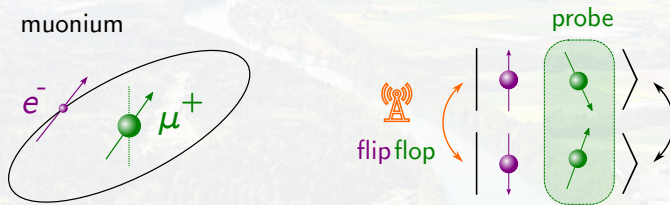


# Multi-Quantum Spectroscopy of Anisotropic Muonium



Andrin Doll

Thomas Hicken, Thomas Prokscha, Zaher Salman



# Main Idea

## 1 Microwave excitation in $\mu$ SR

- Electron gyromagnetic ratio  $\gamma_e$

➔ Muonium transitions

## 2 Relation to previous work

### 1 $\mu$ SR with GHz microwaves

- Muonium spectroscopy

Patterson, Rev. Mod. Phys, **1988**

Nishimura *et al.*, Phys. Rev. A, **2021**

### 2 $\mu$ SR with MHz radio-frequencies

- RF muon rotation

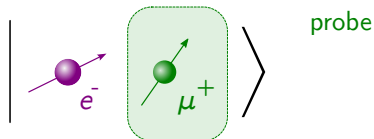
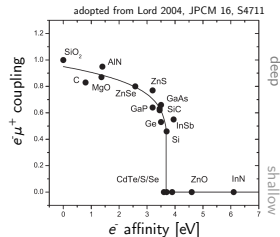
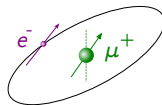
Giblin *et al*, Nucl. Instrum. Meth. Phys. Res.,  
**2014**

- DEMUR, Decoupling, Delayed formation

Patterson, Rev. Mod. Phys, **1988**

Lord *et al*, J. Phys. Condens. Matter, **2004**

muonium



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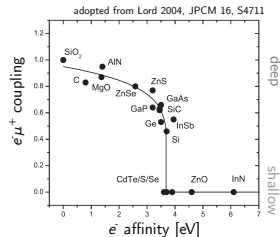
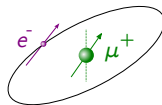
Giblin *et al*, Nucl. Instrum. Meth. Phys. Res.,  
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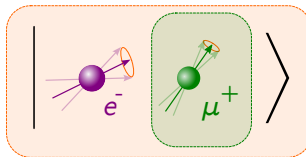
Lord *et al*, J. Phys. Condens. Matter, **2004**

muonium



mechanisms .... and why bother?

pump

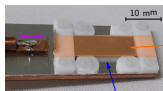
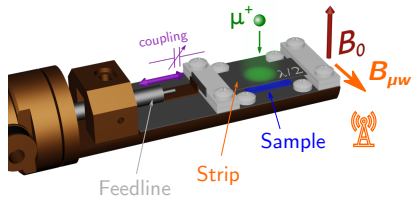


probe

# Realization in practice

probehead

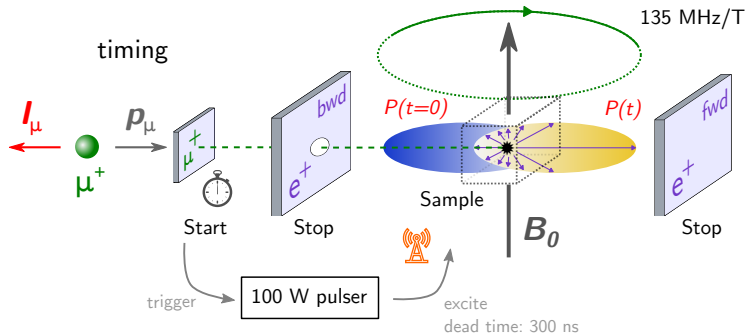
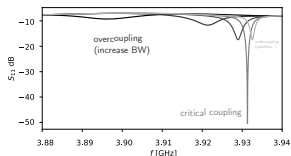
$\lambda/2$ : 3.8 GHz (28 mm)



coupling

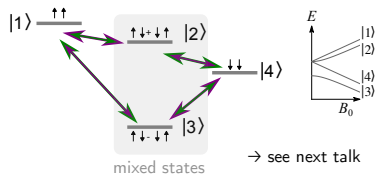
example data at 80 K

(at low T, up to 30 G of wave field)

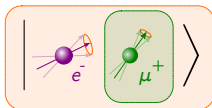


# Detectable microwave transitions

strong coupling

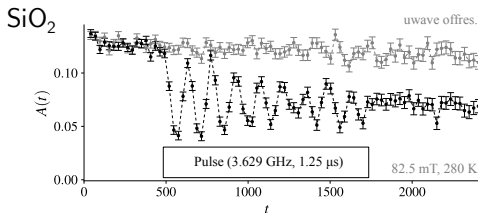
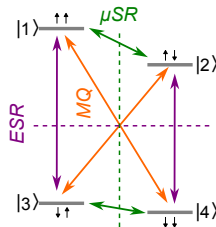


pump

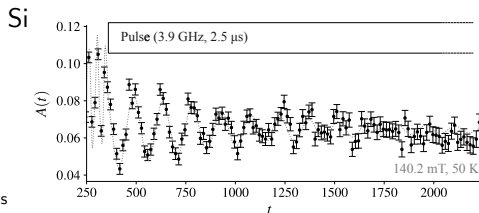


probe

weak coupling + anisotropy

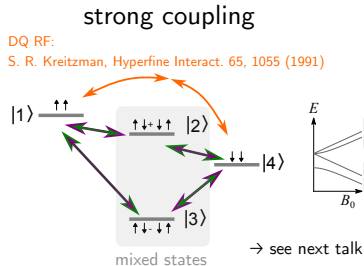


$t_{\pi} \approx 70$  ns

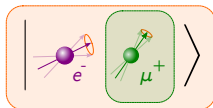


see also Doll *et al.*, PRR 7, 033059, 2025

# Detectable microwave transitions

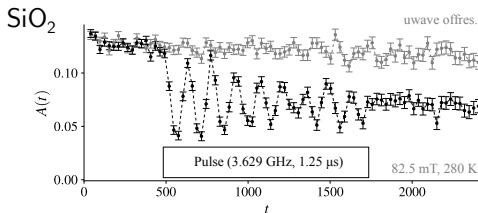
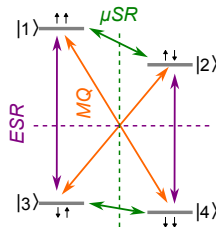


pump

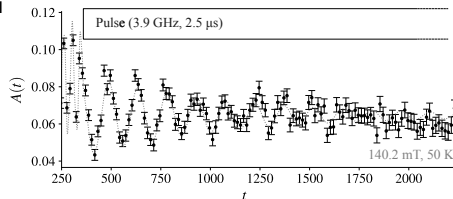


probe

weak coupling + anisotropy

 $t_\pi \approx 70$  ns

Si

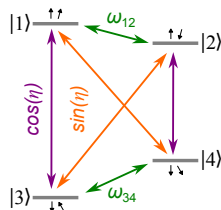
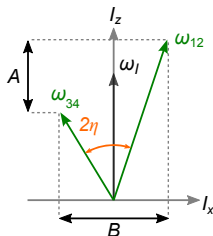
see also Doll *et al.*, PRR 7, 033059, 2025

# State mixing by dipolar coupling

$$\hat{\mathcal{H}}_0 = \underbrace{\omega_S \cdot \hat{S}_z + \omega_I \cdot \hat{I}_z + A \cdot \hat{S}_z \hat{I}_z}_{\text{diagonal}} + \underbrace{B \cdot \hat{S}_z \hat{I}_x}_{\text{mixing}}$$

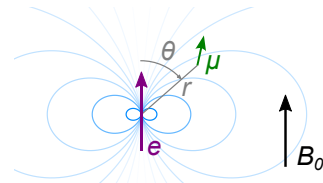
$S = 1/2$  and high-field limit  
 $I = 1/2$  (not in high-field limit)

many more routes to state mixing  
 for  $S > 1/2$  or  $I > 1/2$   
 see e.g. Schweiger/Jeschke book

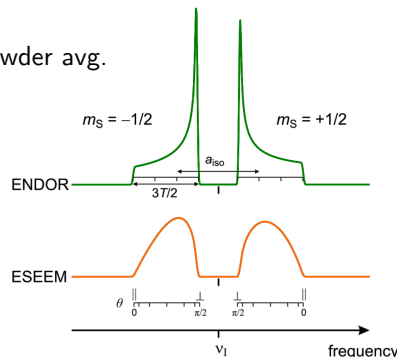


$$A = T \cdot (3 \cos^2(\theta) - 1) + a_{\text{iso}}$$

$$B = 3T \sin(\theta) \cos(\theta) \rightarrow \eta \neq 0$$

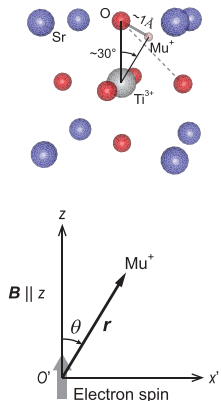


powder avg.



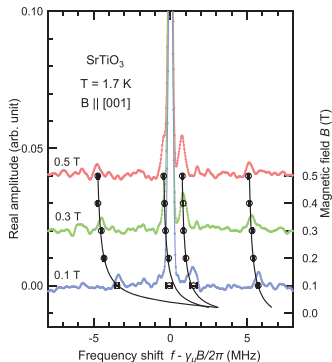
# MQ-μSR on SrTiO<sub>3</sub>

crystal: TF



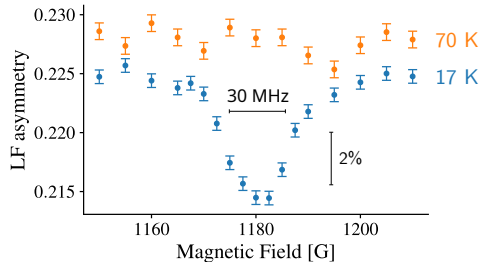
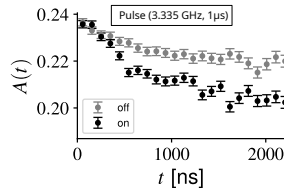
Salman et al., PRL 113, 156801 (2014)

Ito et al., APL 115, 192103 (2019)



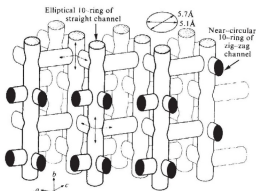
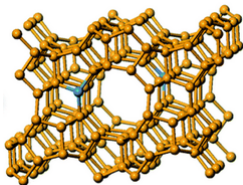
$T = 15 \text{ MHz (dip coup)}$

powder: MQ

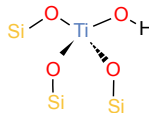


# Titanium silicalite-1

## Zeolite



## Active site



$$g_{\perp} \approx 1.93$$

$$g_{\parallel} \approx 1.99$$

Morra et al.,  
Chem. Eur. J. 20 (2014)

## Input

hydrogen  
peroxide



propylene



## Output

water



propylene oxide



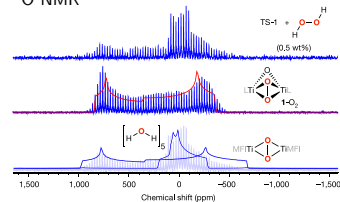
## Product

polyurethane  
(PU foams and more)



TS-1

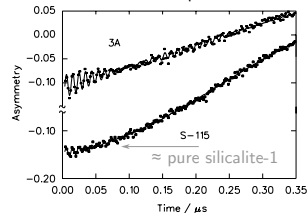
## $^{17}\text{O}$ NMR



Gordon et al., Nature 586, 708-713 (2020)

→ active site is dinuclear !

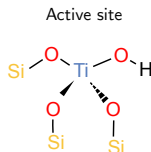
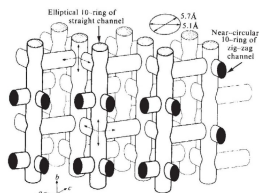
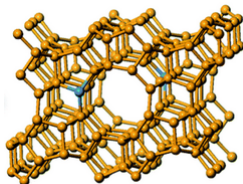
## Zeolite TF μSR



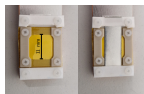
Arsenau et al., Phys. B: Condens. Matter 326, 2003

# MQ-μSR on TS-1

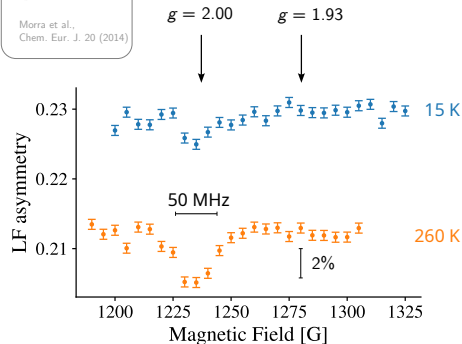
## Zeolite



Sealed flypast cell



$g_{\perp} \approx 1.93$   
 $g_{\parallel} \approx 1.99$   
 Morra et al.,  
 Chem. Eur. J. 20 (2014)



→ electron probably on Si

→ upcoming experiments on  
 silicalite-1 to clarify role of Ti

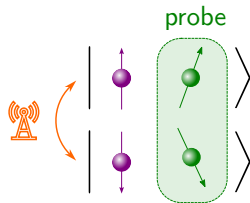
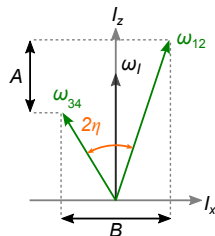
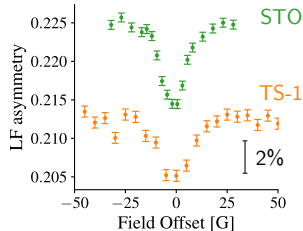
# Summary and Outlook

## • MQ- $\mu$ SR

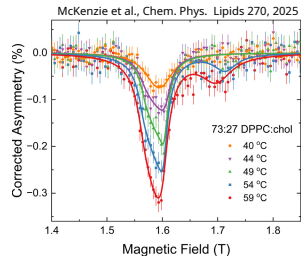
- Selective probe of anisotropic muonium

## • Further work

- 1 How small  $\eta$  are detectable
  - 2 How to extract powder spectra
- Complementarity to ALC
- 3 Increase sensitivity !
- Time integral
  - On/Off contrast
  - HIMB rates

MQ- $\mu$ SR

ALC



## Acknowledgment

- Zaher Salman
- Thomas Hicken
- Thomas Prokscha

Swiss muon source  
(S $\mu$ S)



**PSI**

**Thank you for your  
attention!**