

# Probing nuclear effects with transverse kinematic imbalance

*Stephen Dolan*

*For the T2K Collaboration*

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# Overview

Thanks for voting for my poster!!!

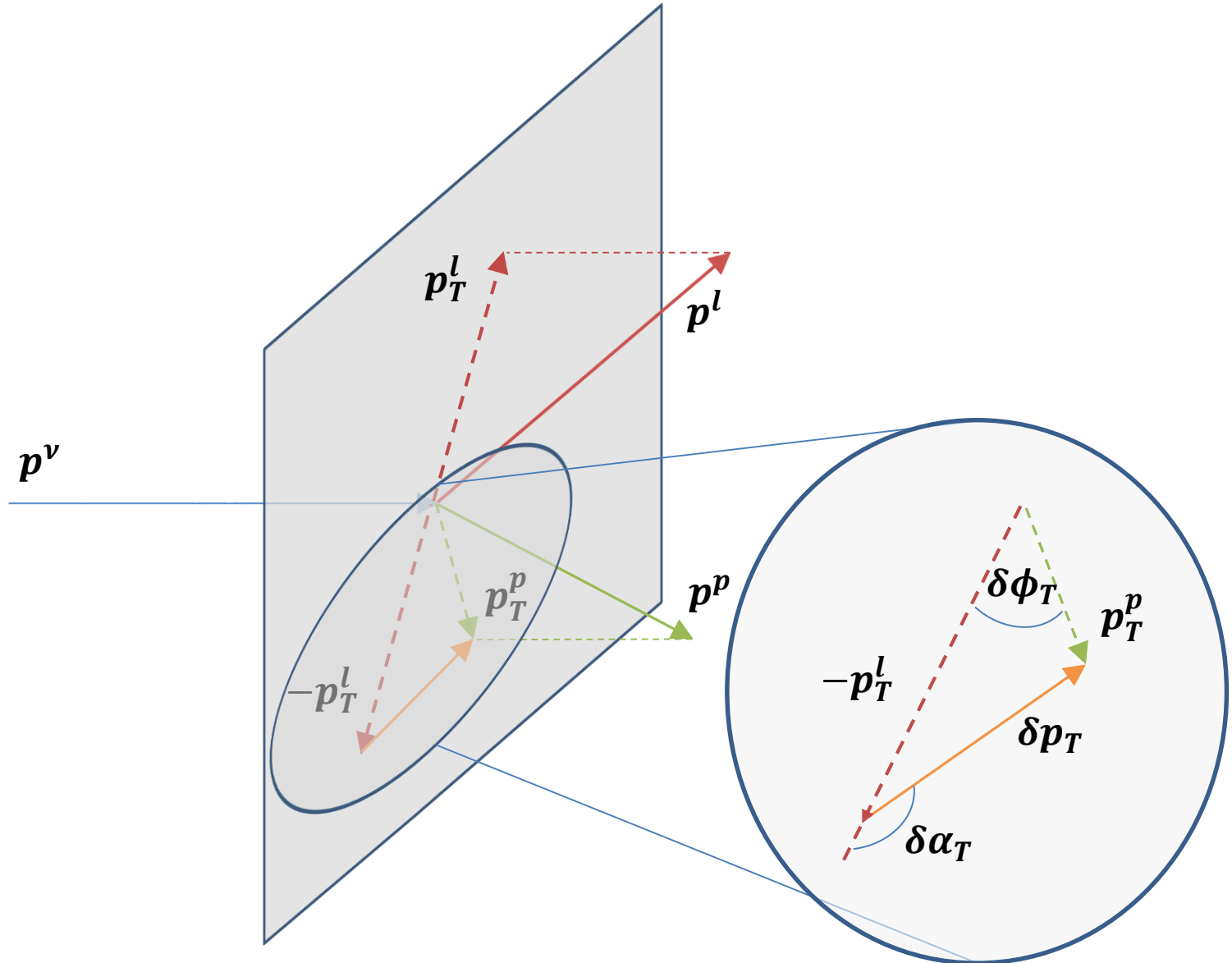
Described the measurement of a **CC0 $\pi$  + Np** (**N  $\geq$  1**) cross section as a function of the **single transverse variables**

[I presented the highlights of this analysis yesterday.](#)

This talk will contain:

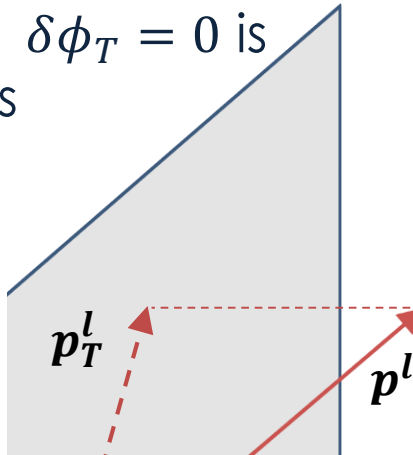
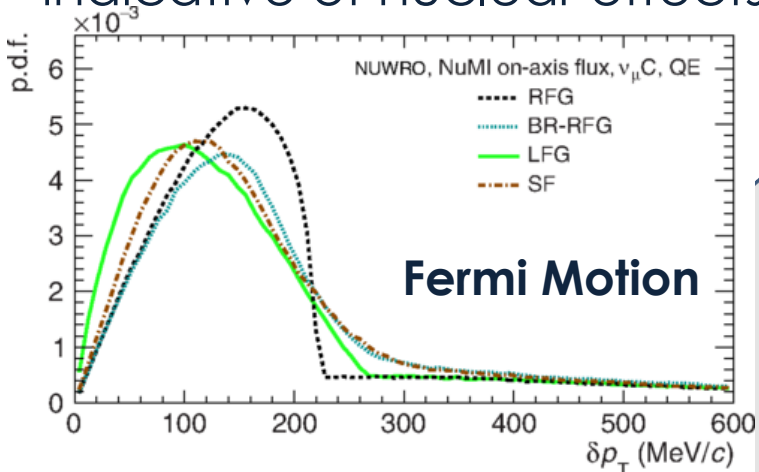
- A quick recap
- A closer look at the generator comparisons

# Single Transverse Variables



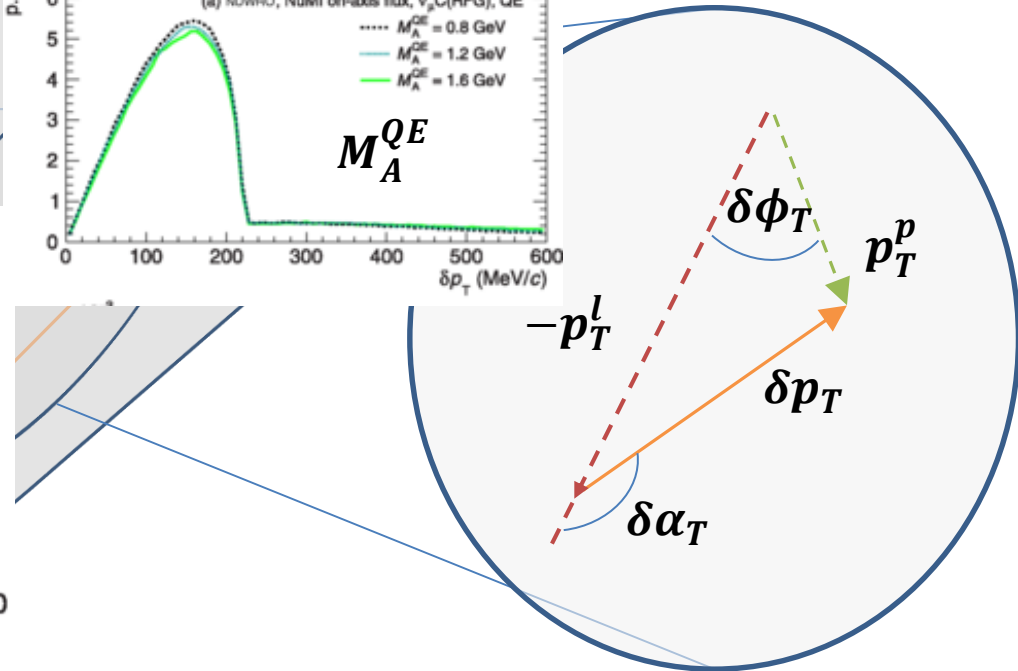
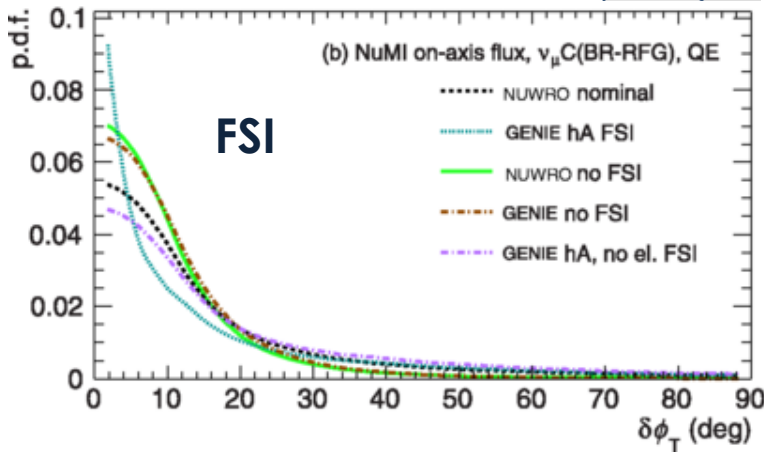
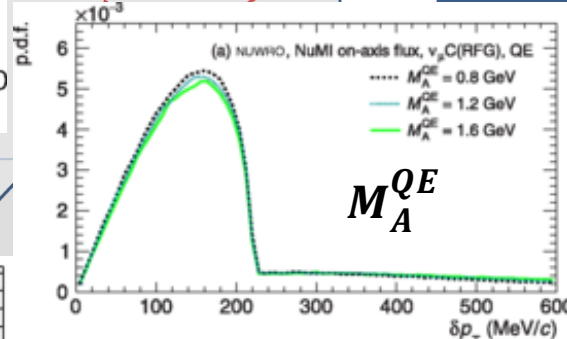
# Single Transverse Variables

Any deviation from  $\delta p_T = 0$ ,  $\delta \phi_T = 0$  is indicative of nuclear effects



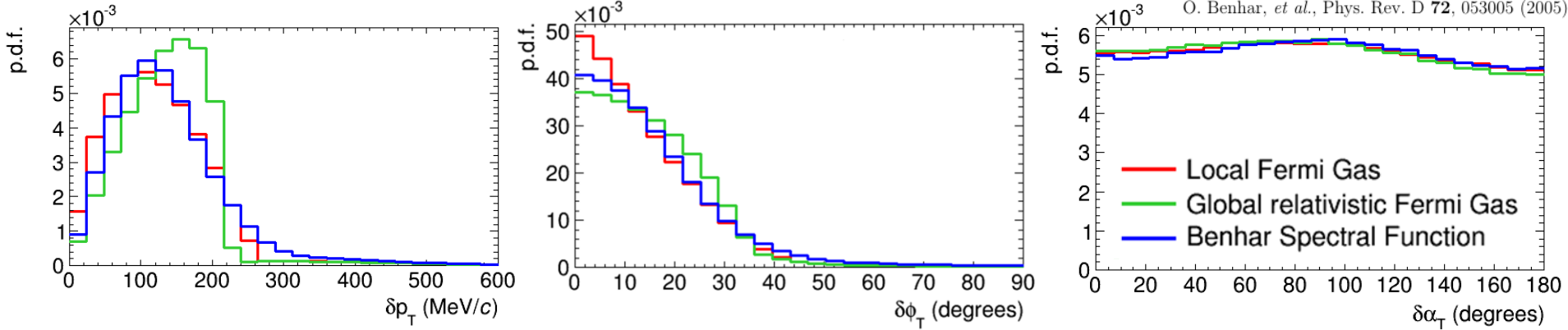
Phys. Rev. C **94**, 015503 (2016)

- Demonstrates interesting sensitivity to nuclear effects for **exclusive interaction modes**

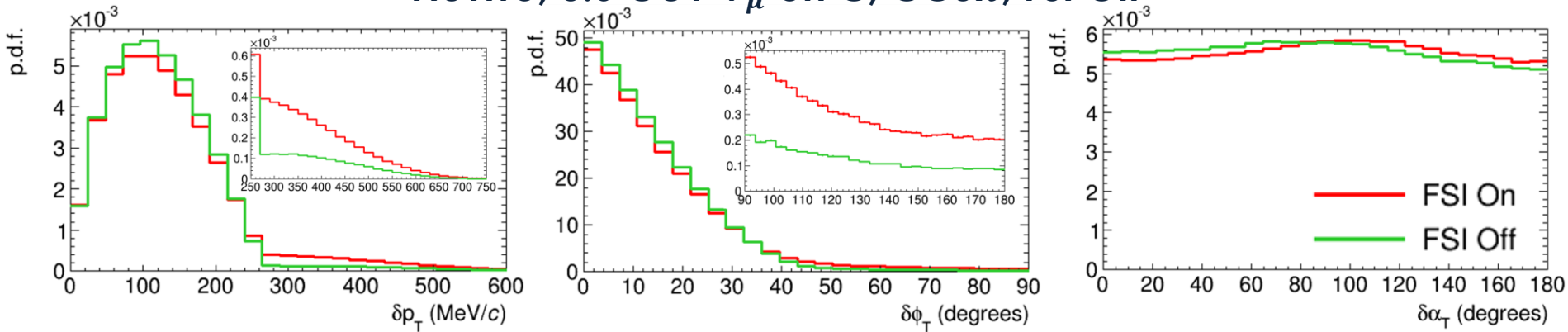


# CC0 $\pi$ in STV - Fermi Motion and FSI

- Moving from CCQE $\rightarrow$ CC0 $\pi$ +N $p$ , STV still a probe of nuclear effects



## NuWro, 0.6 GeV $\nu_\mu$ on C, CC0 $\pi$ , FSI Off



## NuWro, 0.6 GeV $\nu_\mu$ on C, CC0 $\pi$ , LFG

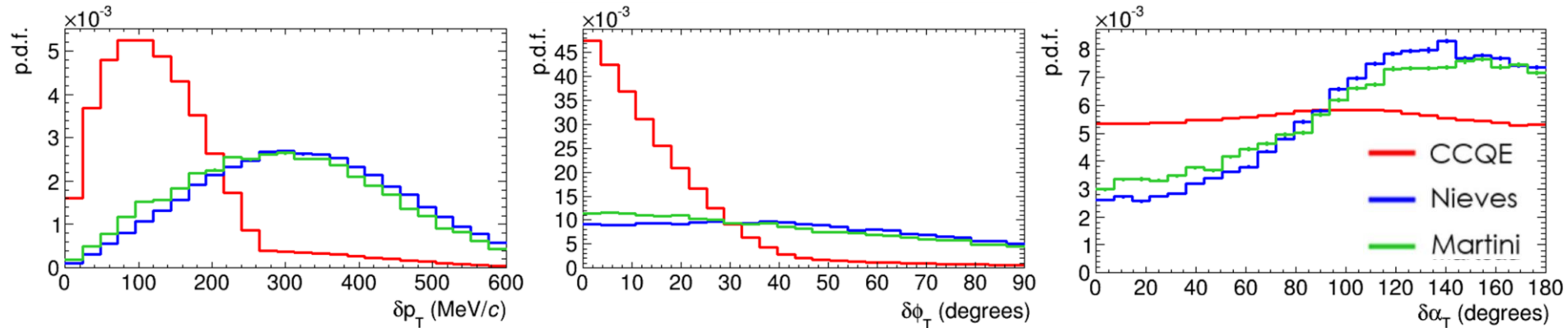
**Quasi-real CC0 $\pi$  selection**, keep events within rough ND280 acceptance :

No Pions, 1 Muon,  $>0$  Protons.  $p_\mu > 250$  MeV,  $p_p > 450$  MeV,  $\cos(\theta_\mu) > -0.6$ ,  $\cos(\theta_p) > 0.4$

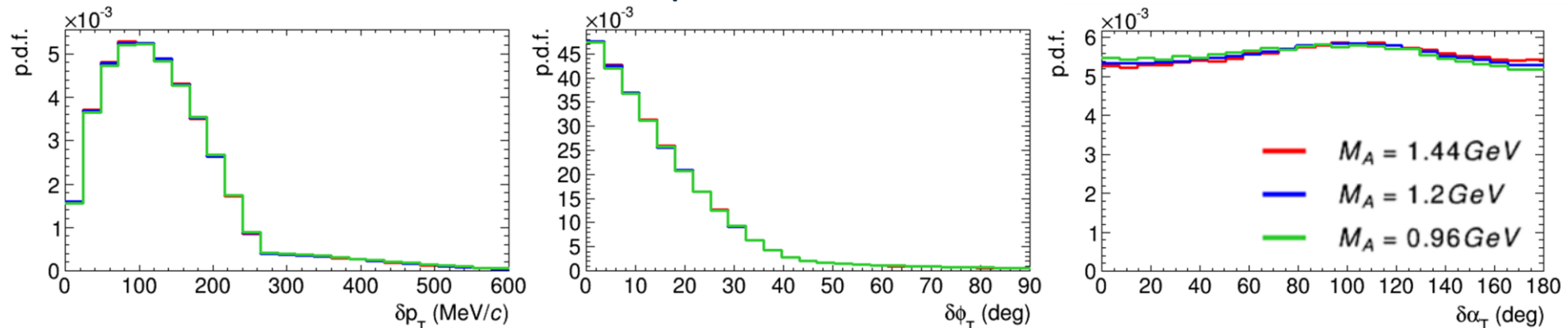
# CC0 $\pi$ in STV - 2p2h and $M_A$

M. Martini, M. Ericson, G. Chanfray, and J. Marteau, Phys. Rev. C **80**, 065501 (2009)

J. Nieves, I. R. Simo, and M. J. V. Vacas, Phys. Rev. C **83**, 045501 (2011)



## NuWro, 0.6 GeV $\nu_\mu$ on C, CC0 $\pi$ , FSI On, LFG



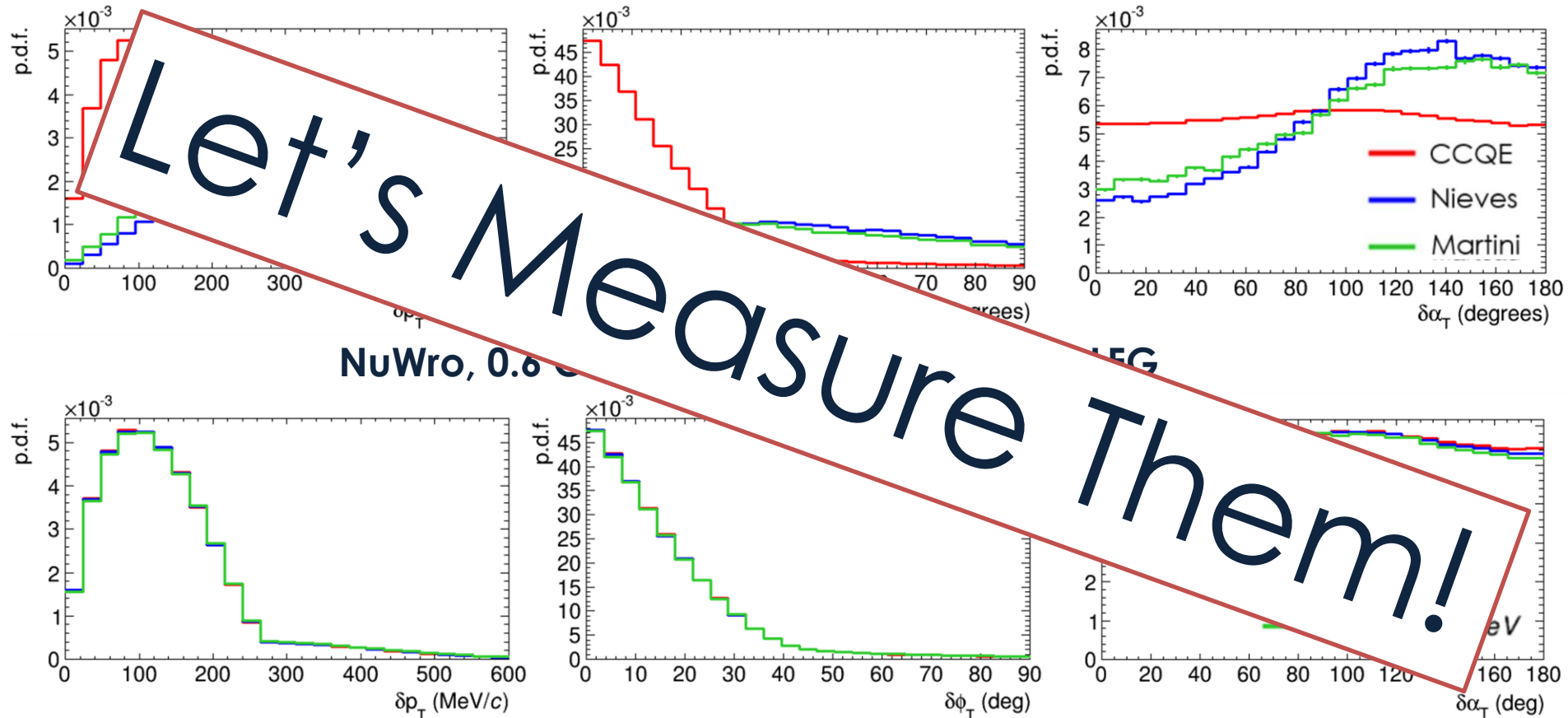
## NuWro, 0.6 GeV $\nu_\mu$ on C, CC0 $\pi$ , FSI On, LFG

- STV shape invariant with  $M_A$ 
  - No ambiguity over  $M_A$  or nuclear effect contributions (MiniBooNE  $M_A$  puzzle)

# CC0 $\pi$ in STV - 2p2h and $M_A$

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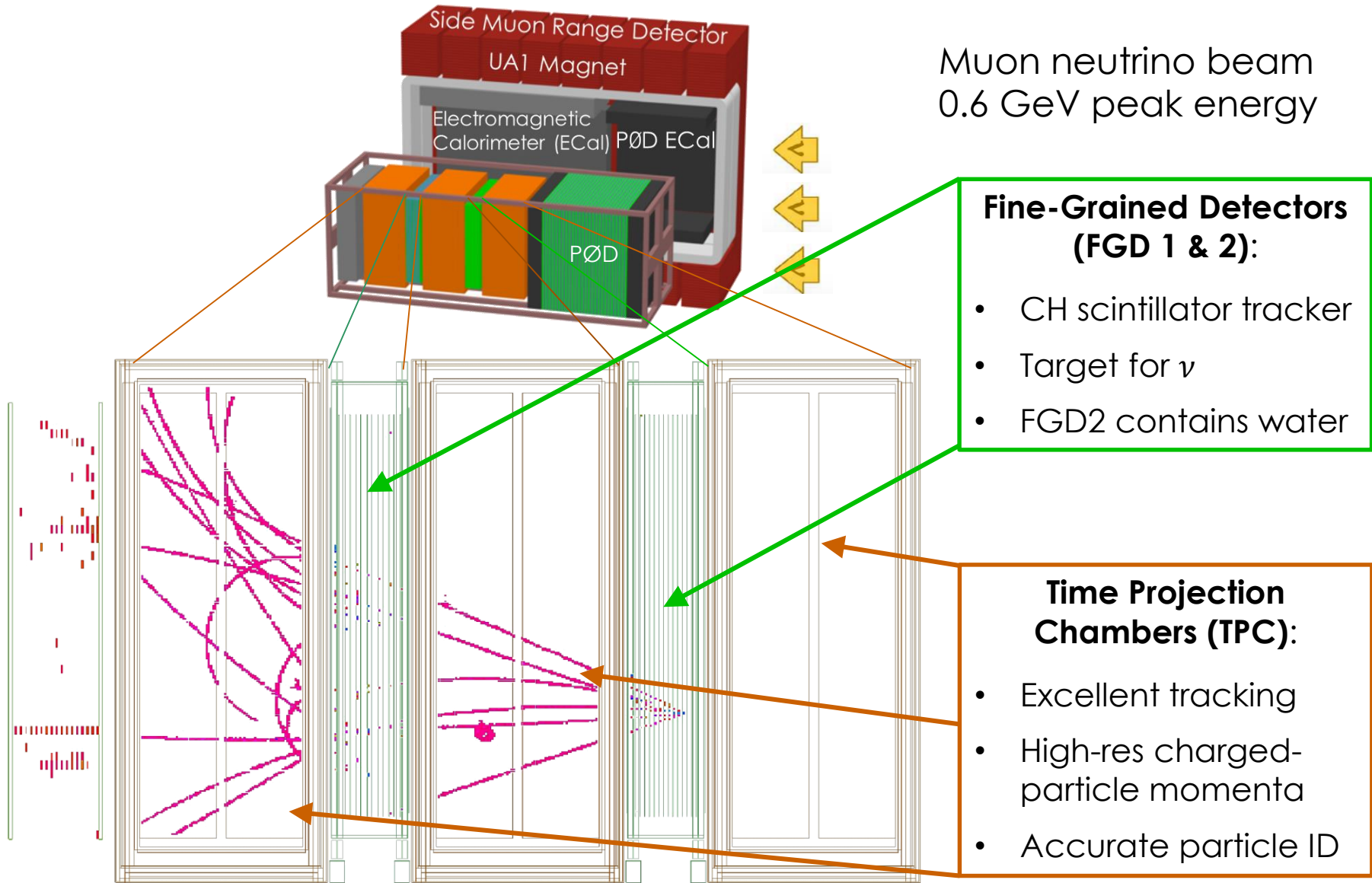


NuWro, 0.6 GeV  $\nu_\mu$  on C, CC0 $\pi$ , FSI On, LFG

- STV shape invariant with  $M_A$ 
  - No ambiguity over  $M_A$  or nuclear effect contributions (MiniBooNE  $M_A$  puzzle)

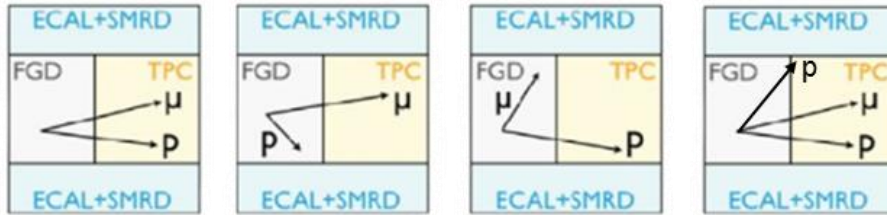


# ND280 (off axis near detector)



# Event Selection

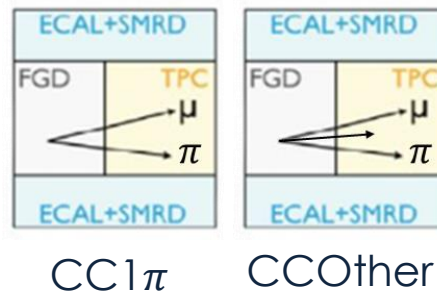
## Signal



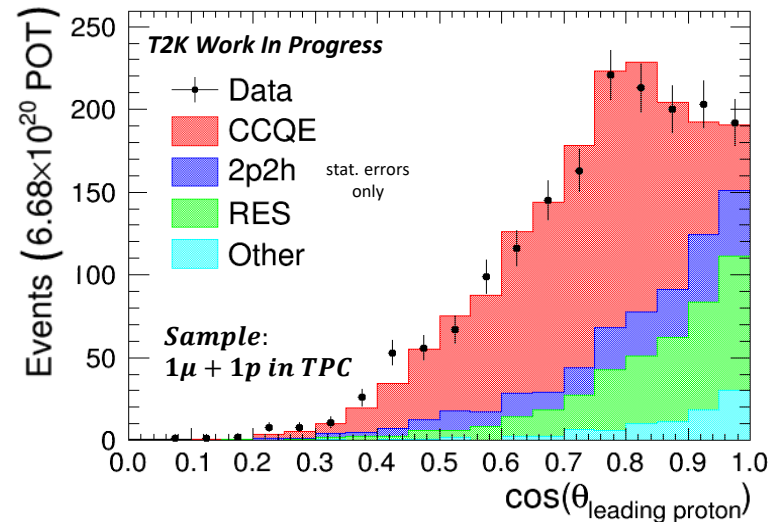
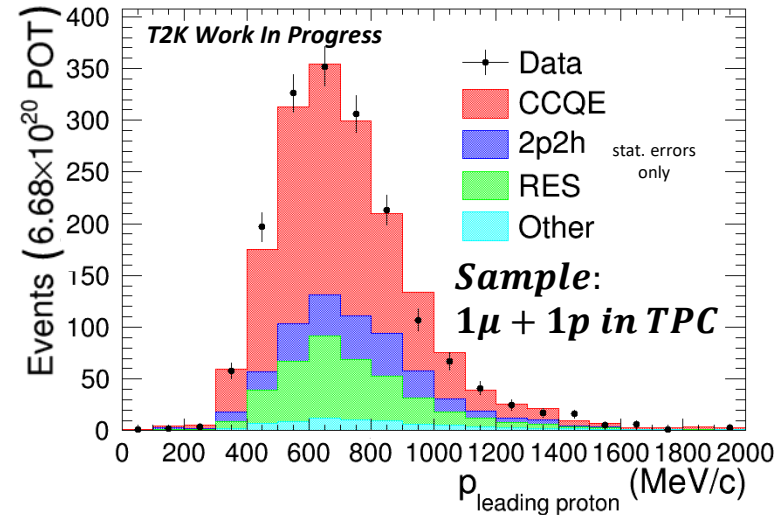
- Require one  $\mu$ -like and  $p$ -like track(s) starting in FGD1 (CH target)
- Use a Michel electron tag and ECal EM shower veto to reject  $1\pi$  backgrounds
- Use of many samples gives wide kinematic acceptance

## Sidebands

- Require extra  $\pi$ -like track(s)



## Reconstructed kinematics



NEUT 5.3.3.2; Benhar SF;  $M_A = 1.21$ ;  
Nieves et al. 2p2h; Area normalised to data

O. Benhar, *et al.*, Phys. Rev. D **72**, 053005 (2005)

J. Nieves, I. R. Simo, and M. J. V. Vacas, Phys. Rev. C **83**, 045501 (2011)

# CC0 $\pi$ +Np in STV

## Signal Definition

- One muon
- At least one proton
- Nothing else
- Adhere to fiducial constraints

- Measure **fiducial** flux-integrated **CC0 $\pi$  + Np** cross section **in bins of STV**
- Restrict cross section to ND280 acceptance
  - *Essential to mitigate model-dependence of acceptance correction*
- Extract cross section using a **binned likelihood fit** with a **data driven** regularisation
- Compare results to predictions available from plethora of generators using NUISANCE

$$p_{\mu} > 250 \text{ MeV}/c$$

$$\cos(\theta_{\mu}) > -0.6$$

$$450 \text{ MeV}/c < p_p < 1 \text{ GeV}/c$$

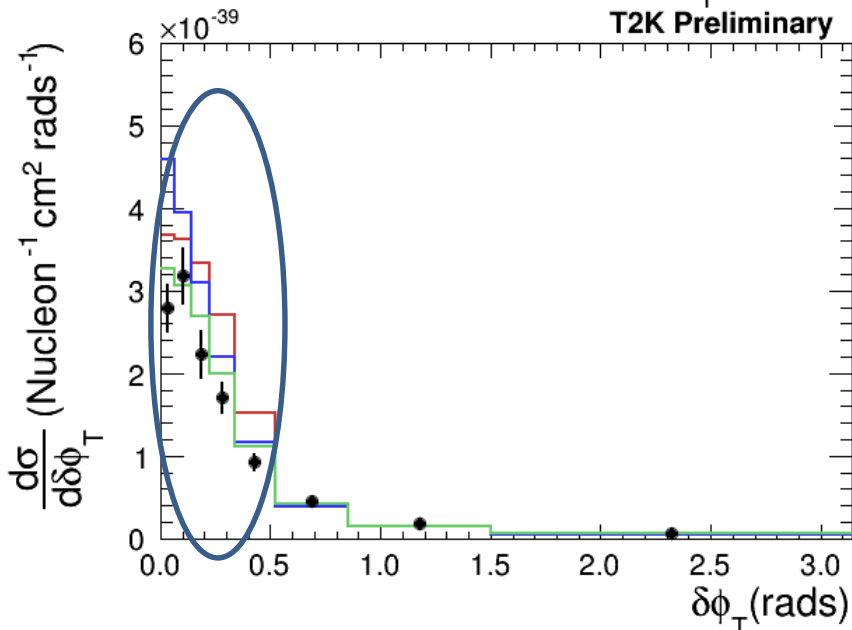
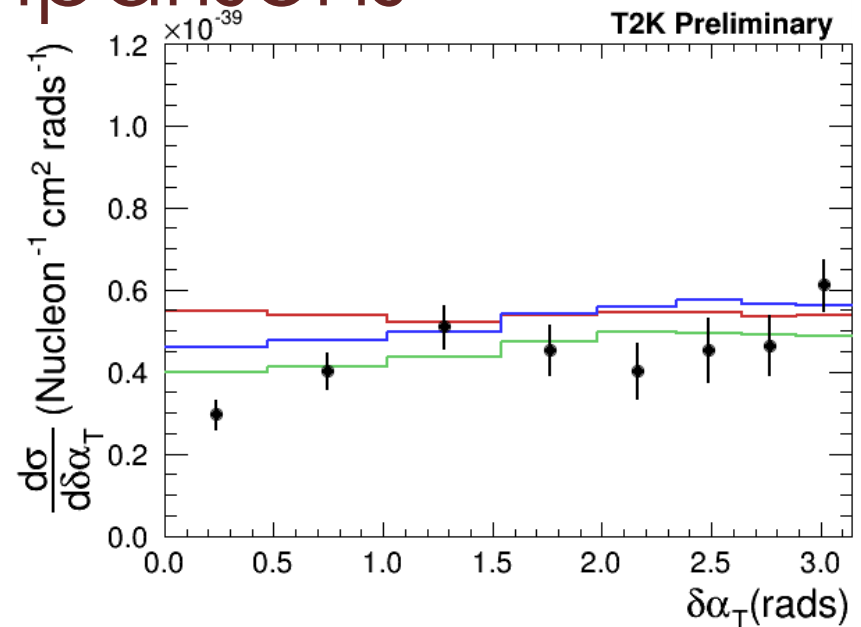
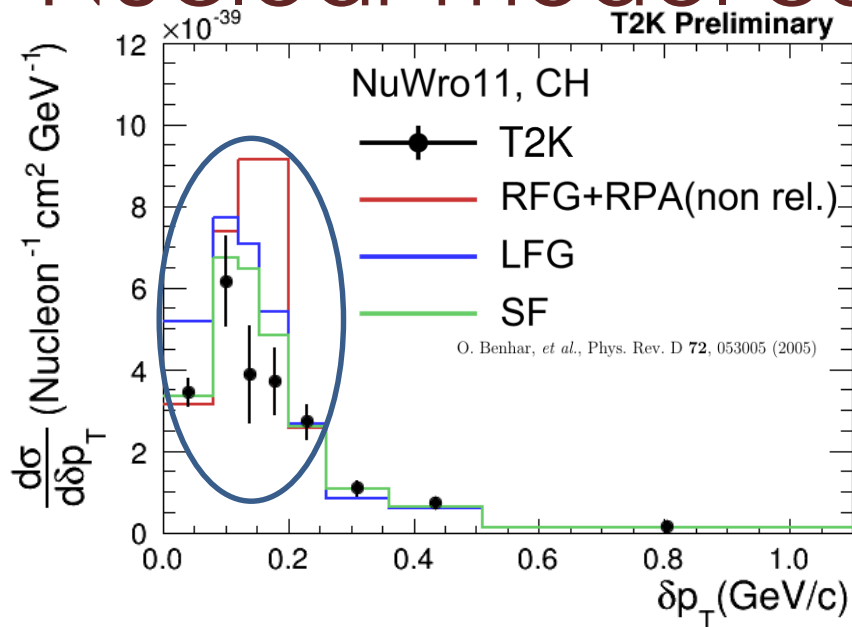
$$\cos(\theta_p) > 0.4$$

For details of unfolding and how model dependence is avoided:

[See slides from State of The Nu-tion](#)

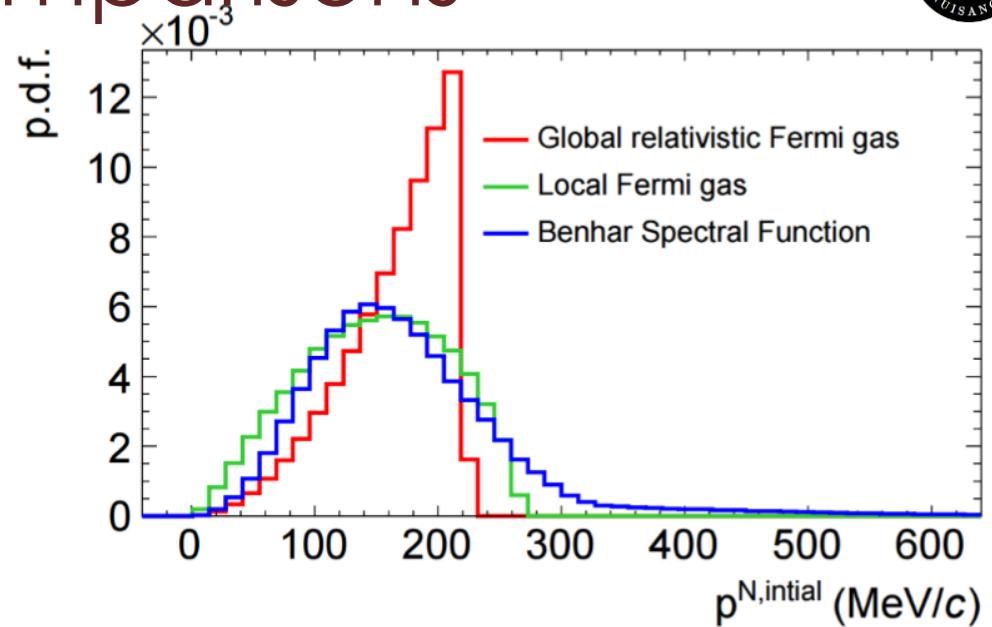
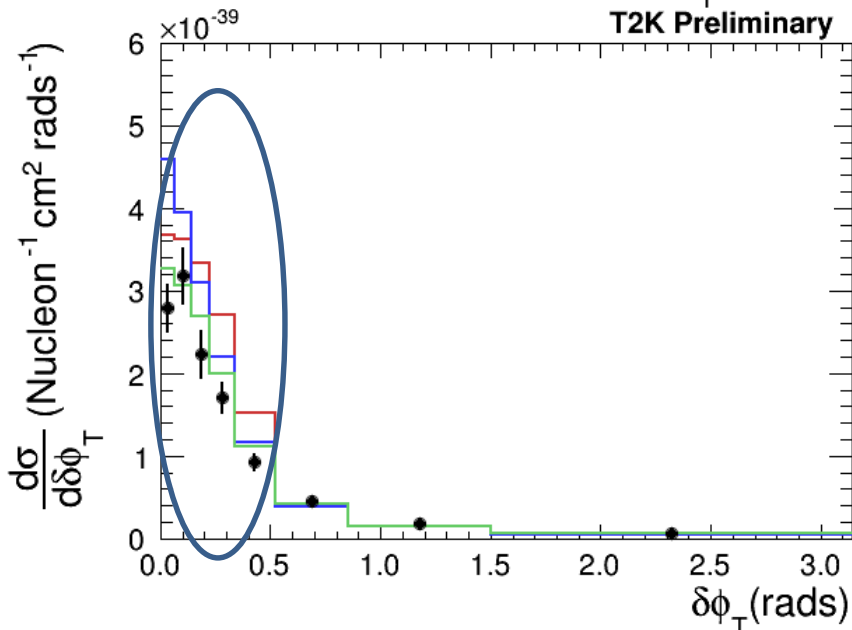
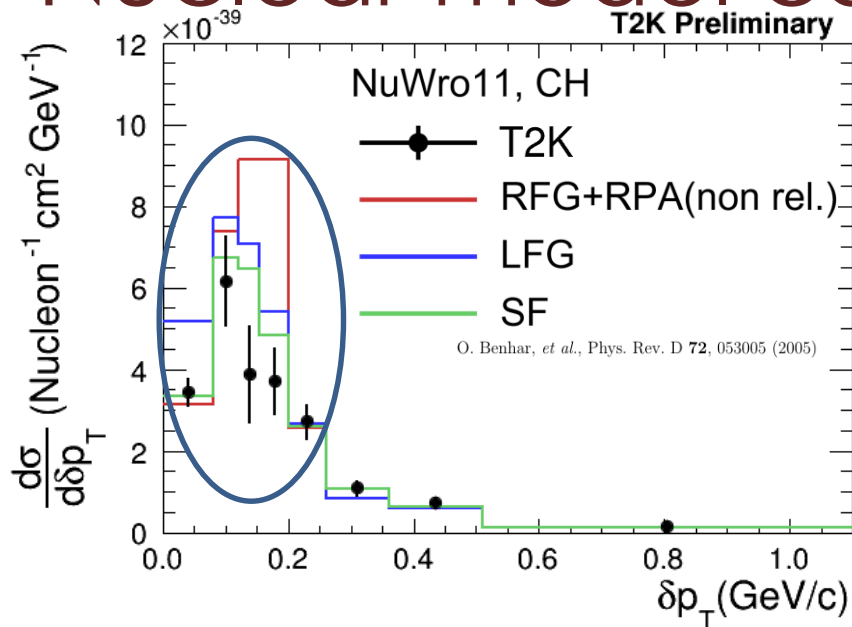
**Detector:** ND280 – FGD1 **Target:** CH **Signal:** CC0 $\pi$ +Np **Variables:** single-transverse **Status:** Paper in preparation

# Nuclear model comparisons



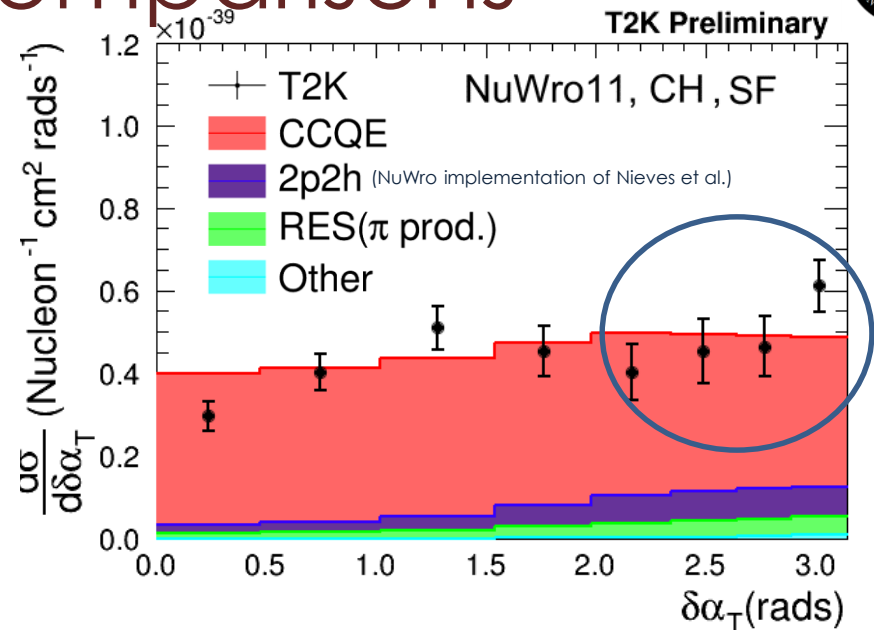
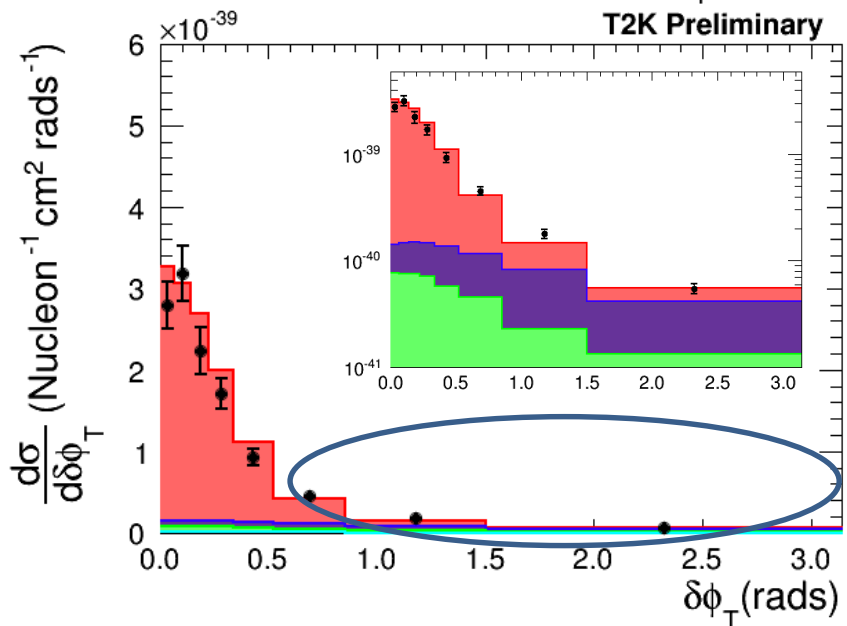
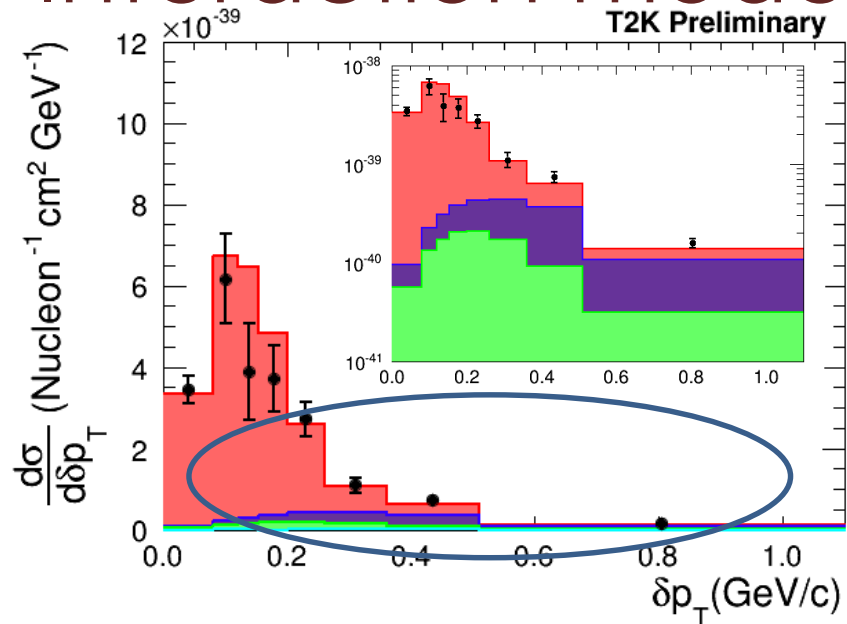
- The peak position and early bins in  $\delta p_T$  and  $\delta\phi_T$  tell us about **Fermi Motion**.

# Nuclear model comparisons



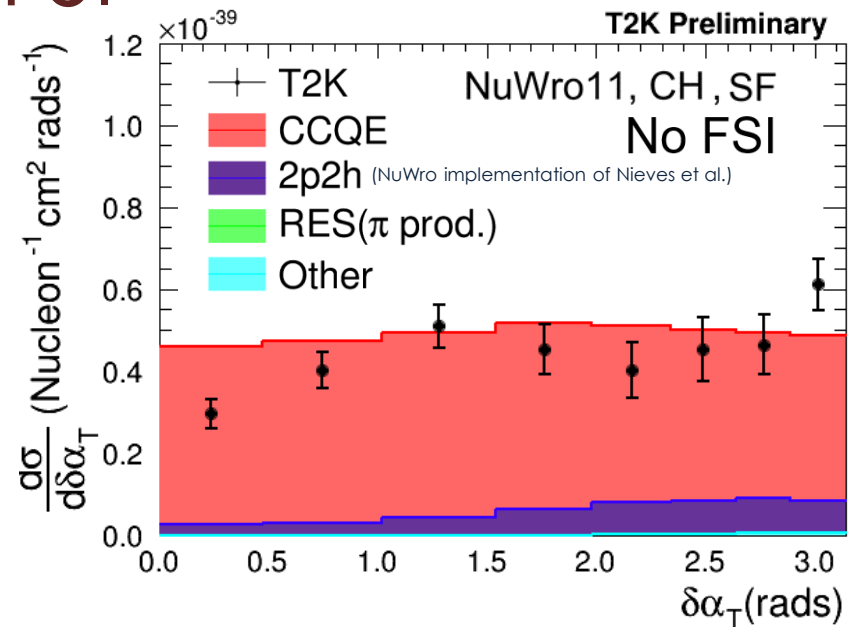
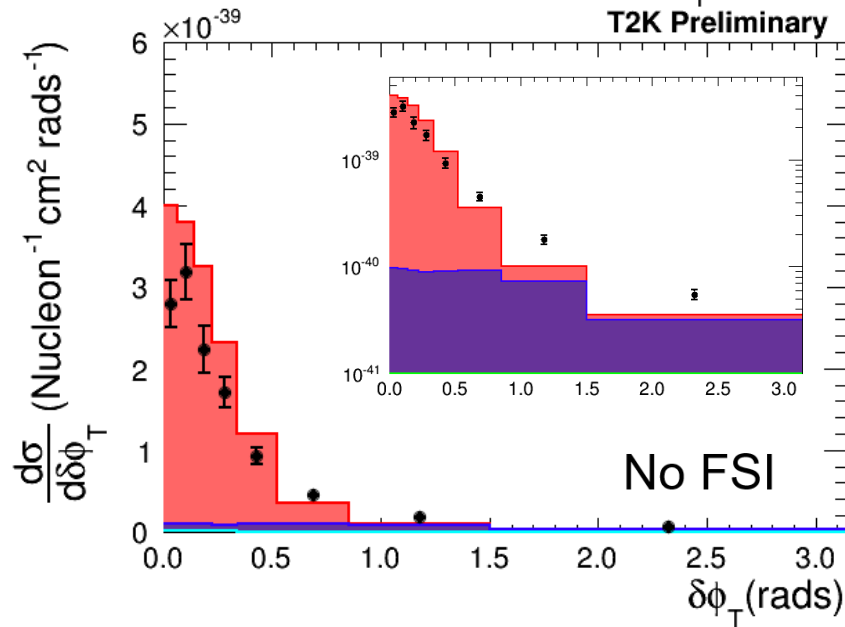
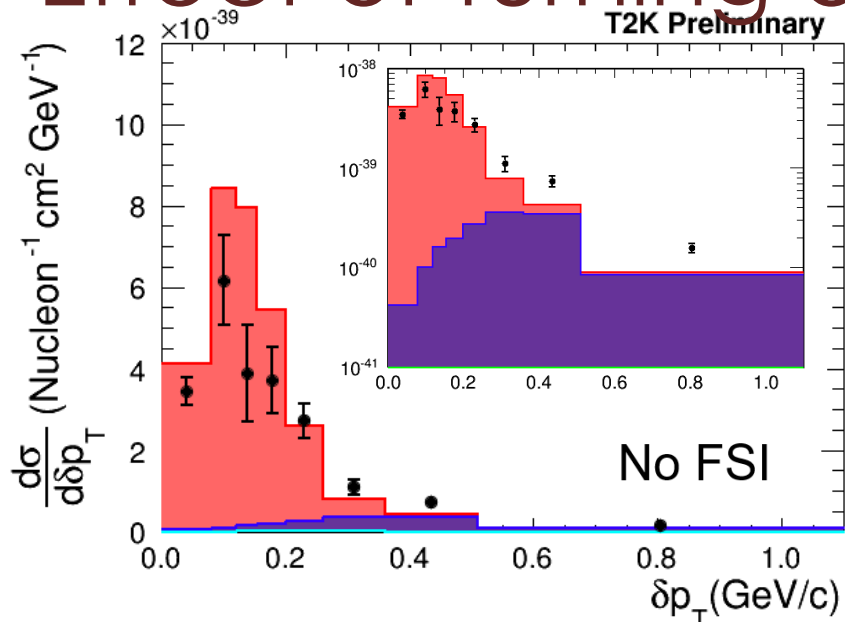
- The peak position and early bins in  $\delta p_T$  and  $\delta\phi_T$  tell us about **Fermi Motion**.

# Interaction mode comparisons



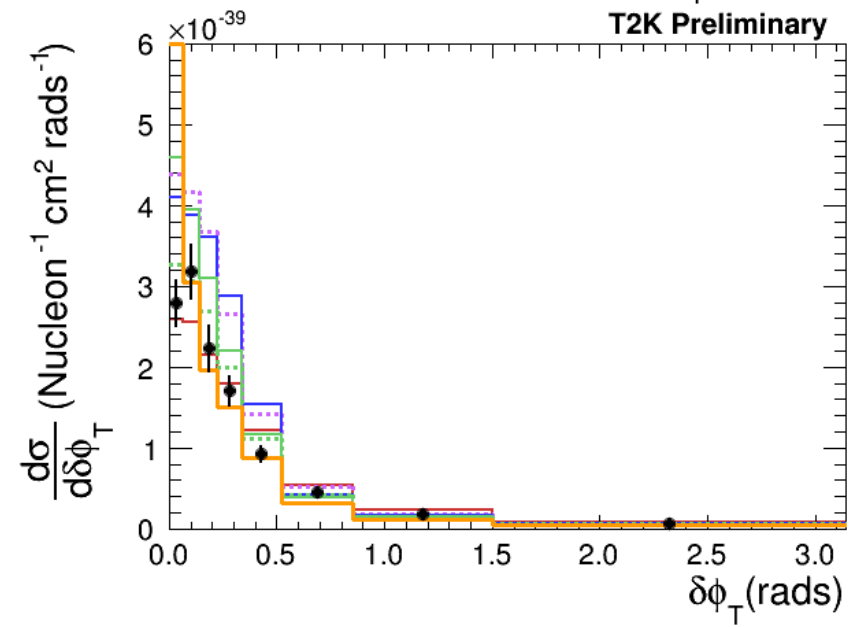
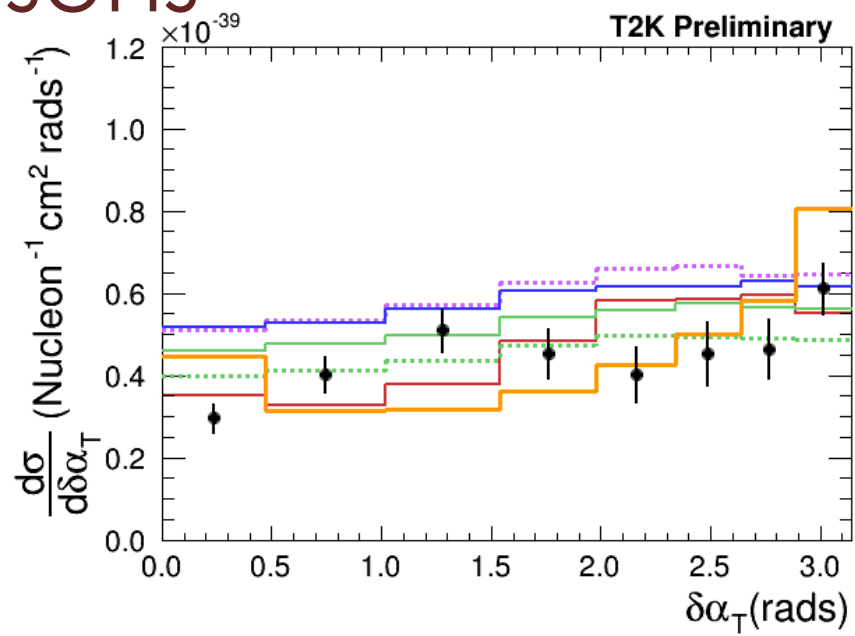
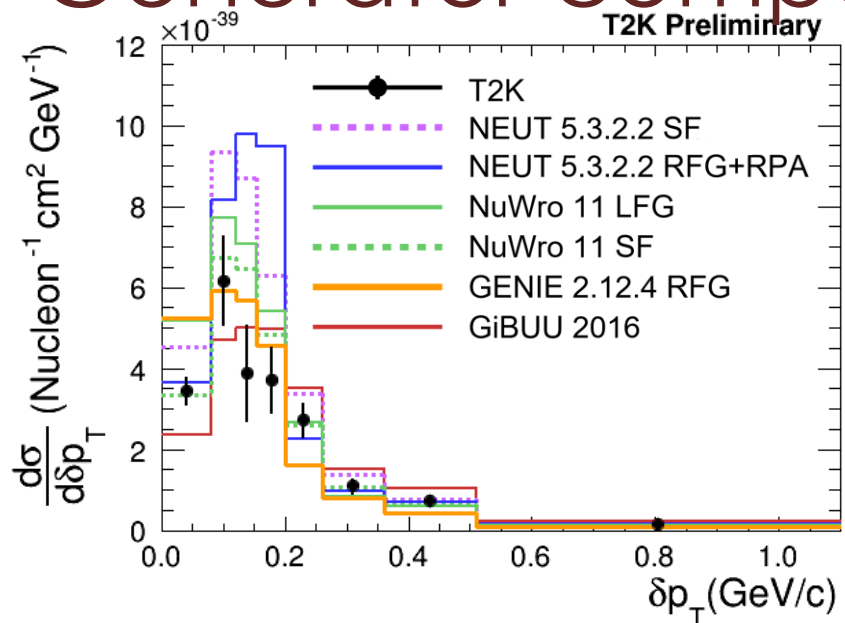
- The peak position and early bins in  $\delta p_T$  and  $\delta\phi_T$  tell us about **Fermi Motion**.
- The tails in  $\delta p_T$  and  $\delta\phi_T$  and the extent of the rise at large  $\delta\alpha_T$  partially isolate the effects of Fermi Motion from **2p2h**.

# Effect of turning off FSI



- The peak position and early bins in  $\delta p_T$  and  $\delta\phi_T$  tell us about **Fermi Motion**.
- The tails in  $\delta p_T$  and  $\delta\phi_T$  and the extent of the rise at large  $\delta\alpha_T$  partially isolate the effects of Fermi Motion from **2p2h**.
- The removal of **FSI** causes a relative deficit of events in the tails, but an increased normalisation.

# Generator comparisons

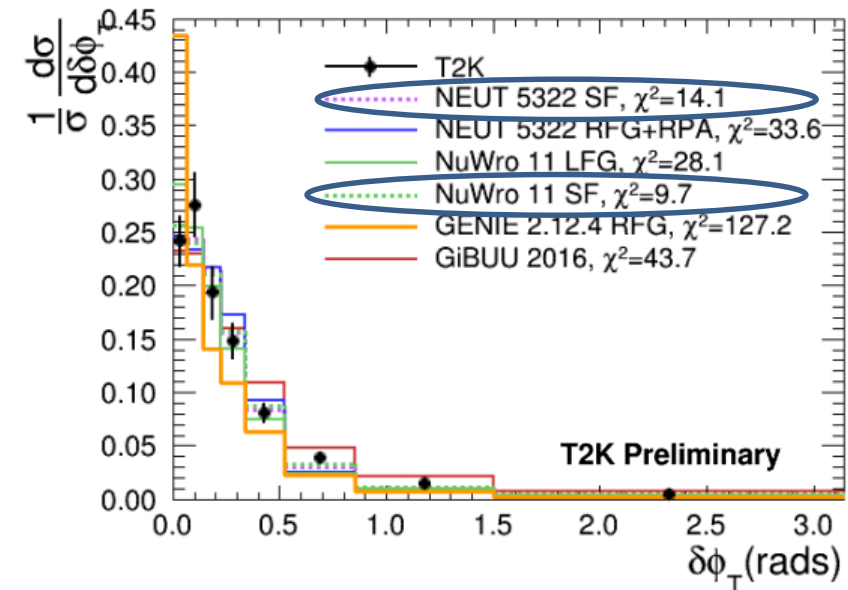
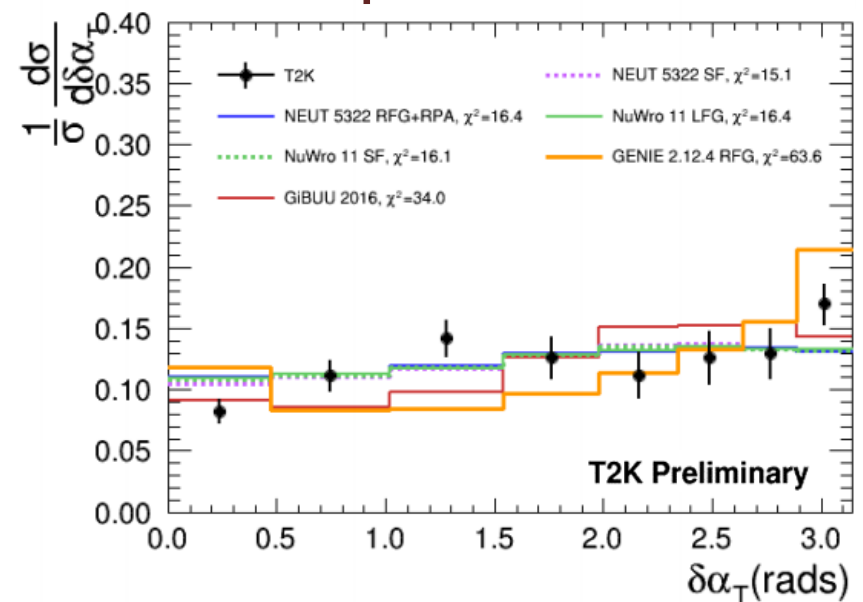
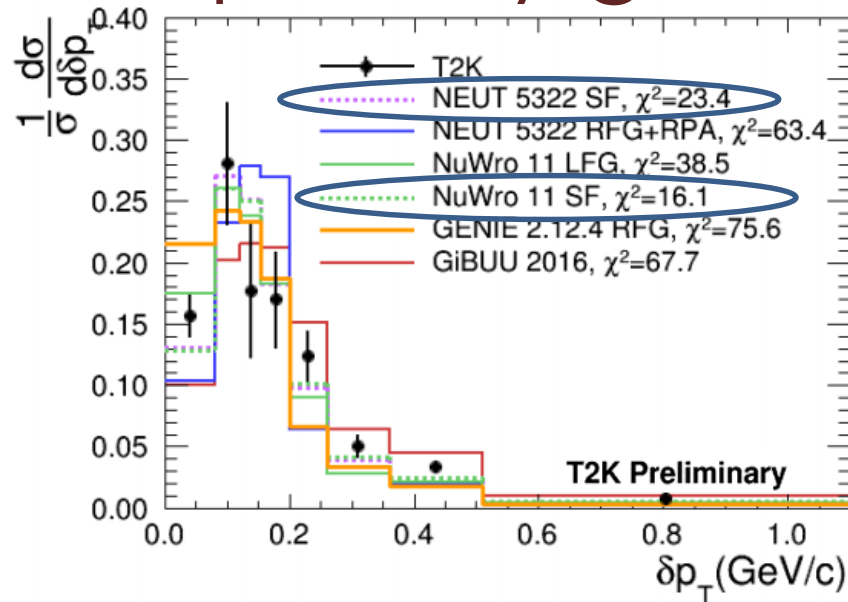


- Plenty of separation
- Result disfavours a 'Fermi cliff' in  $\delta p_T$
- Some nuclear effect isolation



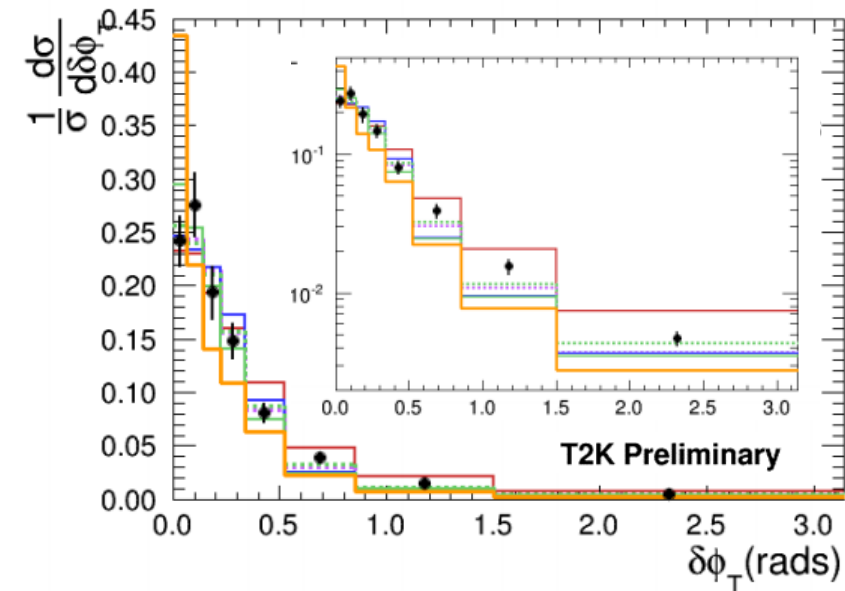
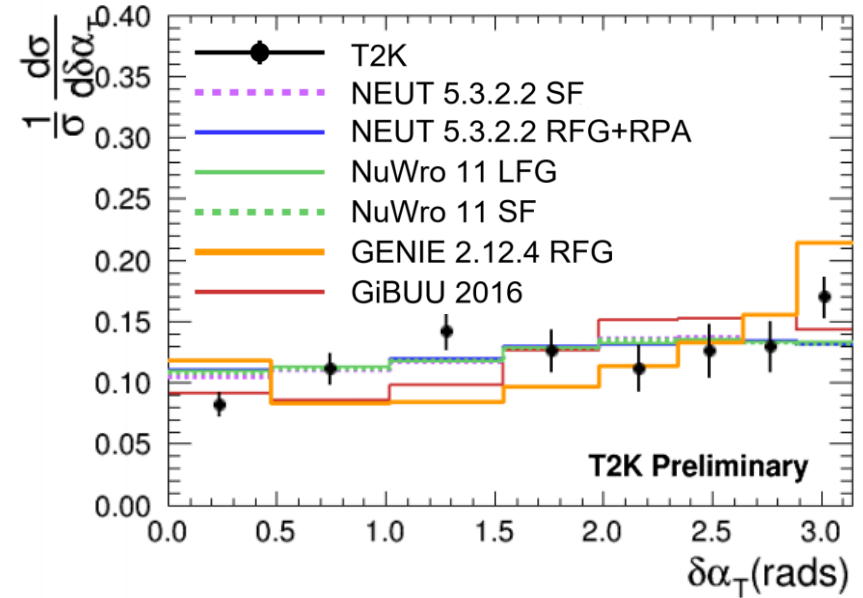
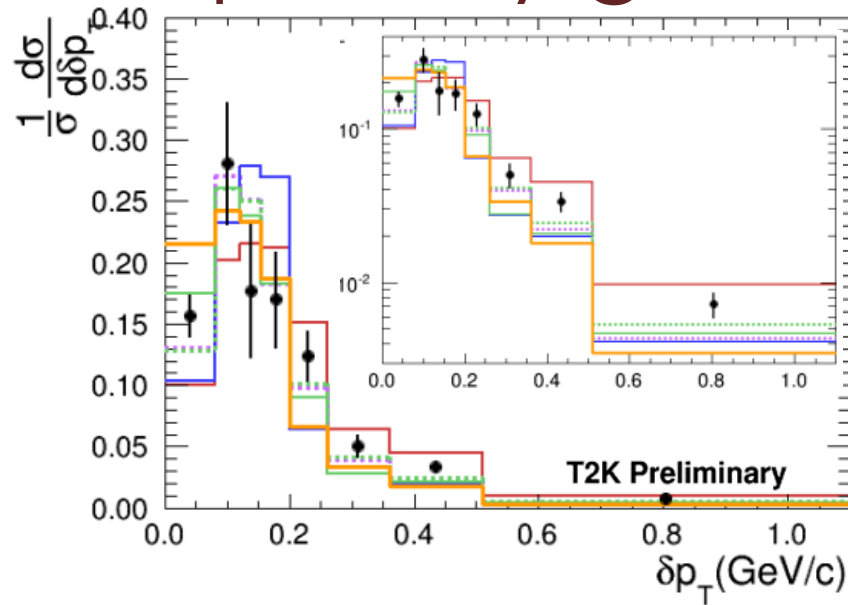


# Shape only generator comparisons



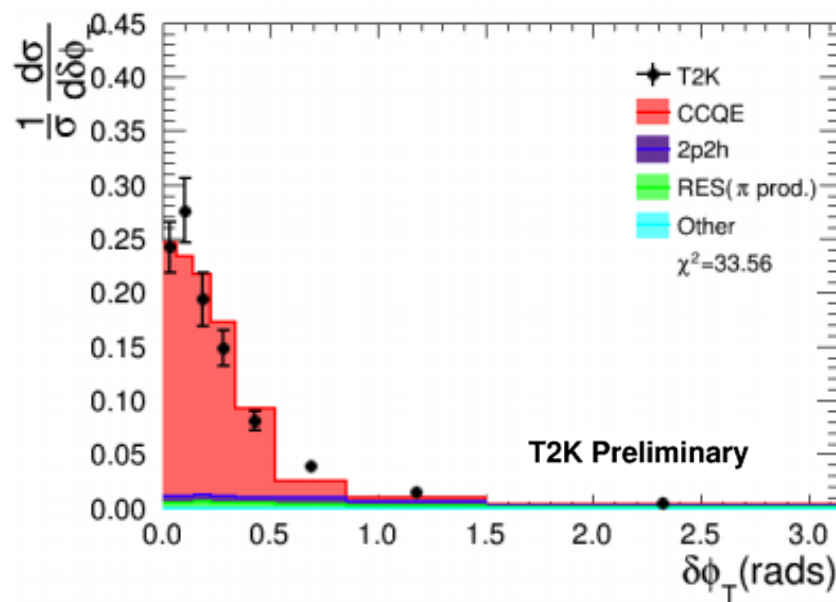
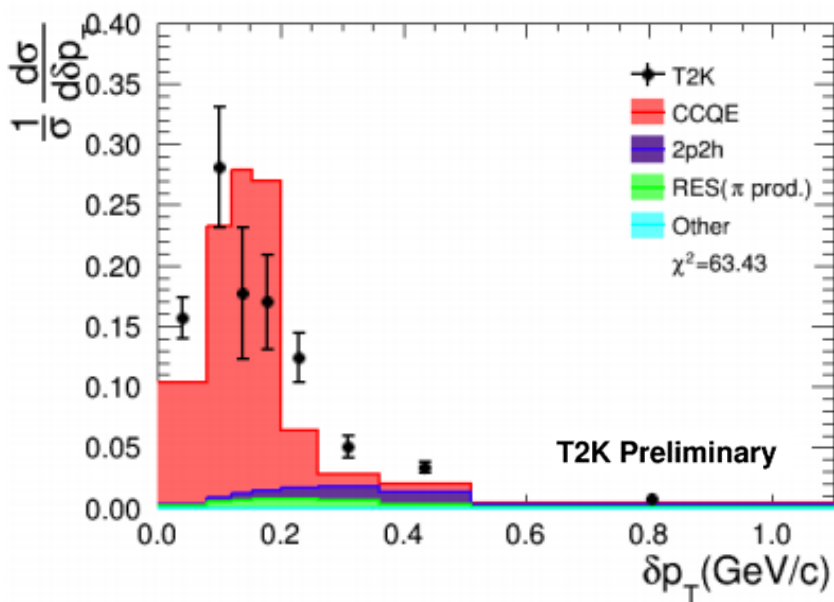
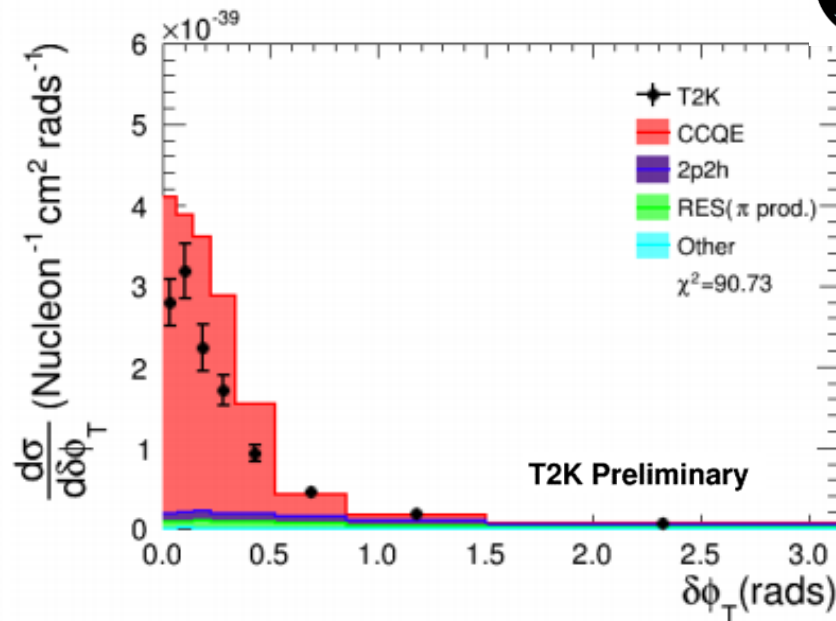
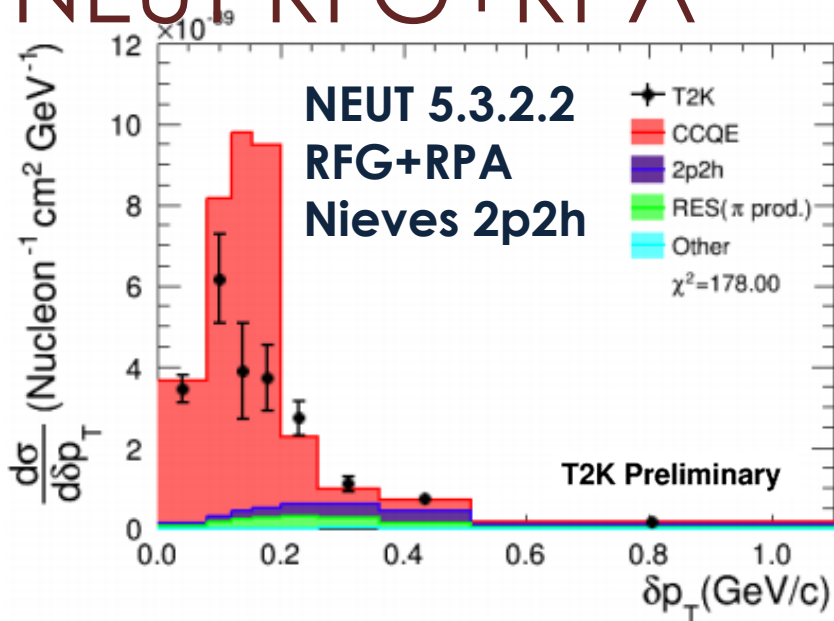
- Preference for a SF + 2p2h franken-model

# Shape only generator comparisons

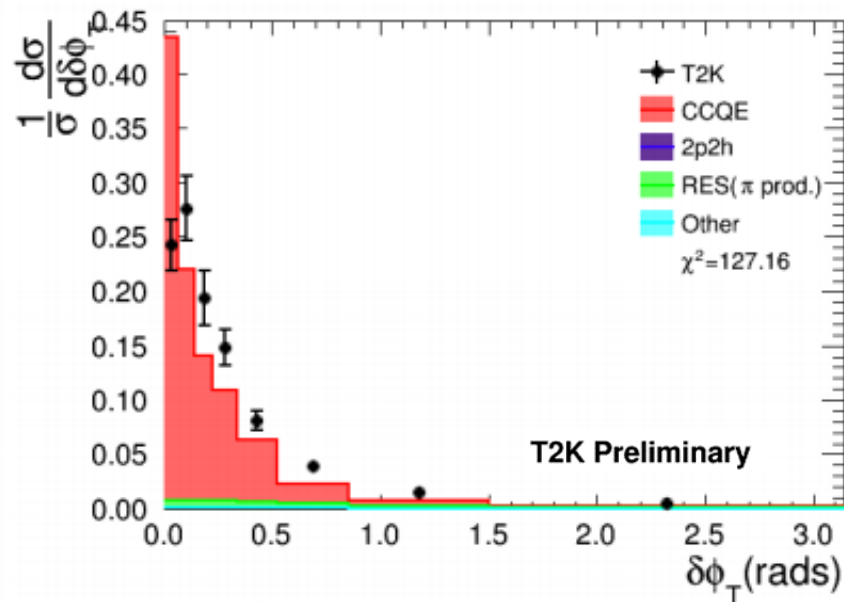
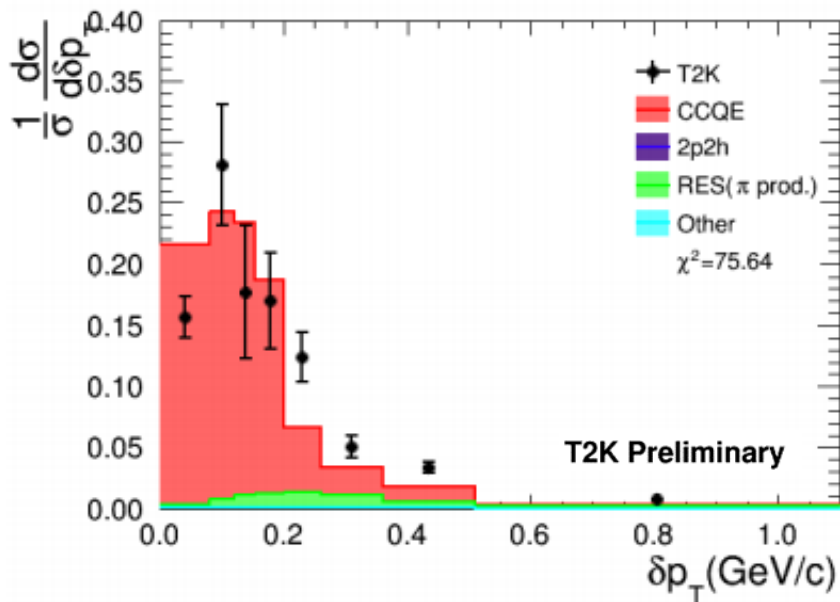
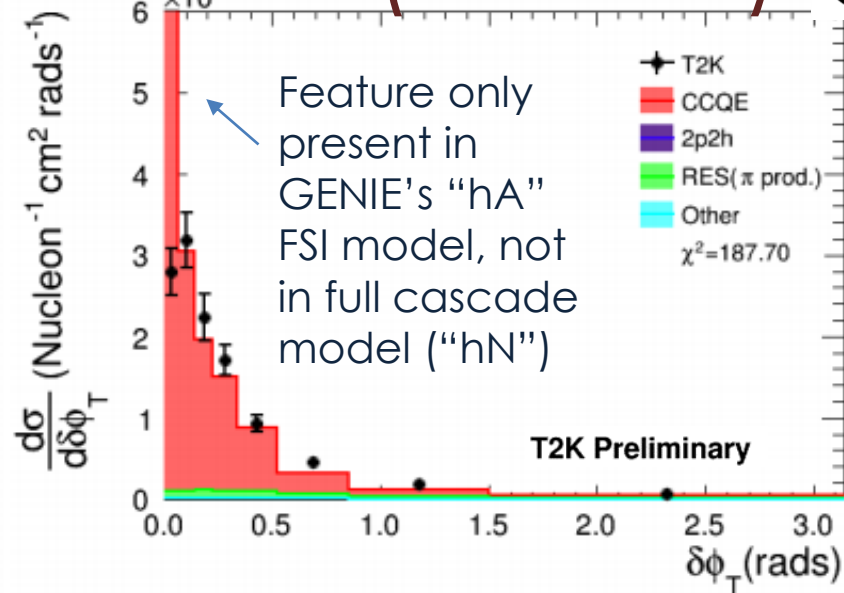
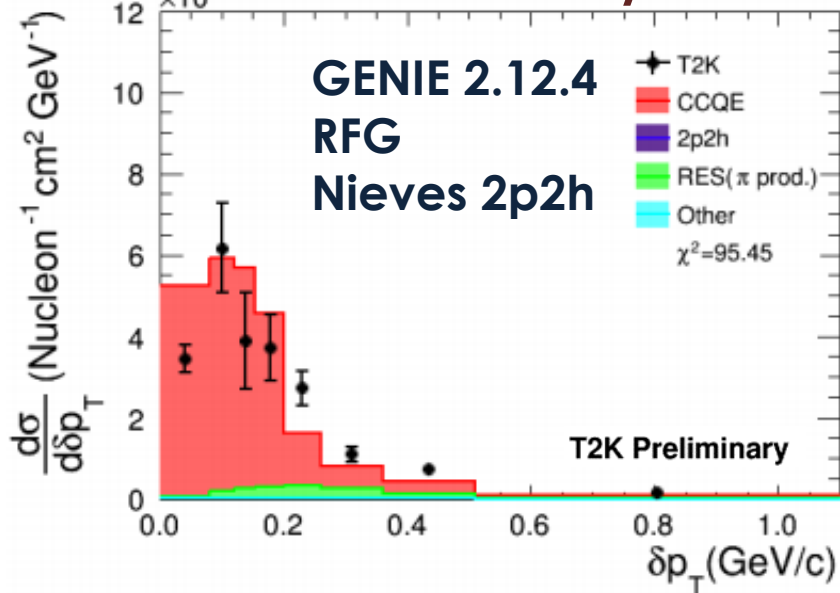


- Preference for a SF + 2p2h franken-model
- Relative excess in the 2p2h enhanced region (for all but GiBUU)

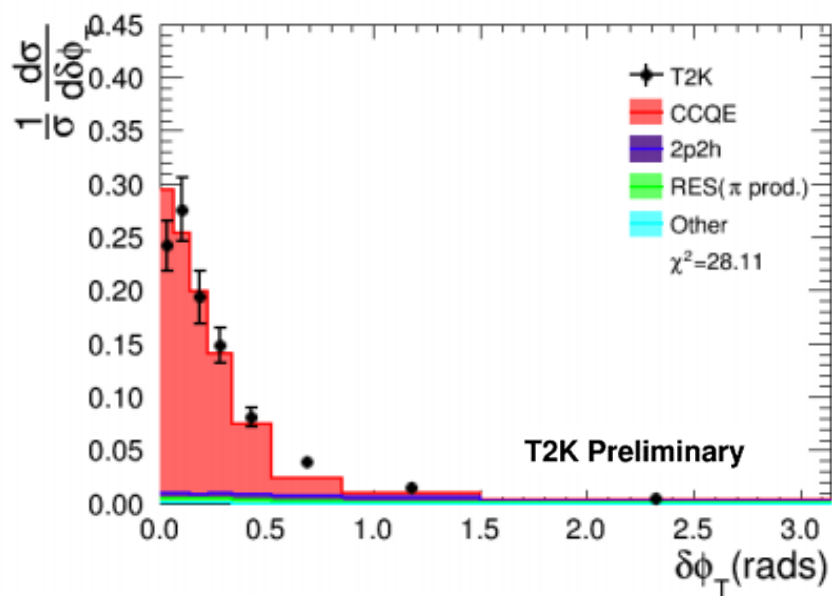
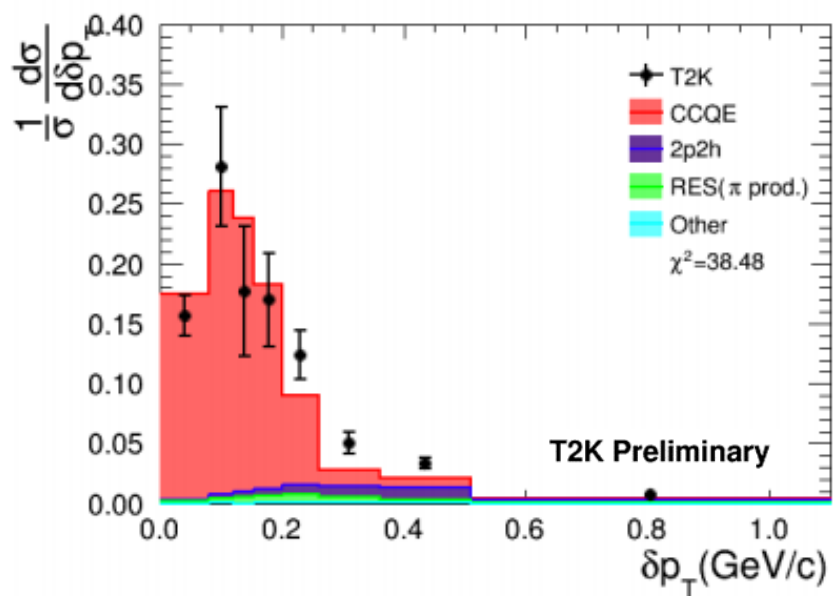
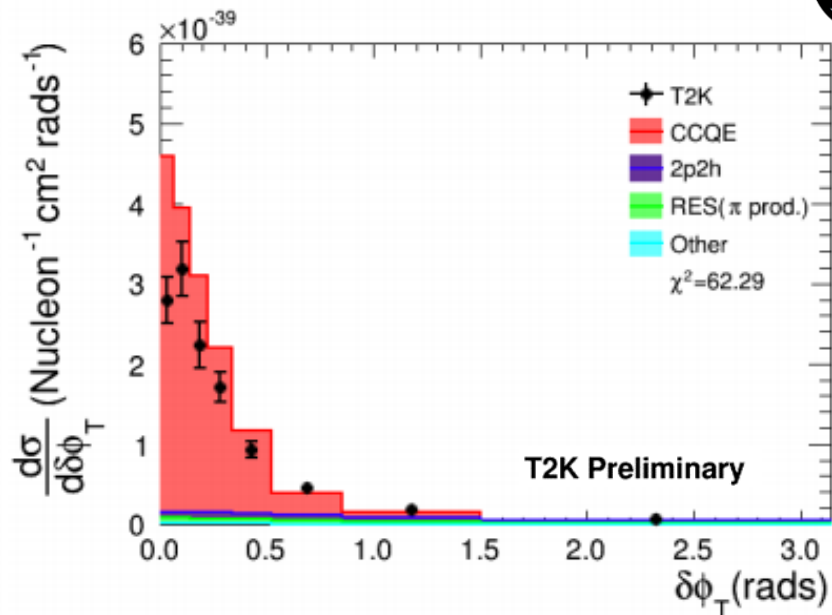
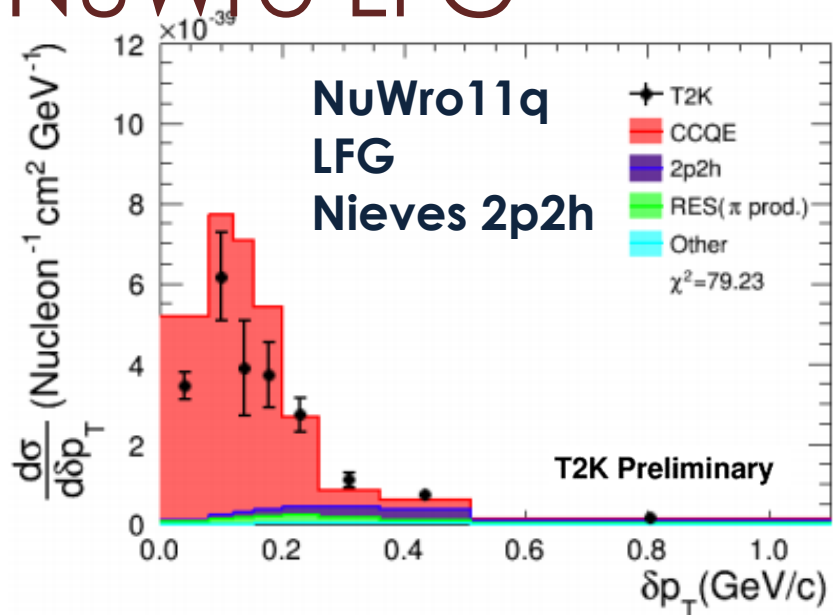
# NEUT RFG+RPA



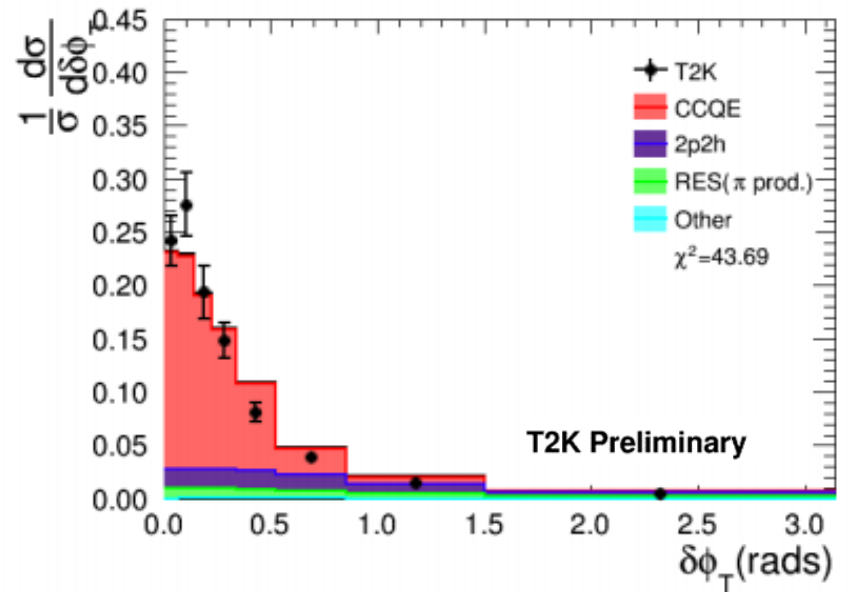
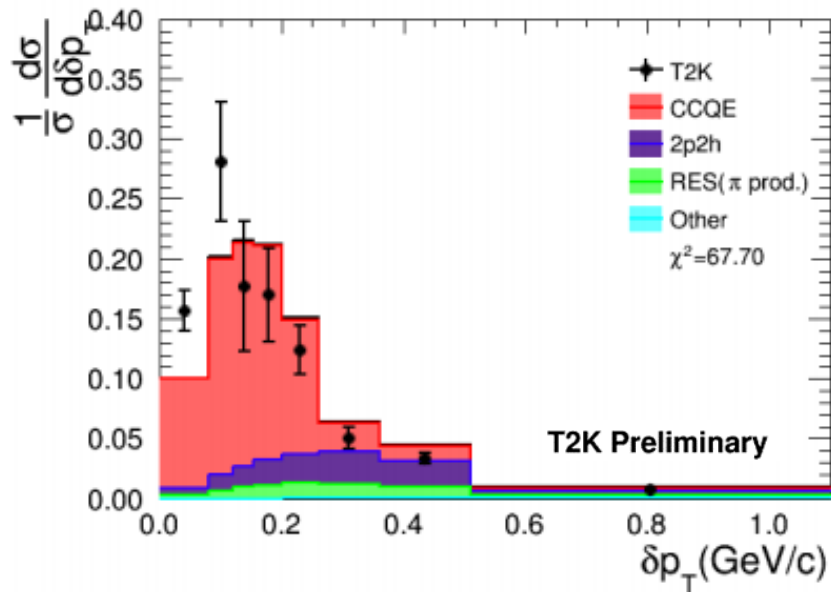
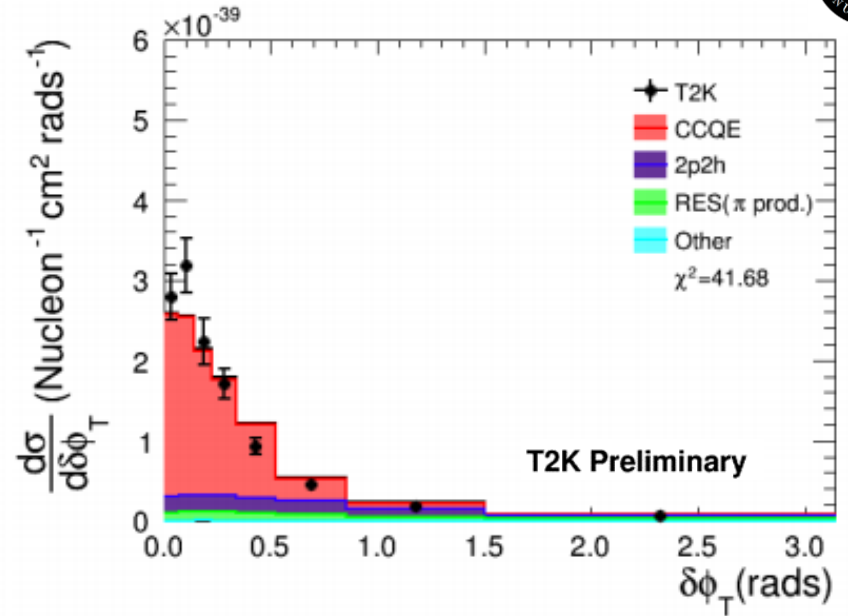
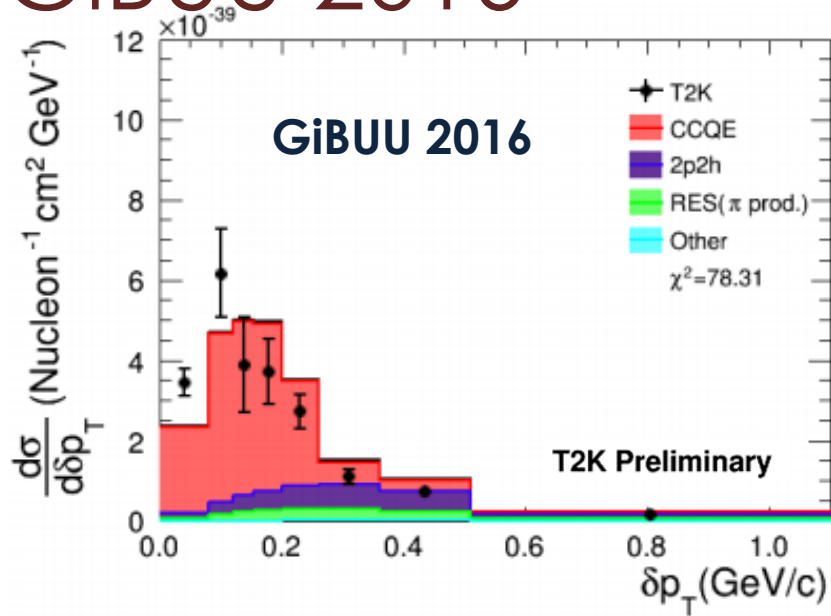
# GENIE RFG w/ BR correction (no RPA)



# NuWro LFG




# GiBUU 2016



# Summary

Lots of interesting model separation!

- **Shape:** idep. of  $M_A^{QE}$  → tells us about:
  - Fermi Motion
  - FSI
  - 2p2h

Characterised by separate STV features
- **Full xsec:** normalisation is sensitive to: nucleon FSI,  $M_A^{QE}$  and RPA
- **Results lift important degeneracies**

# Thank you for listening



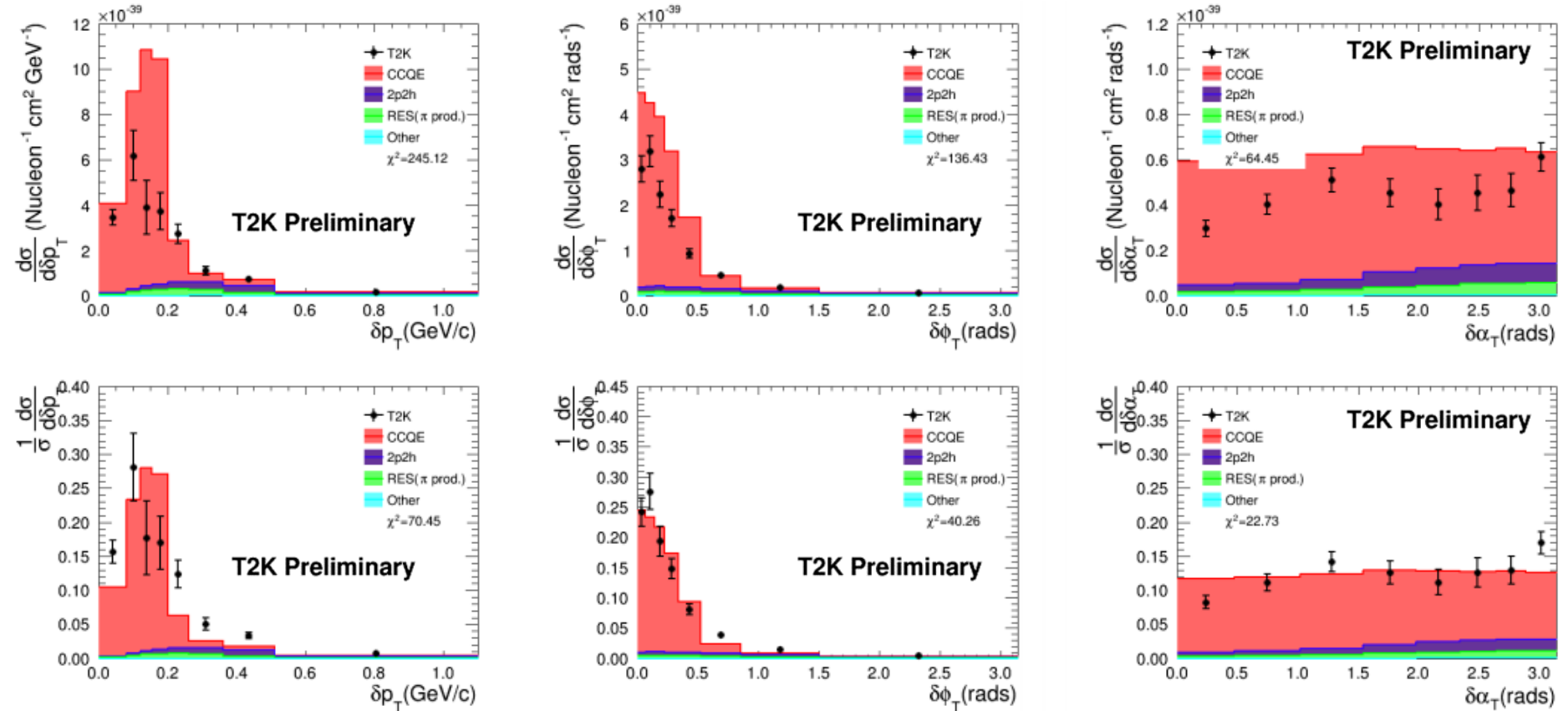


# BACKUPS

# Impact of RPA (relativistic)



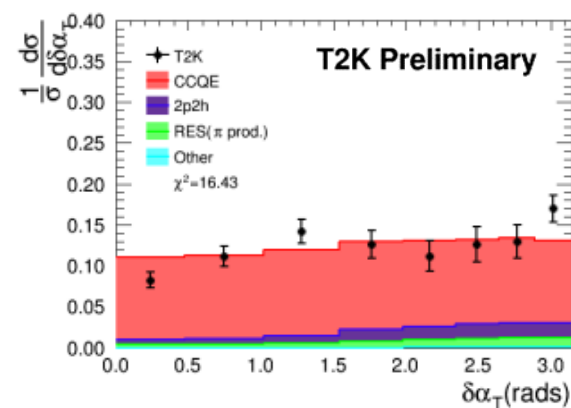
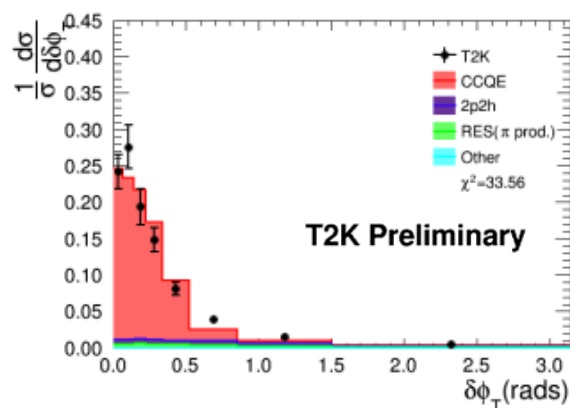
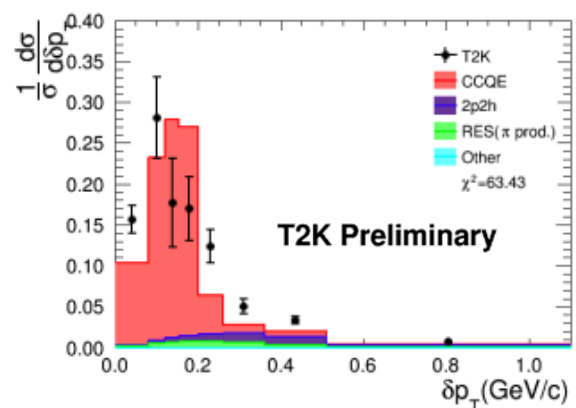
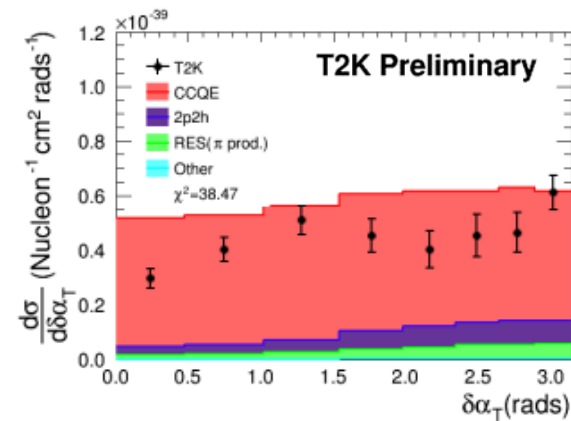
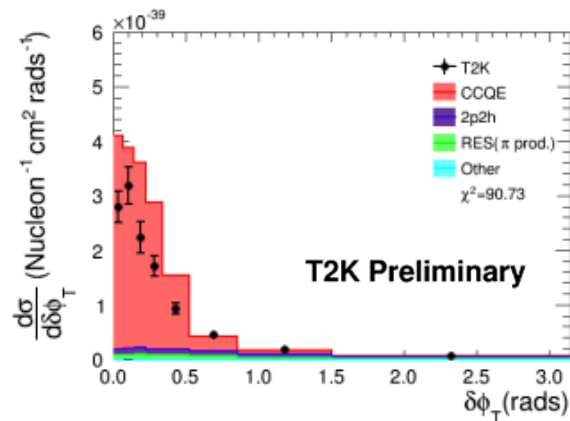
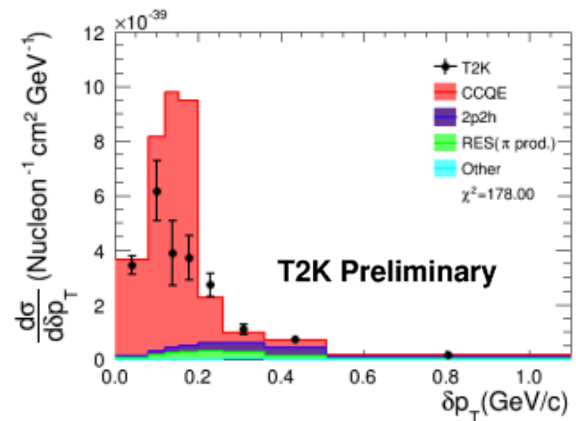
NEUT 5.3.2.2 RFG + RPA (relativistic),  $M_A = 1.03 \text{ GeV}$ , 2p2h is Nieves et. al



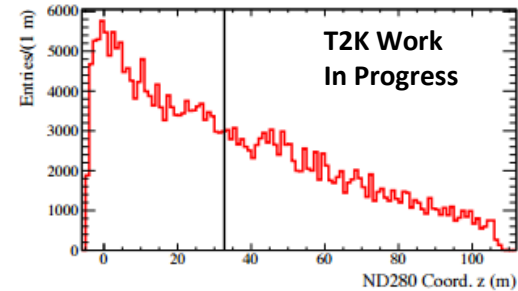
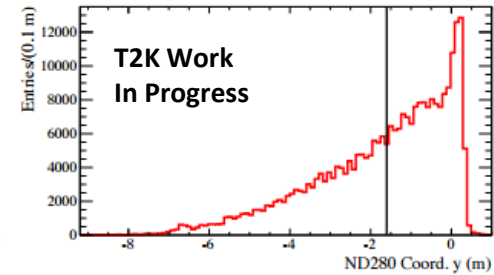
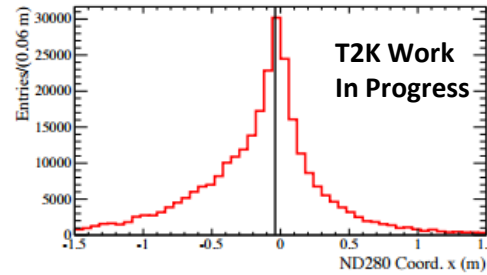
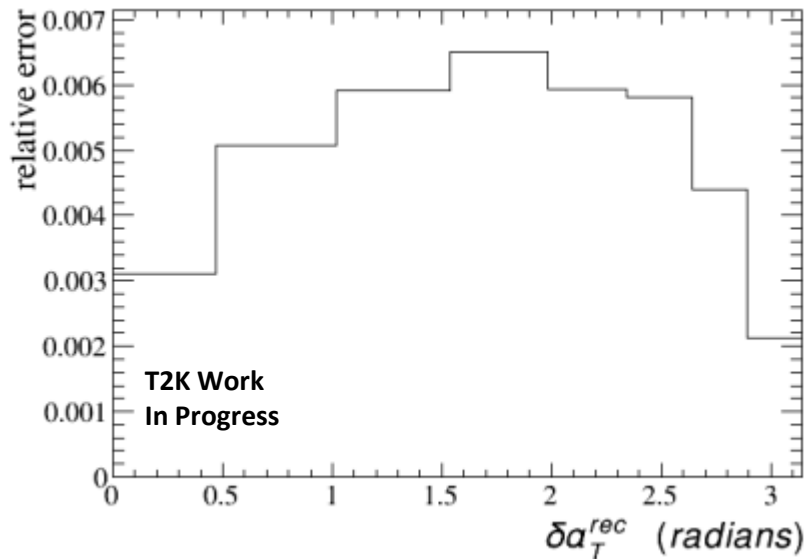
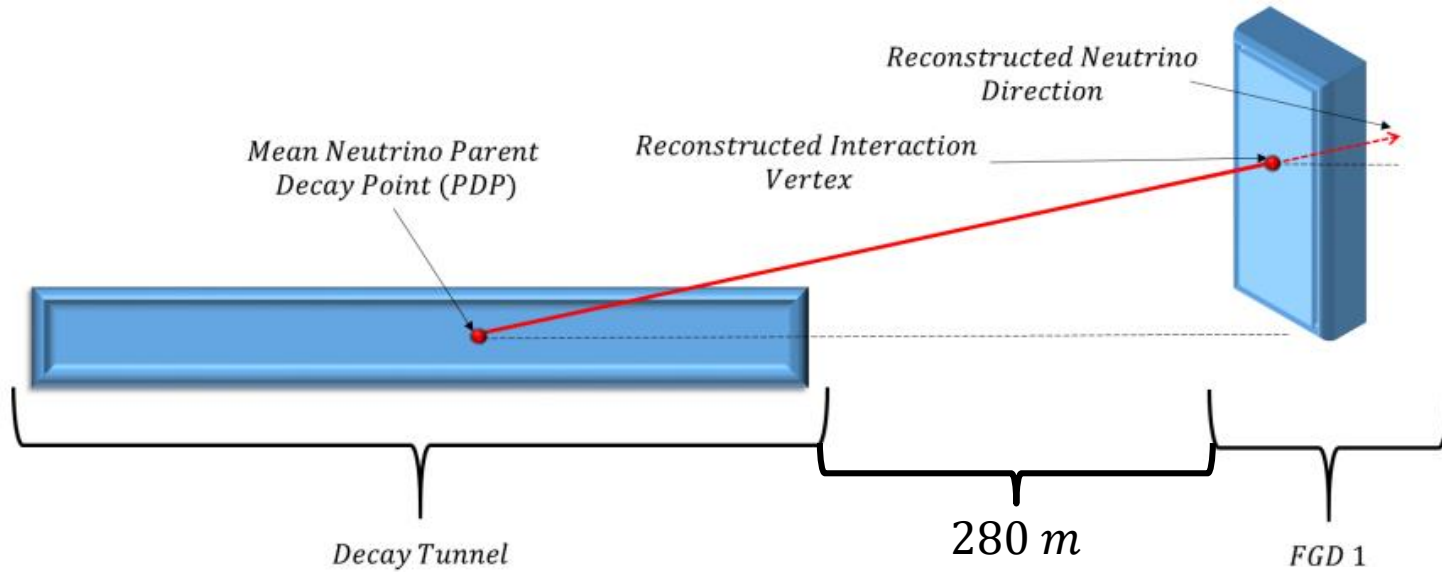
# Impact of RPA (relativistic)



NEUT 5.3.2.2 RFG, no RPA,  $M_A = 1.03 \text{ GeV}$ , 2p2h is Nieves et. al

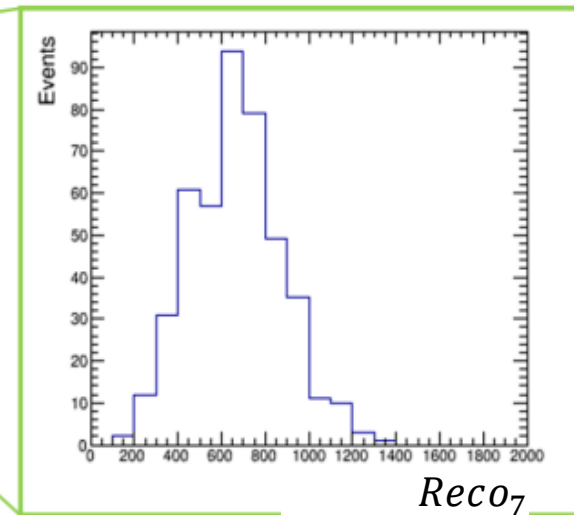
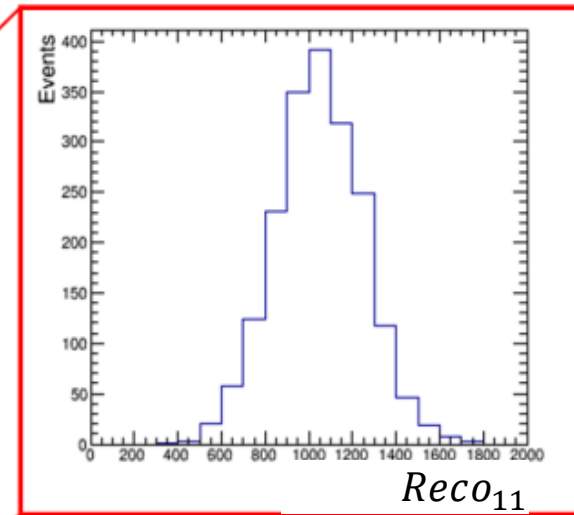
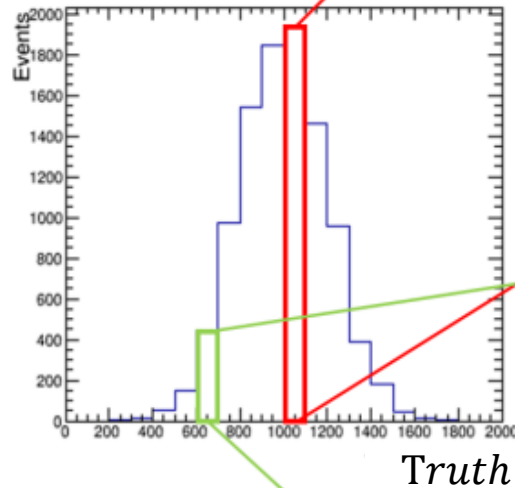


# Reconstructing the Neutrino Direction



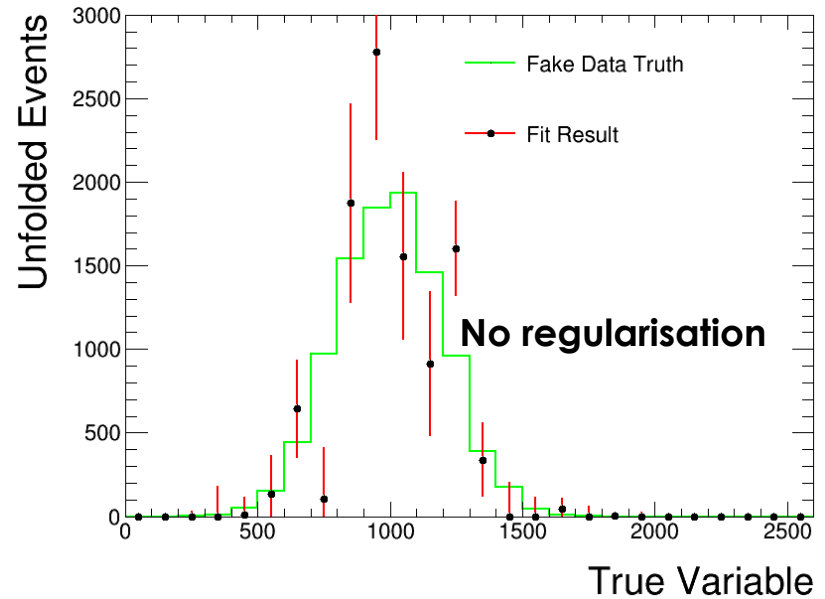
# Binned likelihood fitting

- True bin  $\rightarrow$  Reco. template
- Vary MC template norms ( $c_i$ ) and compare to data
- Maximise Poisson likelihood + syst. penalty term (using max. gradient decent)
- Equivalent to D'Agostini (1995) with infinite iterations



# The ill-posed problem in fit results

- If there is significant smearing between bins  $\rightarrow$  **ill-posed problem** (a typical feature of all unfolding methods)
- Seen as a “zig-zagging” result with **strong anti-correlations** between bins
- Can apply **regularisation** to penalise such results.
- Many ways to regularise, best method depends on the analysis.

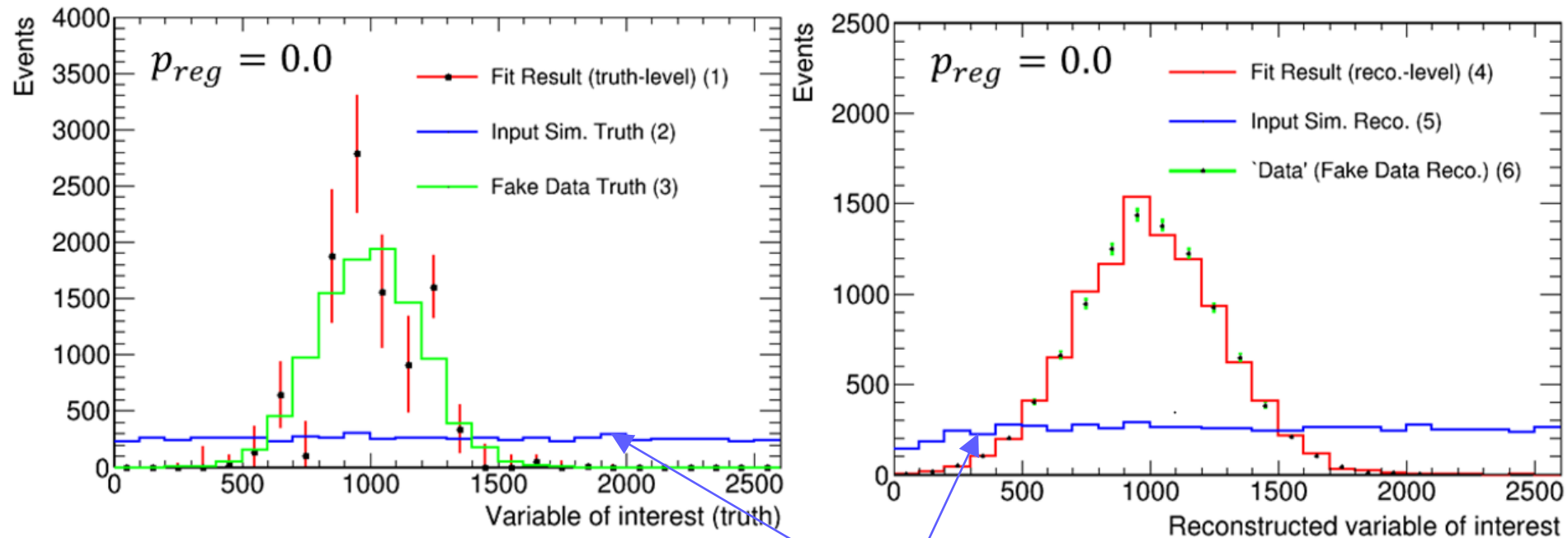


- One option:

$$\chi_{reg}^2 = p_{reg} \sum_i^{truebins-1} (c_i - c_{i+1})^2 = p_{reg} (\vec{c} - \vec{c}_{prior}) (V_{cov}^{reg})^{-1} (\vec{c} - \vec{c}_{prior}).$$

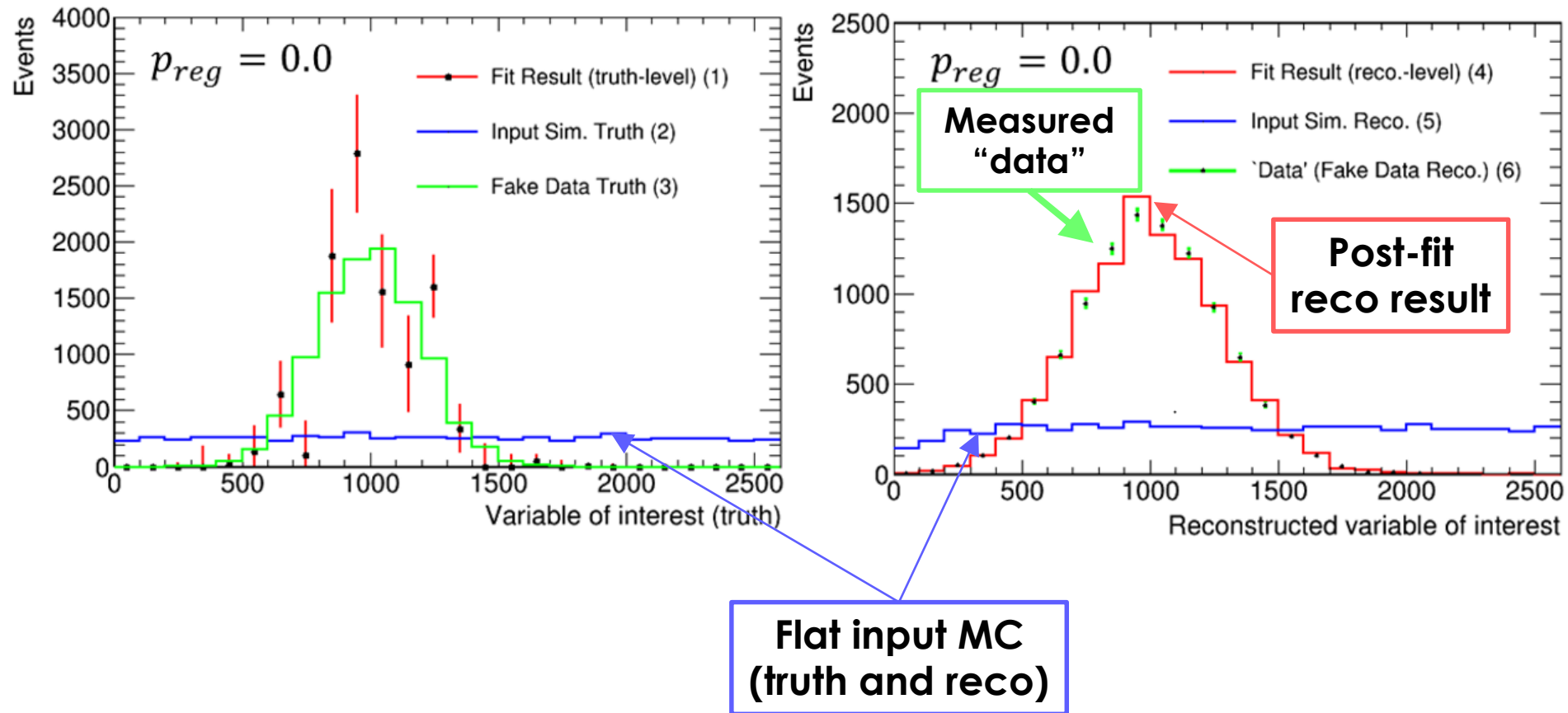
- But note that the **unregularised result is the most correct representation of the truth** (and T2K will provide this!)

# The role of regularisation



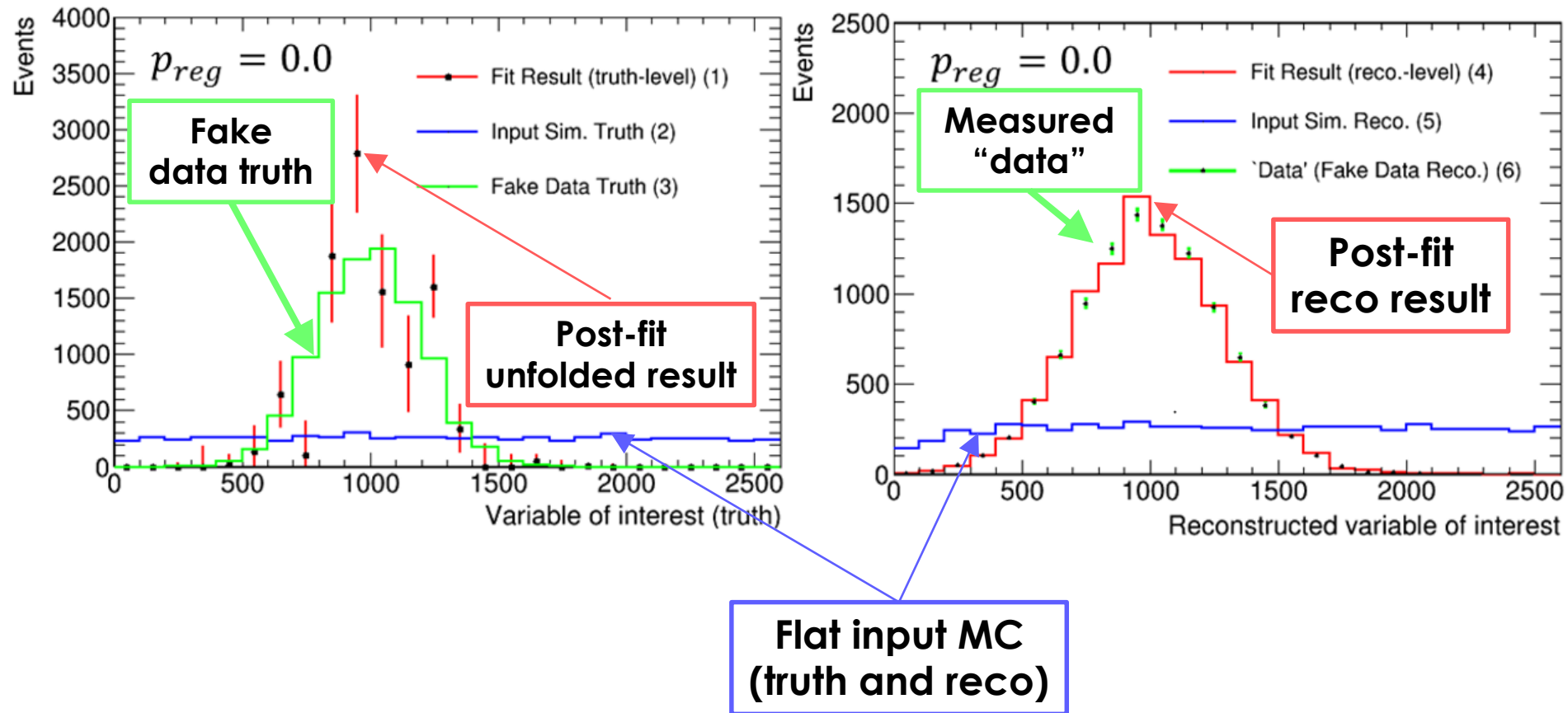
**Flat input MC  
(truth and reco)**

# The role of regularisation

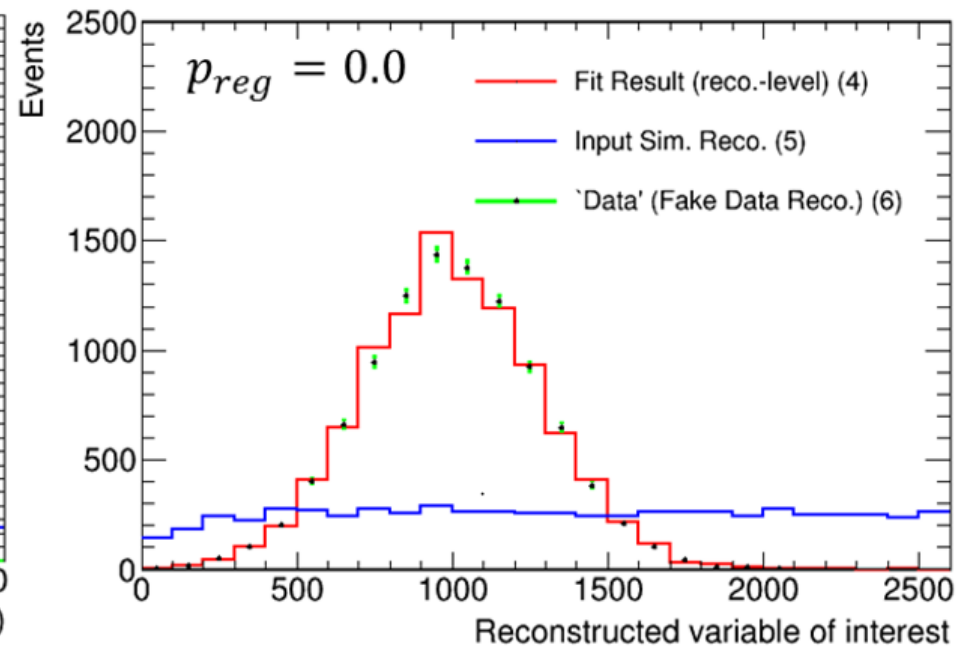
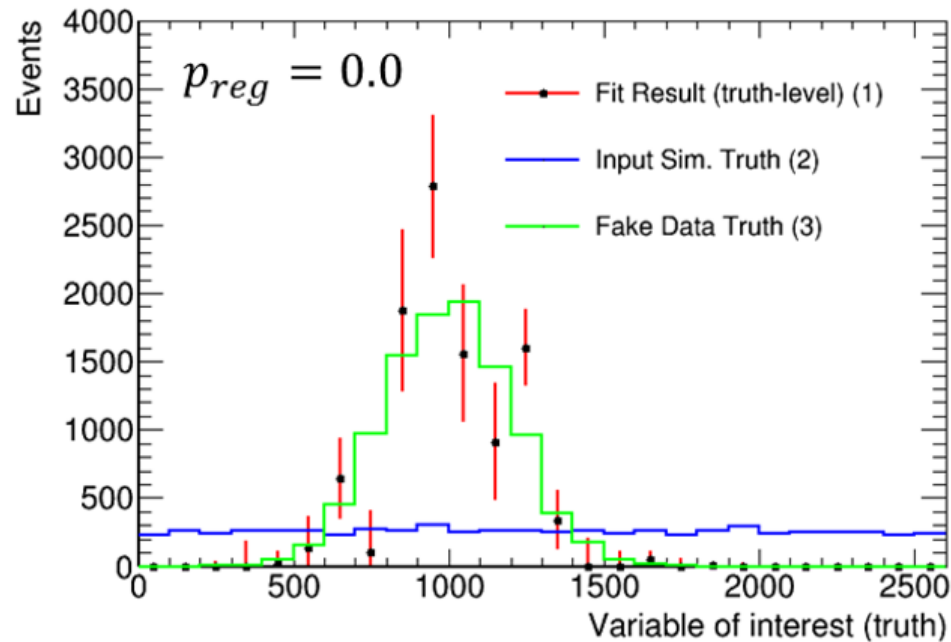




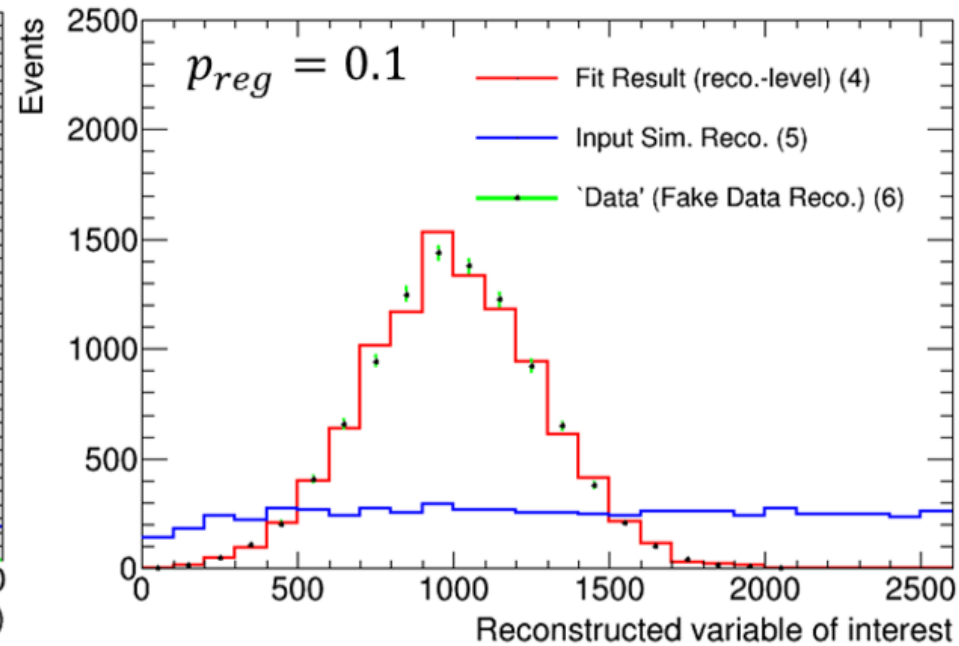
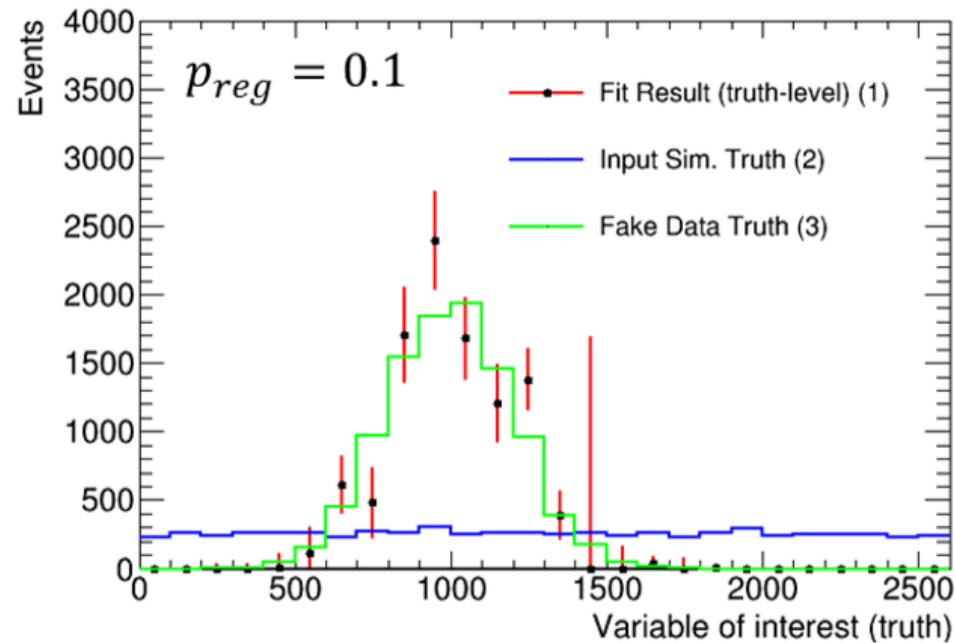
# The role of regularisation



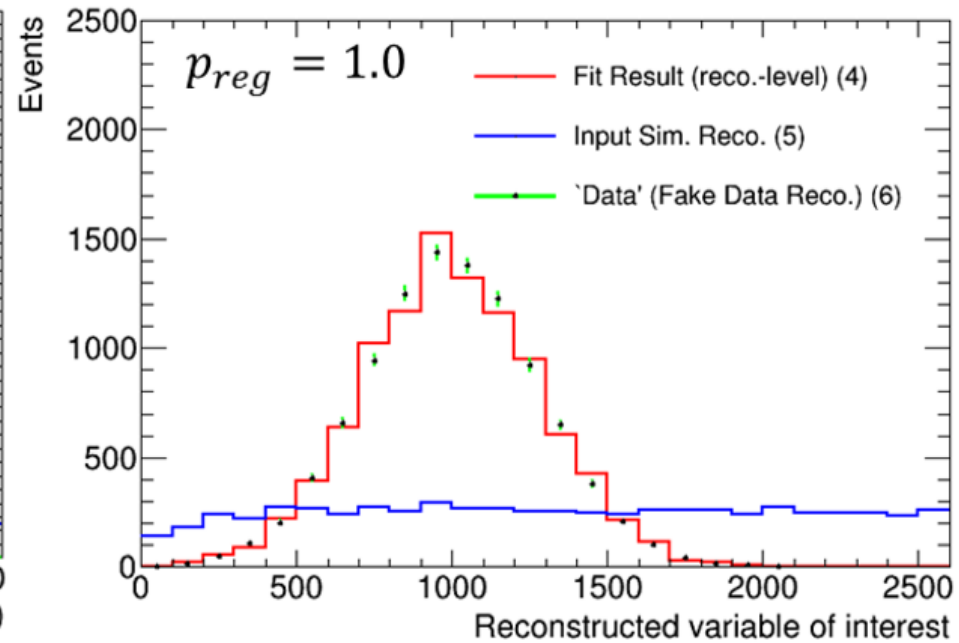
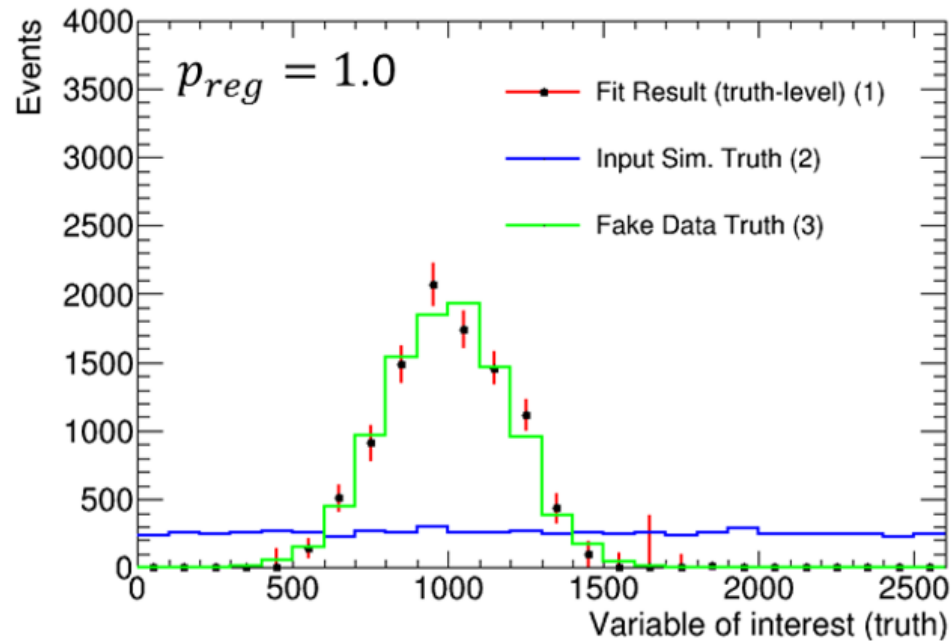
# The role of regularisation



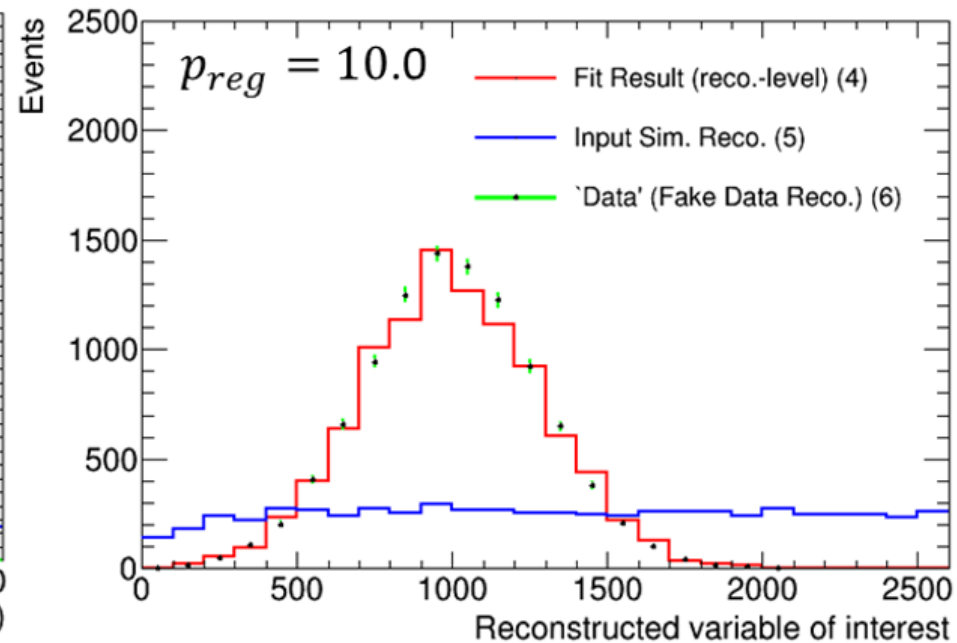
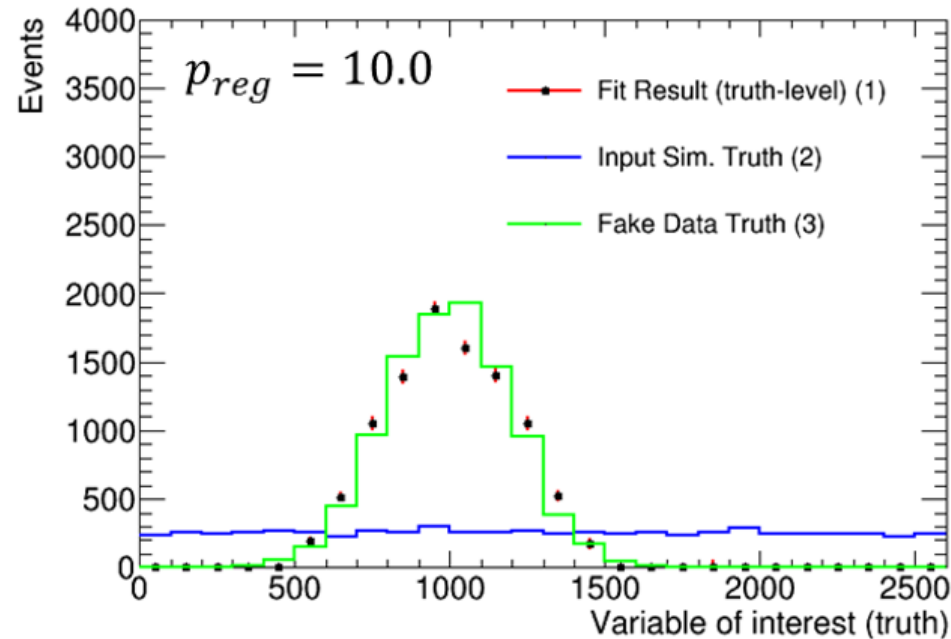
# The role of regularisation



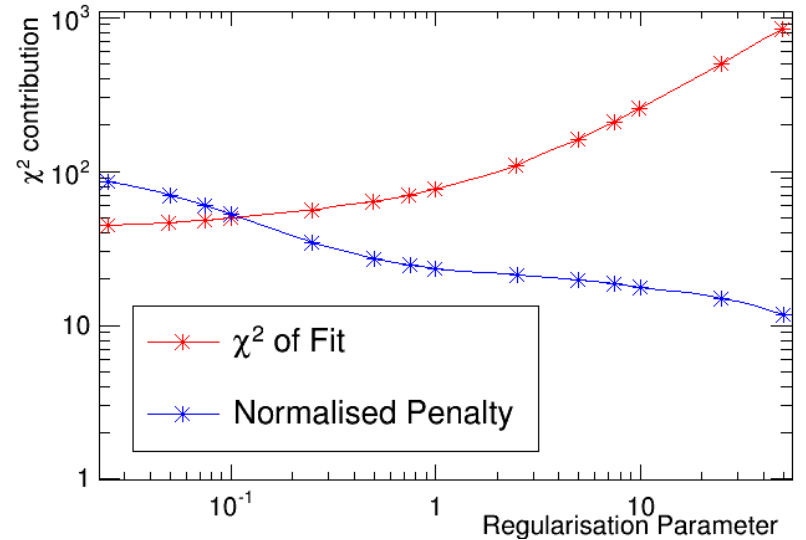
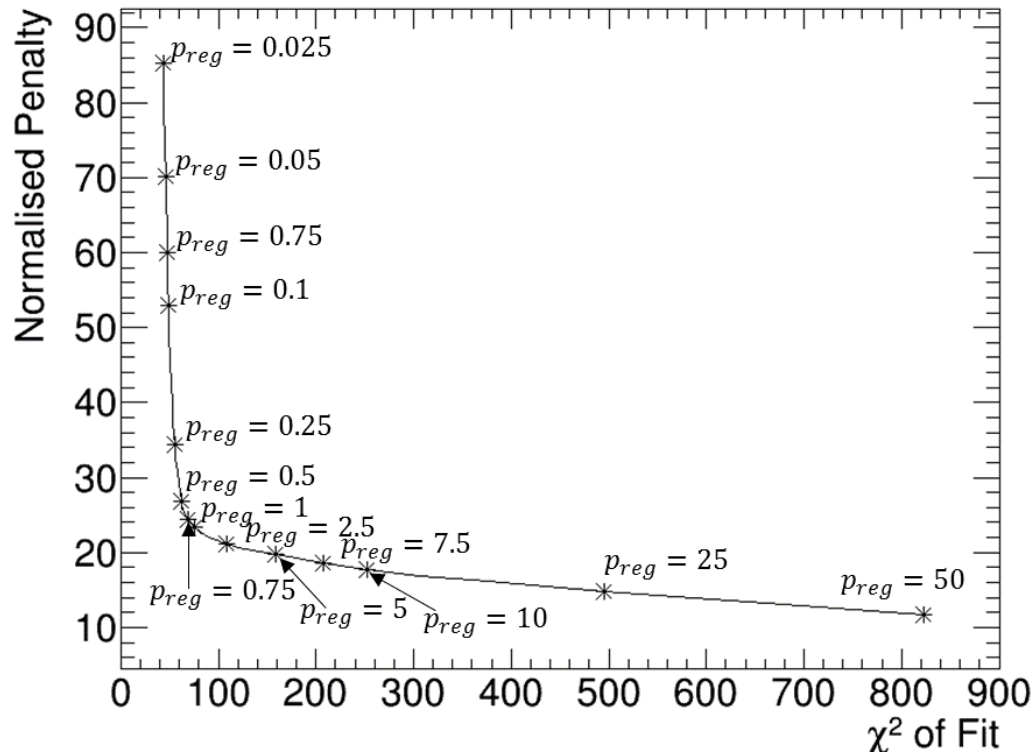
# The role of regularisation



# The role of regularisation



# The role of regularisation



$$\text{Normalised Penalty} = \chi_{reg}^2 / p_{reg}$$

- Best  $p_{reg}$  is the kink of the curve (in this case  $\sim 1$ )
- Balances regulation (in this case smoothness) with bias
- **L-curve can be formed on real data** – data driven regularisation

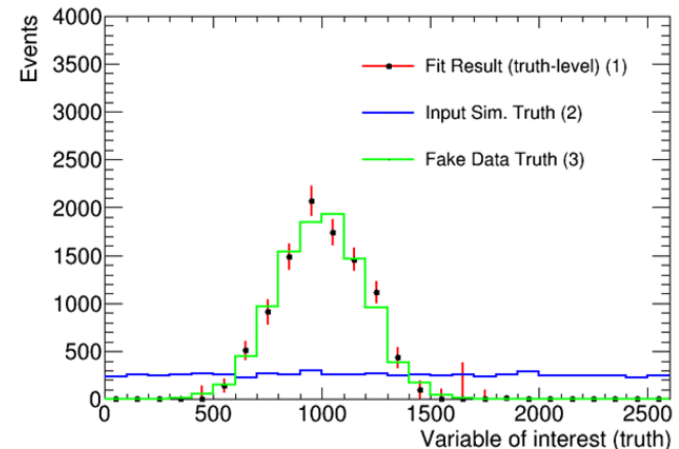
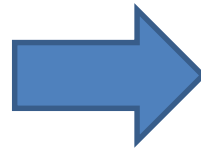
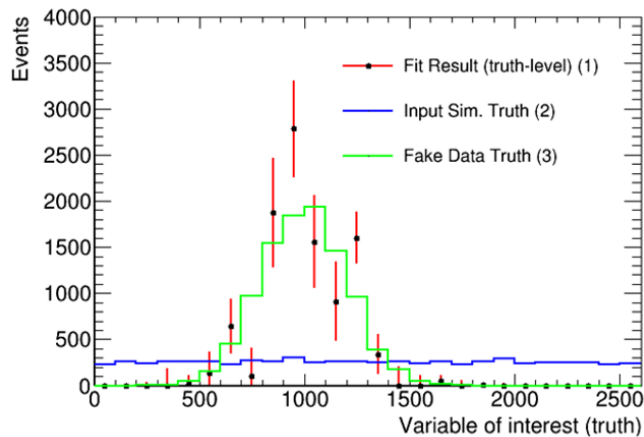
<http://epubs.siam.org/doi/abs/10.1137/1034115>

<http://epubs.siam.org/doi/abs/10.1137/0914086>

<http://arxiv.org/pdf/1205.6201v4.pdf> - use in TUnfold

# Resolving the ill-posed problem

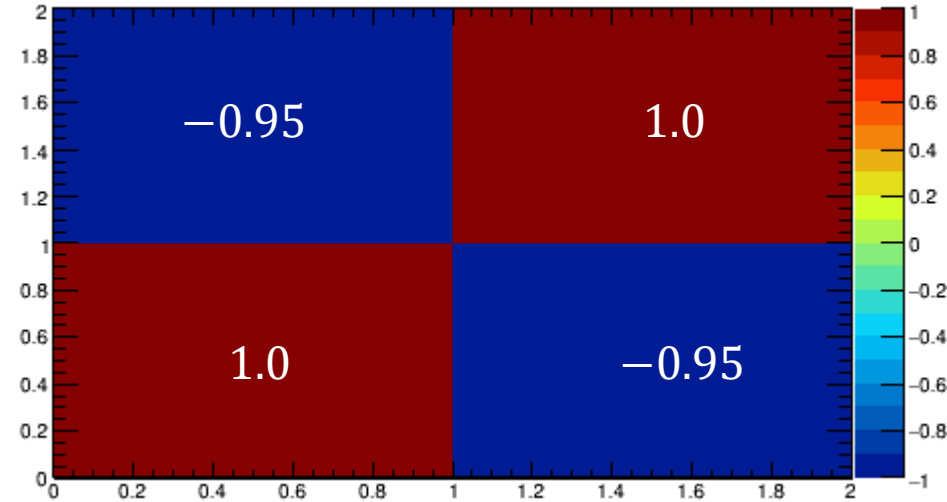
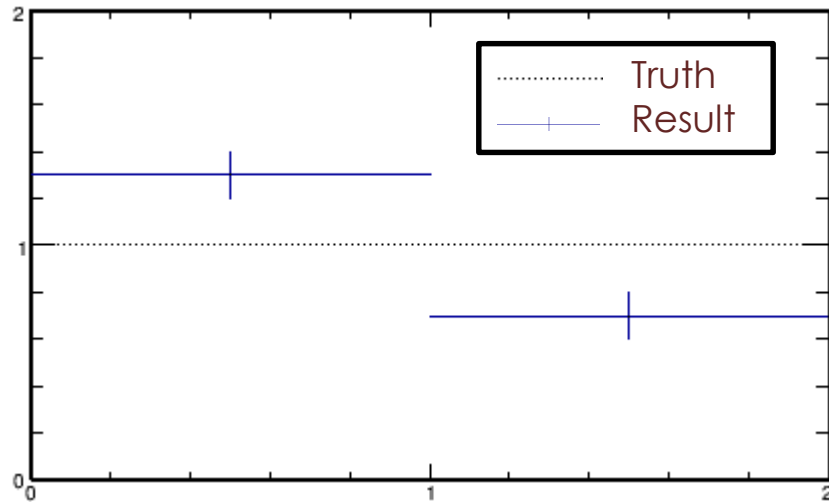
- Unfolding methods mostly differ in the way they resolve these degeneracies (i.e. their **regularisation** implementation)
- Ideally, regularisation should be selecting the “smoothest” of many (almost) degenerate solutions



- **Regularisation always adds some bias**
- The unregularised result is the most “correct” representation of the true unfolded result

# But the unregularised result looks awful!?

- Consider a two bin result:



$$pull_i = \frac{N_{fit} - N_{true}}{Error}$$

$$\left. \begin{aligned} pull_0 &= 3 \\ pull_1 &= 3 \end{aligned} \right\} \text{Fairly awful pull}$$

$$\chi^2 = (\overline{N_{fit}} - \overline{N_{true}})(V_{cov})^{-1}(\overline{N_{fit}} - \overline{N_{true}})$$

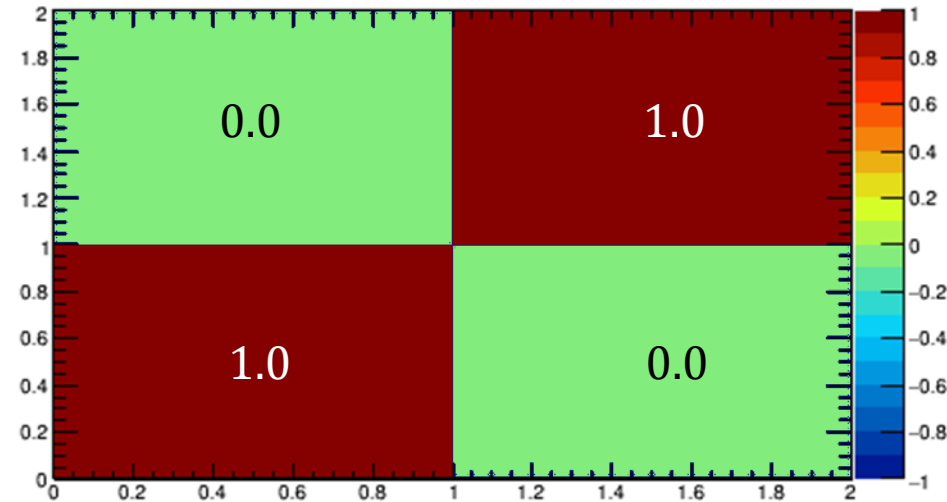
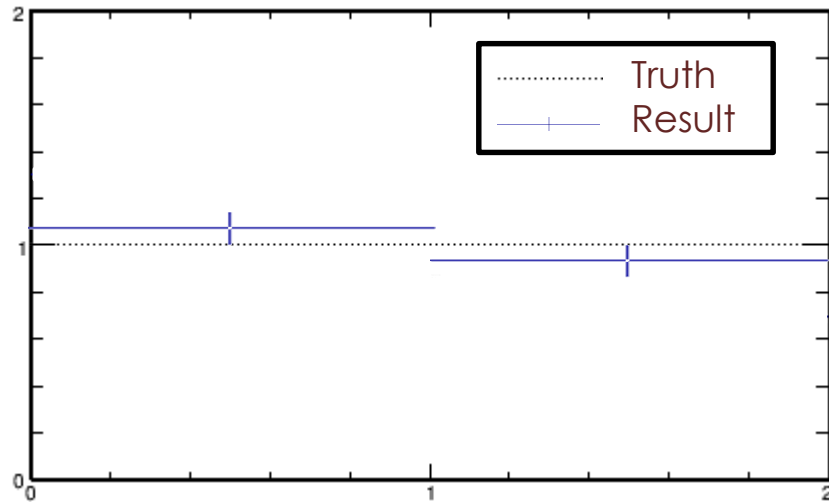
$$\chi^2 = 1.69 \} \text{Good } \chi^2$$

- Need to see the correlation matrix to tell whether the result is good or not.



# But the unregularised result looks awful!?

- Consider a two bin result:



$$pull_i = \frac{N_{fit} - N_{true}}{Error}$$

$$\left. \begin{aligned} pull_0 &= 1 \\ pull_1 &= 1 \end{aligned} \right\} \text{Better pull}$$

$$\chi^2 = (\overline{N_{fit}} - \overline{N_{true}})(V_{cov})^{-1}(\overline{N_{fit}} - \overline{N_{true}})$$

$$\chi^2 = 2.0 \} \text{Worse } \chi^2$$

- Pulls/bin-to-bin bias doesn't tell the whole story