



DTRC-NRC



Calo4pQVAE: Progress and updates



Oct 10 2024



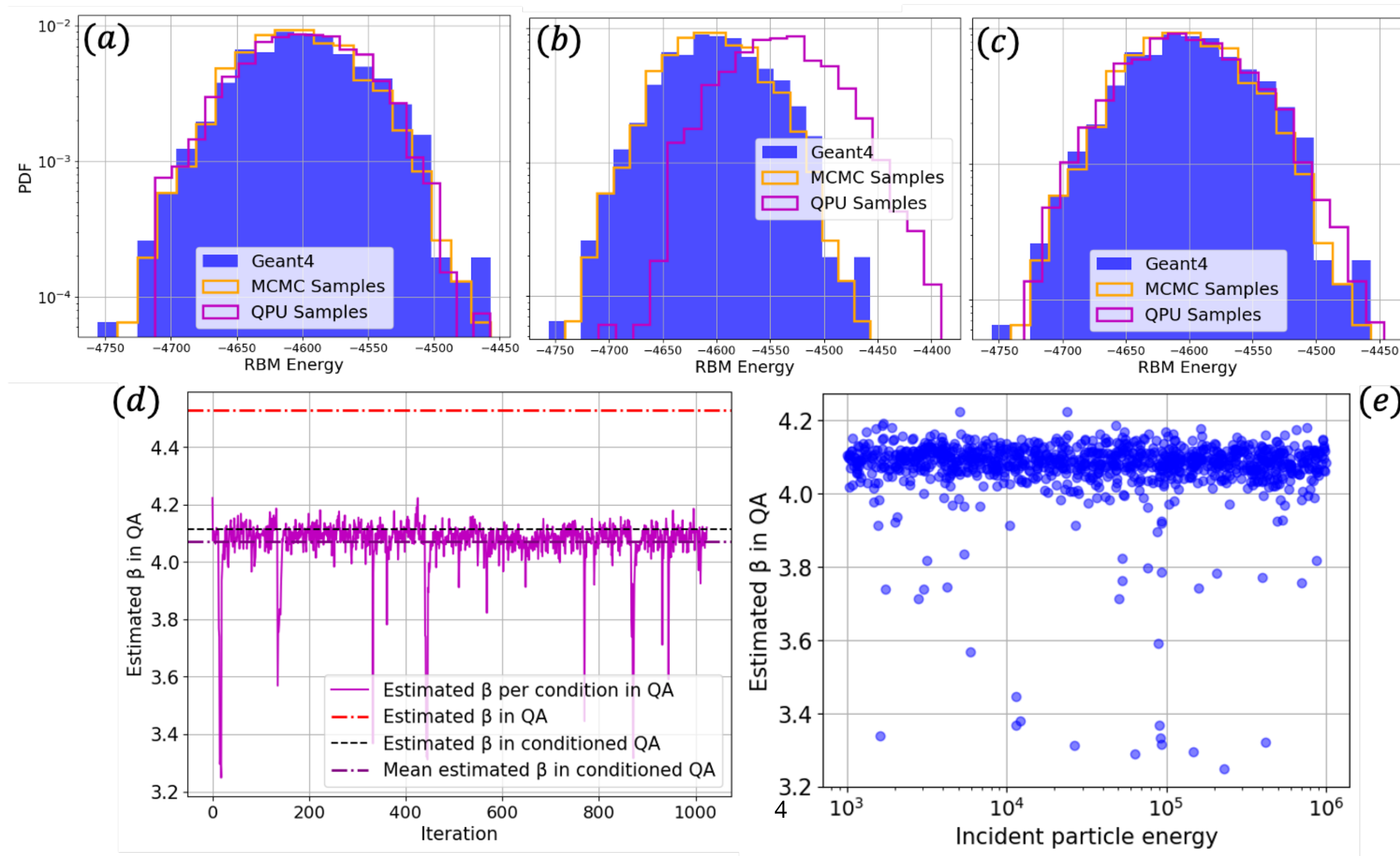
Summary

- ✓ Weight decay removal?
- ✓ Papers status
- ✓ Using the QPU w/ Pegasus and in Zephyr
- ✓ High temperature gradient approximation for trained RBMs
 - RBM and Diffusion model equivalence.
 - Relaxation time in RBMs

Papers status

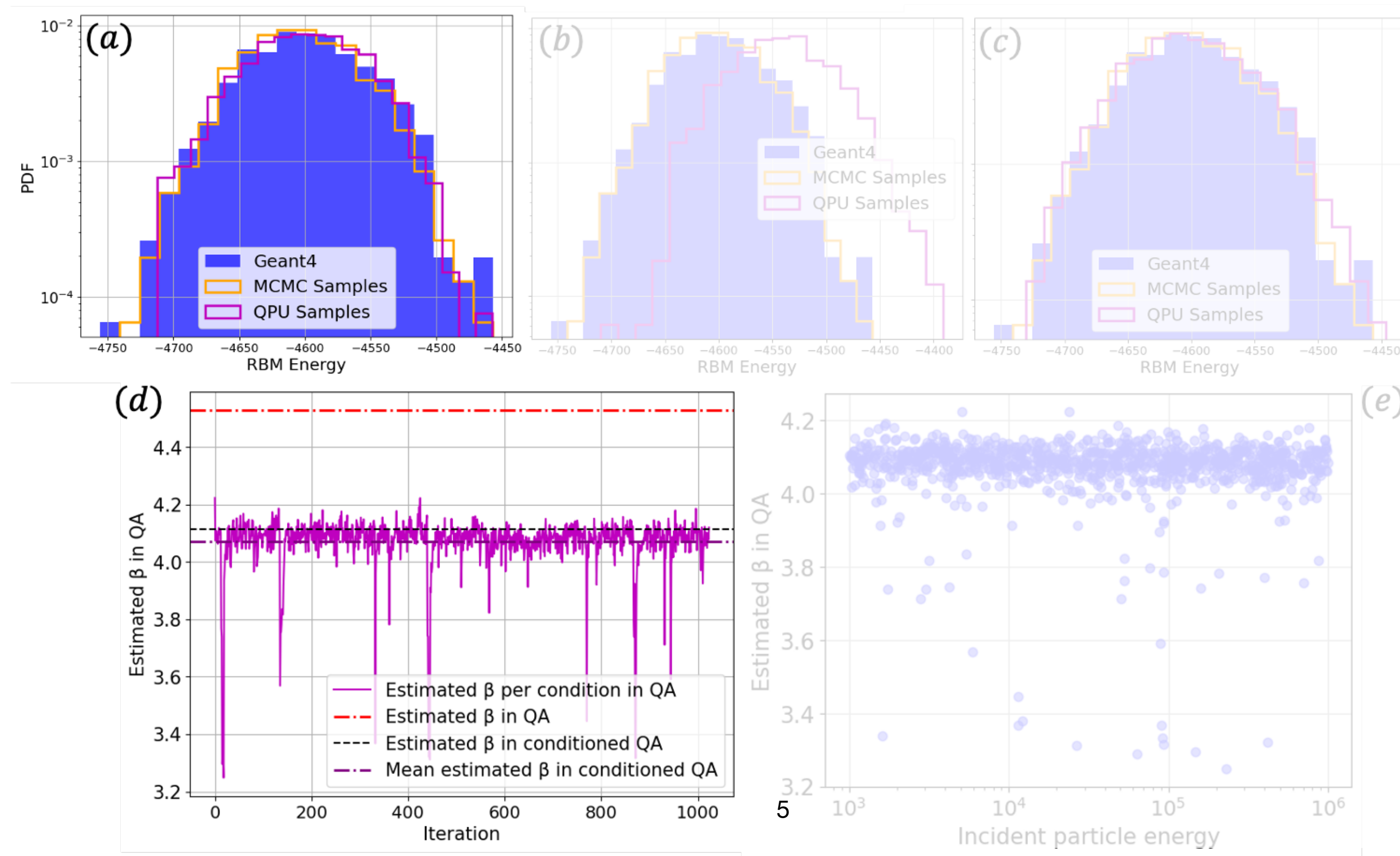
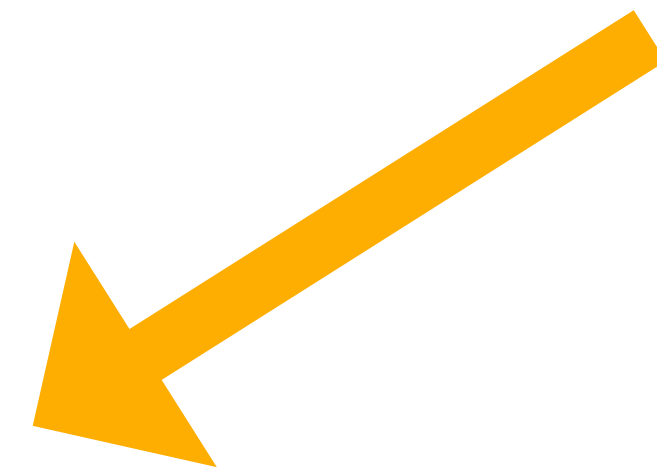
- EPJC -> Rebuttal submitted?
- iEEE QCE Conf -> haven't seen the proceedings online yet
- Neurips ML4Phys -> Got accepted!
- PRX draft -> on countdown for submission

Using QPU w/ Pegasus



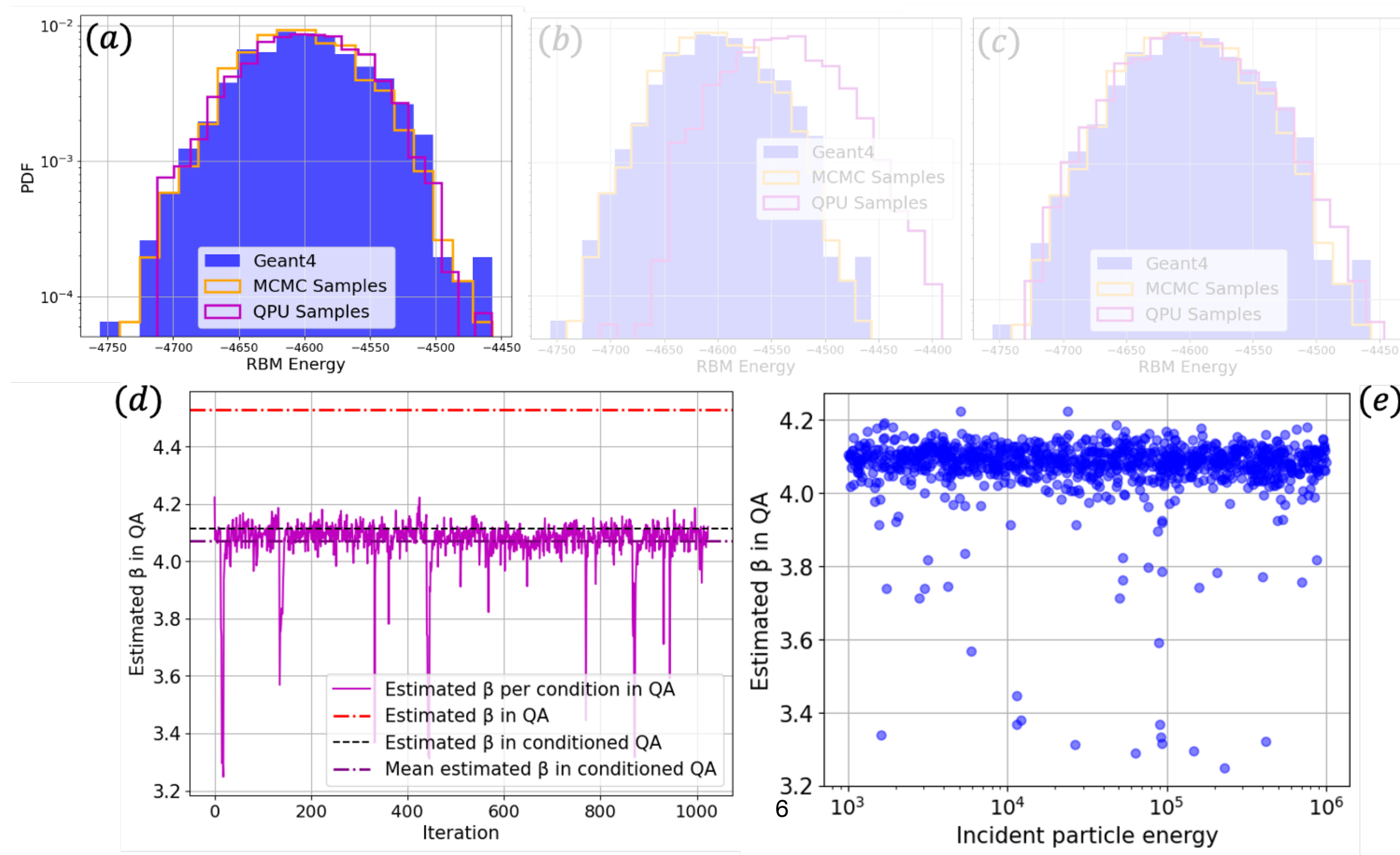
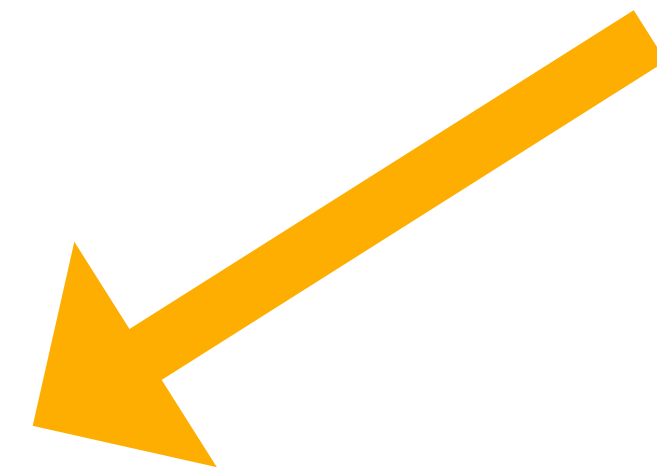
Using QPU w/ Pegasus

We estimate the QA inverse Temperature before generating each sample.



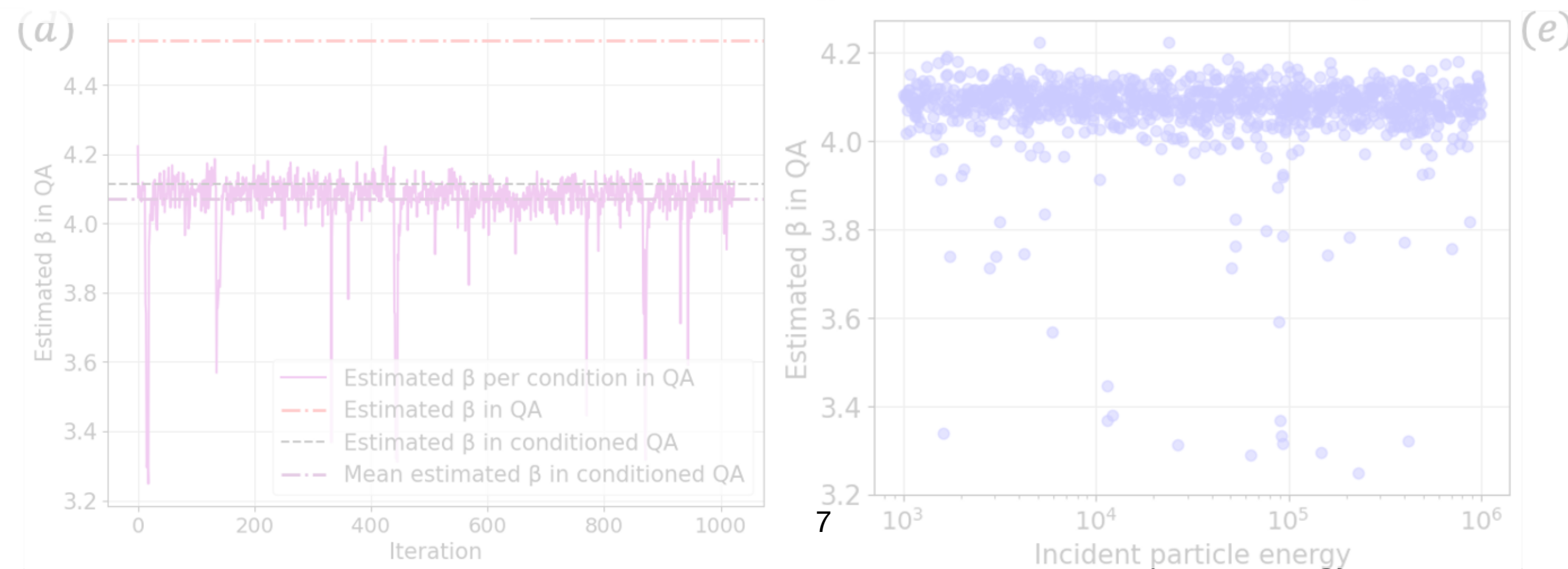
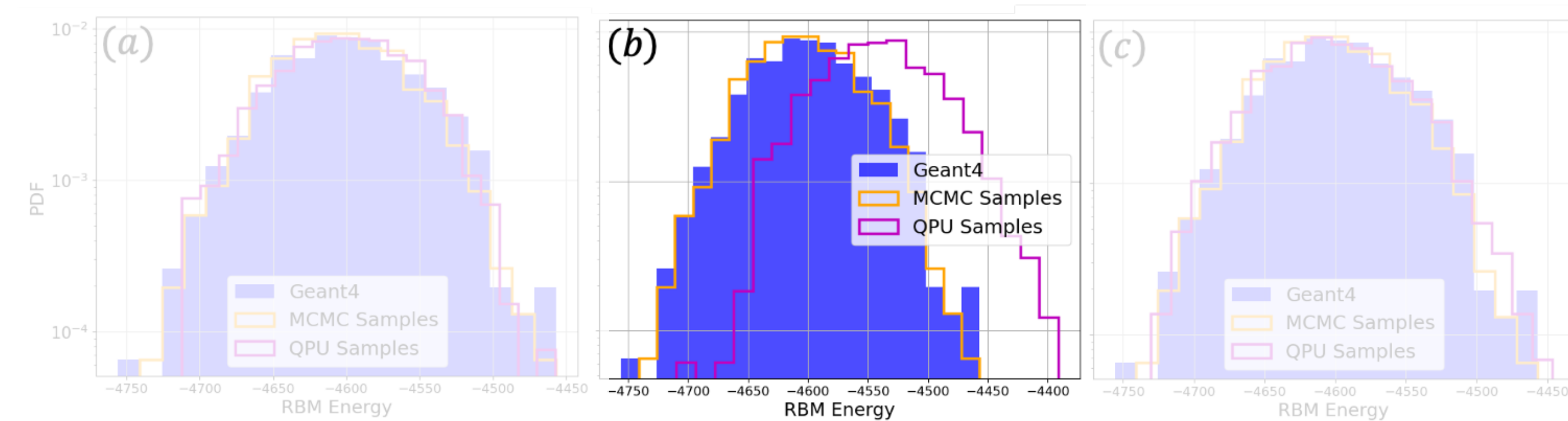
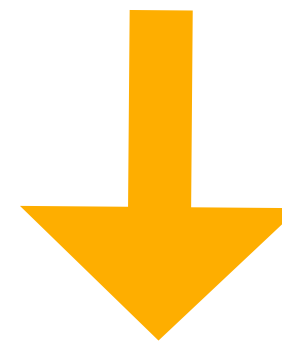
Using QPU w/ Pegasus

We estimate the QA inverse Temperature before generating each sample.



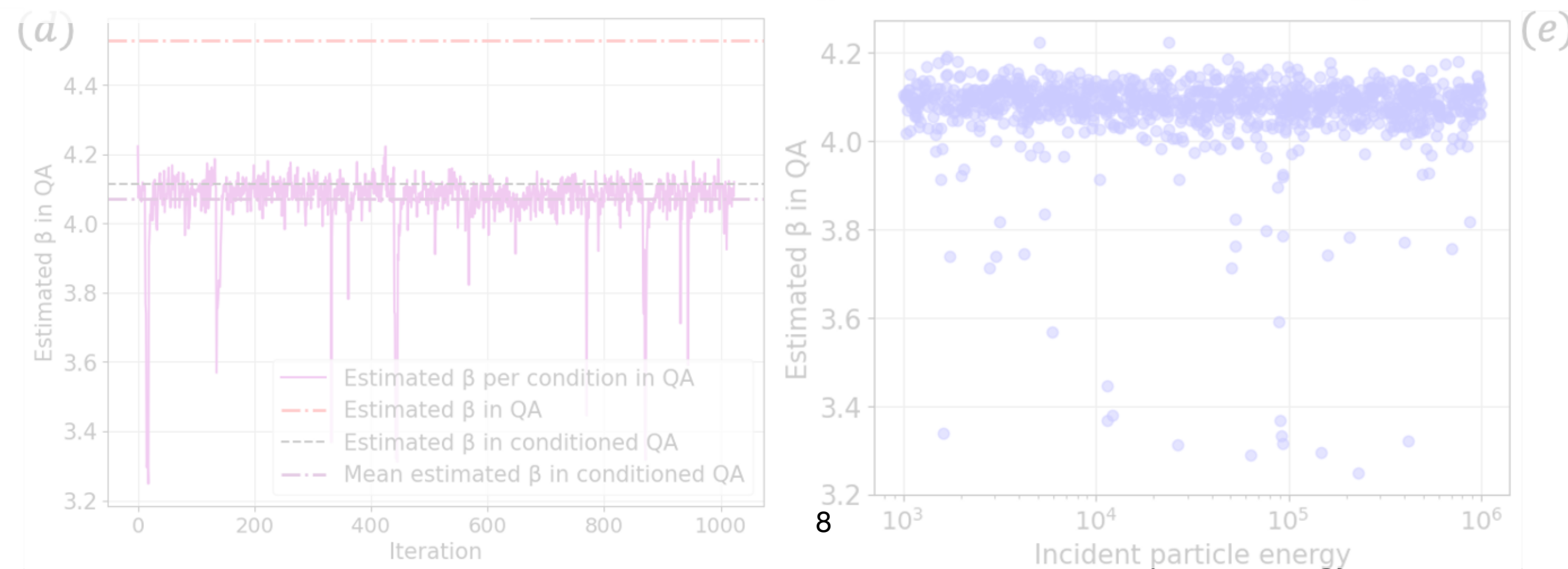
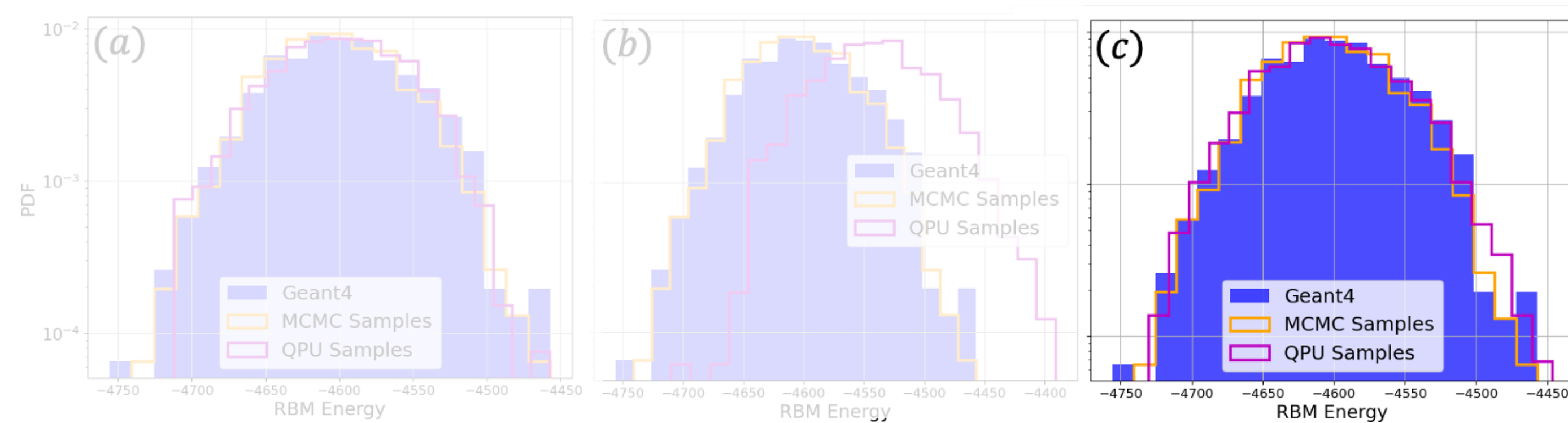
Using QPU w/ Pegasus

We estimate the QA inverse Temperature 1 time. Then generate all samples.



Using QPU w/ Pegasus

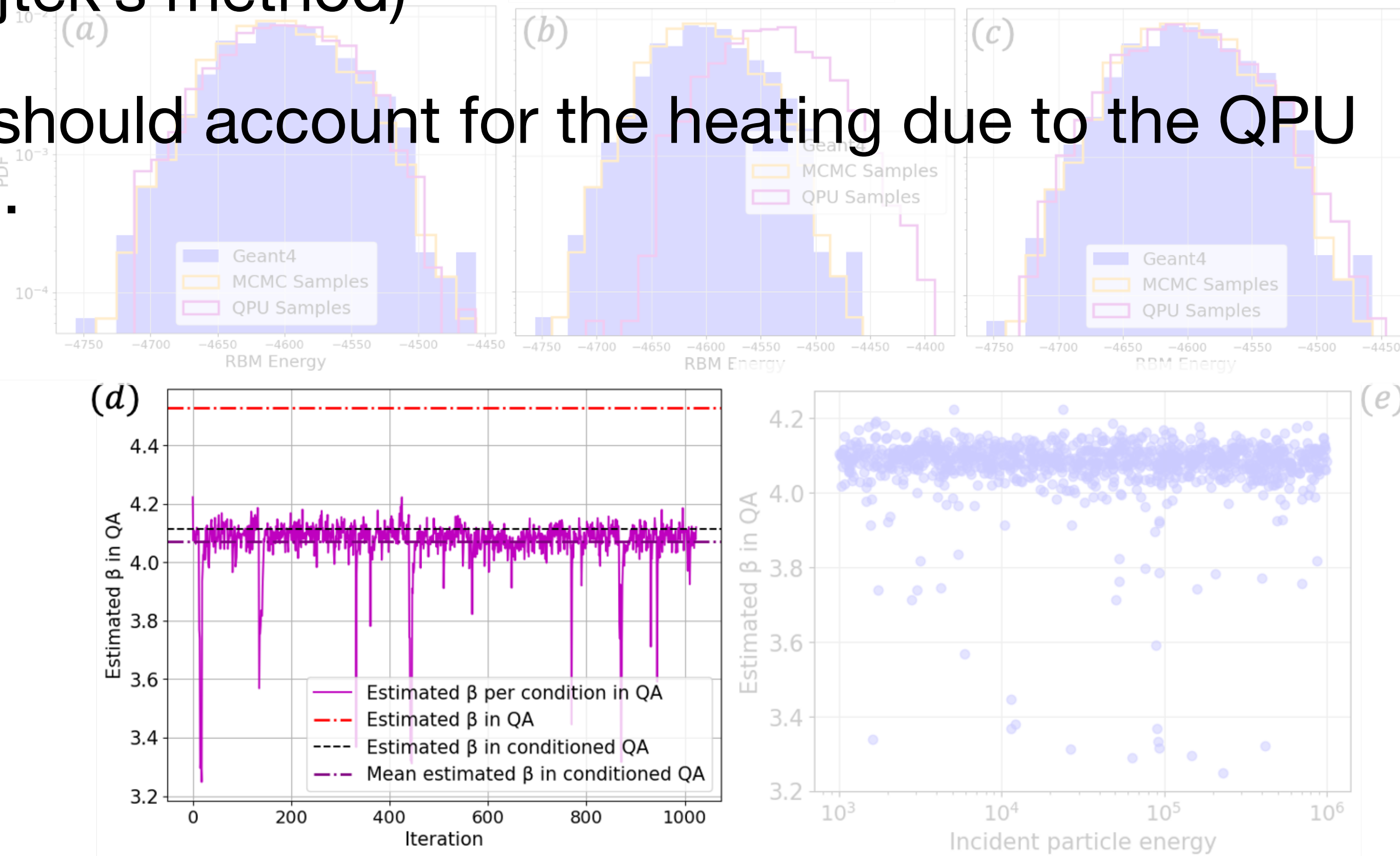
We estimate the QA inverse Temperature 1 time. Then generate all samples. Wait 2.5 seconds between samples



Using QPU w/ Pegasus

What if we estimate the QA inverse by generating 1 sample per API call? (Wojtek's method)

This way we should account for the heating due to the QPU programming.

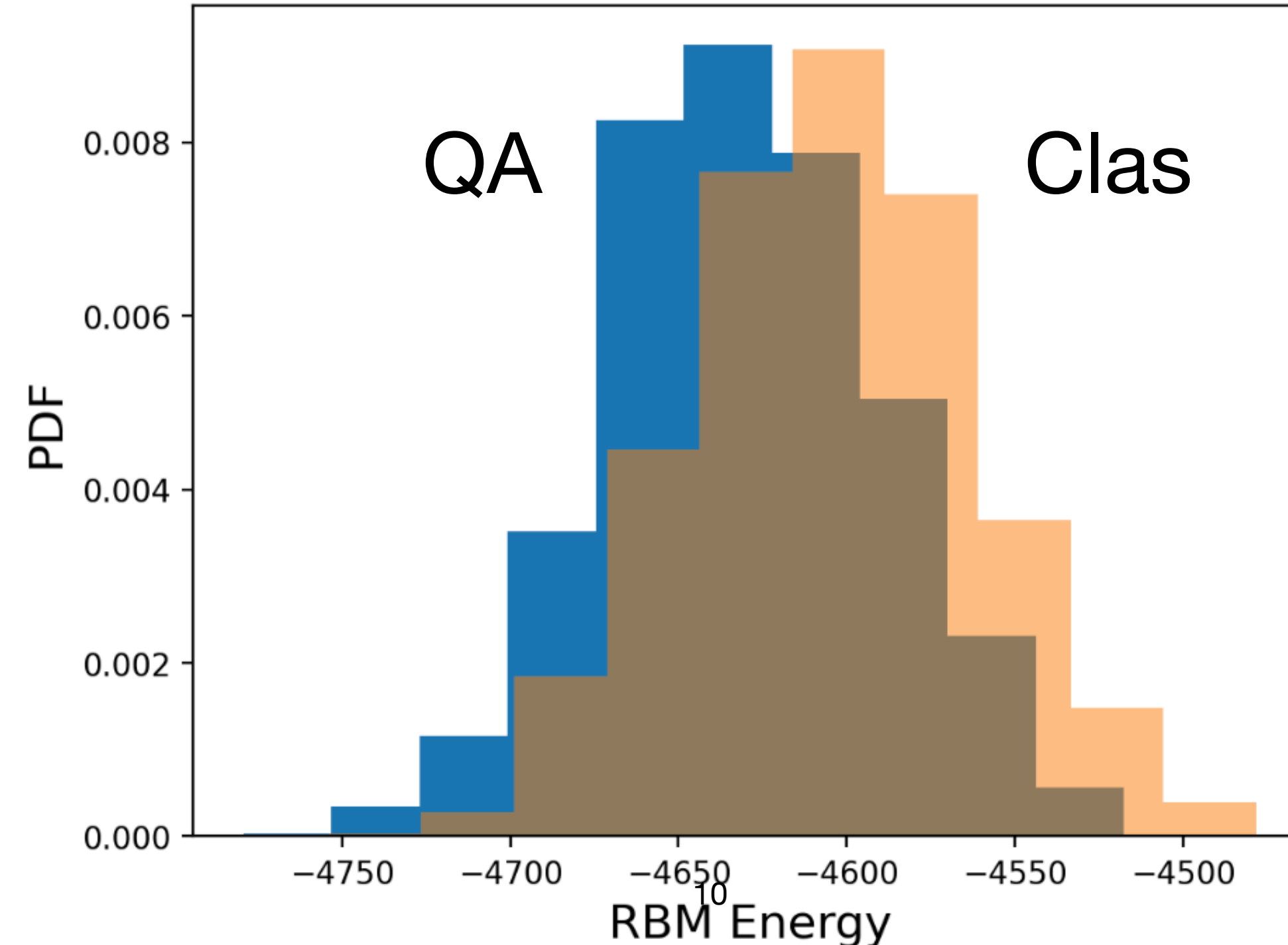


Using QPU w/ Pegasus

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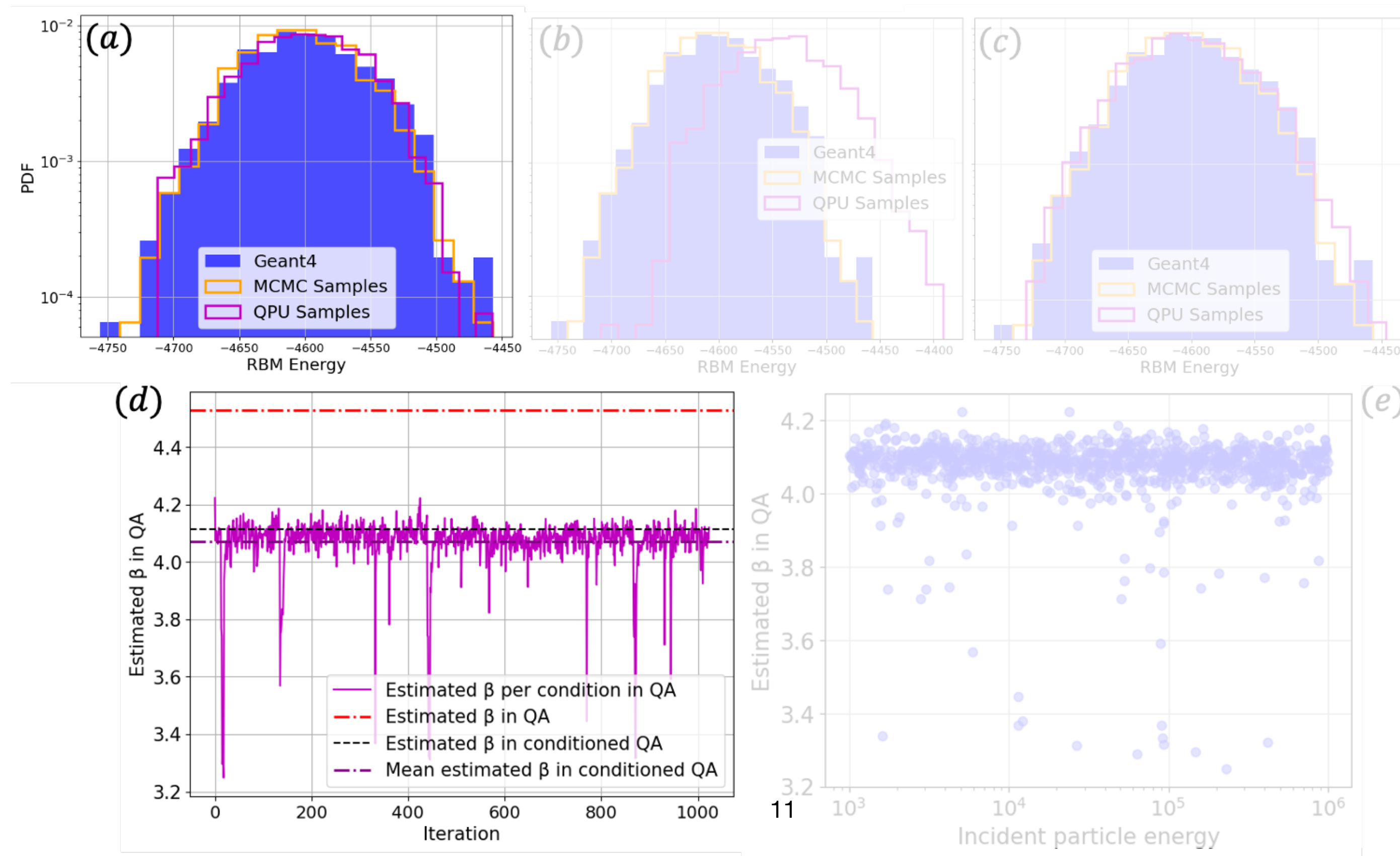
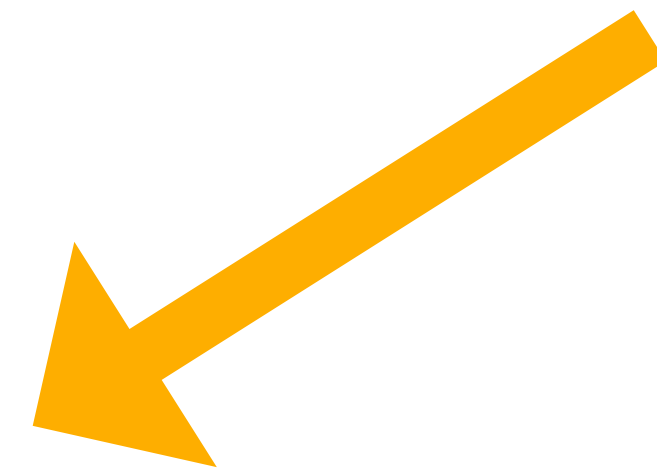
$$\beta_{QA} \approx 2.6$$



Using QPU w/ Pegasus

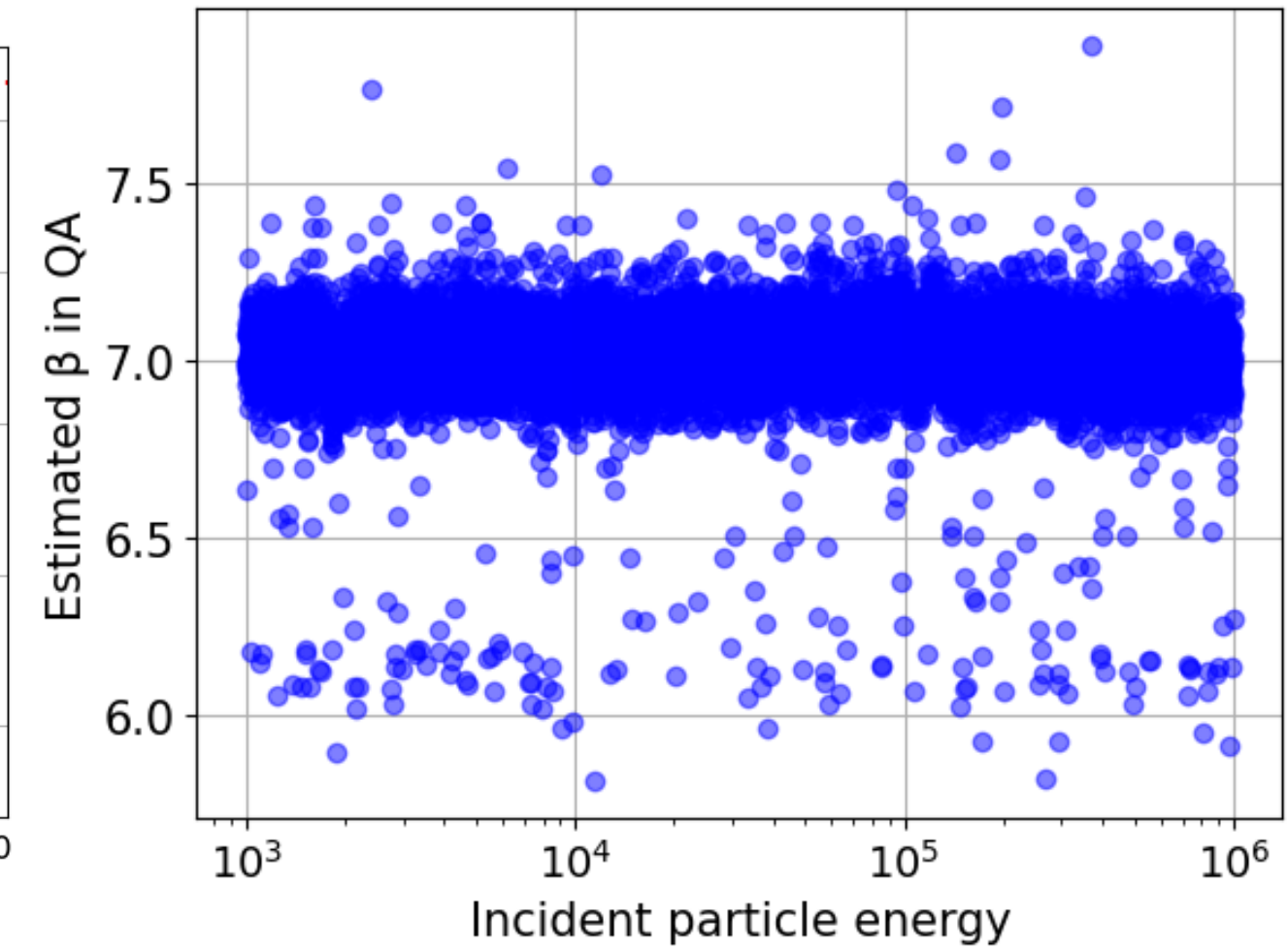
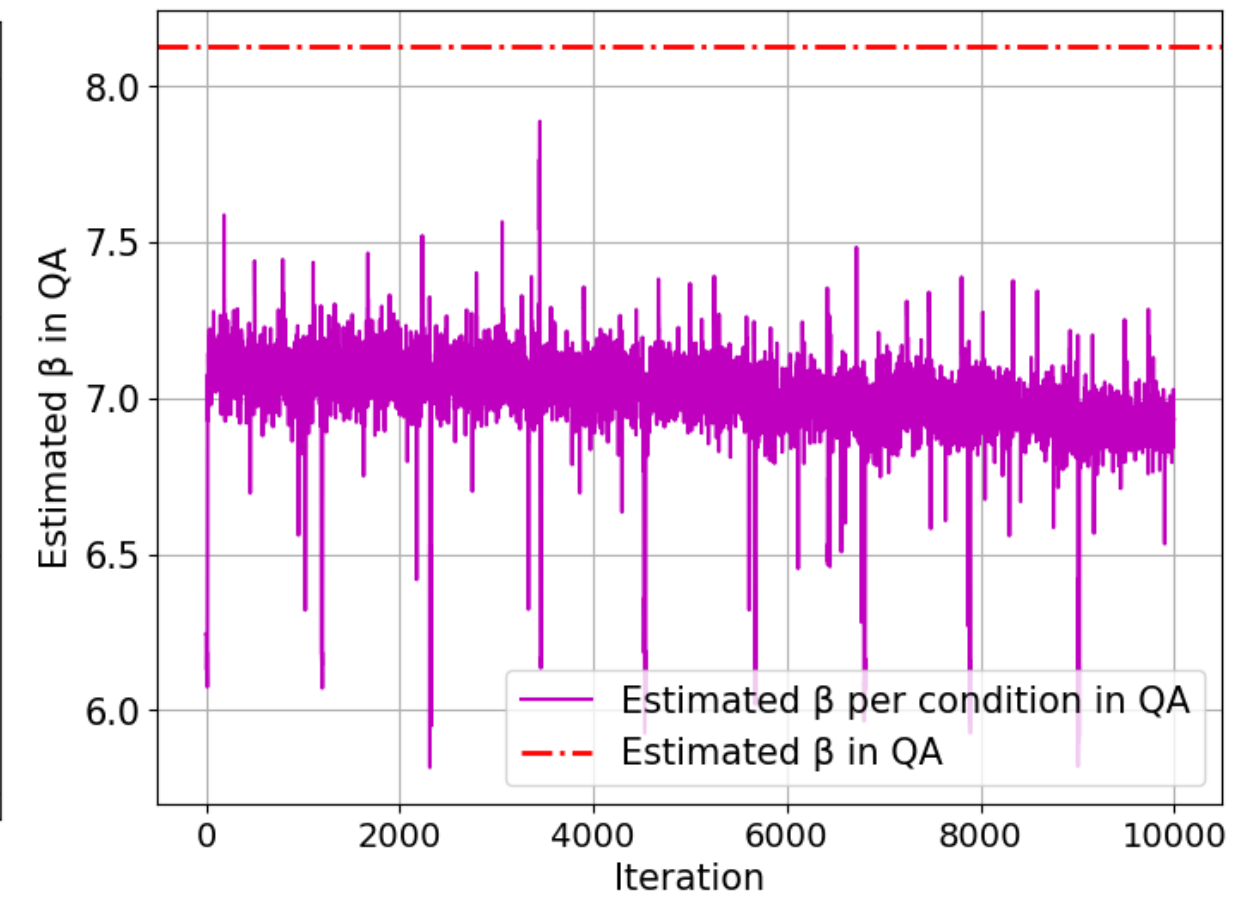
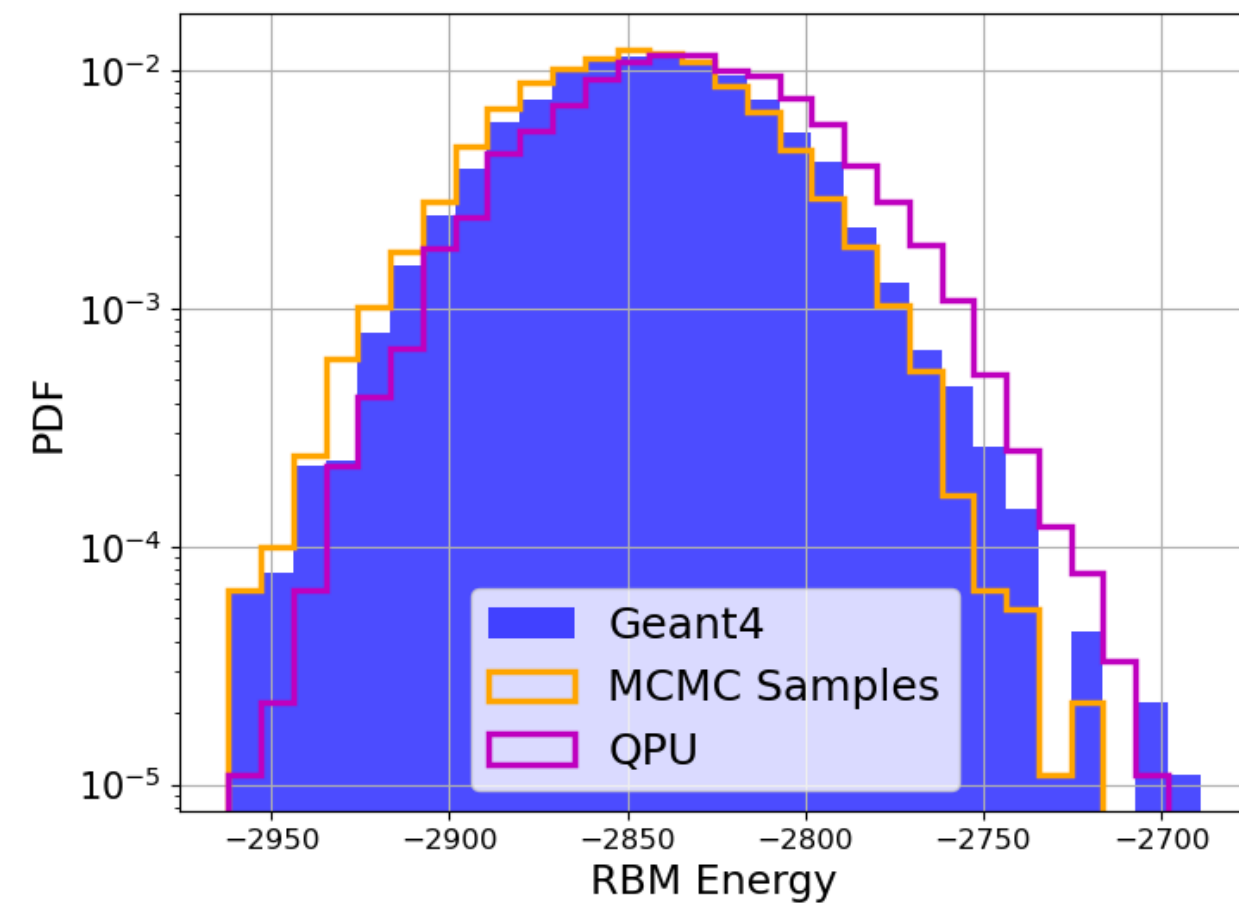
We estimate the QA inverse Temperature before generating each sample.

Winning method!

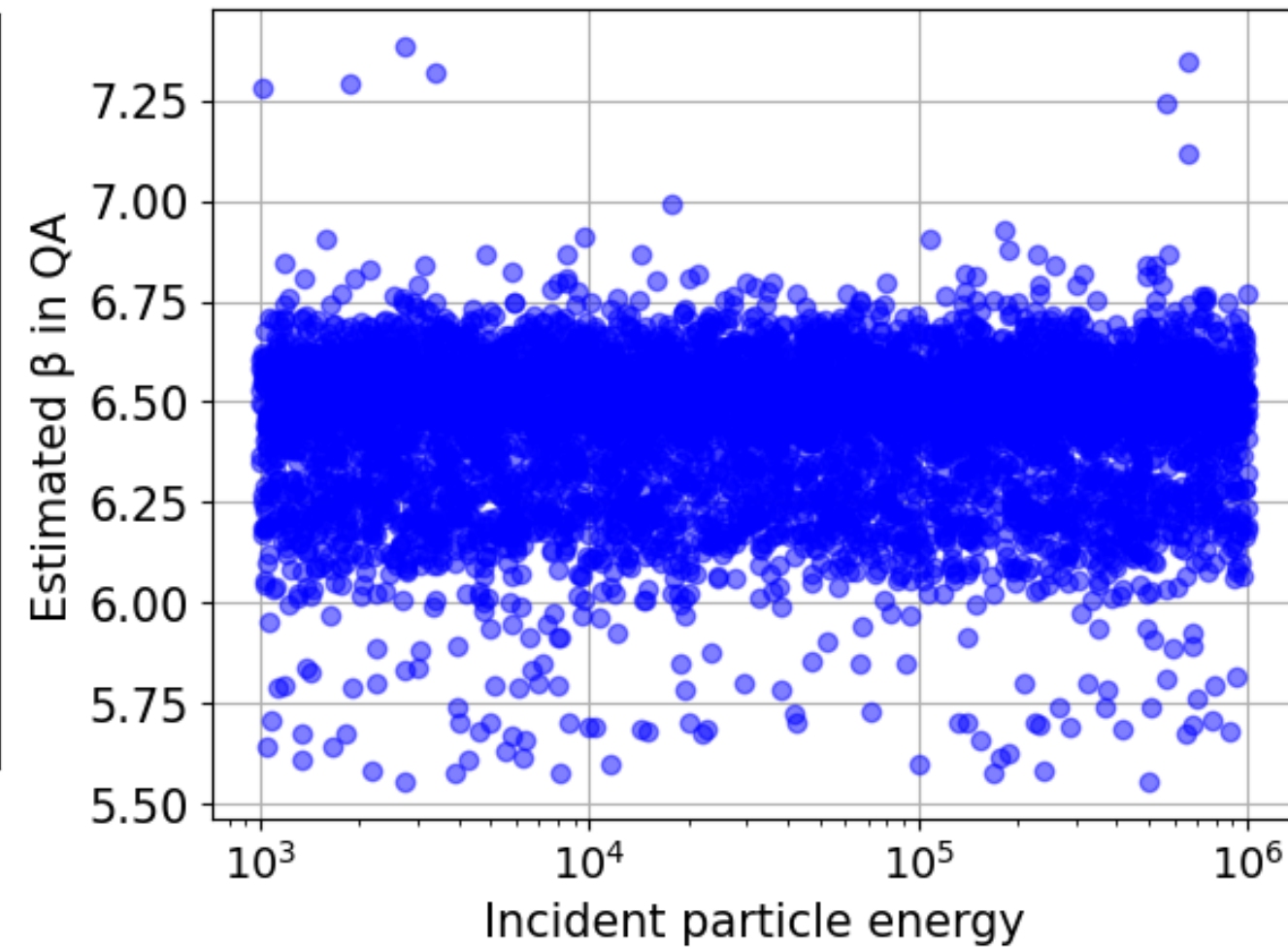
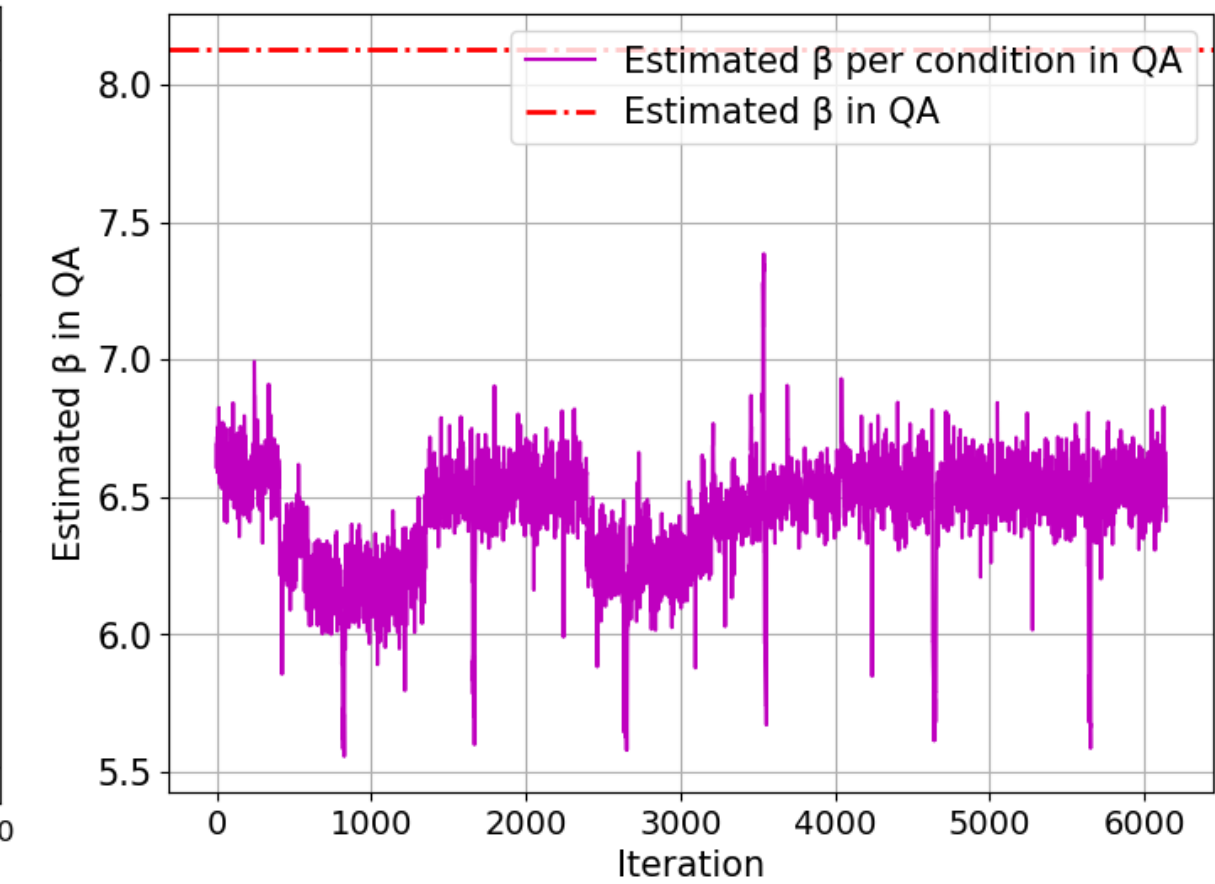
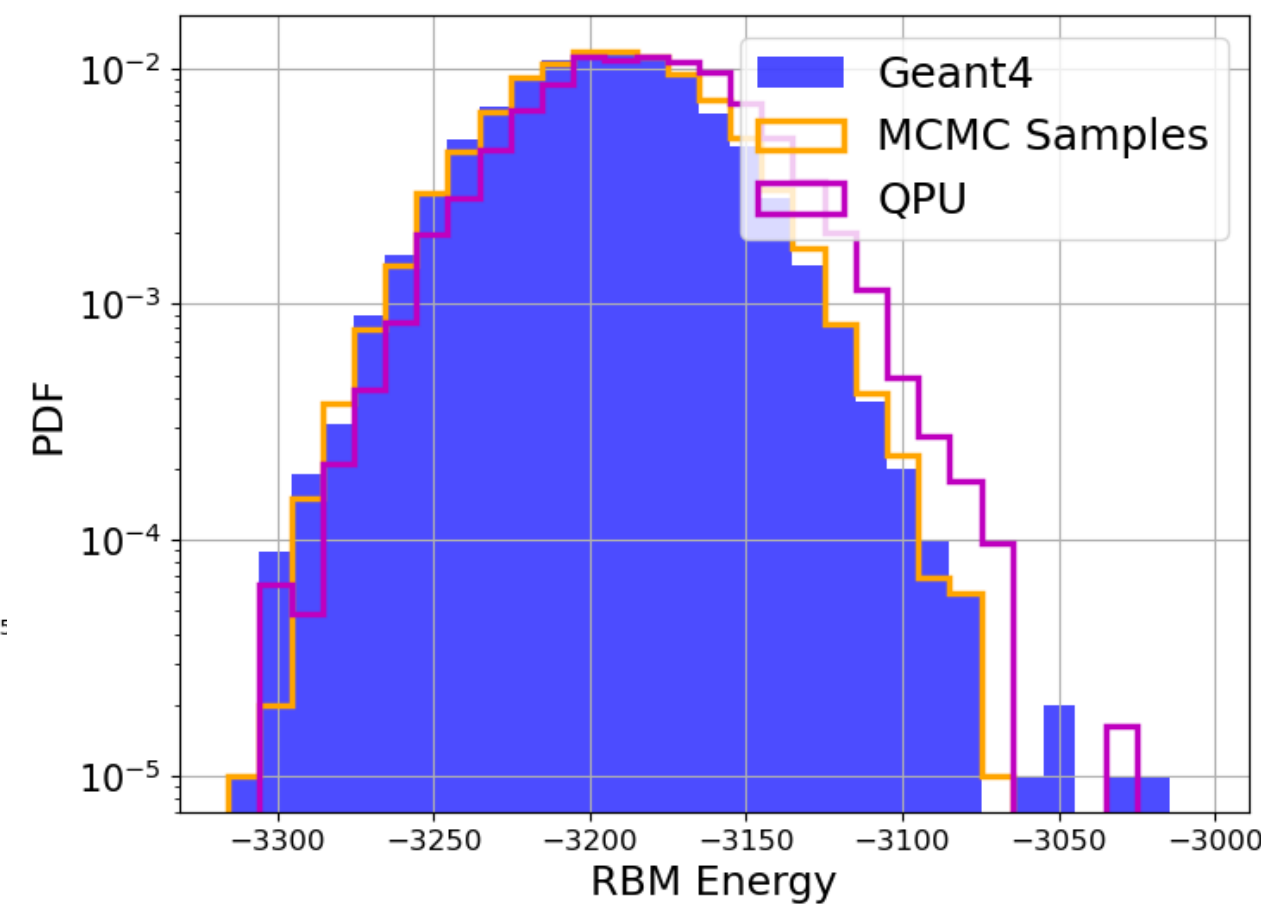
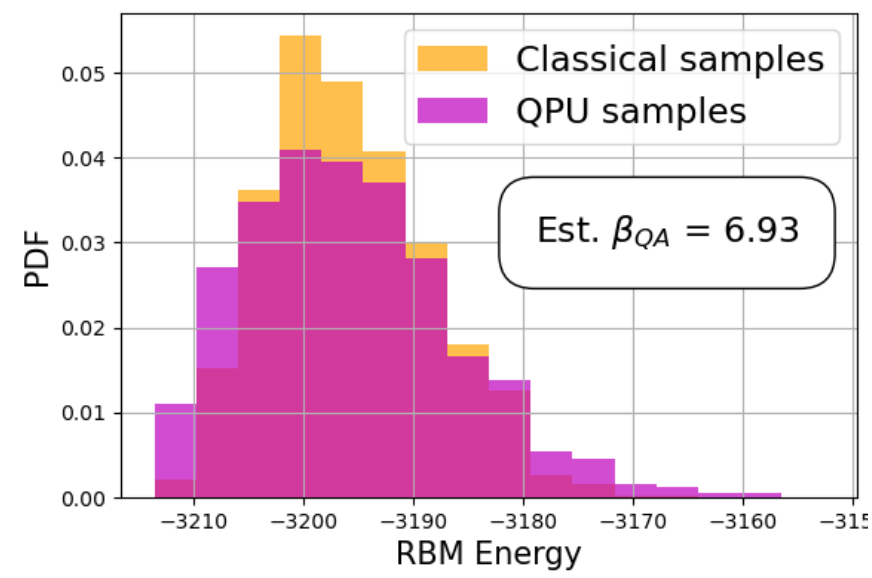


Using QPU w/ Zephyr :: Winning method

Model A

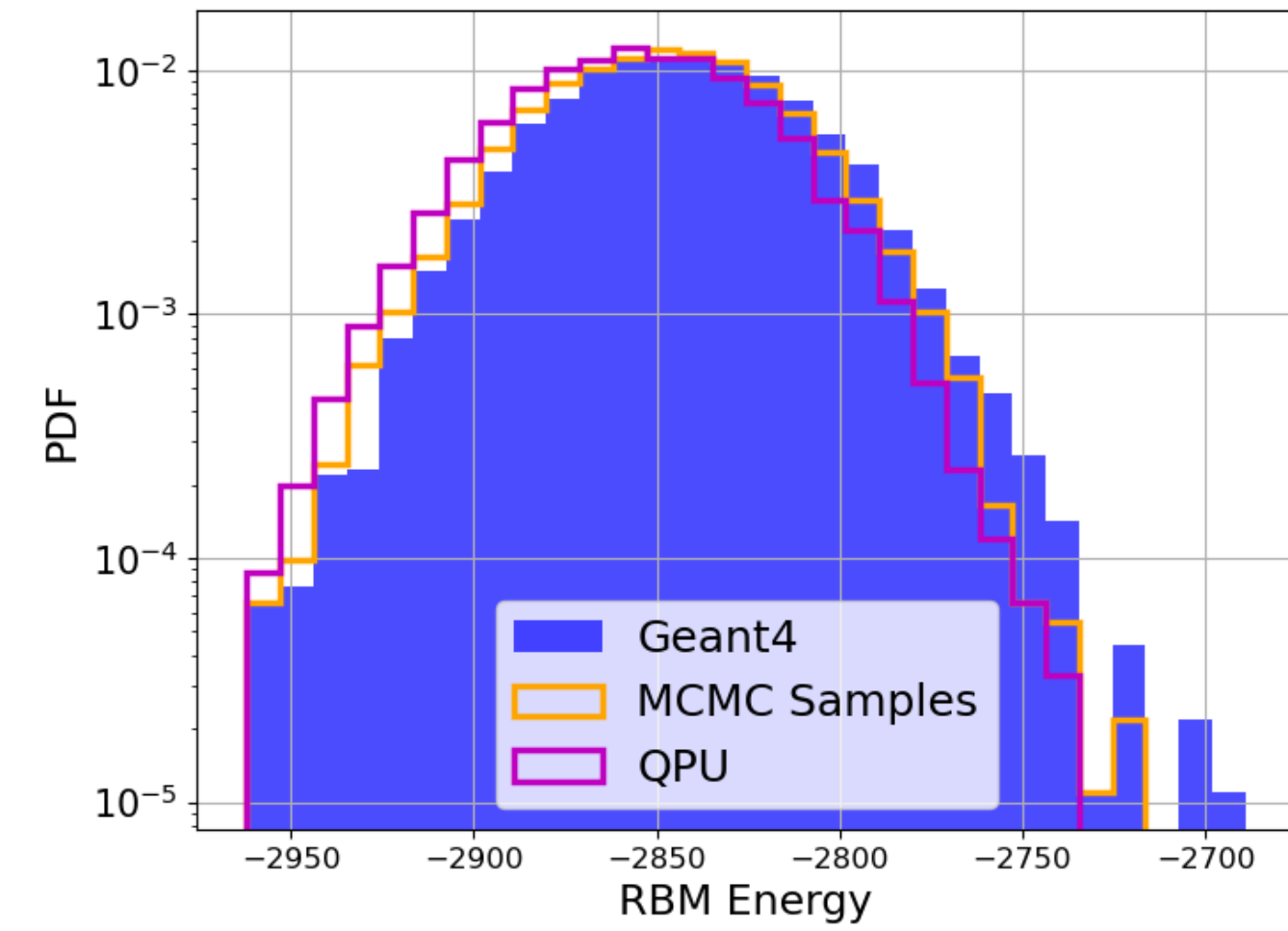
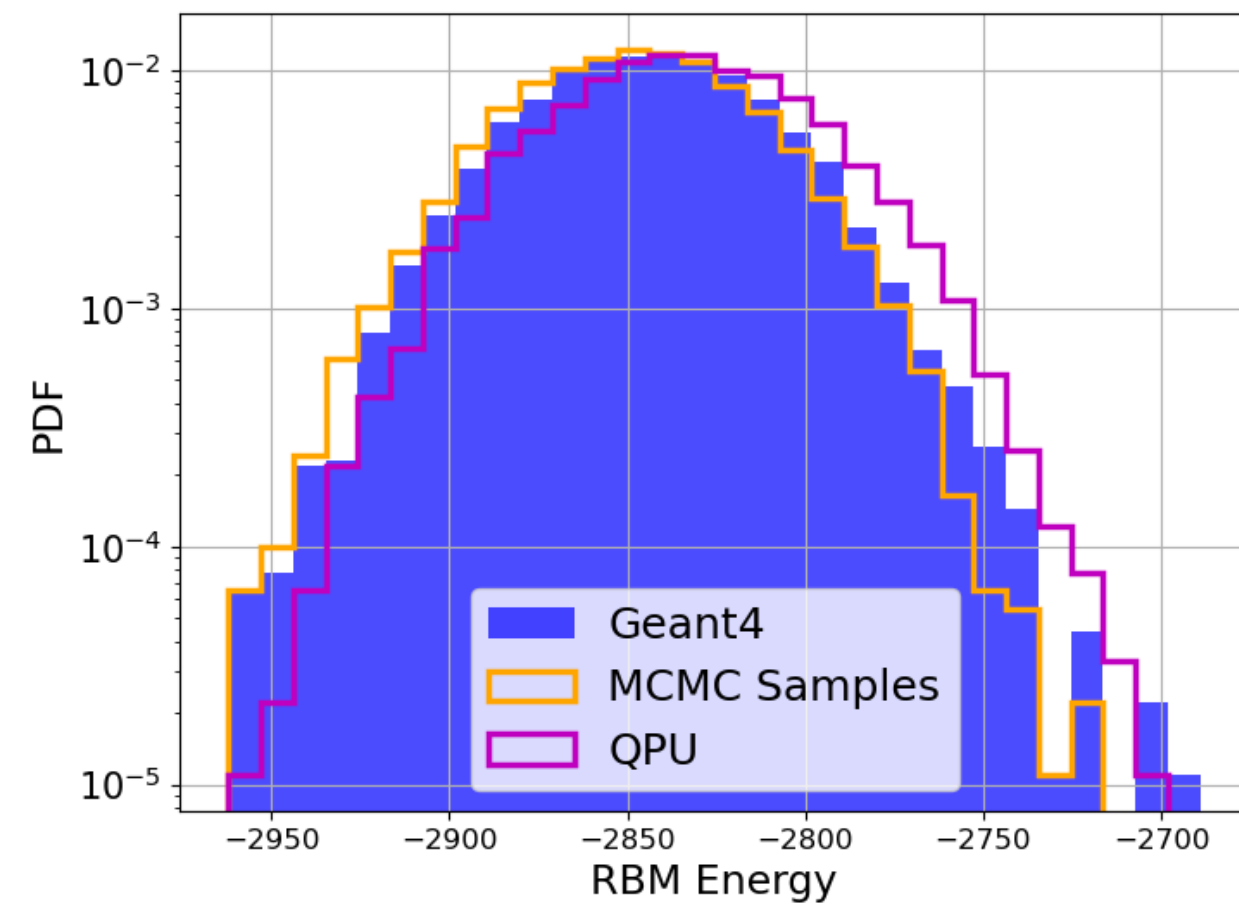


Model B

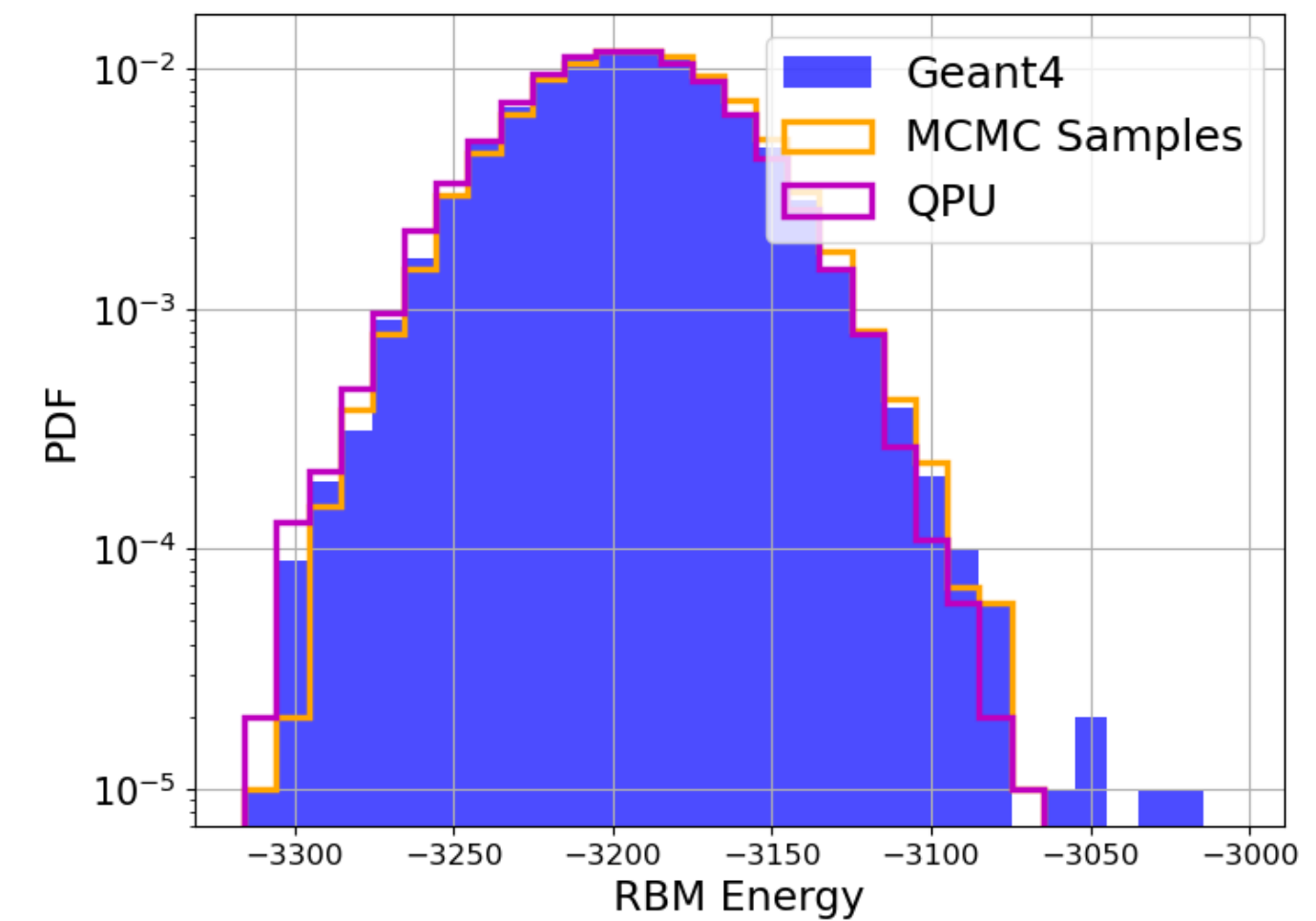
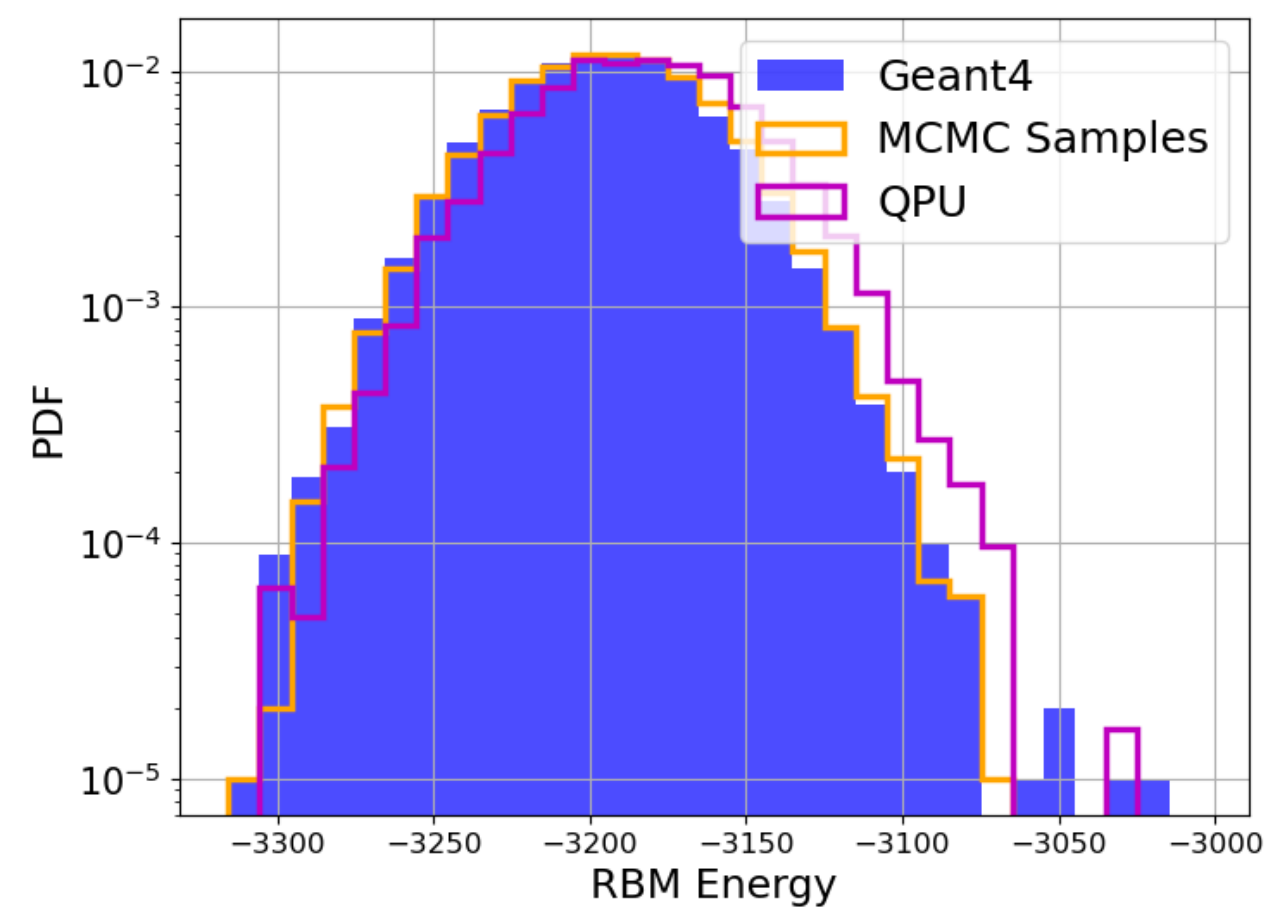


Using QPU w/ Zephyr :: vs Woitek's method

Model A

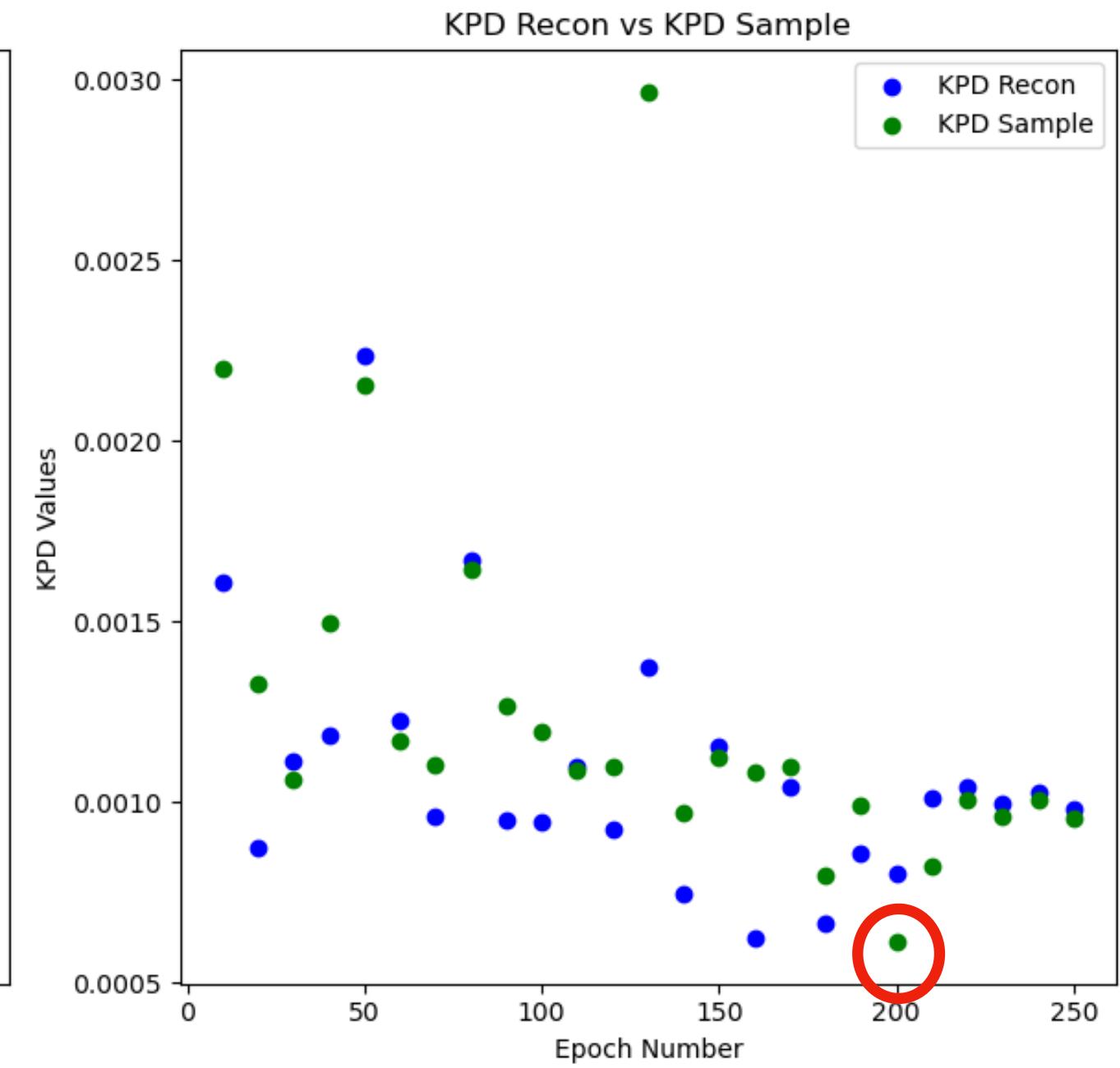
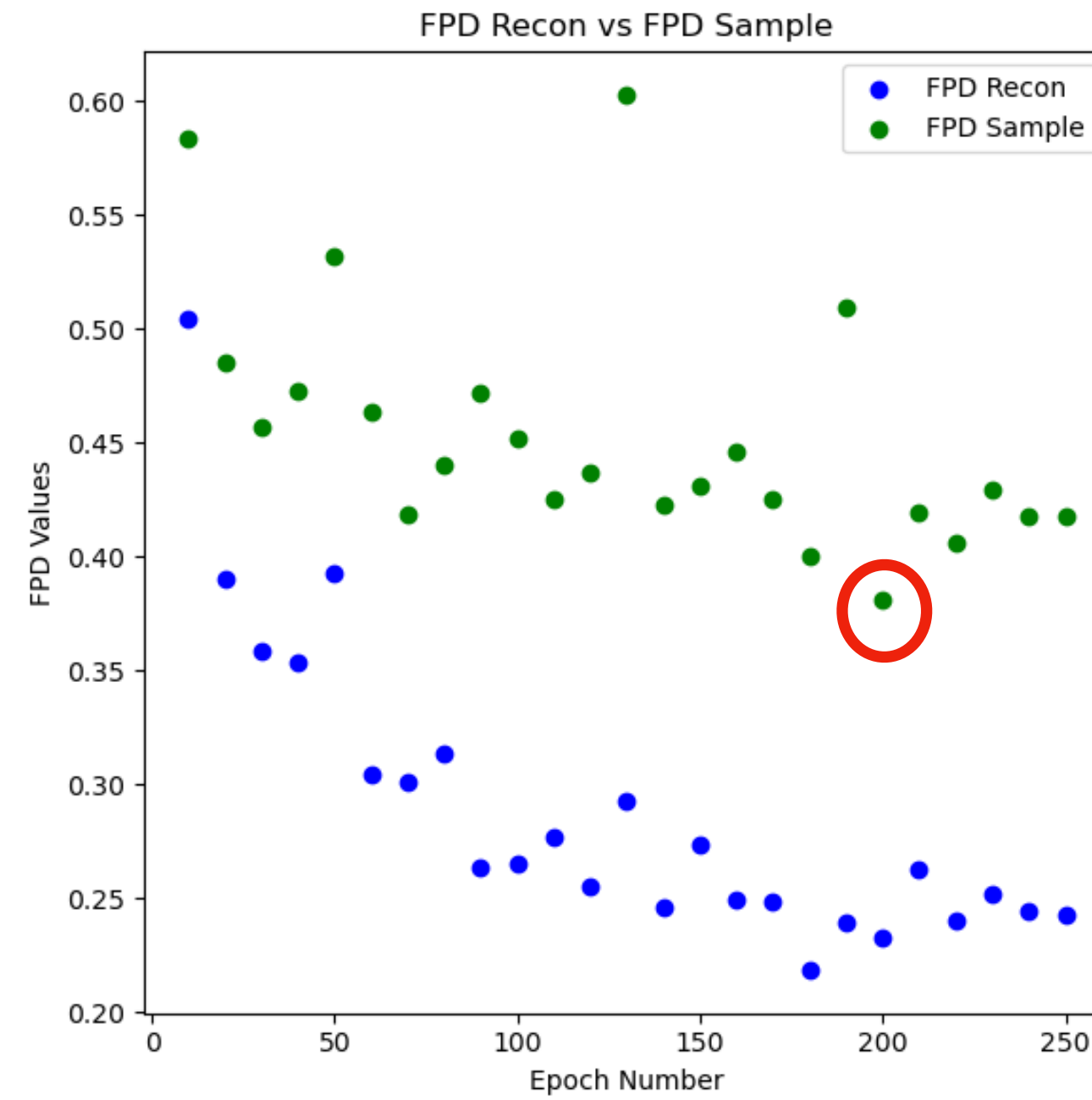
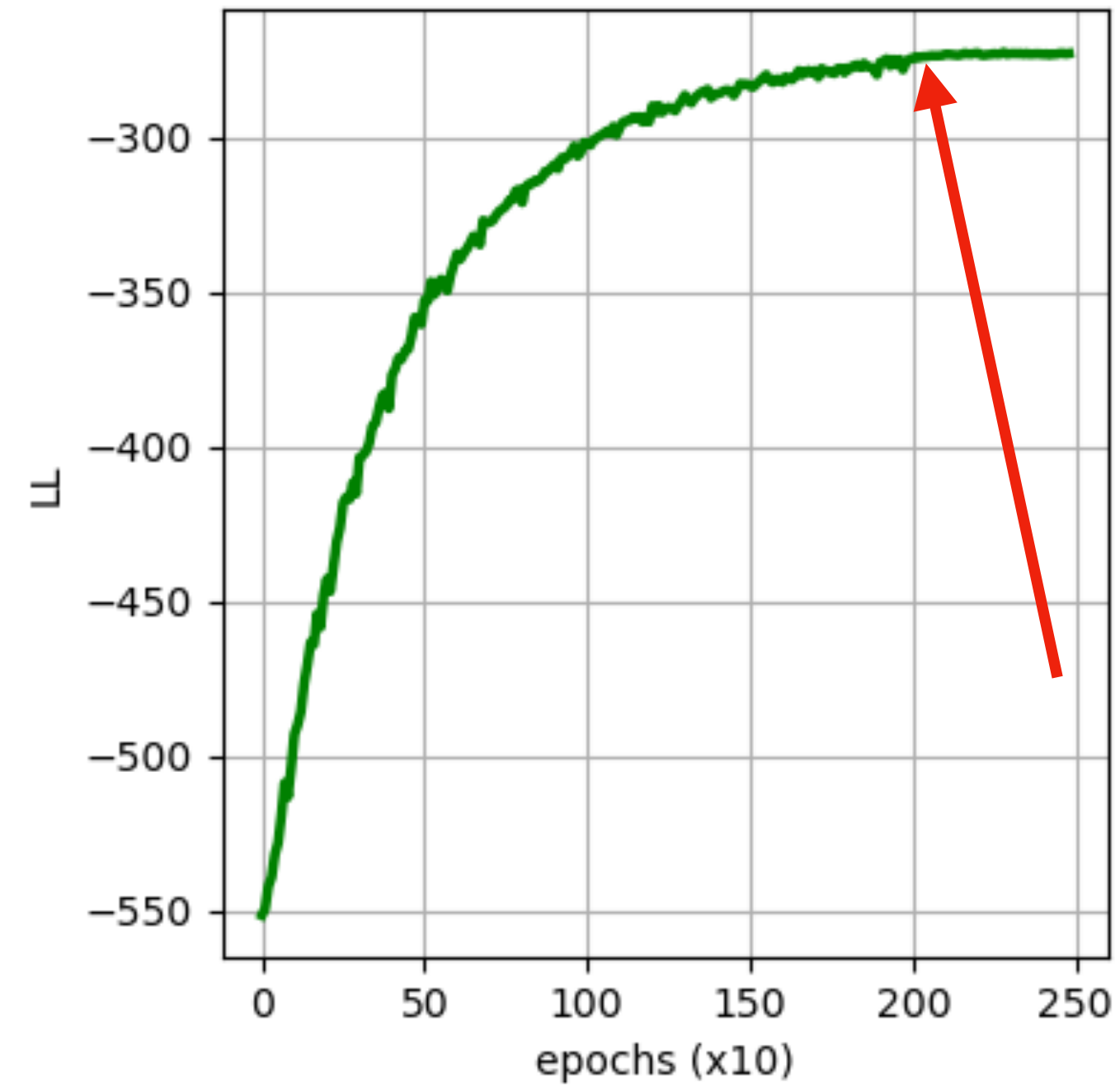


Model B



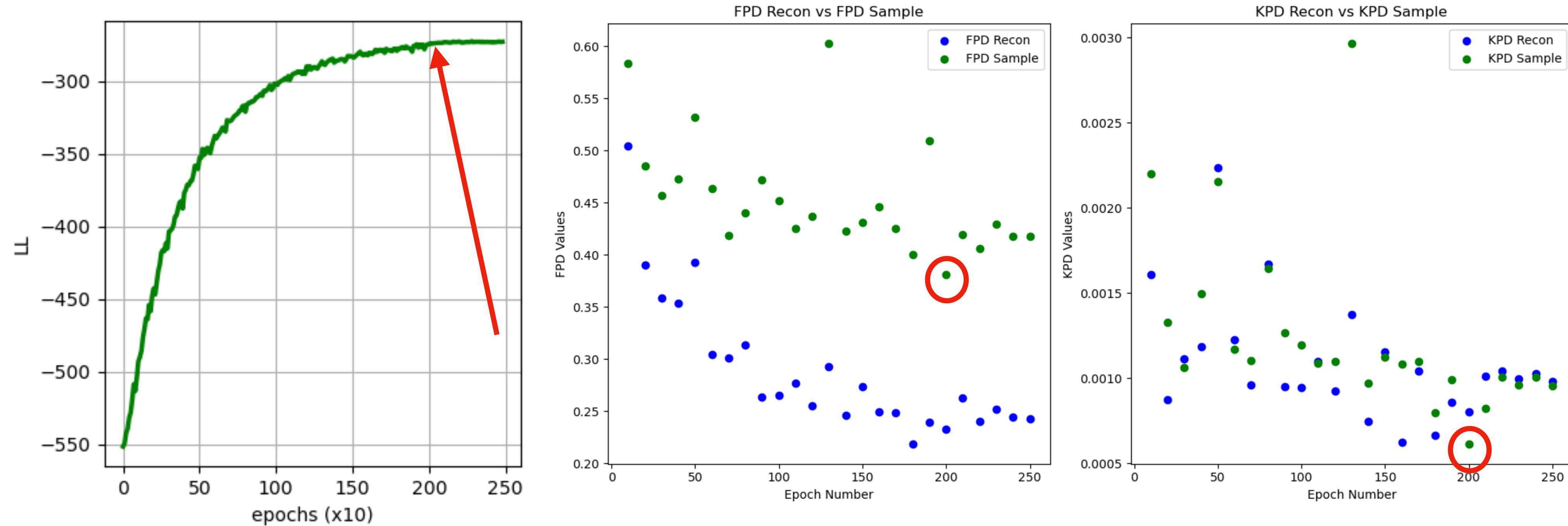
Using QPU w/ Zephyr :: vs Wojtek's method

Model B



Using QPU w/ Zephyr :: vs Wojtek's method

Model B



Time required to train using QPU:

$(1 \text{ sample generation time}) \times (\# \text{ of samples}) \times (\text{epochs})$

$(20\text{ms}) \times (100\text{k}) \times (200) = 111.1 \text{ hrs}$

Using QPU w/ Zephyr :: vs Wojtek's method

- Train Enc and Decoder and train QPU afterwards with a smaller sample.
- Discuss with dwave options and roadmaps

High Temperature gradient approximation

$$\left\langle E \frac{\partial E}{\partial \Theta} \right\rangle - \langle E \rangle \left\langle \frac{\partial E}{\partial \Theta} \right\rangle = 0$$

Condition

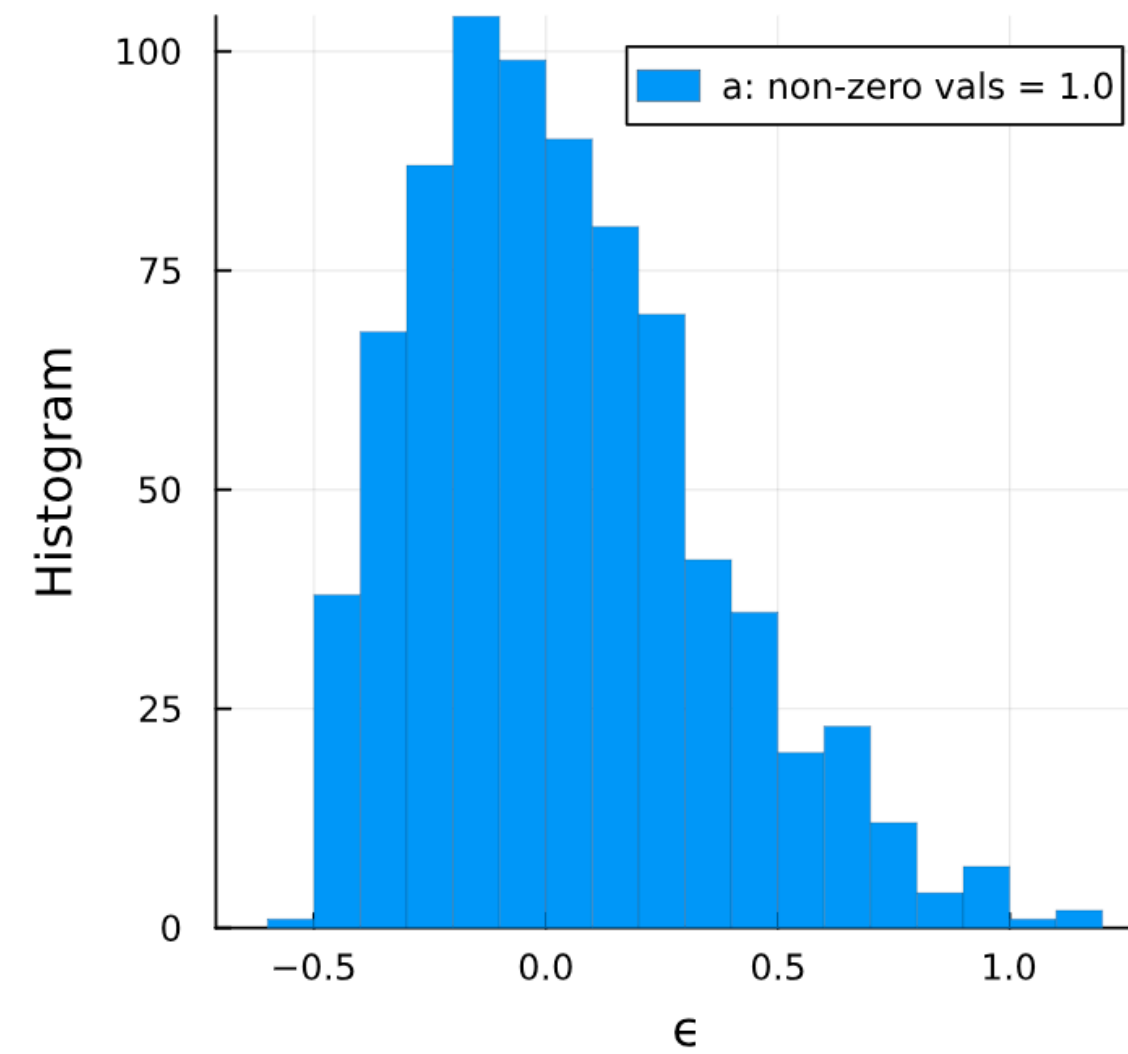
$$\epsilon = \frac{\left\langle E \frac{\partial E}{\partial \Theta} \right\rangle - \langle E \rangle \left\langle \frac{\partial E}{\partial \Theta} \right\rangle}{\left\langle \frac{\partial E}{\partial \Theta} \right\rangle}$$

1000 Gibbs sampling steps

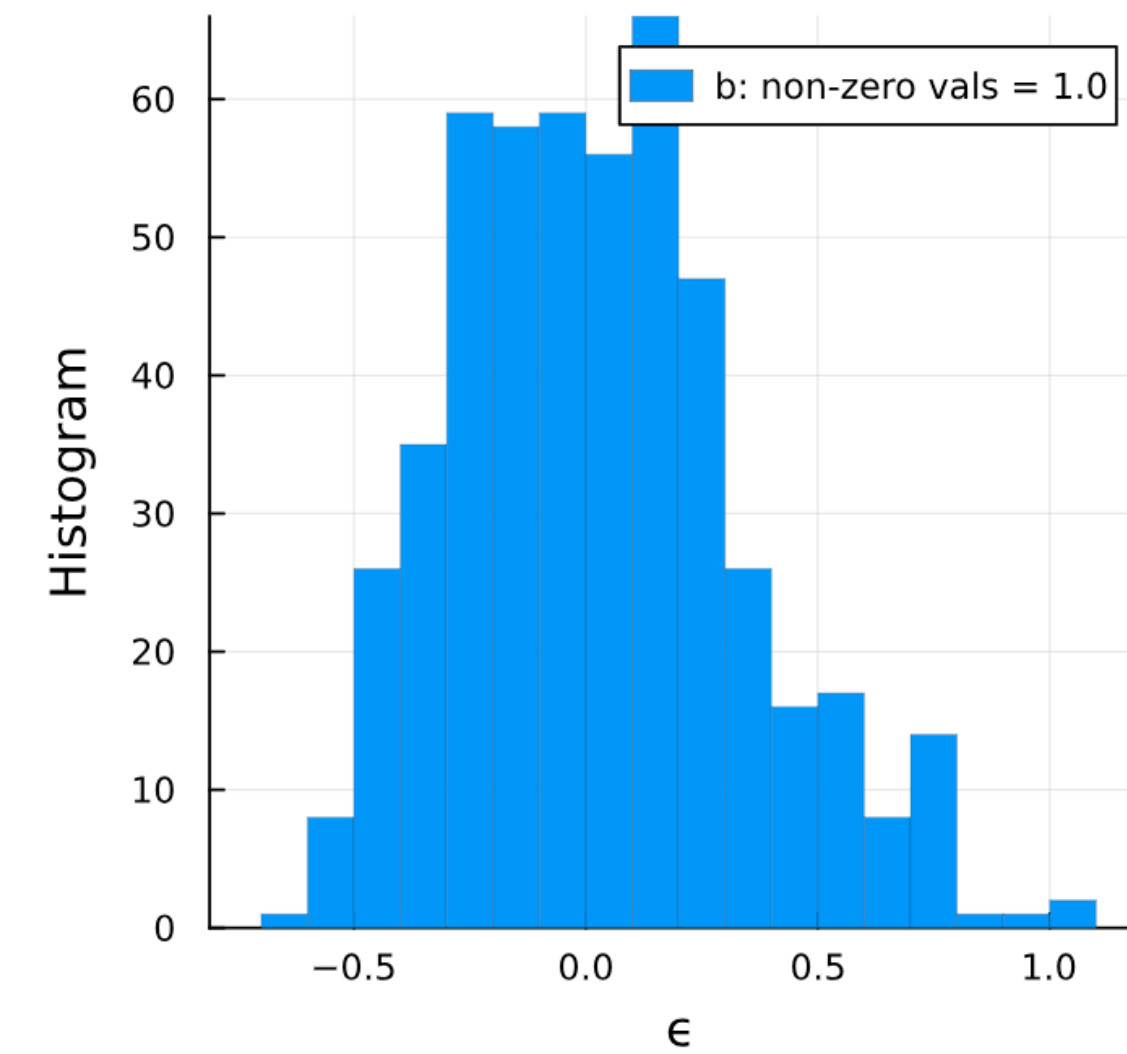
High Temperature gradient approximation

$$\epsilon = \frac{\langle E \frac{\partial E}{\partial \Theta} \rangle - \langle E \rangle \langle \frac{\partial E}{\partial \Theta} \rangle}{\langle \frac{\partial E}{\partial \Theta} \rangle}$$

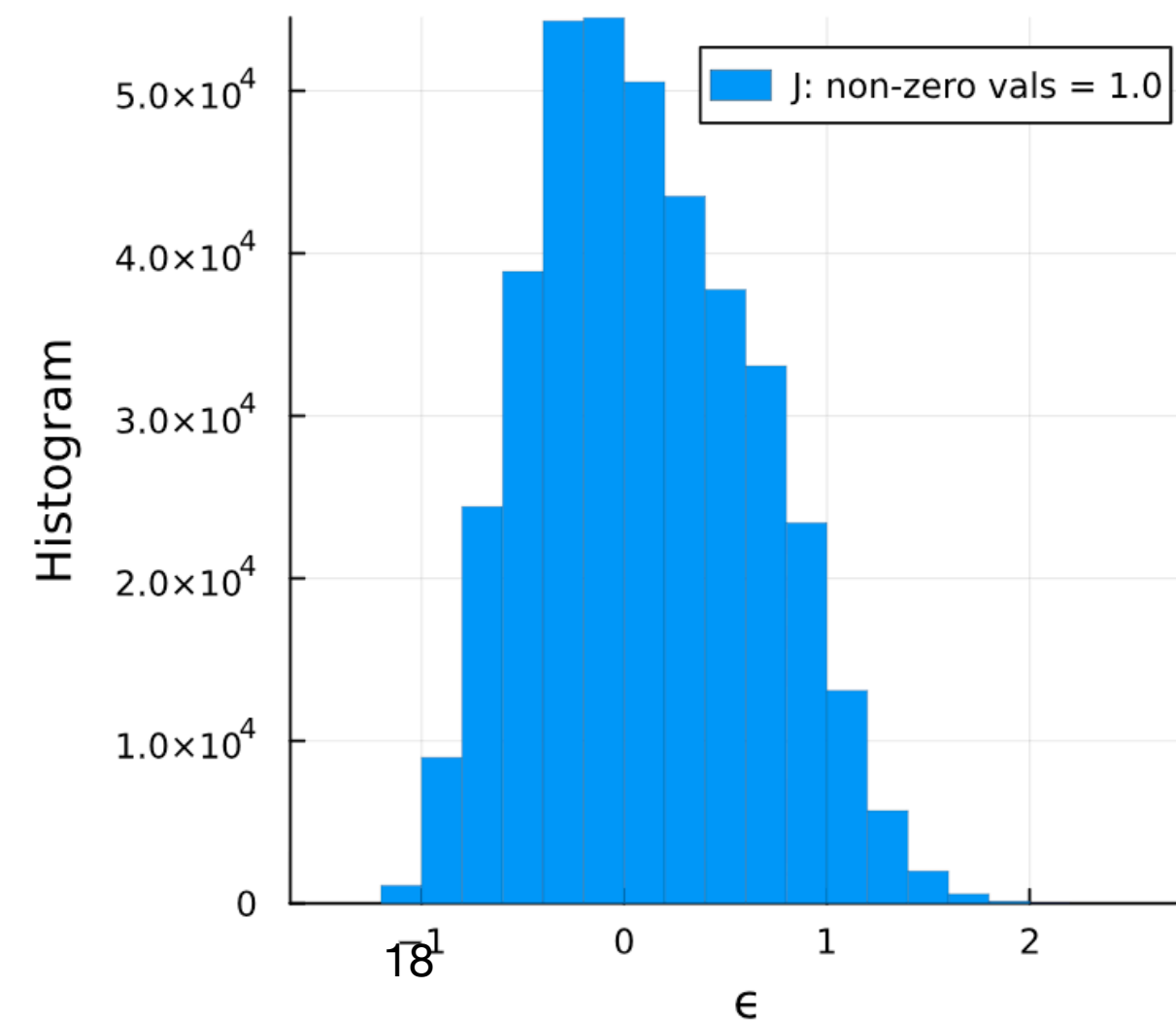
Untrained RBM



Untrained RBM

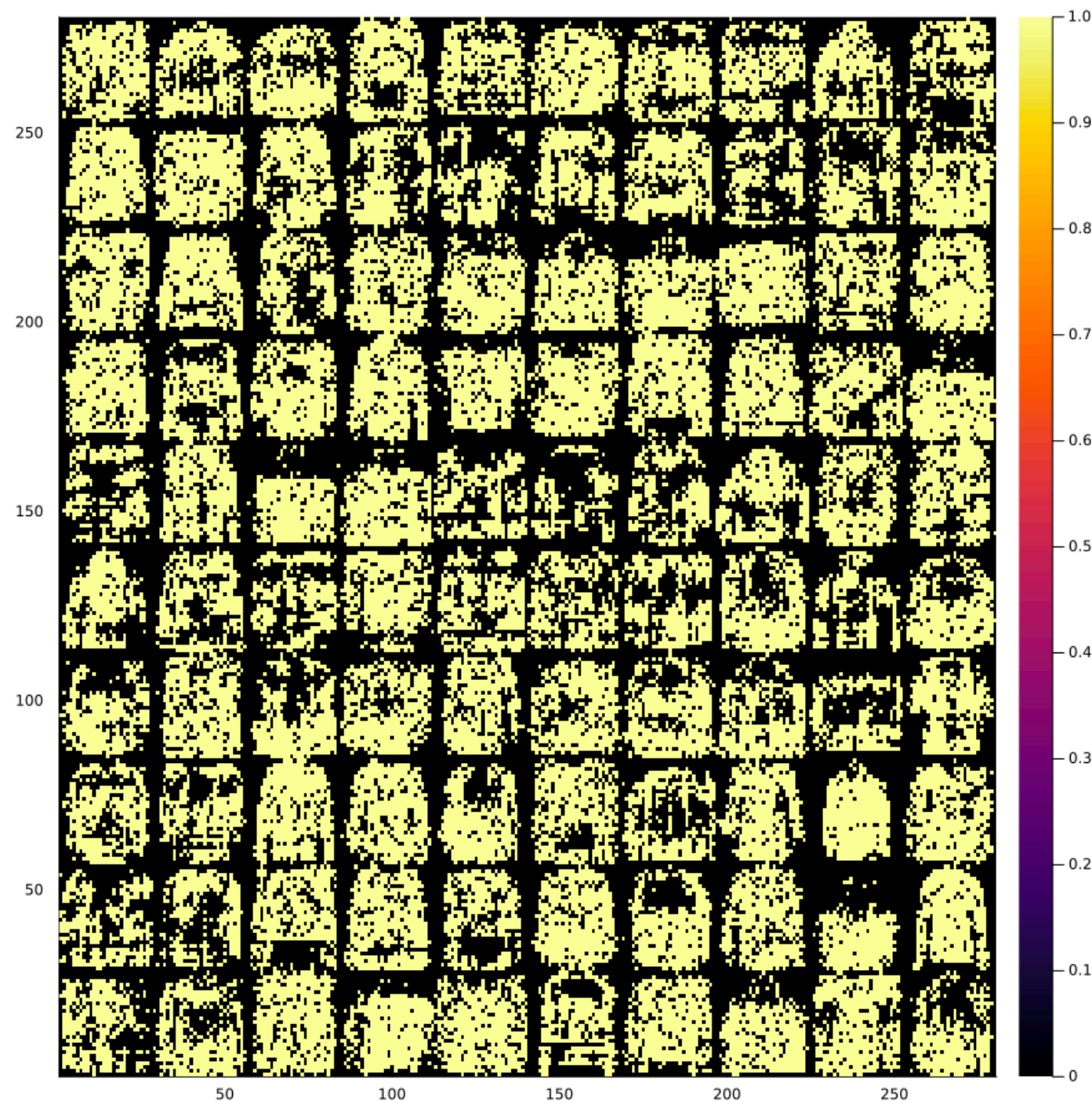


Untrained RBM

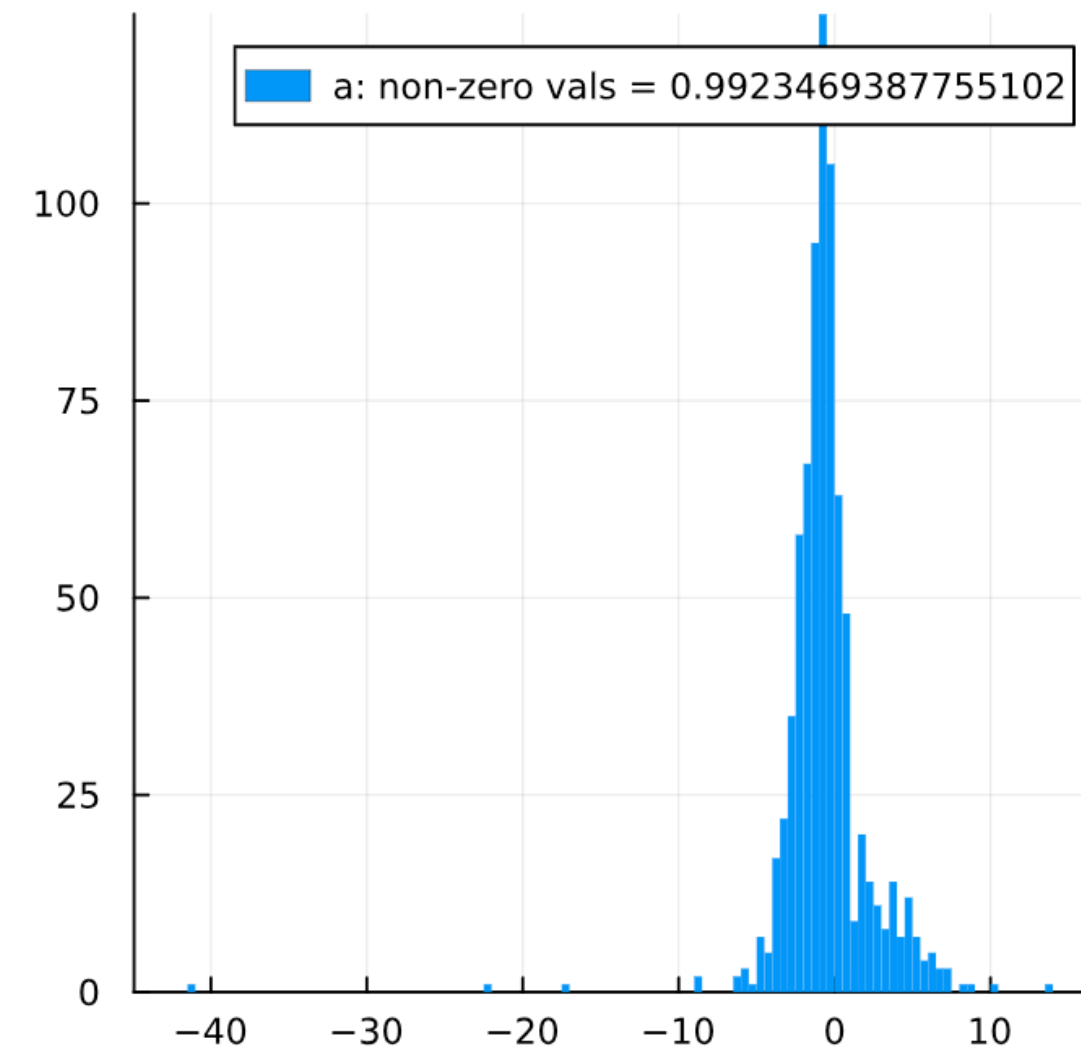


High Temperature gradient approximation

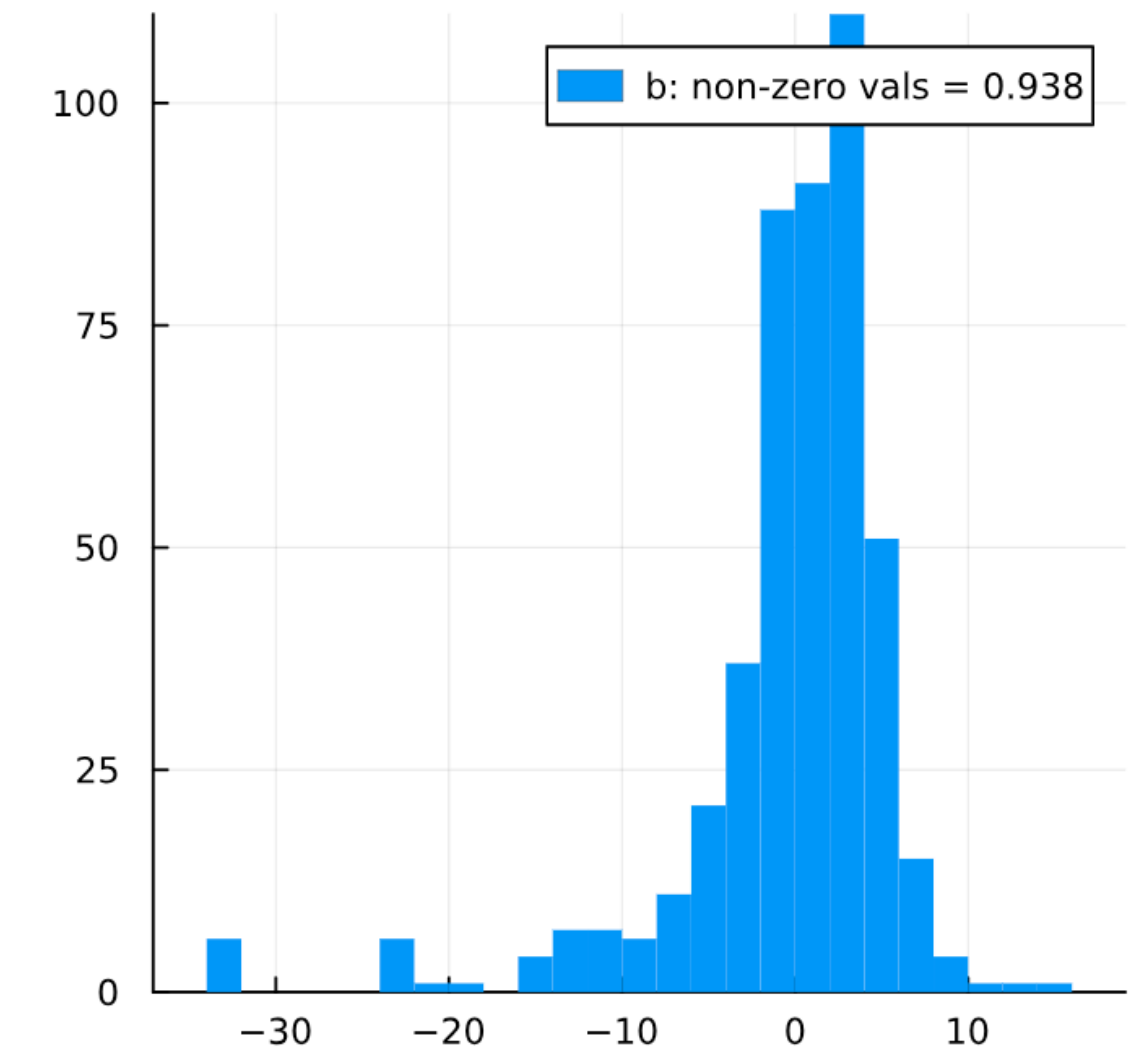
$$\epsilon = \frac{\langle E \frac{\partial E}{\partial \Theta} \rangle - \langle E \rangle \langle \frac{\partial E}{\partial \Theta} \rangle}{\langle \frac{\partial E}{\partial \Theta} \rangle}$$



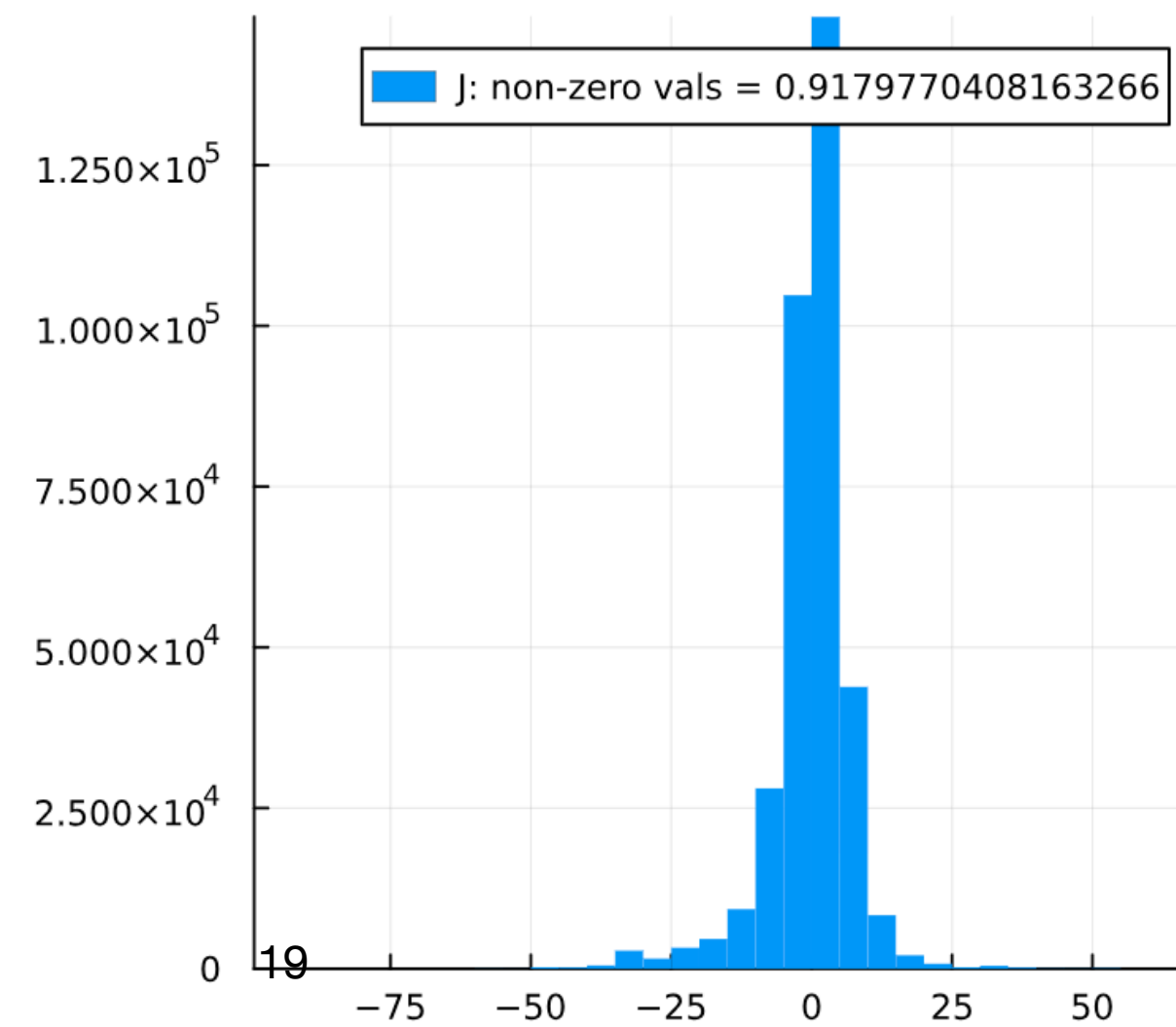
Trained RBMin FMNIST w/ CD



Trained RBMin FMNIST w/ CD

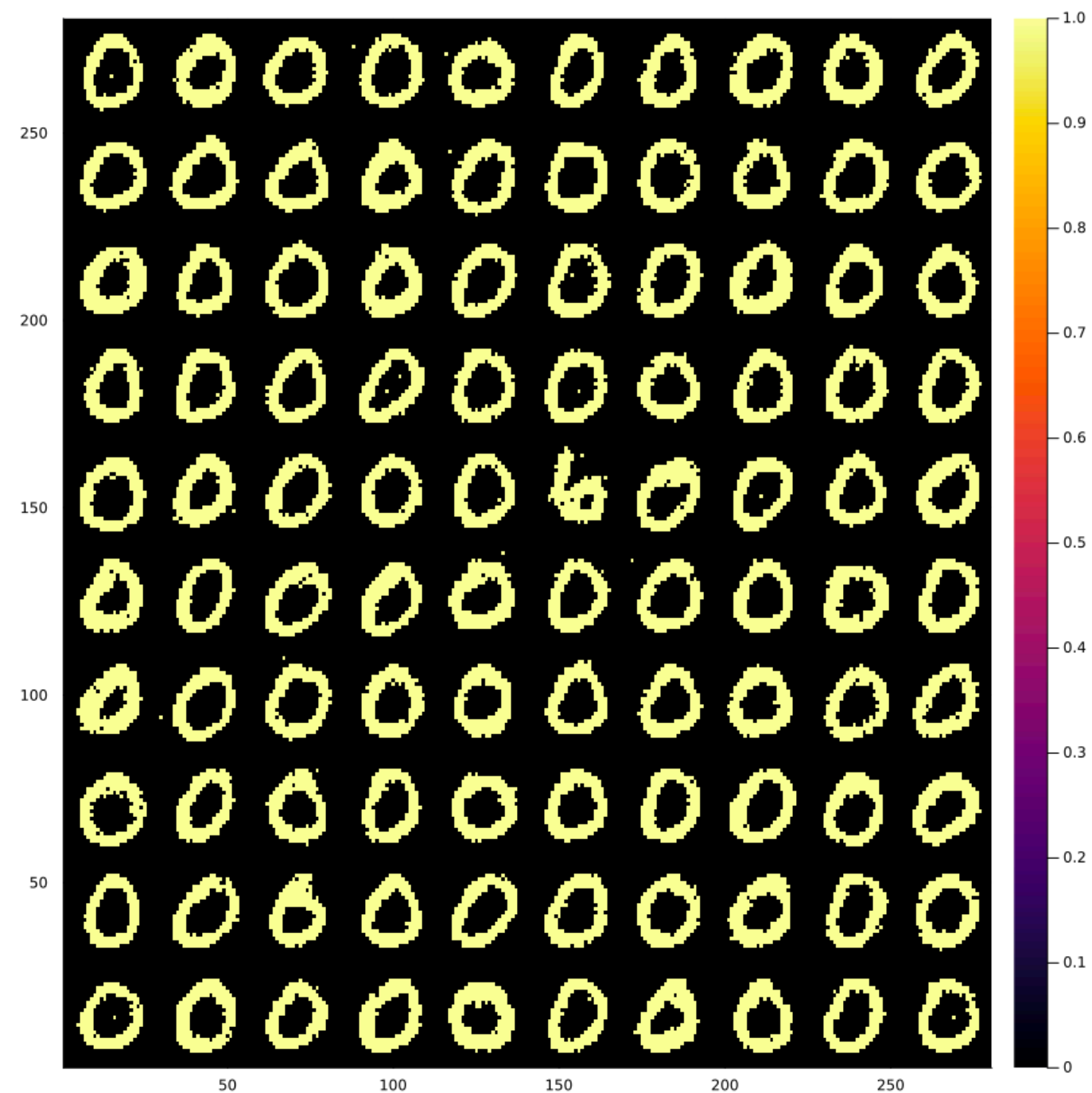


Trained RBMin FMNIST w/ CD

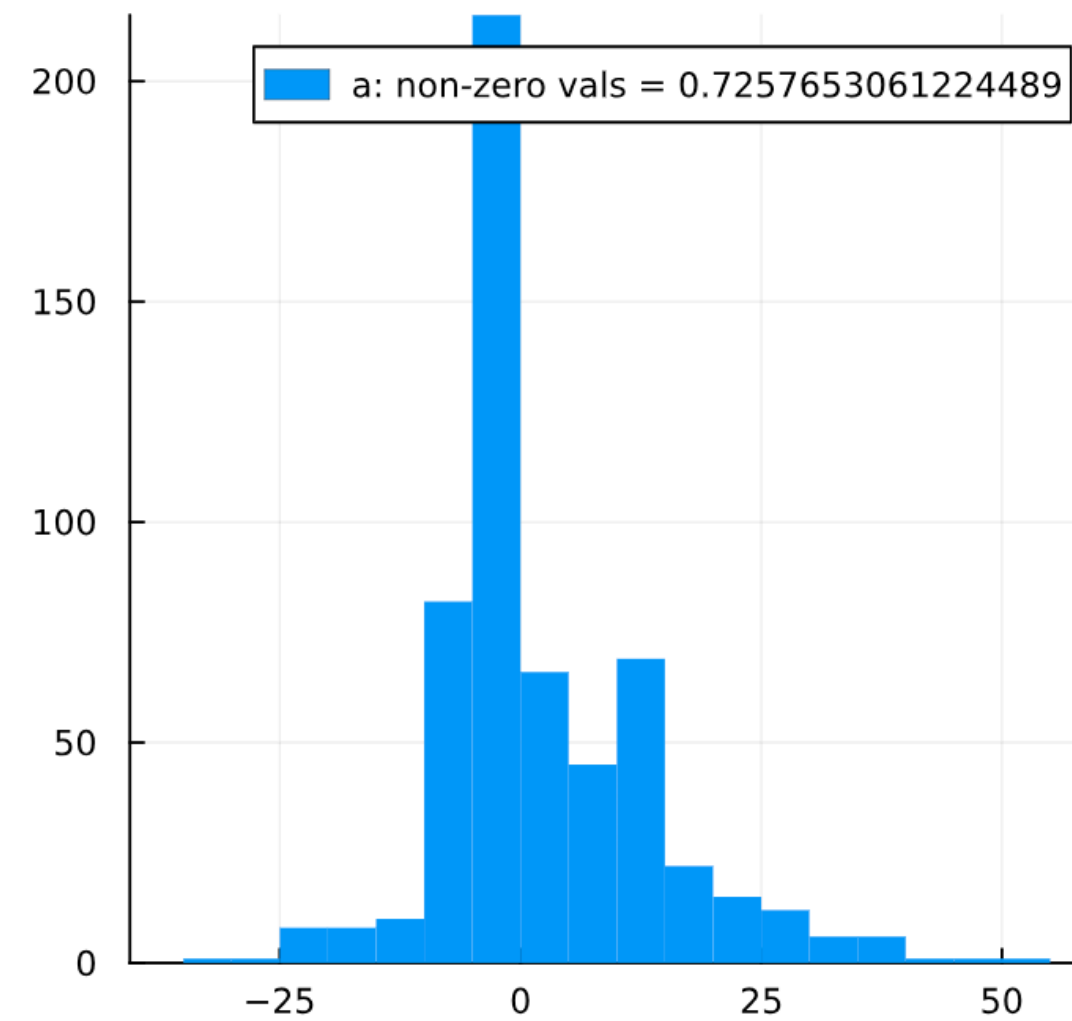


High Temperature gradient approximation

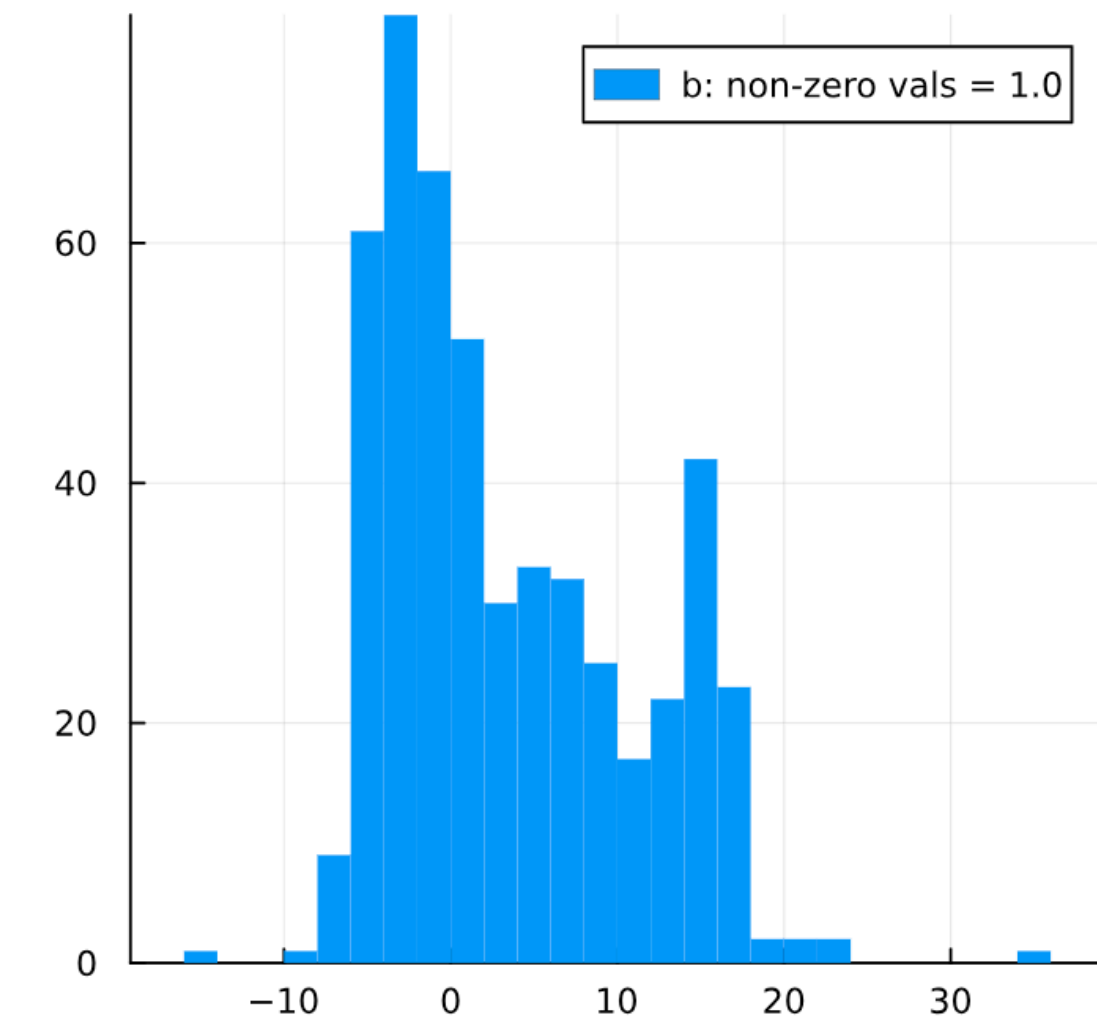
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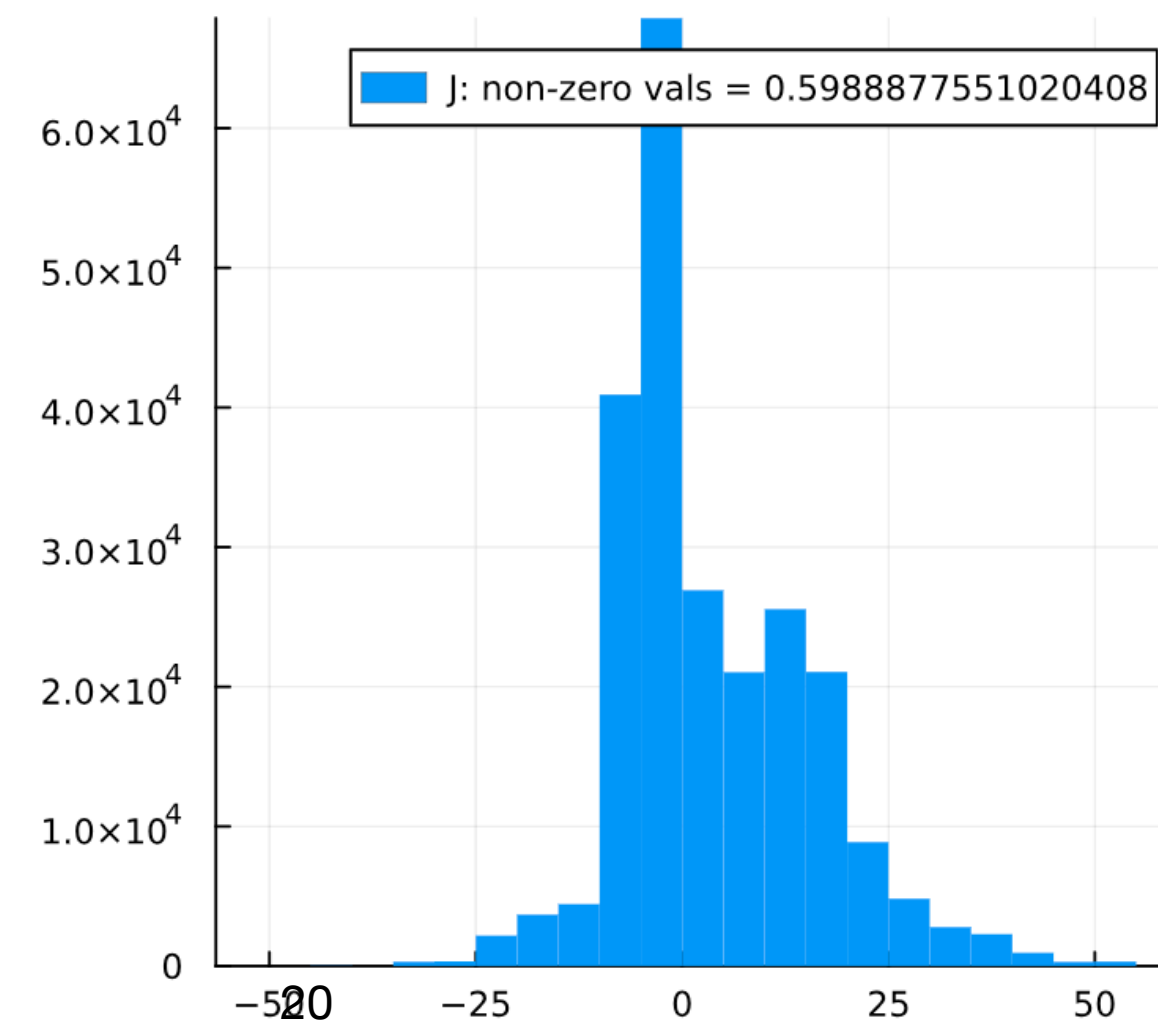
Trained RBMin MNIST w/ CD



Trained RBMin MNIST w/ CD

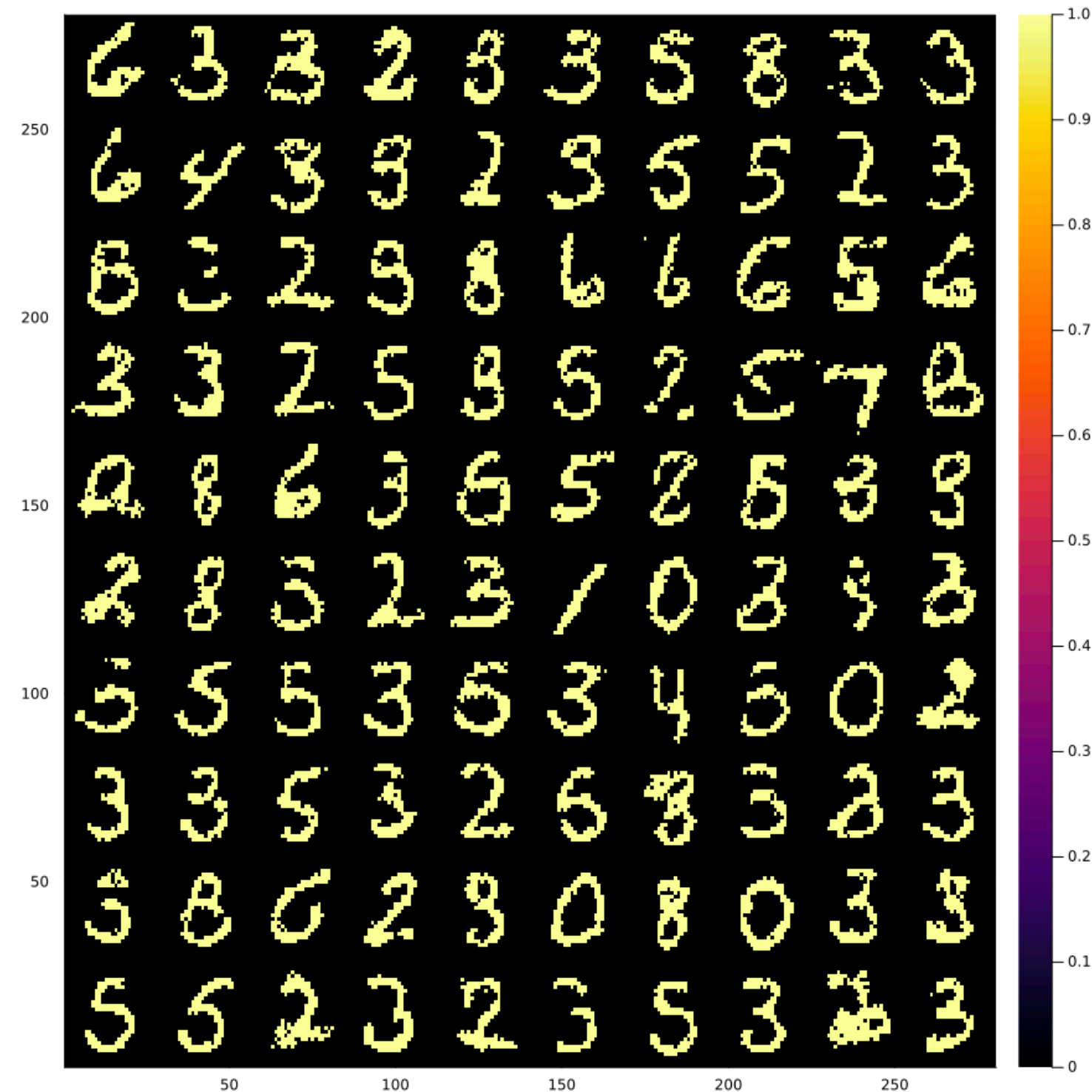


Trained RBMin MNIST w/ CD

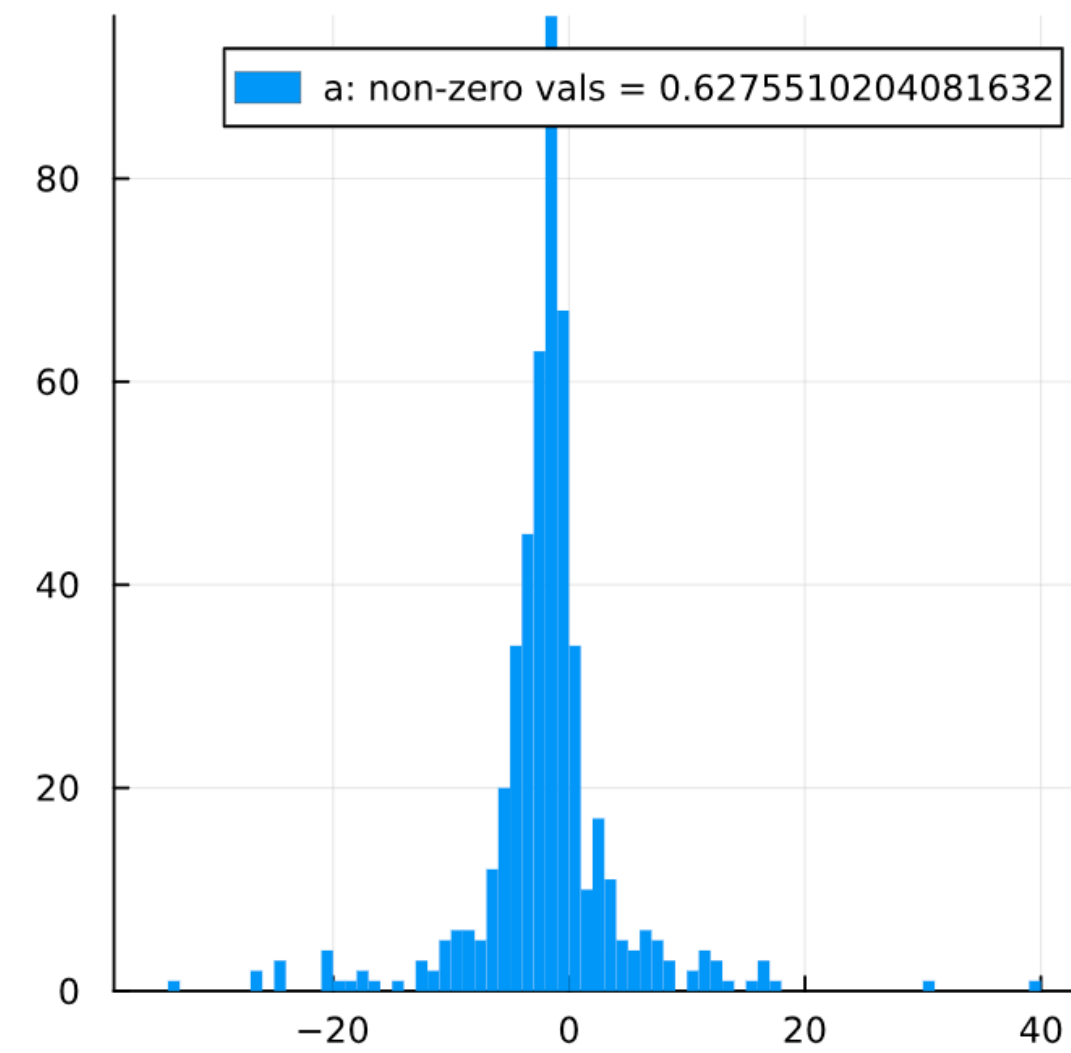


High Temperature gradient approximation

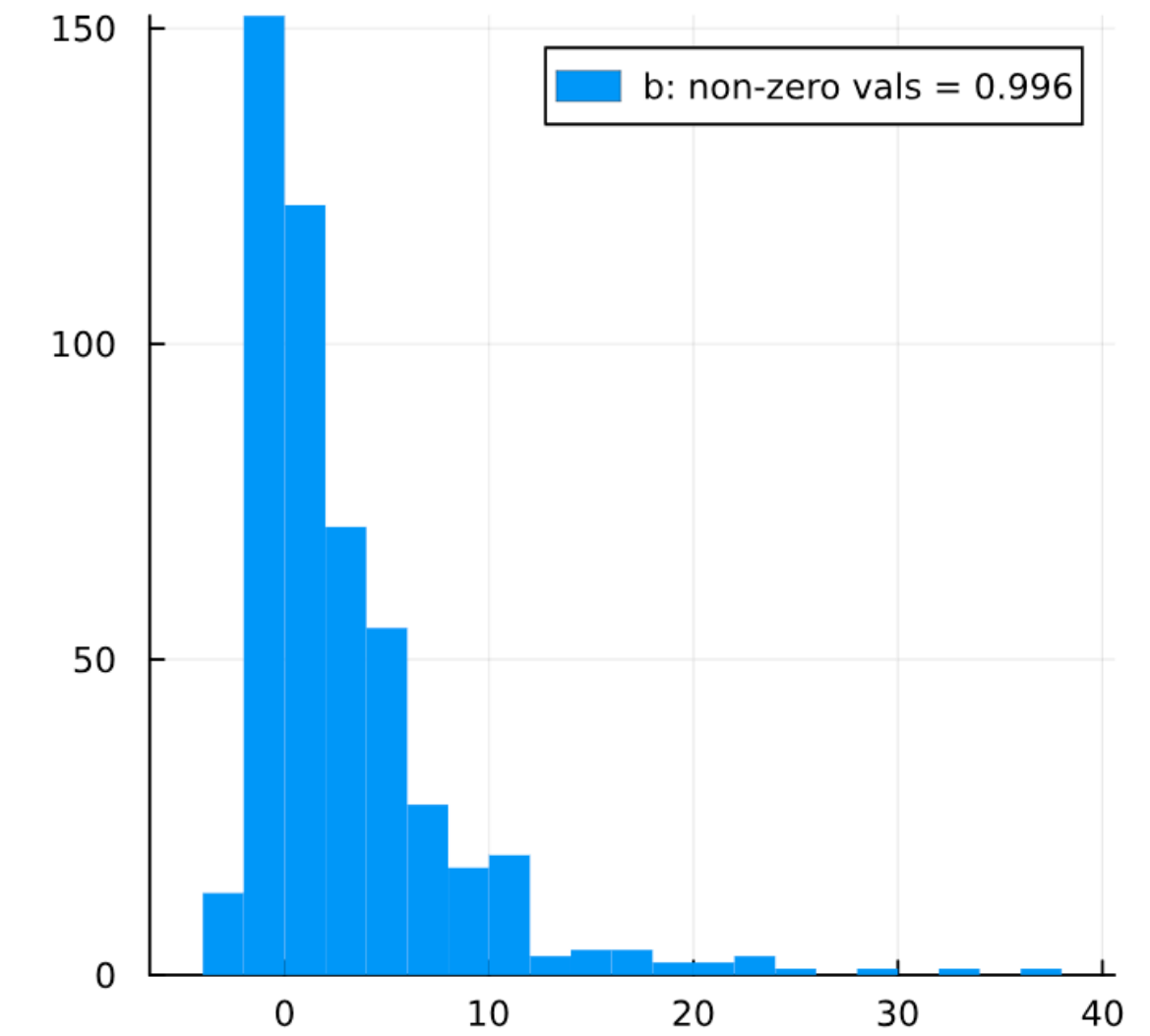
$$\epsilon = \frac{\langle E \frac{\partial E}{\partial \Theta} \rangle - \langle E \rangle \langle \frac{\partial E}{\partial \Theta} \rangle}{\langle \frac{\partial E}{\partial \Theta} \rangle}$$



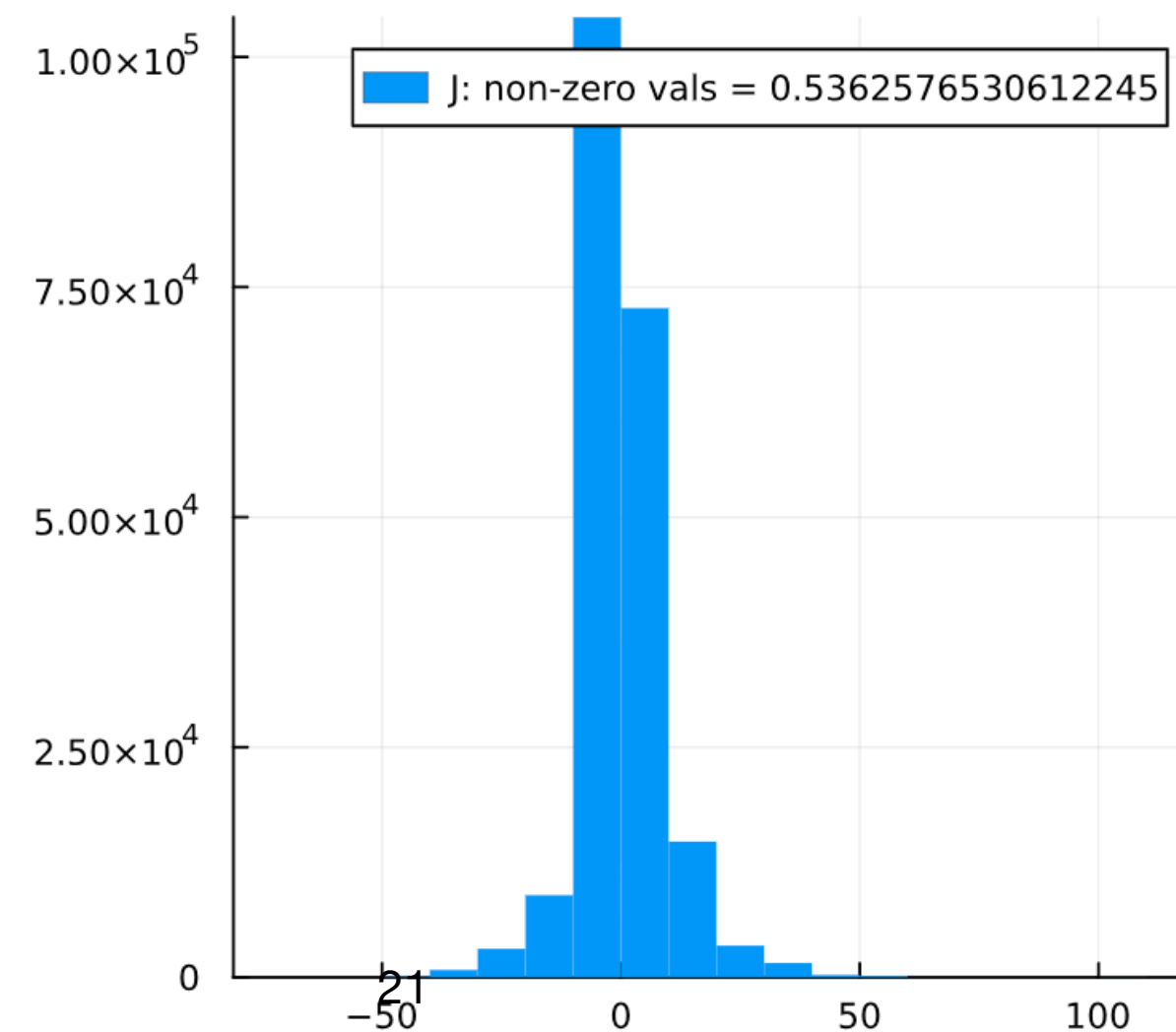
Trained RBM in MNIST w/ PCD



Trained RBM in MNIST w/ PCD



Trained RBM in MNIST w/ PCD

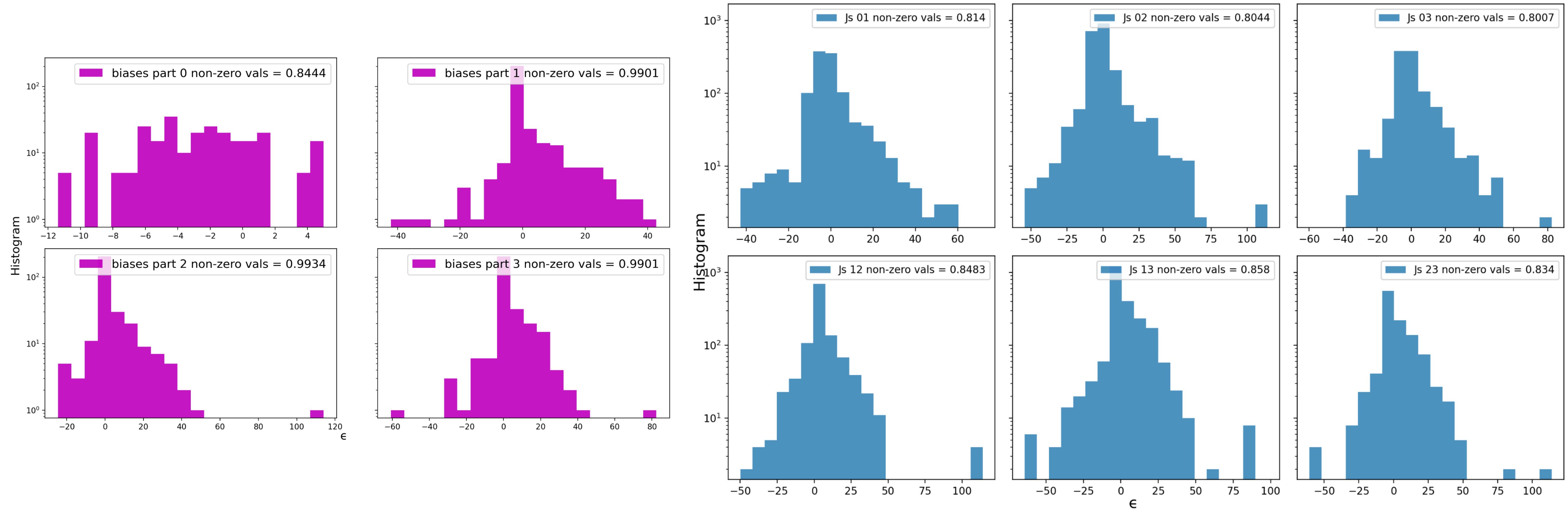


High Temperature gradient approximation

Each point in the histogram corresponds to a parameter being updated *separately* from the rest.

High Temperature gradient approximation

CaloQVAE Model B



High Temperature gradient approximation

Small RBMs

Let's assume an RBM w/ 10 visible and 10 hidden nodes.

$$\epsilon = \frac{\langle E \frac{\partial E}{\partial \Theta} \rangle - \langle E \rangle \langle \frac{\partial E}{\partial \Theta} \rangle}{\langle \frac{\partial E}{\partial \Theta} \rangle}$$

High Temperature gradient approximation

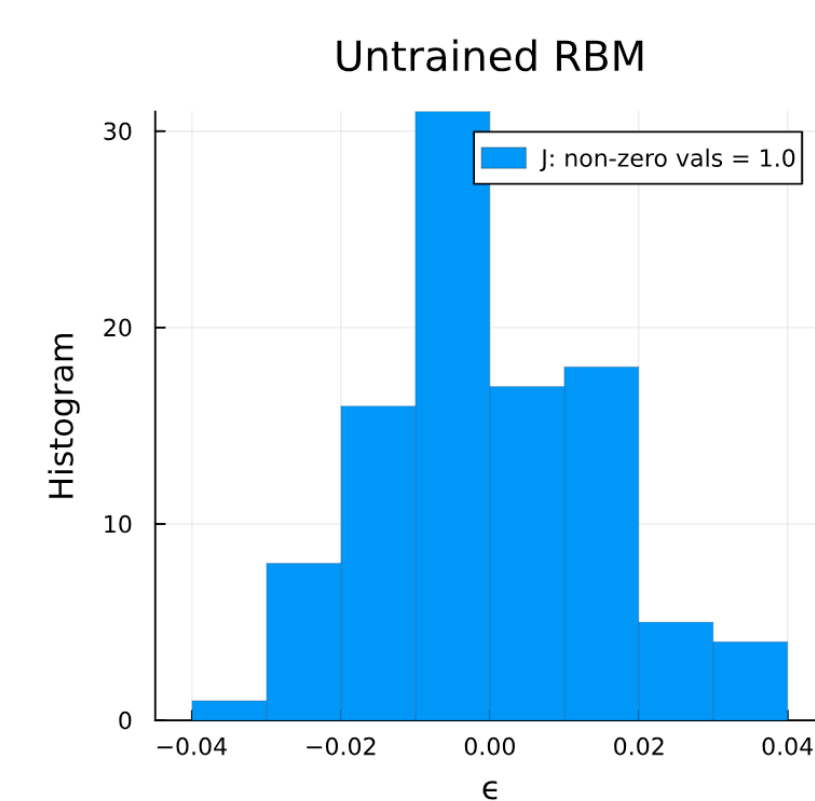
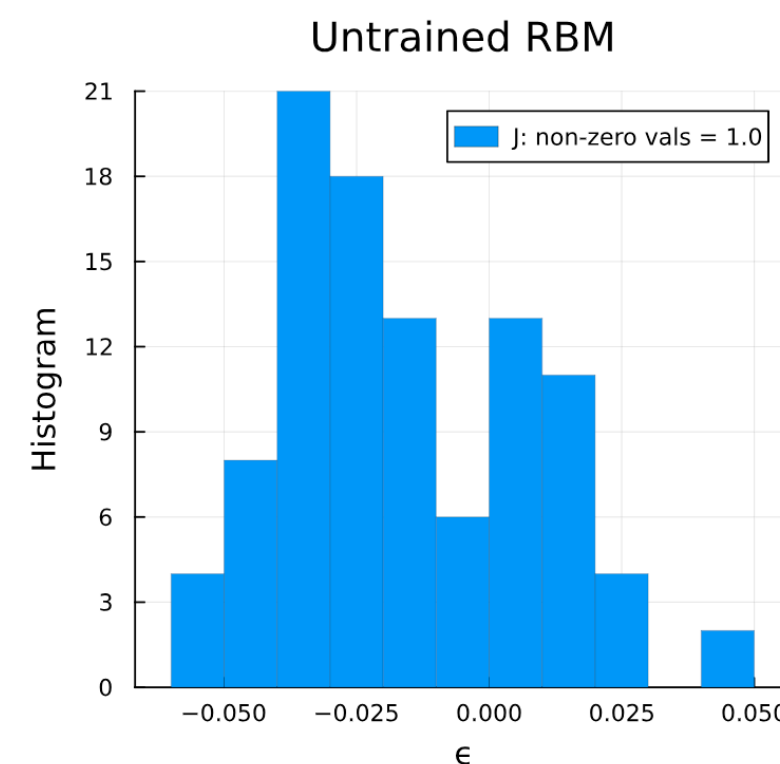
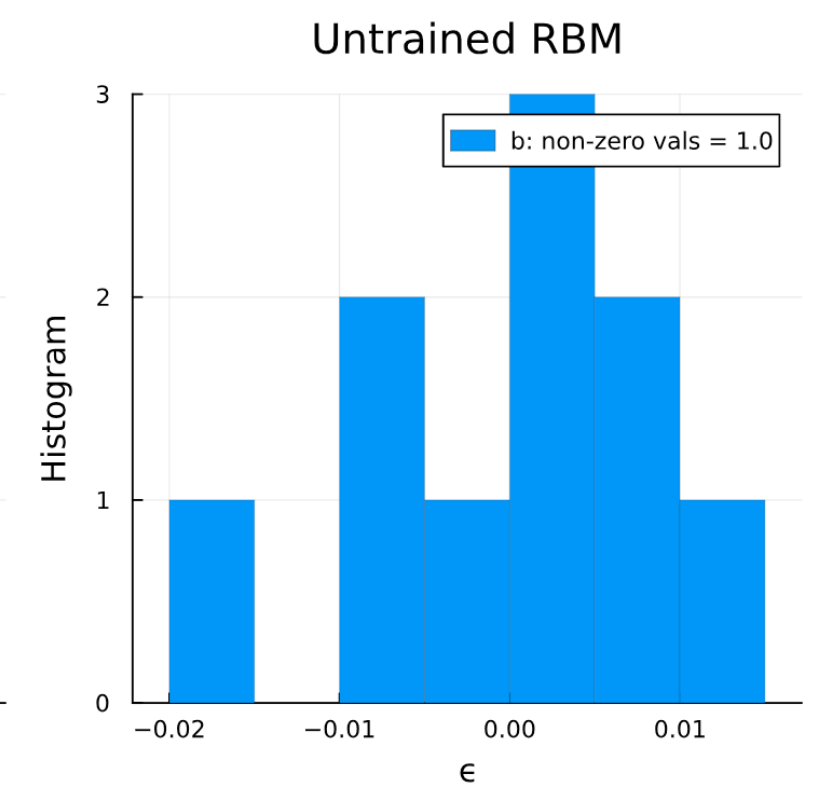
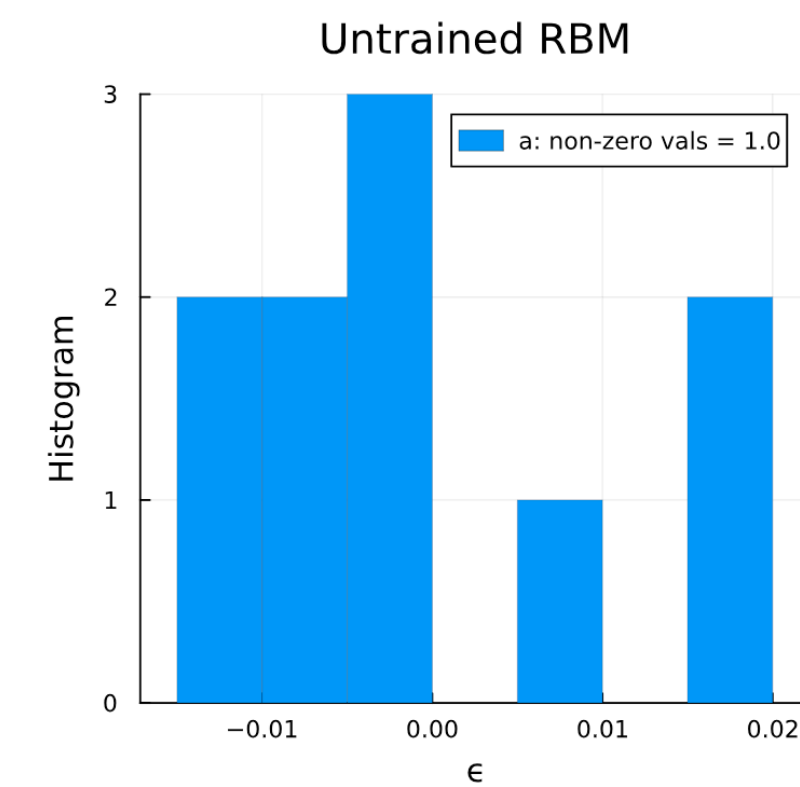
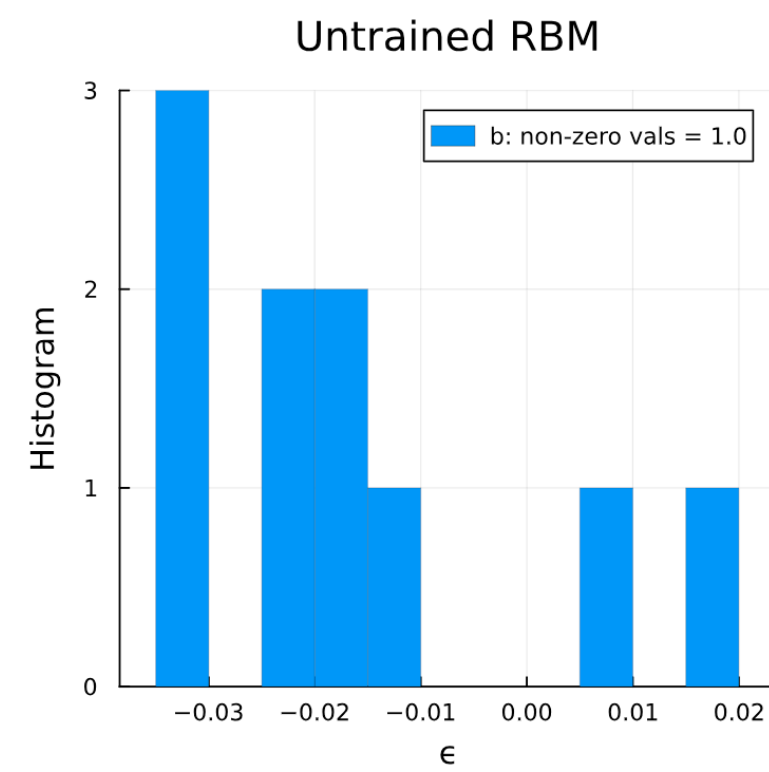
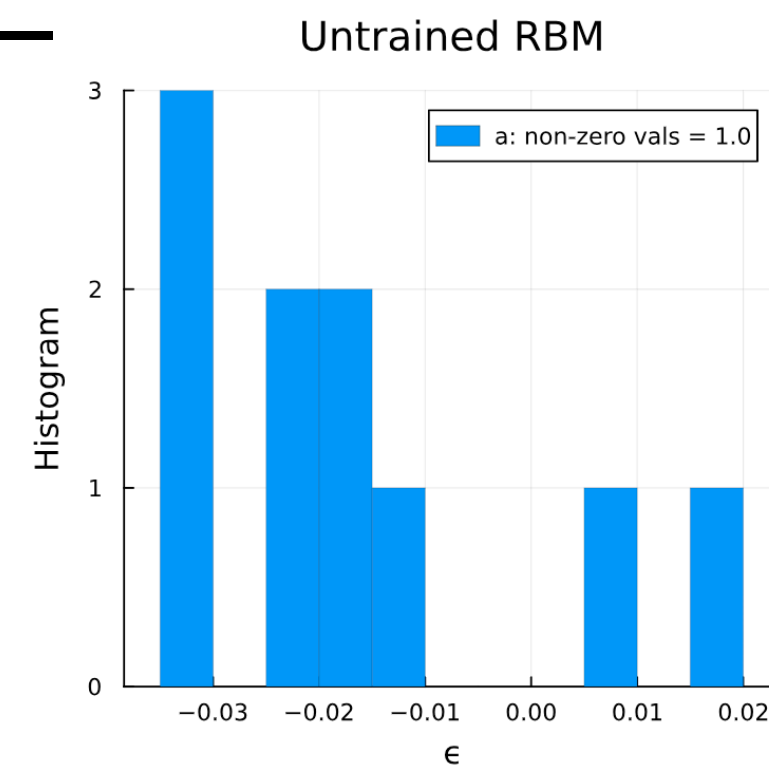
Small RBMs

Let's assume the weights and biases are sampled from a normal $N(0,0.1)$

$$\epsilon = \frac{\langle E \frac{\partial E}{\partial \Theta} \rangle - \langle E \rangle \langle \frac{\partial E}{\partial \Theta} \rangle}{\langle \frac{\partial E}{\partial \Theta} \rangle}$$

Exact

BGS



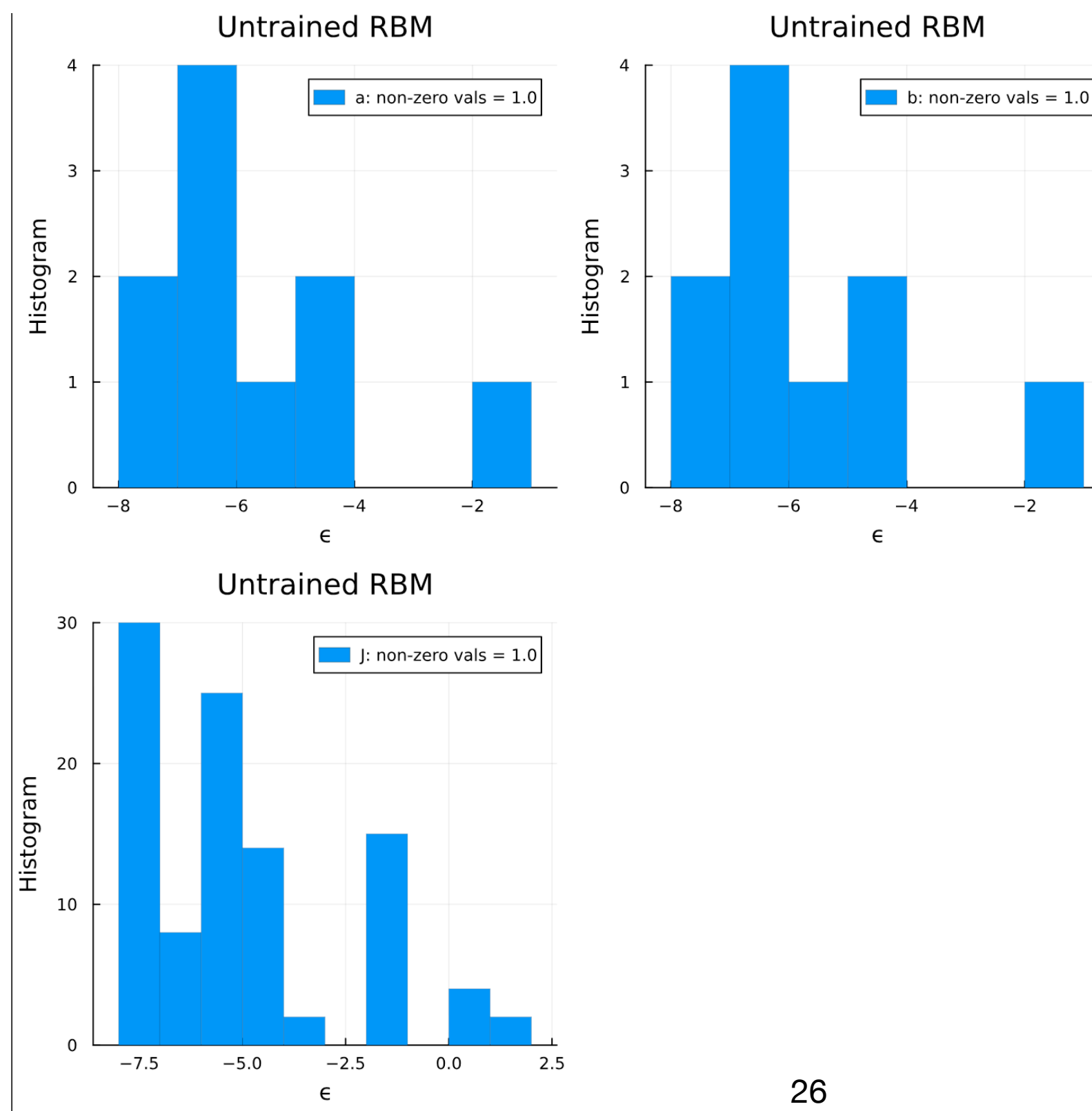
High Temperature gradient approximation

Small RBMs

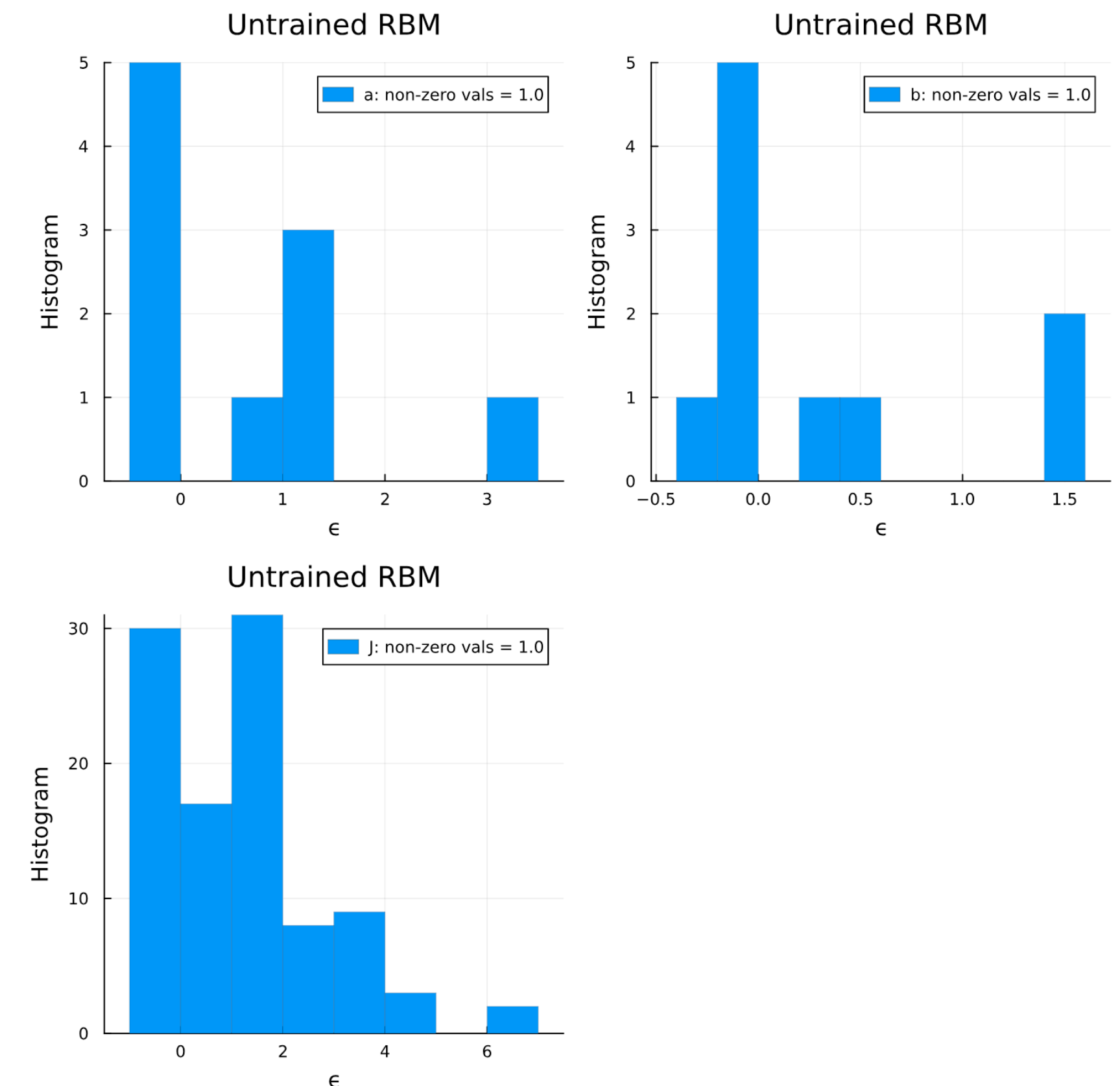
Let's assume the weights and biases are sampled from a Uni(-1,1)

$$\epsilon = \frac{\langle E \frac{\partial E}{\partial \Theta} \rangle - \langle E \rangle \langle \frac{\partial E}{\partial \Theta} \rangle}{\langle \frac{\partial E}{\partial \Theta} \rangle}$$

Exact



BGS



High Temperature gradient approximation

Small RBMs

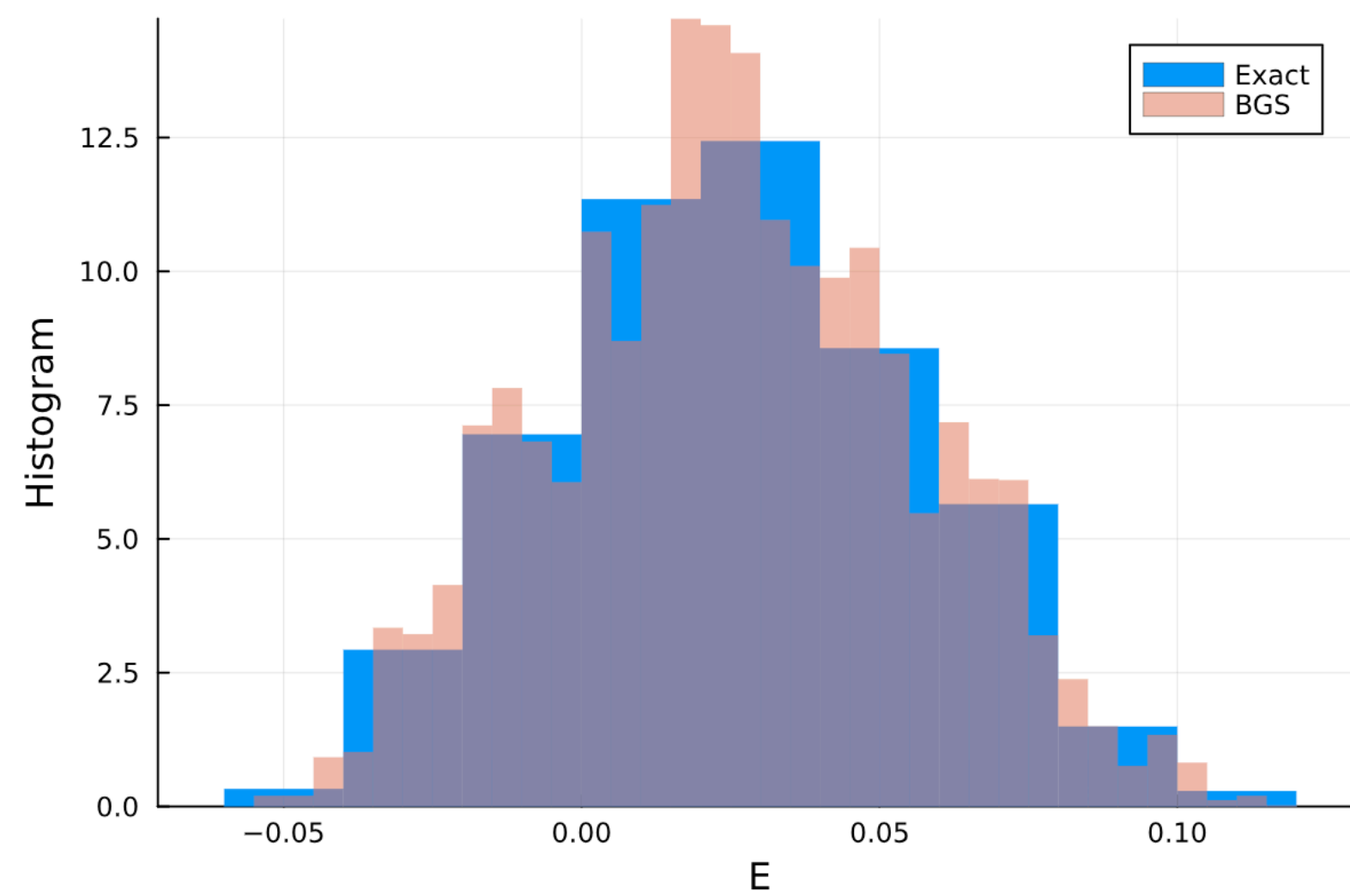
For Uni(-1,1) distributed weights and biases, the range of epsilons do not match between exact and BGS.

High Temperature gradient approximation

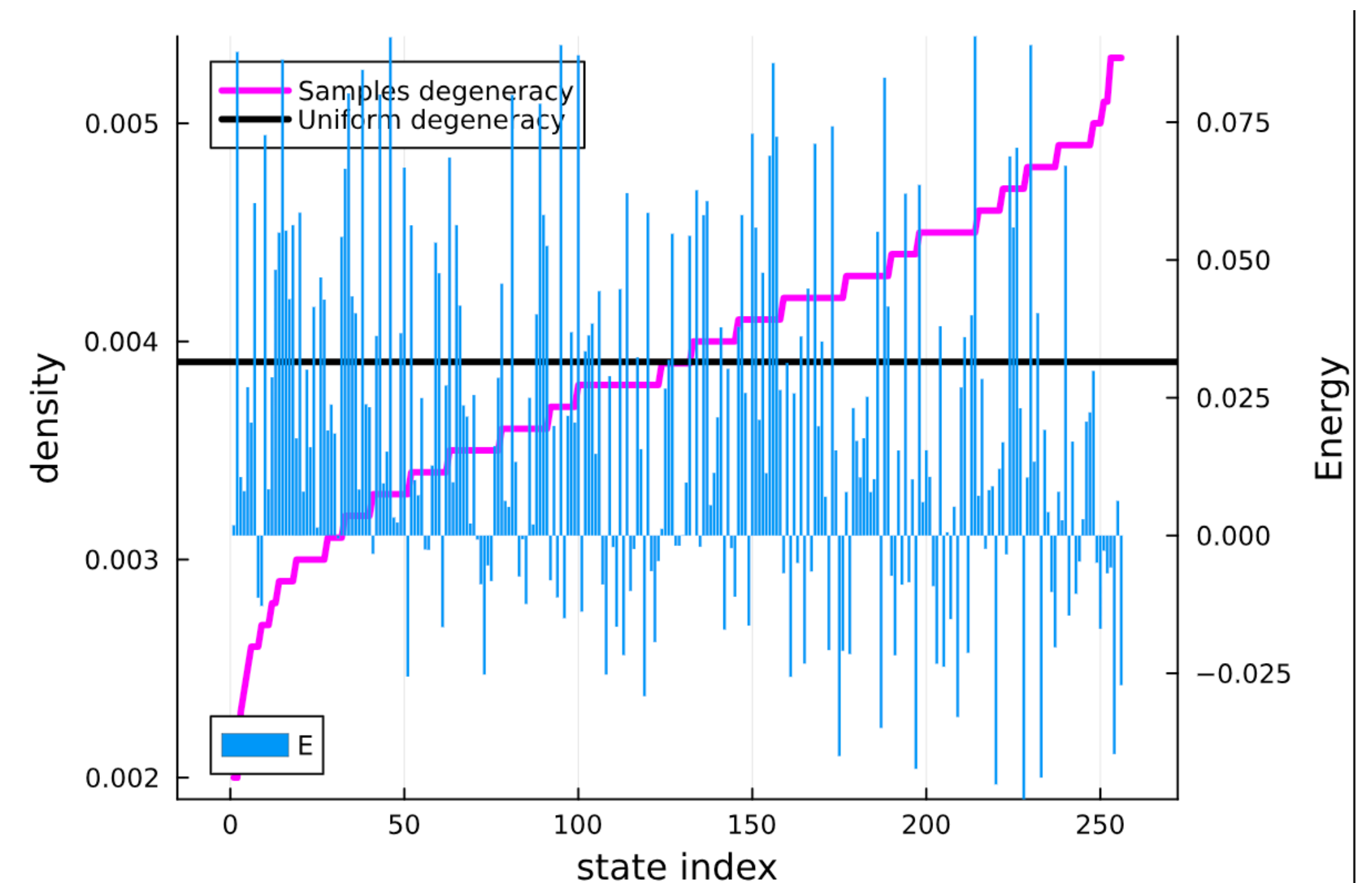
Small RBMs

Let's look at the energy histograms

$N(0,1)$ weights and biases



10k states sampled via BGS.
We measure the state degeneracy

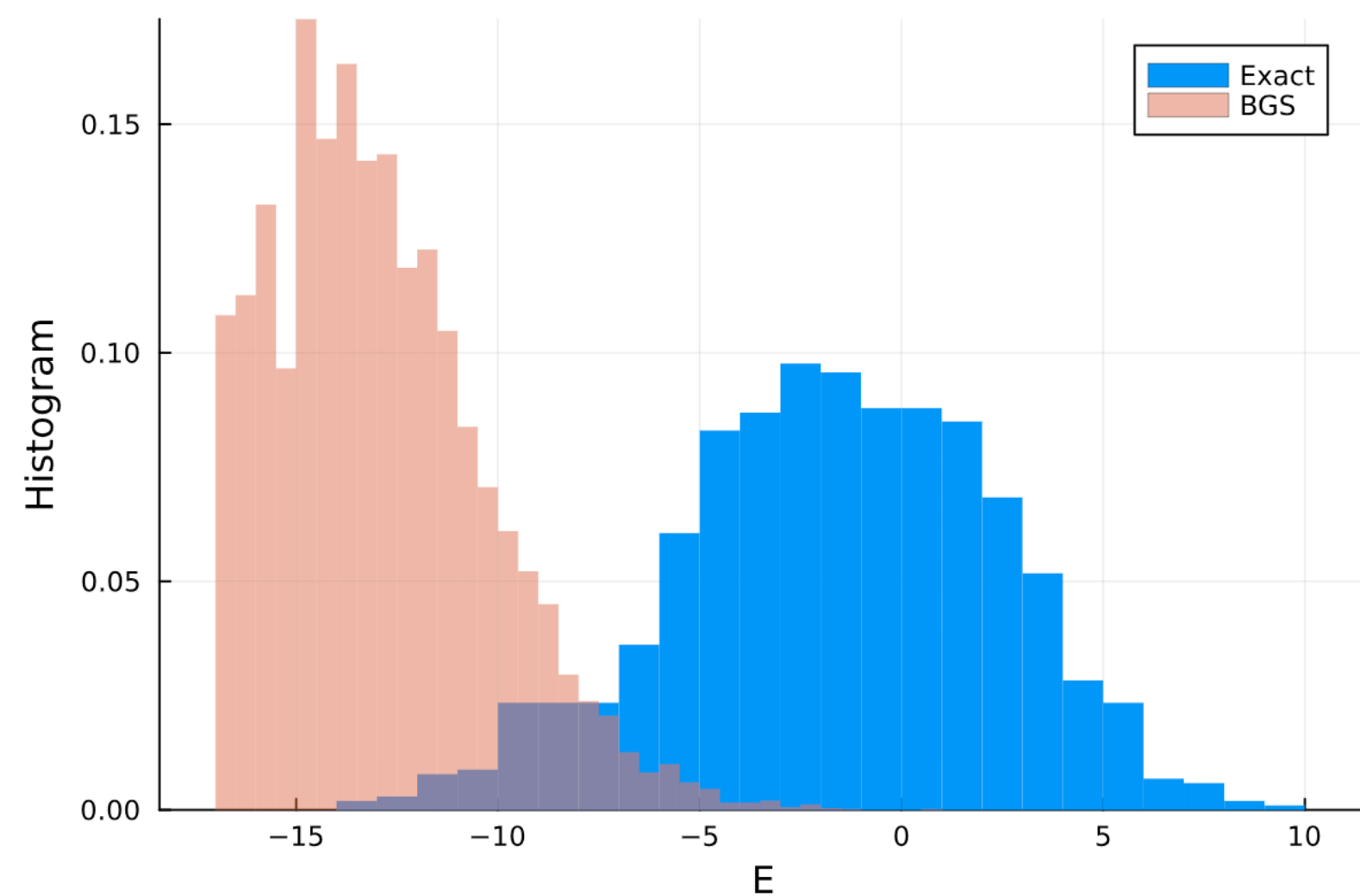


High Temperature gradient approximation

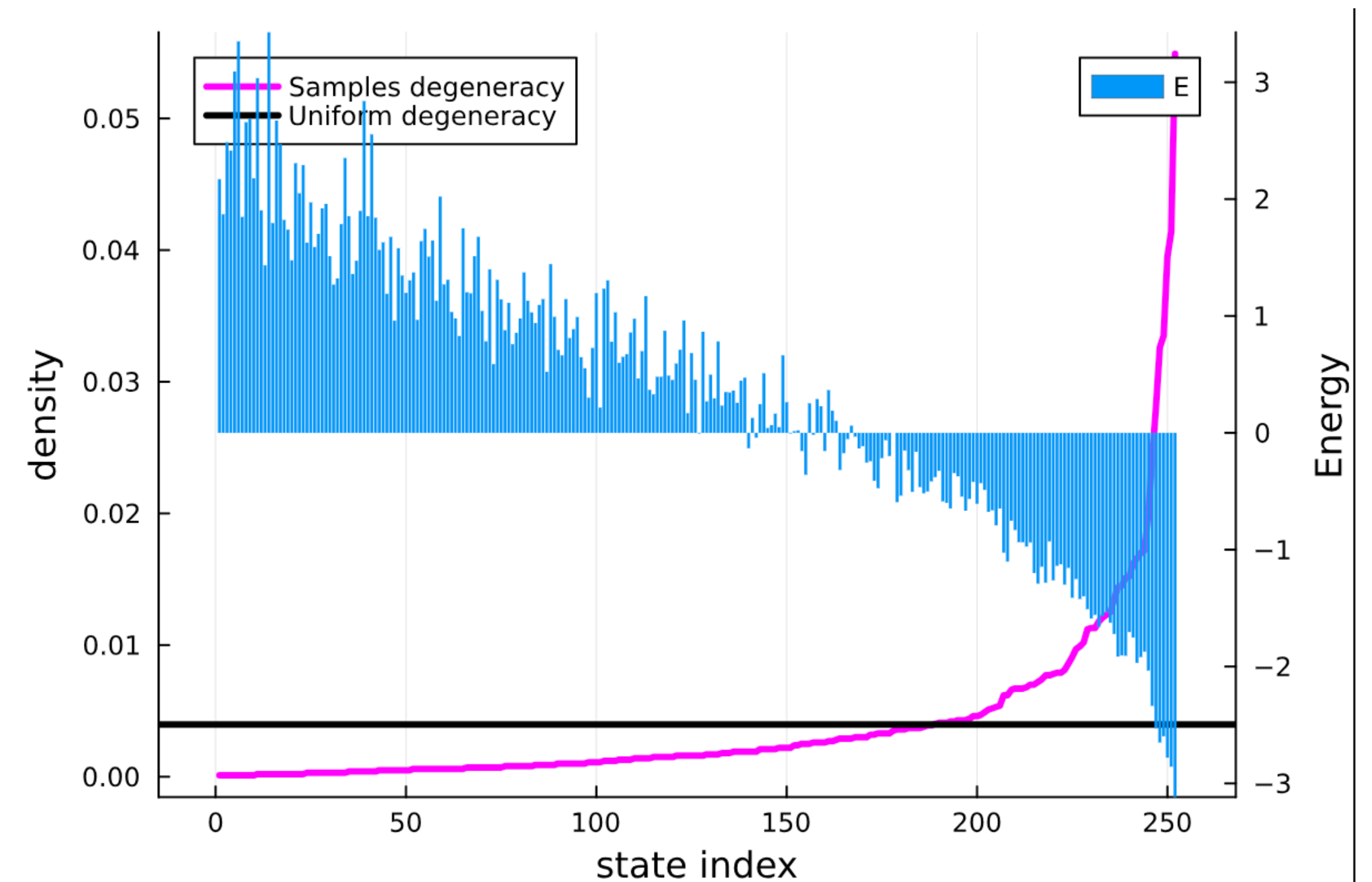
Small RBMs

Let's look at the energy histograms

U(-1,1) weights and biases



10k states sampled via BGS.
We measure the state degeneracy



High Temperature gradient approximation

Small RBMs

$$\mathcal{N}(J_0, J_1)$$

$$\tilde{J}_0 = NJ_0 \rightarrow 20 \cdot \delta$$

$$\tilde{J} = N^{1/2}J \rightarrow \sqrt{20} \cdot 1$$

$$kT = 1$$

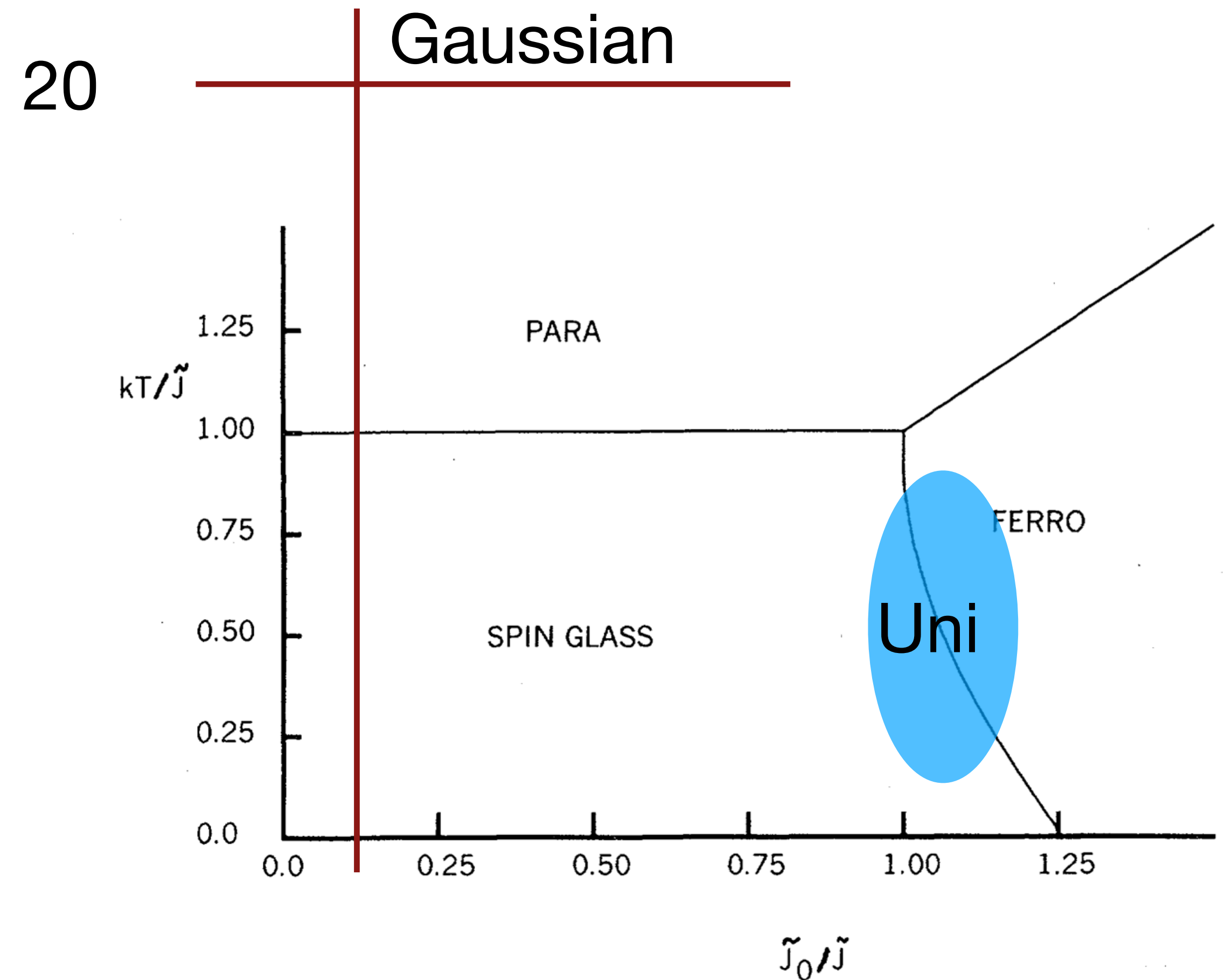


FIG. 1. Phase diagram of spin-glass ferromagnet.

Solvable Model of Spin glass, Kirkpatrick, Sherrington

High Temperature gradient approximation

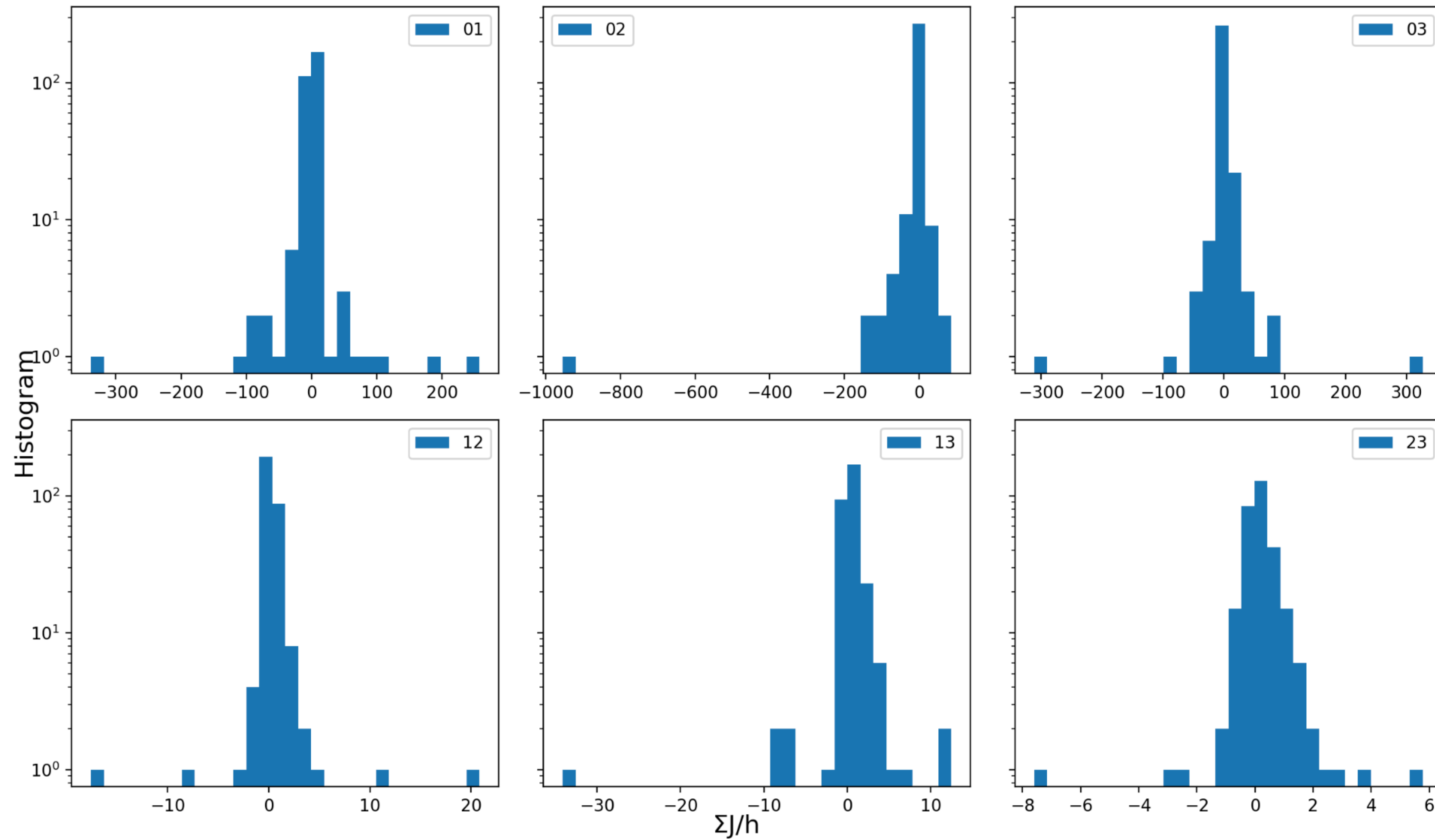
- Next step: Train model w/o this approximation.

Ratio between couplers and fields

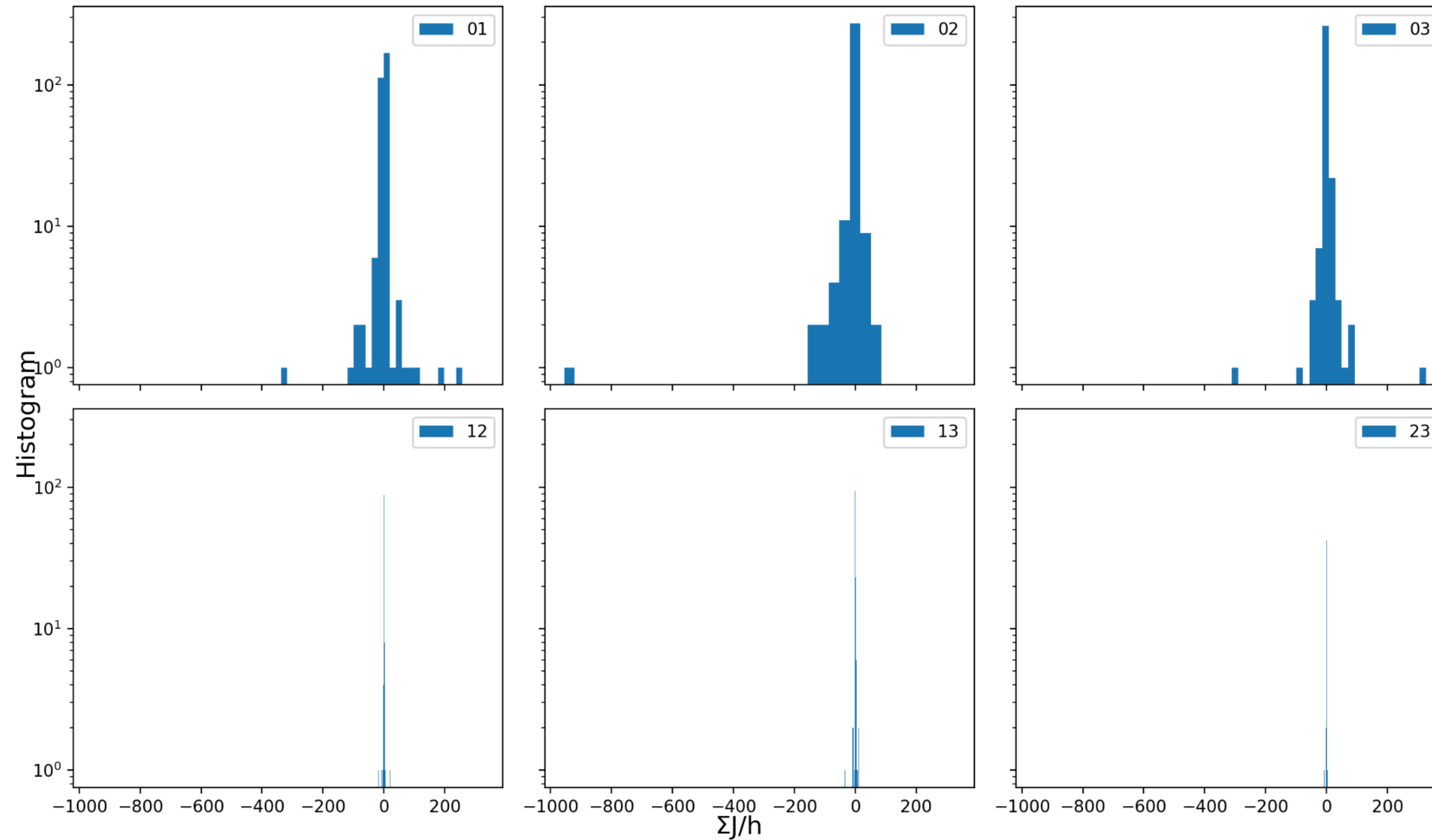
For a given spin i , what is the ratio between the sum over its couplers and the self-field?

$$\frac{1}{h_i} \sum_j J_{ij}$$

Ratio between couplers and fields



Ratio between couplers and fields



RBM to Diffusion Model equivalence

$$Z = \sum_{v,h} e^{-\beta E(v,h)}$$

$$E(v, h) = - \langle v | a_0 \rangle - \langle b_0 | h \rangle - \langle v | W | h \rangle$$

$$W = U \Sigma V^t \text{ (SVD)}$$

$$|x\rangle = U |v\rangle, \quad |y\rangle = V |h\rangle$$

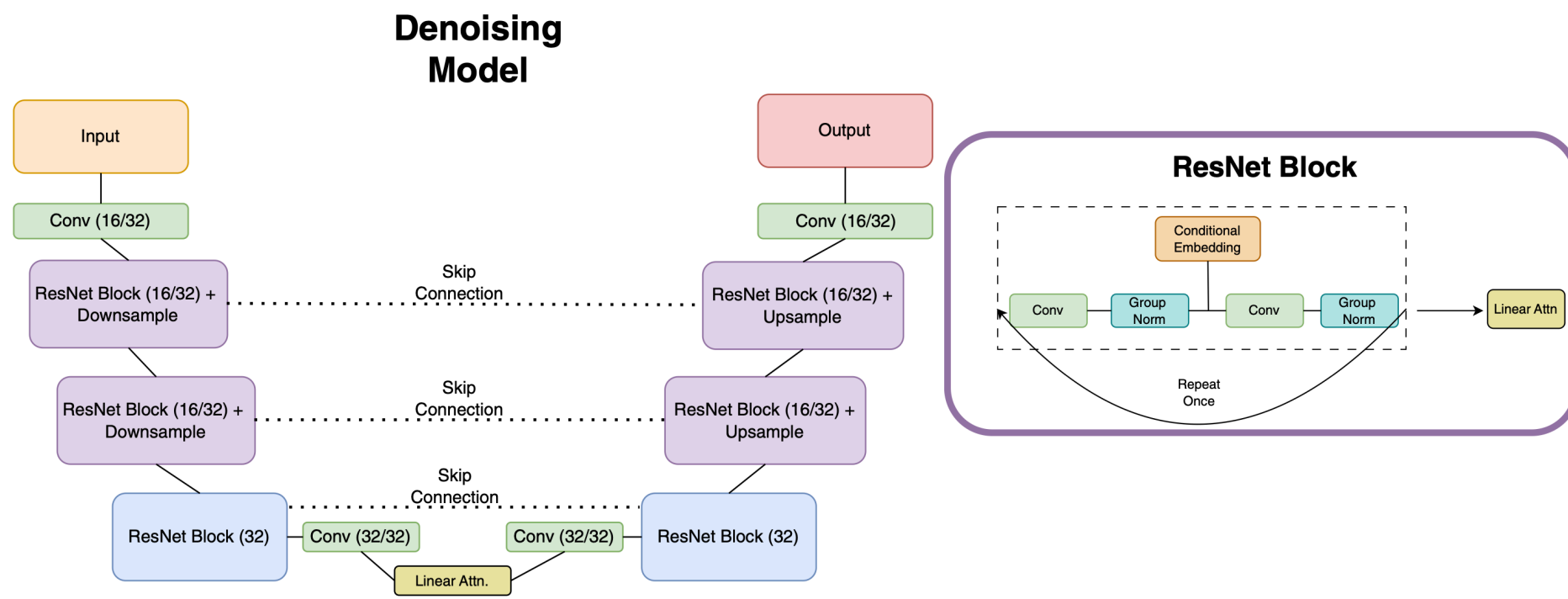
$$Z = \sum_{x,y} e^{-\beta E(x,y)}$$

Diffusion models

How good are they?

CaloDiffusion

Kevin Pedro, Oz Amram



CaloLatentDiffusion

Madula, Mikuni

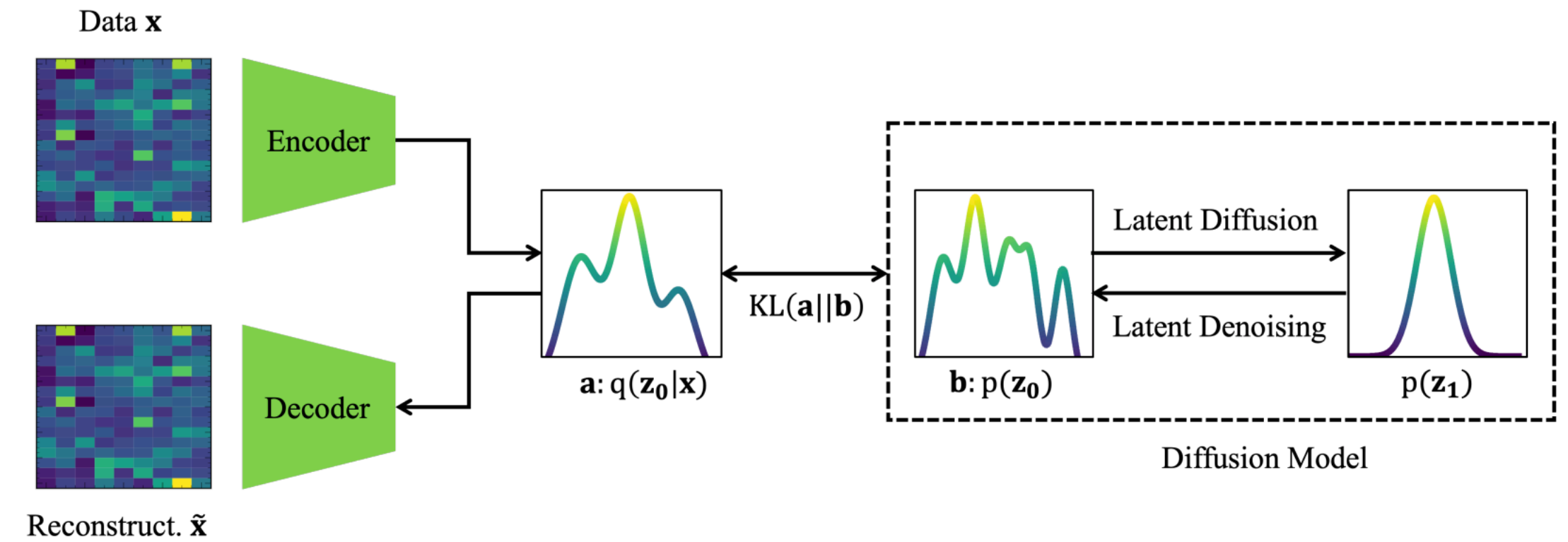
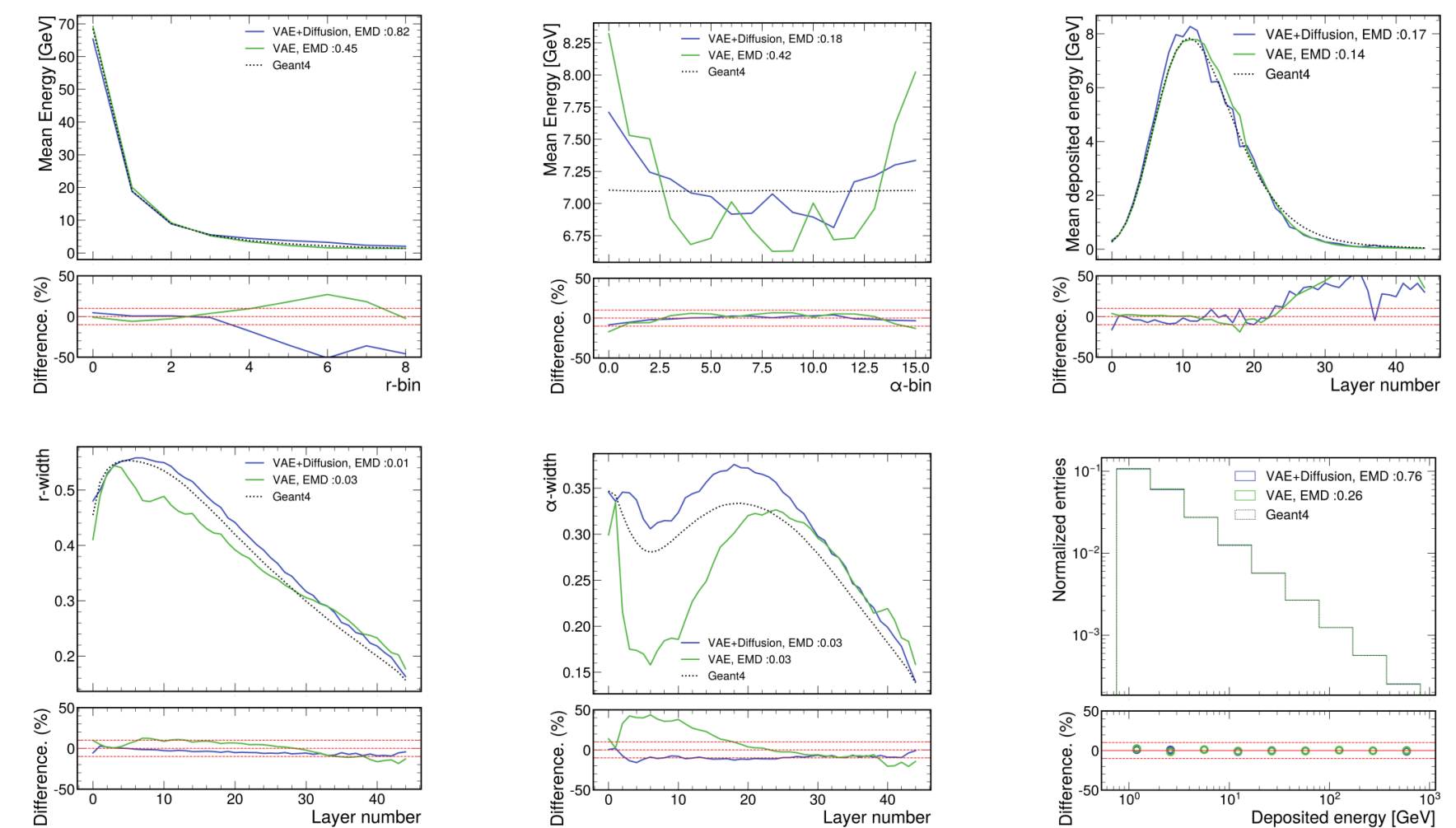


Figure 1: A schematic diagram of latent diffusion



Summary

- ✓ Papers status
- ✓ Using the QPU w/ Pegasus and in Zephyr
 - ➡ Meet with dwave to discuss strategy?
- ✓ High temperature gradient approximation for trained RBMs
 - ➡ Train model w/o this approximation
- ✓ Weight decay removal?
 - RBM and Diffusion model equivalence.
 - Relaxation time in RBMs

ToDo

- ✓ UNet for CaloQVAE — Ian
- ✓ CaloQVAE w/ linear attention layers
- ✓ Train current model with large RBM in Pegasus
- ✓ From RBM to diffusion models. Equivalence.
- ✓ Relaxation times in RBMs
- ✓ Training model with average of the gradient as opposed to gradient of the average in RBM
- ✓ Associative mem in GAN — Coherent samples from Zephyr