

# Di-Higgs measurements at the HL-LHC and future colliders

Physics Potential of Future Colliders workshop, Sep 18-20 2024

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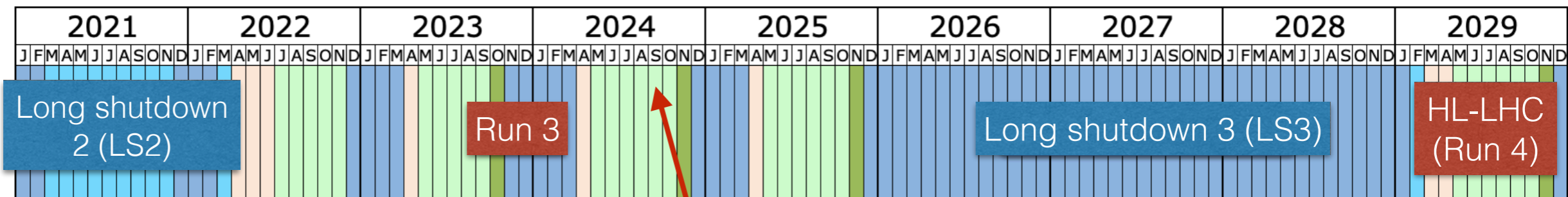




# Introduction

## Di-Higgs and High Luminosity LHC (HL-LHC)

- Already seen in previous talks the **importance of Higgs physics** at future particle colliders.
- What will I try to do here?
  - **Focus on di-Higgs (HH) production**, in particular **at the HL-LHC** expected to start in 2029.
  - HL-LHC: upgrade of the LHC that will increase the collider luminosity by at least a factor of 5.
    - This will bring **more data but also unprecedented detector challenges** due to the high number of simultaneous pp collisions ( $\langle \mu \rangle = 200$ ).
- Some questions I will try to answer:
  - Why are future HH measurements crucial?
  - What can be achieved with the HL-LHC dataset? And after this?
  - What are the limitations for the future?



We are here!

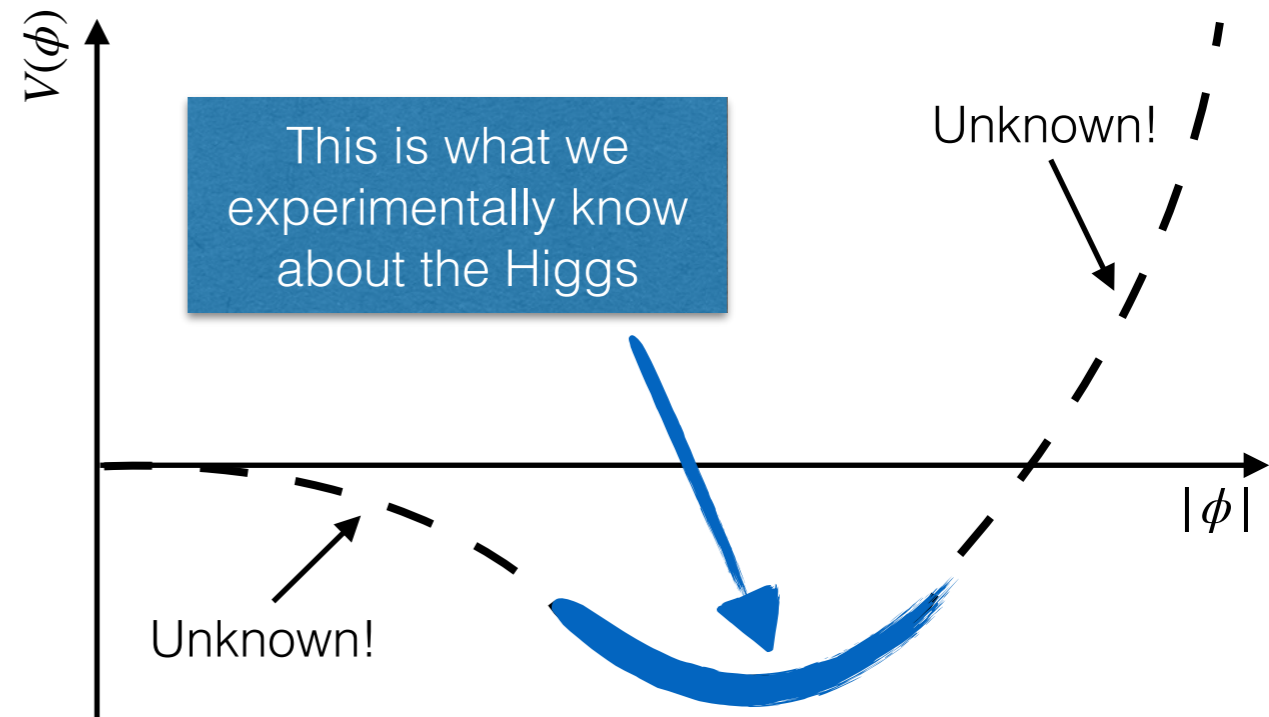
**Why are HH  
measurements  
interesting?**



# The Higgs potential

What is still unknown?

- In the Standard Model, Higgs potential represented by:  
$$V(\phi^\dagger\phi) = -\mu^2\phi^\dagger\phi + \lambda(\phi^\dagger\phi)^2$$
- So far, we only **established where the minimum of the Higgs potential is.**



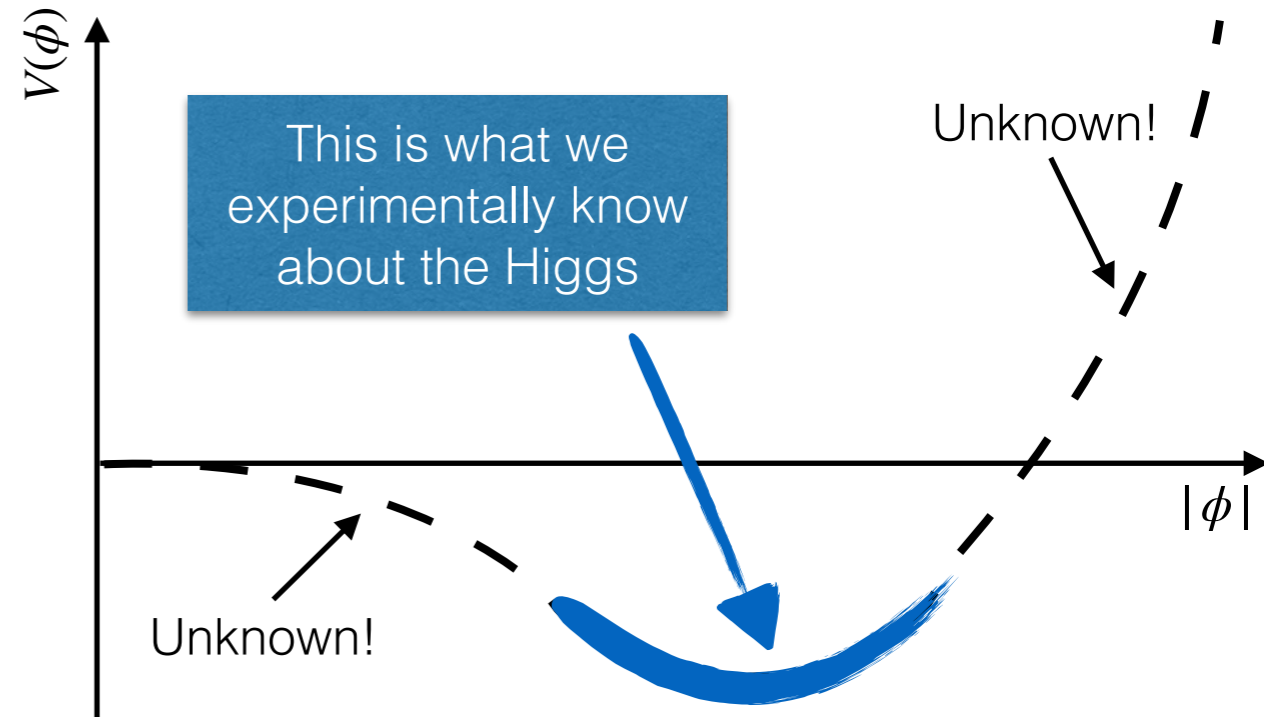


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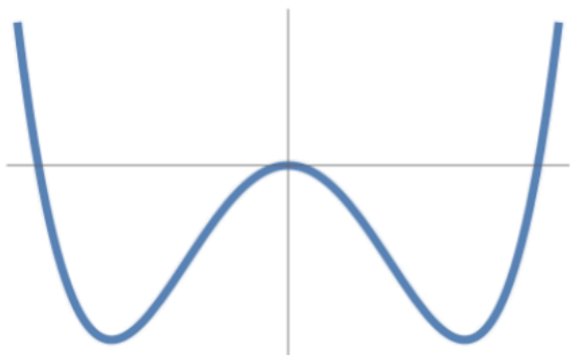
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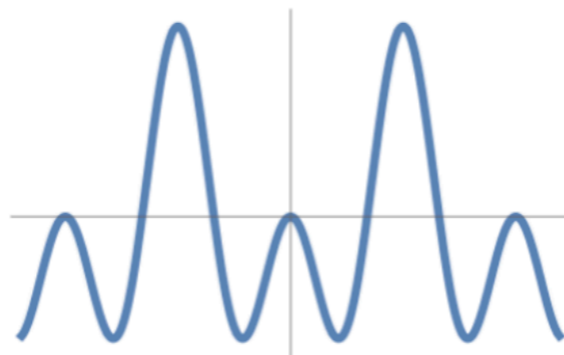
**Different potential shapes could explain the same physics we see now!**

[arxiv:1907.02078](https://arxiv.org/abs/1907.02078)

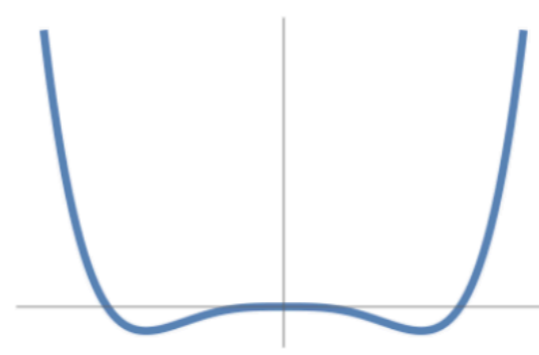
$$V(H) \simeq \begin{cases} -m^2 H^\dagger H + \lambda (H^\dagger H)^2 + \frac{c_6 \lambda}{\Lambda^2} (H^\dagger H)^3, & \text{Elementary Higgs} \\ -a \sin^2(\sqrt{H^\dagger H}/f) + b \sin^4(\sqrt{H^\dagger H}/f), & \text{Nambu-Goldstone Higgs} \\ \lambda (H^\dagger H)^2 + \epsilon (H^\dagger H)^2 \log \frac{H^\dagger H}{\mu^2}, & \text{Coleman-Weinberg Higgs} \\ -\kappa^3 \sqrt{H^\dagger H} + m^2 H^\dagger H, & \text{Tadpole-induced Higgs} \end{cases}$$



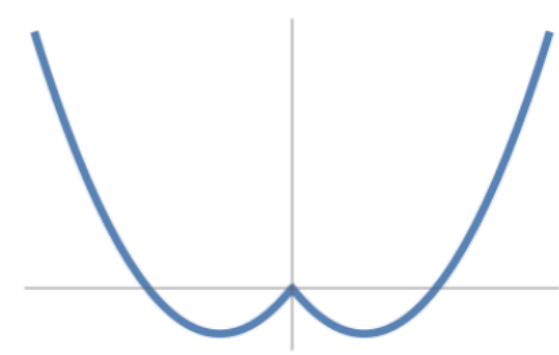
Landau-Ginzburg Higgs



Nambu-Goldstone Higgs



Coleman-Weinberg Higgs



Tadpole-Induced Higgs<sup>4</sup>

# How to measure the Higgs potential?

Multiple-Higgs events

We need to access the  $\lambda$  parameter of the Higgs potential.

$$V(h) = -\mu^2 |\phi|^2 + \lambda |\phi|^4 \simeq \frac{1}{2} m_h^2 h^2 + \lambda v h^3 + \frac{1}{4} \lambda h^4 + \dots$$



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Tells us where the minimum of the potential is  
 $\Rightarrow m_H = \sqrt{2\lambda} v \approx 125 \text{ GeV}$  means  $\lambda_{SM} \approx 0.13$





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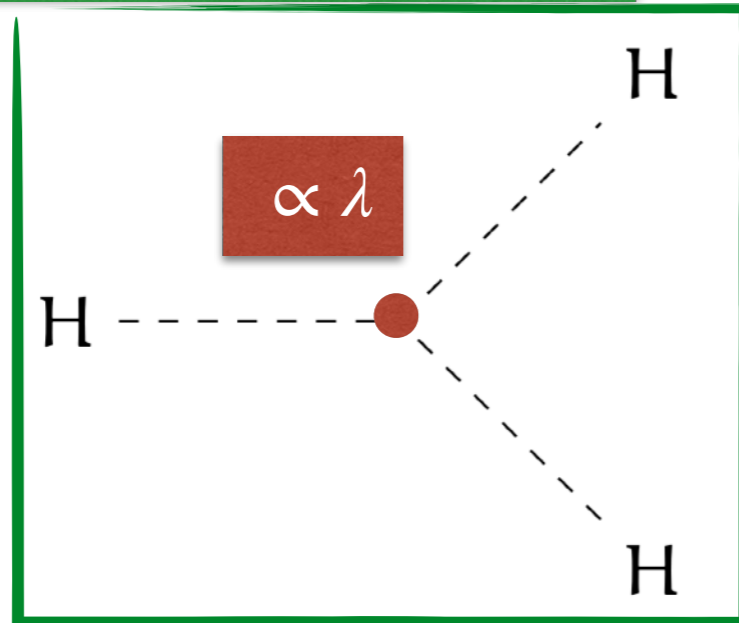
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Trilinear Higgs self-coupling



Access to  $\lambda$  through **3-Higgs interactions**. Possible to access for the first time at HL-LHC

We generally look more at  $\kappa_\lambda$  rather than  $\lambda$  directly

$$\kappa_\lambda \equiv \frac{\lambda}{\lambda_{SM}}$$





# How to measure the Higgs potential?

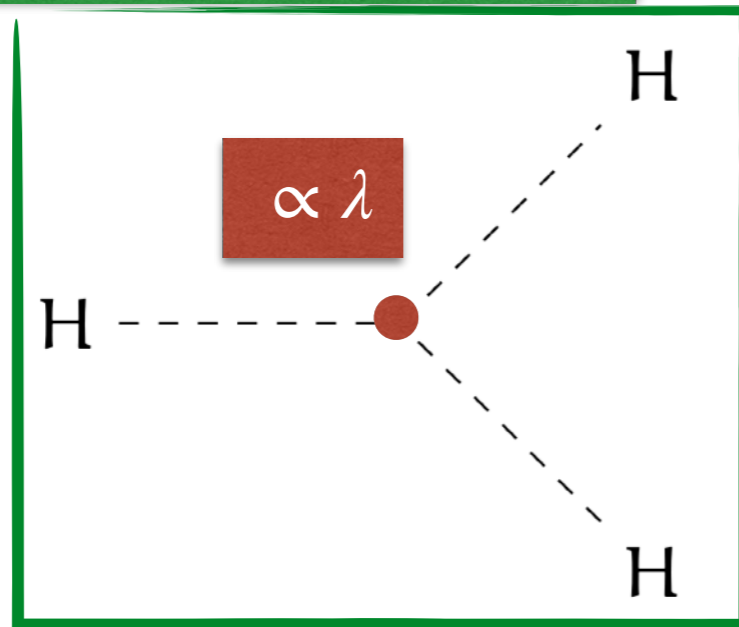
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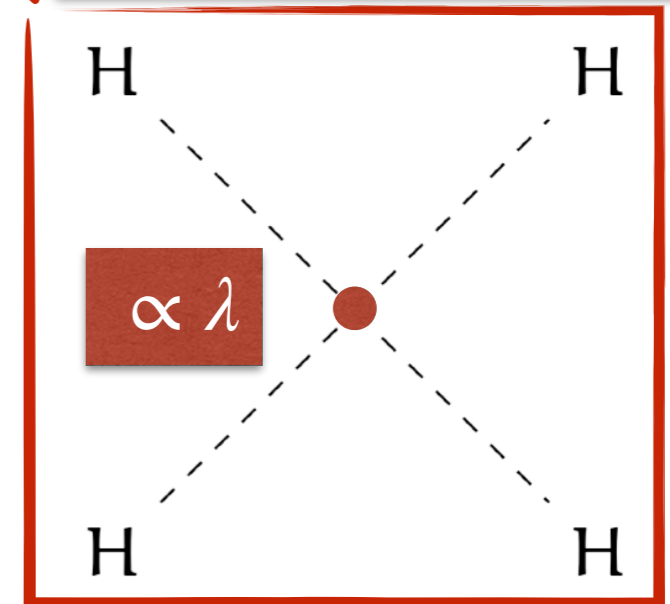
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Trilinear Higgs self-coupling



Access to  $\lambda$  through **3-Higgs interactions**. Possible to access for the first time at HL-LHC

Quadrilinear Higgs self-coupling



Out of the reach of HL-LHC and most of the future collider scenarios.

We generally look more at  $\kappa_\lambda$  rather than  $\lambda$  directly

$$\kappa_\lambda \equiv \frac{\lambda}{\lambda_{SM}}$$



# HH production at the HL-LHC

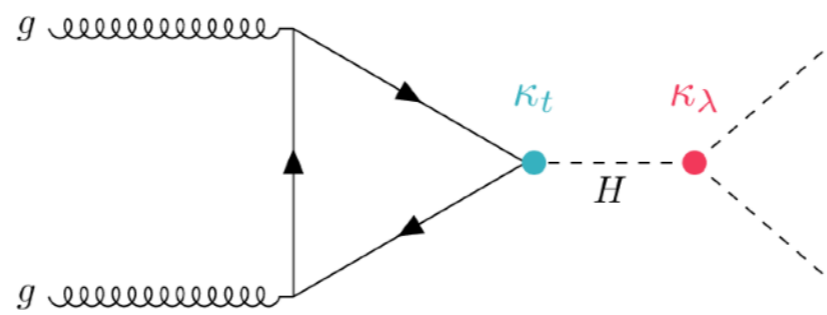
Non-resonant HH production

## Gluon-gluon fusion (ggF)

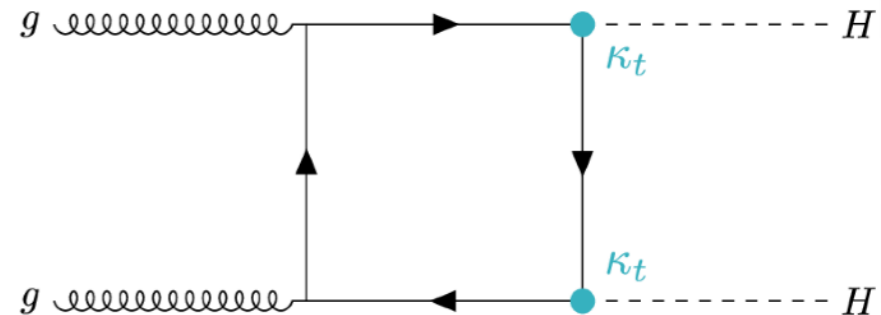
- Destructive interference leads to small cross-section:

$$\sigma_{ggF} = 36.4 \text{ fb}$$

Triangle diagram



Box diagram

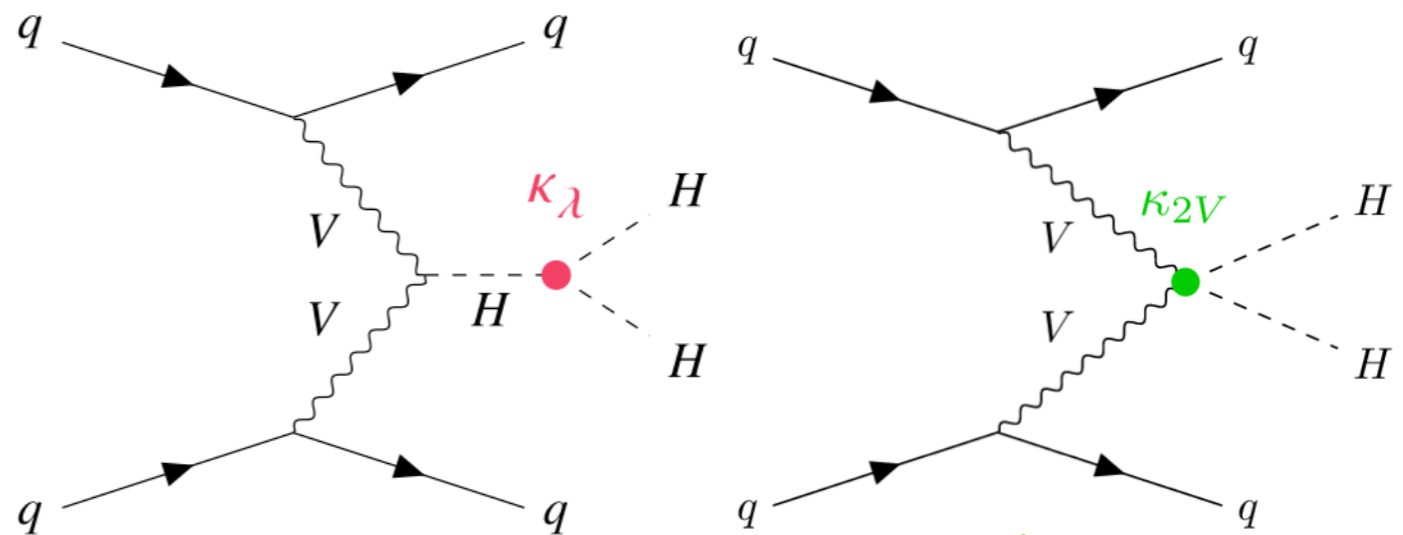


1 HH event every 1000 single-H events!

## Vector-boson fusion (VBF)

- Signature: 2 Higgs + 2 quarks close to the LHC proton beams.
- Access to  $\kappa_\lambda$ , but also to **VVHH process** (never measured!) which could provide test of **SM unitarity** via measurement of  $k_{2V}$ .

- Very tiny** cross-section:  
 $\sigma_{VBF} = 2.0 \text{ fb}$



$$\kappa_{2V} \equiv \frac{c_{2V}}{c_{2V}^{SM}}$$

**What have we  
achieved so far?**

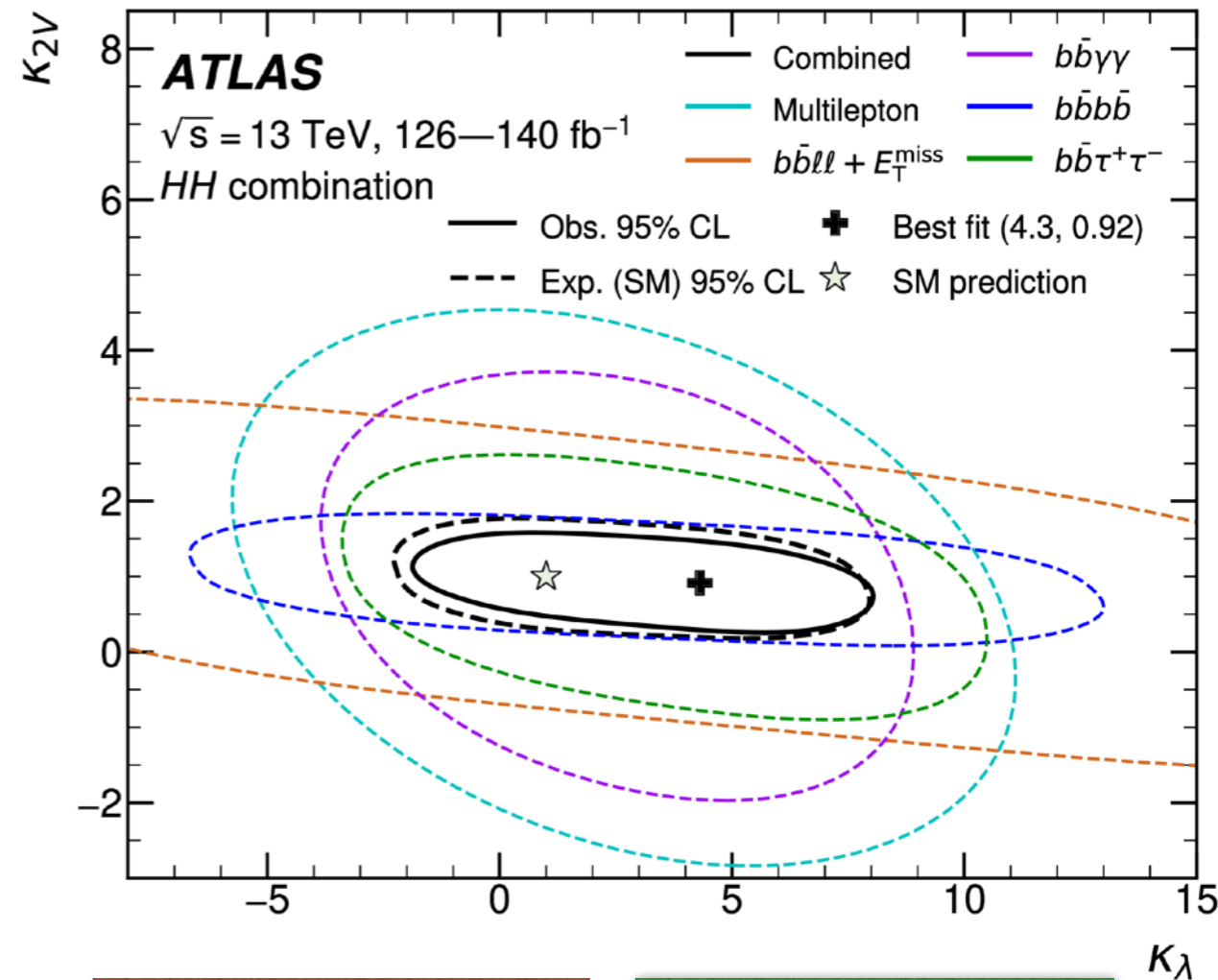
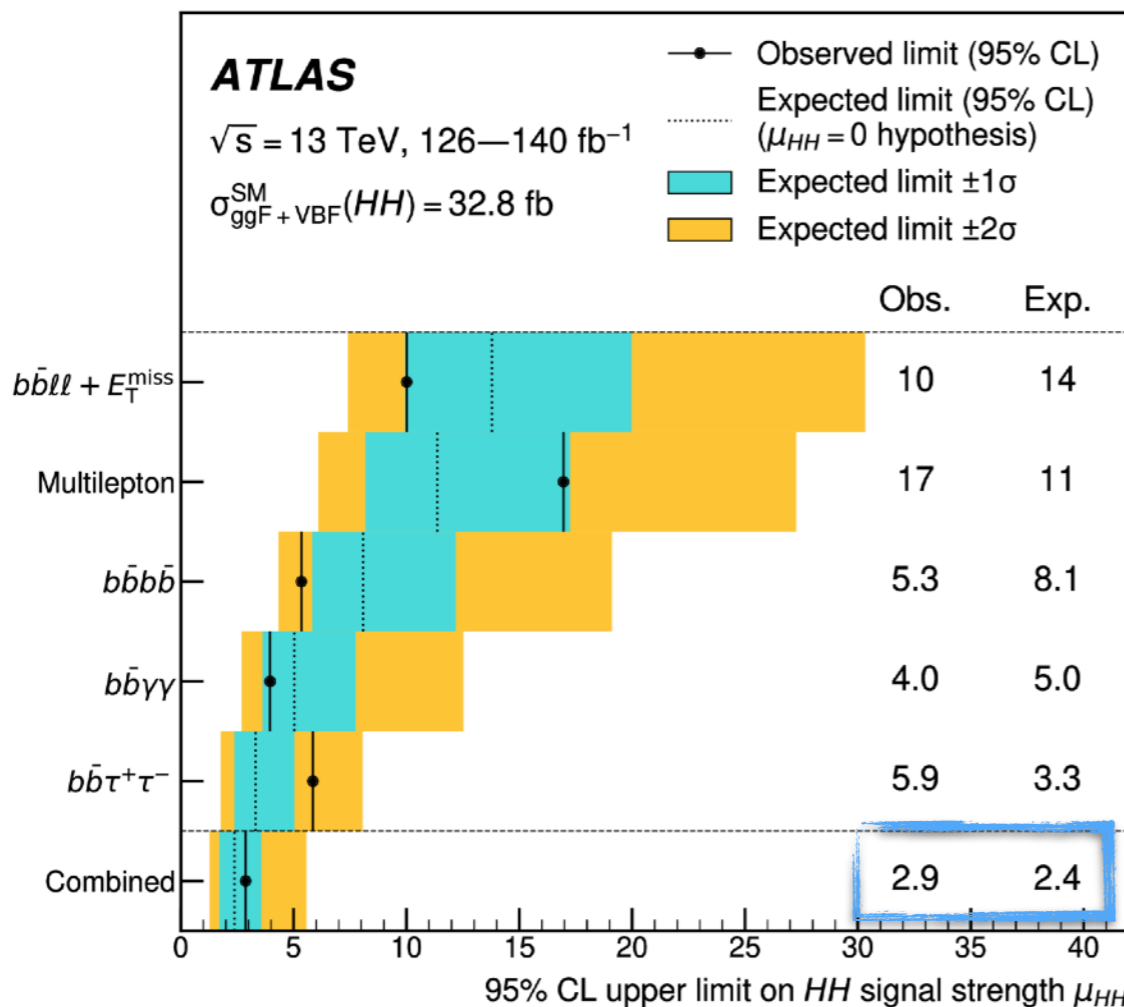


# Latest ATLAS Run 2 results

SM signal strength 95% CL upper limits

- **No signal observed**, but we are **getting very close!** Maximal sensitivity is obtained through combination of different HH decay channels.
  - Observed 95% CL upper limit is  $2.9 \times \sigma_{HH}(SM)$ !
  - **SM hypothesis**  $(\kappa_\lambda, \kappa_{2V}) = (1.0, 1.0)$  **still compatible with observation at 95% CL.**
  - CMS has very similar numbers 😊
- **Dominant uncertainty: statistical! Adding more data will help a lot!**

Phys. Rev. Lett. 133 (2024) 101801



4.0x better than  $36 \text{ fb}^{-1}$  combination

$\kappa_\lambda \in [-1.2, 7.2]$

$\kappa_{2V} \in [0.6, 1.5]$

**What can we achieve  
at the HL-LHC?**

# Di-Higgs at the HL-LHC

Some caveats...

- This is a nice question, but **it is not so simple to answer.** 😊

Can certainly extrapolate the previous Run 2 results with HL-LHC luminosity ( $3000 \text{ fb}^{-1}$ )

- However, many important questions remain:
  - When are we going to hit the **systematics wall**?
  - Can we reduce systematics** in the next years? **By how much?**
  - How much are the detector upgrades going to improve performance?
- ATLAS and CMS will need to be upgraded** to cope with **large radiation doses, high data flows, and challenging reconstruction conditions** (200 simultaneous pp collisions).

|                         | ATLAS upgrades   | CMS upgrades  |
|-------------------------|--|---|
| <b>Inner detector</b>   | <b>Brand new</b> and fully made of silicon!  |   |
| <b>Timing detectors</b> | <b>Yes!</b> Forward region only ( $2.4 <  \eta  < 4.0$ )                                 | <b>Yes!</b> Full eta coverage.  |
| <b>Calorimeter</b>      | <b>New readout</b> electronics   | <b>New readout</b> electronics. <b>New end-cap calorimeter</b> (5D shower reconstruction) |
| <b>Trigger</b>          | Brand new! L1/HLT output rates: <b>1MHz/10kHz</b>  | Brand new! L1/HLT output rates: <b>650kHz/7.5kHz</b>                                      |
| <b>Muon chambers</b>    | New Small Wheel (installed), upgraded barrel RPCs, new TGC chambers, new MDT electronics | <b>Extend eta gaps and increase redundancy</b> with new technologies                      |



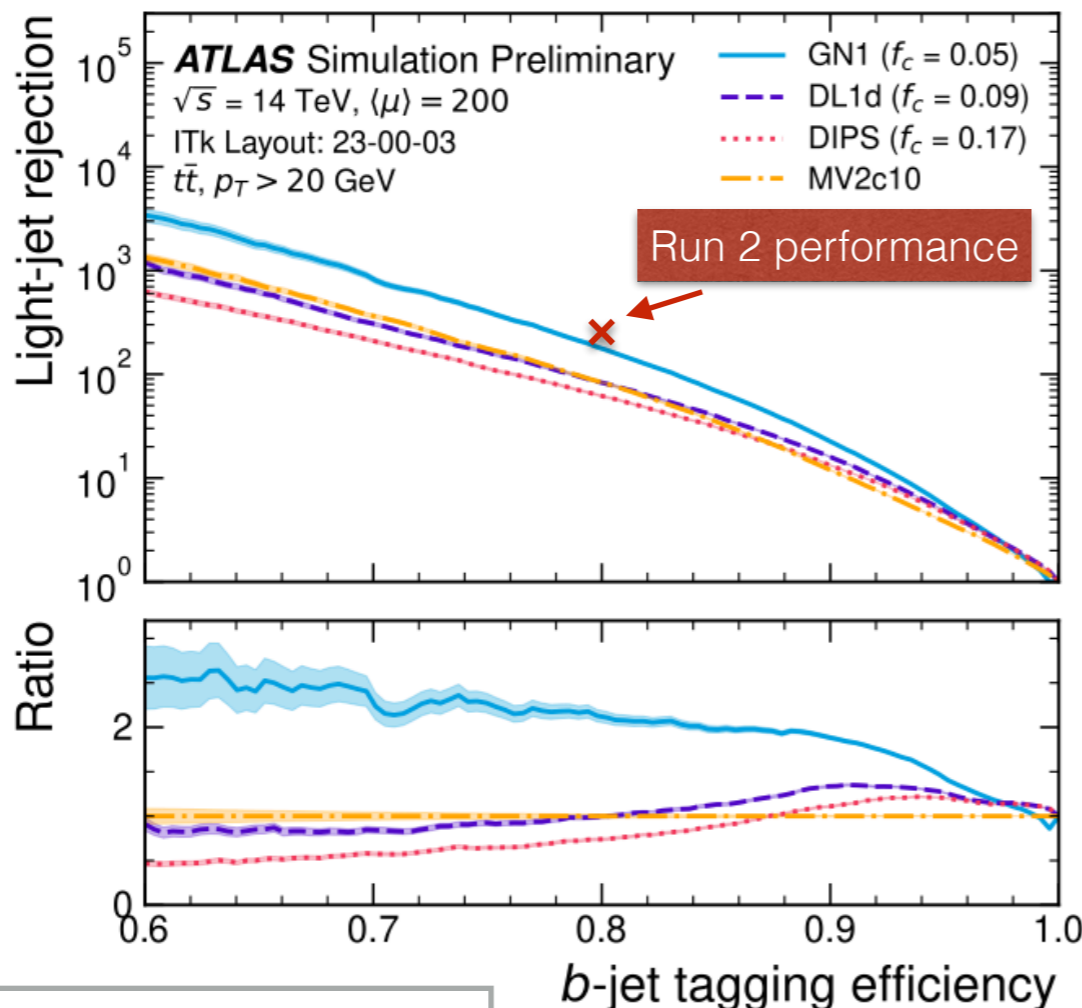


# HL-LHC reconstruction performance

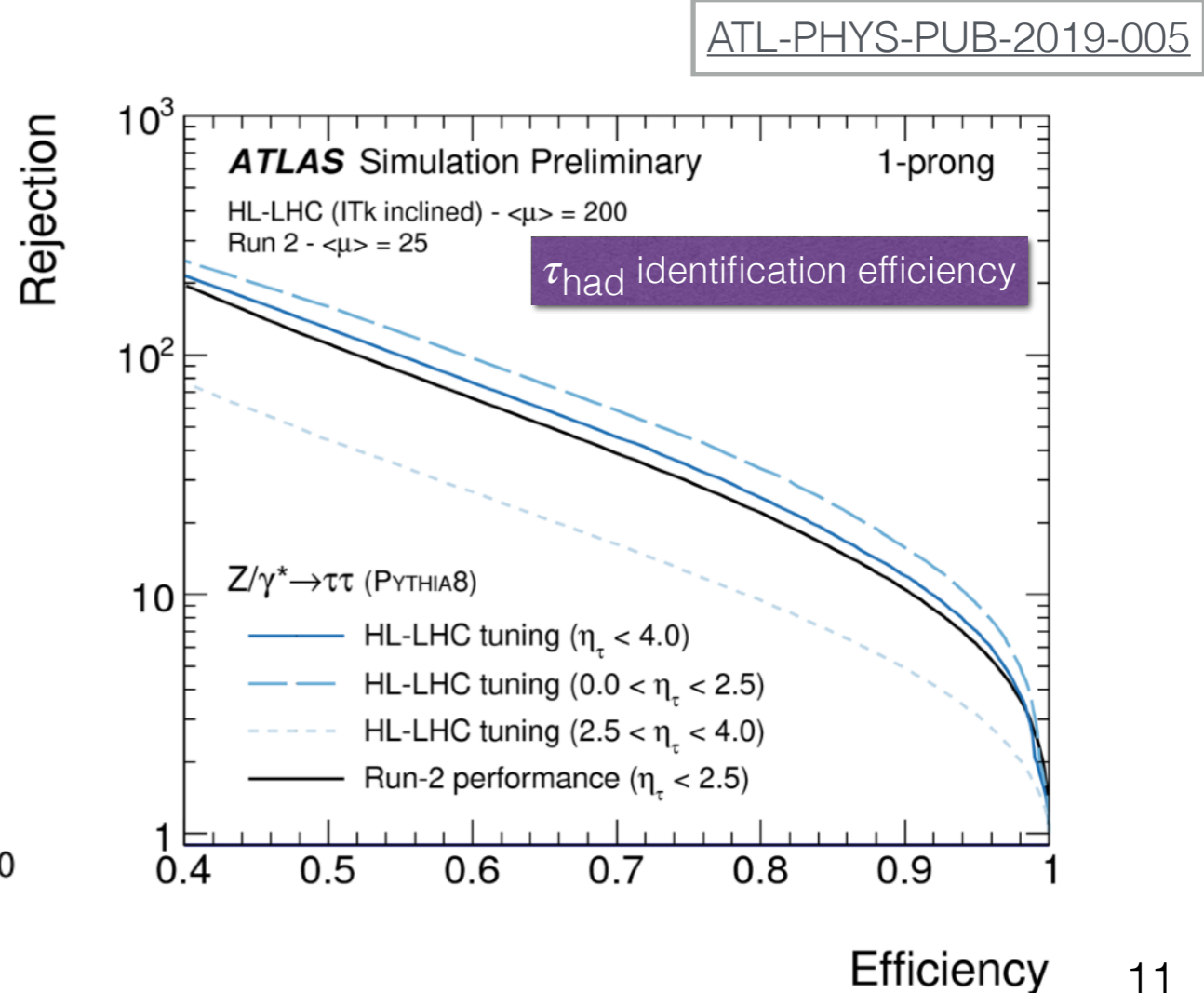
Are detector upgrades enough to cope with the higher pileup conditions?

- For HH, crucial point is the **reconstruction performance of b-jets,  $\tau_{\text{had}}$ , photons, and leptons** ( $e$  and  $\mu$ ).
- Current HL-LHC simulations show **comparable (or better) reconstruction performance** between Run 2 and HL-LHC thanks to upgraded detectors!

An extrapolation from Run 2 analyses should give a realistic idea of the expected H-LHC sensitivity for HH!



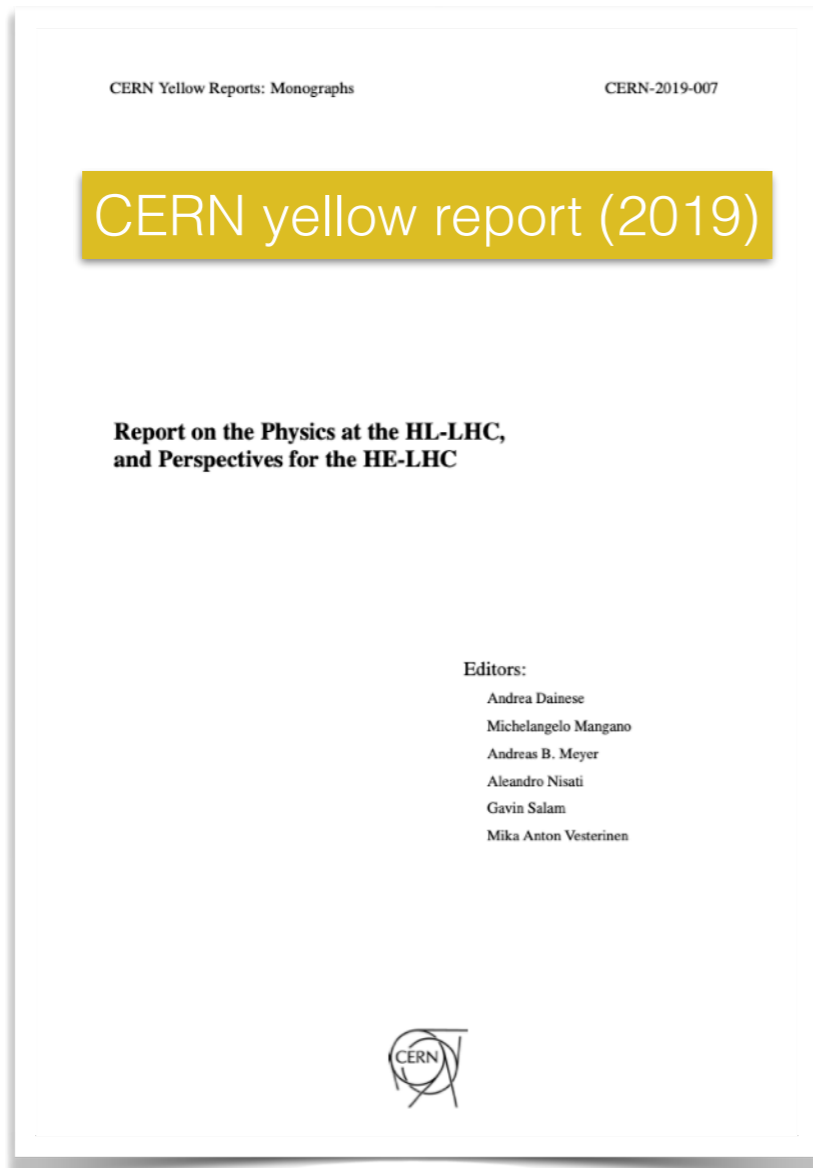
ATL-PHYS-PUB-2022-047



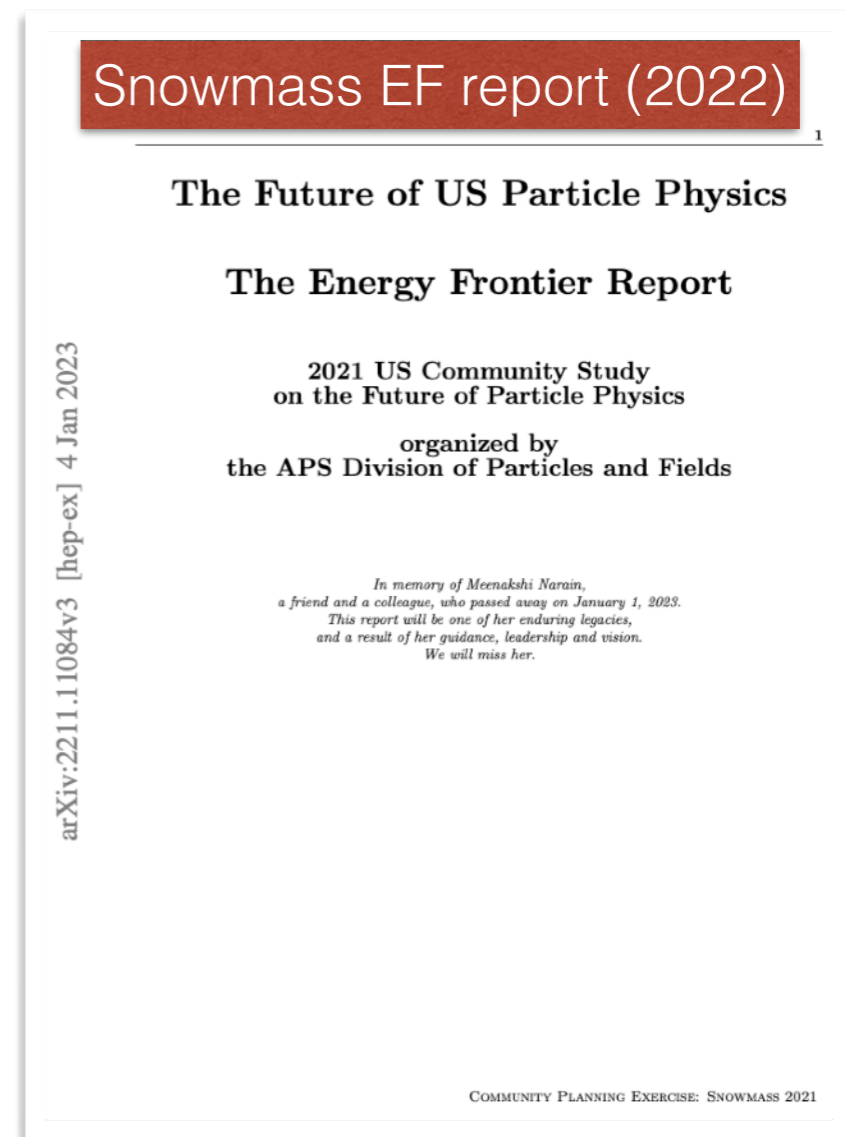
Efficiency

# A history of Run 2 extrapolations

- A little bit of history:
  - Projections for **CERN Yellow-Report (2019)**: based on **partial Run 2 analyses** ( $36 \text{ fb}^{-1}$ )
  - **Snowmass process (2021)**: based on **first round of complete Run 2 analyses** ( $139 \text{ fb}^{-1}$ ).
  - European Strategy update for particle physics: soon in 2025!



[arXiv:1902.10229](https://arxiv.org/abs/1902.10229)



[arXiv:2211.11084](https://arxiv.org/abs/2211.11084)







# ATLAS + CMS projections (2019)

A simple extrapolation...

- CERN Yellow Report extrapolation **based of partial Run 2 ATLAS and CMS results** ( $36 \text{ fb}^{-1}$ ) with expected reduction systematic uncertainties.
  - **Combined significance:  $4.0\sigma$  ( $4.5\sigma$ )** with and without systematic uncertainties.
    - Scenario without systematics give best possible case.
  - **Precision on  $\kappa_\lambda$  modifier:  $\sim 50\%$**

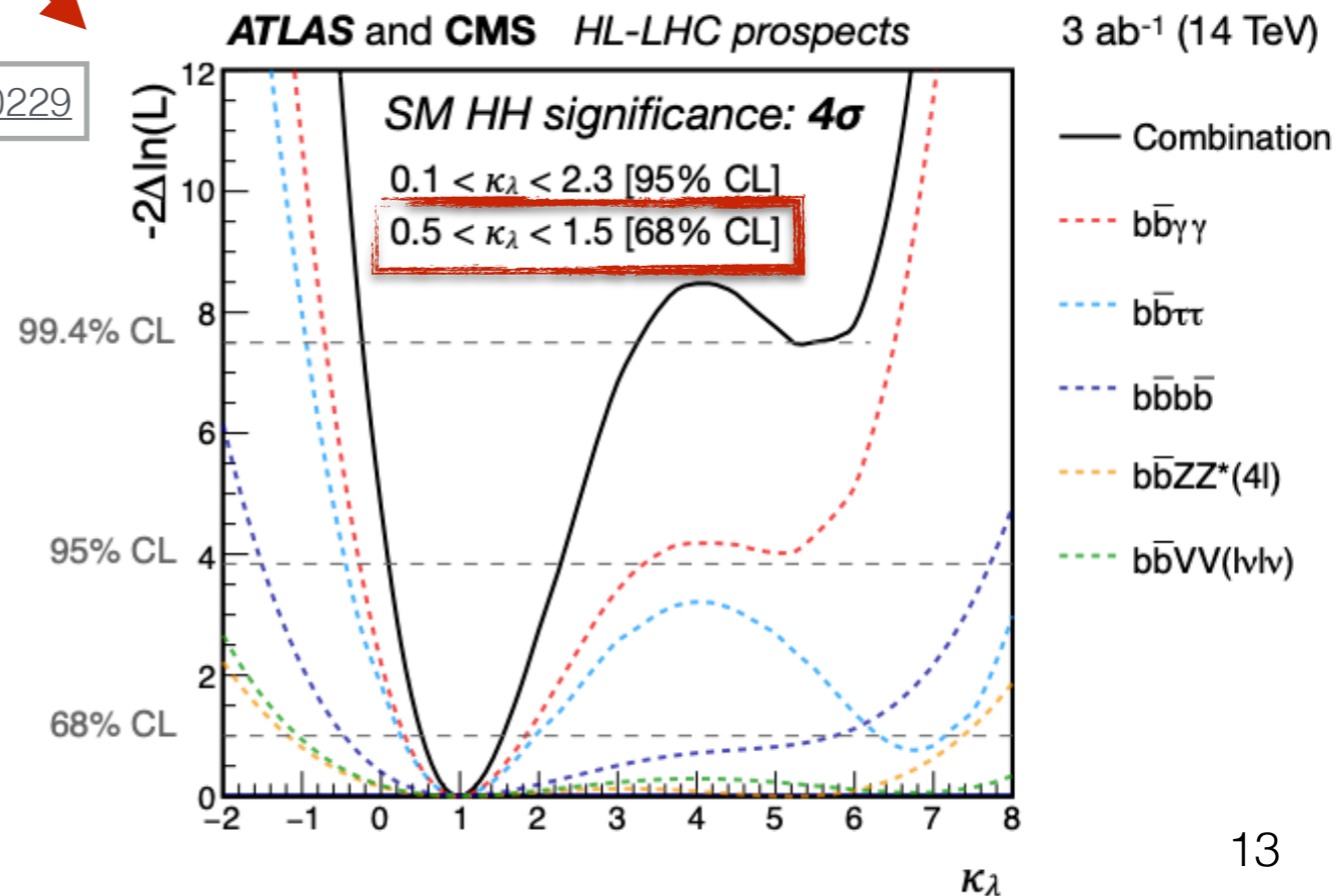
$$Z_{\text{comb}} = \sqrt{\sum_{\text{analysis}} Z_a^2}$$

arXiv:1902.10229

$$\mathcal{L}_{\text{comb}} = \prod_{\text{analysis}} \mathcal{L}_a \quad \rightarrow \quad \log(\mathcal{L}_{\text{comb}}) = \sum_{\text{analysis}} \log(\mathcal{L}_a)$$

|                                       | Statistical-only |      | Statistical + Systematic |      |
|---------------------------------------|------------------|------|--------------------------|------|
|                                       | ATLAS            | CMS  | ATLAS                    | CMS  |
| $HH \rightarrow b\bar{b}b\bar{b}$     | 1.4              | 1.2  | 0.61                     | 0.95 |
| $HH \rightarrow b\bar{b}\tau\tau$     | 2.5              | 1.6  | 2.1                      | 1.4  |
| $HH \rightarrow b\bar{b}\gamma\gamma$ | 2.1              | 1.8  | 2.0                      | 1.8  |
| $HH \rightarrow b\bar{b}VV(l\nu\nu)$  | -                | 0.59 | -                        | 0.56 |
| $HH \rightarrow b\bar{b}ZZ(4l)$       | -                | 0.37 | -                        | 0.37 |
| combined                              | 3.5              | 2.8  | 3.0                      | 2.6  |
|                                       | Combined<br>4.5  |      | Combined<br>4.0          |      |

Statistical significance (Z)



**Are these numbers  
still realistic?**

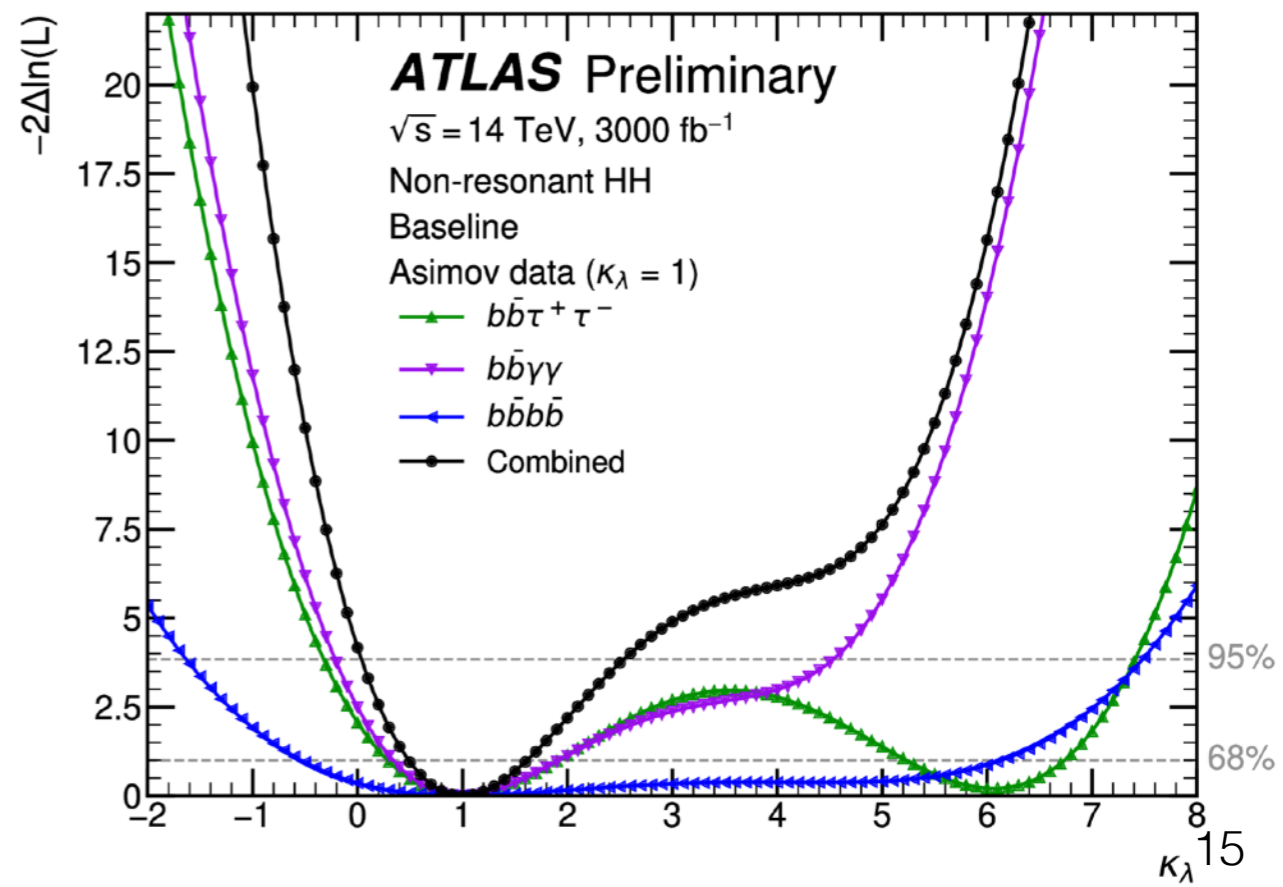
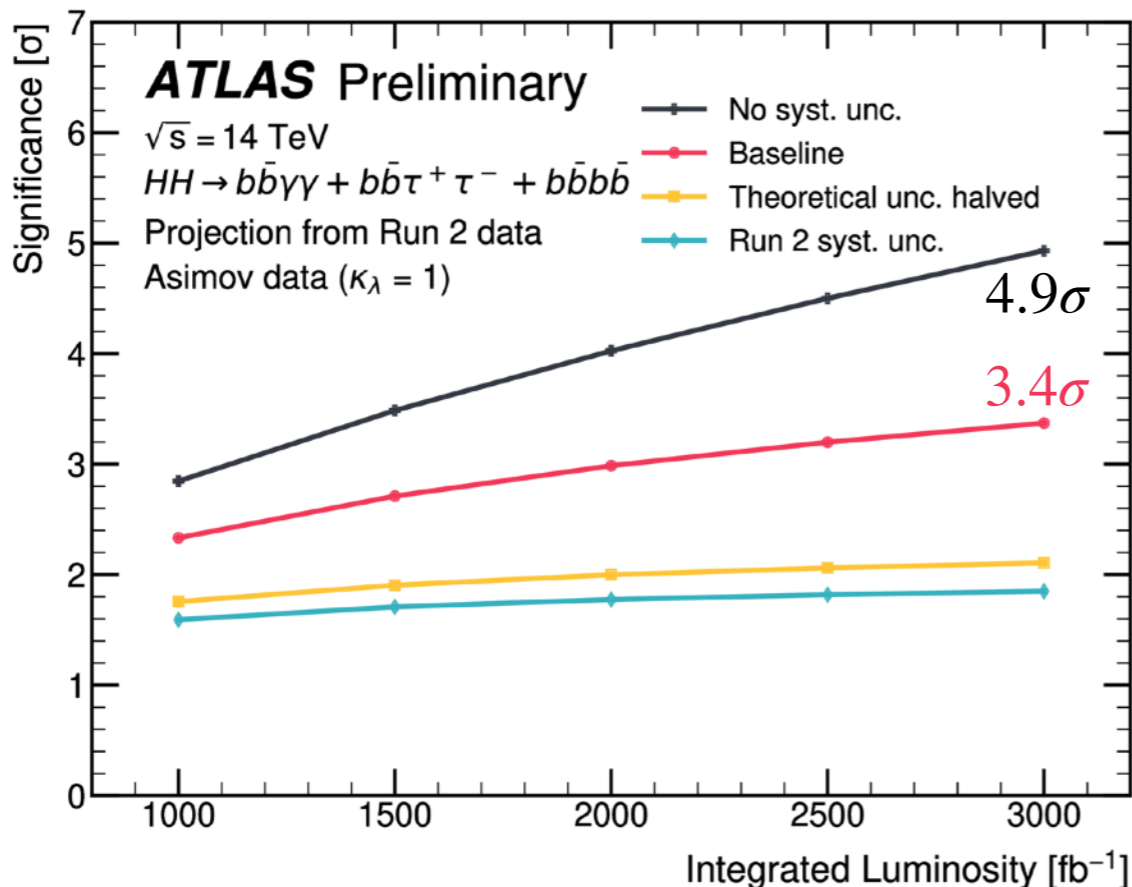


# ATLAS Snowmass projections (2022)

New ATLAS projections

- **Only ATLAS projections were updated** with new Run 2 analyses ( $139 \text{ fb}^{-1}$ )
  - Statistical significance:  $3.4\sigma$  ( $4.9\sigma$ ) with (without) systematic uncertainties.
  - 68% CL  $\kappa_\lambda$  range (with systematics): **[0.5, 1.6]**
- Achieved **almost the same expected sensitivity ATLAS+CMS with ATLAS-only!**
  - Previous CERN Yellow report ATLAS-only  $\kappa_\lambda$  range: [0.25, 1.9]
- **This means that ATLAS+CMS should be much better than  $4.0\sigma$  and 50% precision** on  $\kappa_\lambda$  quoted in many documents. 😊

ATLAS-PHYS-PUB-2022-053





# My personal ATLAS+CMS estimation

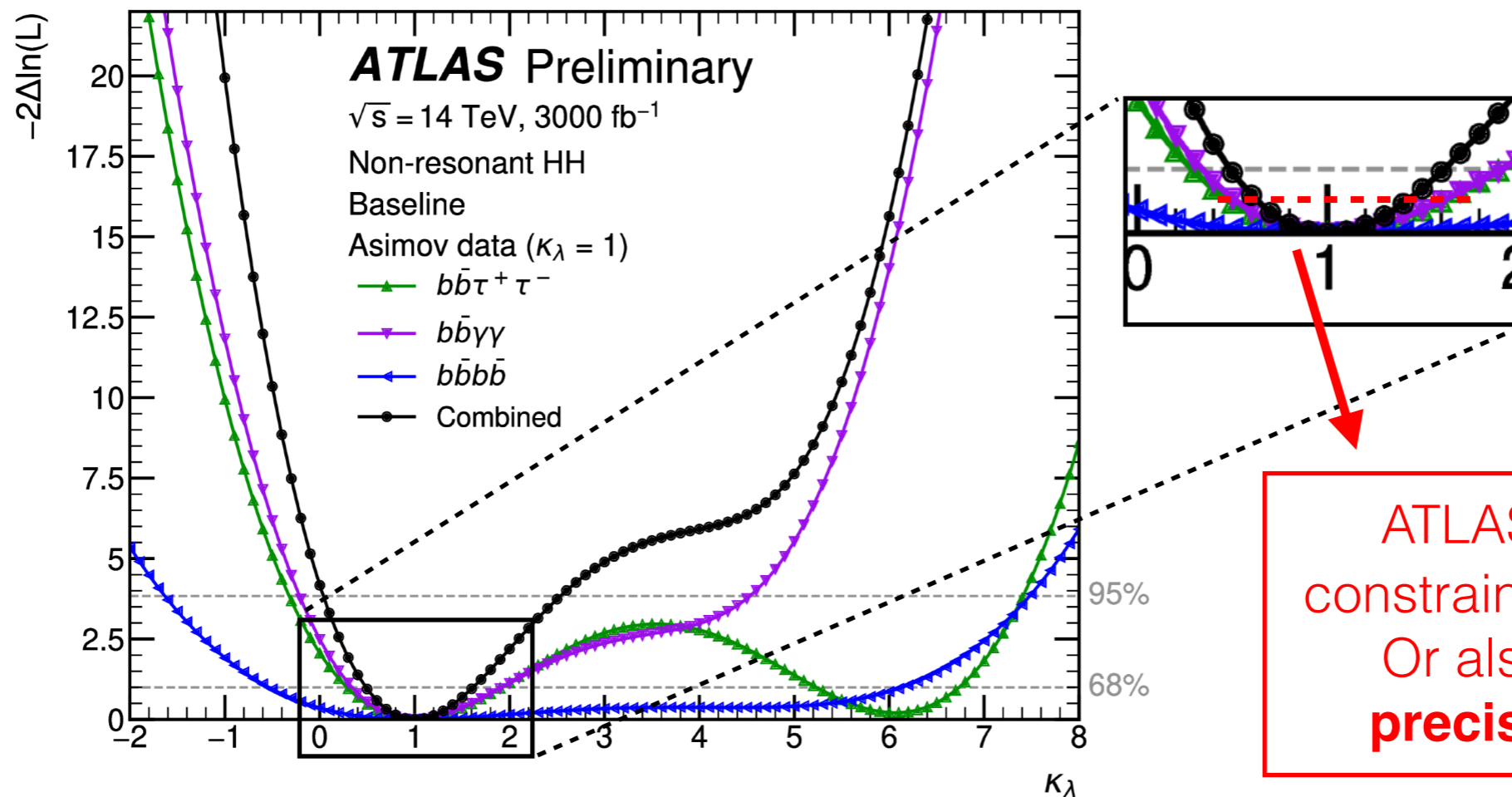
Speculations...

- **Let's assume that ATLAS and CMS will have identical sensitivity** to HH. Not very far from reality if you look at the latest CMS results 😊.
- This means that:

- Significance:  $Z_{\text{ATLAS+CMS}} \approx \sqrt{Z_{\text{ATLAS}}^2 + Z_{\text{ATLAS}}^2} = \sqrt{2} \cdot Z_{\text{ATLAS}}$

$Z_{\text{ATLAS+CMS}} \approx 4.8\sigma$  ( $6.9\sigma$ ) with (without) systematics

- $\kappa_\lambda$  precision:  $\log(\mathcal{L}_{\text{ATLAS+CMS}}) \approx \log_{\text{ATLAS}}(\mathcal{L}) + \log_{\text{ATLAS}}(\mathcal{L}) = 2 \cdot \log_{\text{ATLAS}}(\mathcal{L})$





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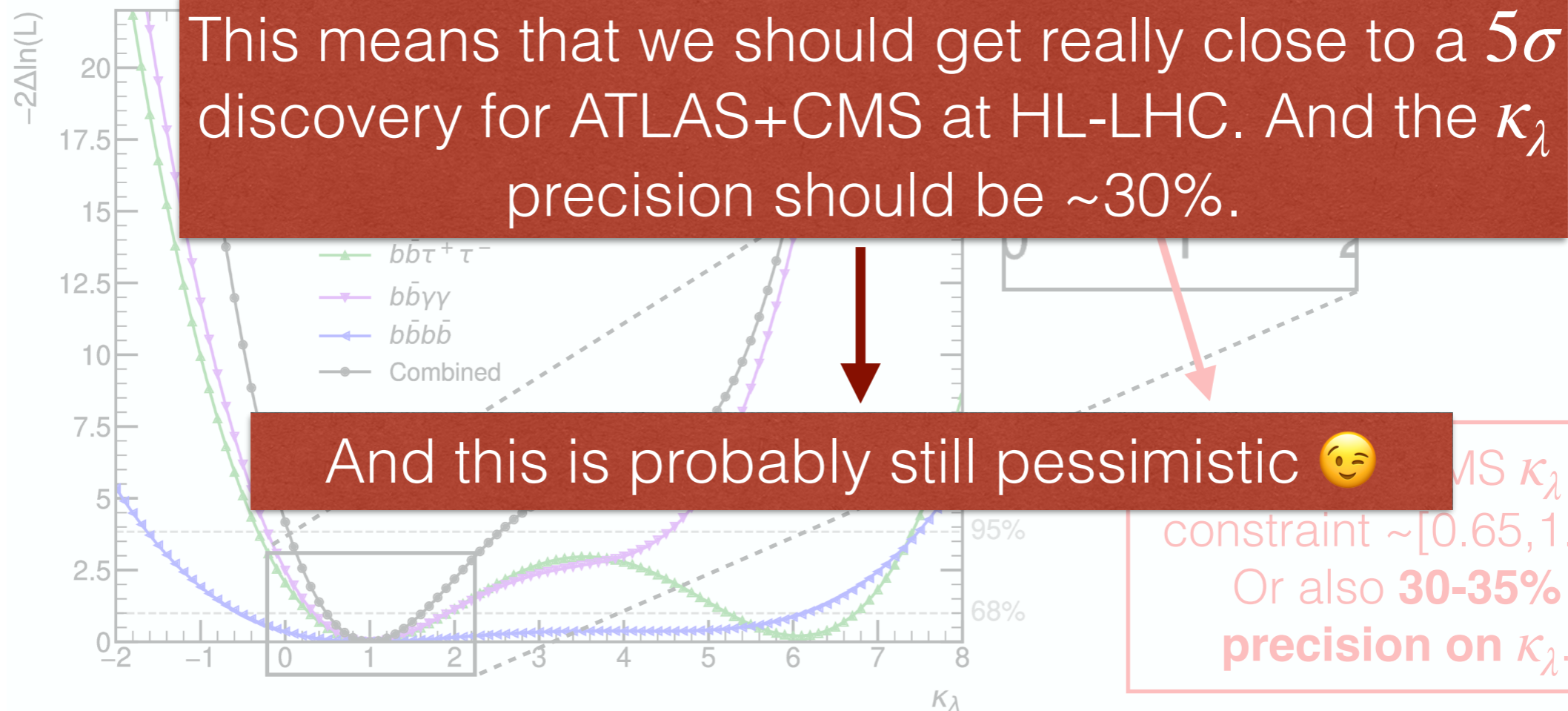
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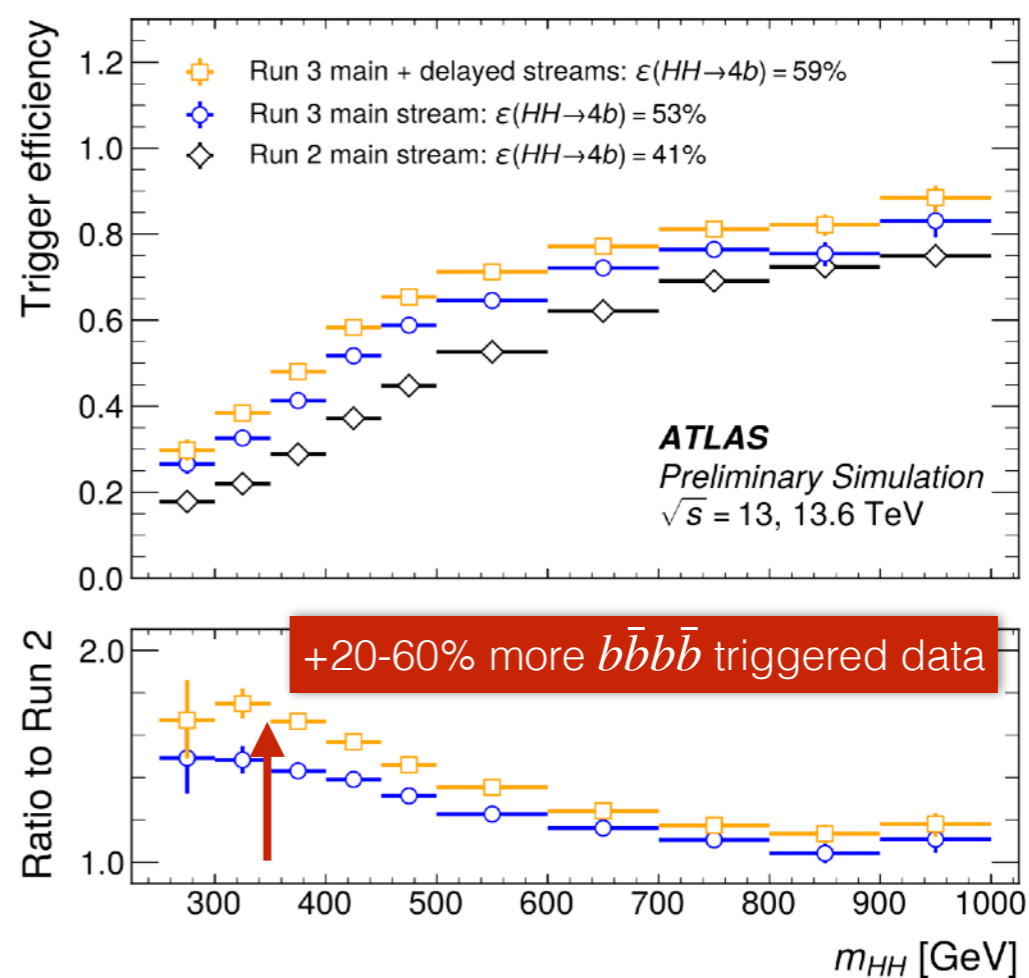
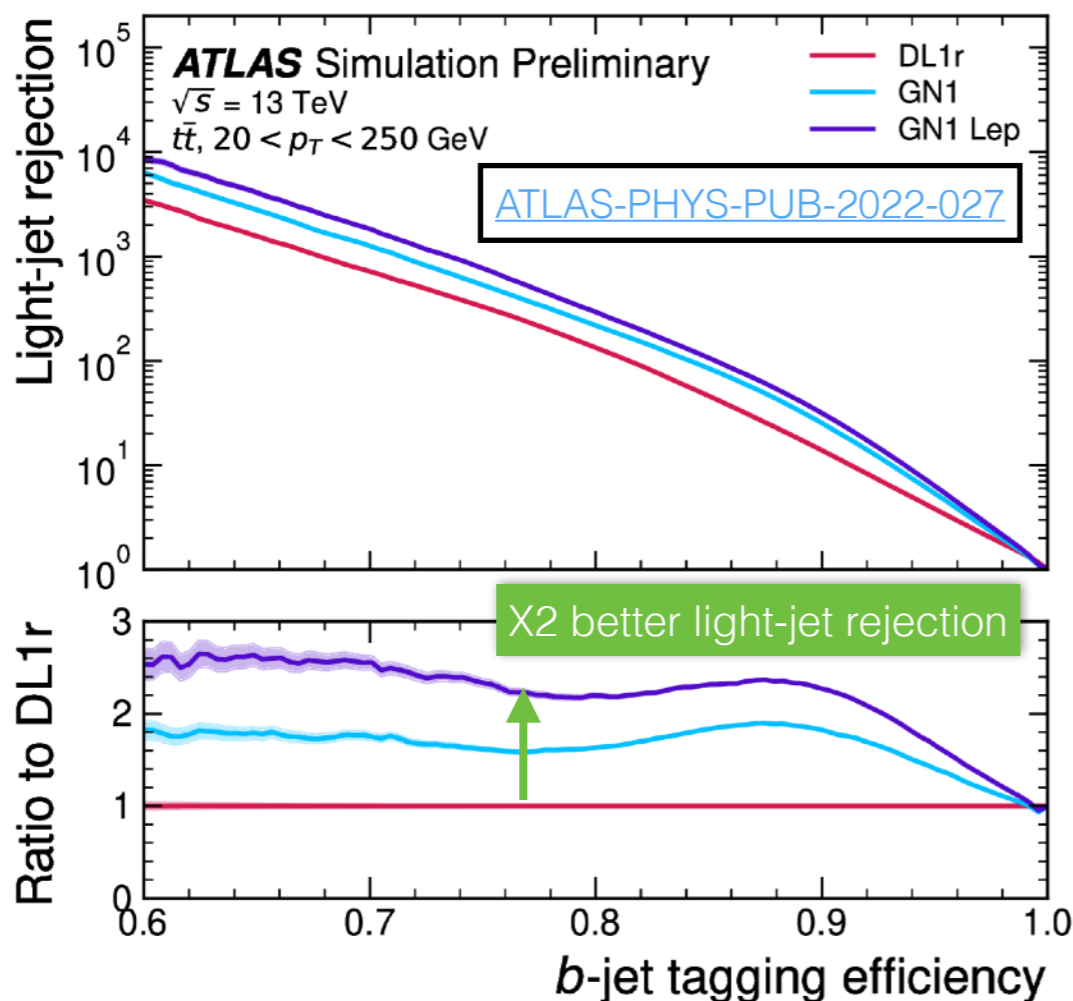
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# Run 3 ATLAS improvements

More data, better reconstruction and triggers

- We **already achieved plenty of improvements in Run 3** for reconstruction and triggers. And these will be all propagated to HL-LHC! 😊
- Some examples:
  - **b-tagging largely improved** with Graph Neural Networks (GN1)!
  - **Triggers significantly improved** (e.g. asymmetric  $HH \rightarrow b\bar{b}b\bar{b}$  triggers)!
- So,  $4.8\sigma$  and 30%  $\kappa_\lambda$  precision is probably still pessimistic (we can do more!)



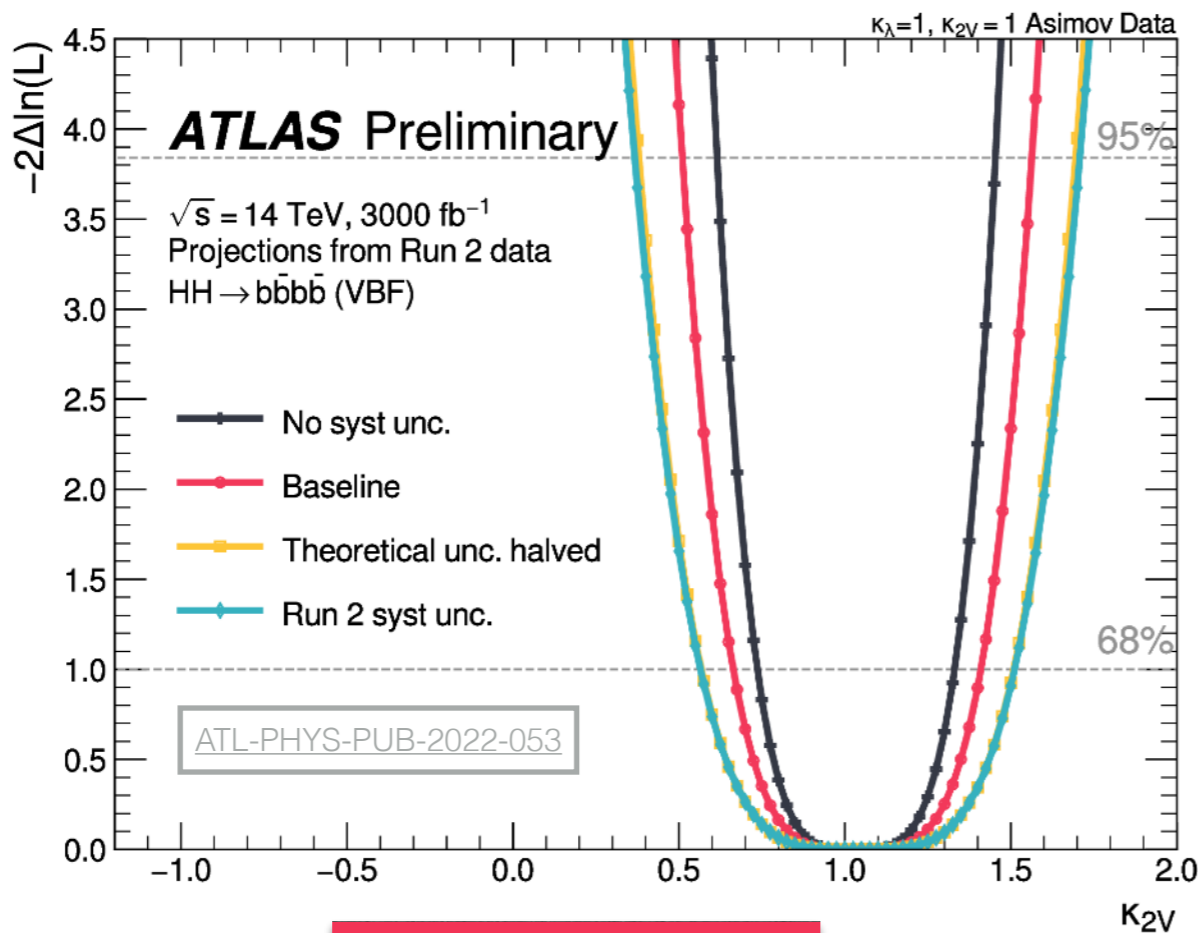


# Boosted VBF $HH \rightarrow b\bar{b}b\bar{b}$ (2024)

$\kappa_{2V}$  limits

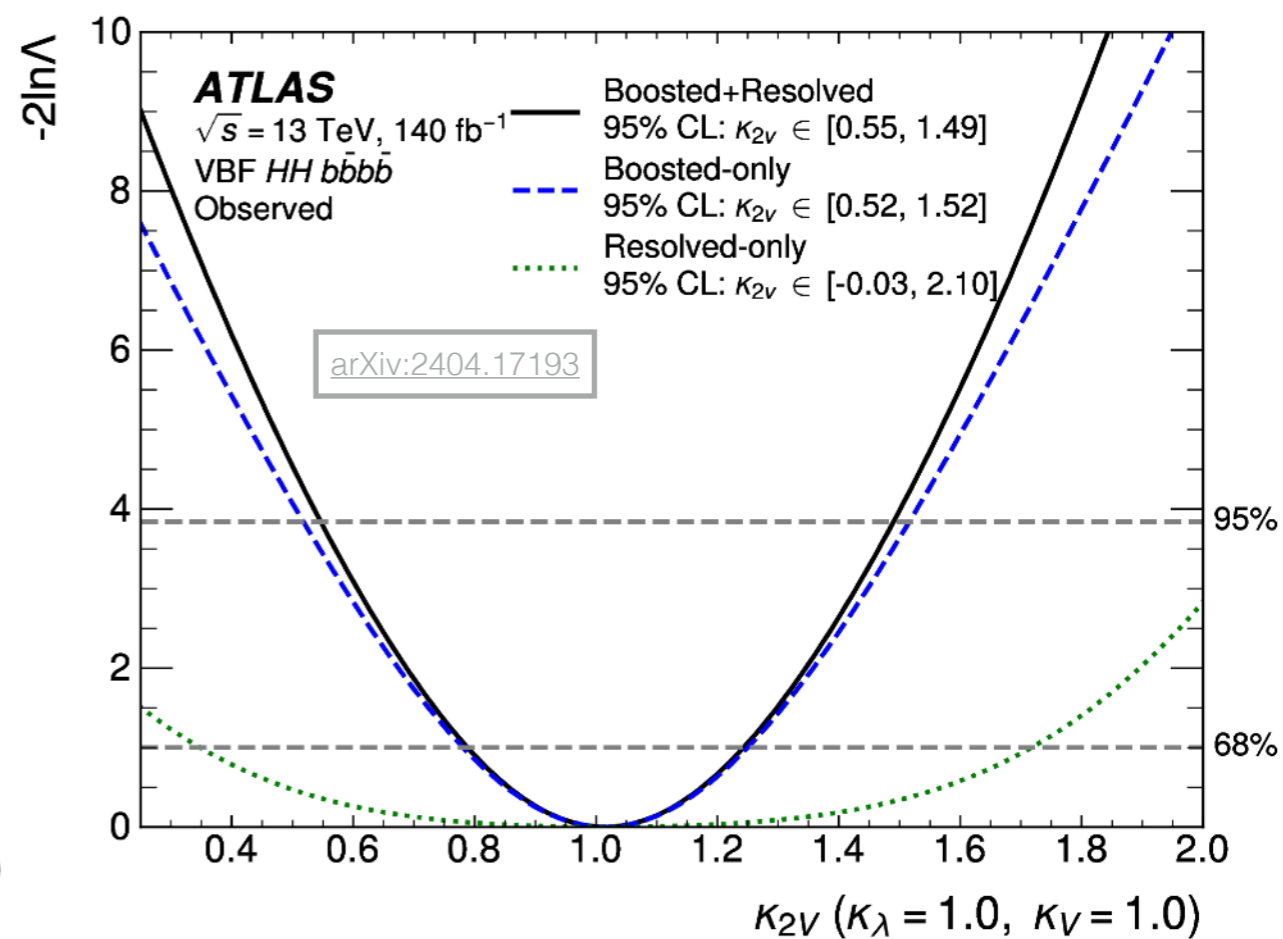
- At 95% CL, expected  $\kappa_{2V} \in [0.5, 1.6]$  at HL-LHC.
- Recently published (2024) a new Run 2 search ( $140 \text{ fb}^{-1}$ ) allowing to already beat HL-LHC limit! **A huge step forward in just 2 years!**
- It isn't hard to believe that all these numbers are still pessimistic!

Resolved  $HH \rightarrow b\bar{b}b\bar{b}$  at HL-LHC ( $3000 \text{ fb}^{-1}$ )



$\kappa_{2V} \in [0.5, 1.6]$

Boosted VBF  $HH \rightarrow b\bar{b}b\bar{b}$  ( $140 \text{ fb}^{-1}$ )



$\kappa_{2V} \in [0.55, 1.49]$

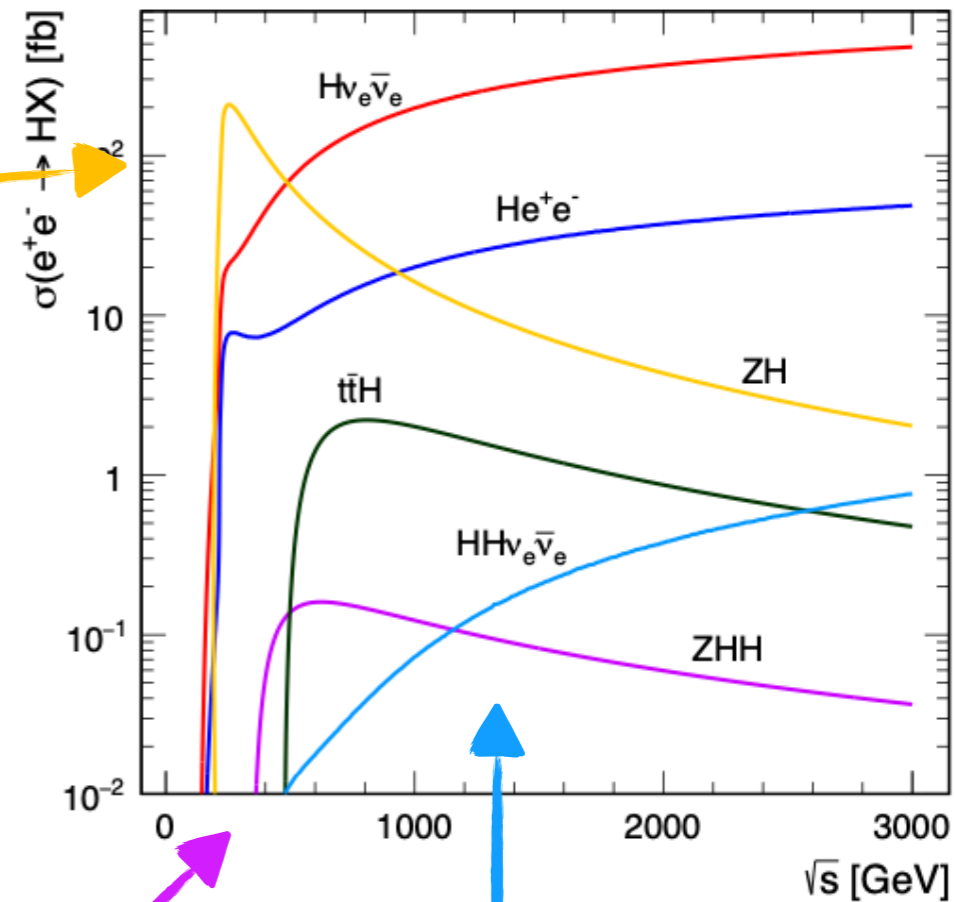
**What can we achieve  
beyond HL-LHC?**





# HH production at future Higgs factories

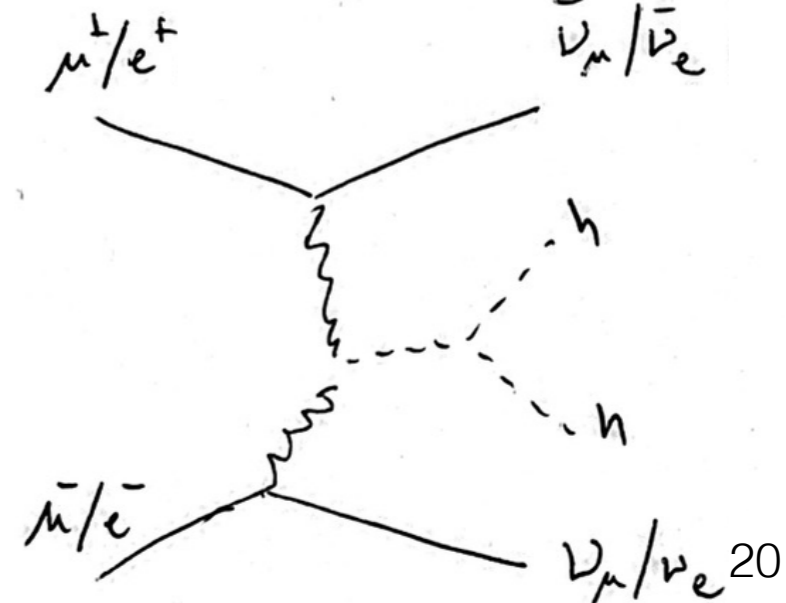
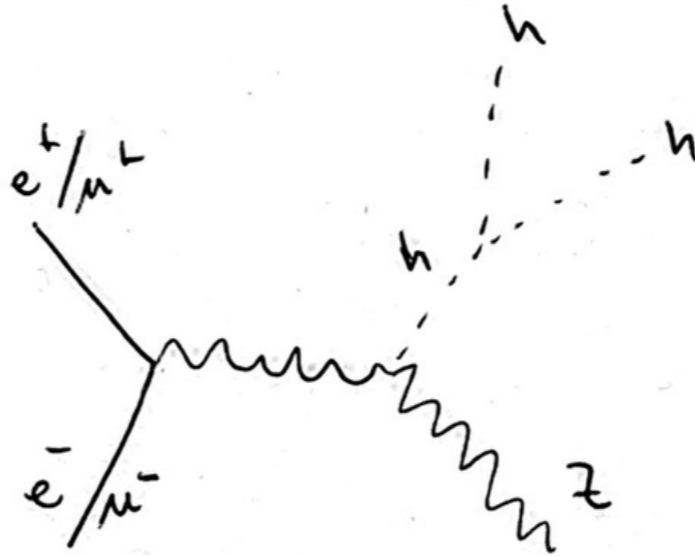
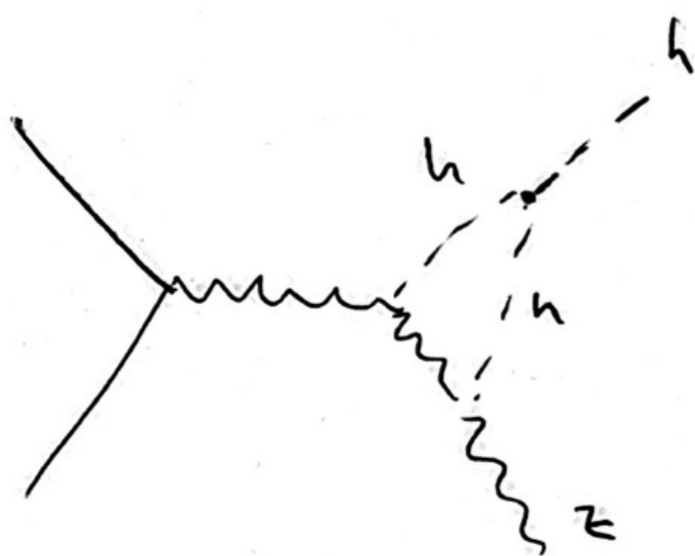
- **Two ways to constrain** self-coupling modifier  $\kappa_\lambda$  at Higgs factories:
  - **Indirect constraint (ZH): no access to HH**
    - **Dominant at circular  $e^+e^-$  colliders** (FCC-ee, CEPC) and **low-energy linear colliders** (ILC250, etc.)
    - **Requires good knowledge of other Higgs couplings** (e.g.  $\kappa_V, \kappa_\gamma$ ) to measure  $\kappa_\lambda$  precisely.
  - **Direct constraint (ZHH,  $\nu\nu$ HH): access to HH**
    - **Dominant at high-energy lepton colliders** (ILC, CLIC, C3, Muon Collider).



$\sqrt{s} \approx m_Z + m_h \sim 250 \text{ GeV}$

$\sqrt{s} \approx m_Z + 2 \cdot m_h \sim 500 \text{ GeV}$

$\sqrt{s} \gg m_Z + 2 \cdot m_h$

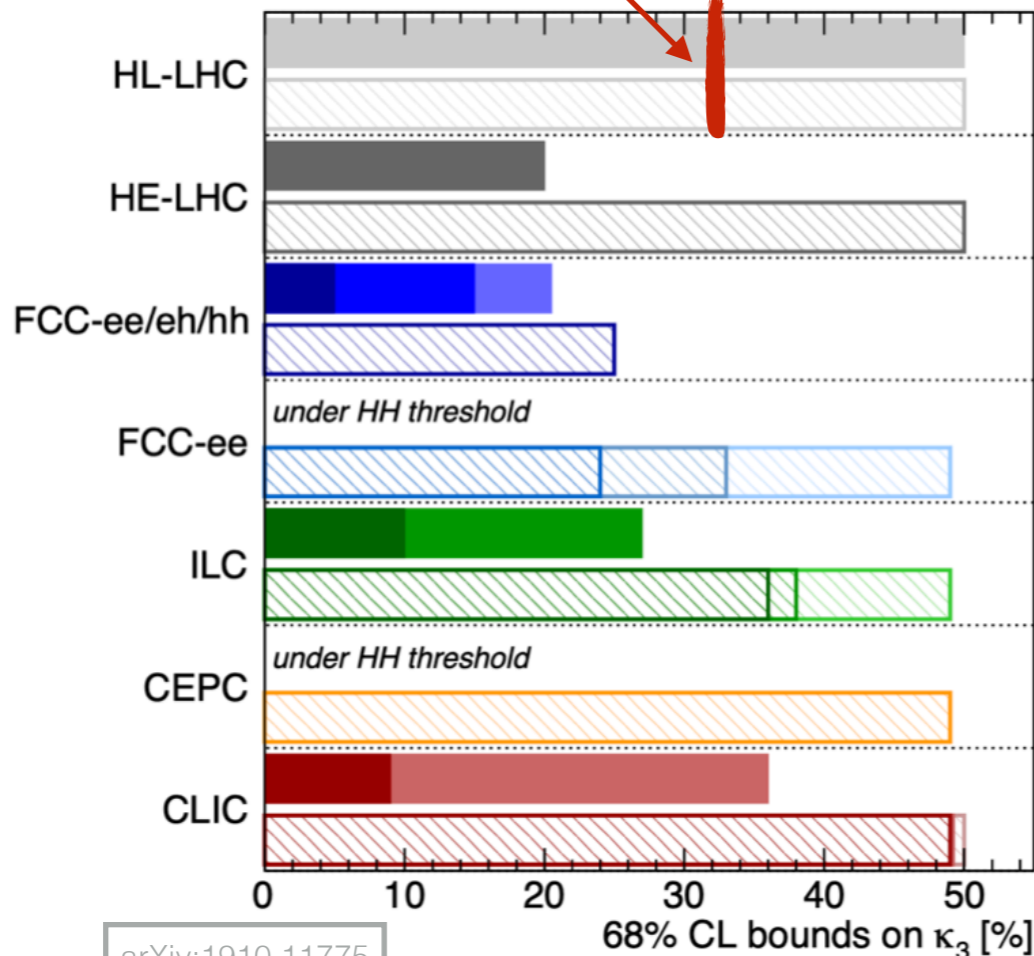




# Comparison of future colliders

- Circular  $e^+e^-$  colliders (FCC-ee, CLIC) could get  $\kappa_\lambda$  precision down to 25-50% with indirect ZH measurements.
  - O(1%) knowledge of other Higgs couplings is expected to be good enough!
- Possible to achieve:
  - ~10% precision with high-energy linear colliders (ILC1000, CLIC3000, etc.)
  - ~5% precision with high-energy hadron colliders (FCC-hh)

Personal estimation 😊



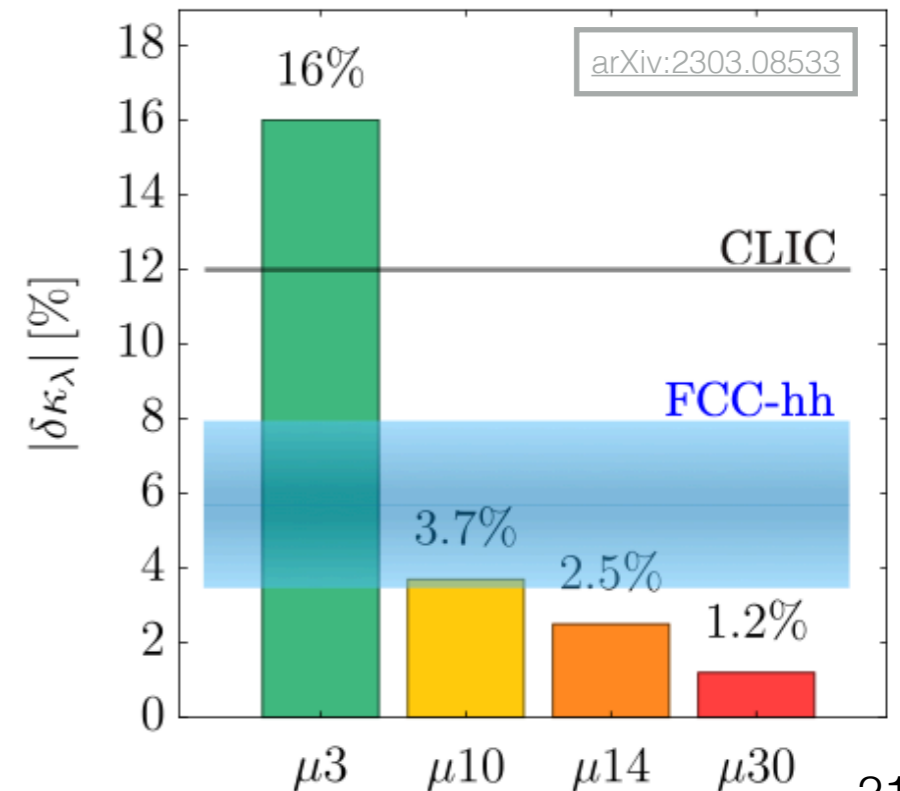
arXiv:1910.11775

Higgs@FC WG September 2019

| di-Higgs                       | single-Higgs                             |
|--------------------------------|--|
| HL-LHC 50%                     | HL-LHC 50%                               |
| HE-LHC [10-20]%                | HE-LHC 50%                               |
| FCC-ee/eh/hh 5%                | FCC-ee/eh/hh 25%                         |
| LE-FCC 15%                     | LE-FCC n.a.                              |
| FCC-eh <sub>3500</sub> -17+24% | FCC-eh <sub>3500</sub> n.a.              |
|                                | FCC-ee <sup>4IP</sup> <sub>365</sub> 24% |
|                                | FCC-ee <sub>365</sub> 33%                |
|                                | FCC-ee <sub>240</sub> 49%                |
| ILC <sub>1000</sub> 10%        | ILC <sub>1000</sub> 36%                  |
| ILC <sub>500</sub> 27%         | ILC <sub>500</sub> 38%                   |
|                                | ILC <sub>250</sub> 49%                   |
|                                | CEPC 49%                                 |
| CLIC <sub>3000</sub> -7%+11%   | CLIC <sub>3000</sub> 49%                 |
| CLIC <sub>1500</sub> 36%       | CLIC <sub>1500</sub> 49%                 |
|                                | CLIC <sub>380</sub> 50%                  |

All future colliders combined with HL-LHC

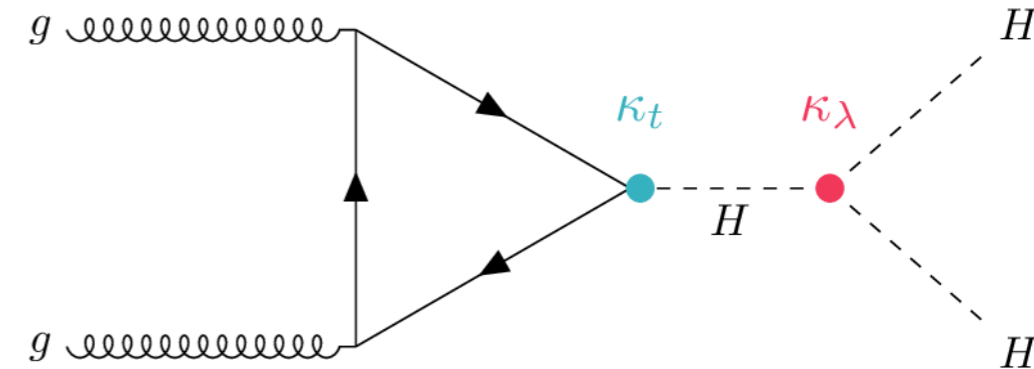
Want more? You need a 30 TeV Muon Collider ( $\nu\nu HH$ )!



arXiv:2303.08533

# Conclusion and outlook

- The Higgs sector is **UNIQUE** and still **largely unexplored!**
  - Shape of the **Higgs potential is essential** to fully understand EWSB!
  - HH searches at HL-LHC will give first **measurement** of potential shape via measurement of  $\kappa_\lambda$ .
- Some personal HL-LHC estimations:**
  - ⚠ Unofficial, please use with caution!**
  - $5\sigma$  discovery should be well within reach!** Especially considering how quickly we are improving things.
- For better precision: future  $e^+e^-$  and hadron-hadron colliders**
  - Want better? Then you need a  $\geq 15$  TeV Muon Collider ( $\sigma(\kappa_\lambda) \sim 1\%$ ).



|                            | Personal HL-LHC projection  |
|----------------------------|---|
| Significance Z             | <b>4.8<math>\sigma</math> (6.9<math>\sigma</math>)</b> with and without systematics |
| Precision $\kappa_\lambda$ | <b>~30%</b> with systs  |
| Precision $\kappa_{2V}$    | <b>~50%</b> with systs  |

Already better than this with Run 2 dataset!

|                                 | Precision on $\kappa_\lambda$ |
|---------------------------------|-------------------------------|
| Circular $e^+e^-$ (FCC-ee/CEPC) | ~ 25-50%                      |
| FCC-hh                          | ~5%                           |
| High-energy linear colliders    | ~10%                          |



**Backup**

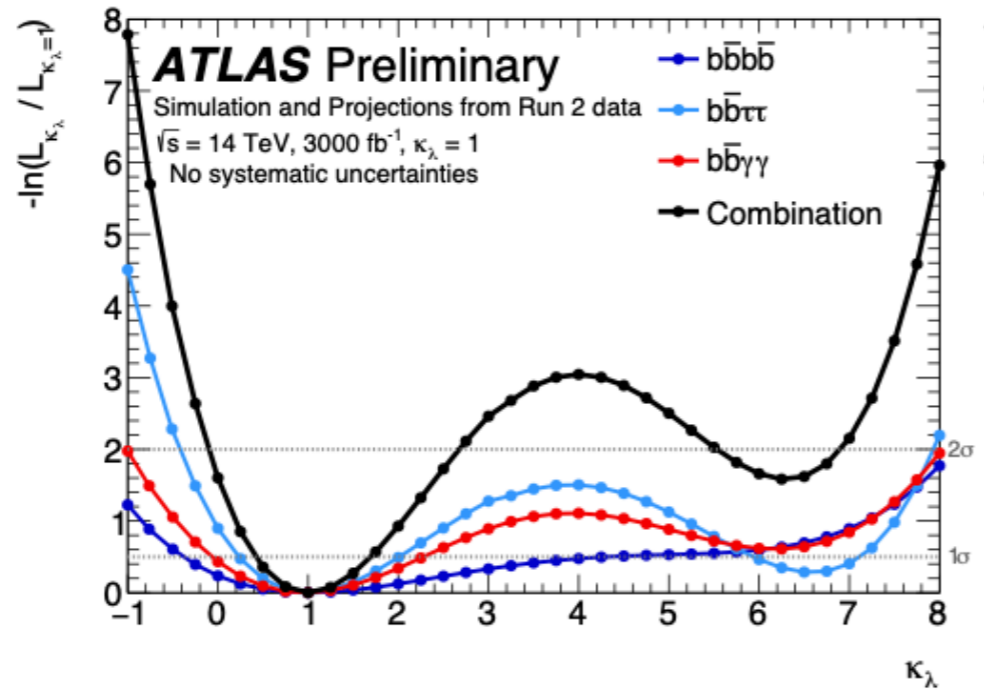
# HL-LHC systematic uncertainties and cross-sections



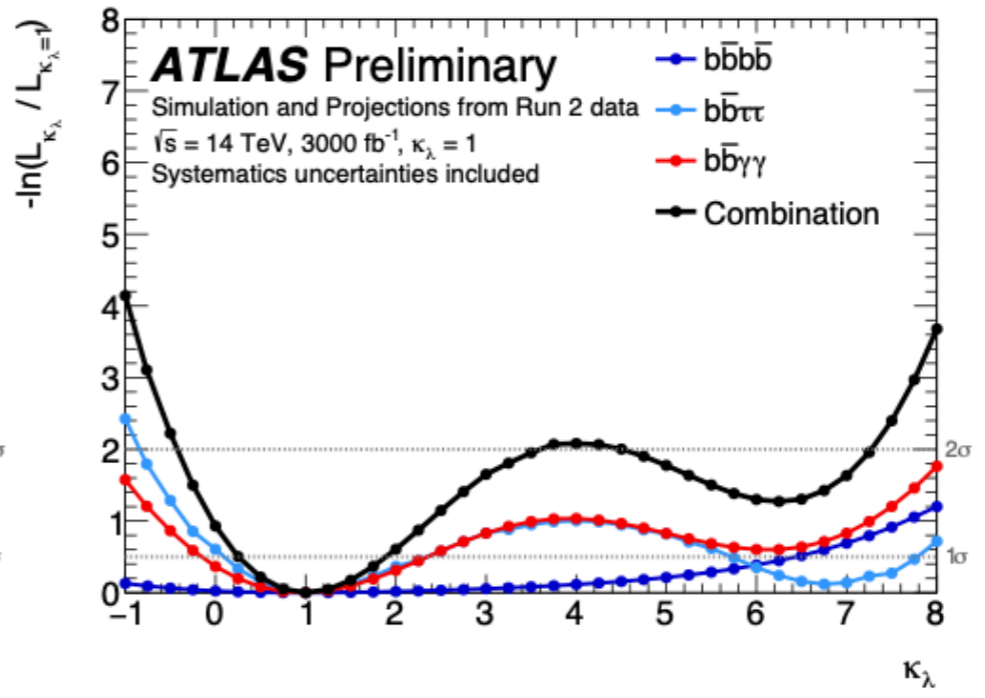
| Source  | Scale factor | $b\bar{b}\gamma\gamma$ | $b\bar{b}\tau^+\tau^-$ |
|---|--------------|------------------------|------------------------|
| <b>Experimental Uncertainties</b>                     |              |                        |                        |
| Luminosity  | 0.6          | *                      | *                      |
| $b$ -jet tagging efficiency                           | 0.5          | *                      | *                      |
| $c$ -jet tagging efficiency                           | 0.5          | *                      | *                      |
| Light-jet tagging efficiency                          | 1.0          | *                      | *                      |
| Jet energy scale and resolution, $E_T^{\text{miss}}$  | 1.0          | *                      | *                      |
| $\kappa_\lambda$ reweighting                          | 0.0          | *                      | *                      |
| Photon efficiency (ID, trigger, isolation efficiency) | 0.8          | *                      |                        |
| Photon energy scale and resolution                    | 1.0          | *                      |                        |
| Spurious signal                                       | 0.0          | *                      |                        |
| Value of $m_H$  | 0.08         | *                      |                        |
| $\tau_{\text{had}}$ efficiency (statistical)          | 0.0          |                        | *                      |
| $\tau_{\text{had}}$ efficiency (systematic)           | 1.0          |                        | *                      |
| $\tau_{\text{had}}$ energy scale                      | 1.0          |                        | *                      |
| Fake- $\tau_{\text{had}}$ estimation                  | 1.0          |                        | *                      |
| MC statistical uncertainties                          | 0.0          |                        | *                      |
| <b>Theoretical Uncertainties</b>                      |              |                        |                        |
|   | 0.5          | *                      | *                      |

| Process            | Scale factor |
|--------------------|--------------|
| <b>Signals</b>     |              |
| ggF $HH$           | 1.18         |
| VBF $HH$           | 1.19         |
| <b>Backgrounds</b> |              |
| ggF $H$            | 1.13         |
| VBF $H$            | 1.13         |
| $WH$               | 1.10         |
| $ZH$               | 1.12         |
| $t\bar{t}H$        | 1.21         |
| Others             | 1.18         |

# ATLAS CERN Yellow report



(a) Statistical uncertainties only



(b) Statistical + systematic uncertainties

The combined minimum negative-log-likelihoods are shown in Figure 66. The 68% Confidence Intervals for  $\kappa_\lambda$  are  $0.52 \leq \kappa_\lambda \leq 1.5$  and  $0.57 \leq \kappa_\lambda \leq 1.5$  with and without systematic uncertainties respectively. The second minimum of the likelihood is excluded at 99.4% CL. A summary of the 68% CI for each channel in each experiment, as well as the combination are shown in Figure 66b.

Table 54: 68% Confidence Intervals for  $\kappa_\lambda$ , estimated for an Asimov dataset containing the backgrounds plus SM signal.

|                                       | Statistical-only   | Statistical + Systematic   |
|---------------------------------------|--|--|
| $HH \rightarrow b\bar{b}b\bar{b}$     | $-0.4 \leq \kappa_\lambda \leq 4.3$                                      | $-2.3 \leq \kappa_\lambda \leq 6.4$                                      |
| $HH \rightarrow b\bar{b}\tau\tau$     | $0.2 \leq \kappa_\lambda \leq 2.0 \cup 5.9 \leq \kappa_\lambda \leq 7.2$ | $0.1 \leq \kappa_\lambda \leq 2.3 \cup 5.7 \leq \kappa_\lambda \leq 7.8$ |
| $HH \rightarrow b\bar{b}\gamma\gamma$ | $-0.1 \leq \kappa_\lambda \leq 2.4$                                      | $-0.2 \leq \kappa_\lambda \leq 2.5$                                      |
| combined                              | $0.4 \leq \kappa_\lambda \leq 1.7$                                       | $0.25 \leq \kappa_\lambda \leq 1.9$                                      |

# Future colliders luminosities

