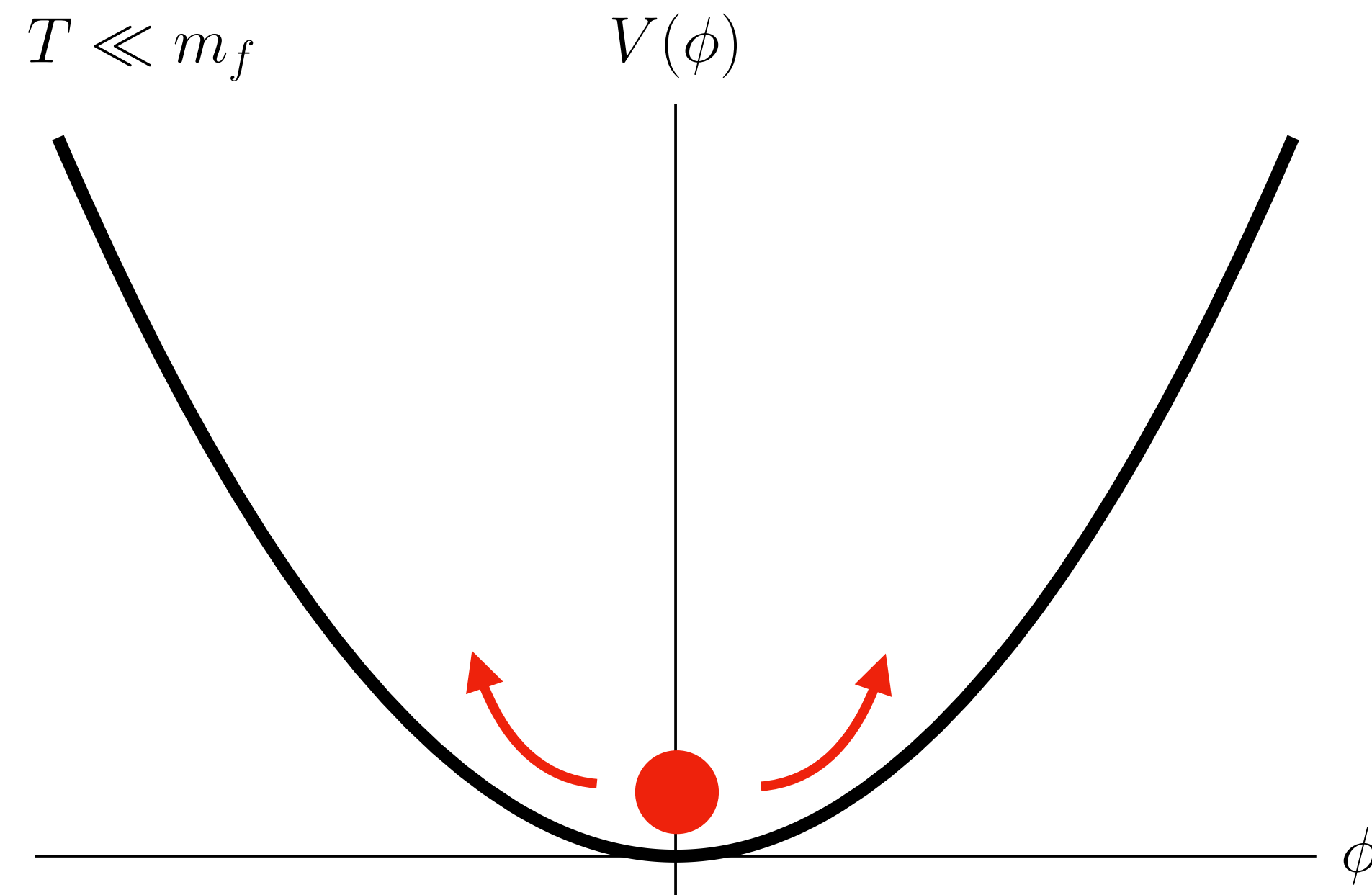
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Cartoon sketch of the mechanism

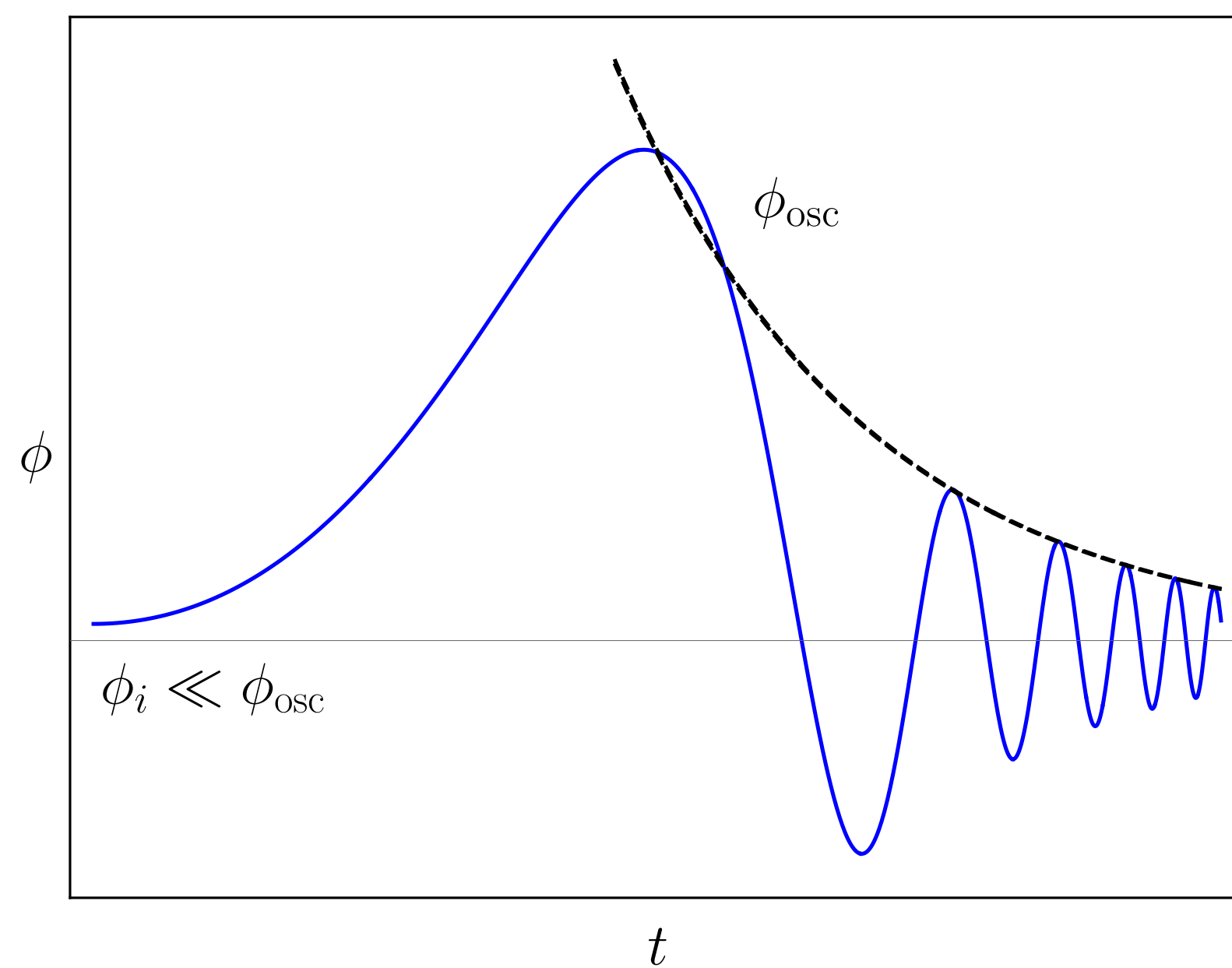
Slide by BB

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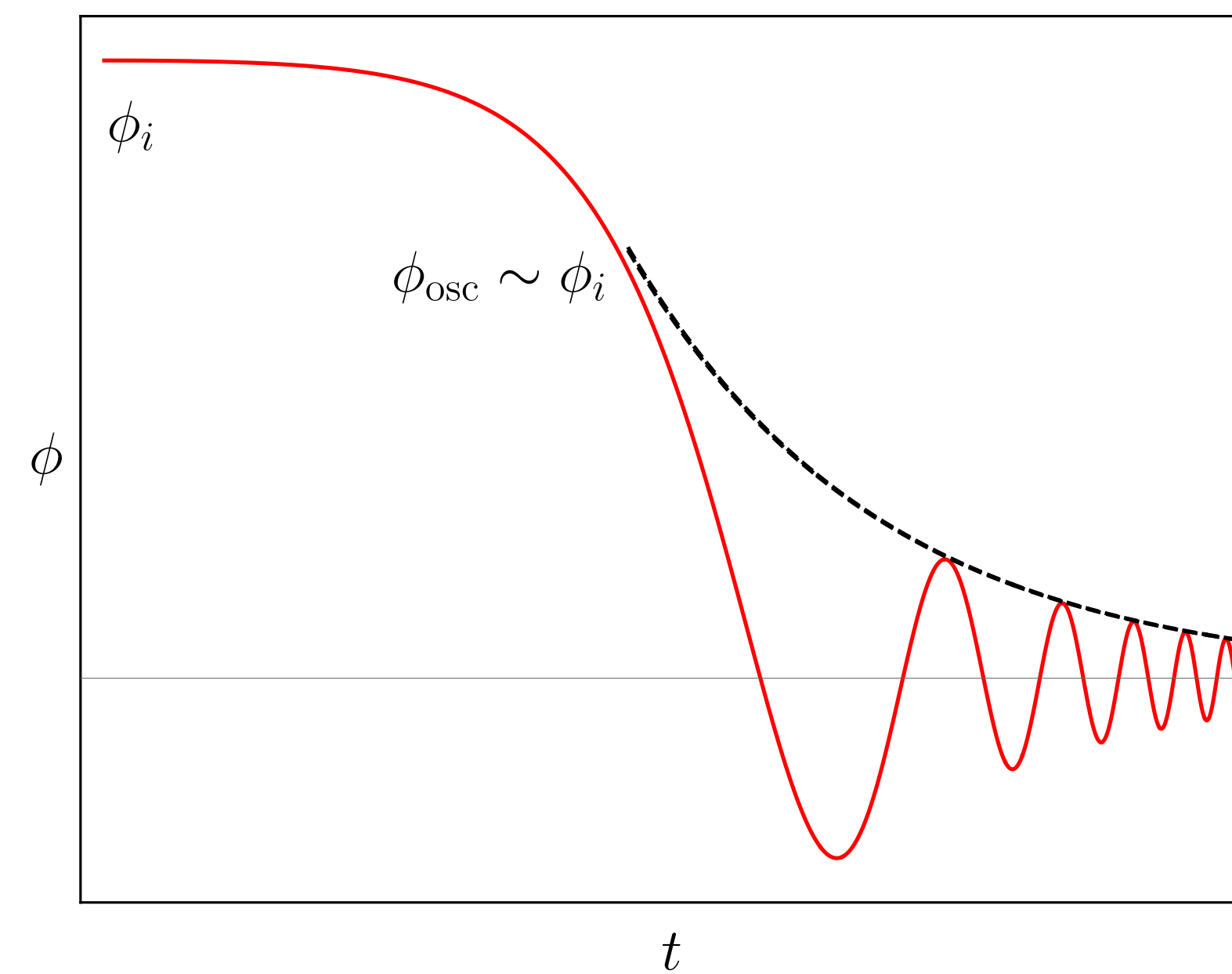
Thermal misalignment mechanism

Thermal Misalignment



- At high temperatures, ϕ is dynamically misaligned from a small initial value to its oscillation amplitude

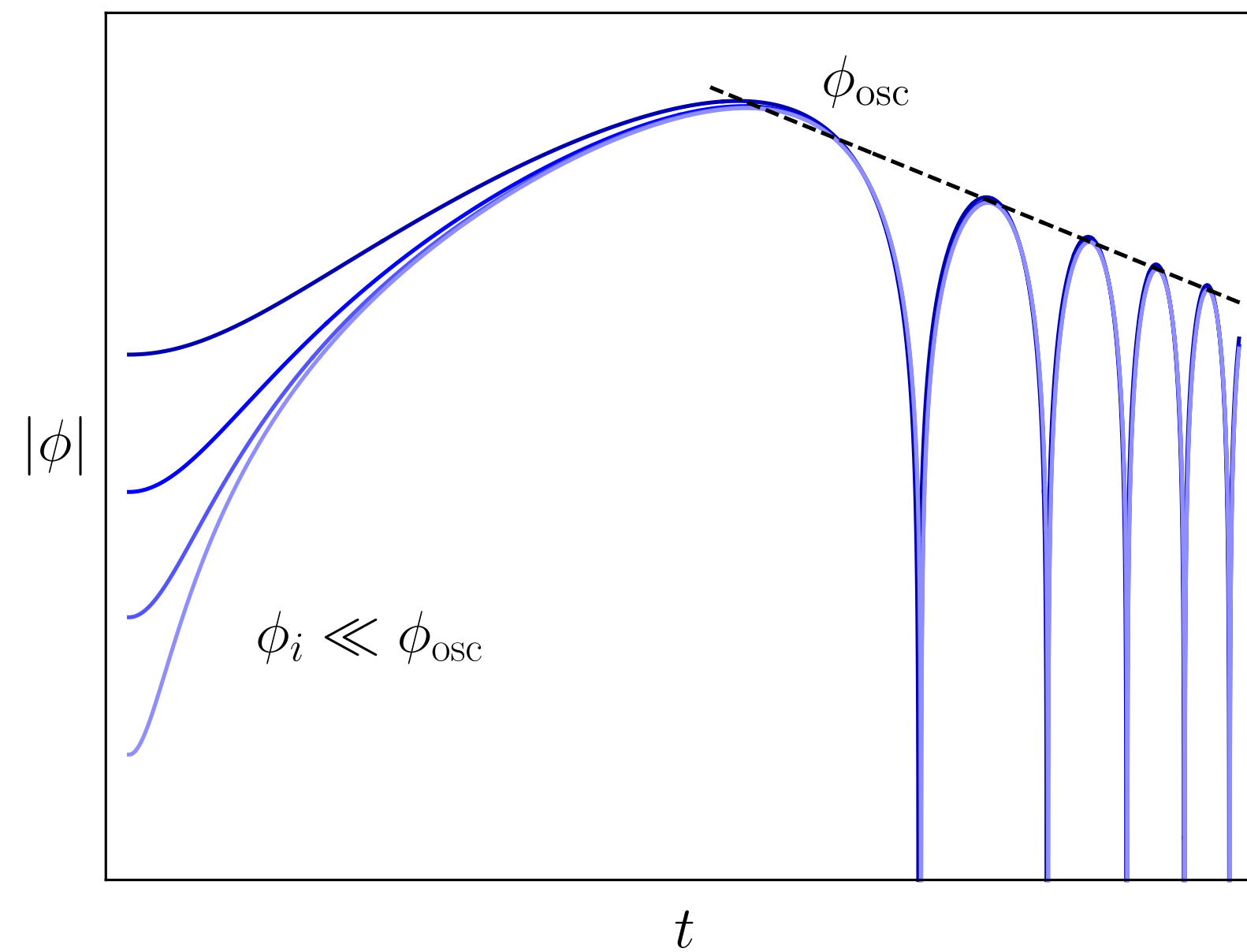
Classic Misalignment



- ϕ oscillation amplitude and abundance dictated by initial conditions

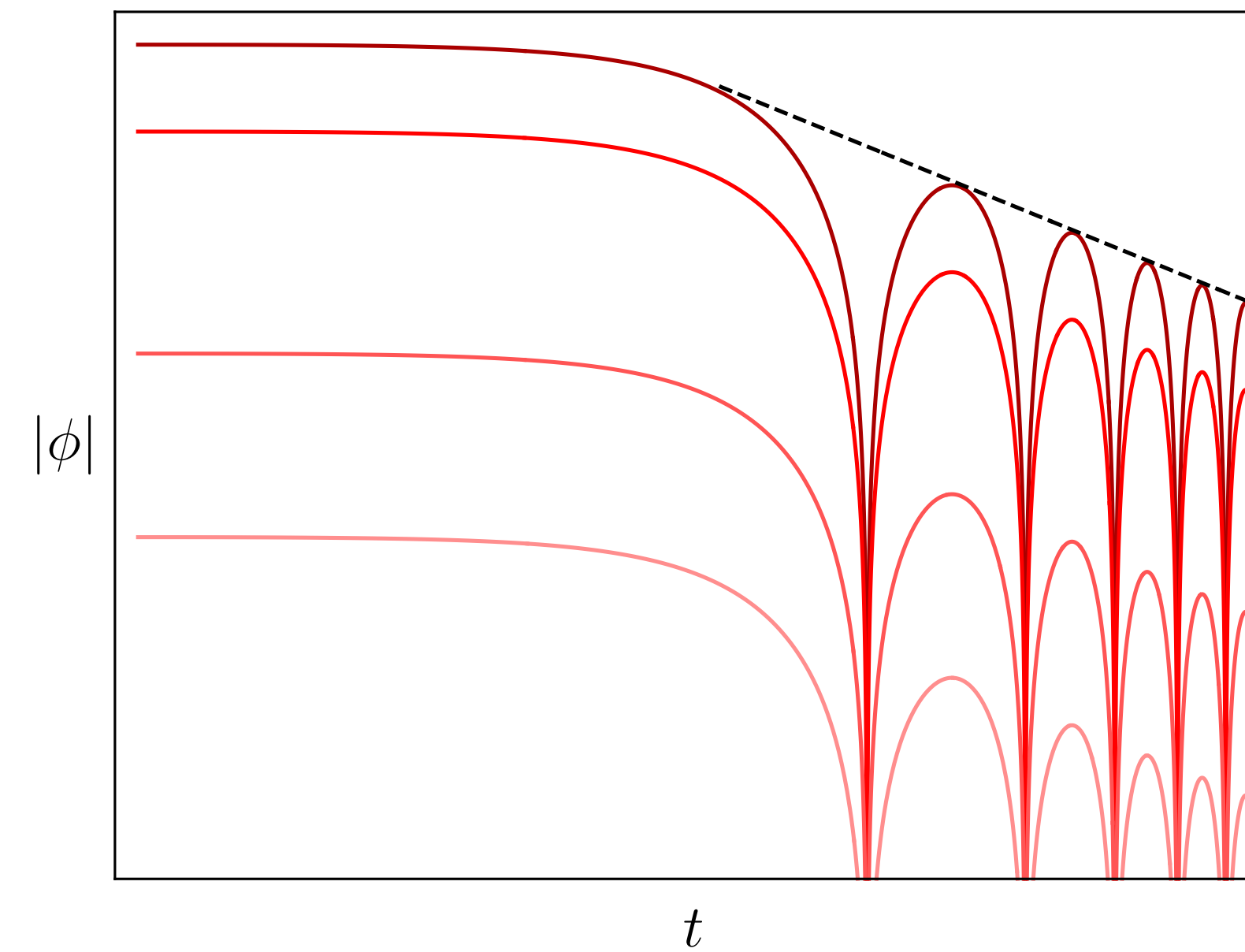
Thermal misalignment mechanism

Thermal Misalignment



- At high temperatures, ϕ is dynamically misaligned from a small initial value to its oscillation amplitude
- The oscillation amplitude is an attractor for $\phi_i \ll \phi_{osc}$ - insensitive to initial conditions

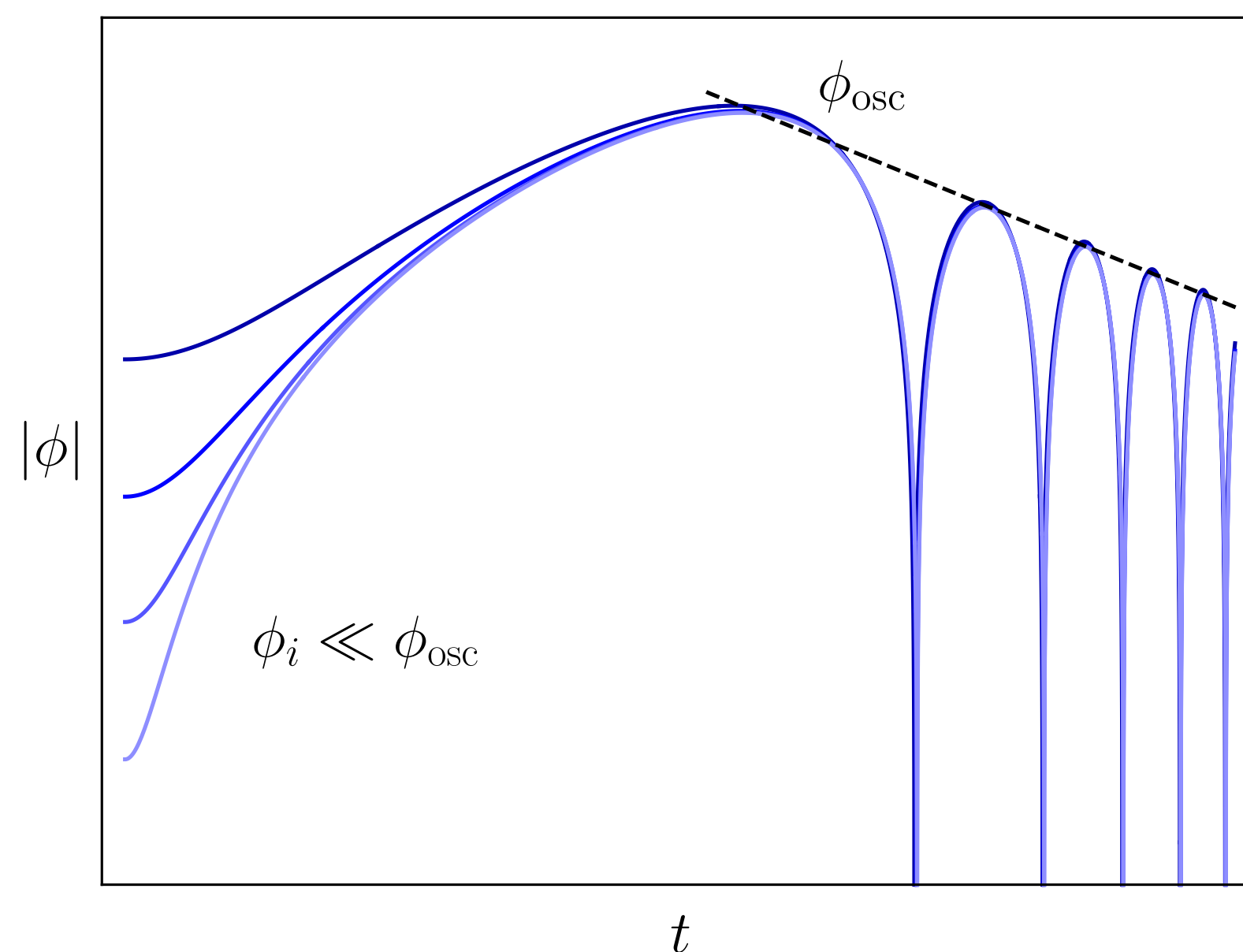
Classic Misalignment



- ϕ oscillation amplitude and abundance dictated by initial conditions

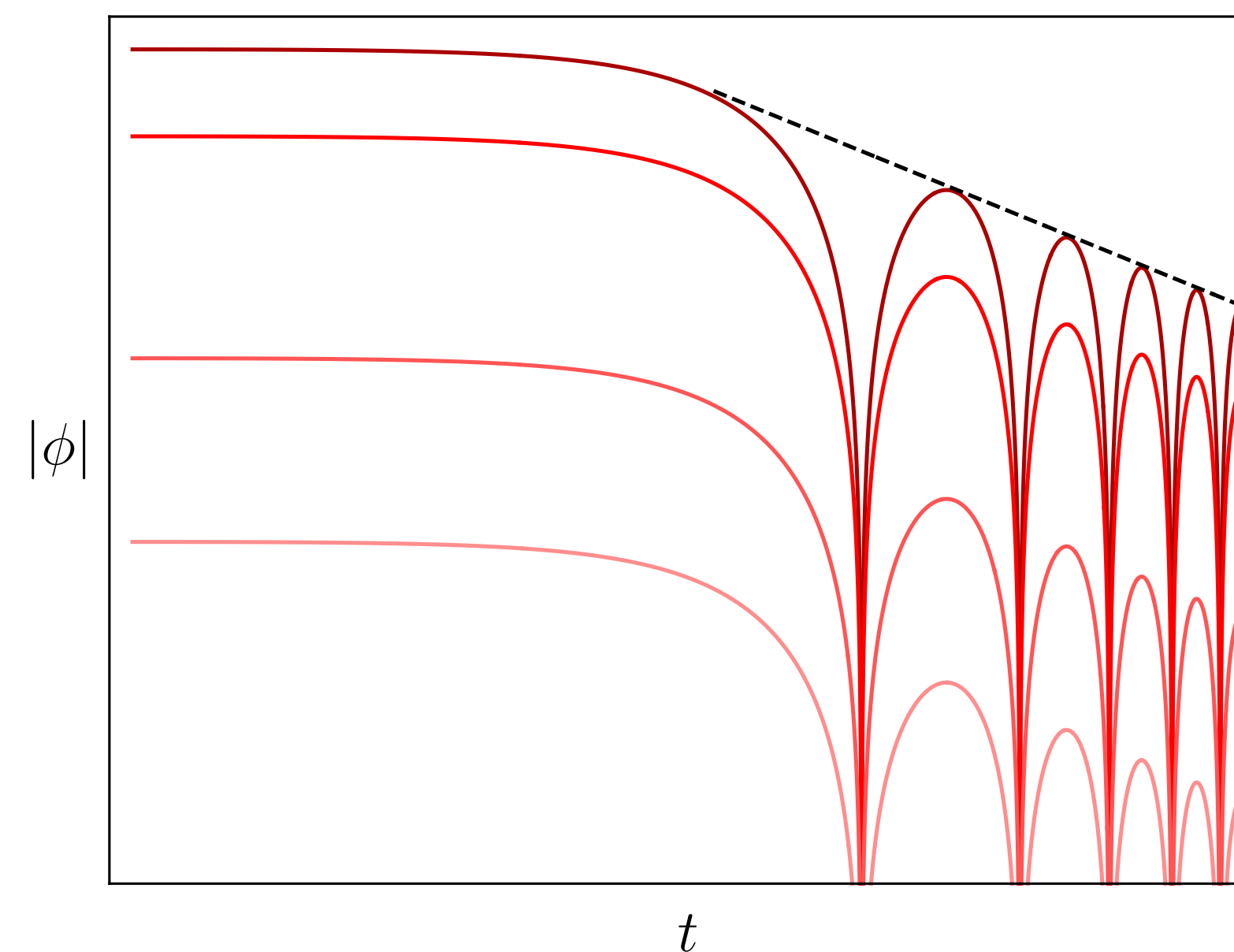
Thermal misalignment mechanism

Thermal Misalignment



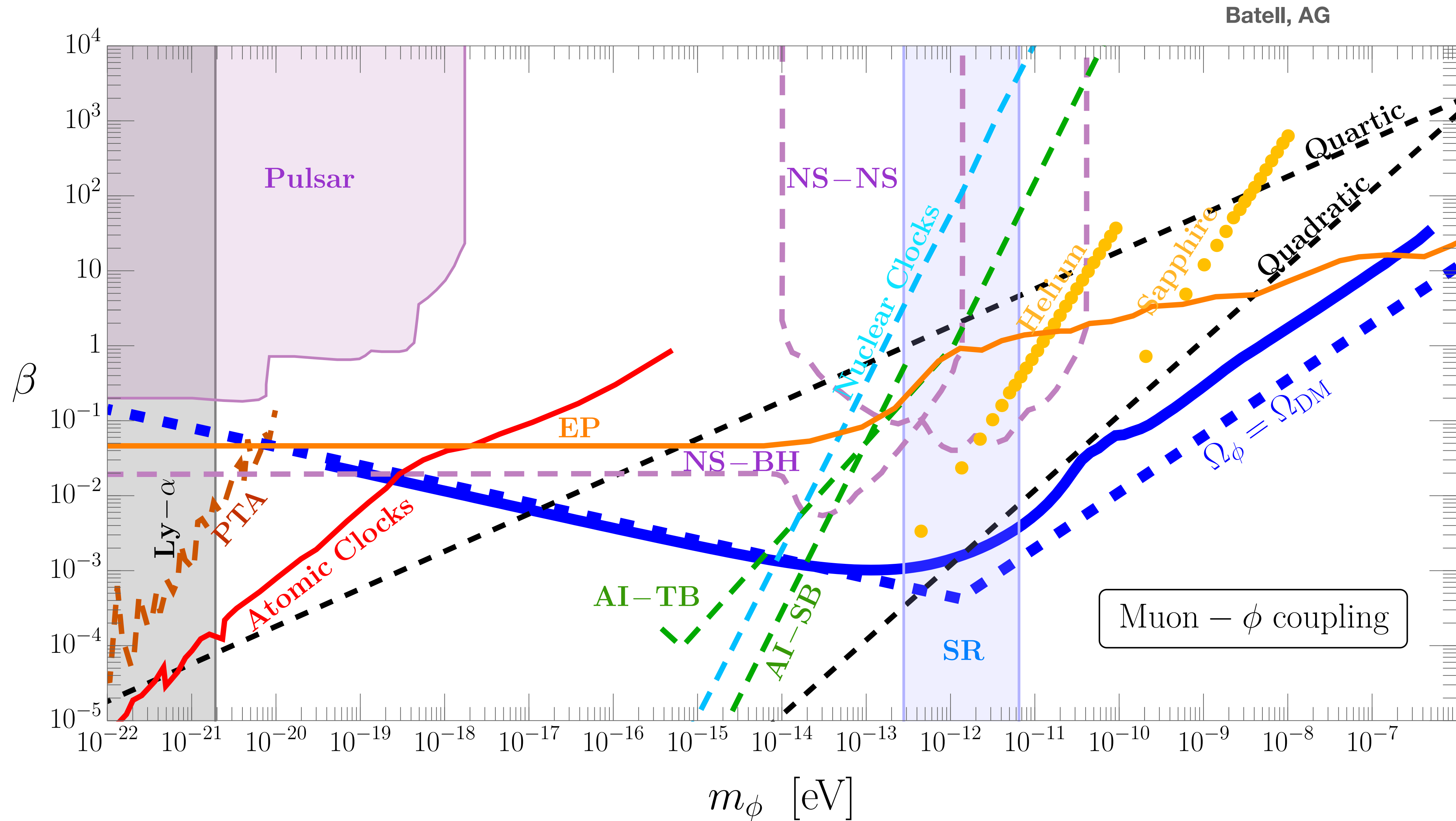
- At high temperatures, ϕ is dynamically misaligned from a small initial value to its oscillation amplitude
- The oscillation amplitude is an attractor for $\phi_i \ll \phi_{\text{osc}}$ - insensitive to initial conditions
- The oscillation amplitude and resulting abundance is dictated by microscopic particle physics

Classic Misalignment



- ϕ oscillation amplitude and abundance dictated by initial conditions

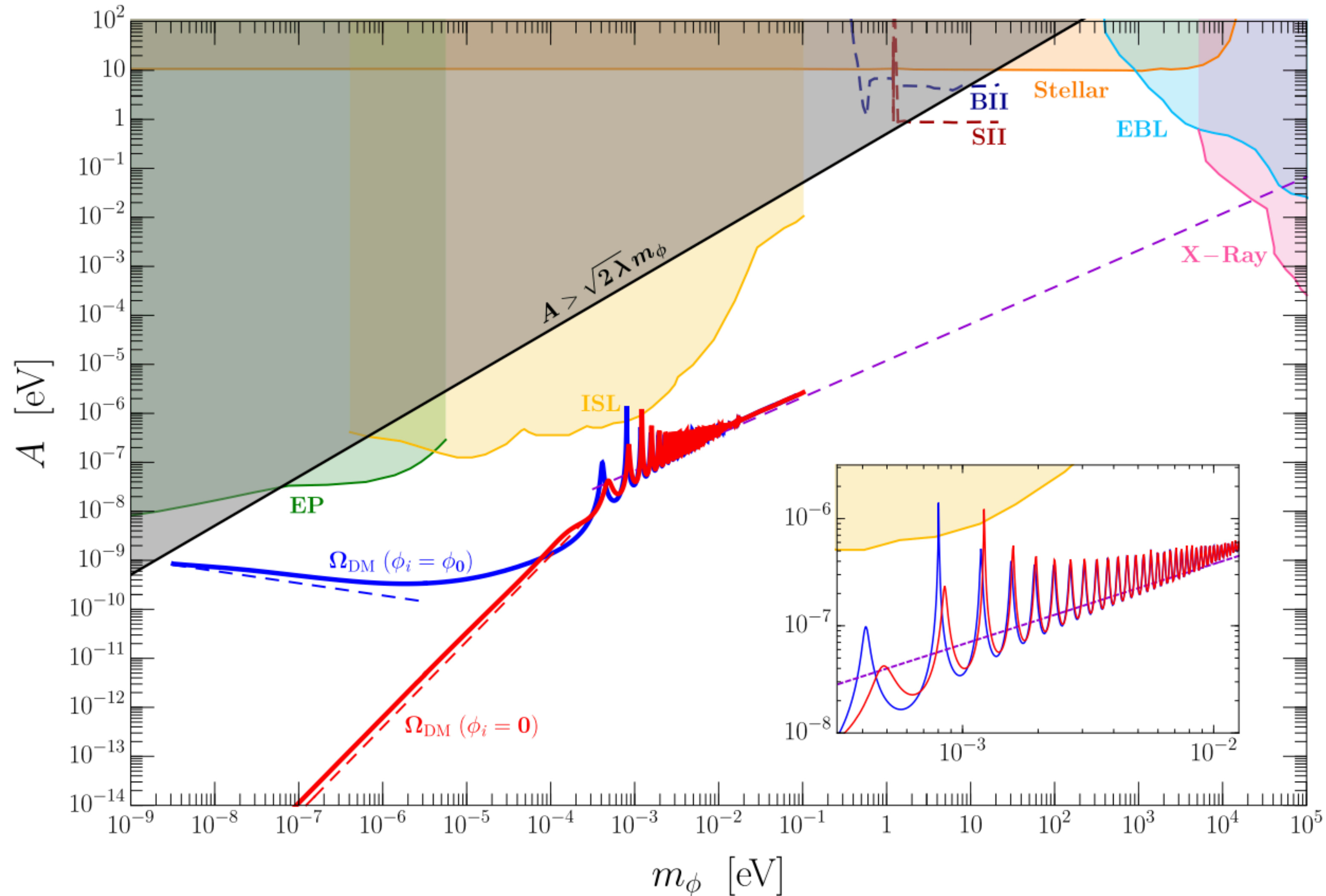
Constraints from Thermal Misalignment



Thermal Misalignment of Higgs portal scalar

$$V \supset -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2 + A\phi H^\dagger H + \frac{1}{2}m_\phi^2 \phi^2$$

Batell, AG, Rai



Summary

- Ultralight bosons can be DM.
- Purely gravitational interactions constraint $m_\phi \gtrsim 10^{-20} \text{eV}$ (and intermediate masses from superradiance)
- Couplings with SM mediate long range forces which can be detected
- Large number of Ultralight bosons can modify fundamental constants/masses
- Increasingly precise ways to measure time/distance has allowed us to put strong constraints on ULDM-SM coupling
- Presence of large amount of SM particles in the early universe modifies the ULDM scalar potential, modifying ULDM dynamics, sourcing misalignment