

# FROM SPIN TO STRUCTURE

Beam Spin Asymmetry in Exclusive Pion Electroproduction

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WNPPC 2025

University of Regina

Jefferson Lab KaonLT/PionLT Collaboration



University  
of  
Regina



# Motivation

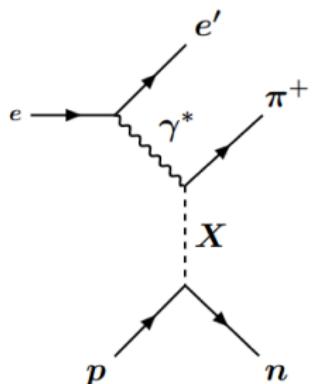
- Many unknowns in theory of **strong force**
- Meson electroproduction in Jefferson Lab Hall C probes **hadron structure**
- Use observables to study **non-perturbative QCD** in the **transition regime**



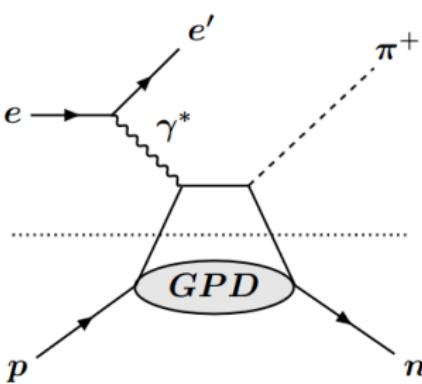


# Theoretical Approaches

(a)



(b)



**Regge:** considers **baryon** and **meson** degrees of freedom

**Generalized Parton Distribution (GPD):** considers **quark** and **gluon** degrees of freedom

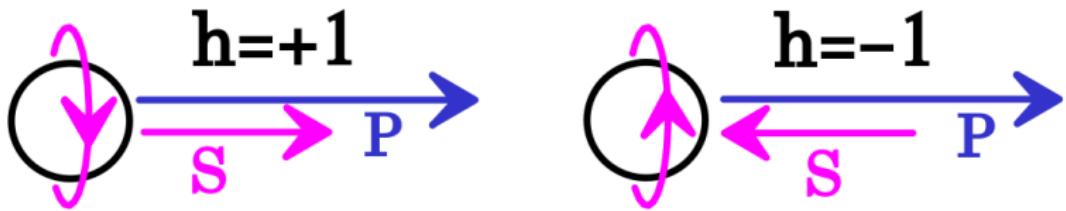
Compare observables to Regge and GPD models  
= test **relevant degrees of freedom** at given kinematics



# Beam Spin Asymmetry

$$A_{LU} = \frac{1}{P} \left( \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} \right)$$

- Difference in cross-sections based on **helicity** ( $\pm 1$ ) of the incident electron

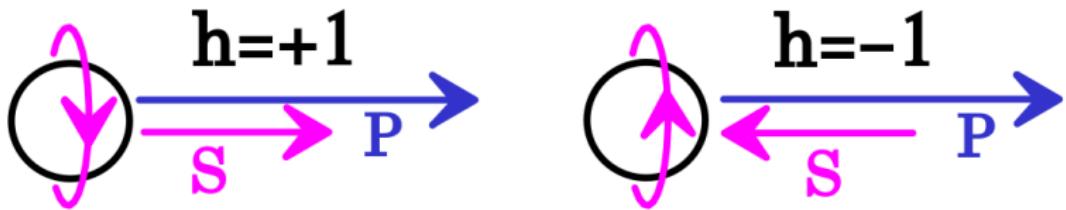




# Beam Spin Asymmetry

$$A_{LU} = \frac{1}{P} \left( \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} \right) \propto \frac{\sigma_{LT'}}{\sigma_0}$$

- Difference in cross-sections based on **helicity** ( $\pm 1$ ) of the incident electron
- Caused by interference between transversely and longitudinally polarized virtual photons  $\gamma^*$





# Beam Spin Asymmetry

$$A_{LU} = \frac{1}{P} \left( \frac{Y^+ - Y^-}{Y^+ + Y^-} \right) \propto \frac{\sigma_{LT'}}{\sigma_0}$$

- Difference in cross-sections based on **helicity** ( $\pm 1$ ) of the incident electron
- Caused by interference between transversely and longitudinally polarized virtual photons
- Acceptances cancel in a ratio

**My research:** asymmetry analysis of the reaction:



Extraction of  $\sigma_{LT'}/\sigma_0$  over a range of kinematics



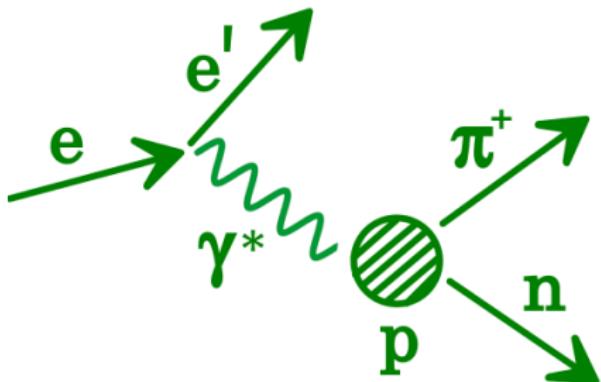
## Some Definitions

$\mathbf{Q}^2$ : 4-momentum of  $\gamma^*$

$x_B$ : momentum fraction of struck parton

$-\mathbf{t}$ : 4-momentum transfer from  $\gamma^*$  to meson

$\epsilon$ : longitudinal to transverse  $\gamma^*$  flux ratio





# Some Definitions

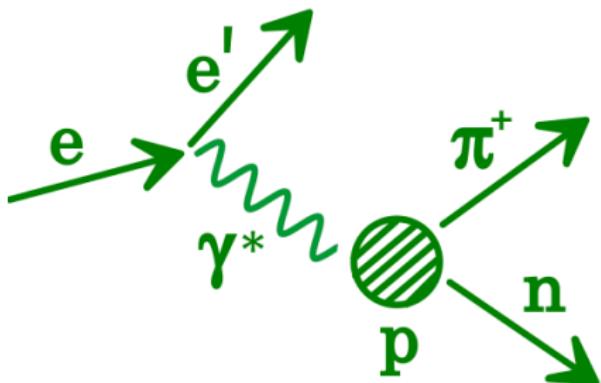
$\mathbf{Q}^2$ : 4-momentum of  $\gamma^*$

$$Q^2 = -(\mathbf{p}_e - \mathbf{p}'_e)^2$$

$x_B$ : momentum fraction of struck parton

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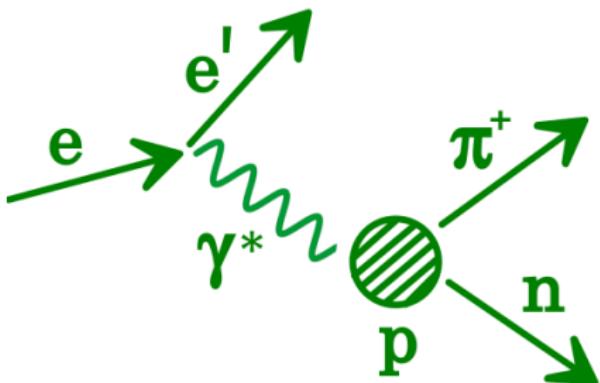
$$Q^2 = -(\mathbf{p}_e - \mathbf{p}'_e)^2$$

$x_B$ : momentum fraction of struck parton

$$x_B = \frac{Q^2}{2\mathbf{p}_p \cdot \mathbf{p}_{\gamma^*}}$$

$-\mathbf{t}$ : 4-momentum transfer from  $\gamma^*$  to meson

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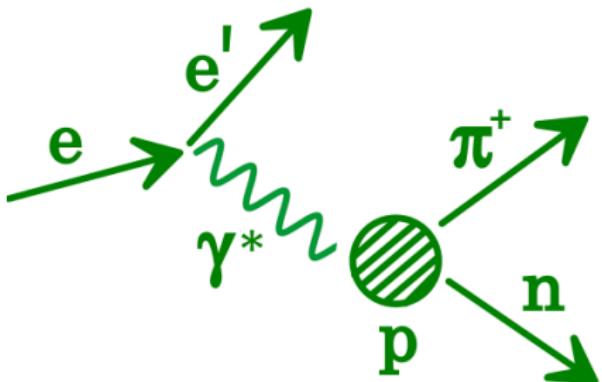
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$$x_B = \frac{Q^2}{2\mathbf{p}_p \cdot \mathbf{p}_{\gamma^*}}$$

$-\mathbf{t}$ : 4-momentum transfer from  $\gamma^*$  to meson

$$-t = -(\mathbf{p}_{\gamma^*} - \mathbf{p}_\pi)^2$$

$\epsilon$ : longitudinal to transverse  $\gamma^*$  flux ratio





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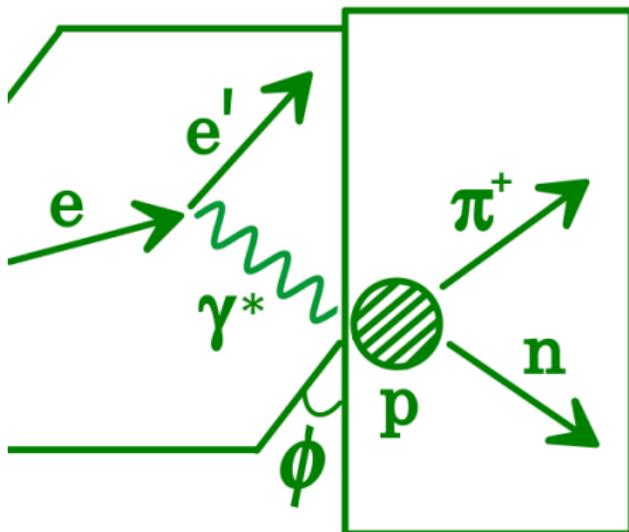
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$-t$ : 4-momentum transfer from  $\gamma^*$  to meson

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# Welcome to Hall C!



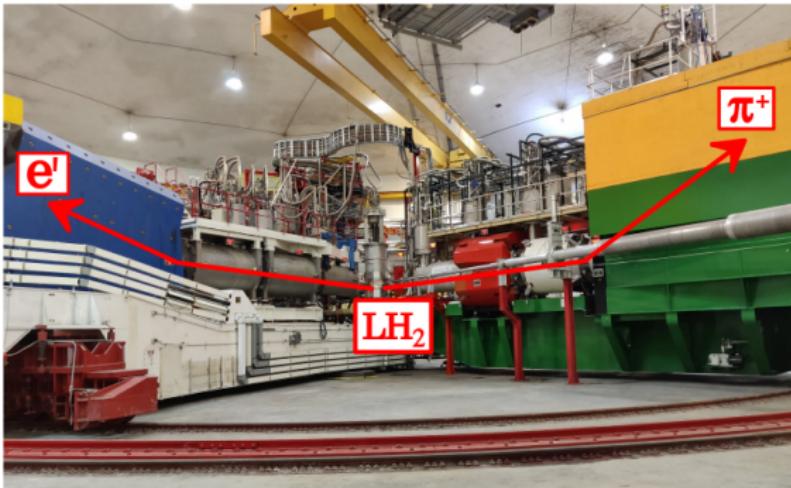
- Hall C: electron beam → fixed target → spectrometers



- Spectrometers are magnetic and moveable → choose charge, momentum, and angles to detect
- Coincidence experiment: need simultaneous detection in **High Momentum Spectrometer** and **Super HMS**



- Hall C: electron beam → fixed target → spectrometers

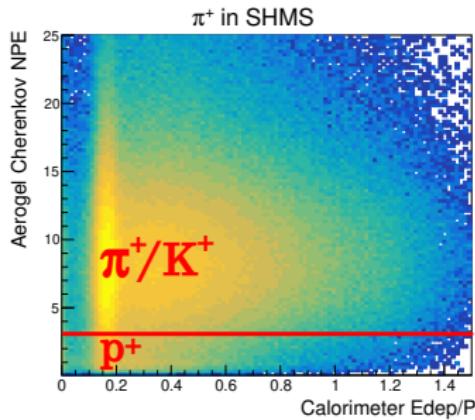
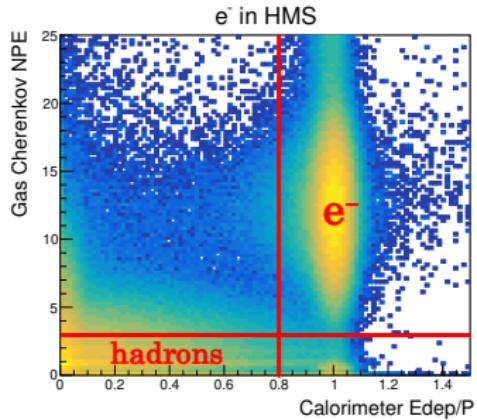


- Spectrometers are magnetic and moveable → choose charge, momentum, and angles to detect
- Coincidence experiment: need simultaneous detection in **High Momentum Spectrometer** and **Super HMS**

# Particle Identification (PID)



- Spectrometer detector stack contains **drift chambers** for **tracking**, **hodoscopes** for **triggering**, **threshold Cherenkovs** and **calorimeter** for **PID**
- Fixed charge, momentum: PID via **mass separation**
  - Choose index of refraction to distinguish between particles





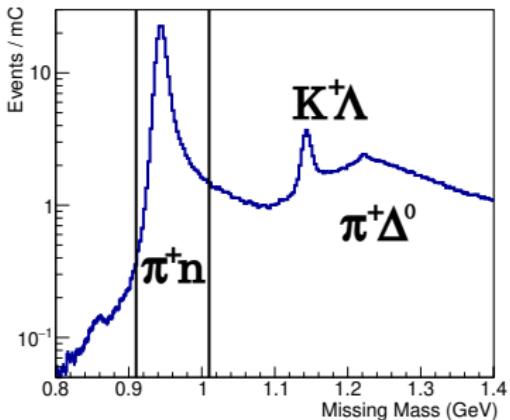
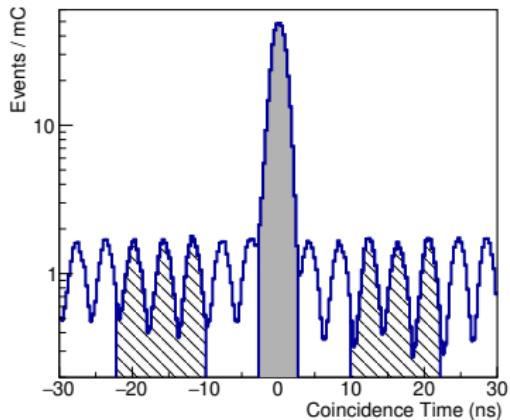
# Event Selection



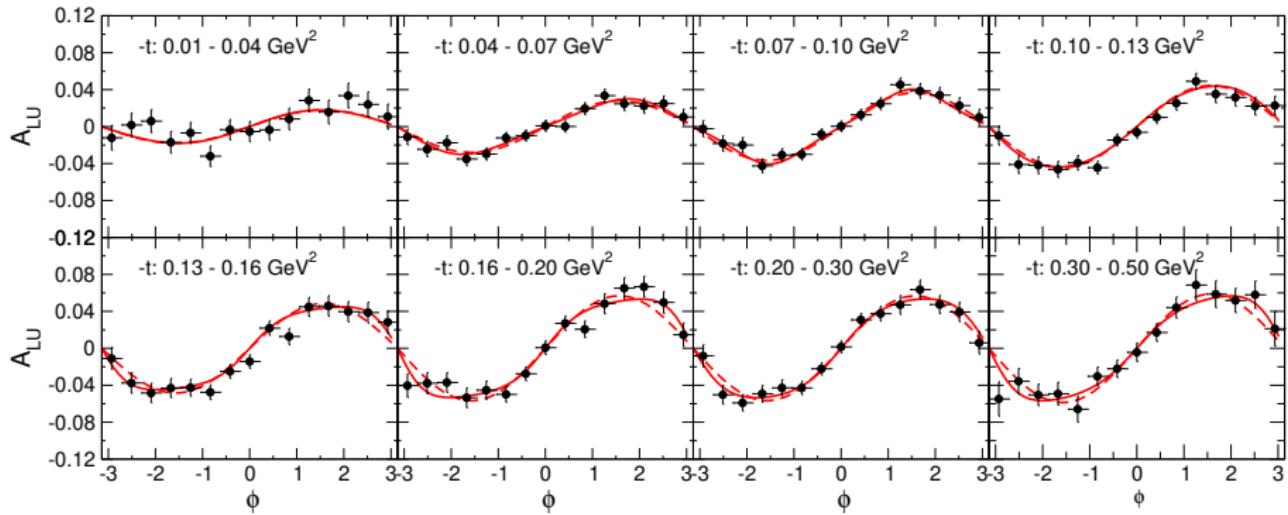
- Select coincidences via  $t_{COIN} = t_{HMS} - t_{SHMS} \approx 0$
- Neutron not detected  $\rightarrow$  use missing mass  $m_X \approx m_N$

$$m_X^2 = (\mathbf{p}_e + m_p - \mathbf{p}_{e'} - \mathbf{p}_\pi)^2$$

- Subtract random time sample, empty target background



# Asymmetry $Q^2=2.1 \text{ GeV}^2$ , $x_B=0.21$

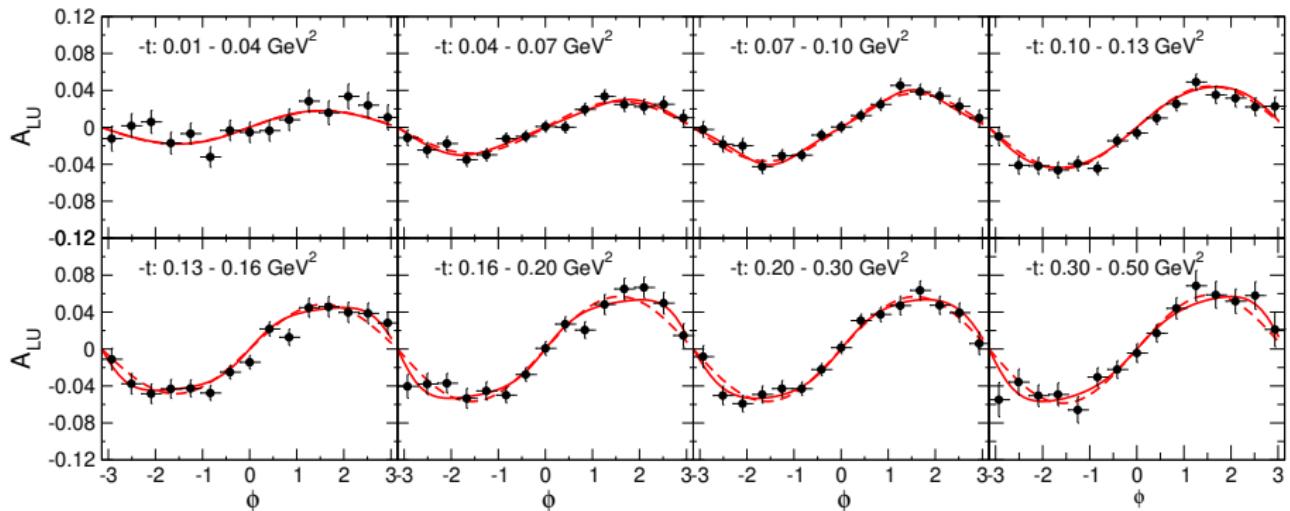


$$A_{LU} = \frac{1}{P} \left( \frac{Y^+ - Y^-}{Y^+ + Y^-} \right)$$

$$\delta_{\text{stat}} = \frac{2}{P} \sqrt{\frac{Y^+ Y^-}{(Y^+ + Y^-)^3}}$$



# Asymmetry $Q^2=2.1 \text{ GeV}^2$ , $x_B=0.21$



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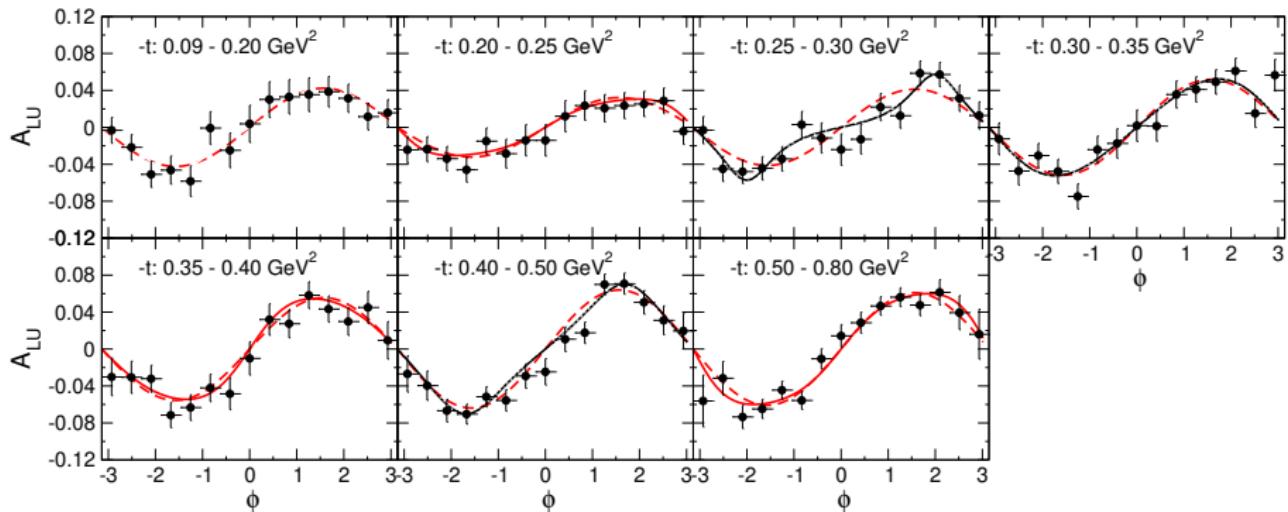
$$A_{LU} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos \phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

---

$$A_{LU} = \sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi \quad (\text{approx.})$$



# Asymmetry $Q^2 = 3.0 \text{ GeV}^2$ , $x_B = 0.40$



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$$A_{LU} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos \phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

---

$$A_{LU} = \sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi \quad (\text{approx.})$$



# Systematic Errors

## 1. Fitting Error

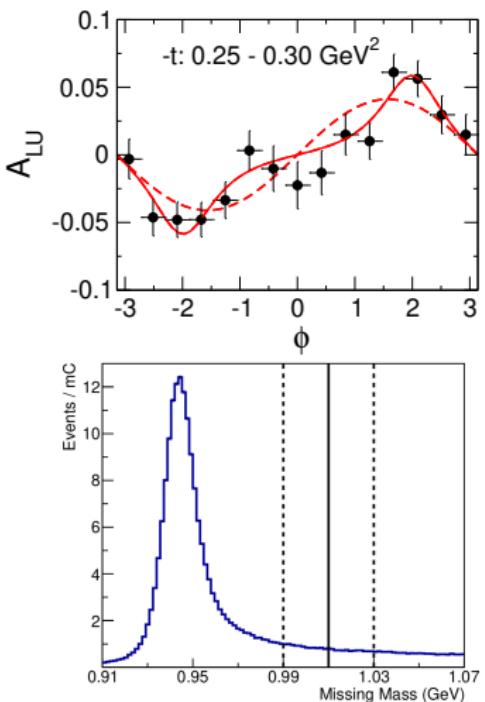
- Difference in  $\sigma_{LT'}/\sigma_0$  extracted using **full** (solid line) or **approximated** (dashed) fit
- Has a direction → total systematic error **asymmetric**

## 2. Cut Dependence

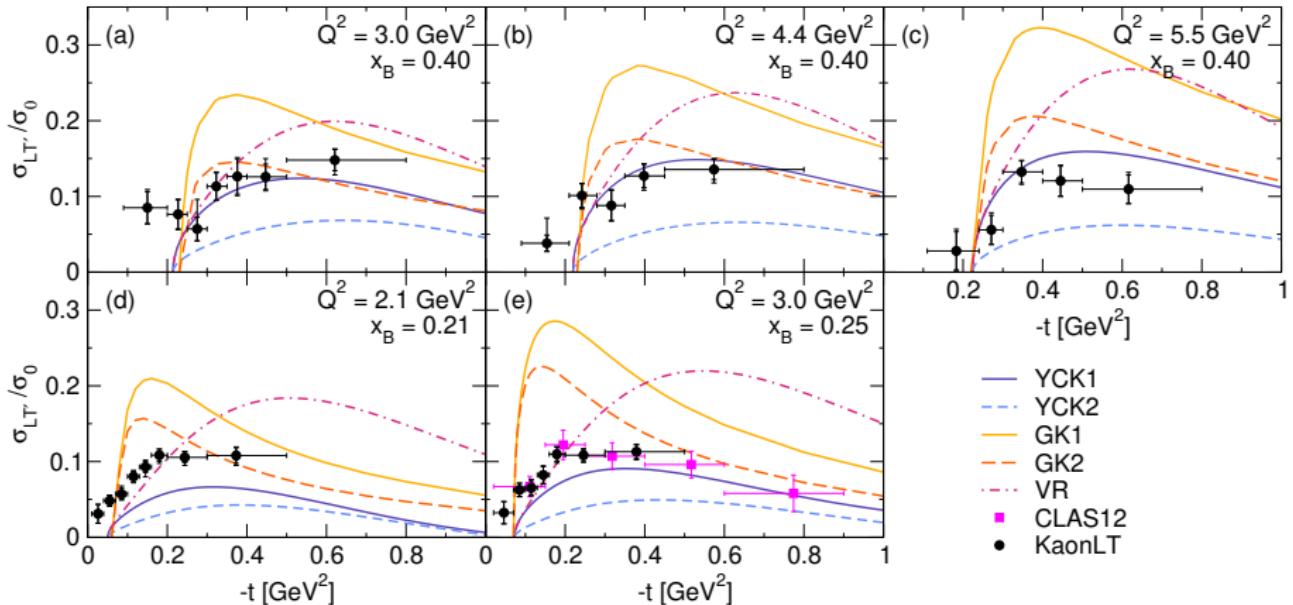
- $\sigma_{LT'}/\sigma_0$  varies with exact values of **missing mass** and **coincidence time** cuts

## 3. Beam Polarization

- $P = 89^{+1}_{-3}\%$  → Propagate to  $\sigma_{LT'}/\sigma_0$



# Results



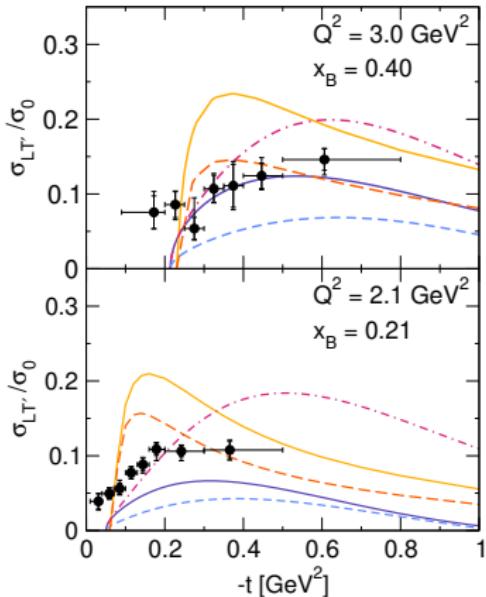
S.V. Goloskokov, P. Kroll, Eur. Phys. J. C **65** 137 (2010).

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T. Vrancx, J. Ryckebusch & J. Nys, Phys. Rev C, **89** 065202 (2014). S. Diehl et al., Phys. Lett. B **839**, 137761 (2023).

T. K. Choi, K.-J. Kong & B.-G. Yu, J. Korean Phys. Soc. **67**, 1089-1094 (2015).

# Comparison with Theory



**GK1 (GPD)**: Overestimates magnitude

**GK2 (GPD,  $H_T^* \cdot 2$ )**: Comparable magnitude, overall shape still different

**VR (Regge)**: Good agreement at low  $-t$ , poor agreement for higher  $-t$

**YCK1 (Regge + GPD EMFF)**: Decent reproduction of magnitude and shape

**YCK2 (Regge + dipole EMFF)**: Underestimates magnitude

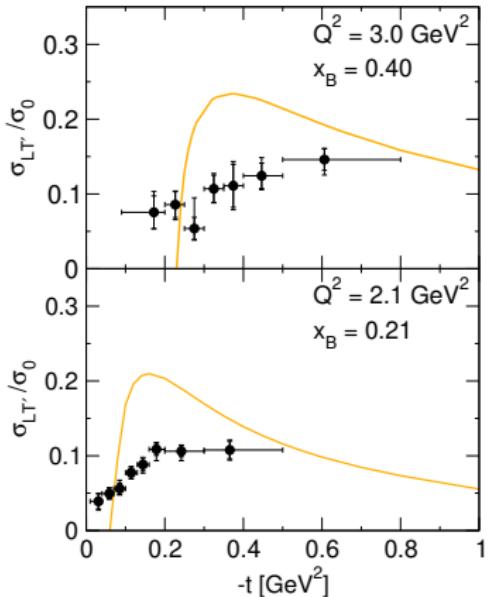
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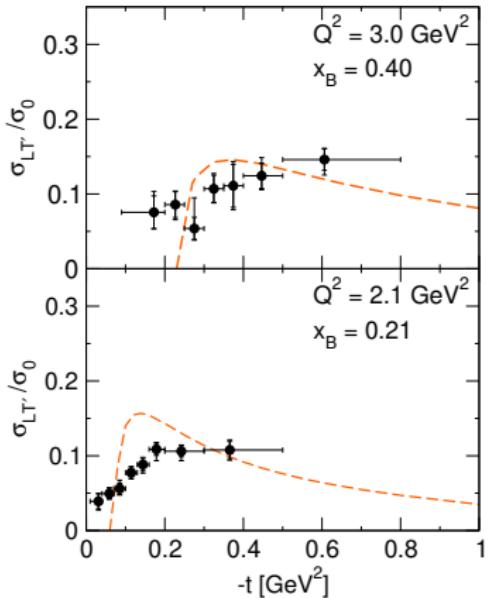
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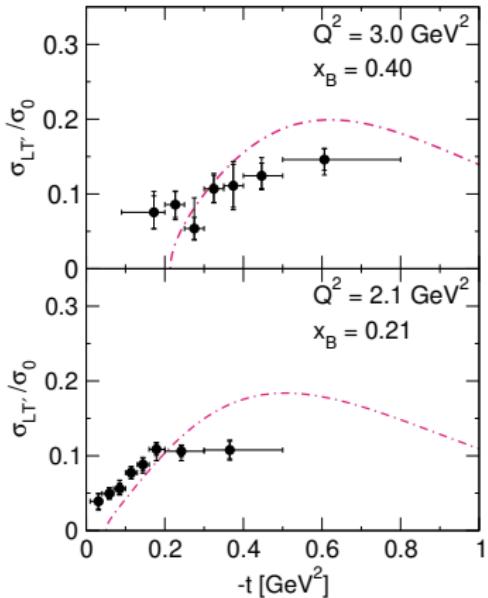
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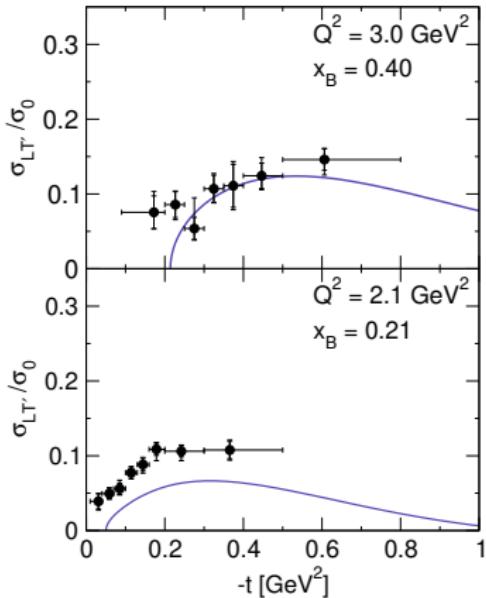
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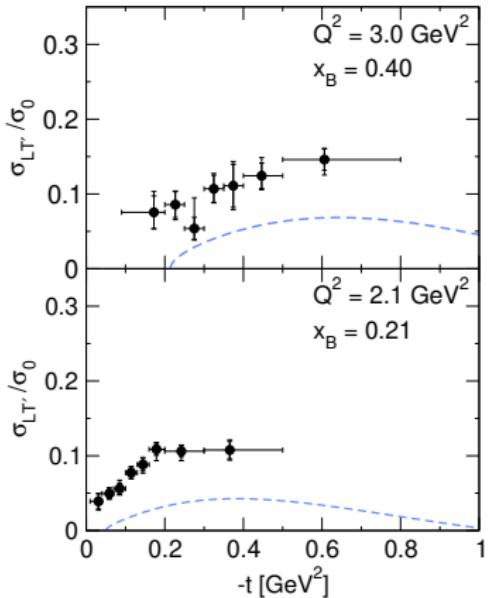
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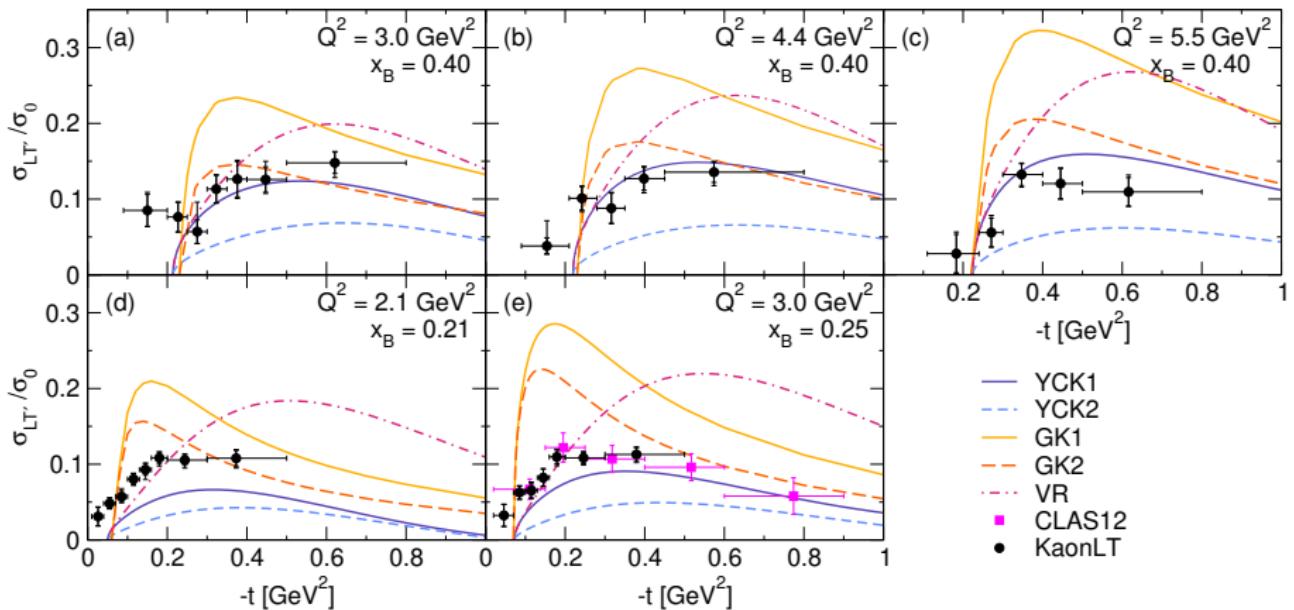
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B. Berthou et al, Eur. Phys. J. C **78** 478 (2018).

T. Vrancx, J. Ryckebusch & J. Nys, Phys. Rev C, **89** 065202 (2014).

T. K. Choi, K.-J. Kong & B.-G. Yu, J. Korean Phys. Soc. **67**, 1089-1094 (2015).

# Comparison with Theory (2)



Best overall agreement is **YCK1**: Regge model with GPD parametrization of nucleon electromagnetic form factors (EMFFs)

S.V. Goloskokov, P. Kroll, Eur. Phys. J. C **65** 137 (2010).

T. Vrancx, J. Ryckebusch & J. Nys, Phys. Rev C, **89** 065202 (2014).

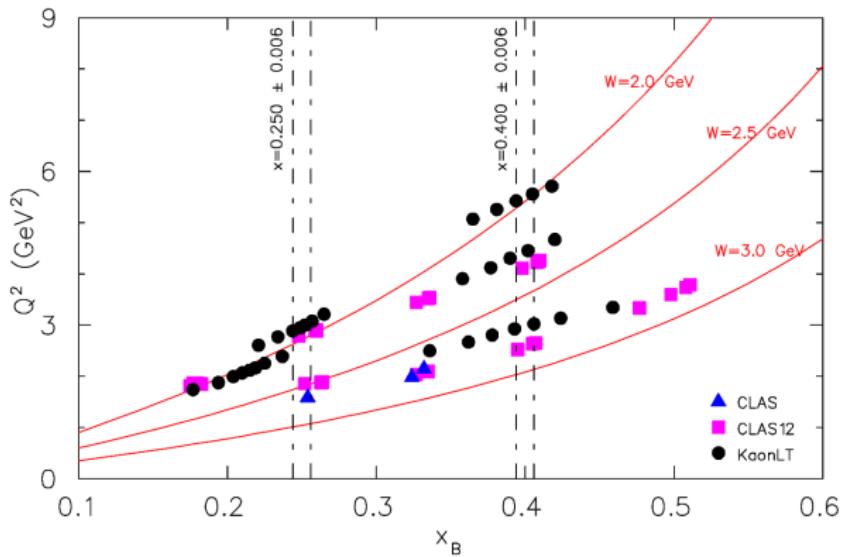
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S. Diehl et al., Phys. Lett. B **839**, 137761 (2023).

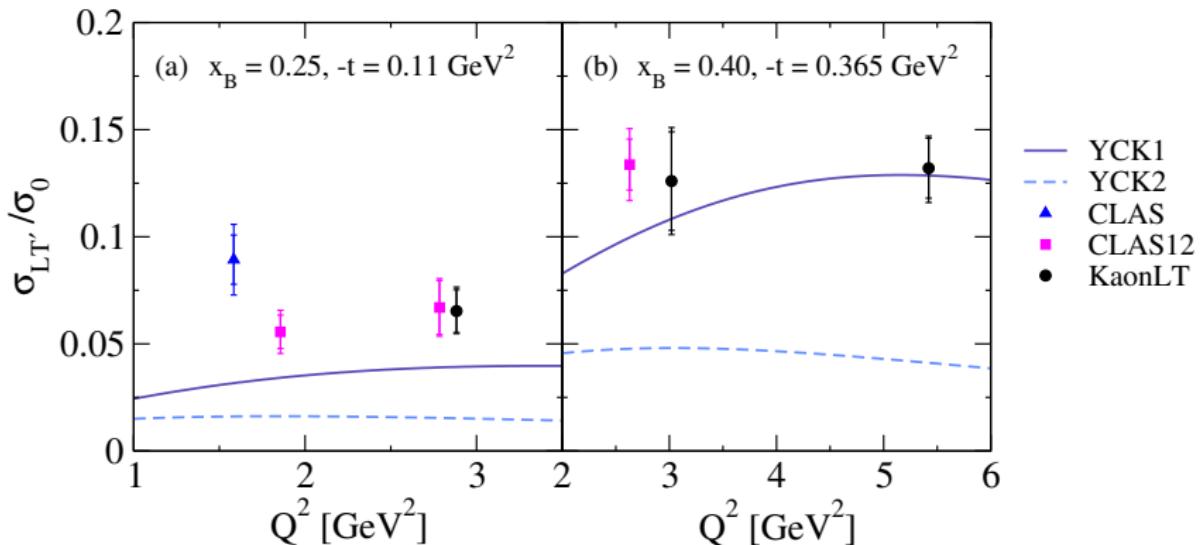
# $Q^2$ Scan

- Measurements of  $\sigma_{LT'}/\sigma_0$  from **KaonLT**, **CLAS**, and **CLAS12**
- **KaonLT** data extends kinematic range with finer  $t$ -binning
- Combine to determine  **$Q^2$  dependence** at fixed  $(x_B, -t)$





# $Q^2$ Dependence (New!)



- $\sigma_{LT'}/\sigma_0$  from **KaonLT**, **CLAS**, and **CLAS12** as a function of  $Q^2$
- Flat or weak  $Q^2$  dependence

S. Diehl et al., Phys. Lett. B **839**, 137761 (2023).

T. K. Choi, K.-J. Kong & B.-G. Yu, J. Korean Phys. Soc. **67**, 1089-1094 (2015).

S. Diehl et al., Phys. Rev. Lett. **125**, 182001 (2020).



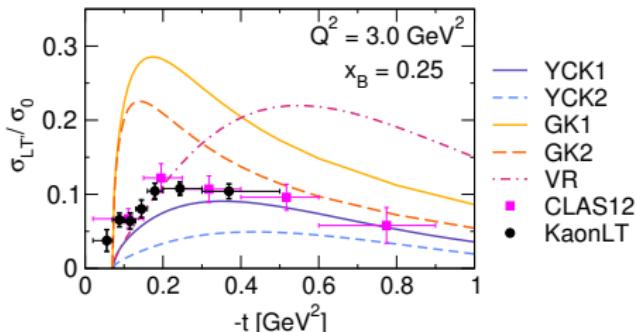
**CLAS12** conclusions: best fit is

**GK2 (GPD  $H_T^*{}^2$ )**

→ GPD picture applicable

**KaonLT** conclusions: best fit is

**YCK1 (Regge + GPD EMFF)**



- Our measured  $\sigma_{LT'}/\sigma_0$  is not explained by only quark and gluon degrees of freedom
- Hadronic degrees of freedom may be more relevant
- **YCK1** uses GPDs in EMFF parametrization → hybrid approach?
- ★ Need model-independent tests of GPD picture (*see next talk*)

S.V. Goloskokov, P. Kroll, Eur. Phys. J. C **65** 137 (2010).

B. Berthou et al, Eur. Phys. J. C **78** 478 (2018).

T. Vrancx, J. Ryckebusch & J. Nys, Phys. Rev C, **89** 065202 (2014). S. Diehl et al., Phys. Lett. B **839**, 137761 (2023).

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## Summary and Conclusions

- Measured  $A_{LU}$  in  $e + p \rightarrow e' + \pi^+ + n$  and extracted  $\sigma_{LT'}/\sigma_0$  from KaonLT data over range of kinematics
- No exact agreement with predictions, closest is **YCK1 (Regge + GPD EMFF)**
- Flat or weak  $Q^2$  dependence of  $\sigma_{LT'}/\sigma_0$
- *Manuscript being prepared for Physics Letters B*

Precision data of hadronic reaction observables critical for proton structure and the strong force!



# Acknowledgements

## KaonLT/PionLT Collaboration:

Dave Gaskell\*, Nathan Heinrich,  
Garth Huber\*, Tanja Horn\*,  
Muhammad Junaid, Stephen Kay,  
Vijay Kumar, Pete Markowitz\*,  
Alicia Postuma, Julie Roche,  
Richard Trotta, Ali Usman

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*NSERC SAPIN-2021-00026*

*NSF PHY 2309976, 2012430, 1714133*

*NSF PHY 2209199*



**NSERC  
CRSNG**



**Canadian Institute of  
Nuclear Physics**  
**Institut canadien de  
physique nucléaire**

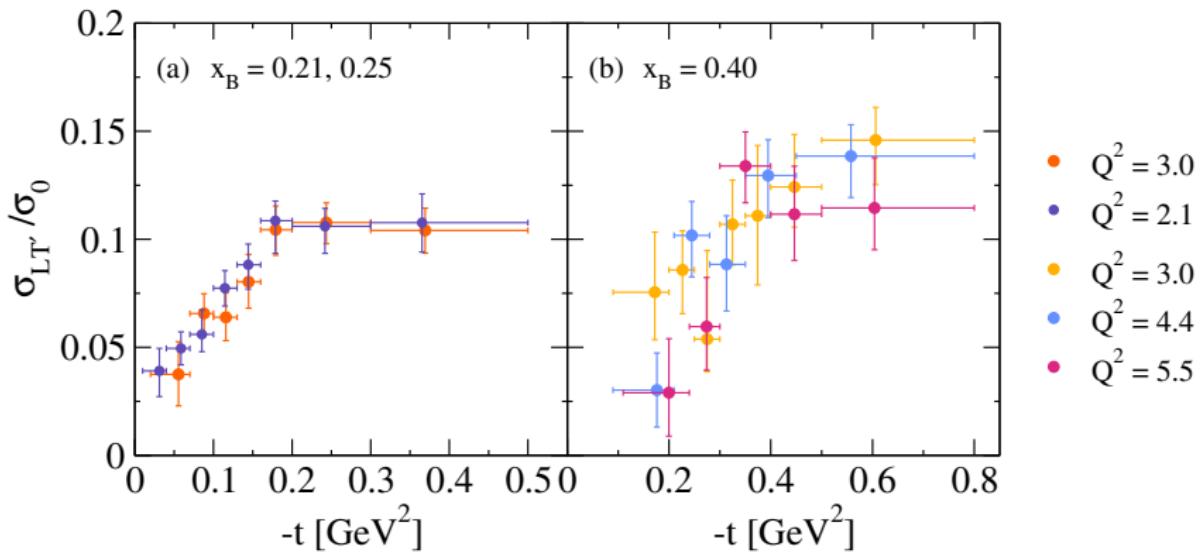


This research was carried out at the University of Regina, on what is Treaty 4 land and the territories of the nêhiyawak, Anishinabé, Dakota, Lakota, Nakoda, and the Métis/Michif Nation.

# EXTRA SLIDES



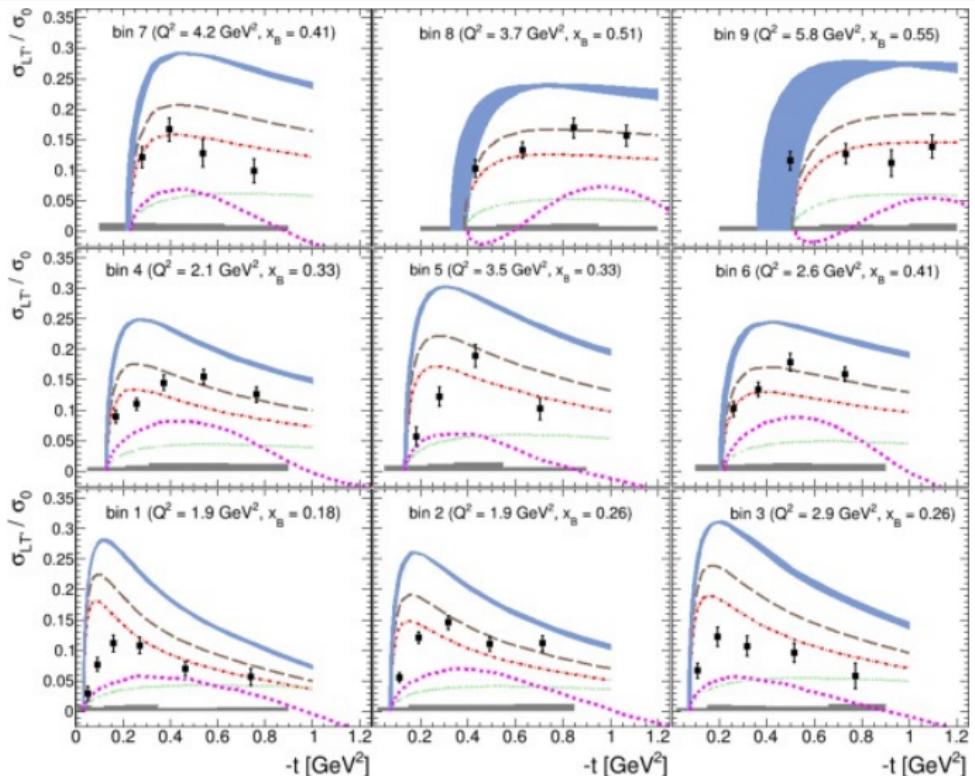
# What If...



- No  $Q^2$  dependence  $\rightarrow$  overlay curves at same  $x_B$
- Seems to show same  $-t$  dependence within uncertainties



# CLAS12 Results



GK (default)  
GK ( $H_T * 1.5$ )  
GK ( $H_T * 2$ )  
JML (Regge)  
GK (no pion pole)



# Quick Derivation

- Define the beam spin asymmetry  $A_{LU}$  as:

$$A_{LU} = \frac{1}{P} \left( \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} \right) = \frac{1}{P} \left( \frac{Y^+ - Y^-}{Y^+ + Y^-} \right)$$

- Polarized cross-section in Rosenbluth equation appears when separating events by helicity:

$$2\pi \frac{d^2\sigma}{dt d\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos \phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$
$$+ h \sqrt{2\epsilon(1-\epsilon)} \frac{d\sigma_{LT'}}{dt} \sin \phi$$

- Beam spin asymmetry provides much cleaner access to  $\sigma_{LT'}$ :

$$A_{LU} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos \phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

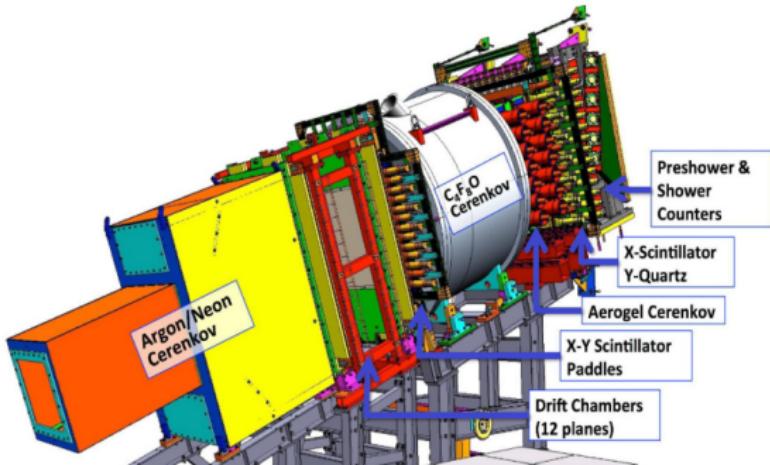
# SHMS Focal Plane Detectors



Photo by N. Heinrich.

Detector	Purpose
Ar/Ne Cherenkov	Not installed
Drift chambers	Tracking
Hodoscopes	Triggering, tracking
C <sub>4</sub> F <sub>8</sub> O Cherenkov	Particle identification
Aerogel Cherenkov	Particle identification
Shower counters	Calorimetry

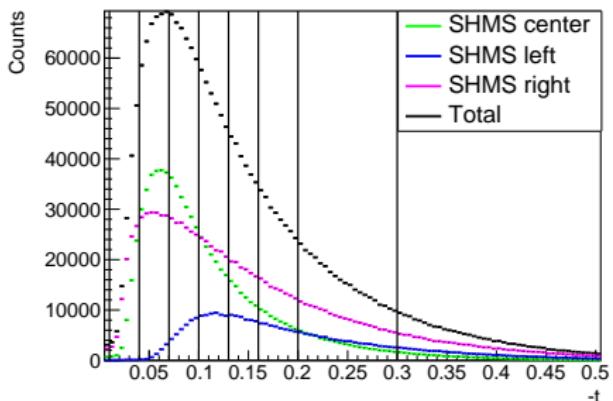
S. Ali et al, to be published (2022).



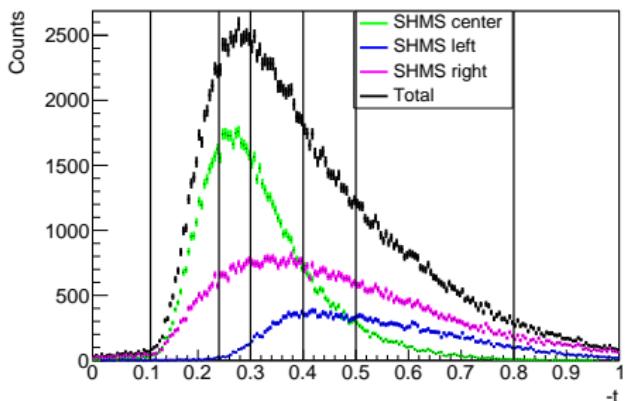


# -t Binning

- Sum all events at one  $(Q^2, x_B)$  and separate into  $-t$  bins with similar numbers of events



$Q^2 = 2.1 \text{ GeV}^2, x_B = 0.25$   
 $\mathcal{O}(10^6)$  events, 8  $t$ -bins

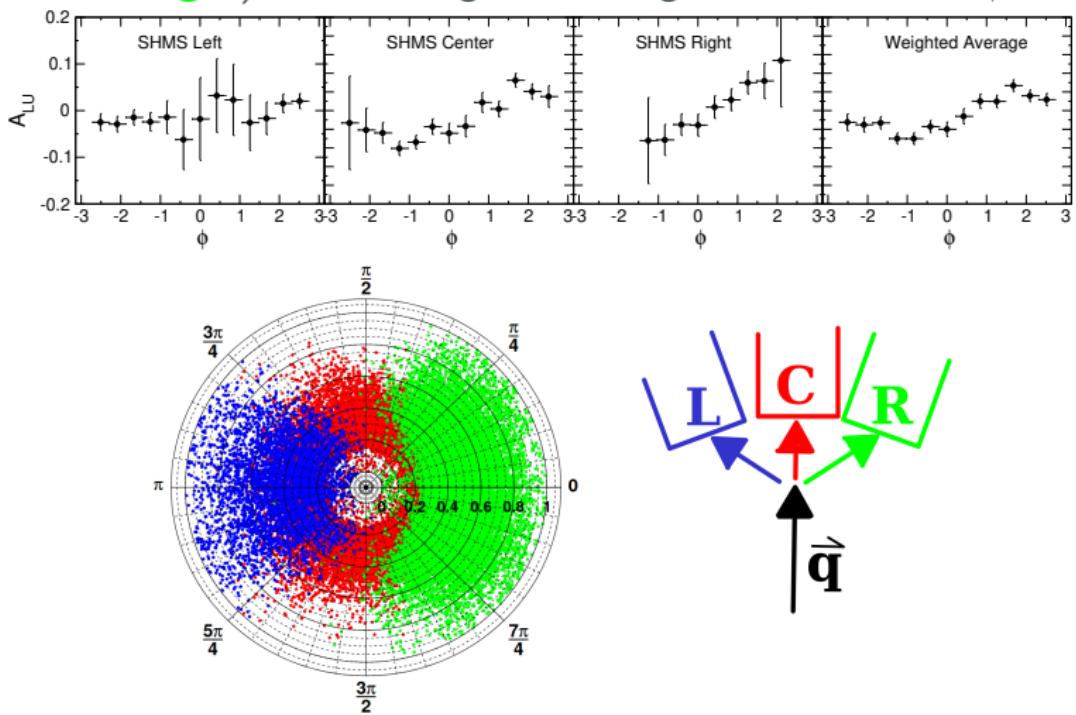


$Q^2 = 5.5 \text{ GeV}^2, x_B = 0.40$   
 $\mathcal{O}(10^5)$  events, 5  $t$ -bins

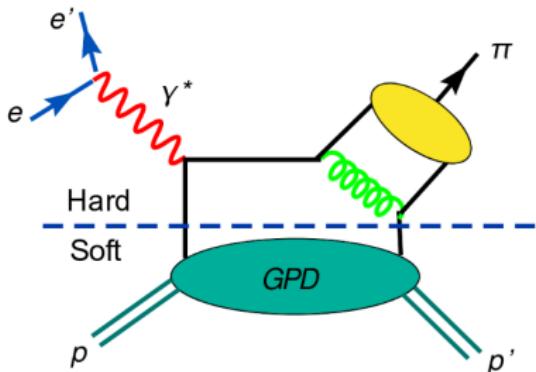


# Combining SHMS Settings

Asymmetry is calculated separately for three SHMS angles (**left**, **center**, **right**), then a weighted average is taken for full  $\phi$  coverage.



# GPDs and Hard/Soft Factorization

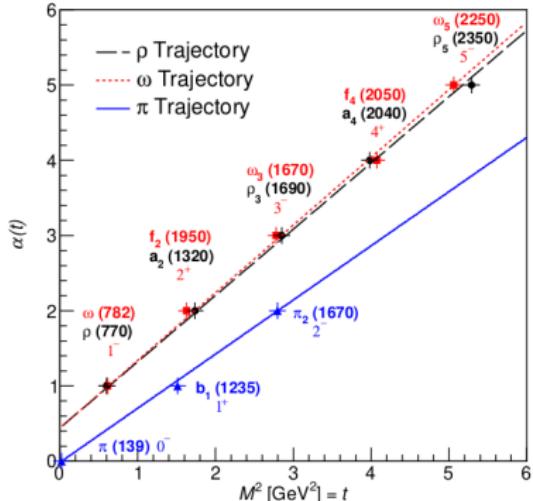


GPD models rely explicitly on **hard/soft factorization**: process can be written as convolution of hard (perturbative) scattering and soft (non-perturbative) object

- GPDs encode **3D nucleon structure** information: extraction is of high interest
- QCD predicts factorization at “**sufficiently high**”  $Q^2$
- Experimental data needed to identify onset of factorization



# Regge Models



## Regge trajectories

Linear relationship observed between mass  $M^2$  and spin  $\alpha$  for baryons of the same quark content

- Feynman propagator replaced with Regge propagator
- Exchange of a series of particles along a Regge trajectory
- My reaction: mesons exchanged, typically  $\pi$  and  $\rho$  propagators
- Cutoff is a free parameter in many models



## Model Details

- Vrancx-Ryckebusch (**VR**): exchange of  $\pi(140)$ ,  $\rho(770)$ , and  $a_1(1260)$  **Regge** trajectories
- Goloskokov-Kroll (**GK**): uses twist-2 longitudinal ( $\tilde{E}, \tilde{H}$ ) and twist-3 transverse ( $E_T, H_T$ ) **GPDs**, with pion pole contributions.
  - GK1:** default GK model
  - GK2:** modification  $H_T \rightarrow H_T * 2$ , as seen in CLAS12 BSA paper
- Yu-Choi-Kong (**YCK**): **Regge** trajectories, including tensor meson  $a_2(1320)$  and axial mesons  $a_1$  and  $b_1(1235)$ , with pion pole contributions.

*YCK are co-authors on this paper.*

  - YCK1:** nucleon EMFFs mediated by GPDs
  - YCK2:** nucleon EMFFs use dipole parametrization

T. Vrancx, J. Ryckebusch & J. Nys, Phys. Rev C, **89** 065202 (2014). arXiv:1310.7715

S.V. Goloskokov, P. Kroll, Eur. Phys. J. C **65** 137 (2010). arXiv:1106.4897

T. K. Choi, K.-J. Kong & B.-G. Yu, J. Korean Phys. Soc. **67**, 1089-1094 (2015). arXiv:1508.00969

S. Diehl et al., Phys. Lett. B **839**, 137761 (2023). arXiv:2210.14557



## Beam Polarization

- CEBAF produces polarized beam up to 12 GeV
- Polarization flipped at 30 Hz in a pseudo-random sequence
- Mott polarimeter at injector gives source polarization:  $90 \pm 1\%$
- Spin precession calculation shows Hall C receives 99% of the source polarization
- Final value  $P = 89^{+1}_{-3}\%$ : Uncertainty from the beam energy uncertainty (3.6 MeV) and the range of possible linac energy imbalance

Thanks to Steve Wood for polarization calculations and Dave Gaskell for uncertainty estimate