



DTRC-NRC



Conditioned Calo4pQVAE: High-energy calorimeter-particle interactions using deep learning and quantum annealers

★arXiv:2410.22870



11/11/24 :: IFAE UAB

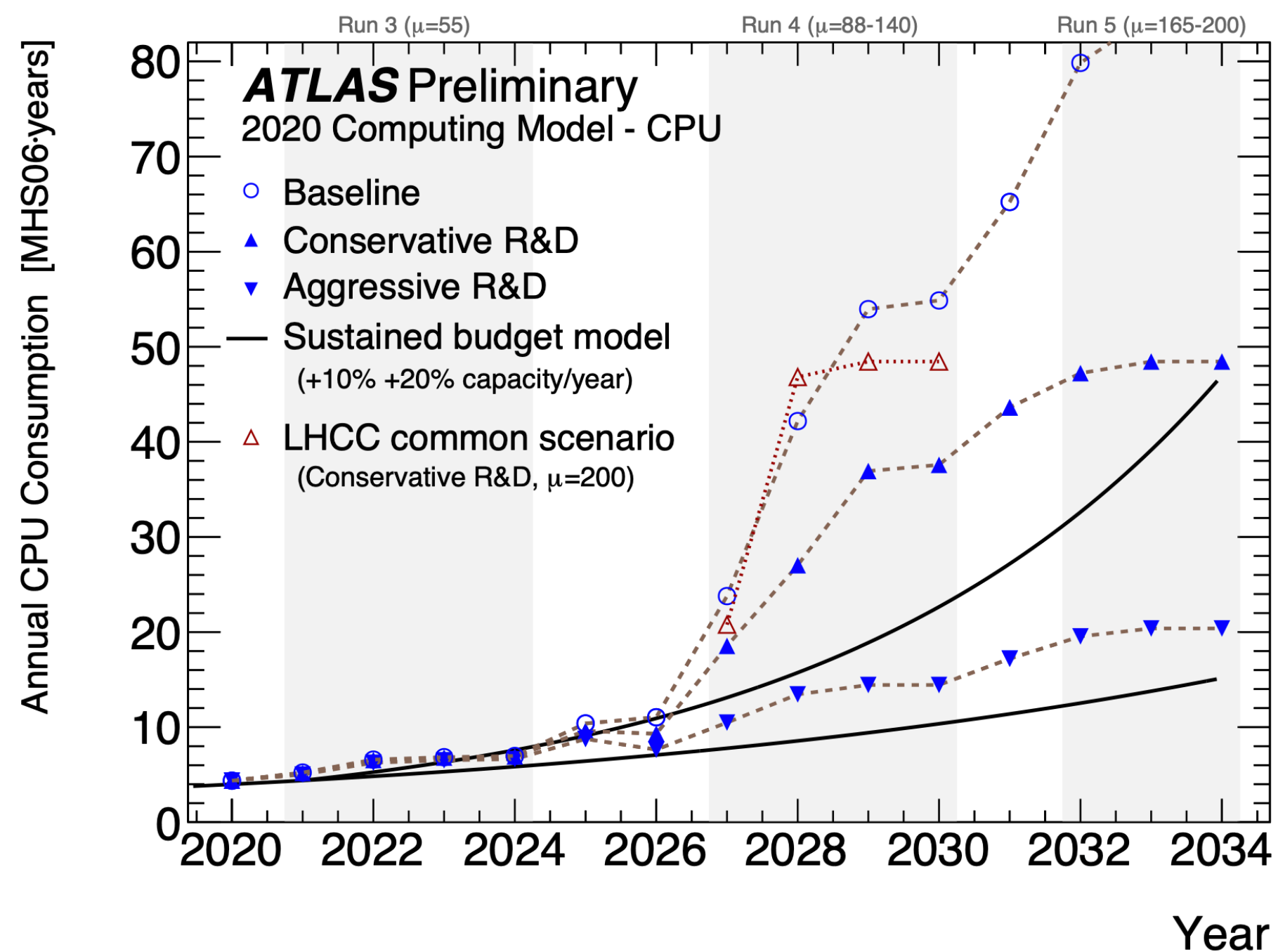
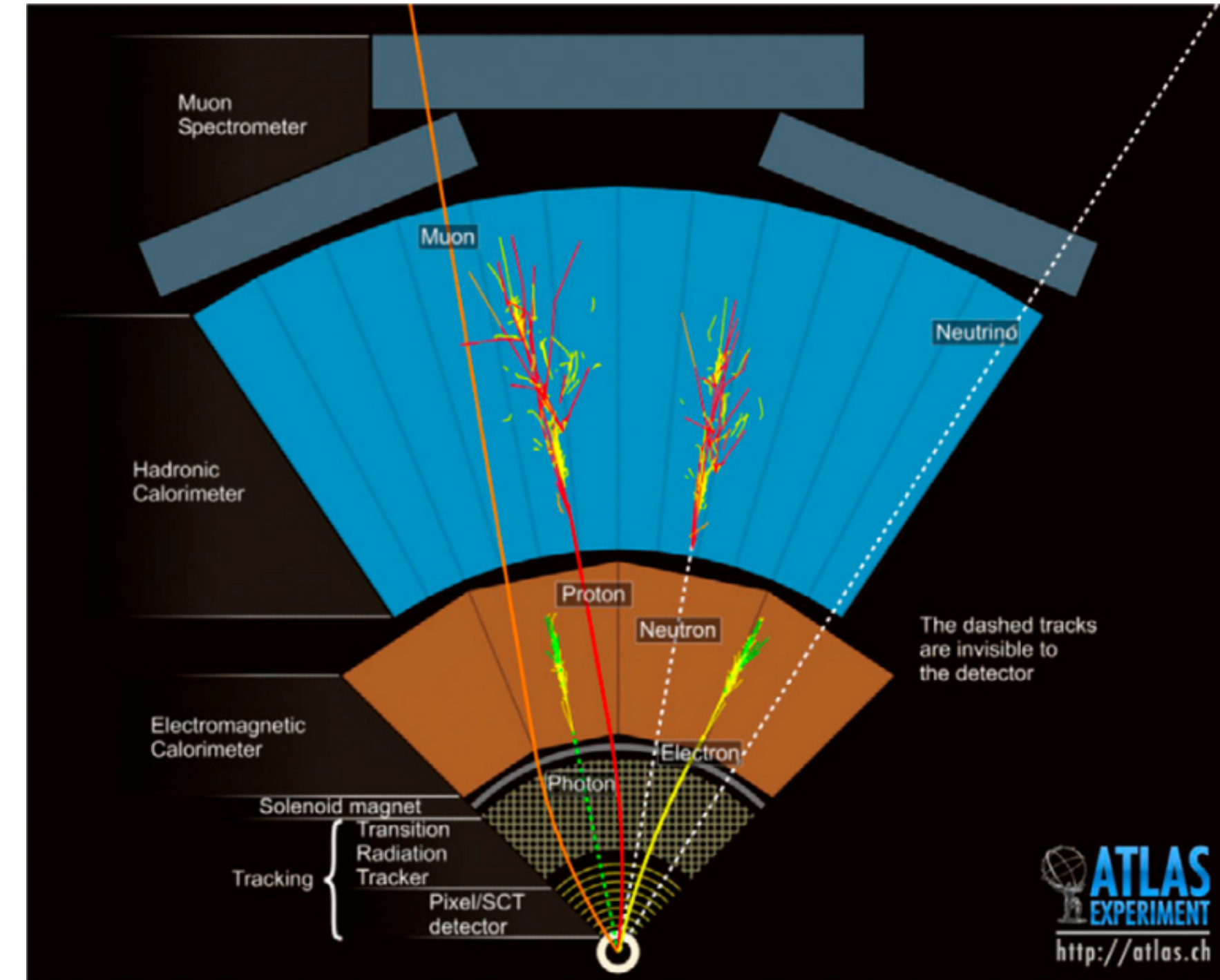
J. Quetzalcoatl Toledo-Marin
Quantum Machine Learning Research Associate



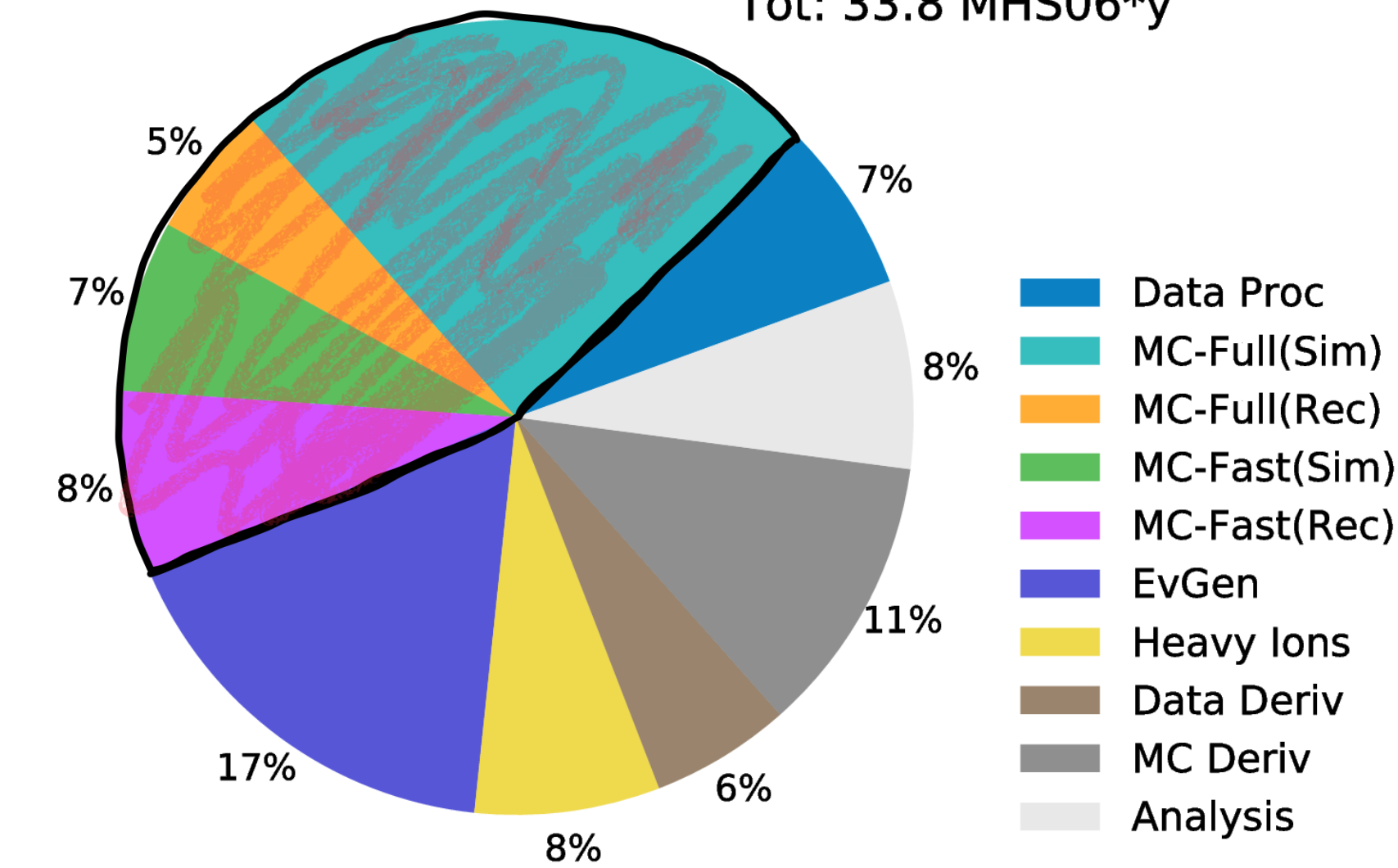
Canada's particle accelerator centre
Centre canadien d'accélération des particules

Motivation

- As we approach the launch of the High Luminosity Large Hadron Collider (HL-LHC) by the decade's end, the computational demands of traditional collision simulations have become untenably high.
- Current methods, relying heavily on Monte Carlo simulations for event showers in calorimeters, are projected to require millions of CPU-years annually, a demand far beyond current capabilities.
- This bottleneck presents a unique opportunity for breakthroughs in computational physics through the integration of generative AI with quantum computing technologies.

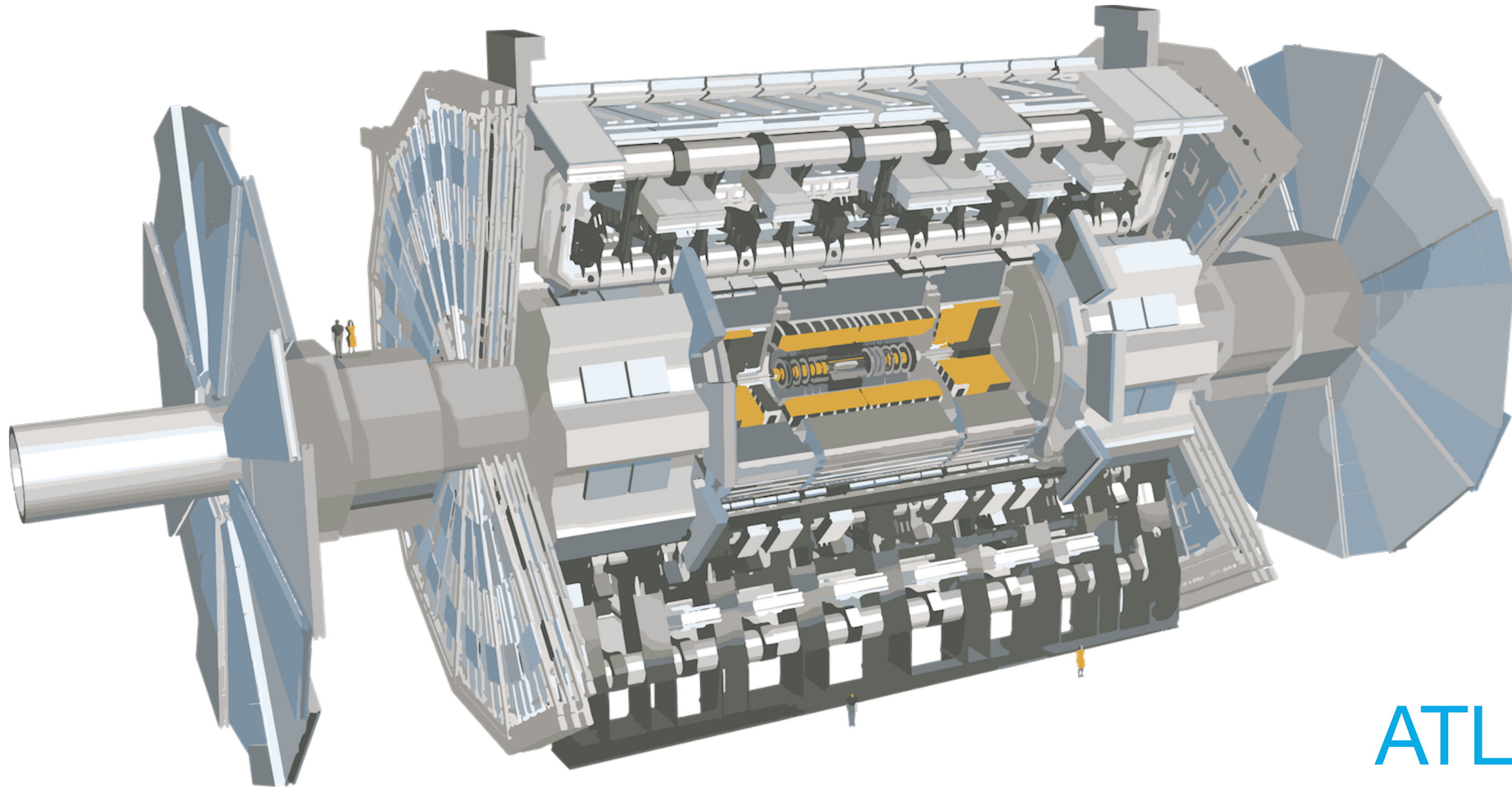


ATLAS Preliminary
2022 Computing Model - CPU: 2031, Conservative R&D
Tot: 33.8 MHS06*y



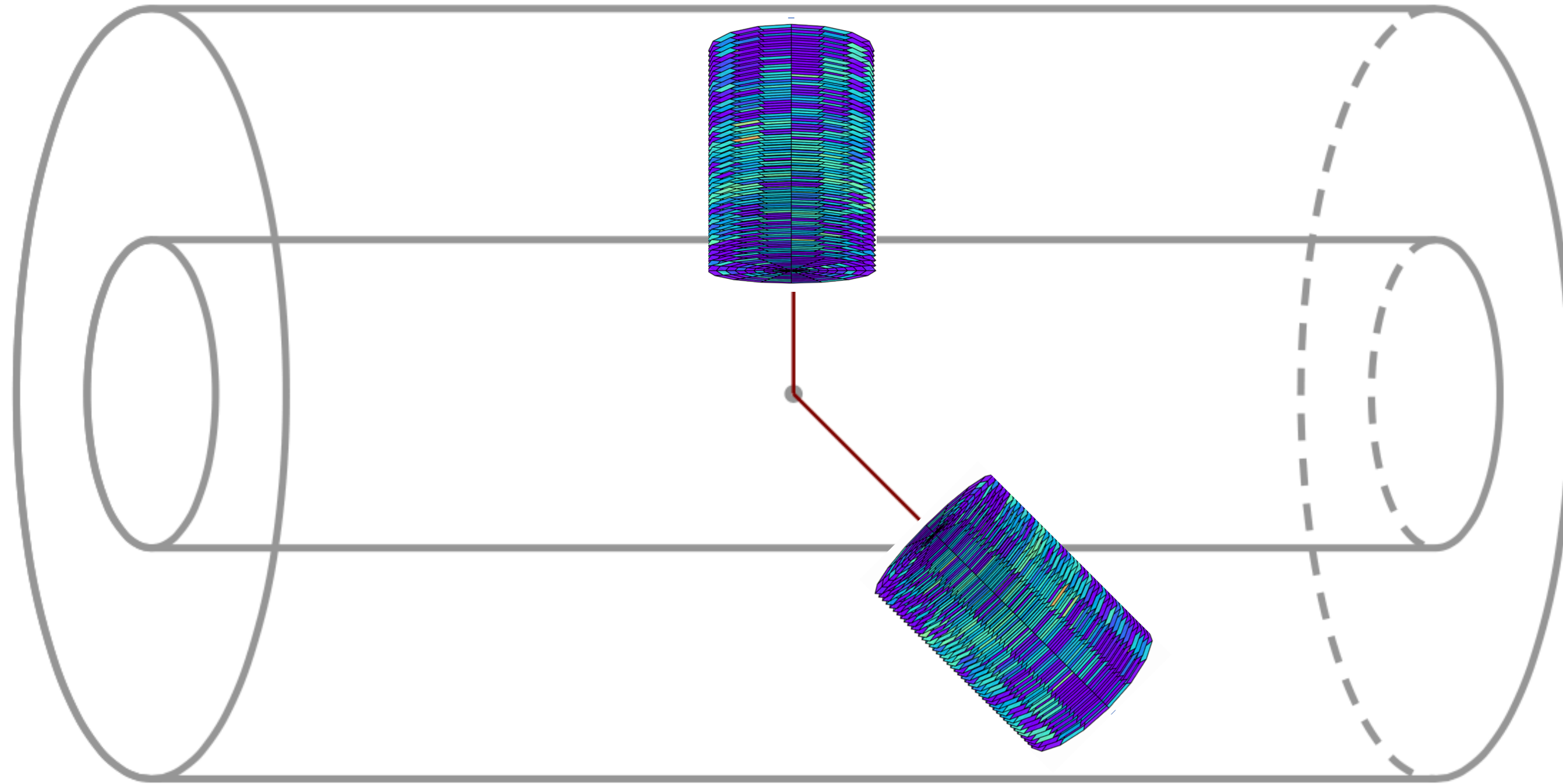
Scientific Data Lake for High Luminosity LHC project and other data-intensive particle and astro-particle physics experiments. InJournal of Physics: Conference Series 2020 Dec 1 (Vol. 1690, No. 1, p. 012166). IOP Publishing.

CaloChallenge



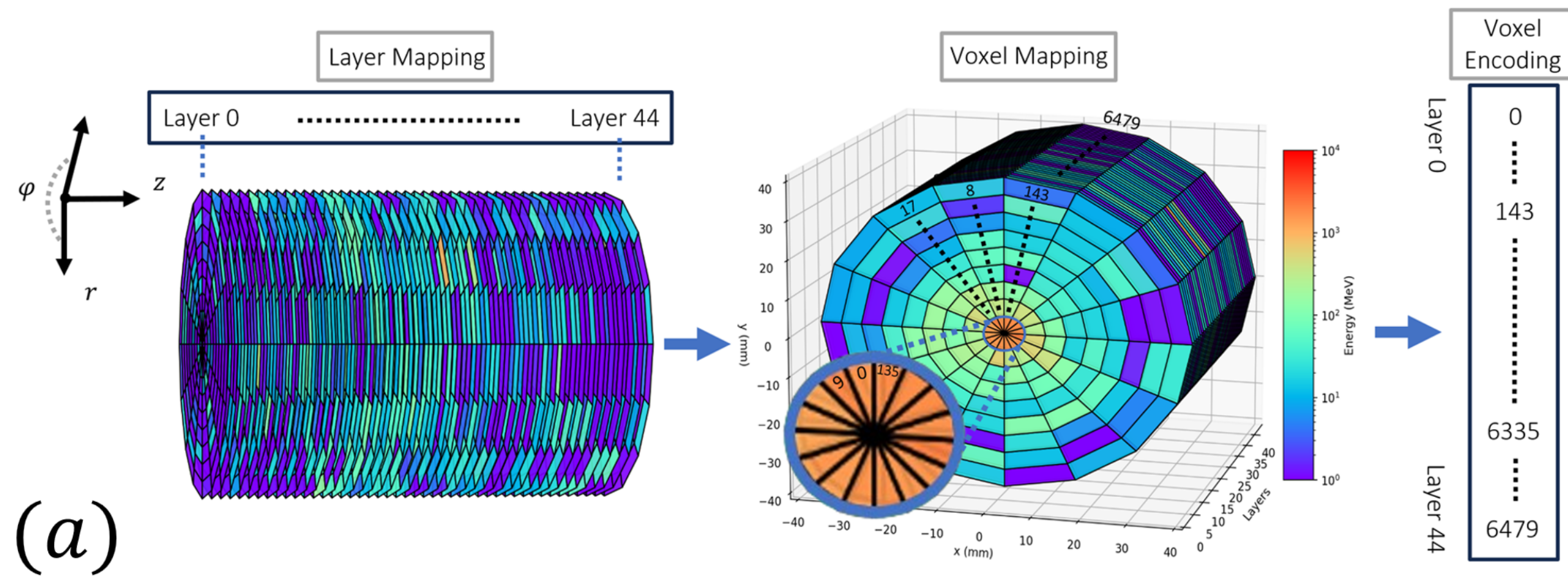
ATLAS Detector

CaloChallenge

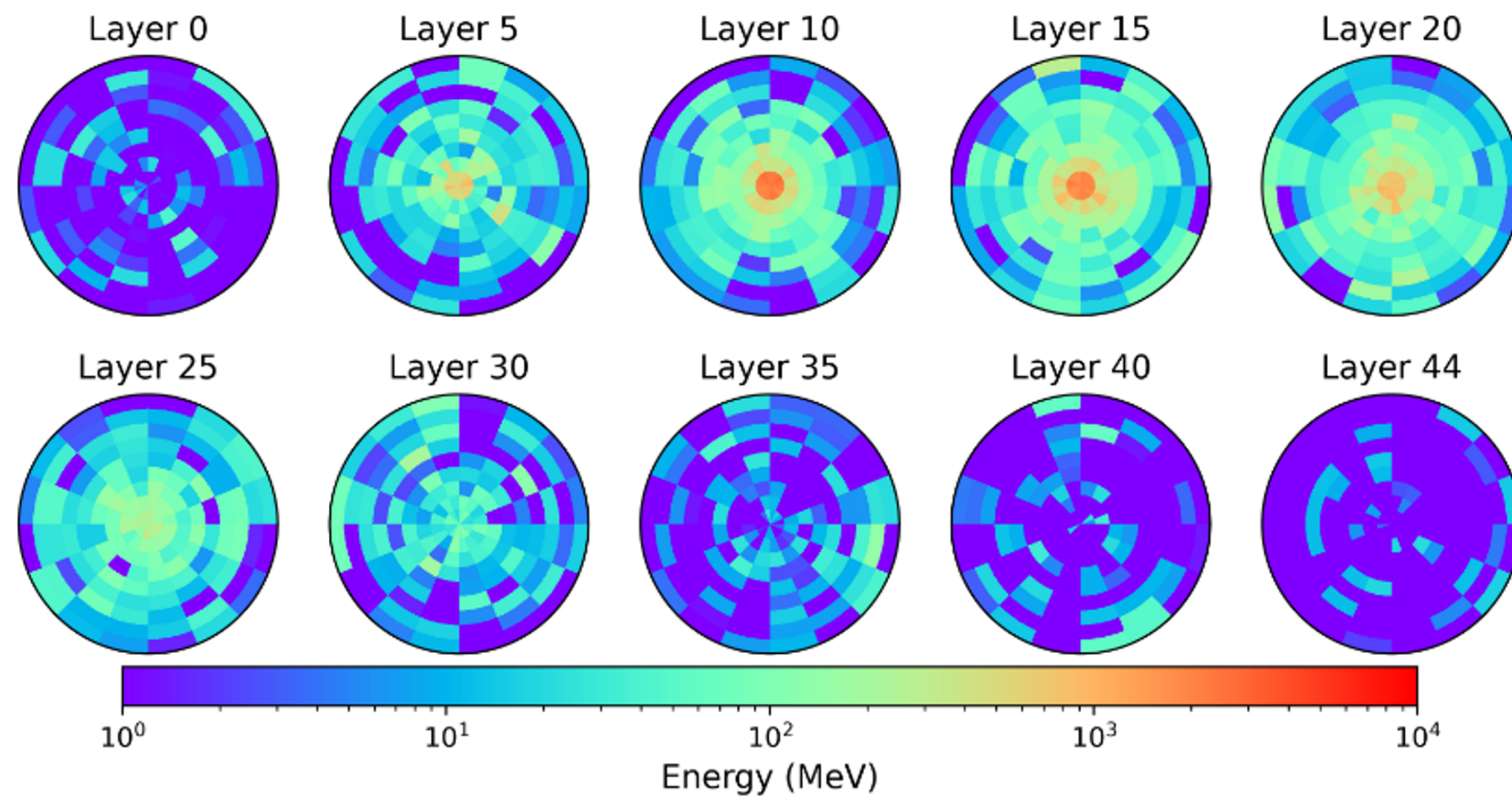


ATLAS Detector
(Simplified)

CaloChallenge



(a)

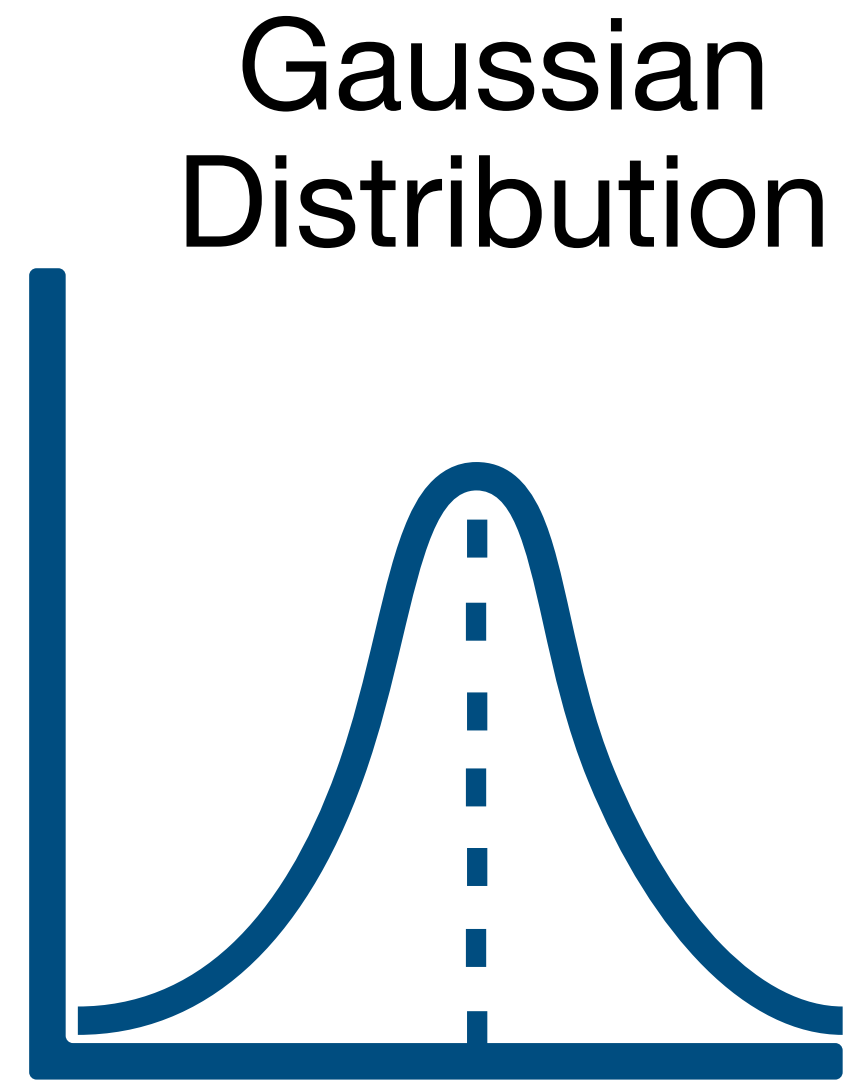


(b)

Dataset	
Particle type	Electron showers
Layers	45
Voxels per layer	9 radial * 16 angular
Incident energies	Log-uniform distribution (1GeV-1TeV)
N. of events	100,000

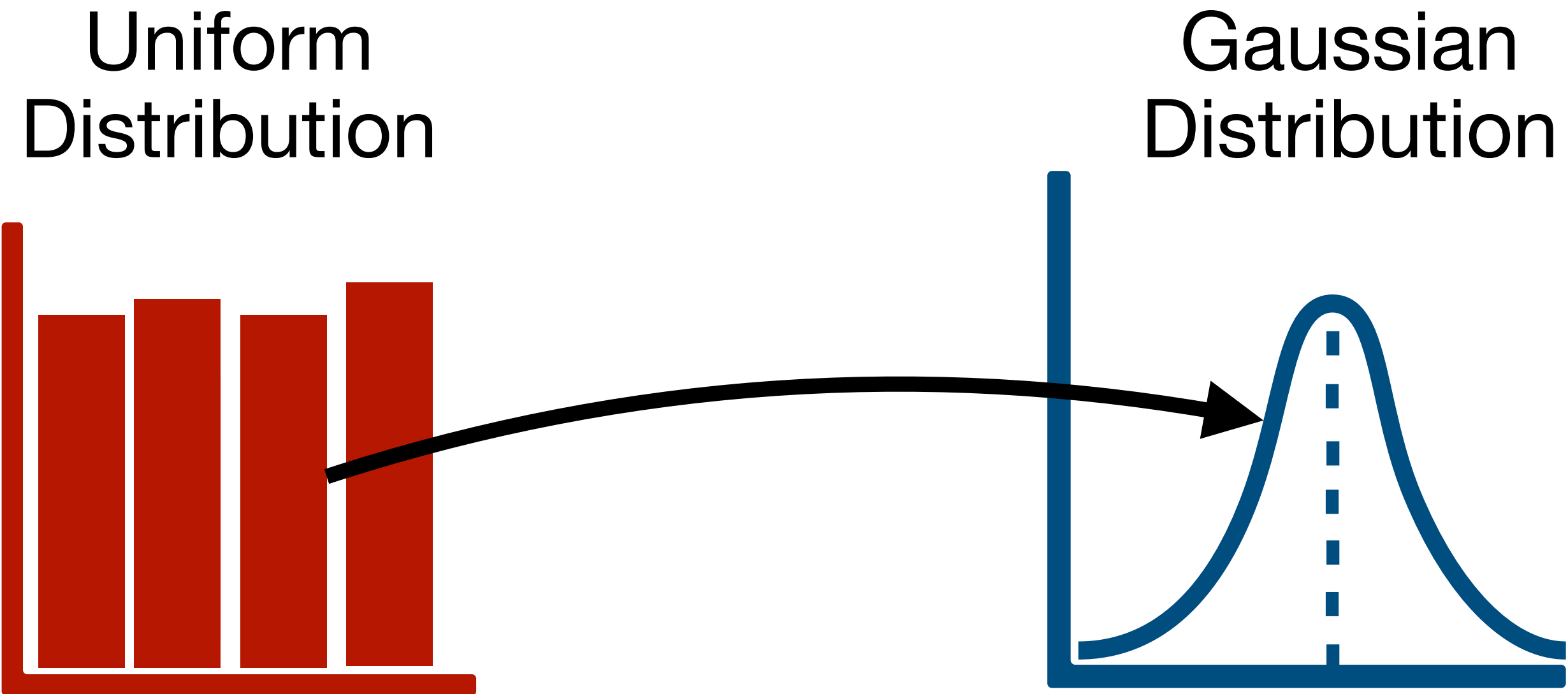
Generative Models

Simplest Example: Box-Muller Method



Generative Models

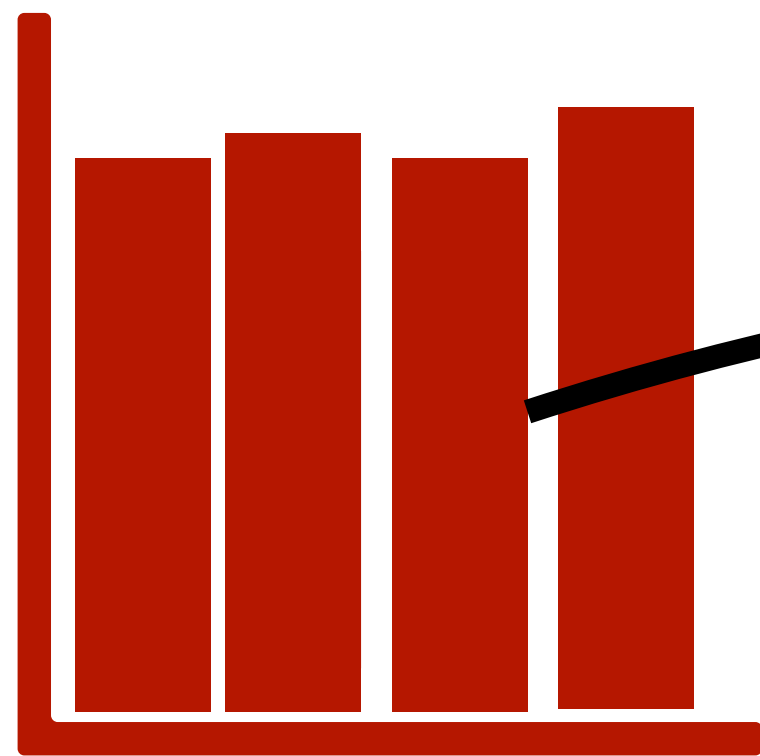
Simplest Example: Box-Muller Method



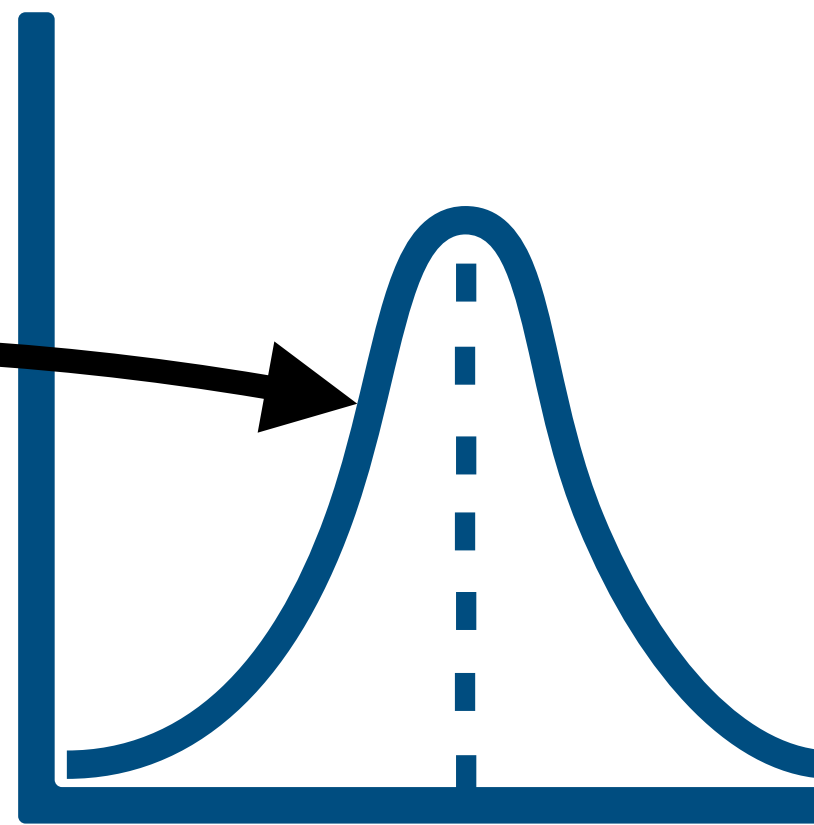
Generative Models

Simplest Example: Box-Muller Method

Uniform
Distribution



Gaussian
Distribution



$$f_0(U_1, U_2)$$

$$f_1(U_1, U_2)$$

Recipe:

1. Generate two **uniformly** independent, identically distributed random numbers U_1 and U_2 .

2. Substitute in:

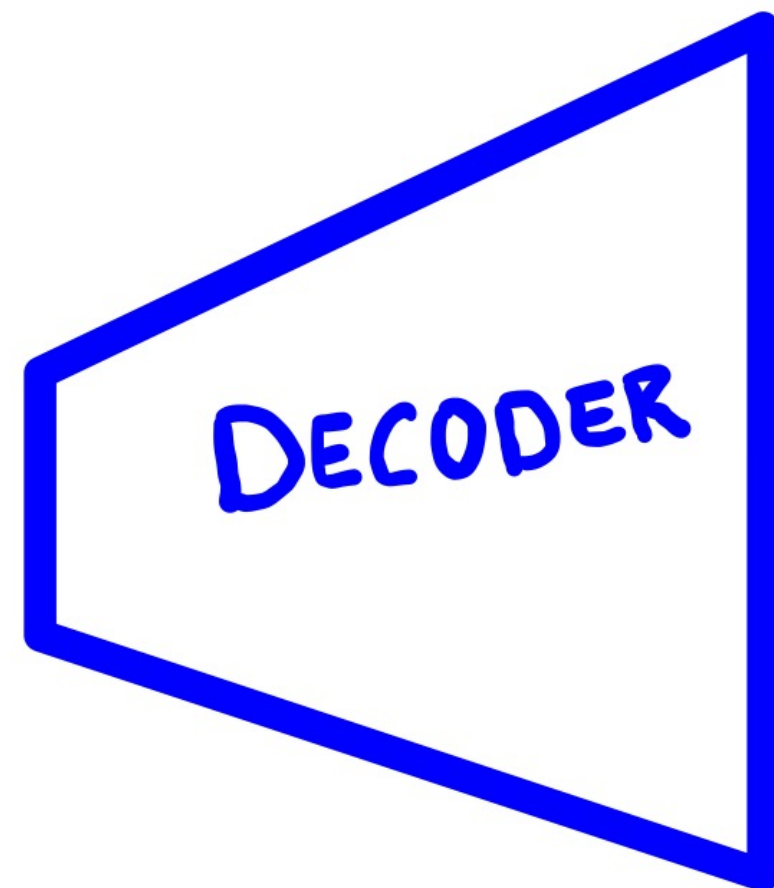
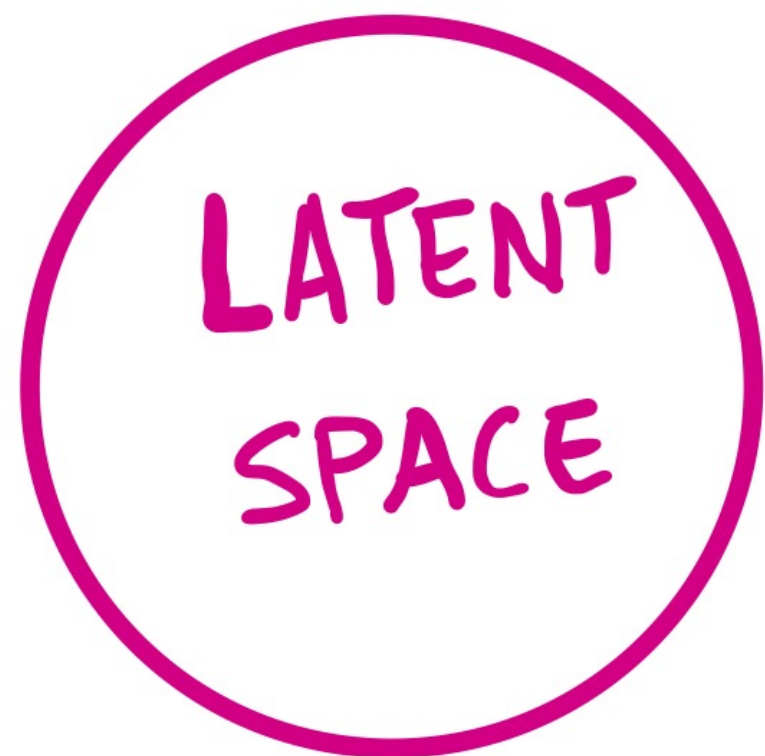
$$Z_0 = f_0(U_1, U_2) = \sqrt{-2 \ln U_1} \cos(2\pi U_2)$$

$$Z_1 = f_1(U_1, U_2) = \sqrt{-2 \ln U_1} \sin(2\pi U_2)$$

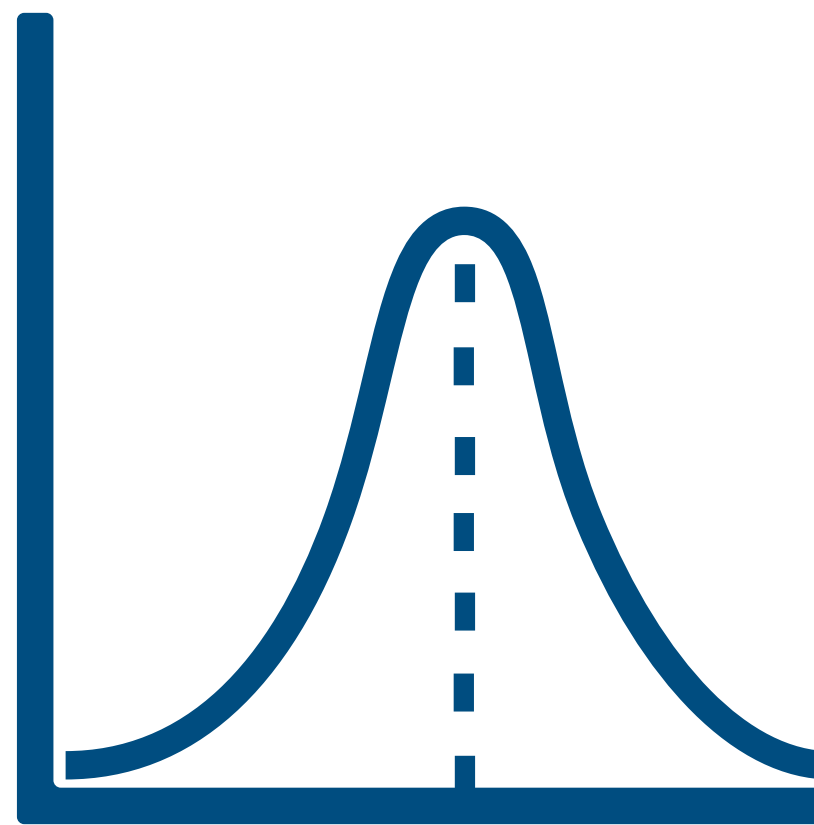
Generative Models

Simplest Example: Box-Muller Method

Uniform
Distribution



Gaussian
Distribution



1. Generate two **uniformly** independent, identically distributed random numbers U_1 and U_2 .

2. Substitute in:

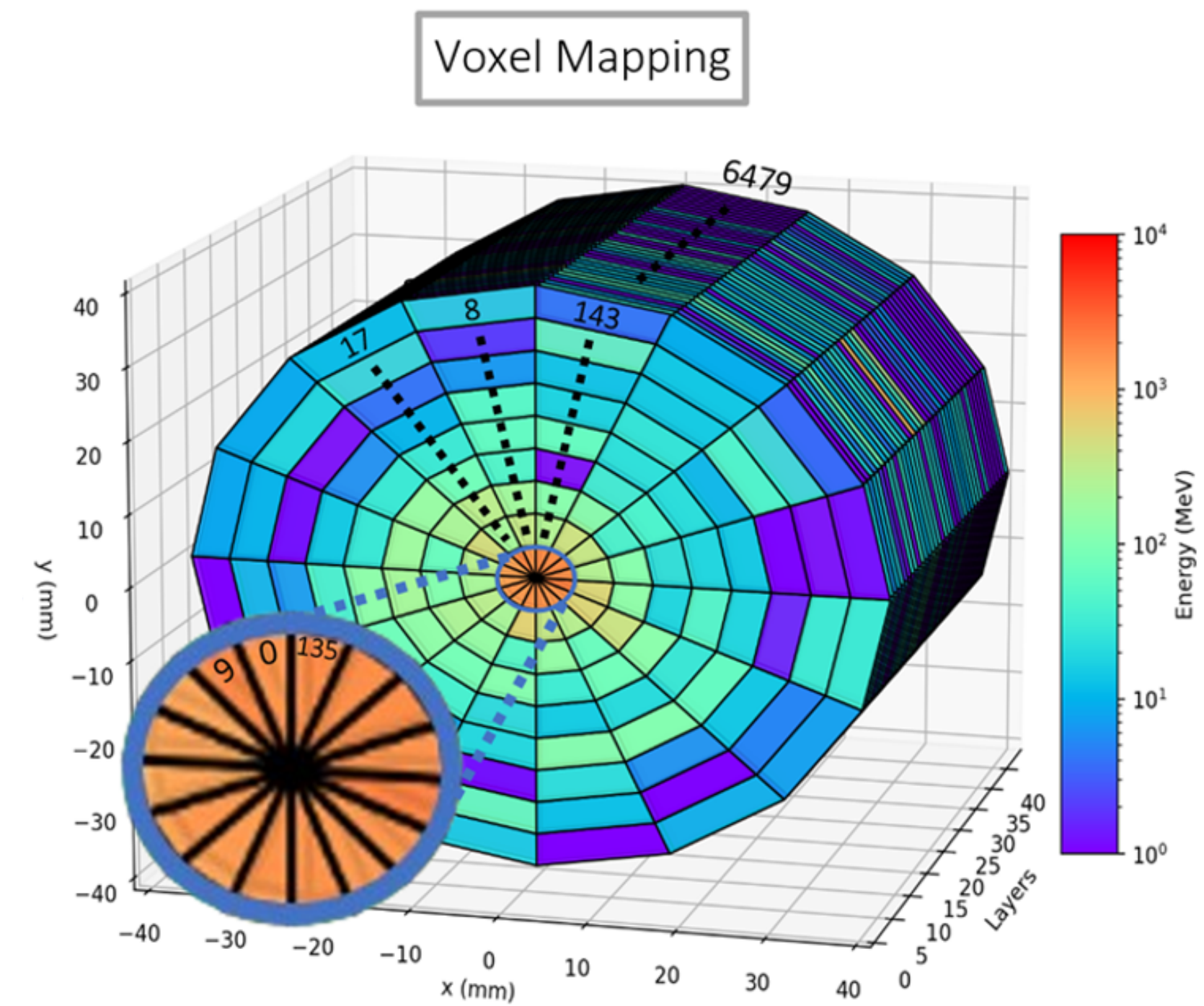
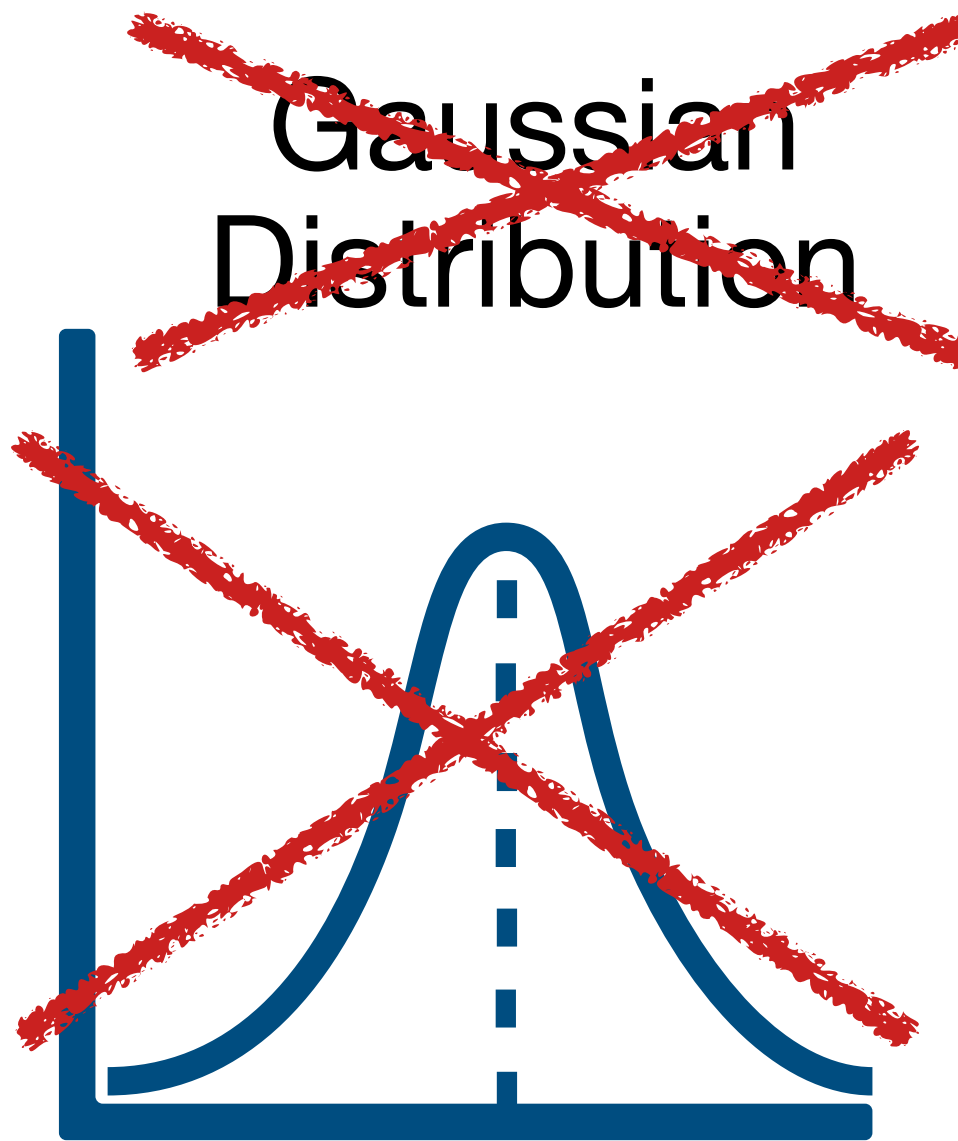
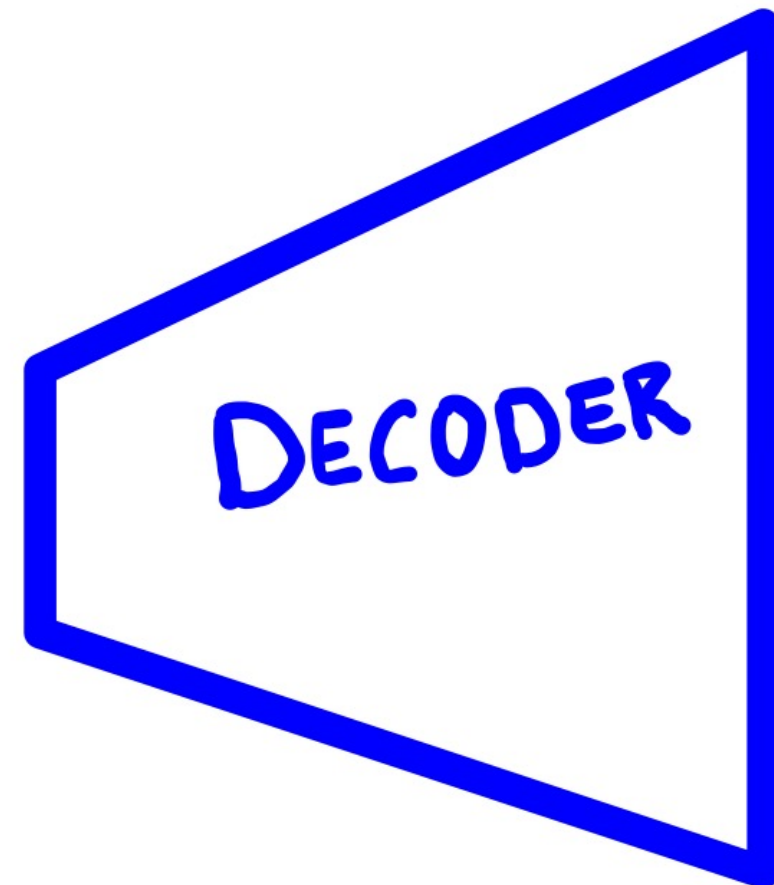
$$Z_0 = f_0(U_1, U_2) = \sqrt{-2 \ln U_1} \cos(2\pi U_2)$$

$$Z_1 = f_1(U_1, U_2) = \sqrt{-2 \ln U_1} \sin(2\pi U_2)$$

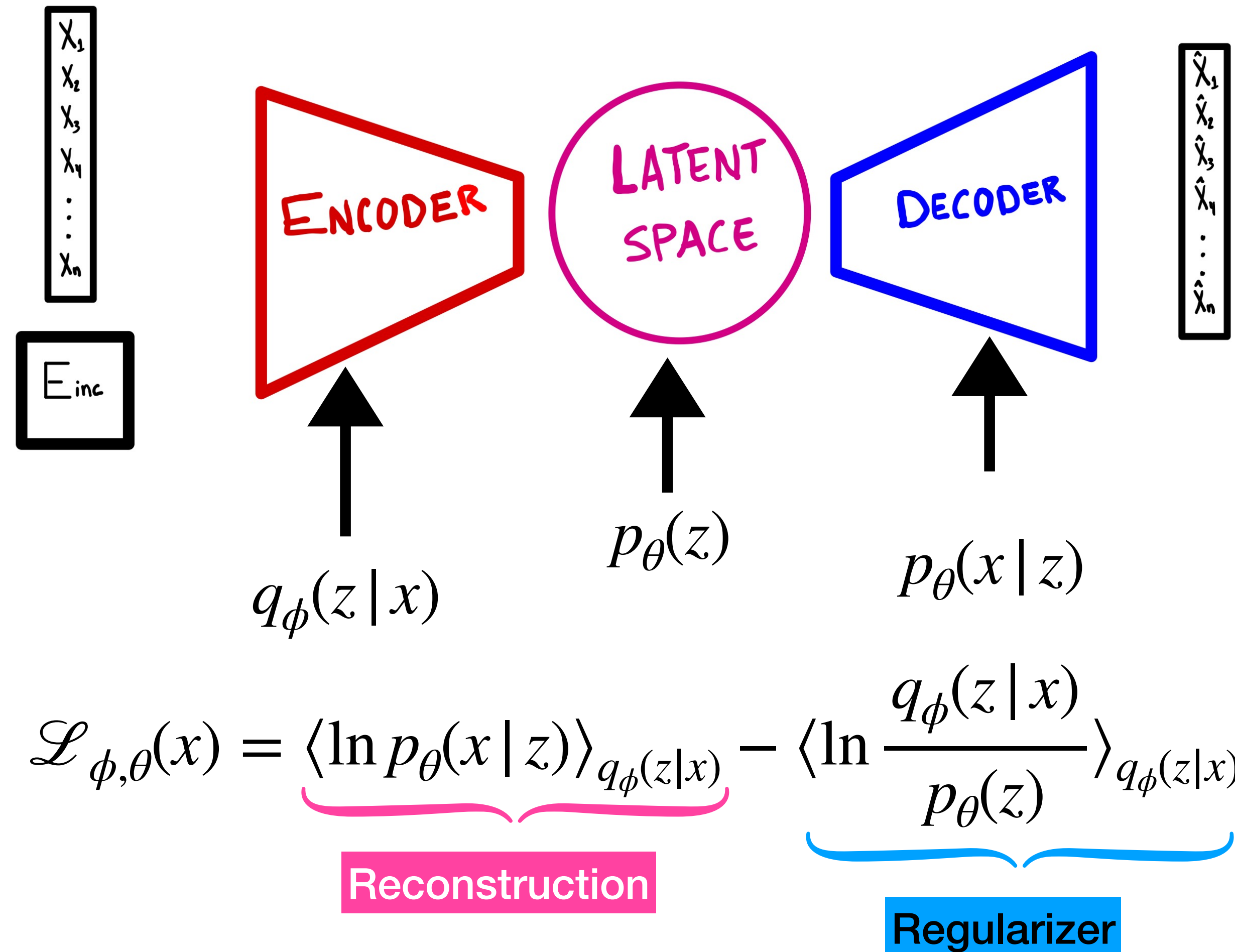
Generative Models

For particle-calorimeter interactions + quantum-assisted

~~Uniform
Distribution~~

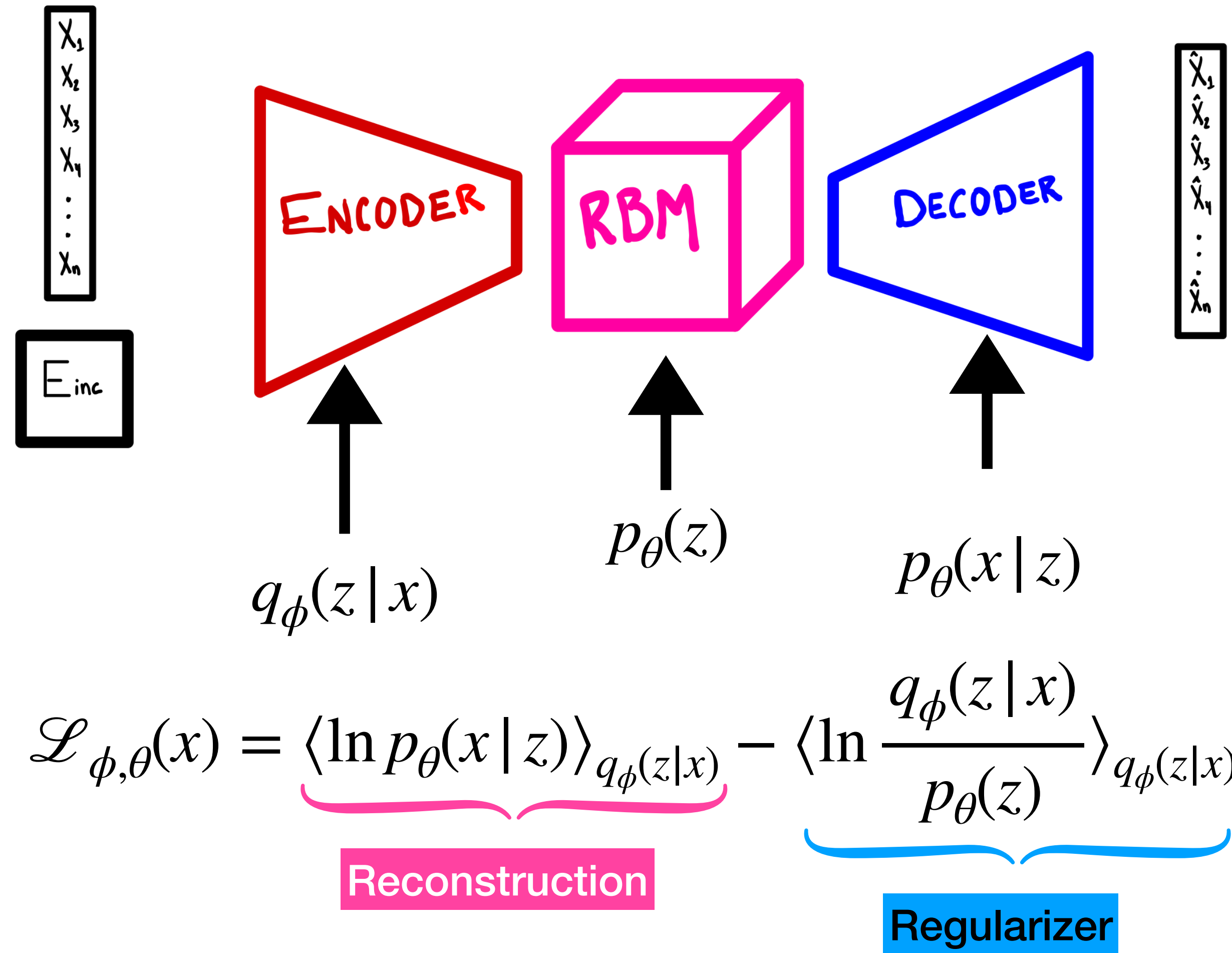


Variational Autoencoders (VAE)



- ◆ Easy to train.
- ◆ Average performance.
- ◆ Legacy VAE assumes a Gaussian prior.

VAE + Restricted Boltzmann Machine

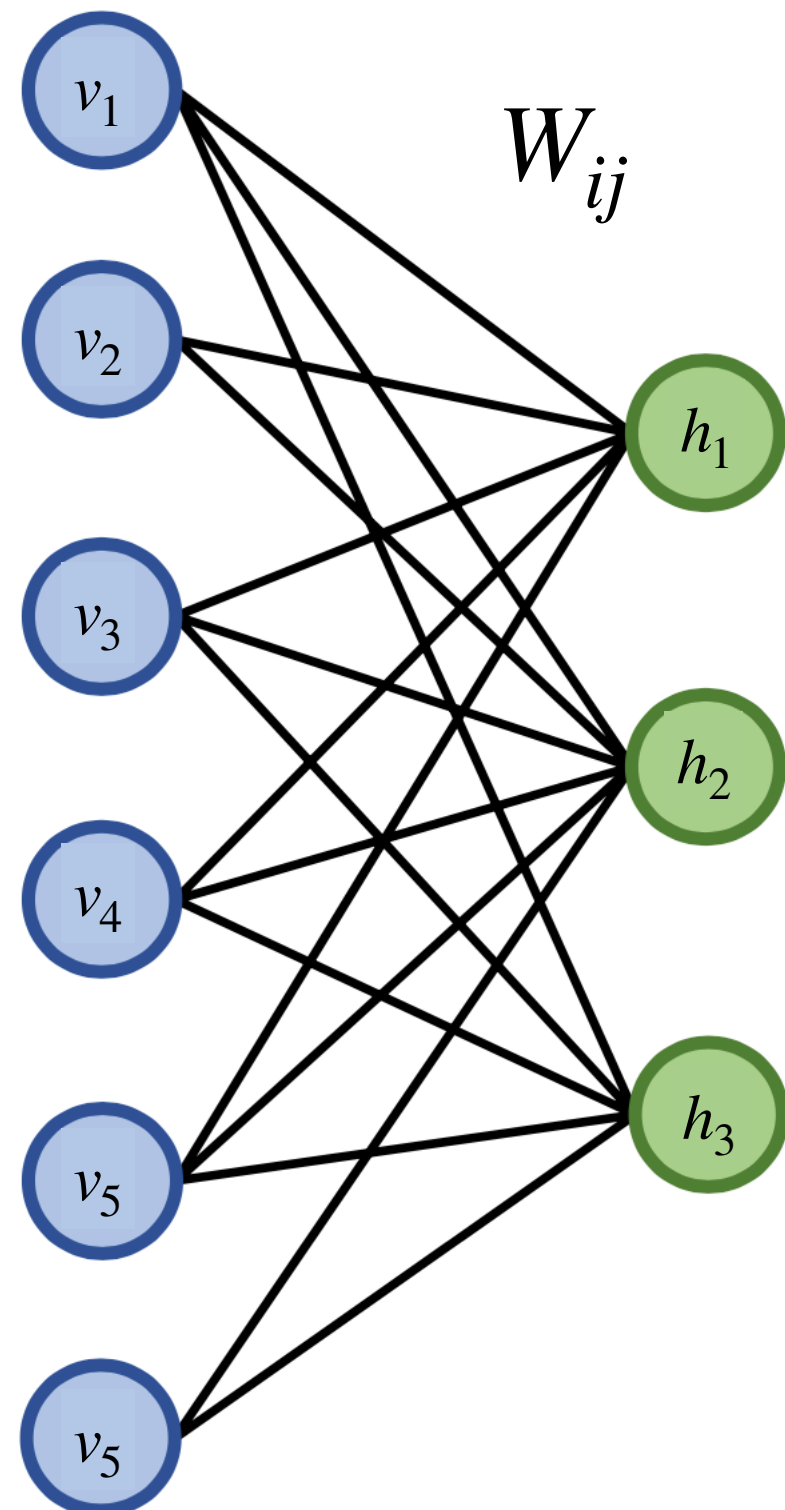


- ◆ Replace Gaussian prior with Boltzmann prior.
- ◆ More expressiveness.
- ◆ However, this comes at a cost.

Restricted Boltzmann Machine

Basics

$\langle v | \quad | h \rangle$



Suppose a data set $\{v^\alpha\}_{\alpha=1}^n$, such that $v_i \in \{0,1\}$.

I) An RBM will fit a Boltzmann distribution, $p(v)$, to the data set.

II) The fitting is done by maximizing the log-likelihood, $\ln p(v)$.

III) RBMs are composed by a two-partite graph, where \mathbf{v} denotes the visible layer and \mathbf{h} the hidden layer.

$$p(v, h) = \frac{\exp(-E(v, h))}{Z}$$

Boltzmann Dist

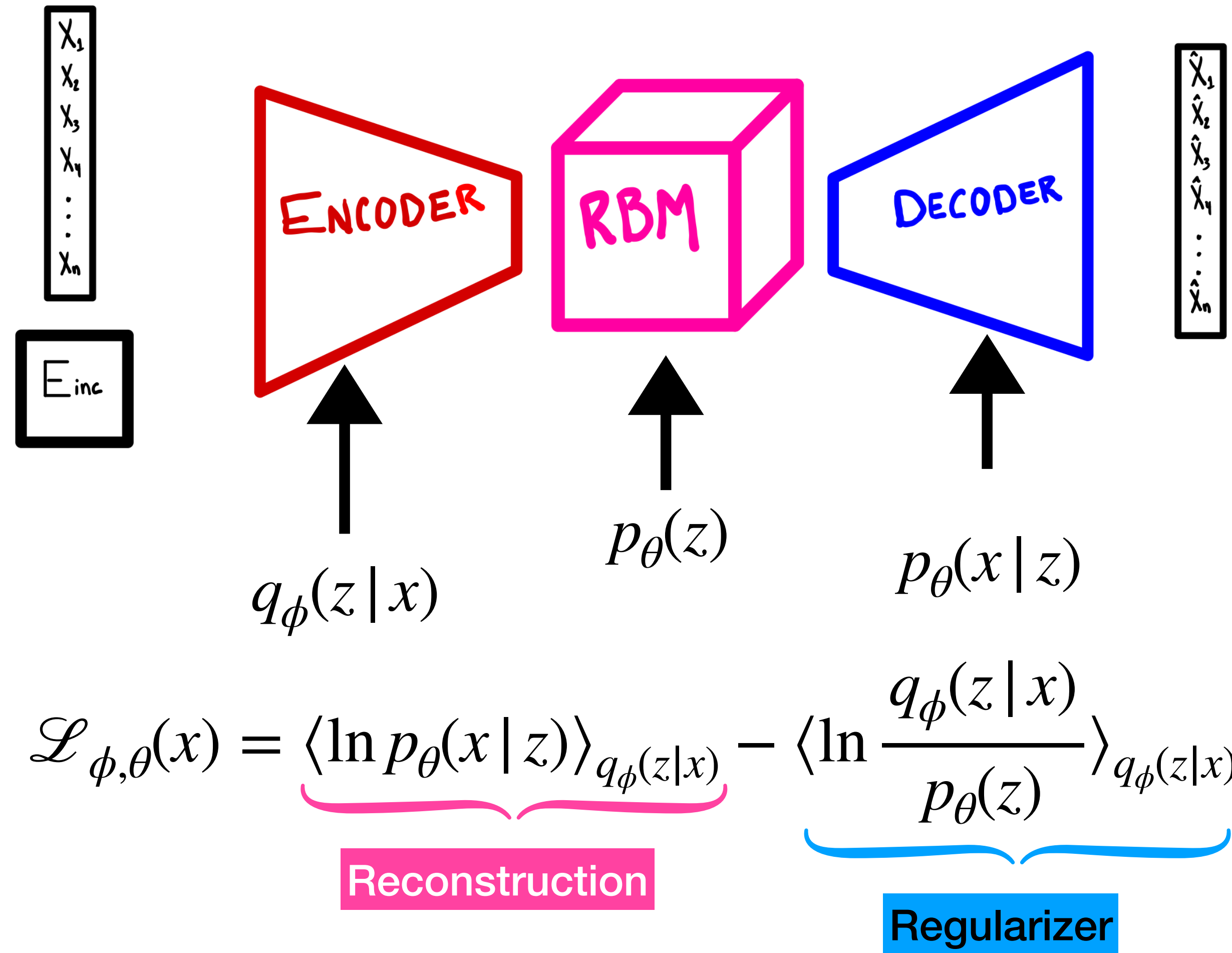
$$E(v, h) = - \sum_{i=1}^{n_v} v_i a_i - \sum_{j=1}^{n_h} b_j h_j - \sum_{i,j} v_i W_{ij} h_j$$

Energy

$$Z(W, a, b, \beta = 1) = \sum_{v', h'} \exp(-E(v', h'))$$

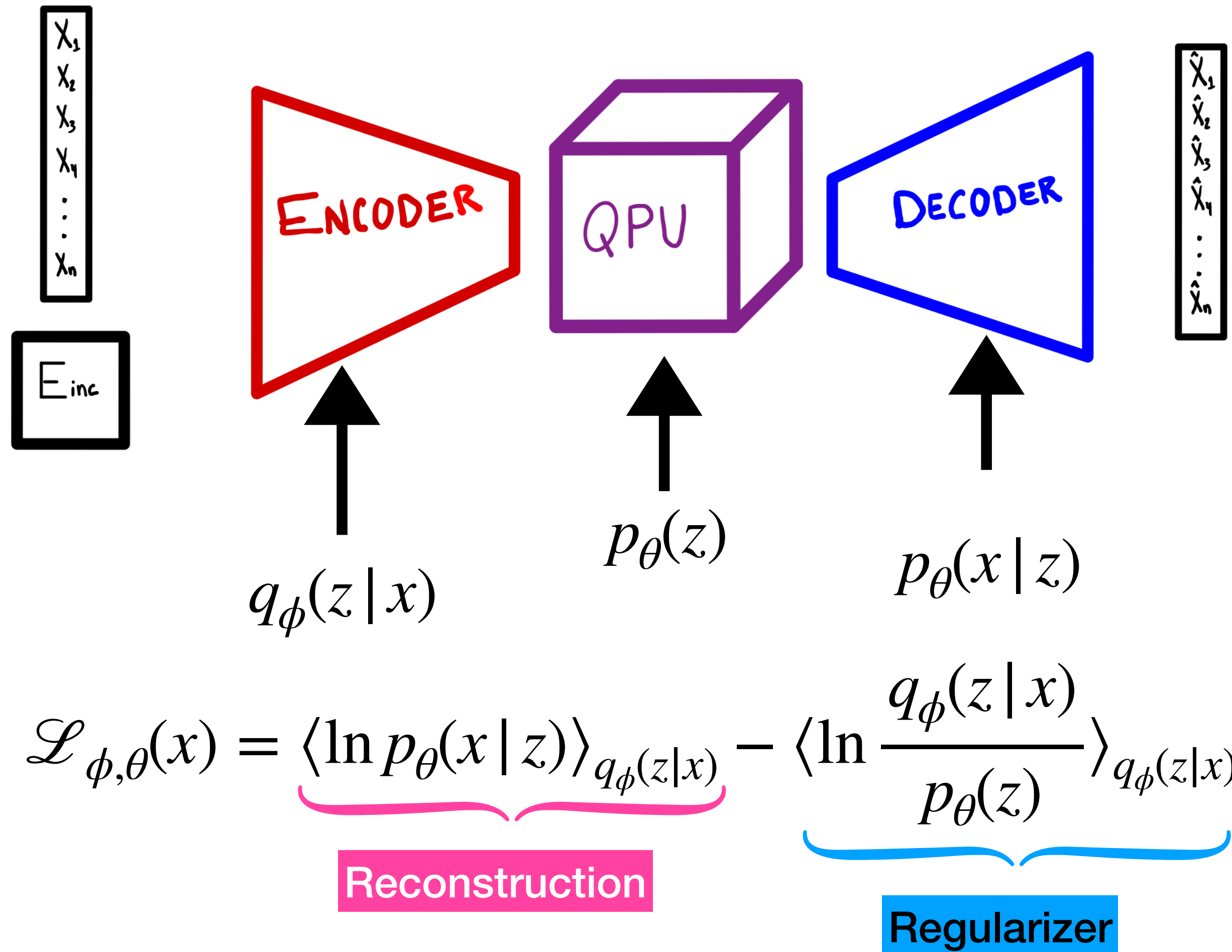
Partition Function

VAE + Restricted Boltzmann Machine



- ◆ Replace Gaussian prior with Boltzmann prior.
- ◆ More expressiveness.
- ◆ However, this comes at a cost.

Quantum-Assisted Discrete VAE



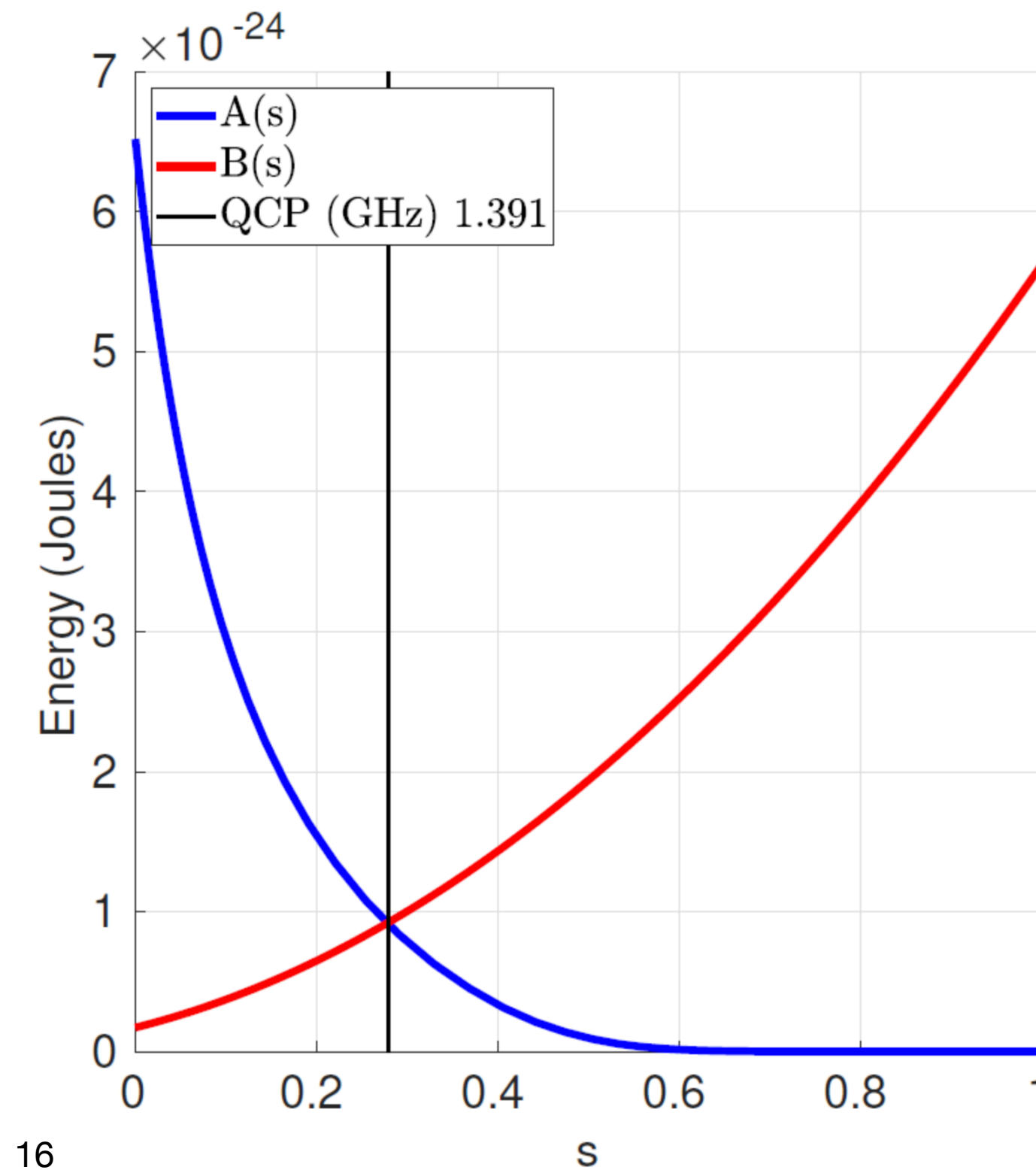
- ◆ Replace Gaussian prior with Boltzmann prior.
- ◆ More expressiveness.
- ◆ However, this comes at a cost.
- ◆ But we might be able to avoid Gibbs sampling...

Quantum Annealer

Basics

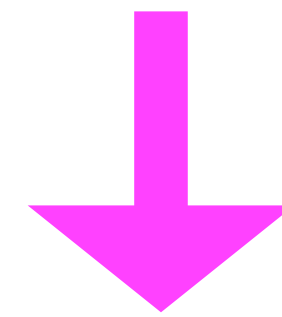
- ◆ An array of **superconducting flux quantum bits** with **programmable spin-spin couplings** and **self-fields**.
- ◆ Relies on the Adiabatic Approximation.
- ◆ The goal is to find the ground state of a Hamiltonian H_0 .
- ◆ In practice, quantum annealers have a strong interaction with the environment which lead to **thermalization** and **decoherence**. It can also reach a **dynamical arrest**.

$$\mathcal{H}_{ising} = \underbrace{-\frac{A(s)}{2} \left(\sum_i \hat{\sigma}_x^{(i)} \right)}_{\text{Initial Hamiltonian } H_1} + \underbrace{\frac{B(s)}{2} \left(\sum_i C_i \hat{\sigma}_z^{(i)} + \sum_{i>j} J_{i,j} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)} \right)}_{\text{Final Hamiltonian } H_0}$$



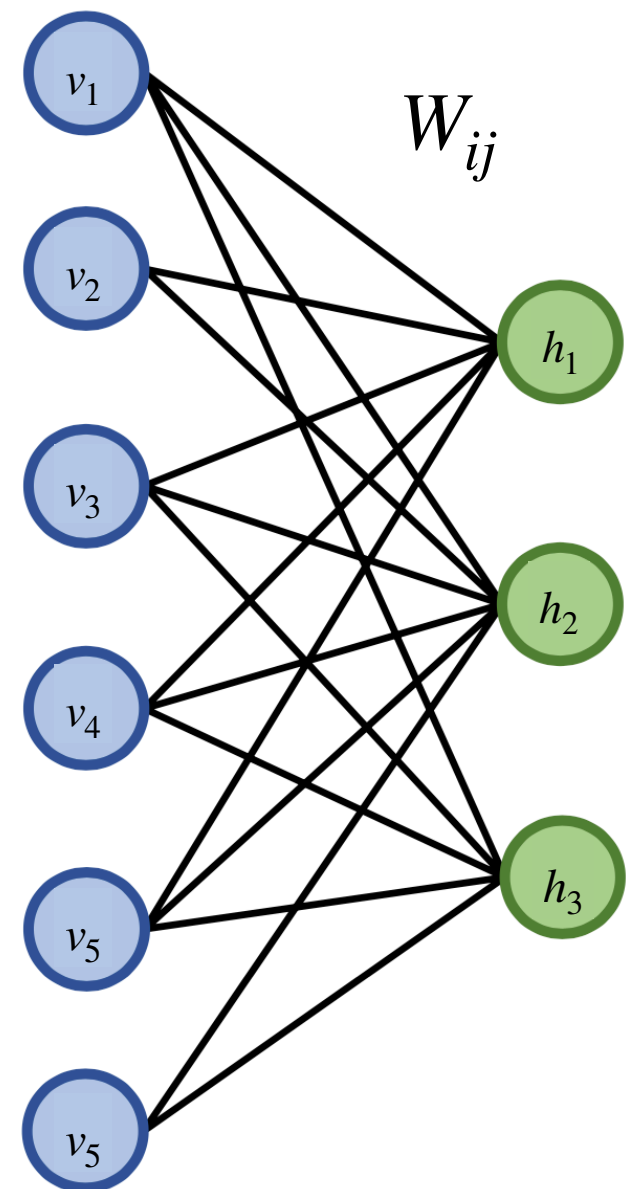
Quantum Annealer

Topologies



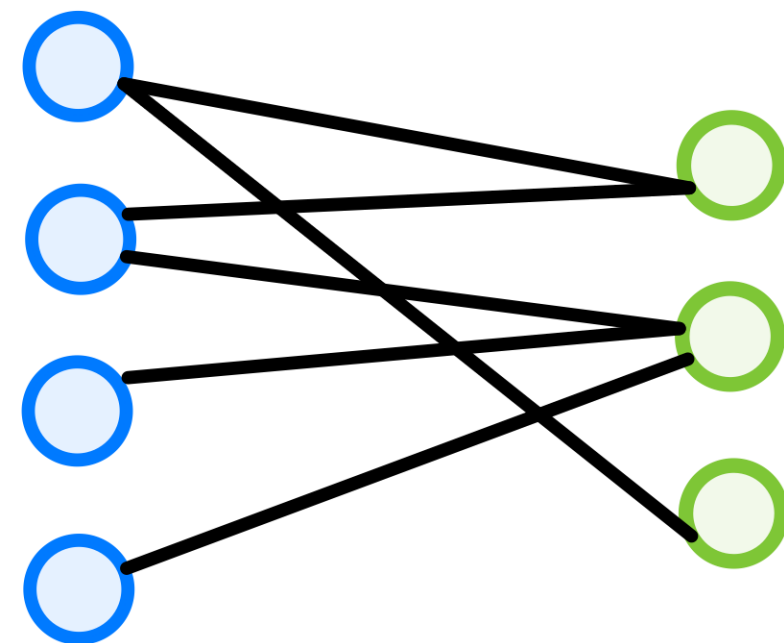
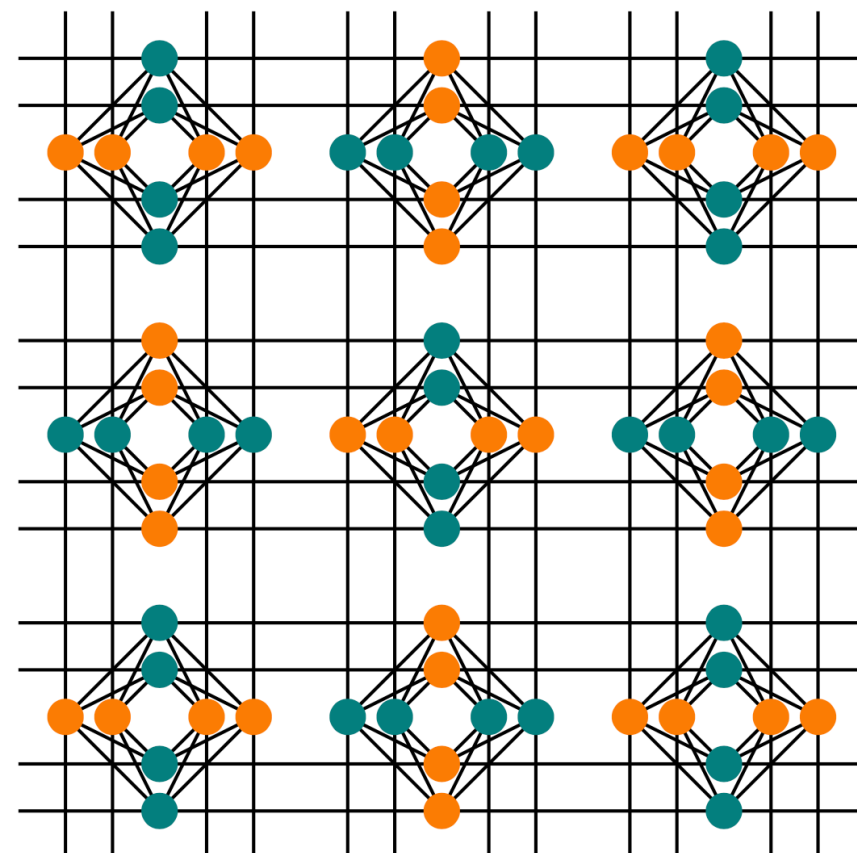
Fully Connected RBM

2-partite Graph



Chimera QA

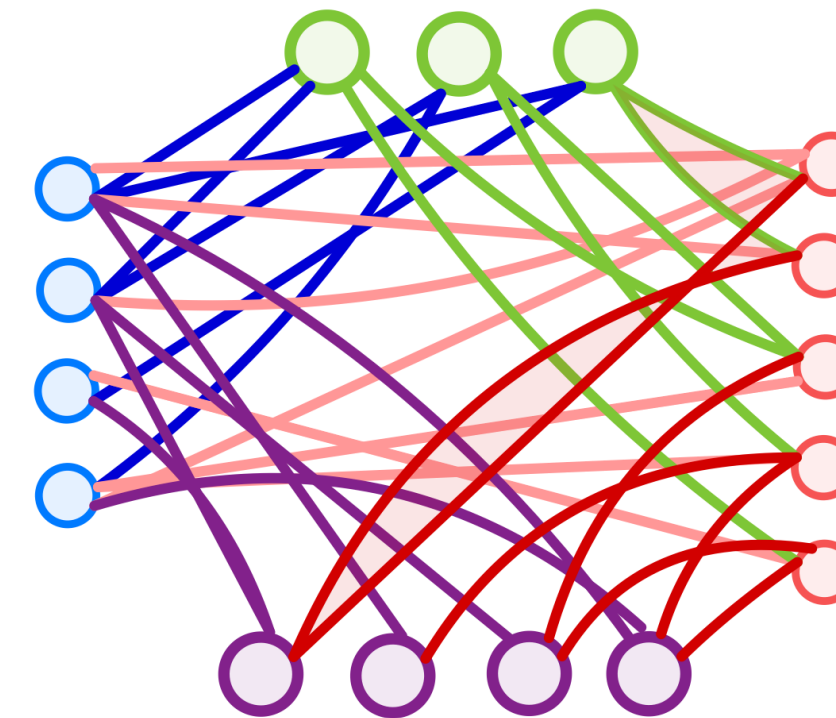
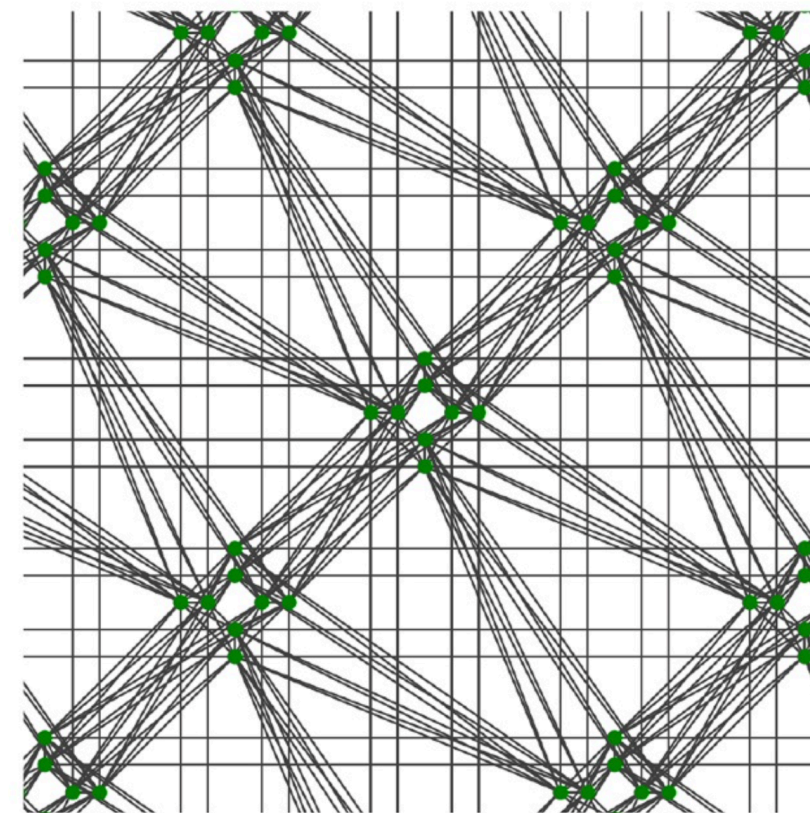
2-partite Graph



Pegasus QA

4-partite Graph

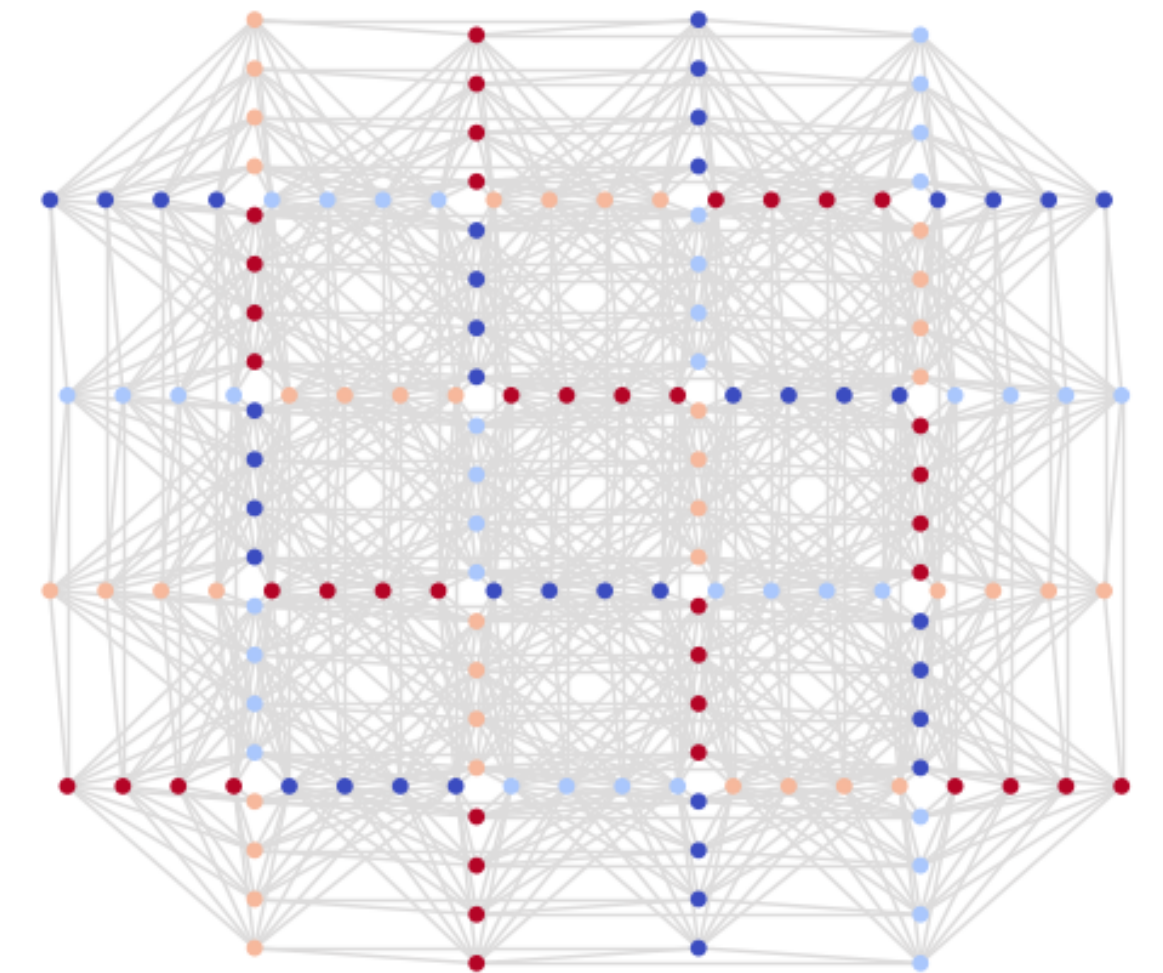
Max coord num=15



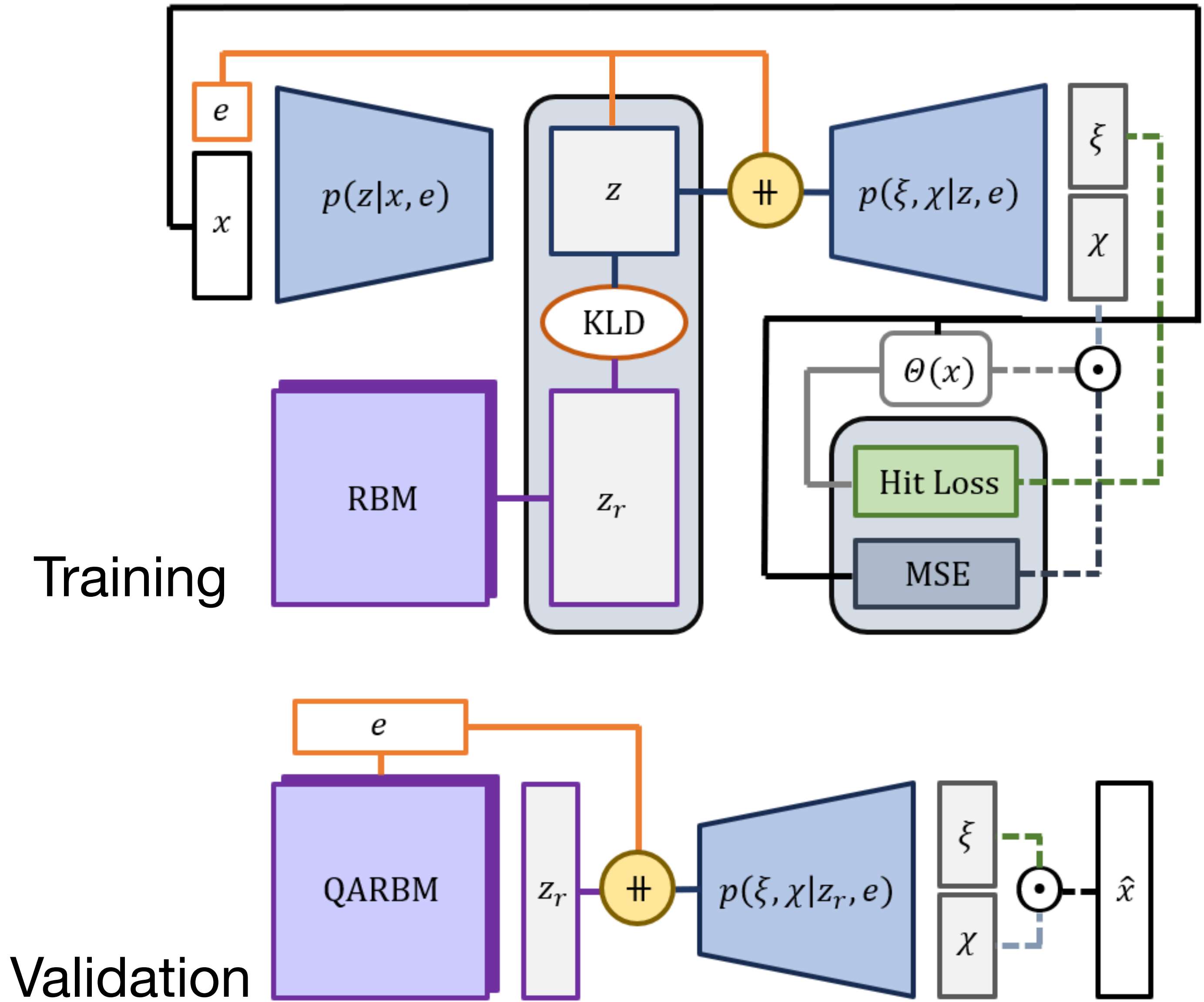
Zephyr QA

4-partite Graph

Max coord num=20



Calo4pQVAE

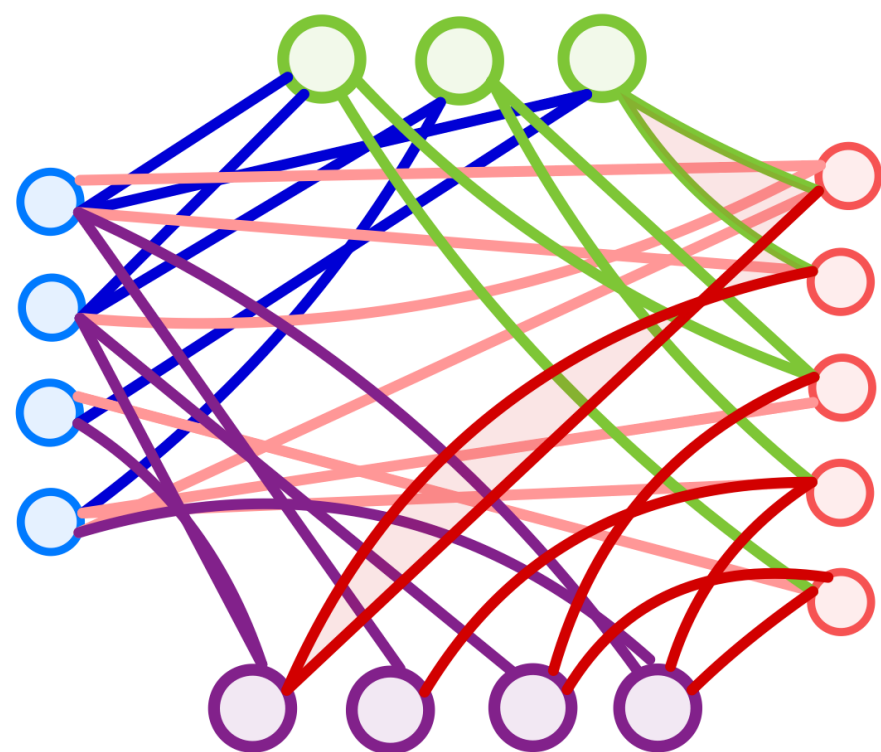
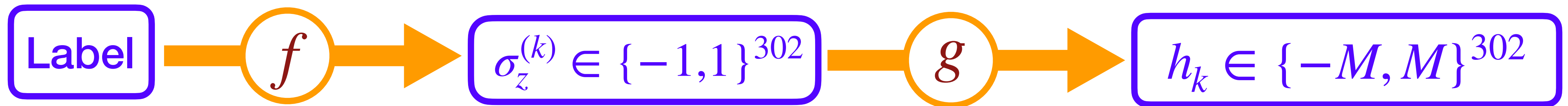


QPU conditioning

★arXiv:2410.22870

$$\sigma_z^{(i)} = \begin{cases} 1 & h_i < 0 \text{ and } |h_i| > \sum_j |J_{ij}| \\ -1 & h_i > 0 \text{ and } |h_i| > \sum_j |J_{ij}| \end{cases}$$

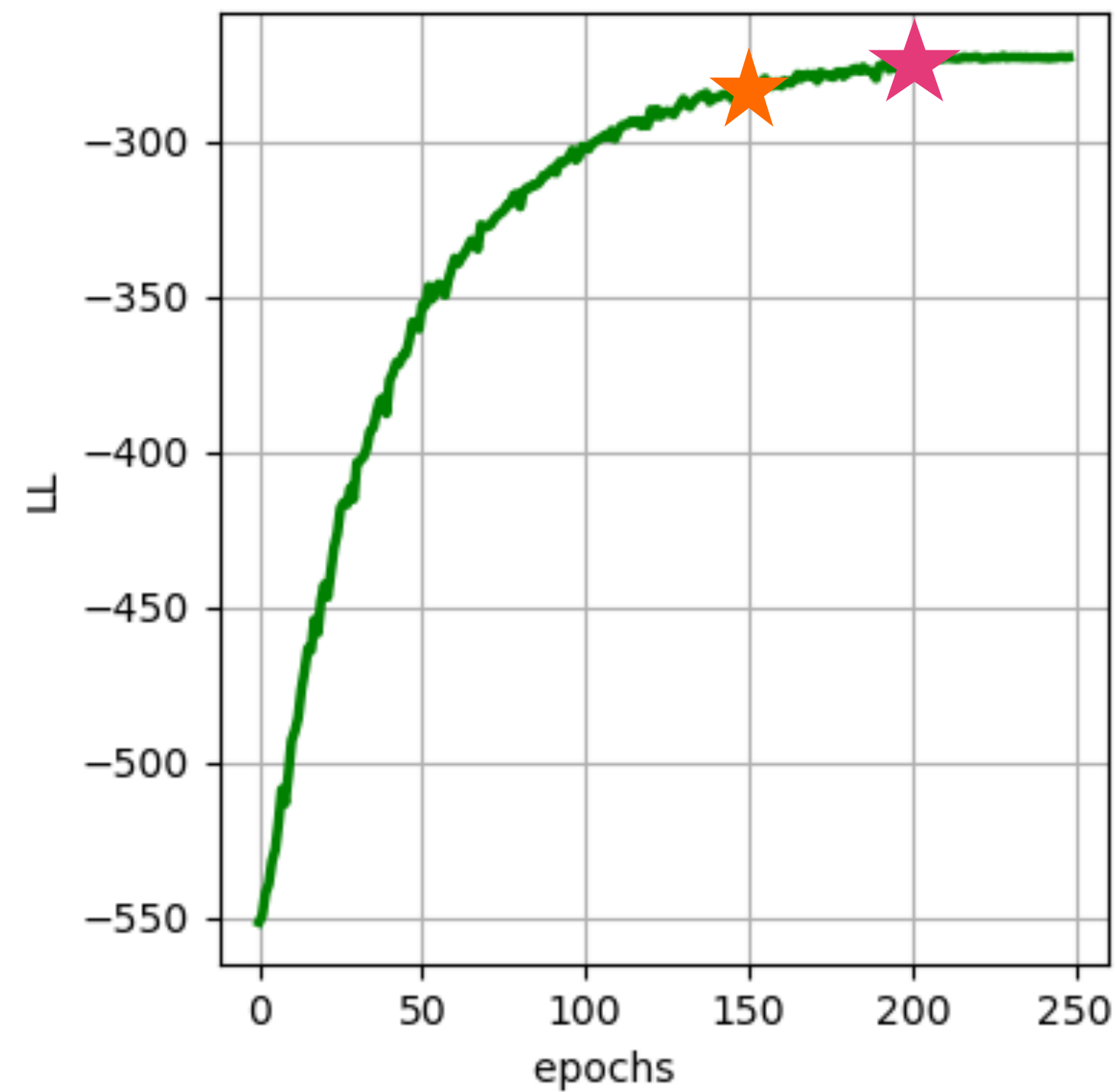
$k = 1, \dots, 302$ (Condition partition)



$$\mathcal{H}_{ising} = \underbrace{-\frac{A(s)}{2} \left(\sum_i \hat{\sigma}_x^{(i)} \right)}_{\text{Initial Hamiltonian}} + \underbrace{\frac{B(s)}{2} \left(\sum_i h_i \hat{\sigma}_z^{(i)} + \sum_{i>j} J_{i,j} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)} \right)}_{\text{Final Hamiltonian}}$$

Results

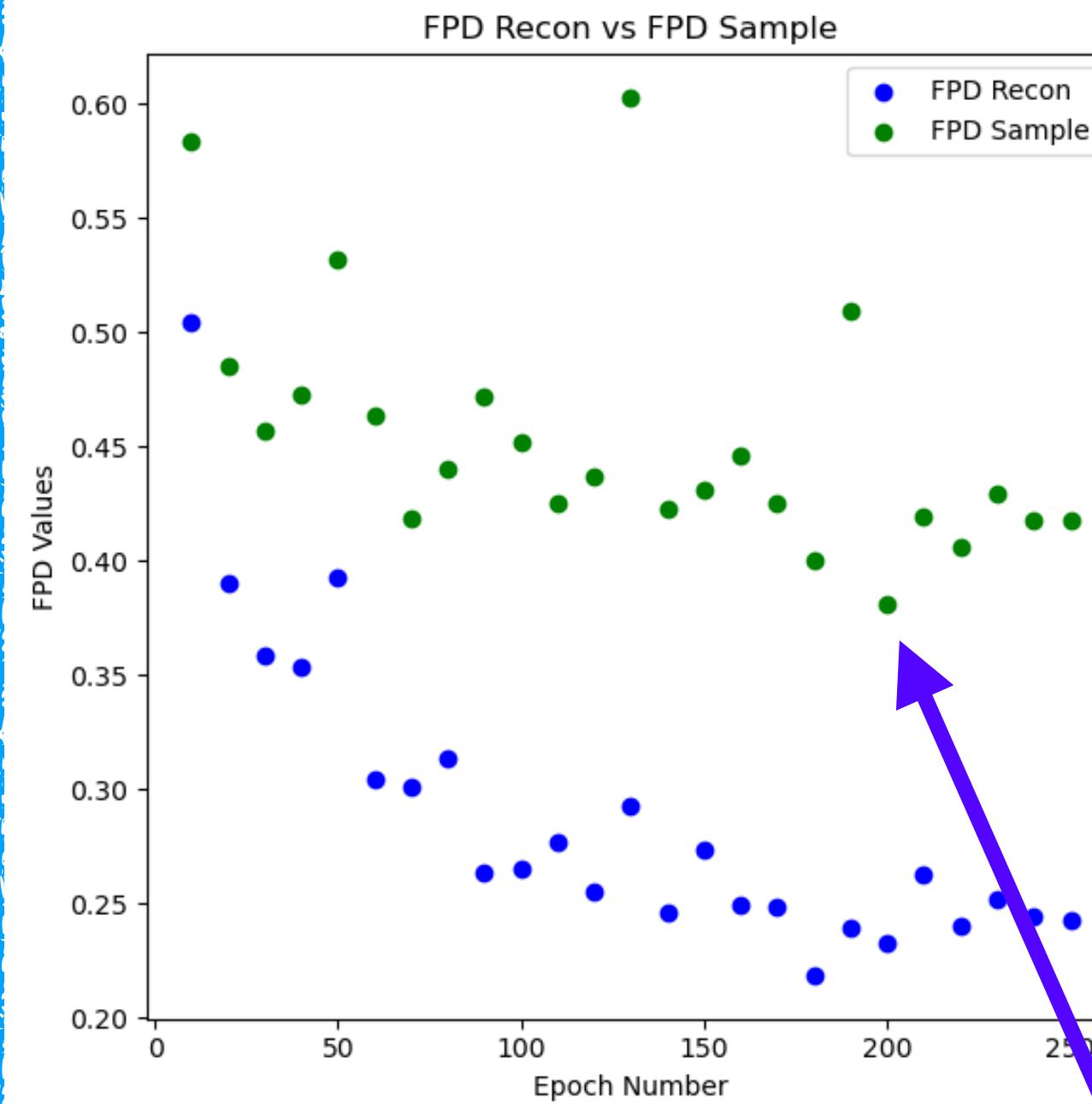
RBM Log-likelihood saturates, indicating the RBM has trained.



★ Slope annealing ends

★ Encoder and decoder params frozen

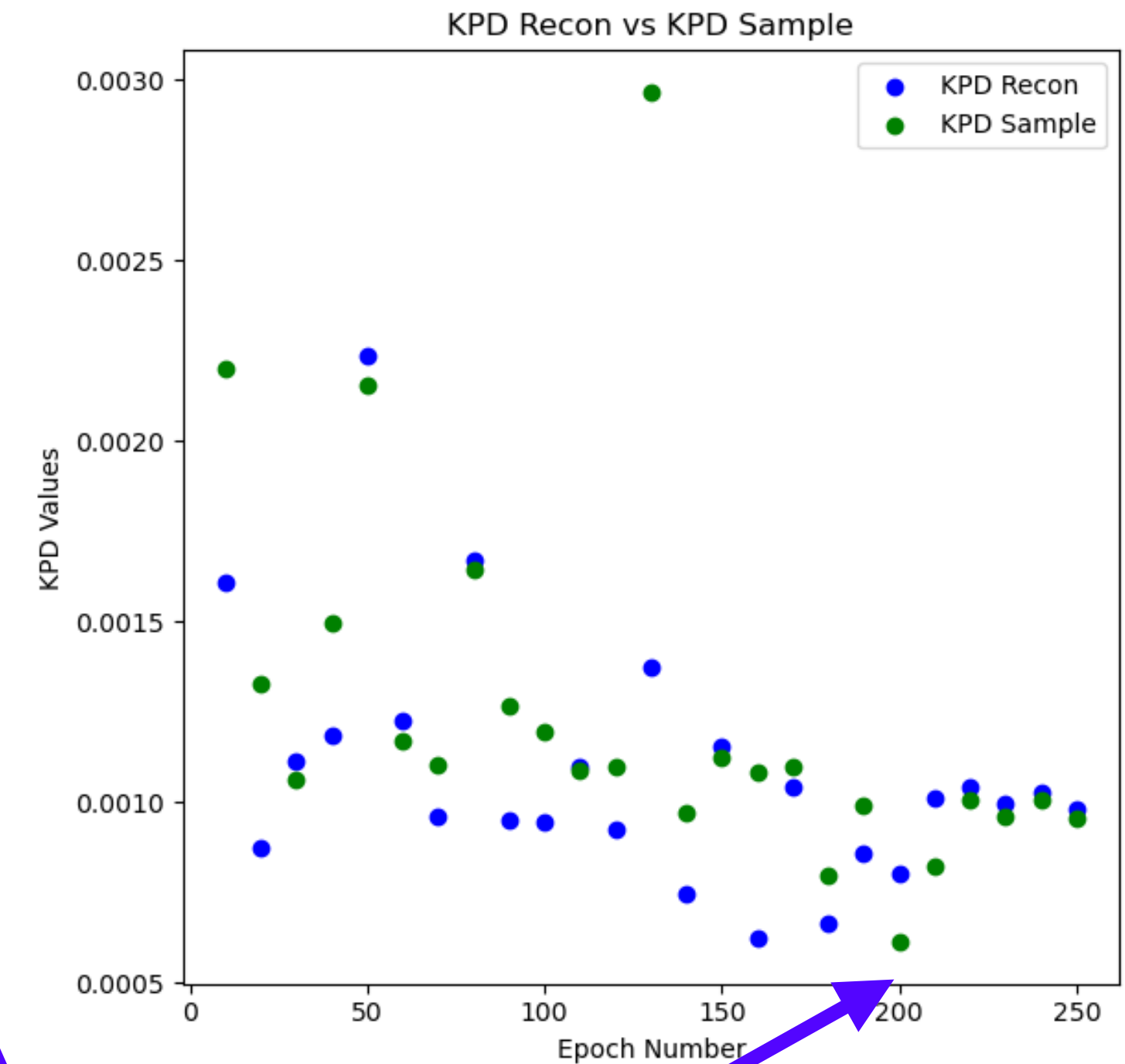
Frechet Particle Distance



$$FPD(\times 10^3) = 380.7 \pm 1.1$$

$$KPD(\times 10^3) = 0.61 \pm 0.06$$

Kernel Particle Distance



Following results correspond to model instance = epoch 200

Results

QA temperature estimation

★ arXiv:2410.22870

System QA at
Temperature $1/\beta_{QA}$

System B at
Temperature $1/\beta$

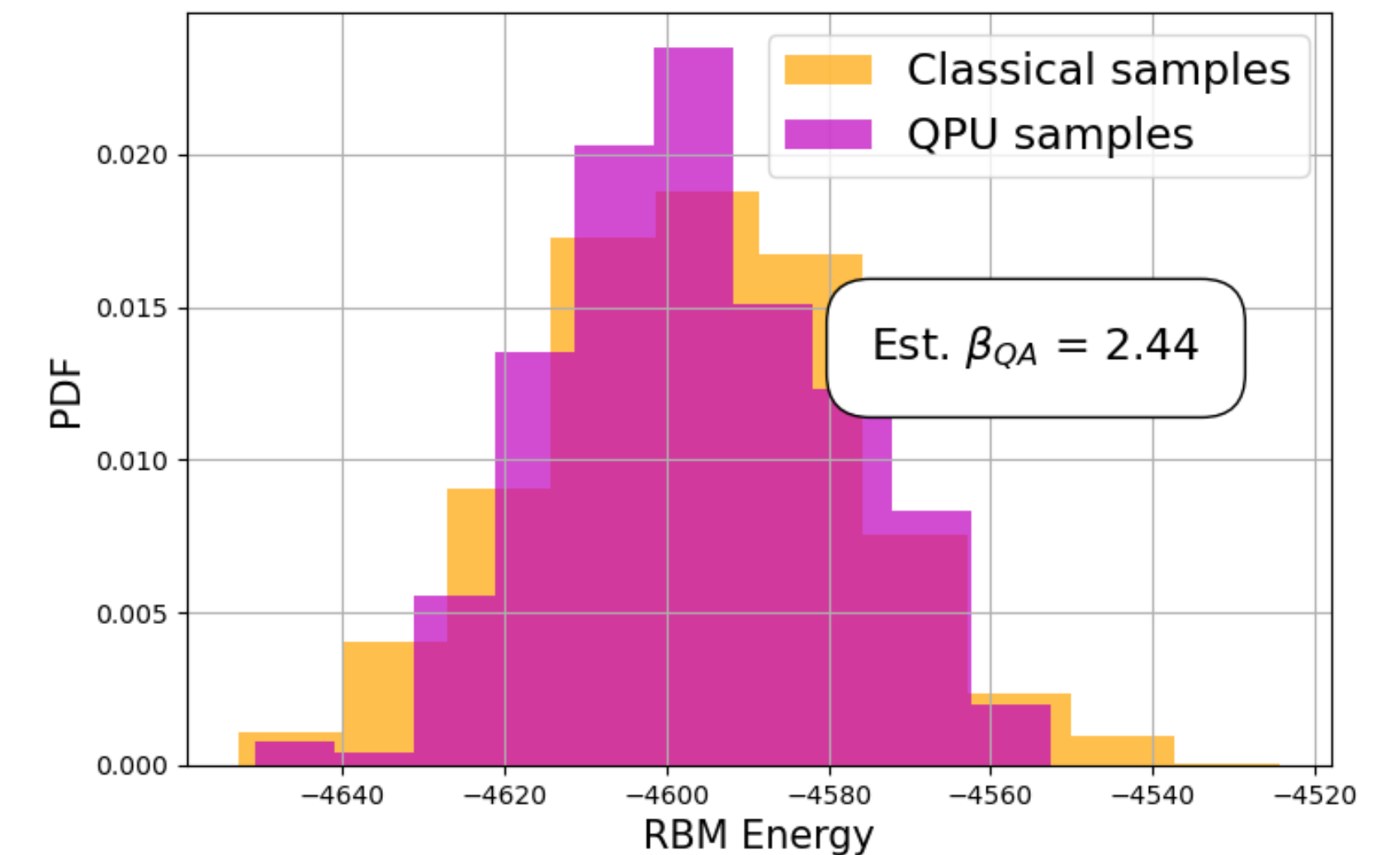
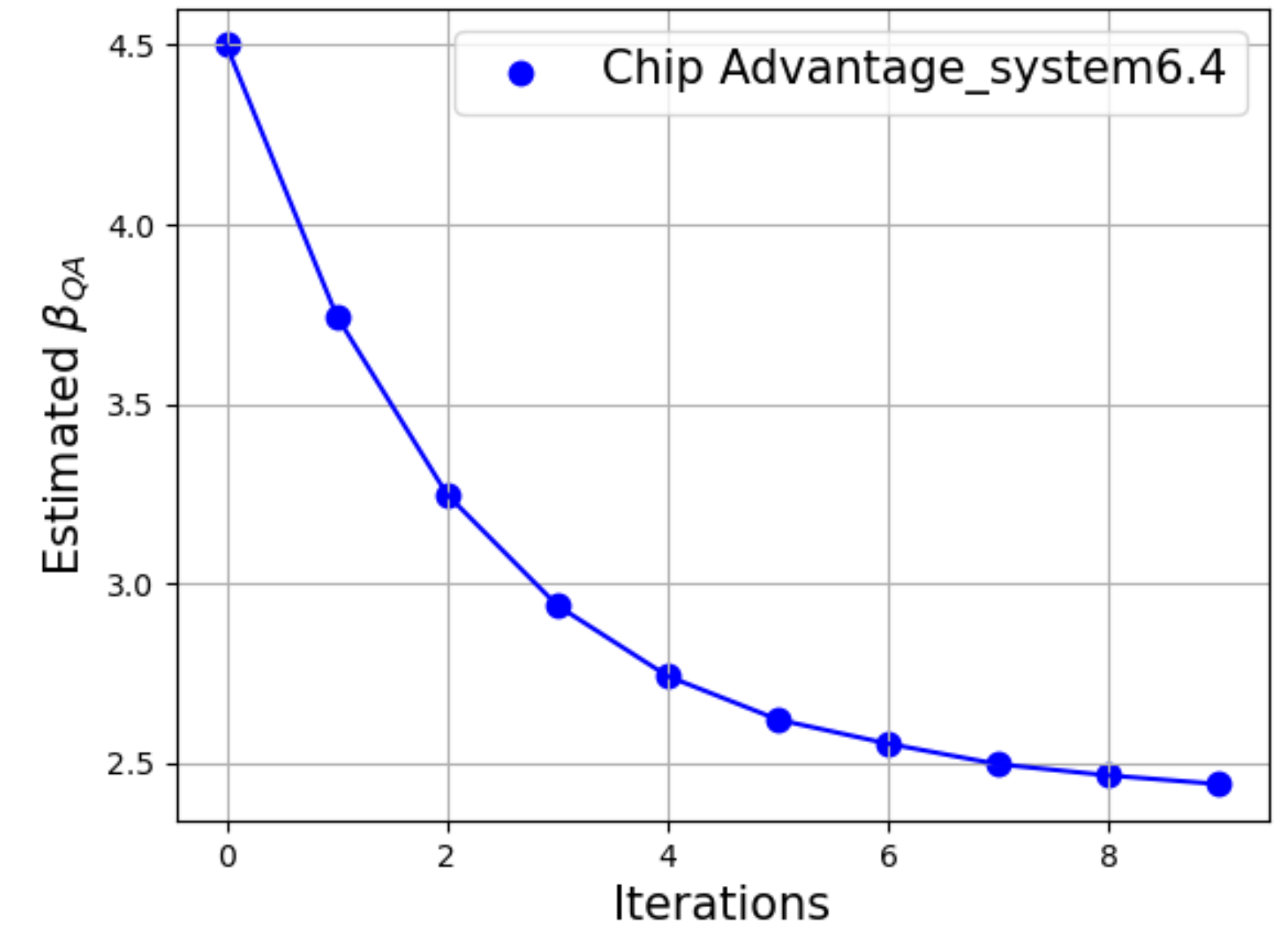
$$P_{QA}(x) = \frac{e^{-\beta_{QA}H(x)}}{Z(\beta_{QA})}$$

$$P_B(x) = \frac{e^{-\beta H(x)}}{Z(\beta)}$$

- ◆ Equate entropy of system QA to entropy of system B
- ◆ Assume $\beta = \beta_{QA} + \Delta\beta$

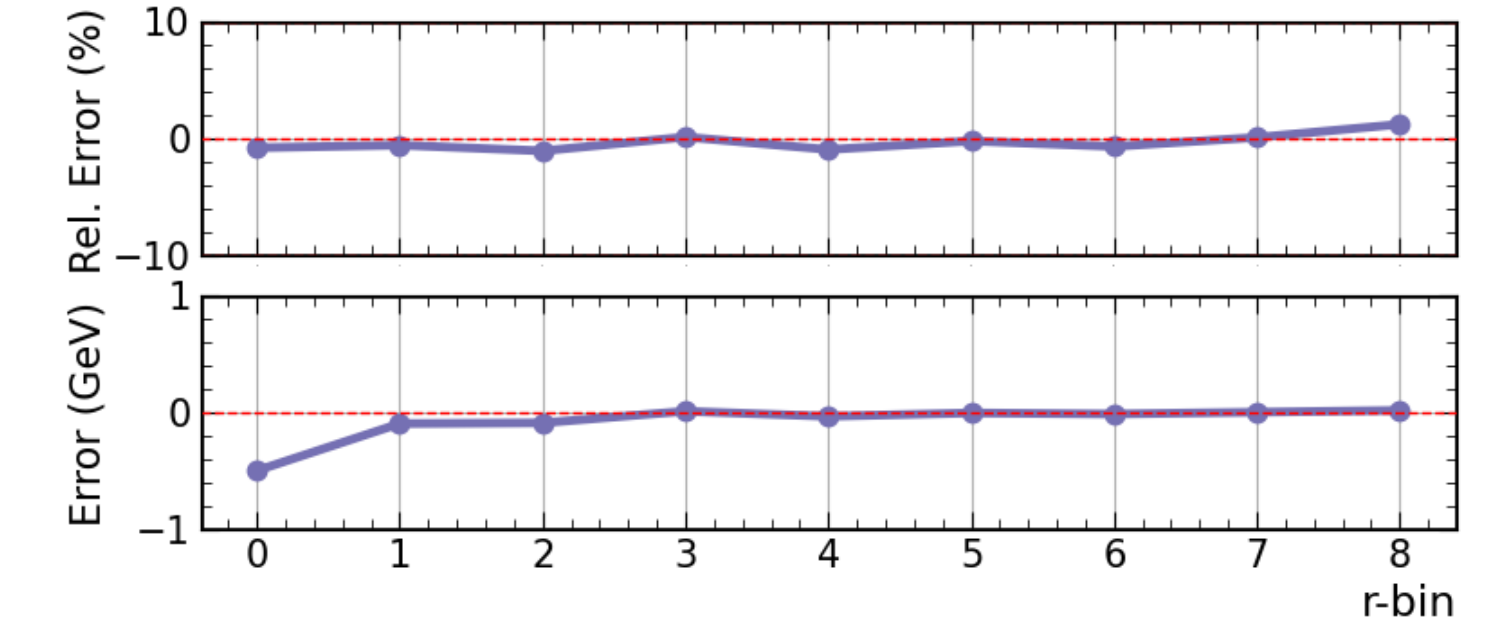
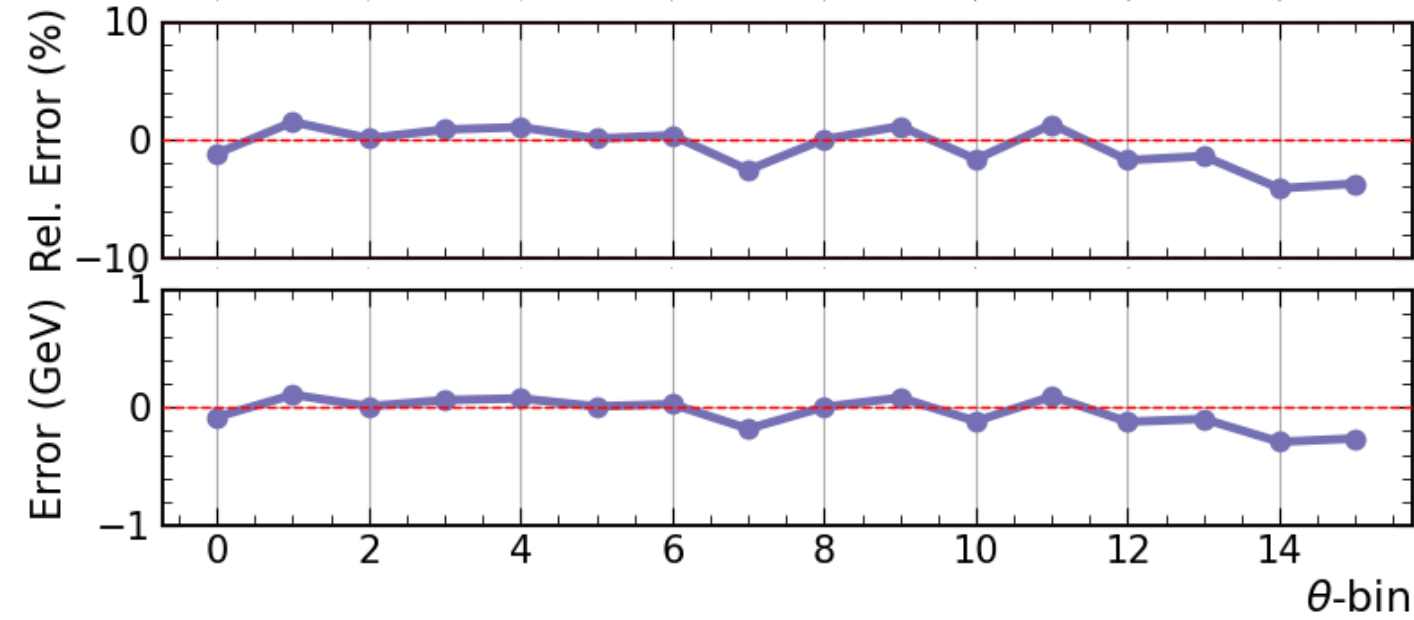
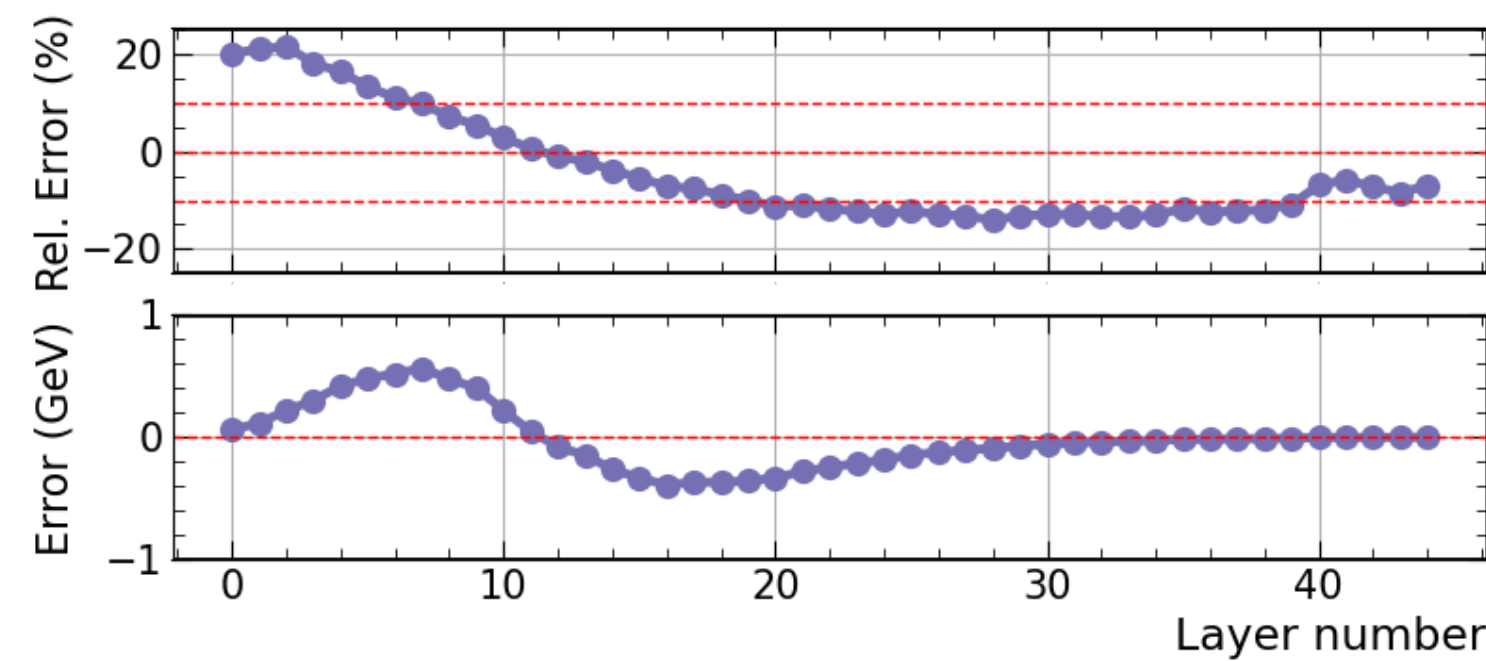
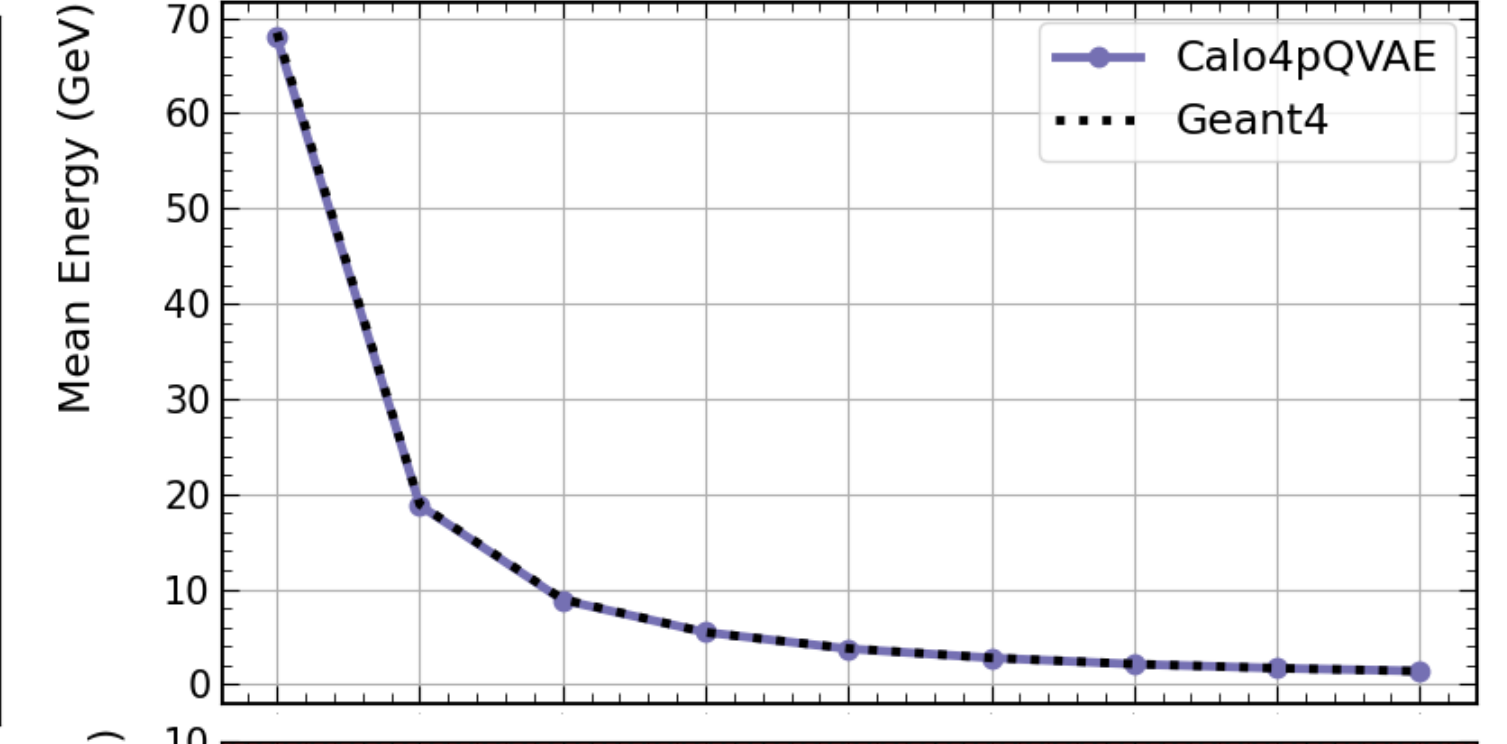
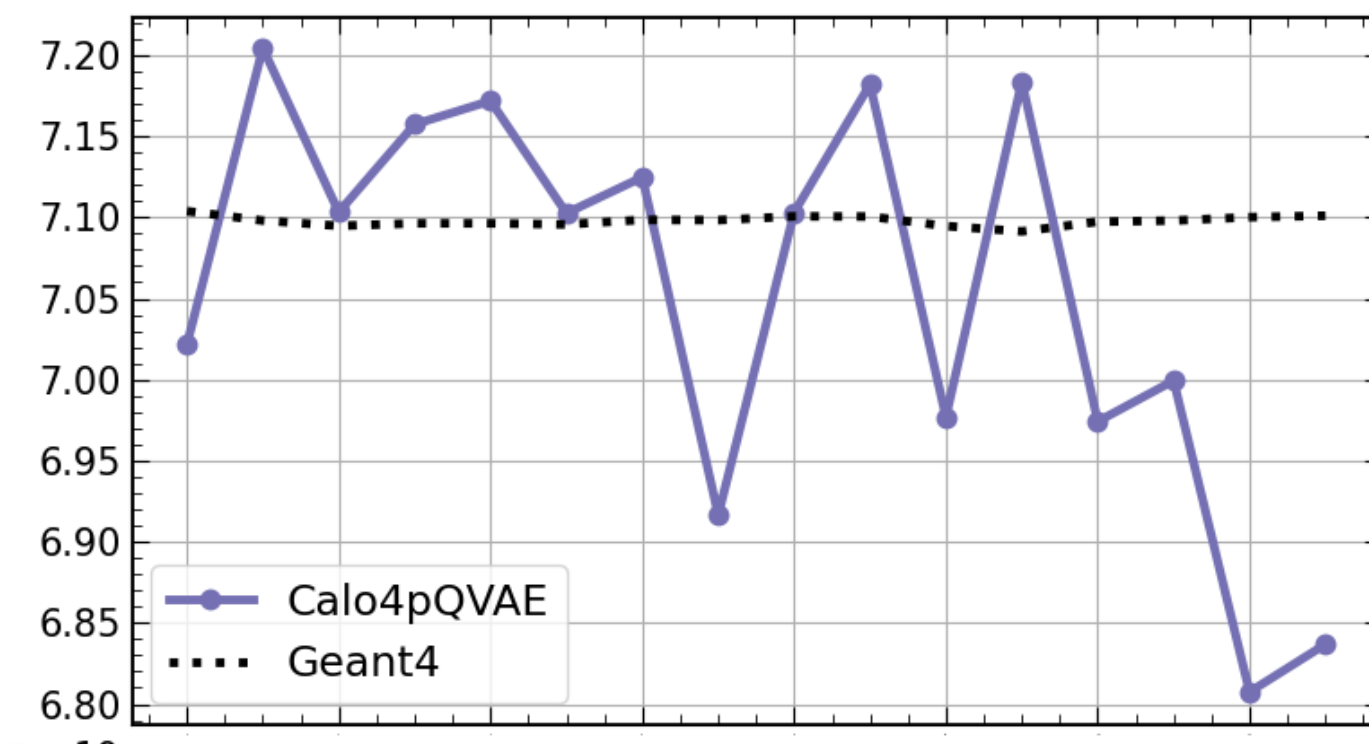
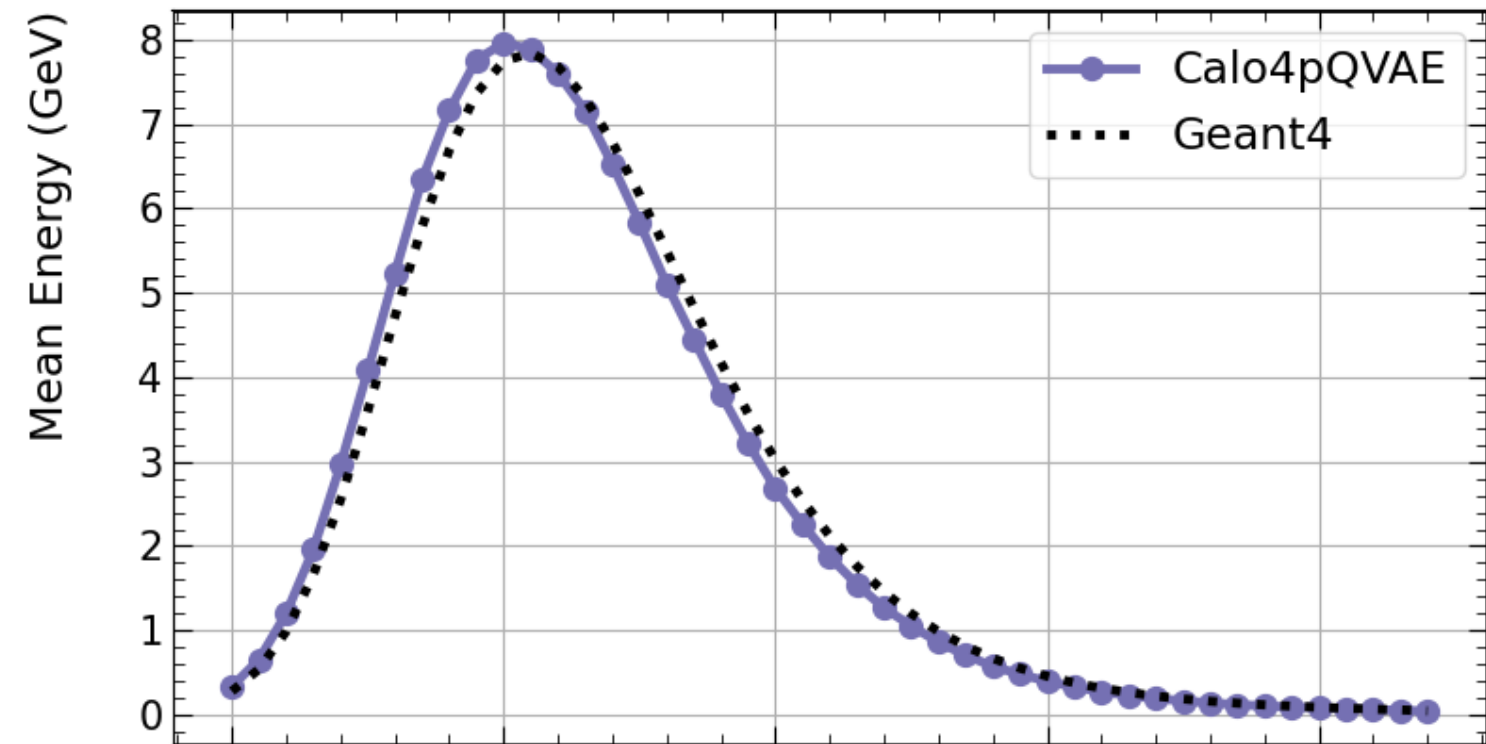
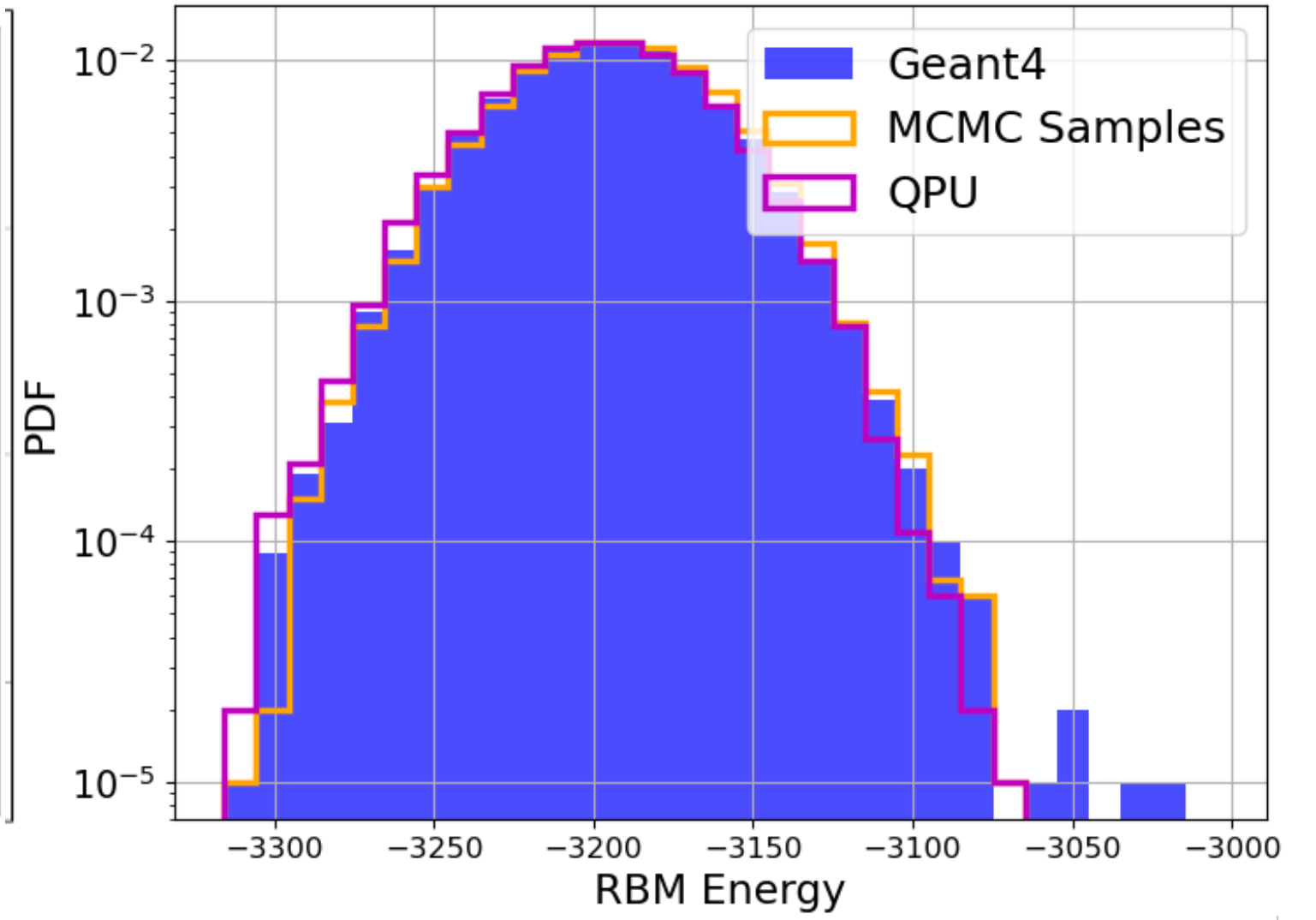
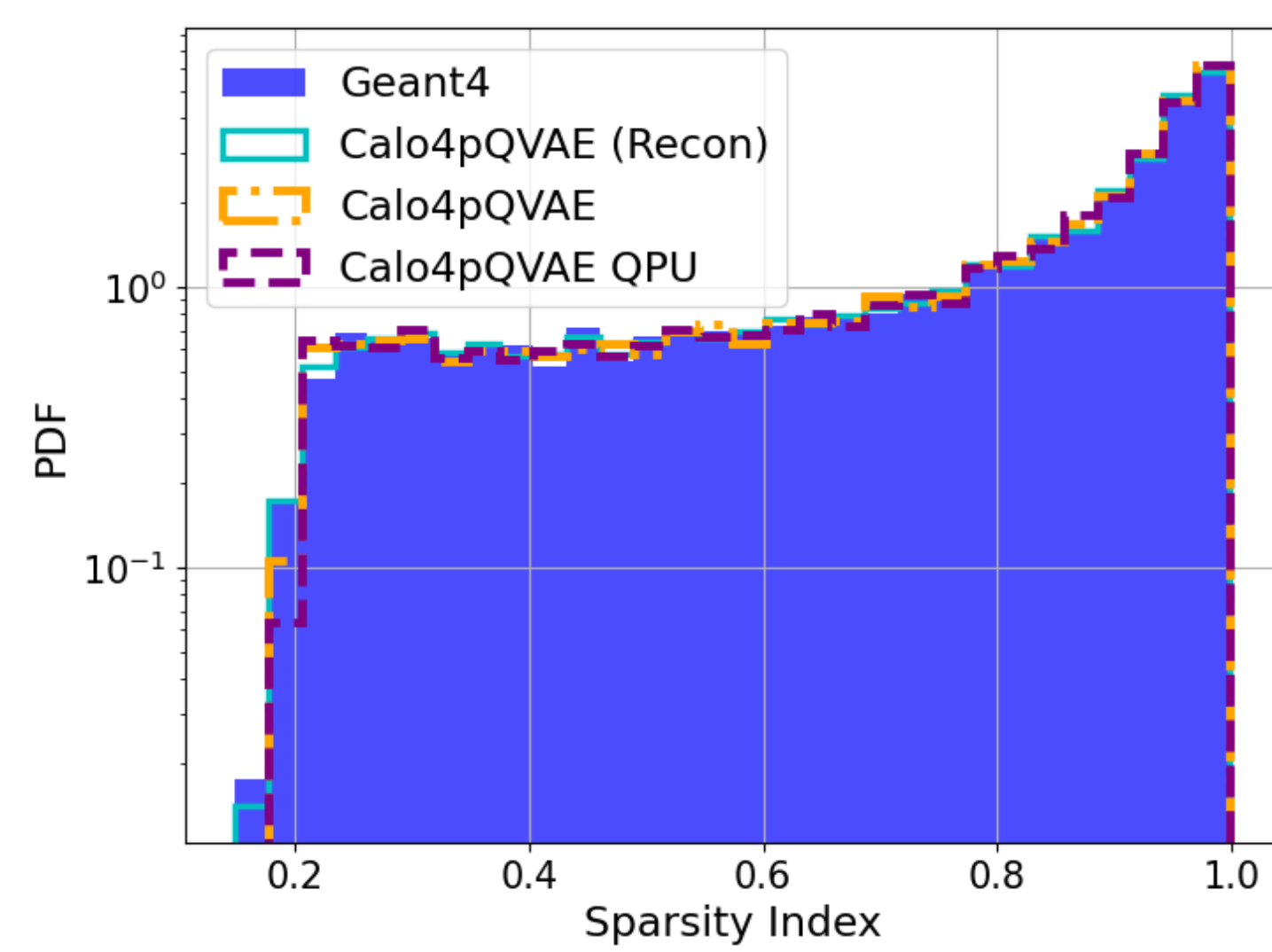
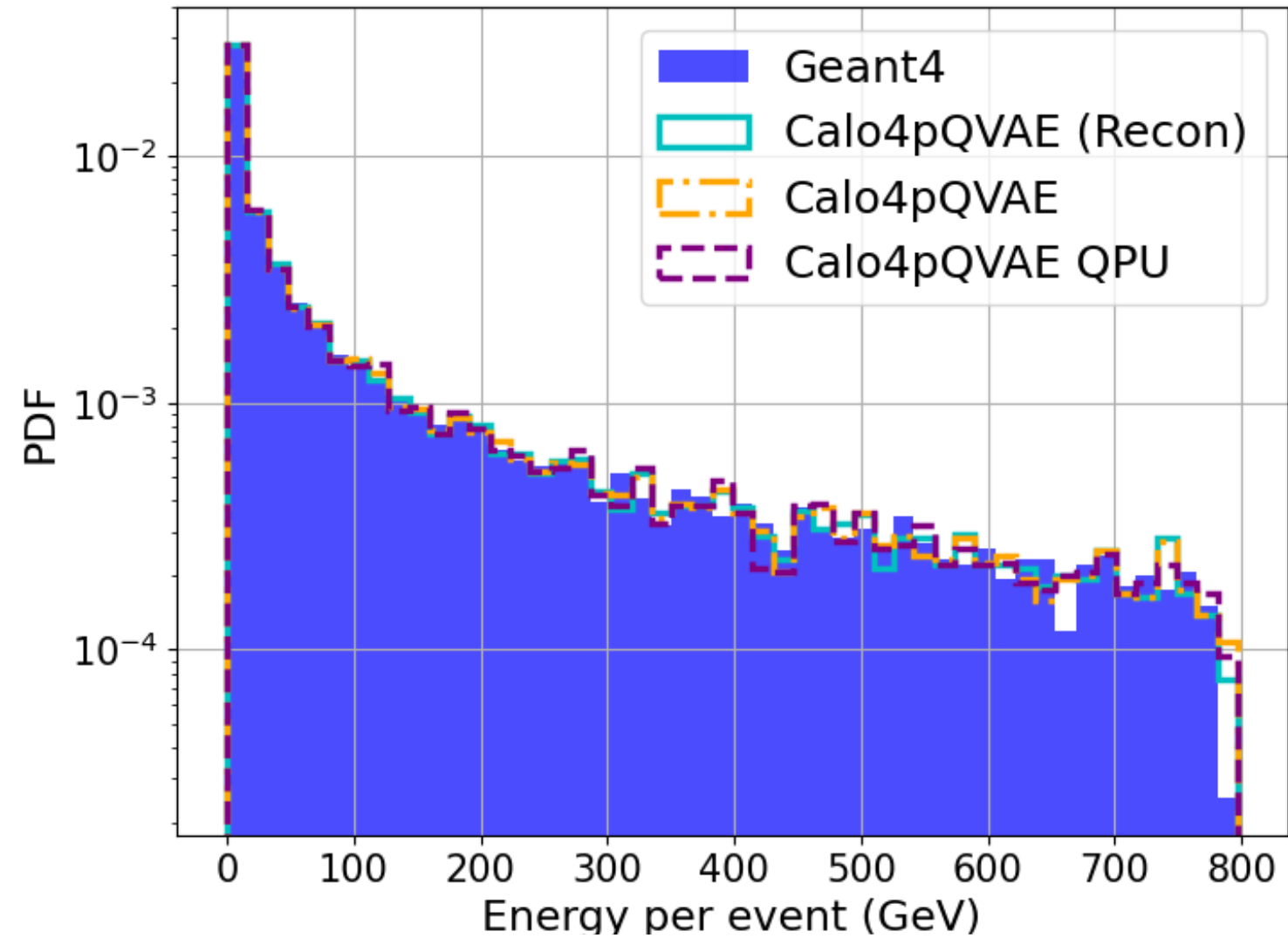
$$\beta_{t+1} = f_\delta(\beta_t) \equiv \beta_t \left(\frac{\langle H \rangle_{QA(r)}}{\langle H \rangle_{B(1)}} \right)^\delta$$

QA inverse temperature estimation



Results

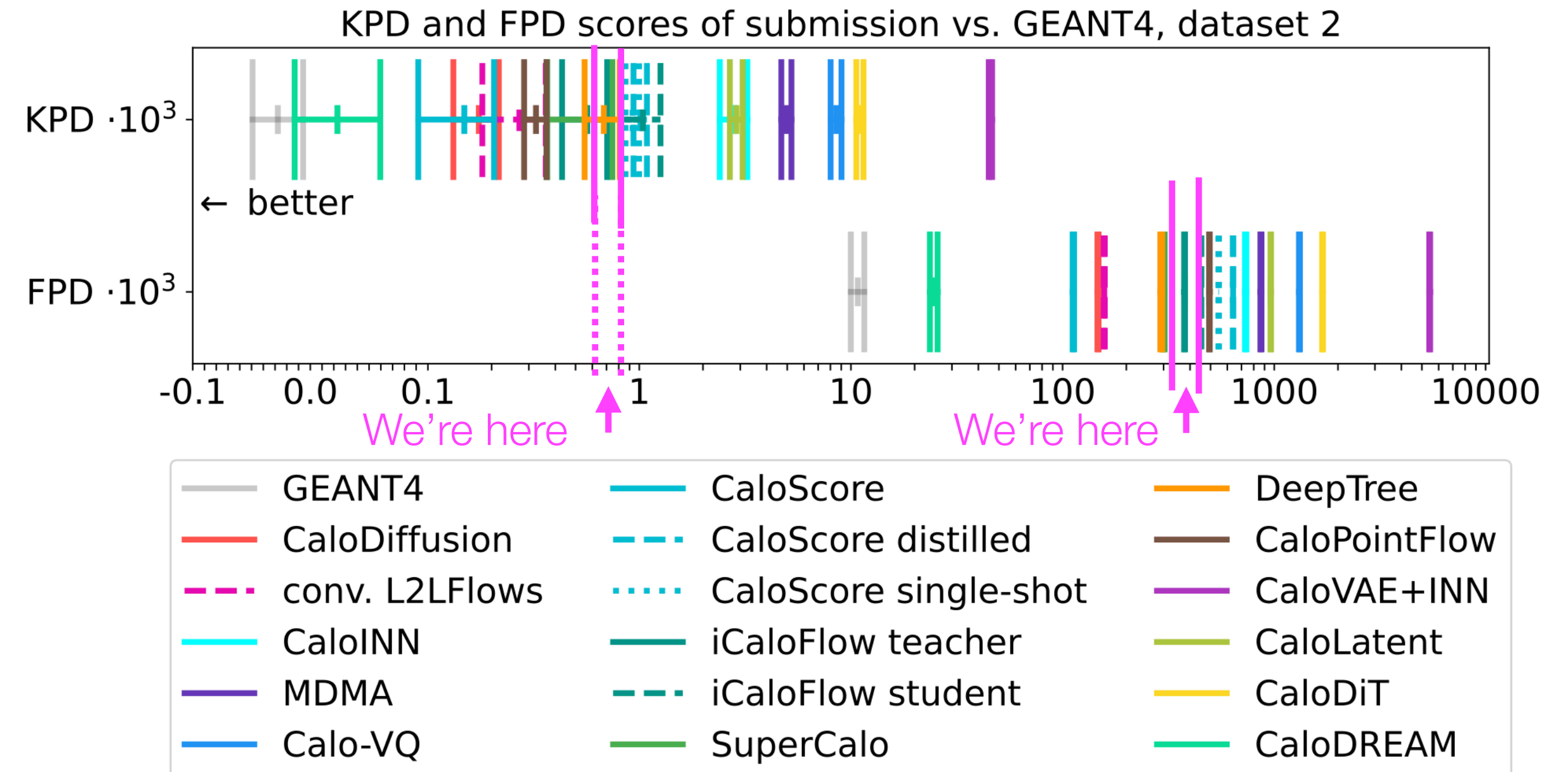
★ arXiv:2410.22870



Discussion / Conclusions / Perspectives

	GEANT4	GPU (A100)	QPU	Annealing time
Time	~ 1 s	~ 2 ms	0.2 ms	~ 0.02 ms

	FPD ($\times 10^3$)	KPD ($\times 10^3$)
Pegasus	443.0 ± 2.4	0.84 ± 0.1
Zephyr	380.7 ± 1.1	0.61 ± 0.06
Zephyr	362.7 ± 1.7	0.57 ± 0.08



- ◆ In the process of getting dataset from ATLAS.
- ◆ Implementing hierarchical decoder.
- ◆ Training using QPU.

Acknowledgements

Undergrads:

- ◆ Ian Lu @ UofT
- ◆ Deniz Sogutlu @ UBC

PhDs:

- ◆ Hao Jia @ UBC

PIs

- ◆ Eric Paquet @ NRC
- ◆ Colin Gay @ UBC
- ◆ Roger Melko @ Perimeter Institute
- ◆ Geoffrey Fox @ University of Virginia
- ◆ Max Swiatlowski @ TRIUMF
- ◆ Wojtek Fedorko @ TRIUMF

★ arXiv:2410.22870



★ Neurips ML4Phys 2024 (accepted)

★ IEEE-QCE QAI WS (2024)

★ arXiv:2312.03179

★ arXiv:2210.07430. NeurIPS 2021

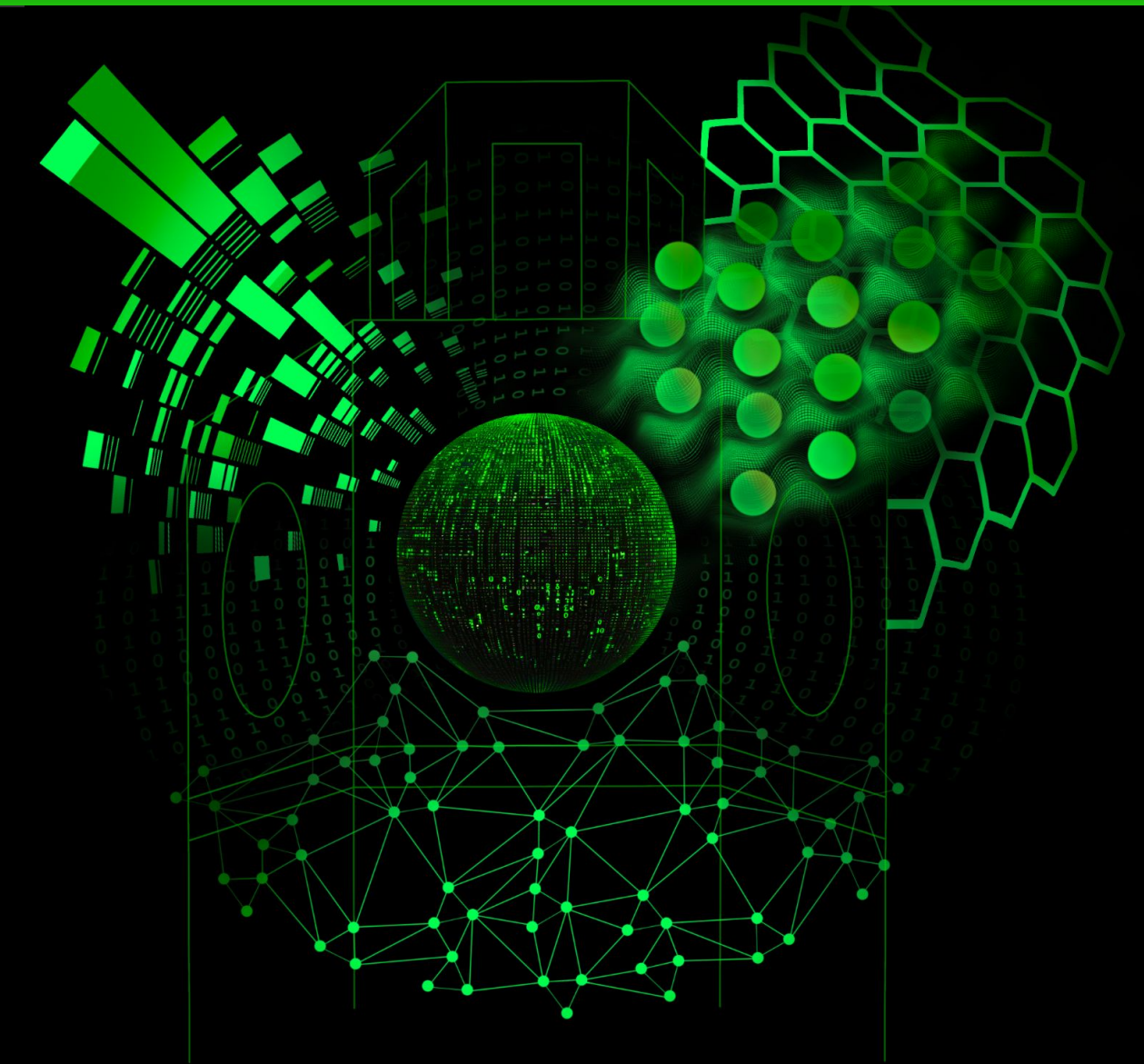
Alumni:

- ◆ Sebastian Gonzalez @ UBC
- ◆ Sehmimul Hoque @ University of Waterloo
- ◆ Abhishek Abhishek @ UBC
- ◆ Soren Andersen @ Lund University

Supported by:

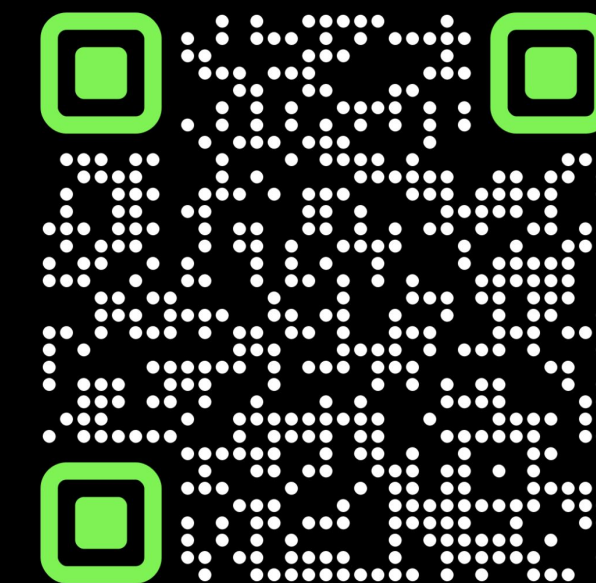
- ★ NRC AQC-002
- ★ NSERC SAPPJ-2020-00032
- ★ SAPPJ-2022-00020
- ★ NSF 2212550
- ★ DOE DE-SC0023452
- ★ Mitacs IT39533

Generative AI for High & Low Energy Physics



Nov. 03, 2025 - Dec. 19, 2025

Application deadline: Dec. 8, 2024



www.kitp.ucsb.edu/activities/genai25

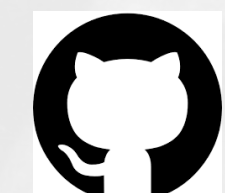
Coordinators:

James Halverson, Jessica N. Howard*, Anindita Maiti**, Roger Melko, J. Quetzalcoatl Toledo-Marín

Scientific Advisors:

Geoffrey Fox, Eun-Ah Kim, Maximilian Swiatlowski

*Lead coordinator **Diversity coordinator



QaloSim/CaloQVAE