

# Short-Range Correlations in Nuclei

## Or Hen – MIT



# Nuclear Physics and Neutrino Oscillations

**Issue I:** Incident neutrino energy reconstruction from the measured final state.

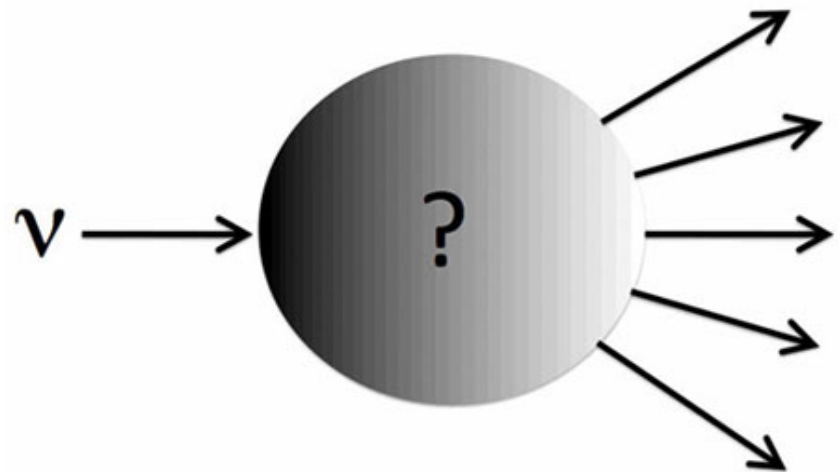
**Issue II:** Interaction cross-section defines the 'no oscillation' baseline.

**Issue III:** proton-neutron dynamics can induce non CPV differences between neutrino and anti-neutrino interaction rates.

...

## Nuclear Physics Inputs:

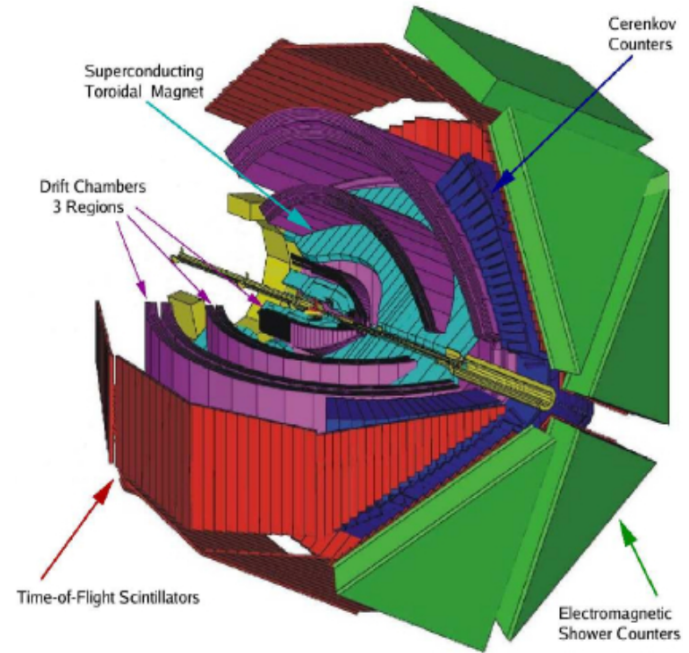
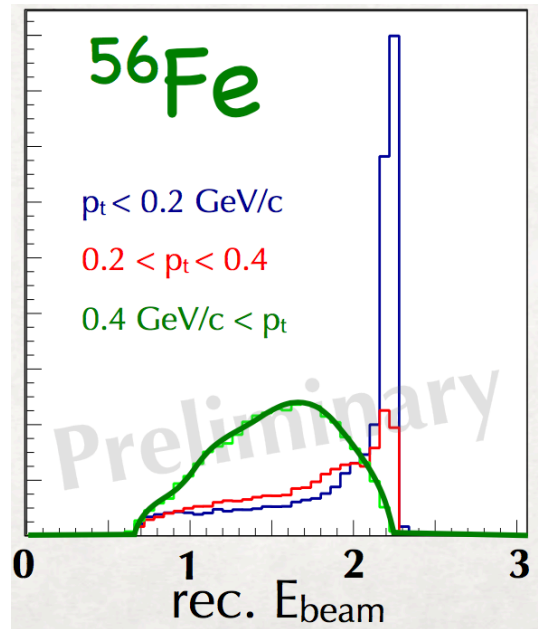
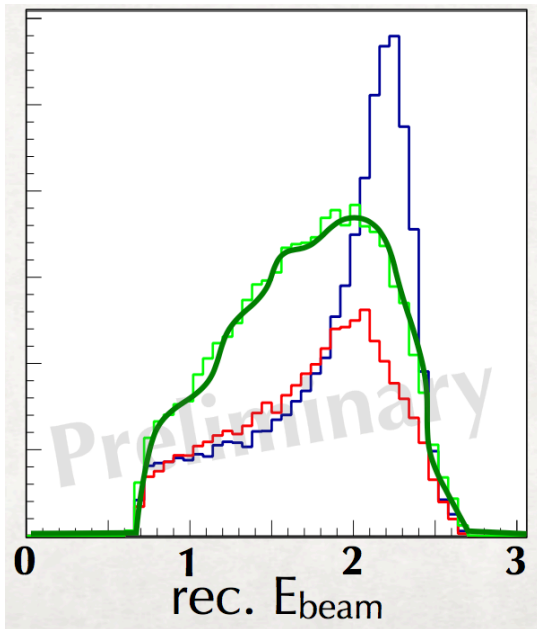
- **Model of the *Nucleus*.**
- **Model of the *Interaction*.**



# Nuclear Physics and Neutrino Oscillations

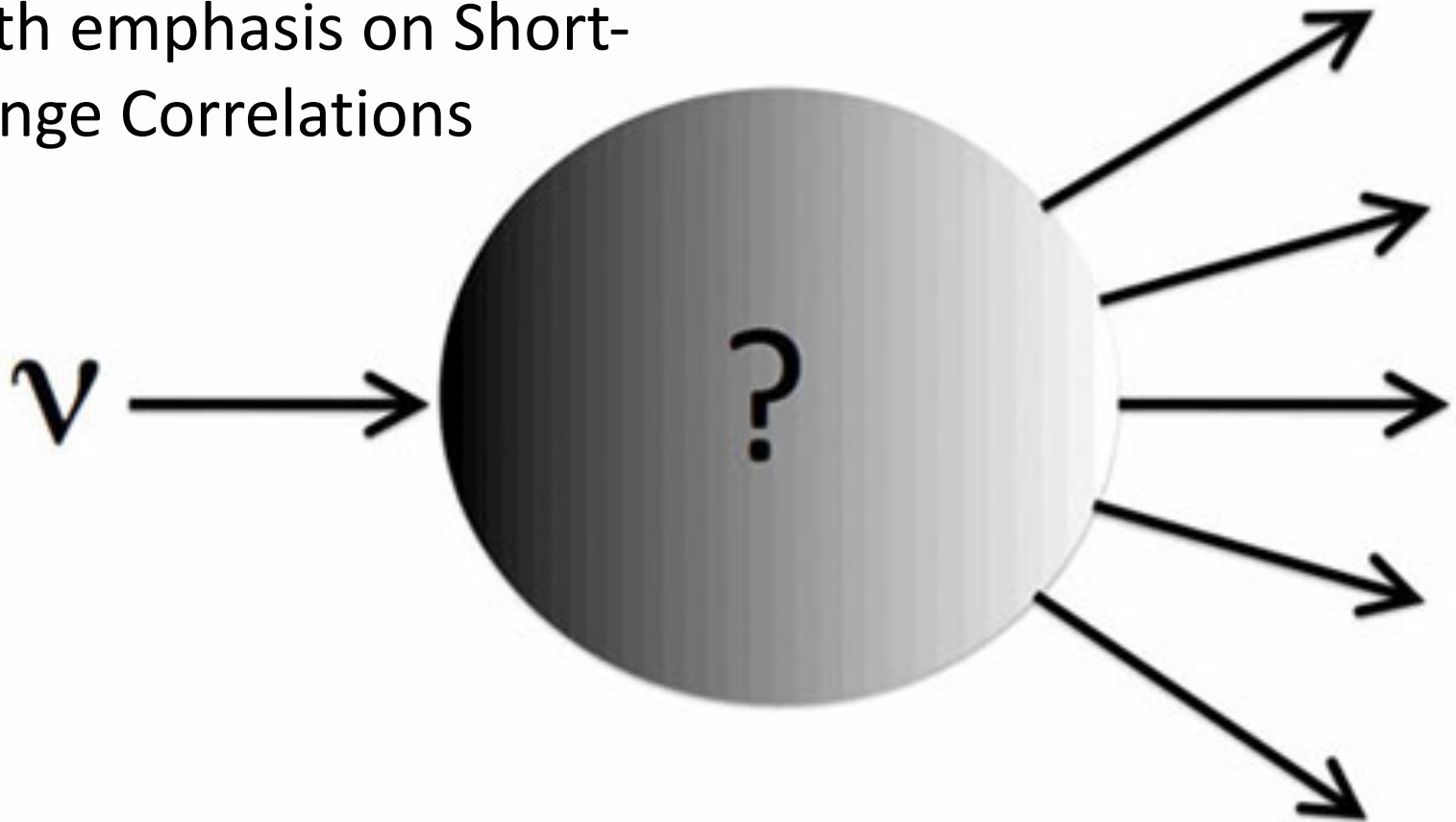
Using JLab CLAS data to study incident neutrino energy reconstruction and reaction modeling.

See talk by  
M. Khachatryan  
and E. Cohen



# Nuclear Physics and Neutrino Oscillations

Today: Improve modeling of the nuclear ground state, with emphasis on Short-Range Correlations





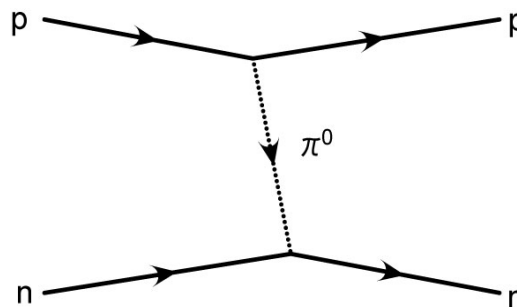
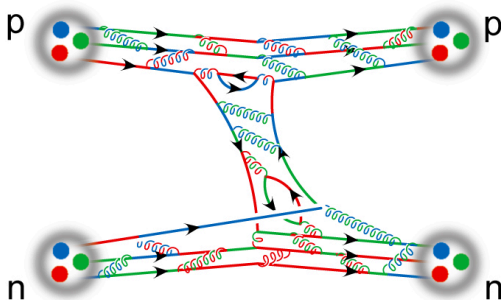
# Nuclear Many-Body Challenge

## Many-body Schrödinger Equation

$$\sum_i \left\{ -\frac{\hbar^2}{2m_i} \nabla_i^2 \Psi(\vec{r}_1, \dots, \vec{r}_N, t) \right\} + U(\vec{r}_1, \dots, \vec{r}_N) \Psi(\vec{r}_1, \dots, \vec{r}_N, t) = i\hbar \frac{\partial}{\partial t} \Psi(\vec{r}_1, \dots, \vec{r}_N, t)$$

### Main Challenges:

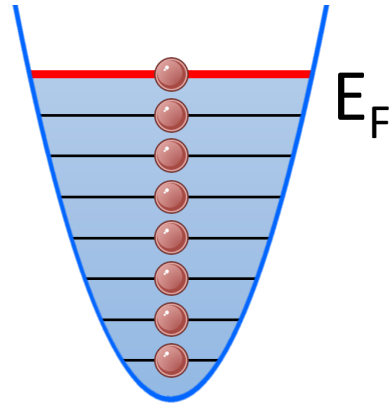
1. No 'fundamental' Interaction.
2. Complex phenomenological parametrizations (e.g. over 18 operators)



Remarkable progress – see talks by Carlson and Lovato

# Solution: Effective Theories

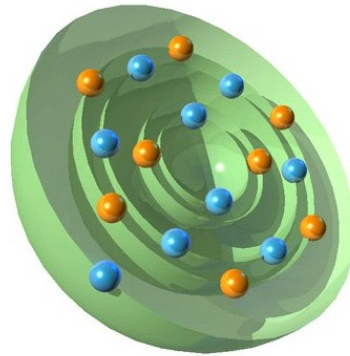
Fermi  
Gas  
Model



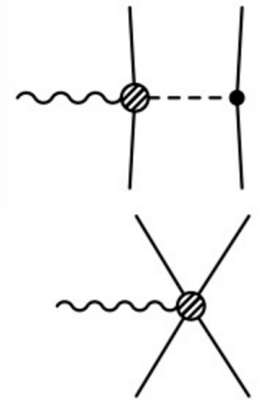
Liquid  
Drop  
Model



Shell  
Model



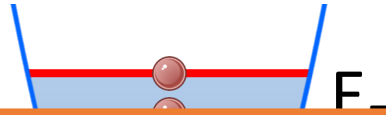
Chiral  
Perturbation  
Theory\*



\* Should converge to exact solution

# Solution: Effective Theories

Fermi



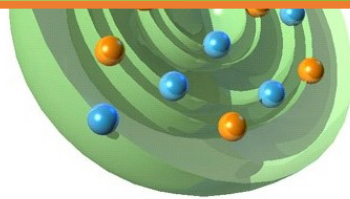
Liquid



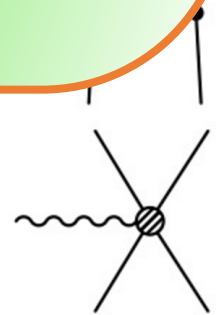
Common idea:

Scale separation of *long* and *short* range dynamics

Model



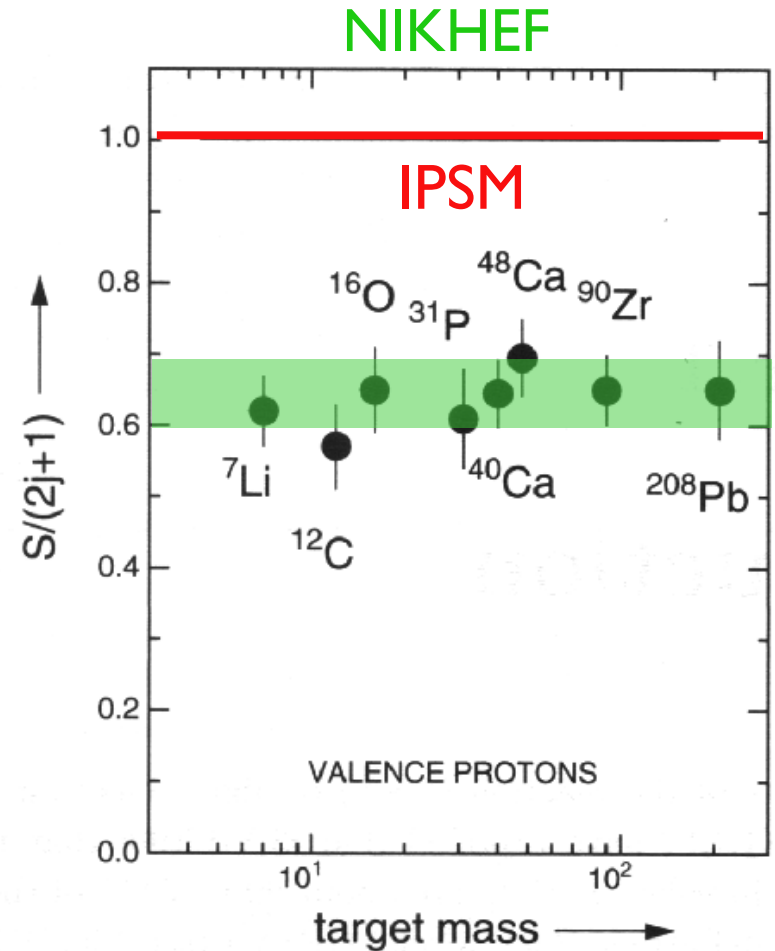
Perturbation Theory\*



\* Should converge to exact solution

# Long-range dynamics

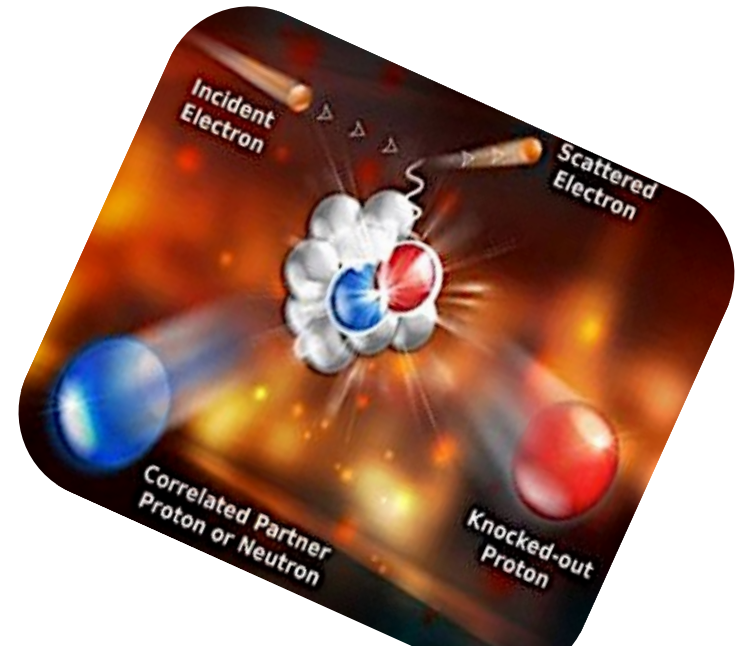
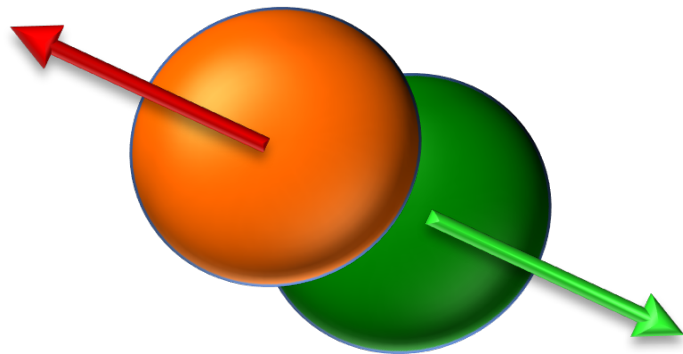
- Described overall well by mean-field models.
- Non negligible pairing effects at long and short distances (/ low and high energy).
- Today's focus is on high-energy, short-range, pairing



# What Are SRC?

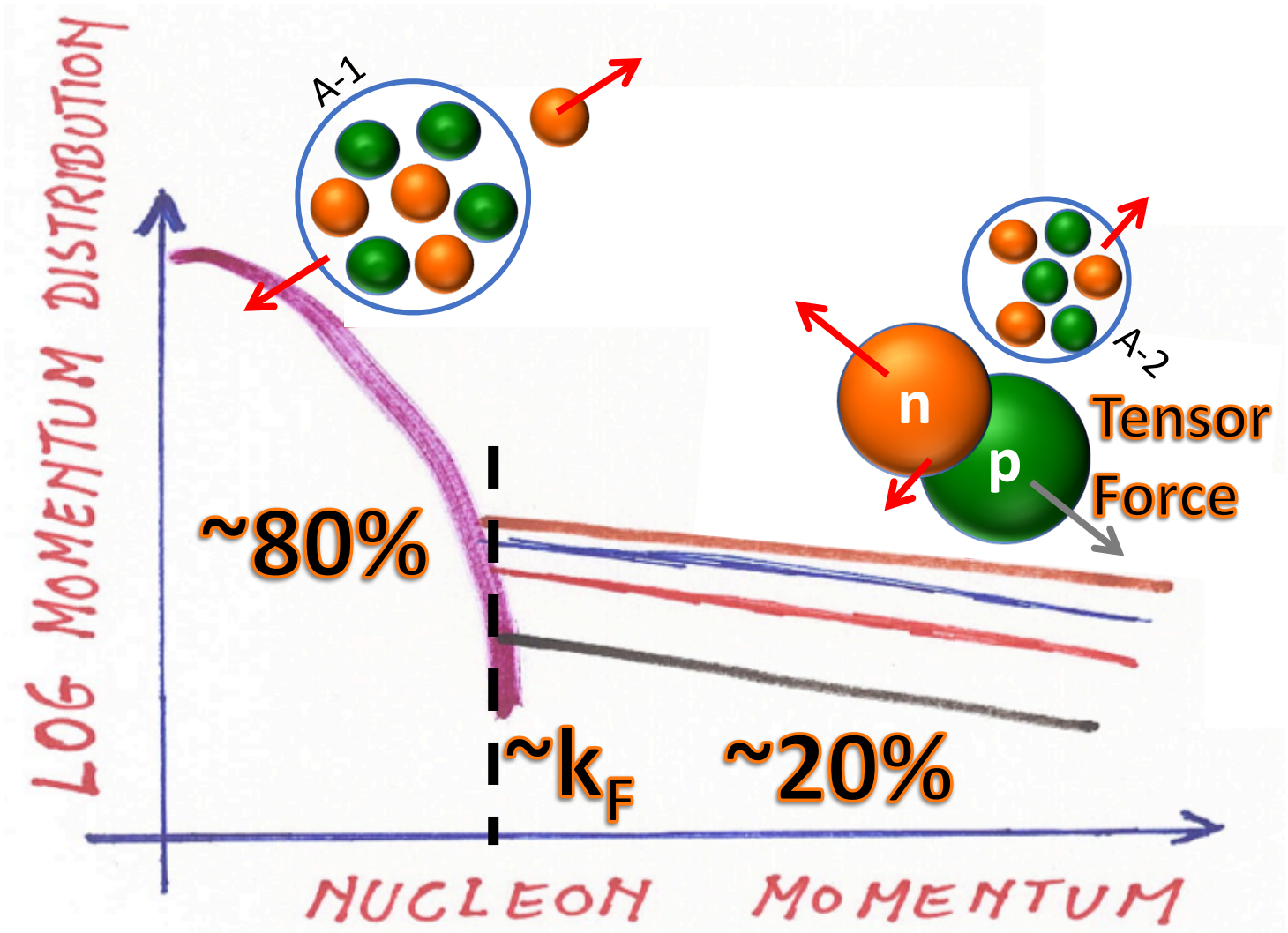
SRC are pairs of nucleon that are close together in the nucleus (wave functions overlap)

=> Momentum space: pairs with high relative momentum and low c.m. momentum compared to the Fermi momentum ( $k_F$ )



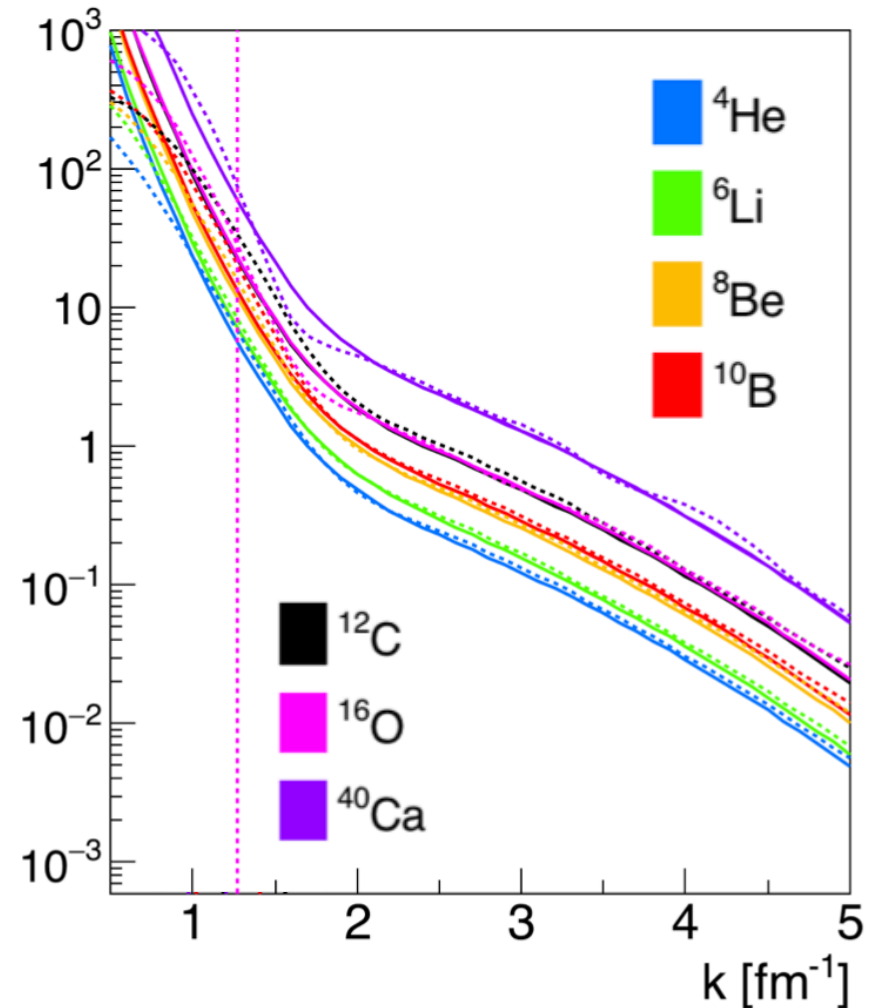


# What do we know about SRC



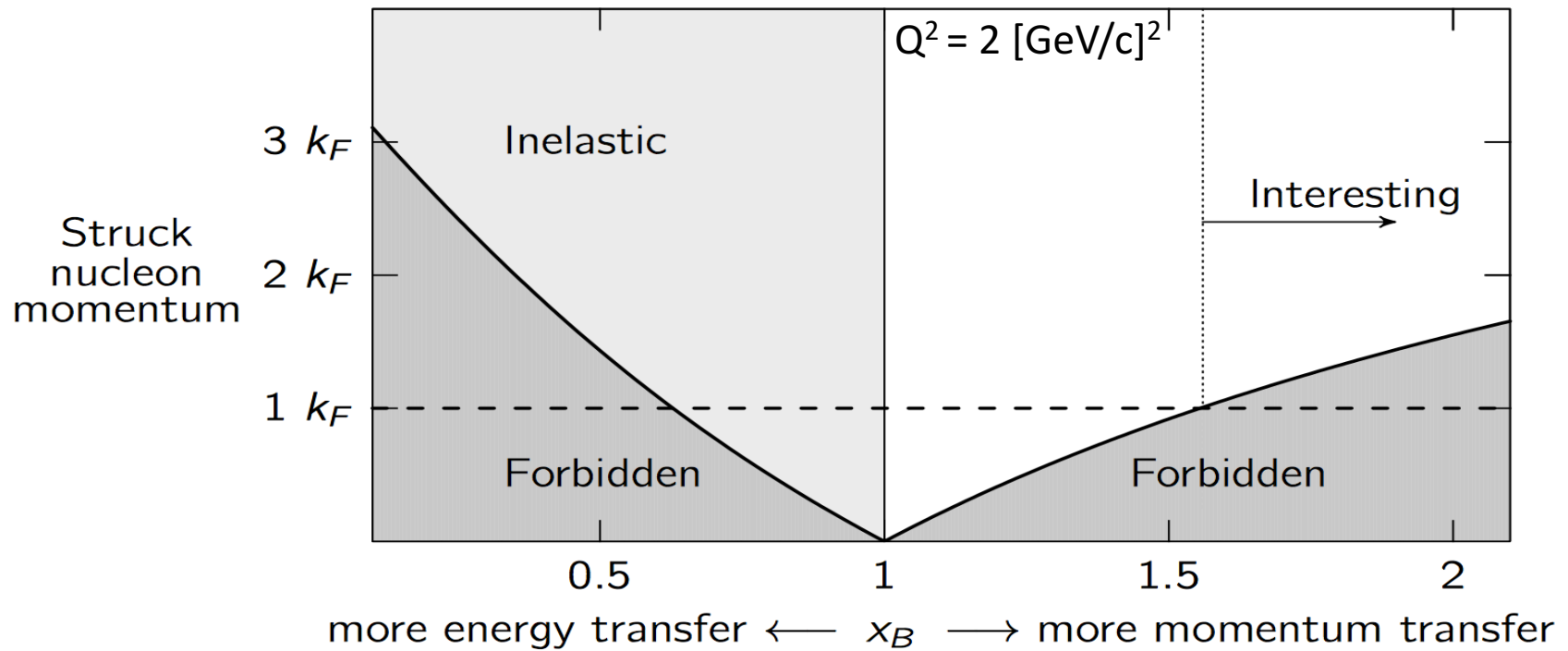
# High-Momentum Tails

- Short-range two-body forces create high-momentum tails to the nuclear momentum distribution
- Expected to be due to pairs of short-range correlated nucleons.
- Ongoing experimental program to ‘dissect’ these high-momentum tails.



# Probing High-Momentum Tails

(e,e') cross section at different kinematics are sensitive to different 'parts' of the nuclear momentum distribution.

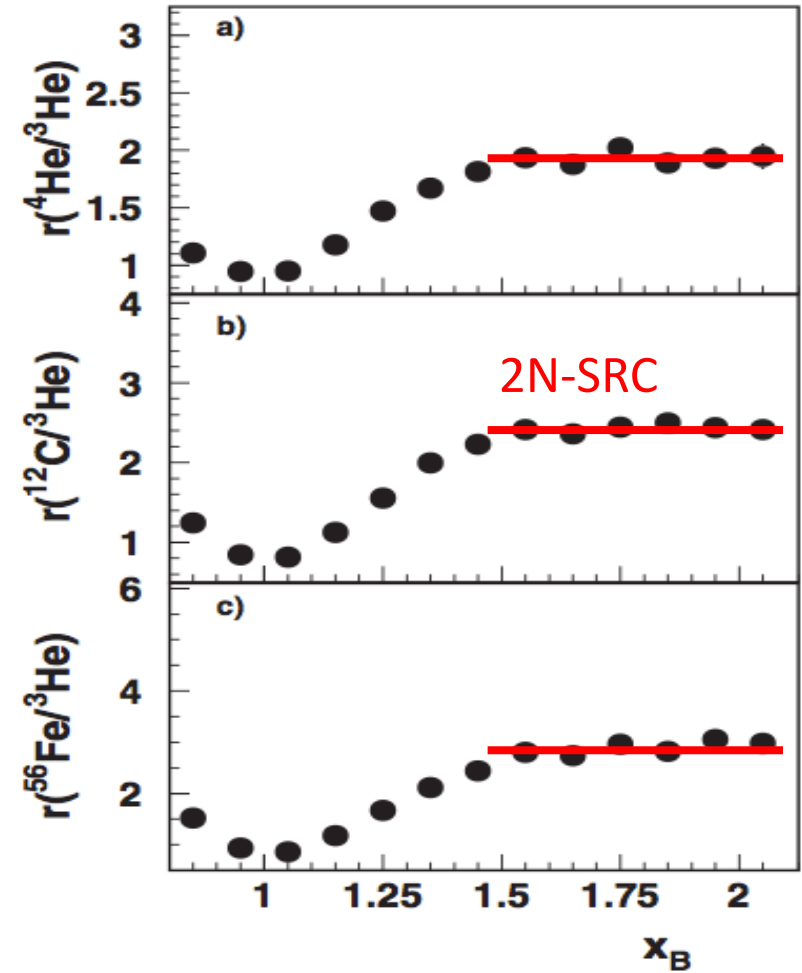


$$(q + p_A - p_{A-1})^2 = p_f^2 = m_N^2$$

# Probing High-Momentum Tails

- $A/d$  (e,e') cross section ratios sensitive to  $n_A(k)/n_d(k)$
- Observed scaling for  $x_B \geq 1.5$ .

$$\Rightarrow n_A(k > k_F) = a_2(A) \times n_d(k)$$



K. Egiyan et al., PRL **96**, 082501(2006).

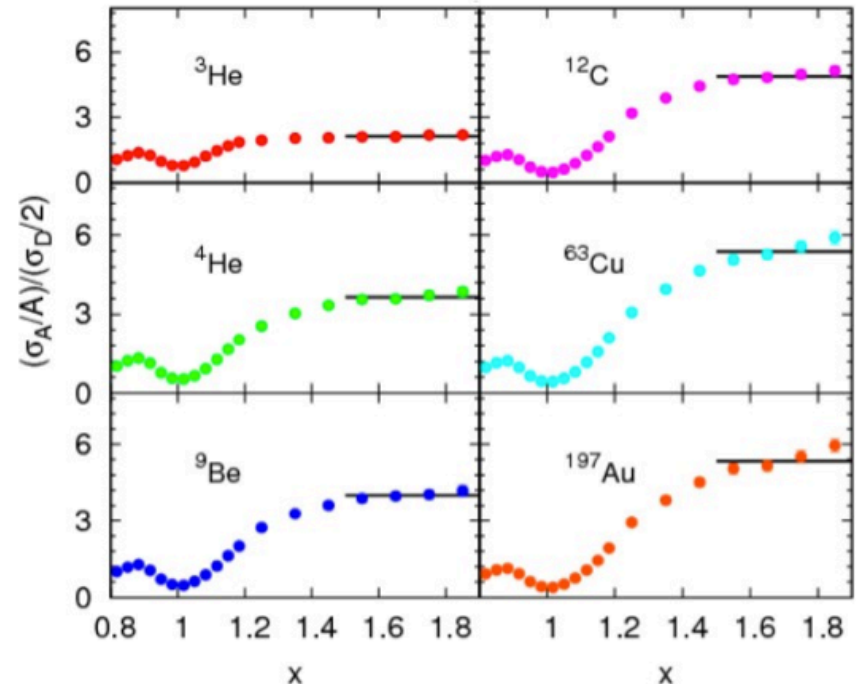
L. Frankfurt et al., Phys. Rev. C **48**, 2451 (1993).

K. Egiyan et al., Phys. Rev. C **68**, 014313 (2003). N. Fomin et al., Phys. Rev. Lett. **108**, 092502 (2012).

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N. Fomin et al., PRL **108**, 092502 (2012)

A	$a_2(A/D)$	A	$a_2(A/D)$
$^3\text{He}$	$2.1 \pm 0.1$	$^{12}\text{C}$	$4.7 \pm 0.2$
$^4\text{He}$	$3.6 \pm 0.1$	$^{63}\text{Cu}$	$5.2 \pm 0.2$
$^9\text{Be}$	$3.9 \pm 0.1$	$^{197}\text{Au}$	$5.1 \pm 0.2$

O. Hen et al., PRC **85**, 047301 (2012)

L. Frankfurt et al., Phys. Rev. C **48**, 2451 (1993).  
 K. Egiyan et al., Phys. Rev. C **68**, 014313 (2003).

K. Egiyan et al., PRL **96**, 082501 (2006)



# Probing High-Momentum Tails

## Nuclei have a high-momentum tail!

$A/d$  (e,e') cross section ratio sensitive to

$n_A(k)/n_d(k)$

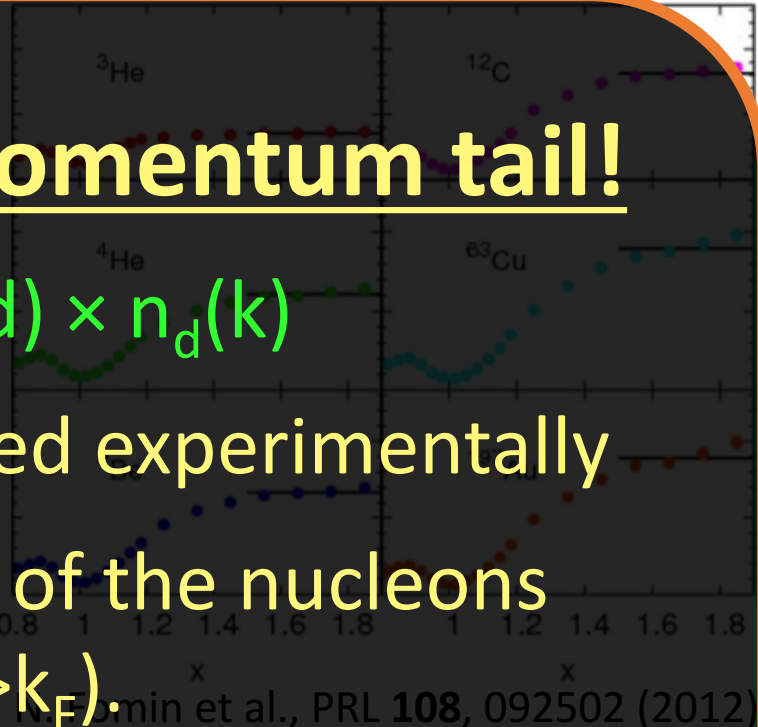
1. It scales:  $n_A(k > k_F) = a_2(A/d) \times n_d(k)$

2. Scale factor,  $a_2$ , determined experimentally

Observed scaling

3. In  $A \geq 12$  nuclei, 20 – 25% of the nucleons have high-momentum ( $k > k_F$ ).

$$\Rightarrow n_A(k > k_F) = a_2(A) \times n_d(k)$$



A	$a_2(A/D)$	A	$a_2(A/D)$
$^3\text{He}$	$2.1 \pm 0.1$	$^{12}\text{C}$	$4.7 \pm 0.2$
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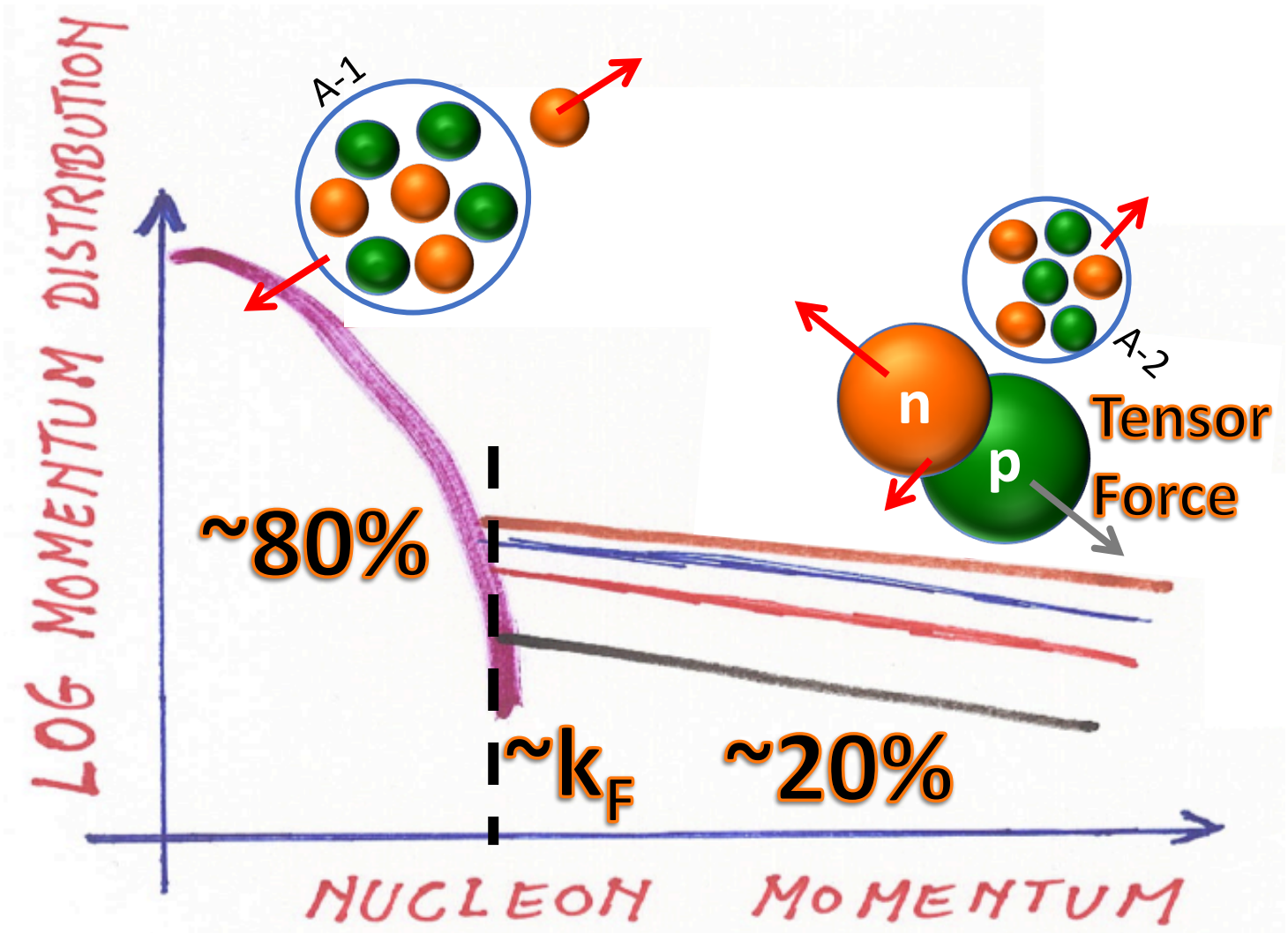
O. Hen et al., PRC **85**, 047301 (2012)

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# What do we know about SRC

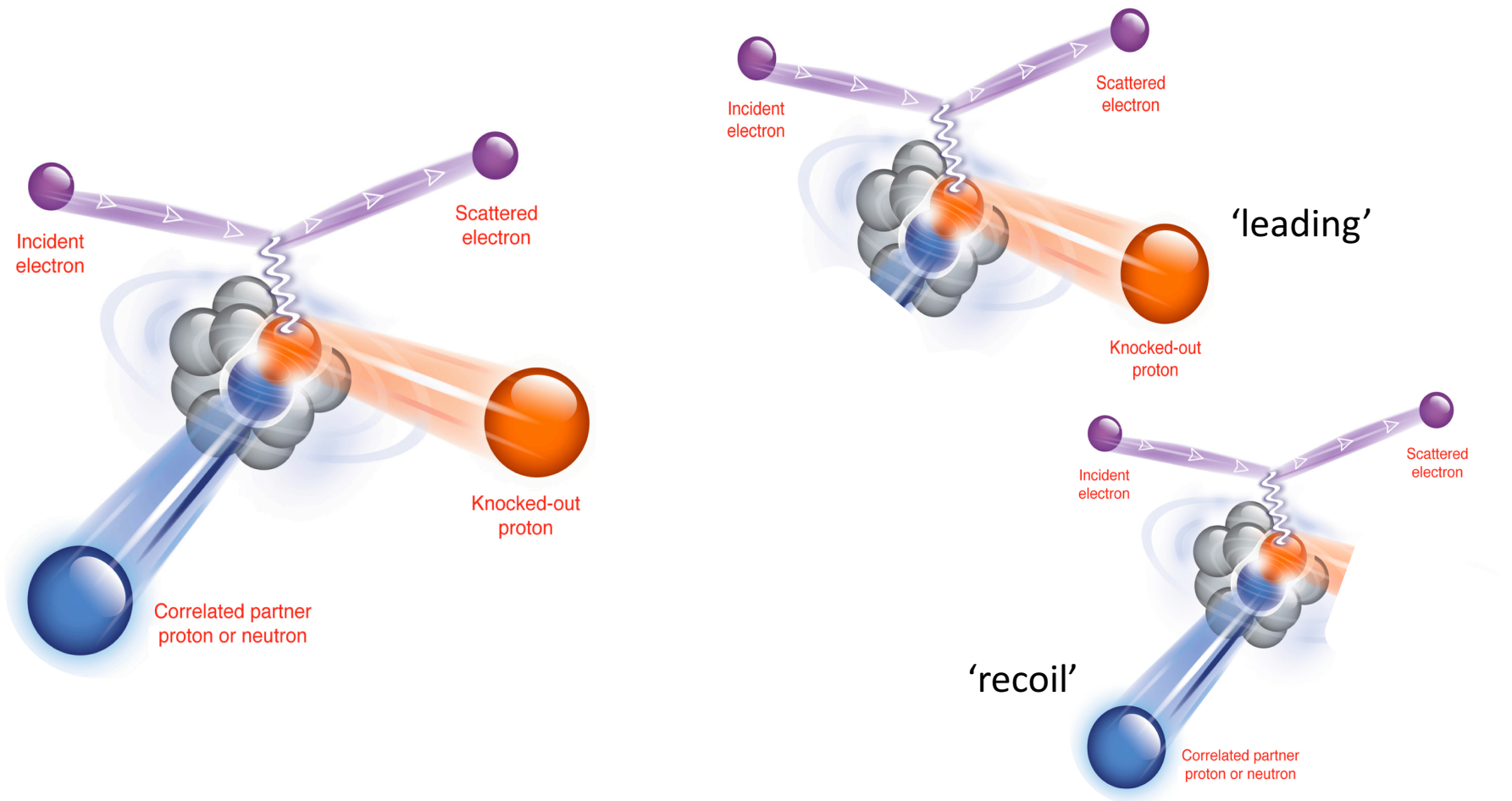


# Exclusive probes for SRC structure

Breakup the pair =>

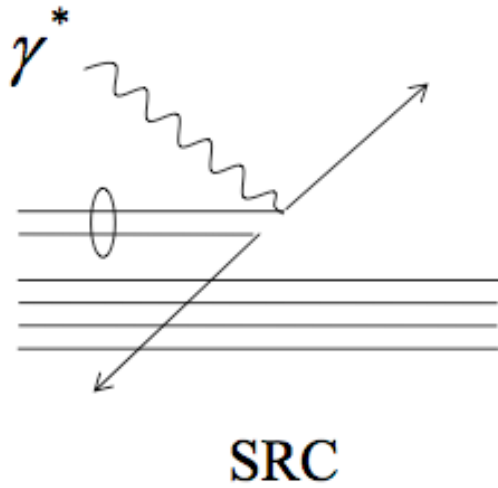
Detect both nucleons =>

Reconstruct 'initial' state

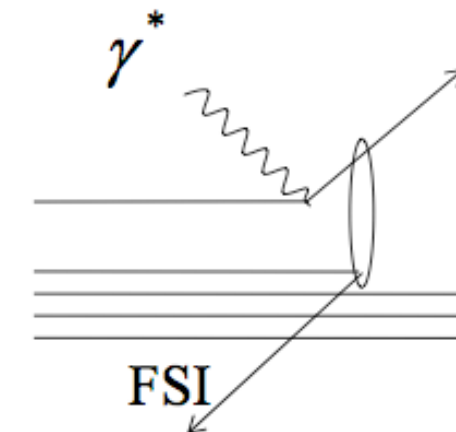
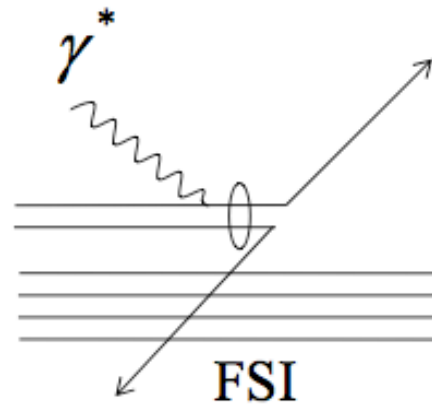
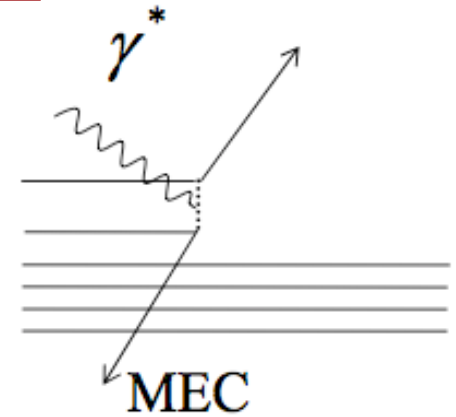
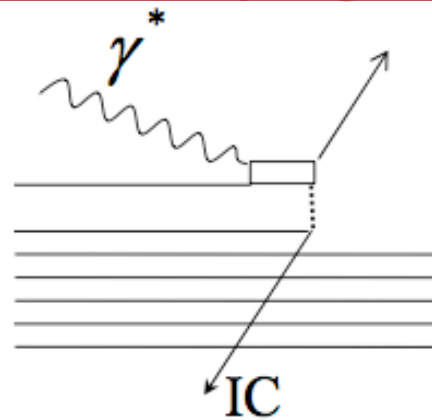


# Interlude: Reaction Mechanisms

## What we want:



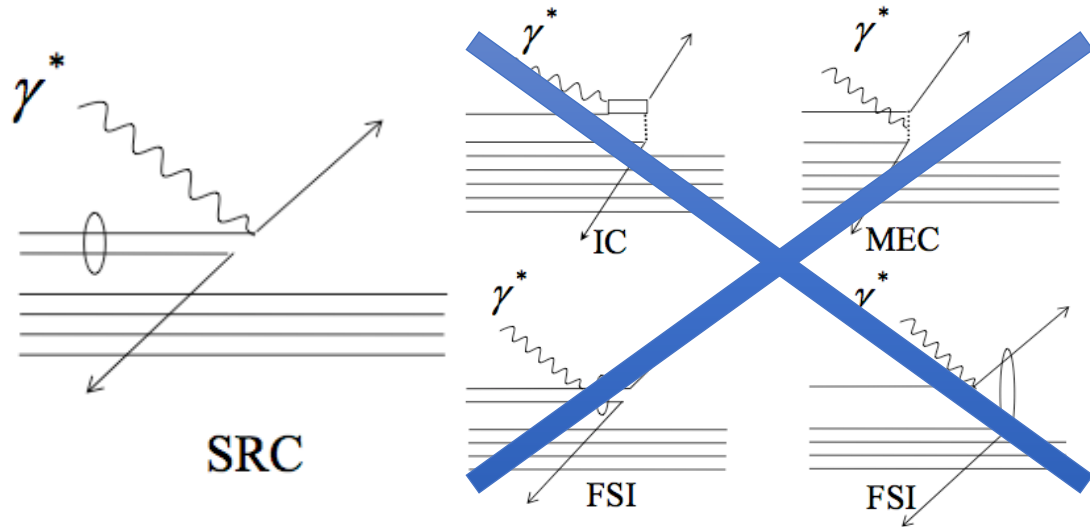
## What we (might) get:



# Interlude: Reaction Mechanisms

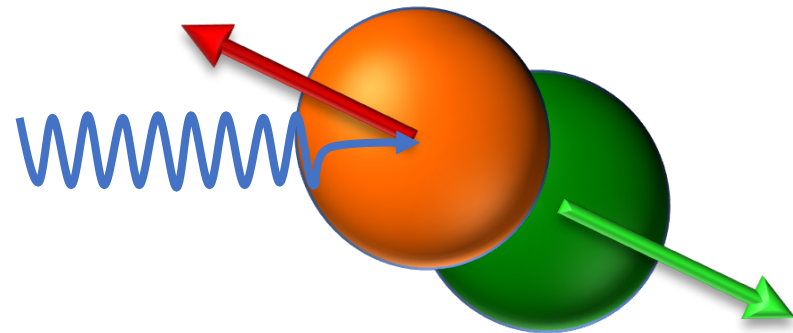
## Trick: choose 'good' kinematics!

- $x_B > 1.2$
- $Q^2 \sim 2$  (GeV/c<sup>2</sup>)
- **Anti-Parallel Kinematics**



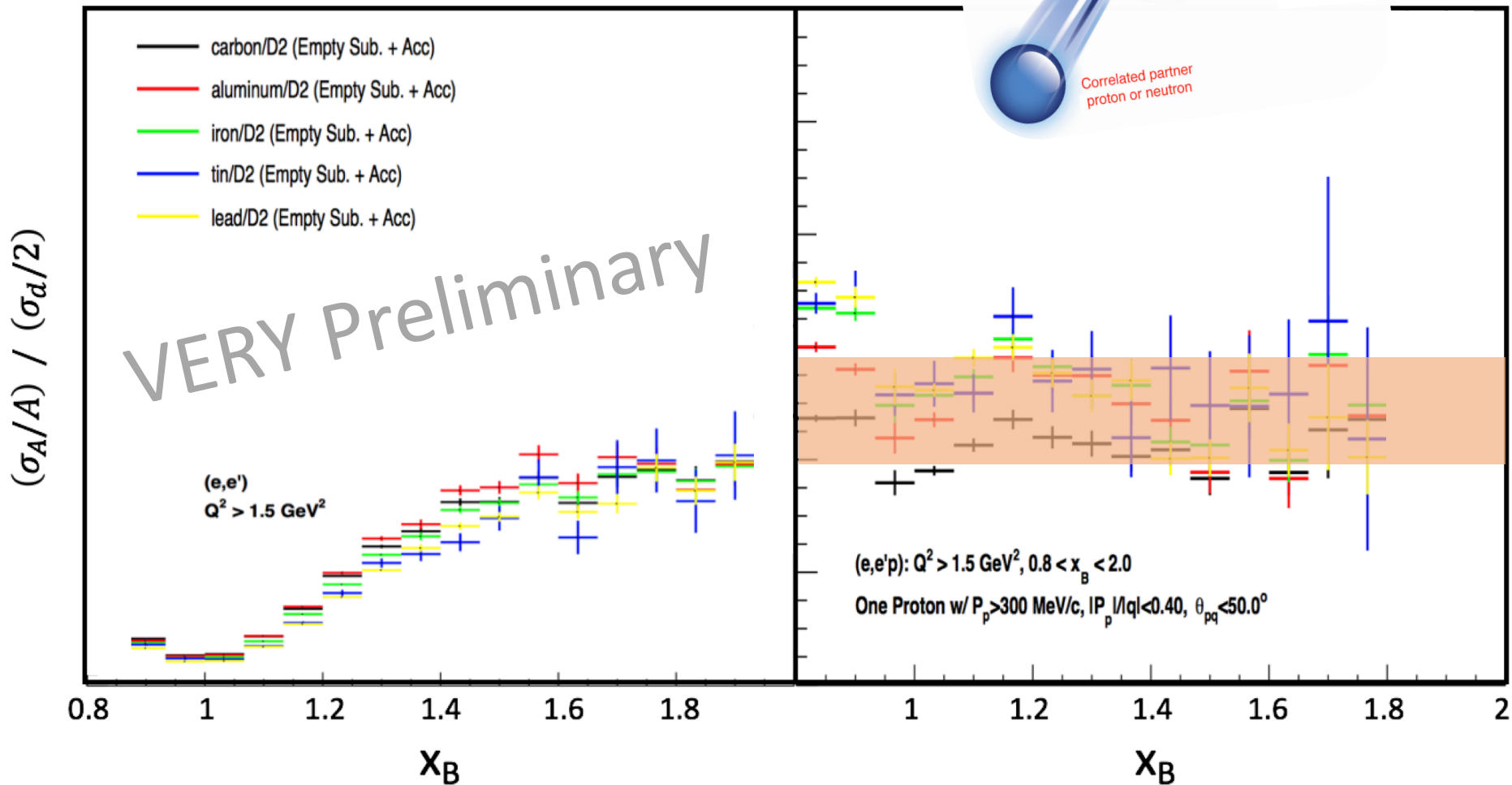
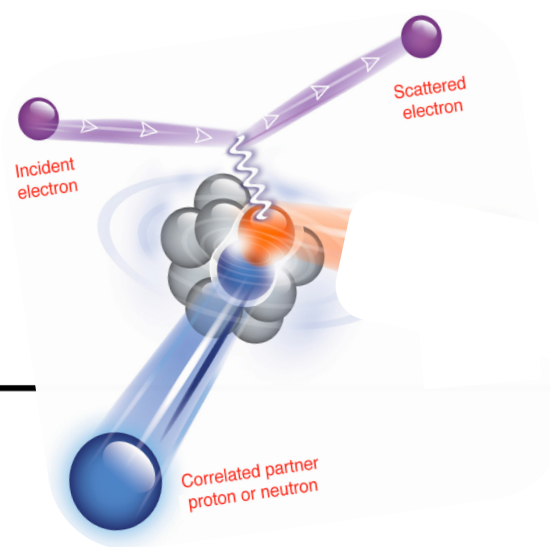
## A word on FSI:

- Large- $Q^2$  (or  $|t,u|$ ) allows using Eikonal approximation for FSI.
  - Combined with  $x_B > 1$  ensures FSI largely confined to between the nucleons of the pair.
- => Large cancellation in ratios.

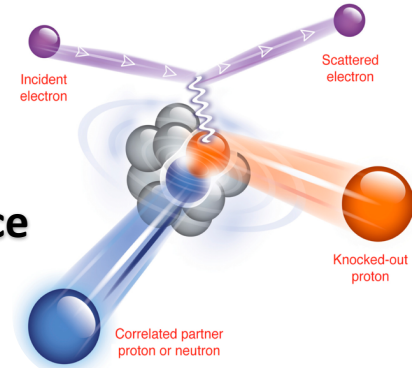




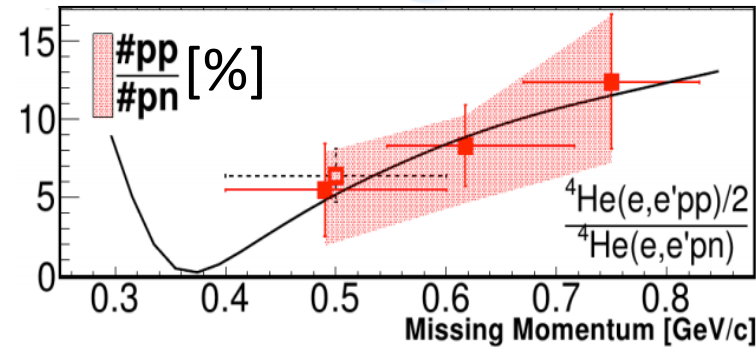
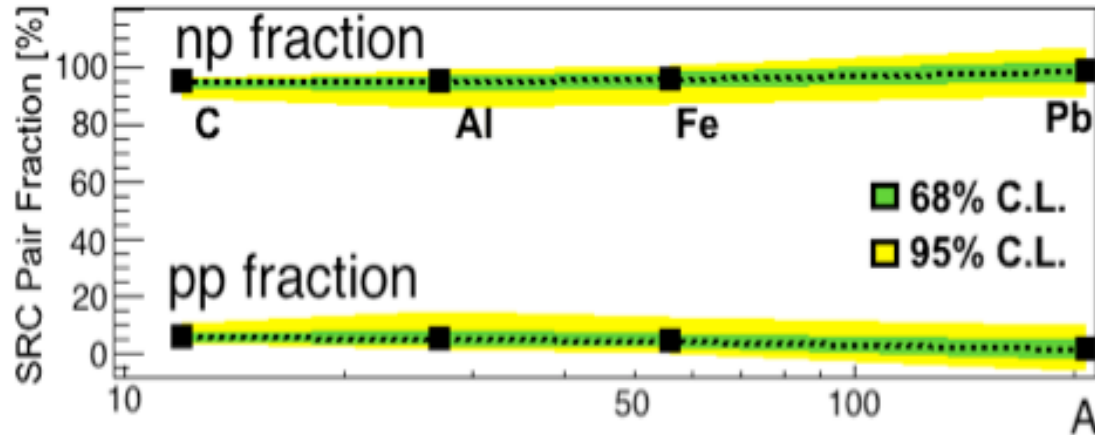
# SRC Spectator Tagging



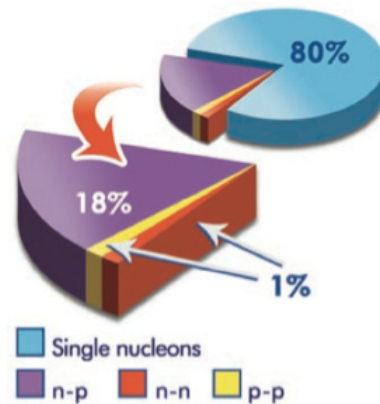
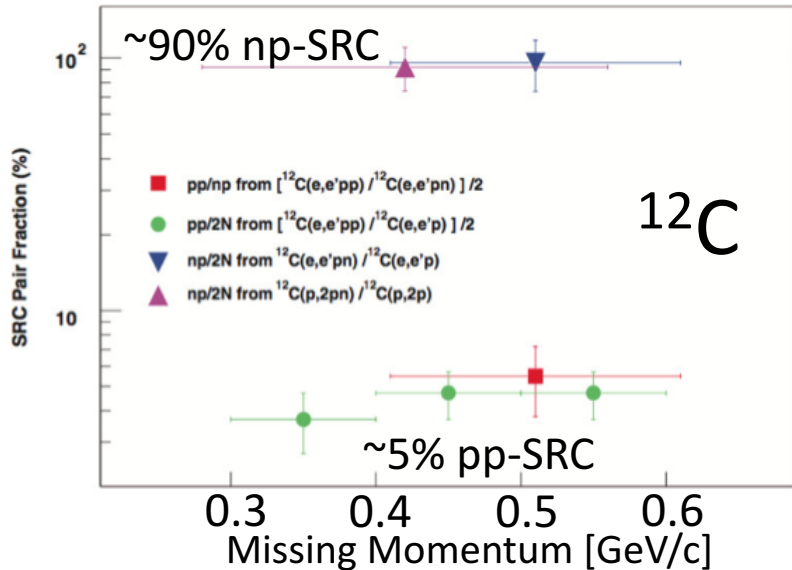
# np dominance results



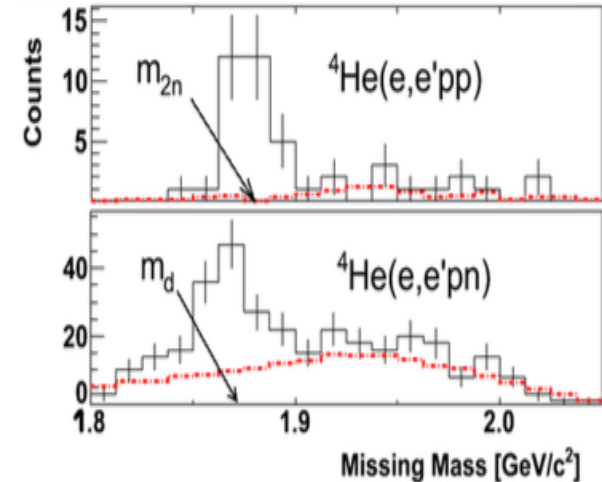
O. Hen et al., Science 364 (2014) 614



R. Subedi et al., Science 320 (2008) 1476



I. Korover et al., PRL 113 (2014) 022501

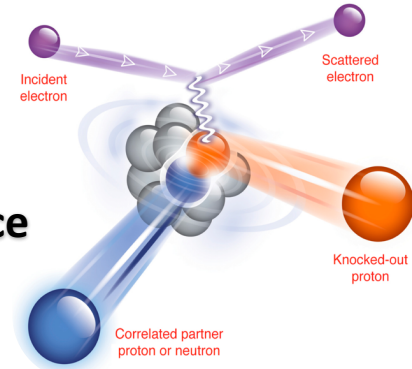


A. Tang et al., PRL (2003);

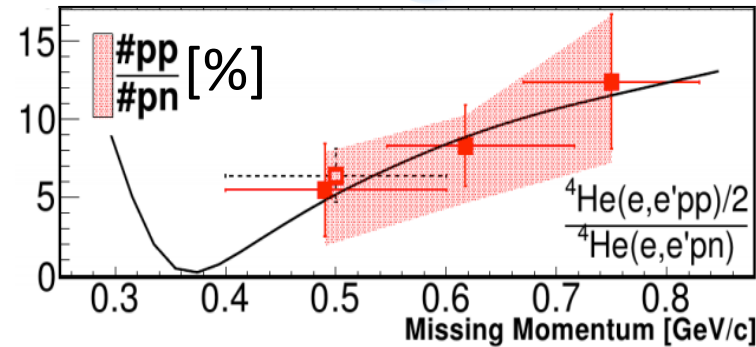
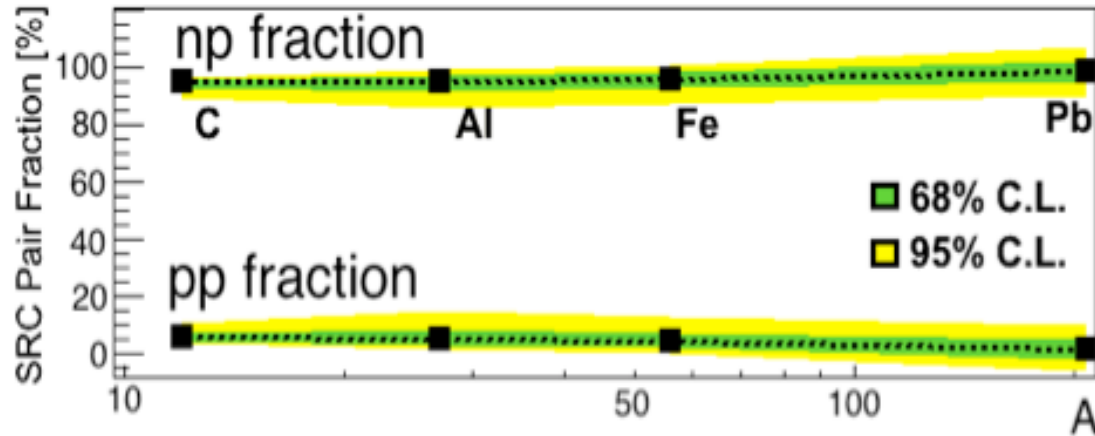
E. Piasezky et al., PRL (2006);

R. Shneor et al., PRL (2007)

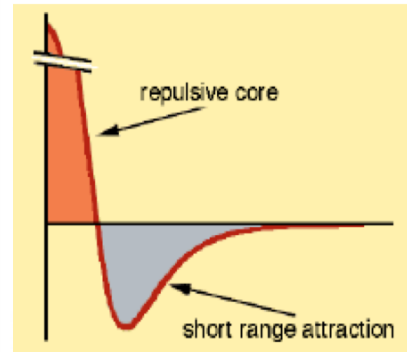
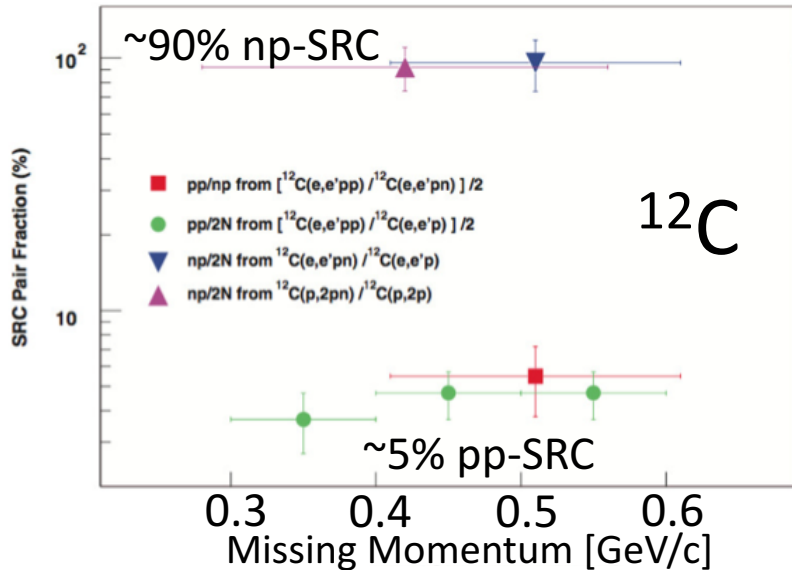
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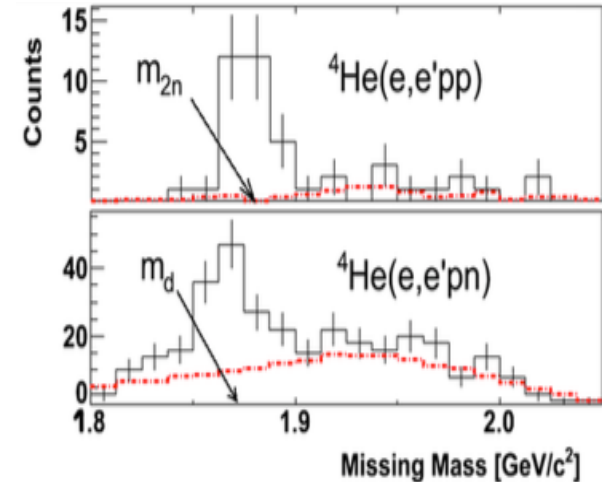
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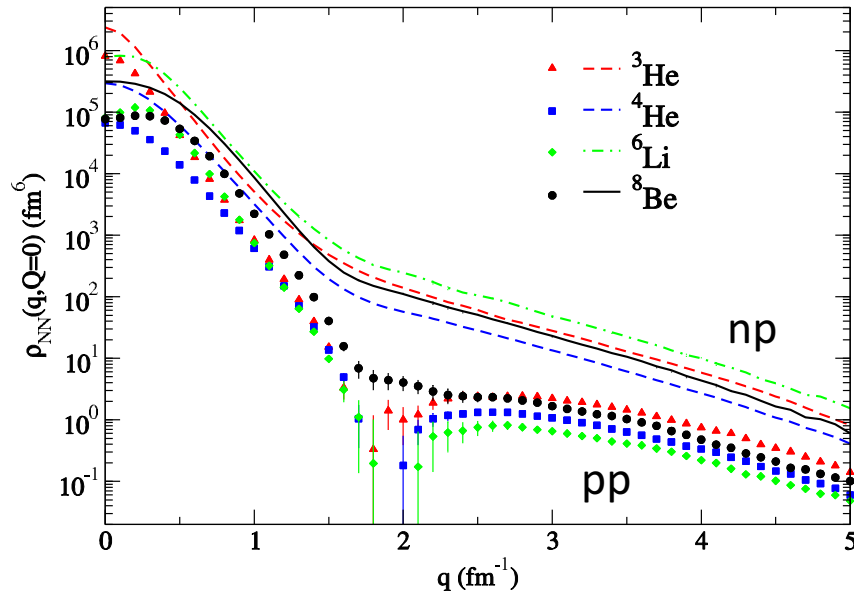
A. Tang et al., PRL (2003);

E. Piasezky et al., PRL (2006);

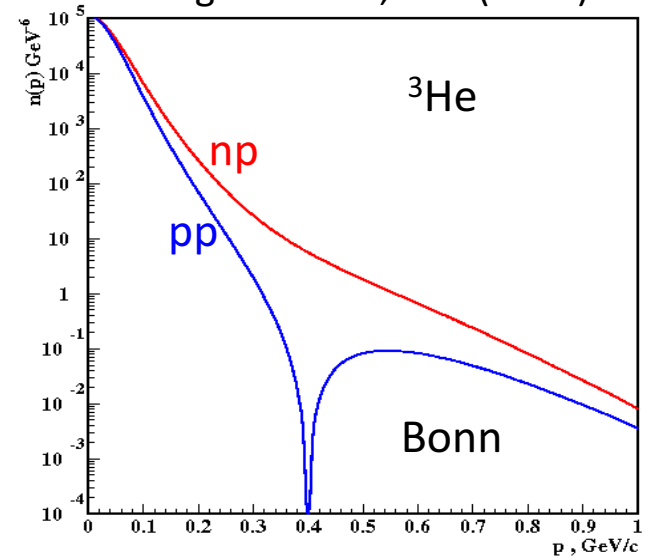
R. Shneor et al., PRL (2007)

# Tensor Force Dominance

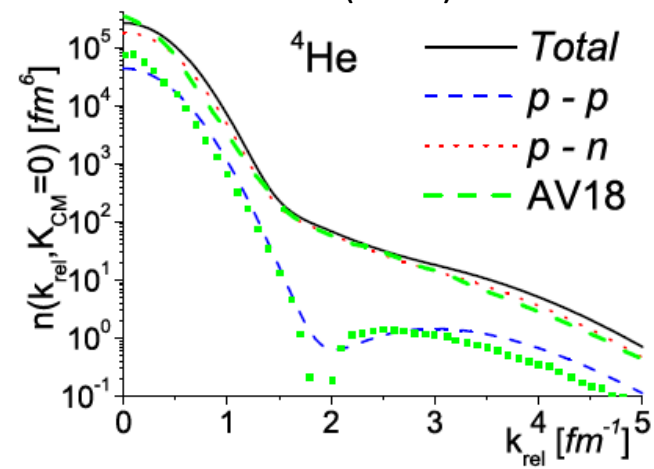
Schiavilla et al., PRL (2007)



Sargsian et al., PRC (2005)

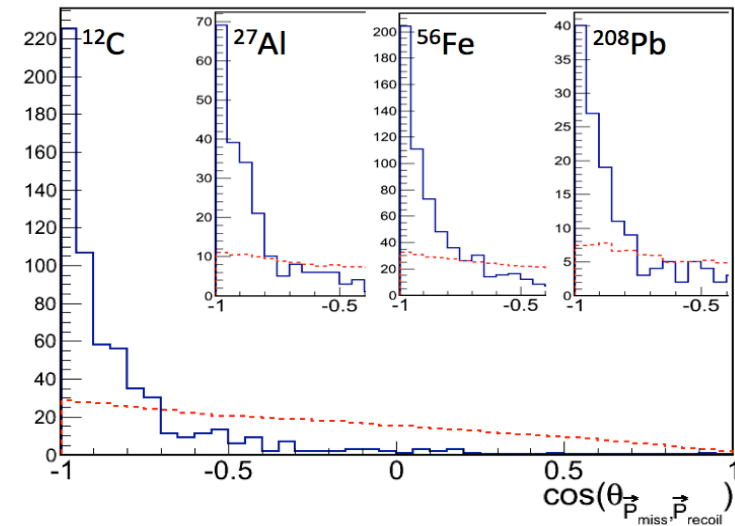
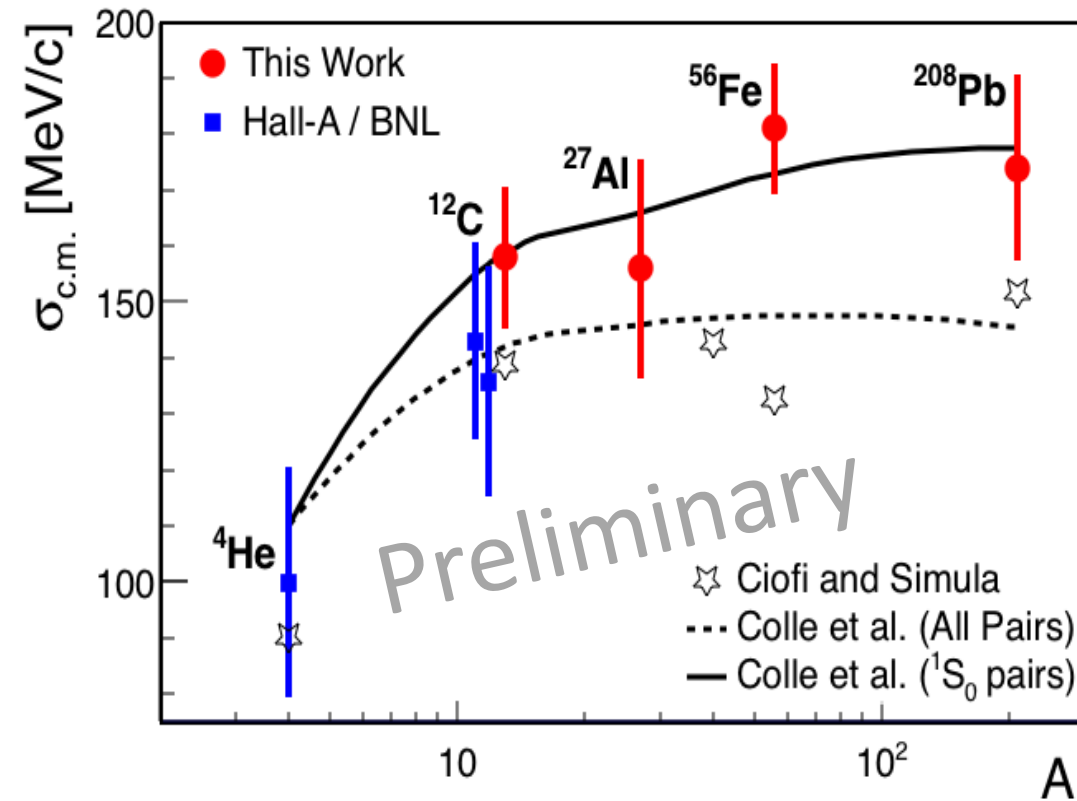


Ciofi and Alvioli PRL (2008)



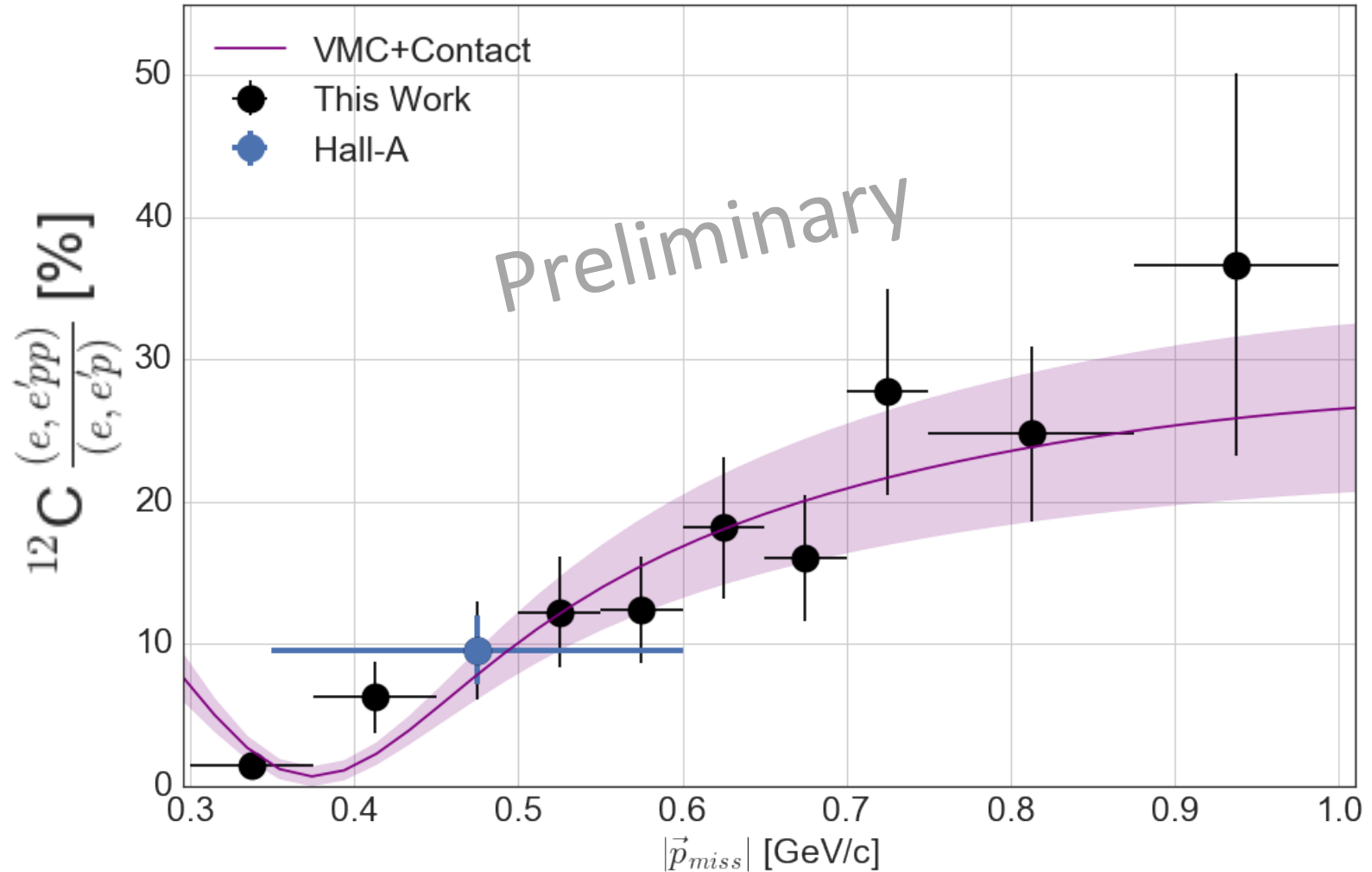
# C.M. Motion and Pairing Mechanisms

“... *high relative momentum* and *low c.m. momentum* compared to the Fermi momentum ( $k_F$ )”

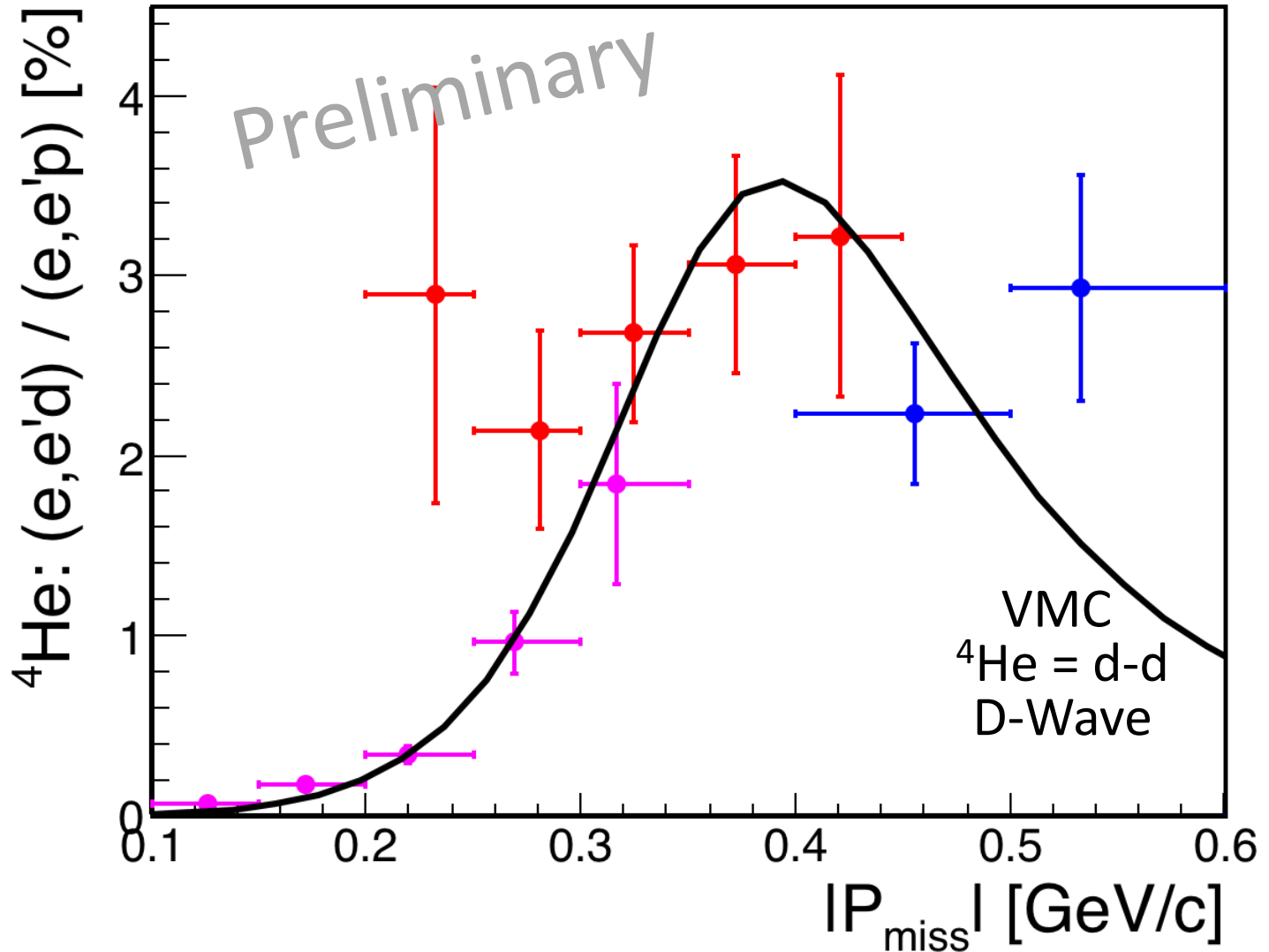




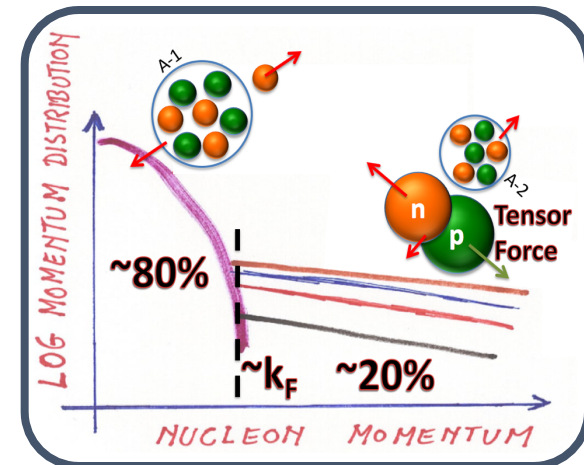
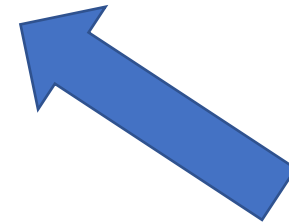
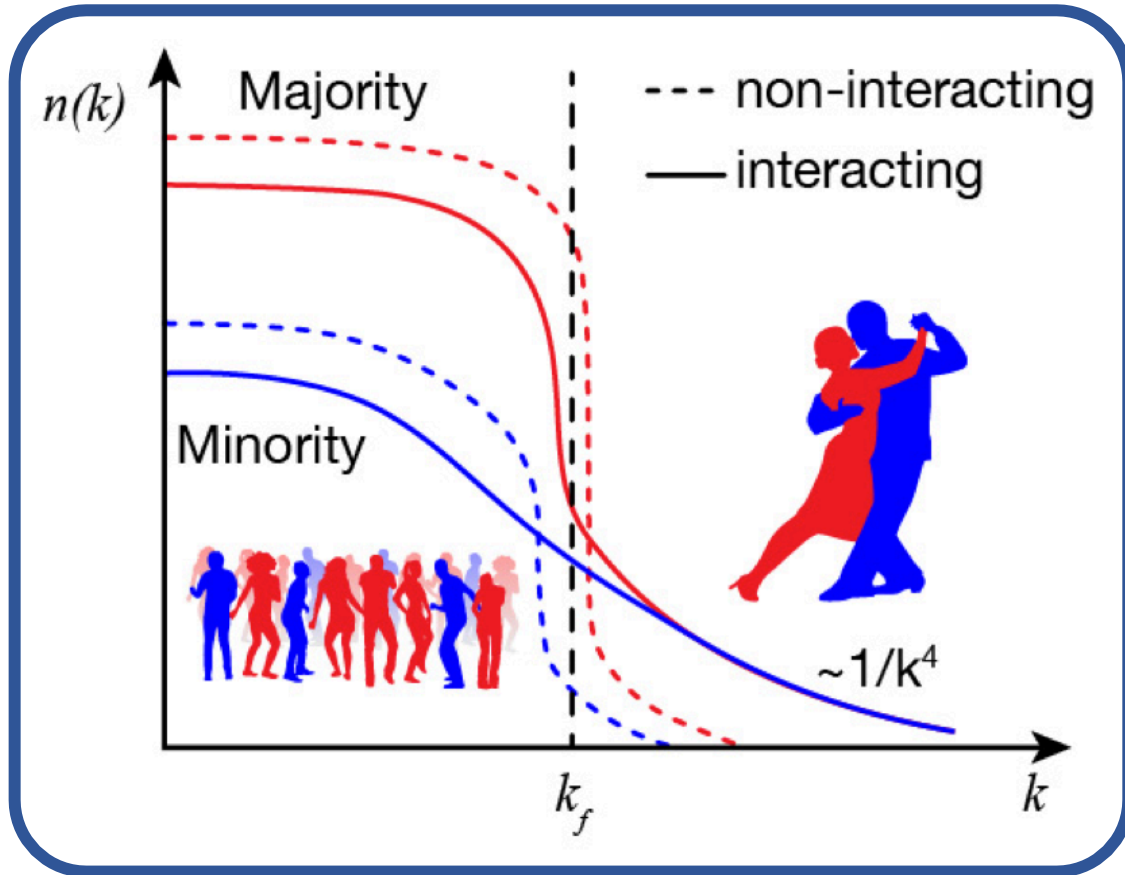
# NN interaction at Short Distances



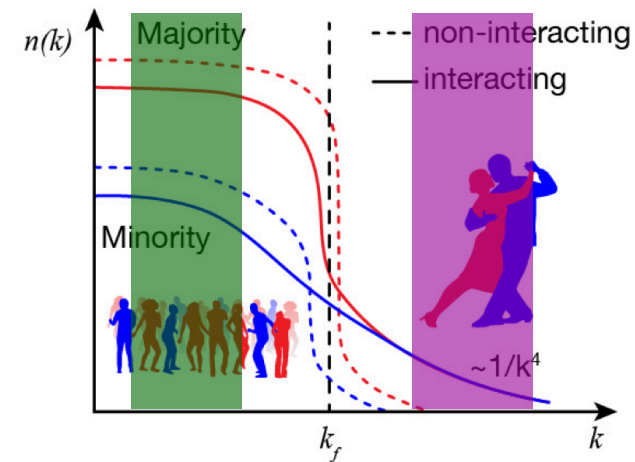
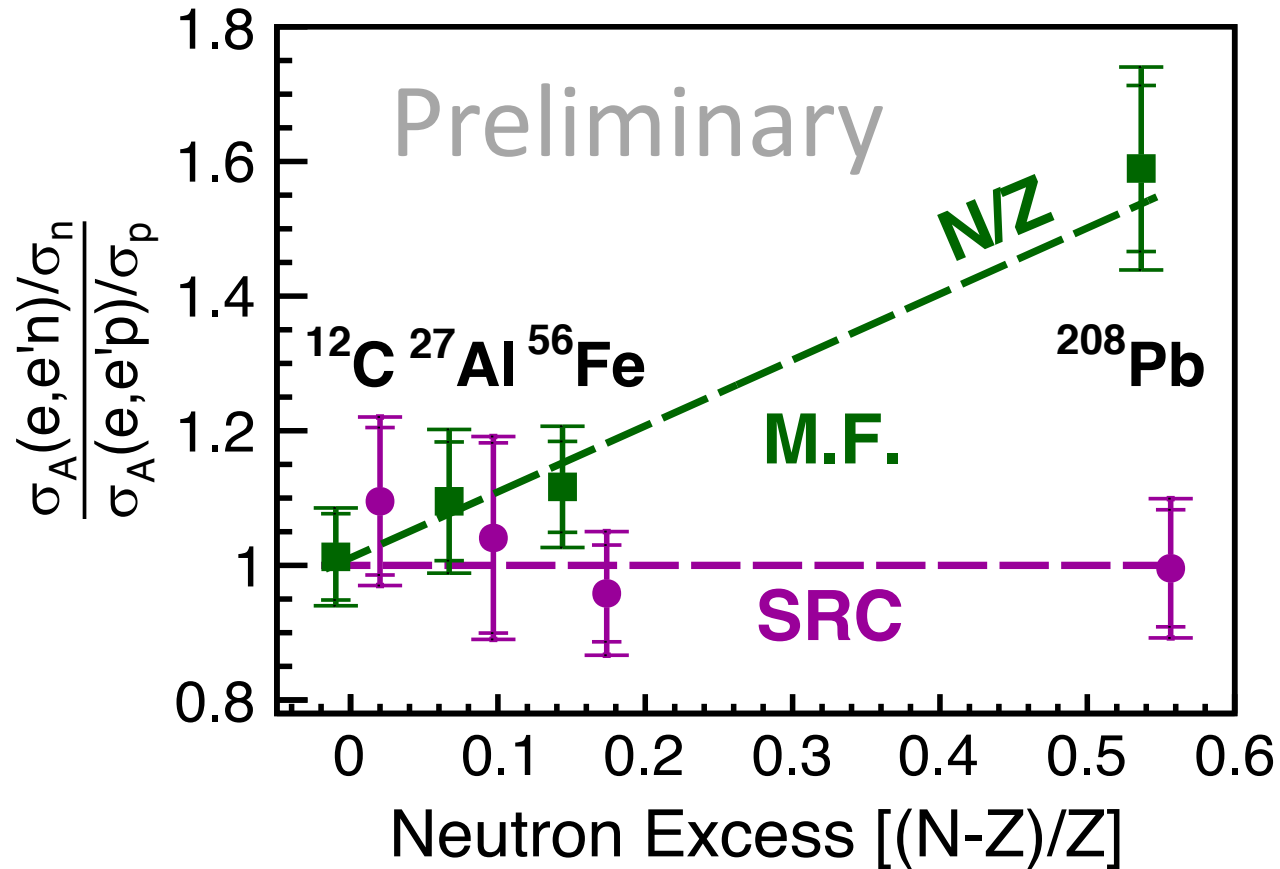
# Short-Range Clustering



# Nuclear Asymmetry Dependence

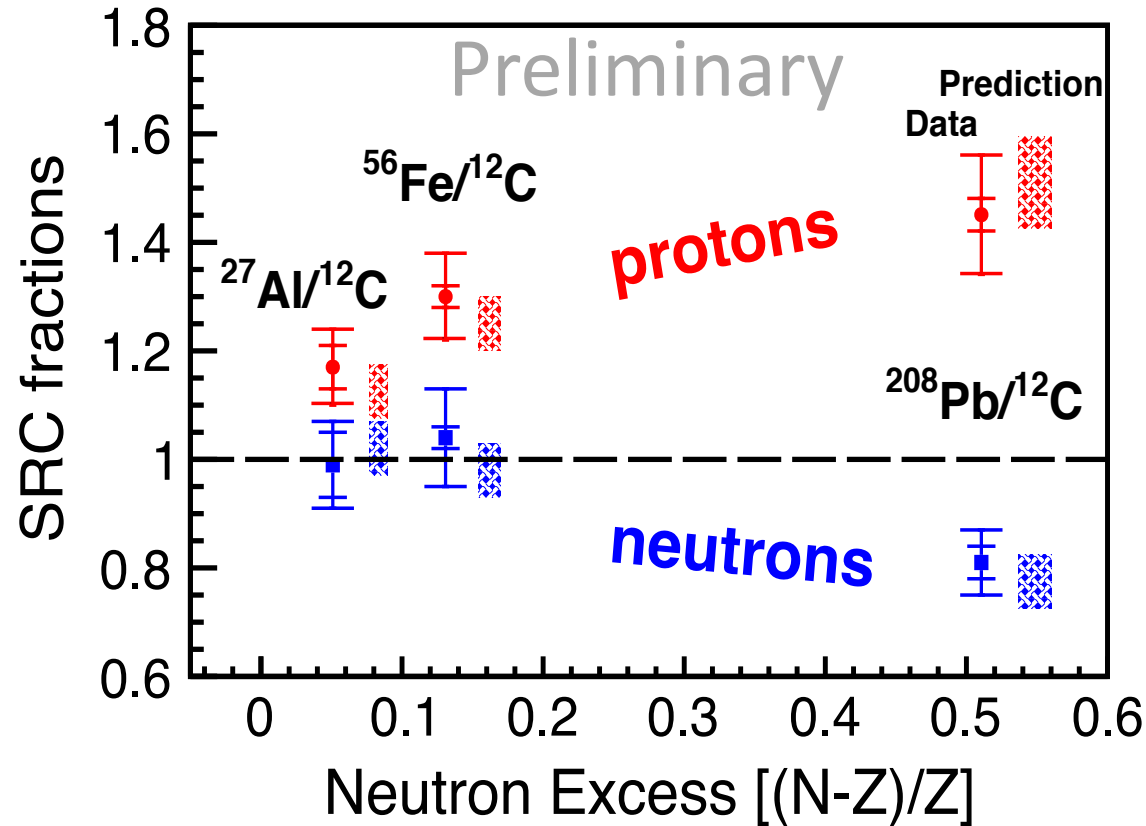


# Nuclear Asymmetry Dependence



$\Rightarrow$  Same number of high- $P$  protons and neutrons!

# Nuclear Asymmetry Dependence



=> Protons more correlated in neutrons rich nuclei!

# New Era in SRC Research!

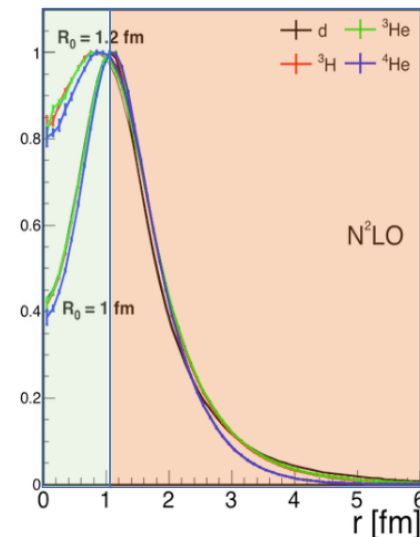
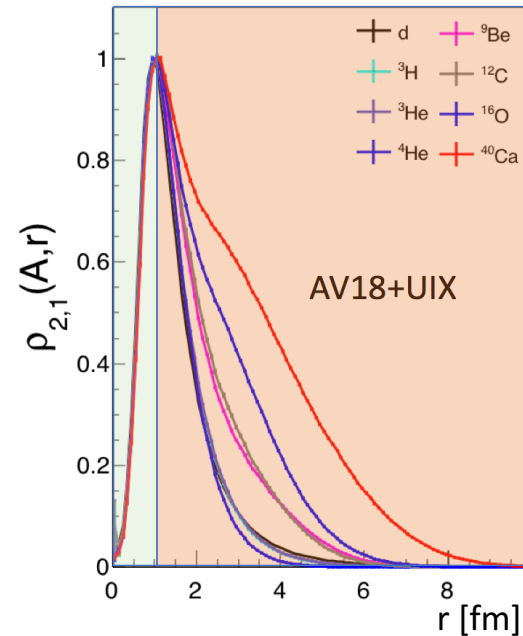
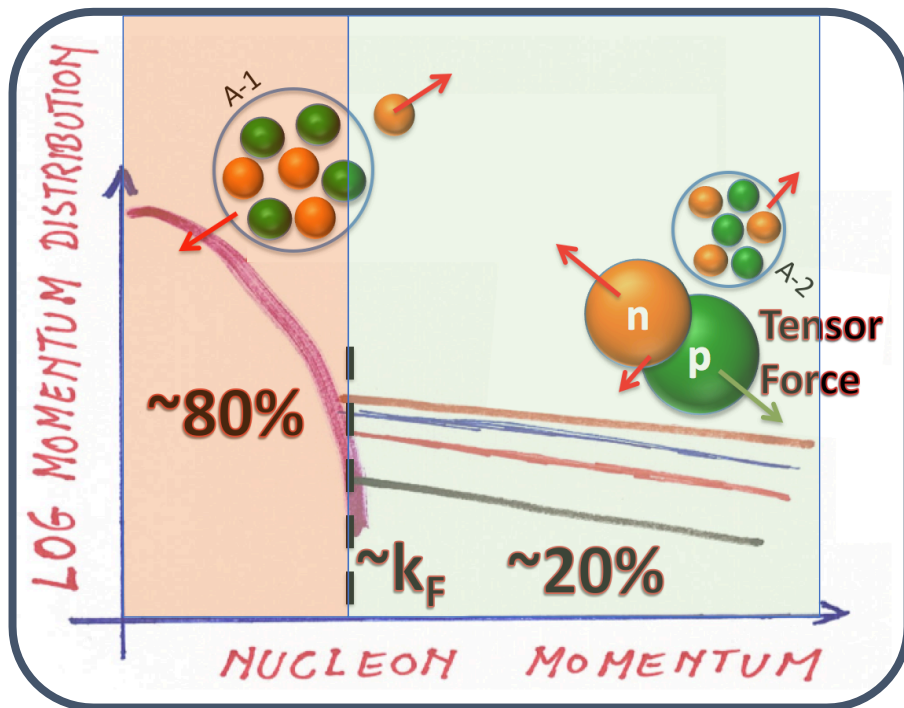
Consistent set of  $(e,e')$ ,  $(e,e'p)$ ,  $(e,e'pN)$  and  $(p,2pn)$  measurements allow quantifying SRCs with unprecedented accuracy!

1. SRC Exist in Nuclei (!) and account for:
  - $\sim 20\%$  of the nucleons in nuclei.
  - $\sim 100\%$  of the high- $p$  ( $k > k_F$ ) nucleons in nuclei.
2. Have large relative momentum and low c.m. momentum.
3. Predominantly due to np-SRC.
4. Universal for  $A = 4 - 208$  nuclei.
5. np-SRC create a larger fraction of high-momentum protons in neutron rich nuclei!
6. Tensor force dominance at short distance.

# Theory Connection: Momentum Densities

Can we formulate a universal description of SRC (both coordinate and momentum space) without relying on many-body calculations? (YES)

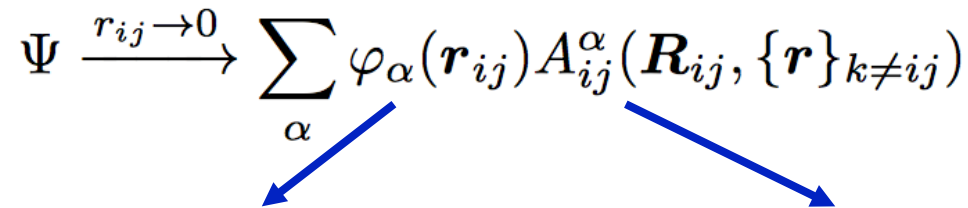
Can we use it to confront theory and experiments? (YES)





# Universal Nuclear Structure?

1. Use a factorized ansatz for the short-distance (high-momentum) part of the many-body wave function:

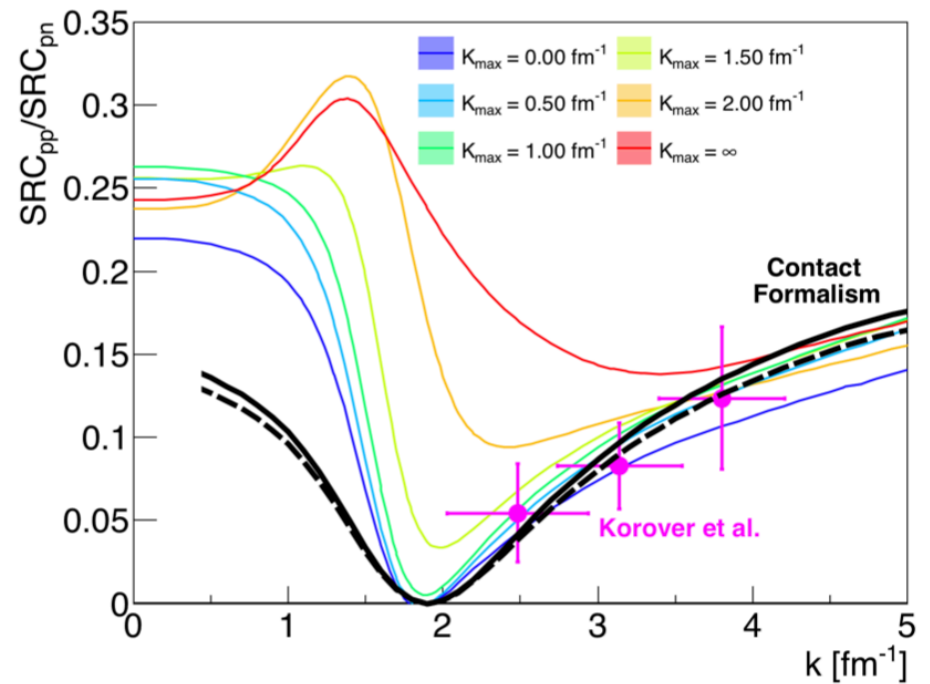
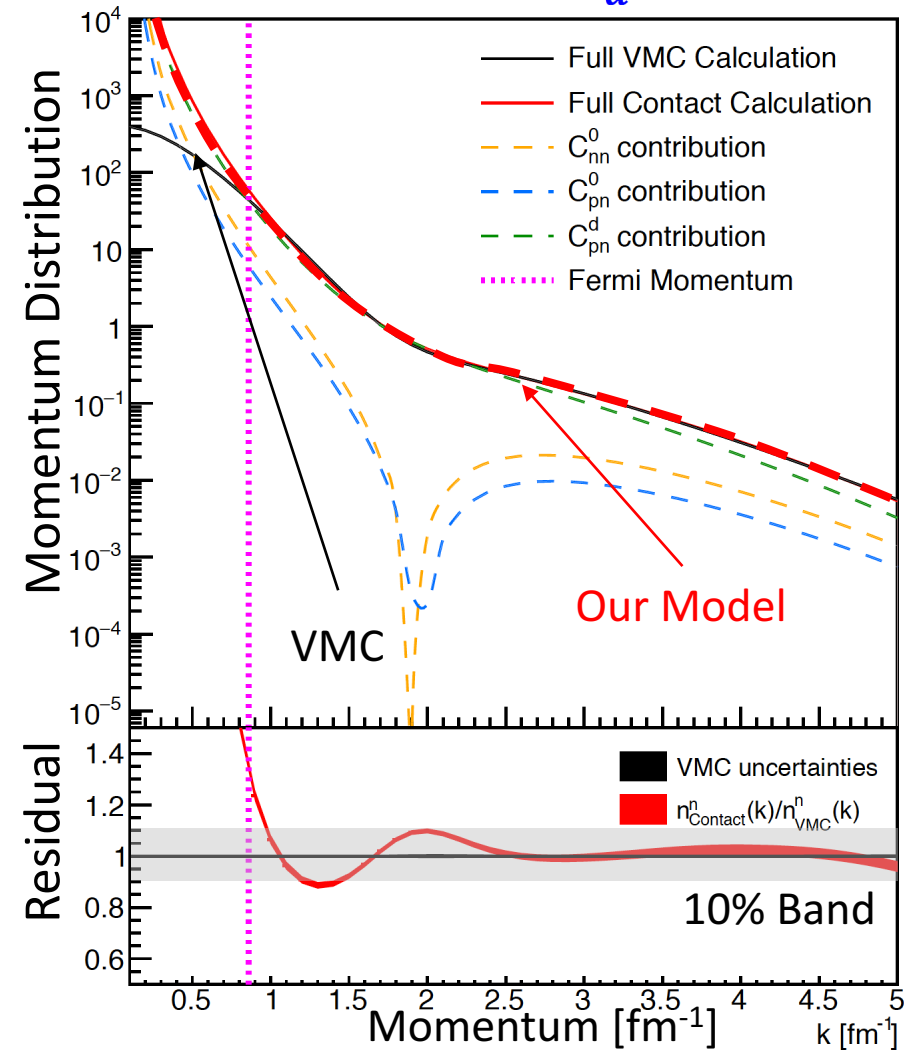
$$\Psi \xrightarrow{r_{ij} \rightarrow 0} \sum_{\alpha} \varphi_{\alpha}(\mathbf{r}_{ij}) A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}\}_{k \neq ij})$$
The equation shows the wave function  $\Psi$  in the limit of short distance  $r_{ij} \rightarrow 0$  factorizing into a sum over states  $\alpha$  of a universal function  $\varphi_{\alpha}(\mathbf{r}_{ij})$  and a nucleus-specific function  $A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}\}_{k \neq ij})$ . Two blue arrows point from the terms in the sum to their respective descriptions in the following list.

- Universal function of the NN interaction.
- Taken as the zero energy solution to the 2 body problem
- Nucleus (/ system) specific function
- Depends on all nucleons except the SRC pair (primarily mean-field)

2. Test by comparing to many-body calculations *and* data from hard knockout measurements

# Universal Nuclear Structure!

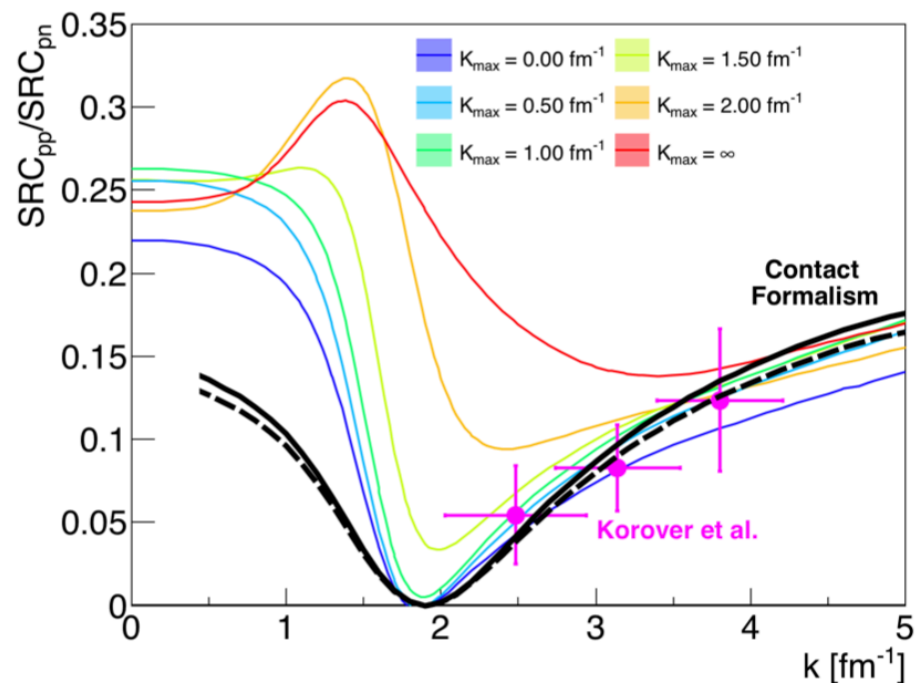
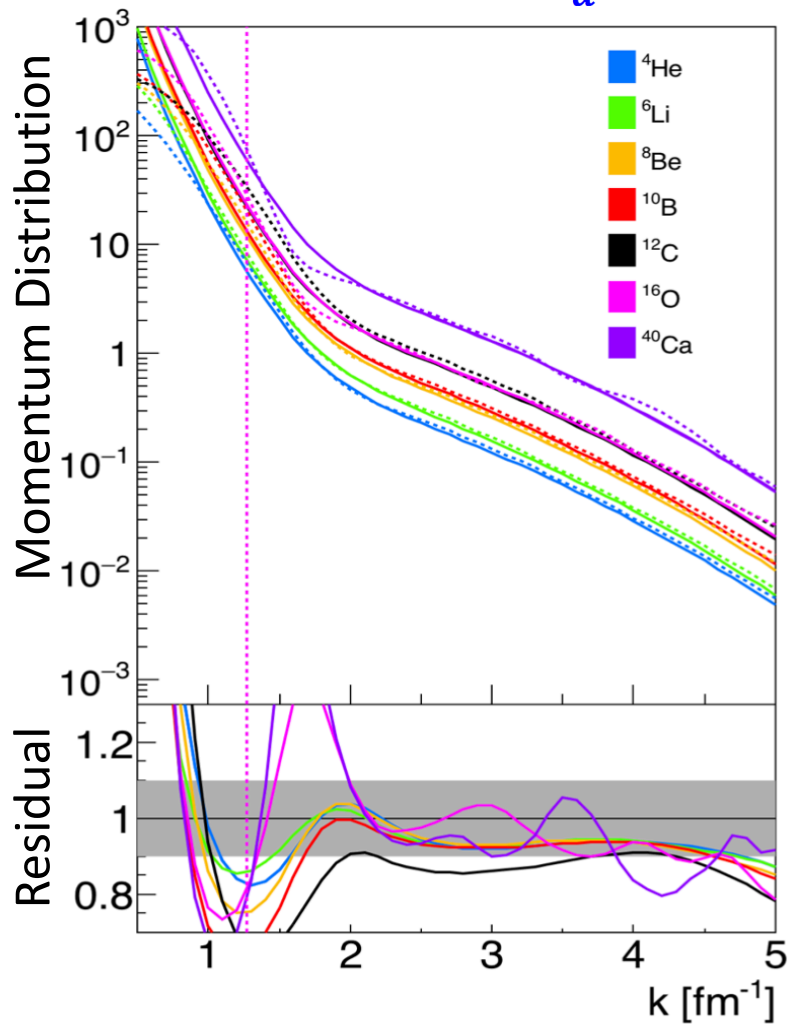
$$n_p(k) = \sum_{\alpha} |\tilde{\varphi}_{pp}^{\alpha}(k)|^2 2C_{pp}^{\alpha} + \sum_{\alpha} |\tilde{\varphi}_{pn}^{\alpha}(k)|^2 C_{pn}^{\alpha}$$



Nuclear contacts can also be extracted from experiment!

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Nuclear contacts extracted from many-body densities in k- and r-space and from experiment

A	k-space				r-space			
	$C_{pn}^{s=1}$	$C_{pn}^{s=0}$	$C_{nn}^{s=0}$	$C_{pp}^{s=0}$	$C_{pn}^{s=1}$	$C_{pn}^{s=0}$	$C_{nn}^{s=0}$	$C_{pp}^{s=0}$
${}^4\text{He}$	$12.3 \pm 0.1$	$0.69 \pm 0.03$	$0.65 \pm 0.03$		$11.61 \pm 0.03$	$0.567 \pm 0.004$		
	$14.9 \pm 0.7$ (exp)	$0.8 \pm 0.2$ (exp)						
${}^6\text{Li}$	$10.5 \pm 0.1$	$0.53 \pm 0.05$	$0.49 \pm 0.03$		$10.14 \pm 0.04$	$0.415 \pm 0.004$		
${}^7\text{Li}$	$10.6 \pm 0.1$	$0.71 \pm 0.06$	$0.78 \pm 0.04$	$0.44 \pm 0.03$	$9.0 \pm 2.0$	$0.6 \pm 0.4$	$0.647 \pm 0.004$	$0.350 \pm 0.004$
${}^8\text{Be}$	$13.2 \pm 0.2$	$0.86 \pm 0.09$	$0.79 \pm 0.07$		$12.0 \pm 0.1$	$0.603 \pm 0.003$		
${}^9\text{Be}$	$12.3 \pm 0.2$	$0.90 \pm 0.10$	$0.84 \pm 0.07$	$0.69 \pm 0.06$	$10.0 \pm 3.0$	$0.7 \pm 0.7$	$0.65 \pm 0.02$	$0.524 \pm 0.005$
${}^{10}\text{B}$	$11.7 \pm 0.2$	$0.89 \pm 0.09$	$0.79 \pm 0.06$		$10.7 \pm 0.2$	$0.57 \pm 0.02$		
${}^{12}\text{C}$	$16.8 \pm 0.8$	$1.4 \pm 0.2$	$1.3 \pm 0.2$		$14.9 \pm 0.1$	$0.83 \pm 0.01$		
	$18 \pm 2$ (exp)	$1.5 \pm 0.5$ (exp)						



# The Correlations group



- MIT (Or Hen):



**Barak Schmookler**



**Reynier Torres**



**Efrain Segarra**



**Afroditi Papadopoulou**



**Axel Schmidt**



**George Laskaris**

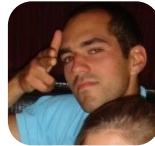


**Maria Patsyuk**



**Adi Ashkenazy**

- TAU (Eli Piassetzky):



**Erez Cohen**



**Meytal Duer**



**Igor Korover**

- ODU (Larry Weinstein):



**Mariana Khachatryan**



**Florian Hauenstein**

- Theory Collaborators (lots!)