

# Update of PionLT DEMP Factorizability Studies

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# Motivation

The PionLT experiment took data at JLab Hall C in 2022

Want to better understand Hadron structure (Thus the Strong Force)

Generalized Parton Distributions (GPDs) are the next step in proton structure.

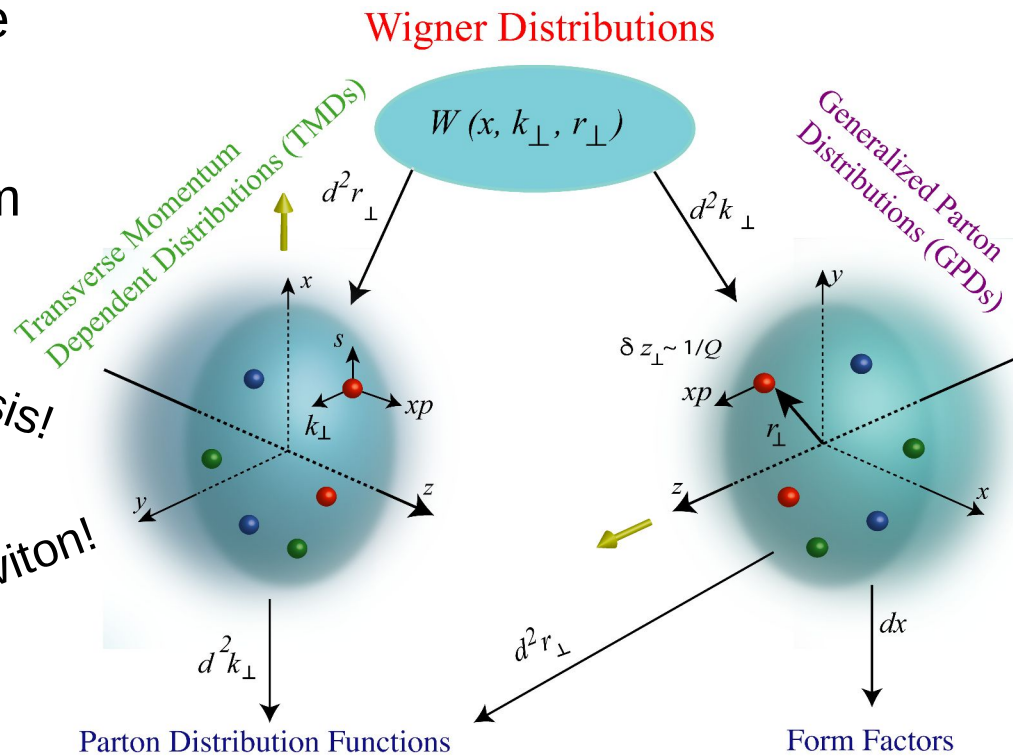
GPDs encode quark position and momentum

Useful for:

- Quark orbital angular momentum
- Pressure/sheer distribution in proton
- Mass radius of proton

Solve Spin Crisis!

Otherwise need Graviton!



# GPDs and Experiment

GPDs are universal quantities and reflect nucleon structure independent of reaction

- There are 2 main methods to extract the chirality conserving GPDs:

- **Deeply Virtual Compton Scattering (DVCS)**

- Sensitive to all 4

$H^{q,g}(x, \xi, t)$   
spin avg  
no hel. flip

$E^{q,g}(x, \xi, t)$   
spin avg  
helicity flip

- **Deep Exclusive Meson Production (DEMP)**

- Pseudoscalar mesons access  $\tilde{H}$   $\tilde{E}$

- Vector mesons access  $H$   $E$

$\tilde{H}^{q,g}(x, \xi, t)$   
spin diff  
no hel. flip

$\tilde{E}^{q,g}(x, \xi, t)$   
spin diff  
helicity flip

The combination of the 2 methods is needed to disentangle the different GPDs

# Accessing GPDs with meson production

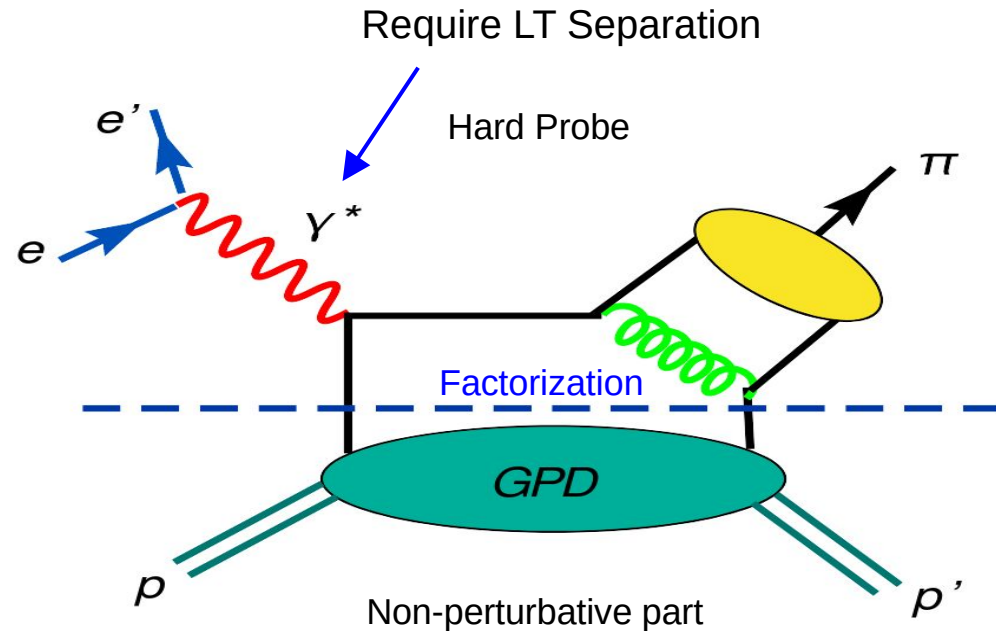
Using a recently proven factorization theorem to separate the process amplitude into two parts:

- A hard scattering process
  - perturbative QCD can be used.
- A non-perturbative part, parameterized by the GPDs

This is shown by the “Handbag Diagram”

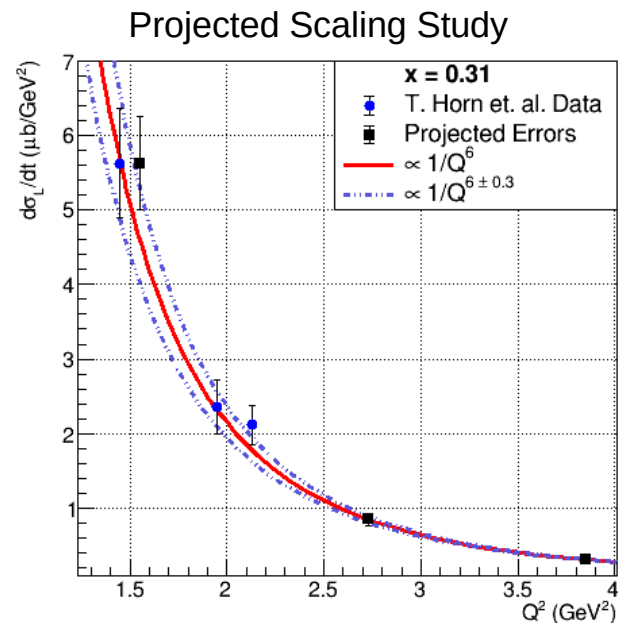
This applies to longitudinally polarized  $\gamma^*$  at sufficiently high  $Q^2$

- First shown by Collins, Frankfurt & Strikman [PRD 56(1997)2982].



# Factorizability

- Factorization regime will have characteristic  $1/Q^6$  scaling of  $\sigma_L$  with fixed  $x_B$
- It should also have  $\sigma_L \gg \sigma_T$
- Model independent test by extracting  $\sigma_L$  to see where this dependence begins
- This experiment does this for pion final state at 3 values of  $x_B$ :  
 $x_B = 0.31, 0.39, 0.55$
- If in regime then this data can be used to extract GPDs, otherwise all results in this  $Q^2$  thrown into question
- Previous studies inconclusive (T. Horn et. al. 2008), both predictions need to be met to be conclusive



$x_B$  - Bjorken scaling variable, and represents longitudinal momentum fraction

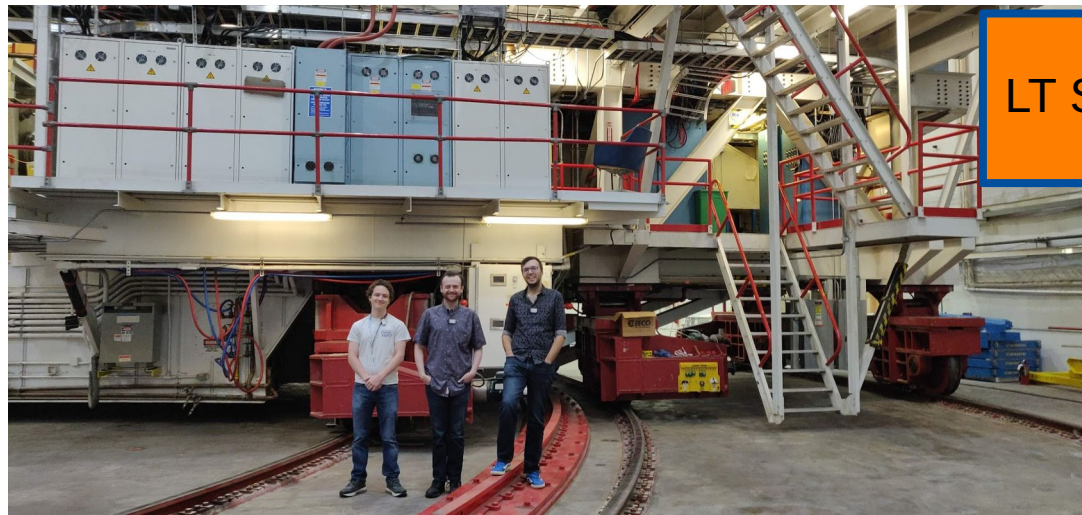
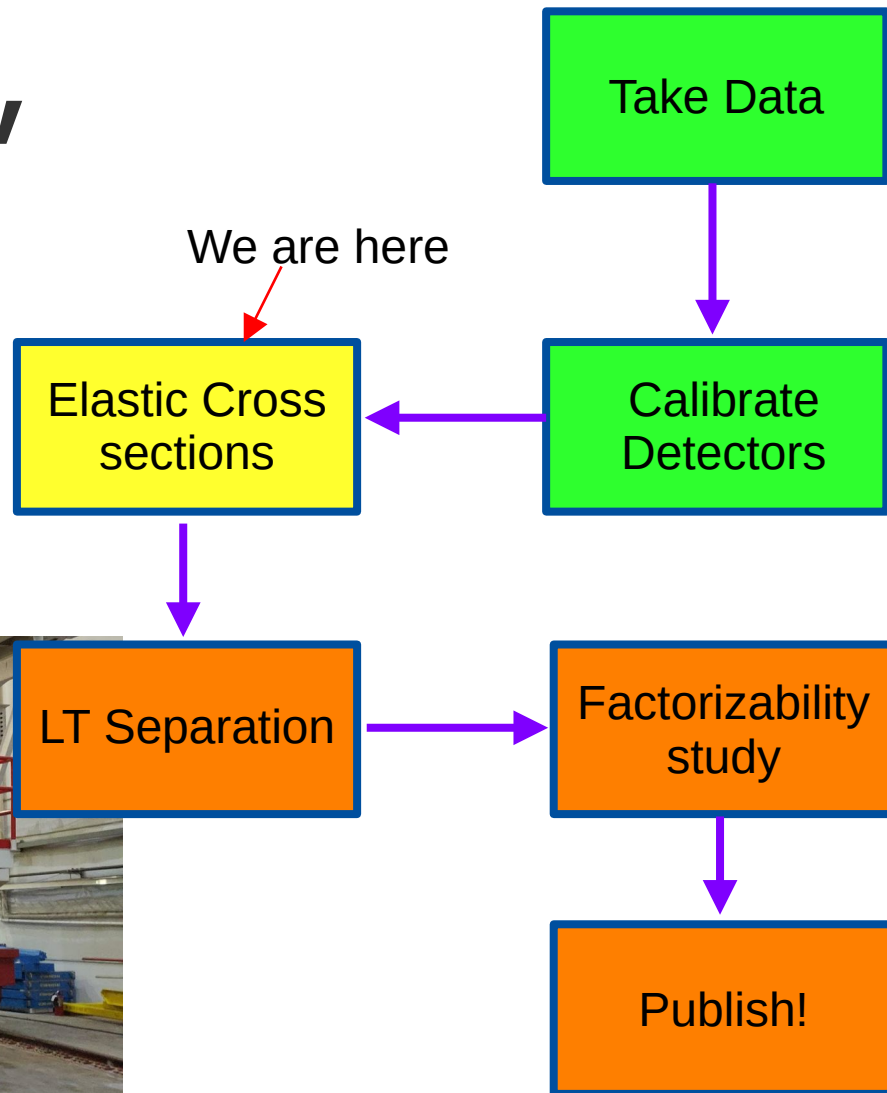
# Analysis Overview

Took Data at Jefferson Lab Hall C in 2022

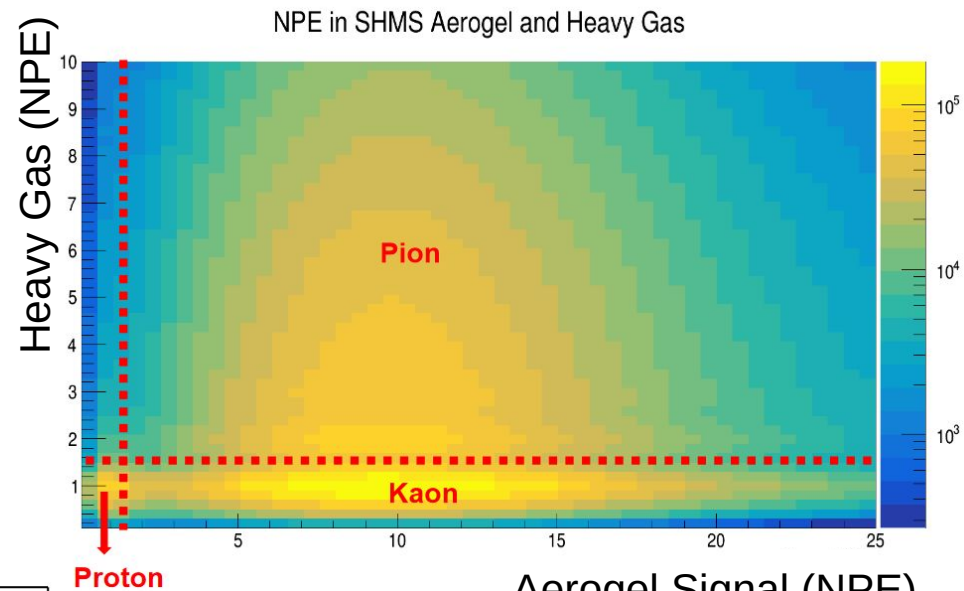
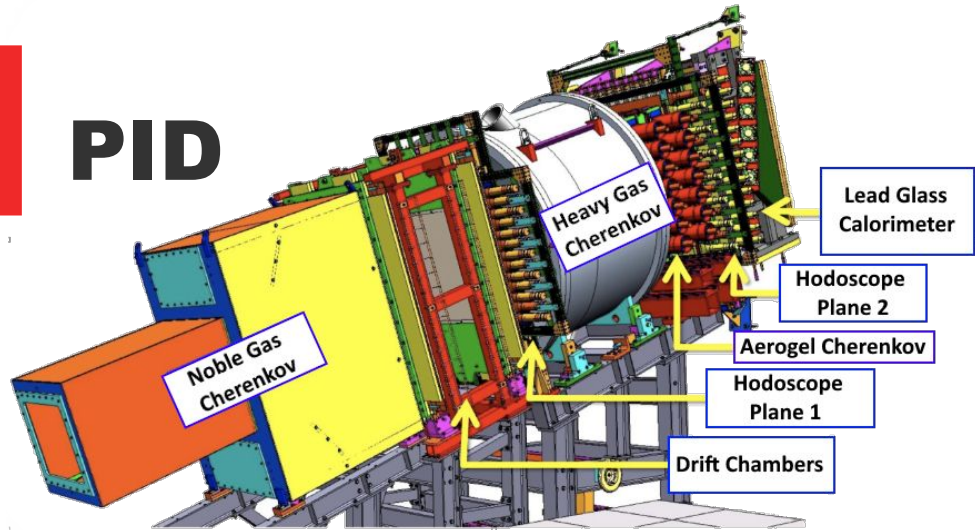
Finished Detector Calibrations

Working on Elastic Cross Sections,  
-> Set our systematics

Move on to LT separations next

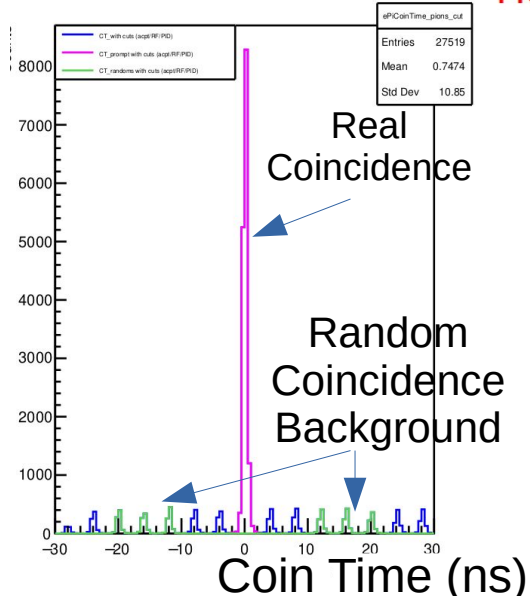


# PID



SHMS Detector Stack

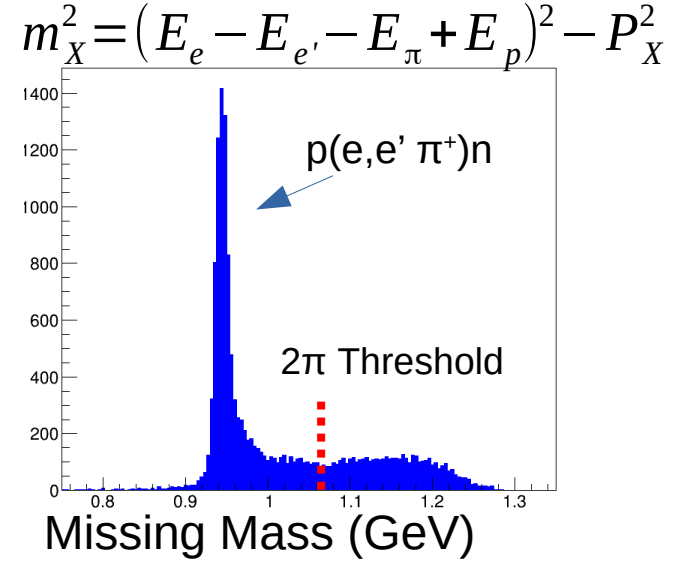
Electron-Pion CTime (with cuts)



Use Cherenkovs, Calorimeters, and timing to select  $p(e, e' \pi) X$

Then Missing Mass to select desired  $p(e, e' \pi) n$  final state

Aerogel Signal (NPE)



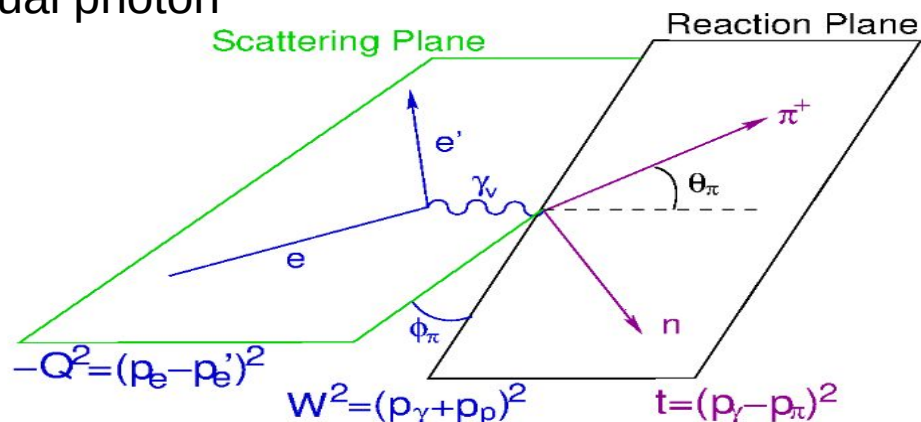
# LT Separation - Simple

$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

- To extract components of cross section based on virtual photon polarization, fit the above equation.
- To do this need to have full  $\phi$  coverage and 2 values of  $\varepsilon$  while keeping  $Q^2$ ,  $W$ , and  $t$  fixed.
- To get 2 values of  $\varepsilon$  we need data from 2 different beam energies.

This means different background and physics rates

For GPD factorization we want  $\sigma_L$  corresponds to longitudinally polarized  $\gamma$



Virtual-photon polarization:

$$\varepsilon = \left( 1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \tan^2 \frac{\theta_{e'}}{2} \right)^{-1}$$



# LT Sep – In detail

Each iteration is actually a multi-step process

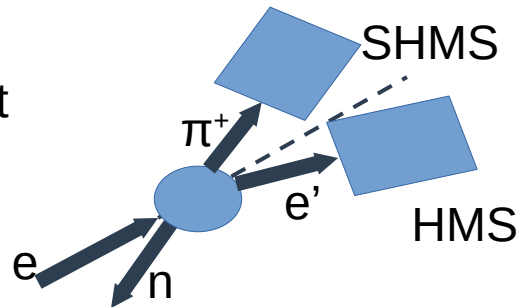
1. Choose functional form of  $\sigma_T, \sigma_L, \sigma_{LT}, \sigma_{TT}$   
 Arbitrary functions to fit  $Q^2, W$  variance across bin

2. Combine SHMS left, right, and centre  
 Done because we need to have to get full coverage in  $\phi$  at fixed  $-t$

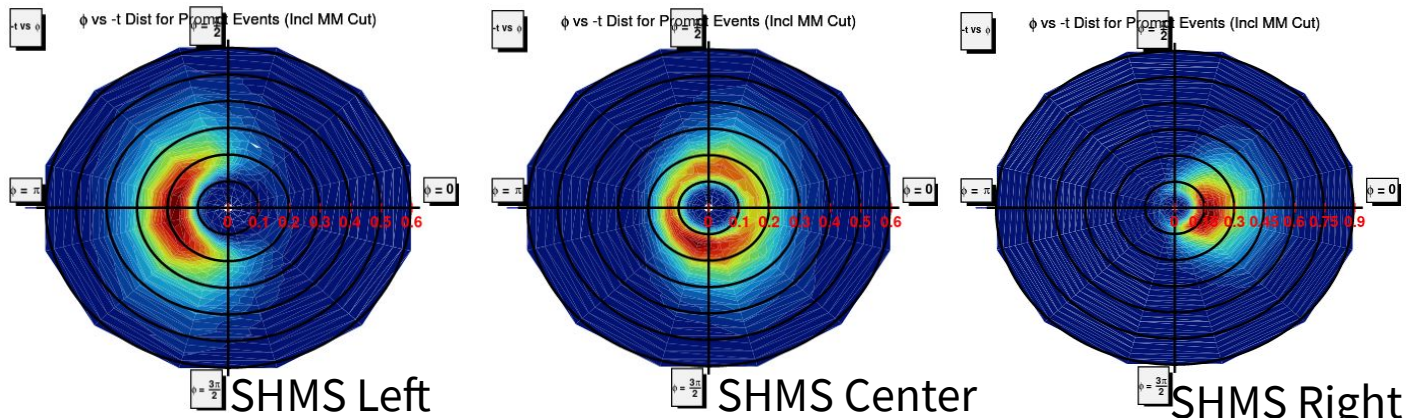
Fit parameters

$$\sigma_L = (A + B * \log(Q^2)) e^{-|t|(C + D * \log(Q^2))}$$

Example From F $\pi$ -2 Experiment



Rotate SHMS to get  $\phi$  coverage

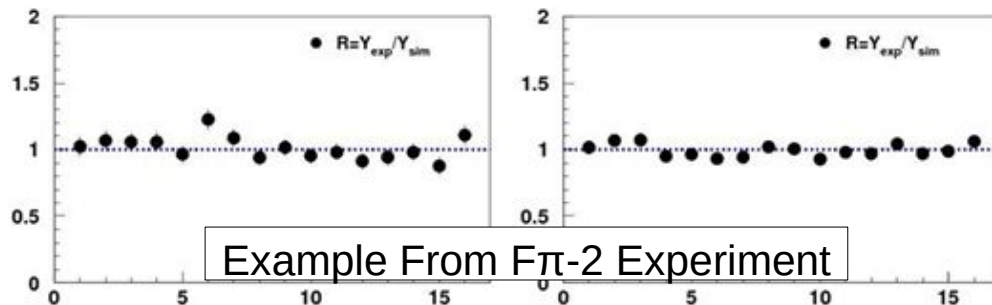


Example  $-t$  vrs  $\phi$  polar plots from setting:  $Q^2=3.85, W=3.07, \text{high } \epsilon$

# LT Sep – In detail

3. Bin in  $-t$  and  $\phi$ , calculate average  $W$ ,  $Q^2$ ,  $\theta$ , and  $\varepsilon$   
final value reported at average value in bin

4. Calculate MC to Data ratio in all bins

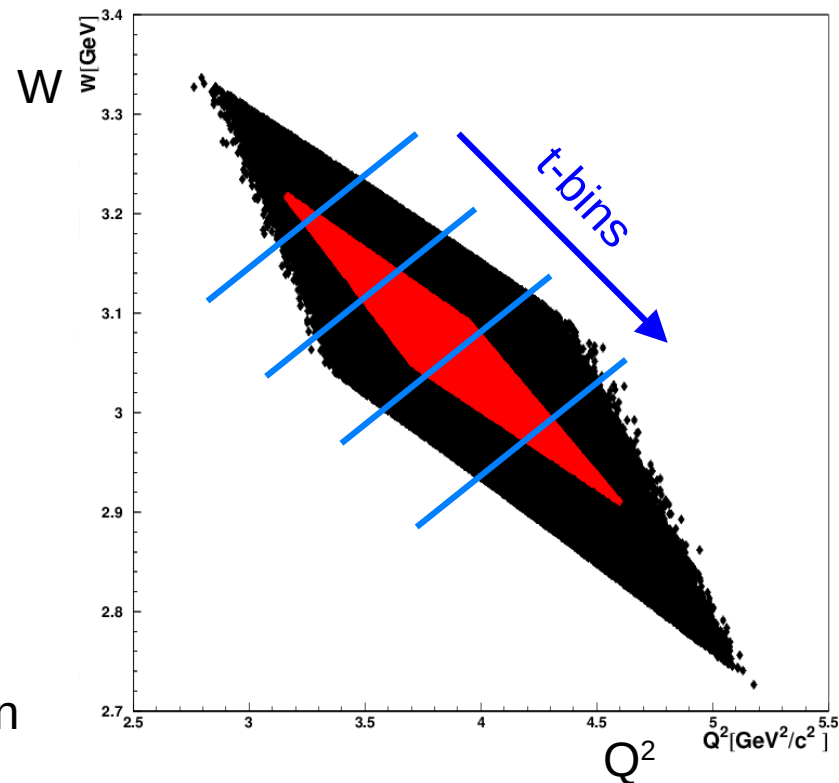


5. Use Monte Carlo to calculate unseparated cross section using equation:

$$\sigma_{\text{exp}}(\bar{W}, \bar{Q}^2, t, \phi; \bar{\theta}, \bar{\varepsilon}) = \frac{\langle Y_{\text{exp}} \rangle}{\langle Y_{\text{sim}} \rangle} \sigma_{\text{MC}}(\bar{W}, \bar{Q}^2, t, \phi; \bar{\theta}, \bar{\varepsilon})$$

Simulated Example “diamond plot”

LH+,  $Q^2=3.85$ ,  $W=3.07$ ,  $\varepsilon=.67$ ,  $\theta_{\text{pq}}=+0.000$

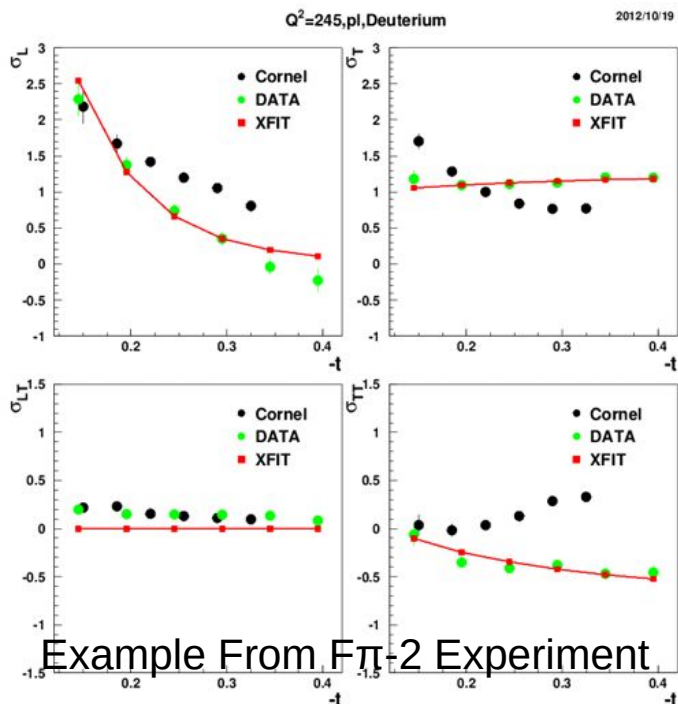


# LT Sep – In detail

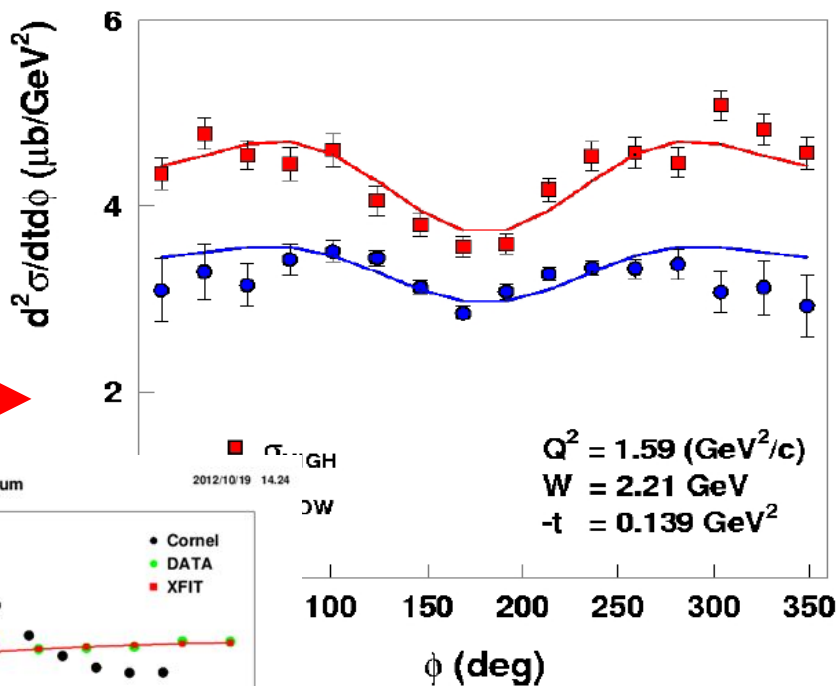
6. Fit Rosenbluth equation extract values of  $\sigma_T$ ,  $\sigma_L$ ,  $\sigma_{LT}$ ,  $\sigma_{TT}$



7. Fit the functional forms to your new values of  $\sigma_T$ ,  $\sigma_L$ ,  $\sigma_{LT}$ ,  $\sigma_{TT}$



Example From Fπ-2 Experiment



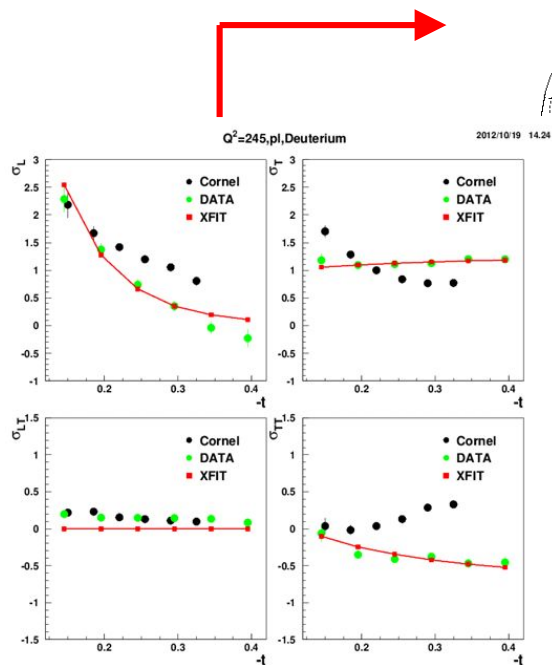
Done when variation in  $\sigma_{exp}$  between iterations is less than 1%,  
And data to MC ratios  $\sim 1$

# LT Separation Overview

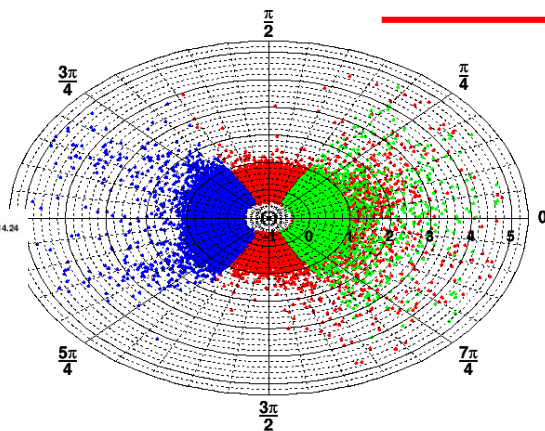
Bin data and calculate MC to data ratio

Calculate Unseparated Cross Sections

$$\sigma_{\text{exp}}(\bar{W}, \bar{Q}^2, t, \phi; \bar{\theta}, \bar{\epsilon}) = \frac{\langle Y_{\text{exp}} \rangle}{\langle Y_{\text{sim}} \rangle} \sigma_{\text{MC}}(\bar{W}, \bar{Q}^2, t, \phi; \bar{\theta}, \bar{\epsilon})$$



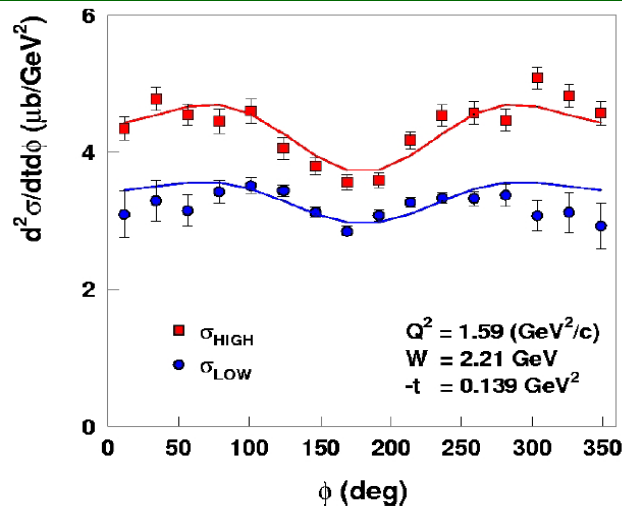
Fit arbitrary functions for  
 $\sigma_T, \sigma_L, \sigma_{LT}, \sigma_{TT}$



Repeat until self consistent

Fit Rosenbluth Equation

$$2\pi \frac{d^2\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



# Summary

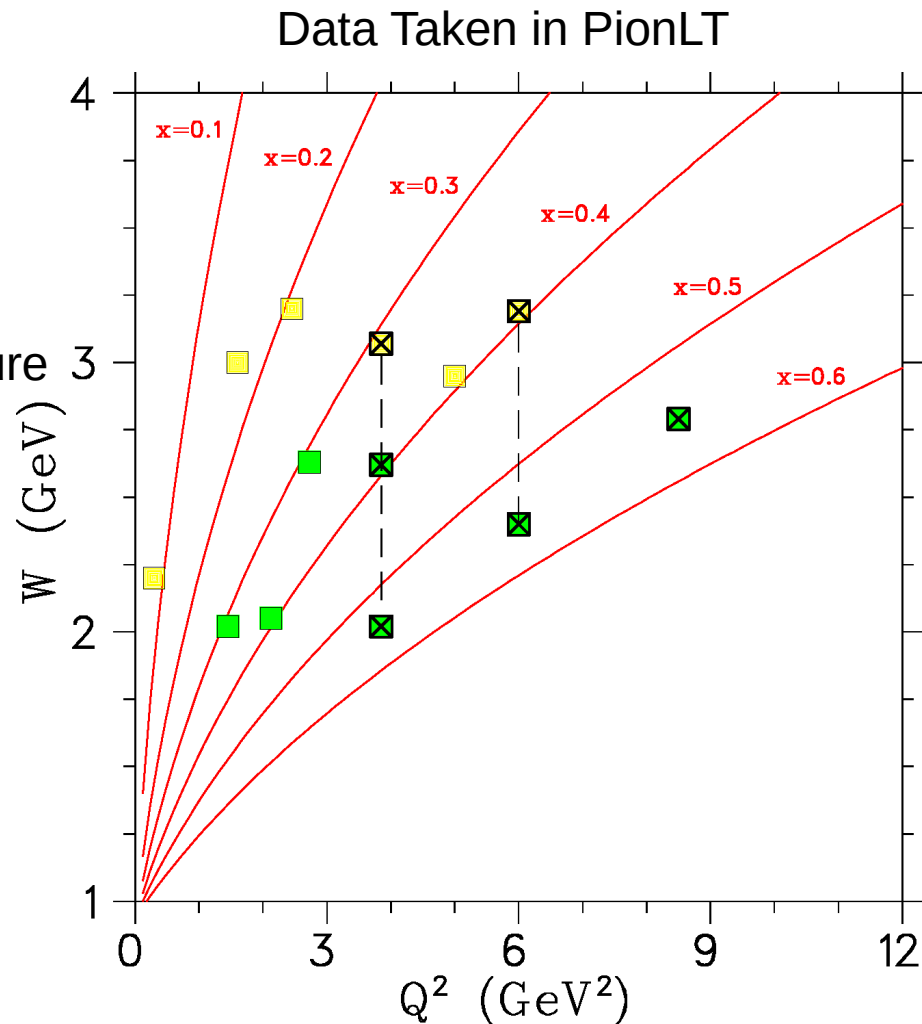
The PionLT experiment is nearly ready to begin LT separation of cross-sections

GPDs are the exciting new frontier of proton structure

LT Separations are crucial:

- Model independent check of factorization
  - Predict both  $1/Q^6$  scaling of  $\sigma_L$  with fixed  $x_B$  and  $\sigma_L \gg \sigma_T$
- Allows access to GPD information

Expect multiple publications starting in December



# Thank You

## Questions?

NSERC grant:  
SAPIN-2021-00026



University  
of Regina

# Solving the Spin Crisis

GPDs are related to the orbital angular momentum of the quarks and gluons:

Christine A. Aidala, Steven D. Bass, Delia Hasch, and Gerhard K. Mallot. The spin structure of the nucleon. Rev. Mod. Phys. 85, 655 – Published 12 April, 2013 <https://doi.org/10.1103/RevModPhys.85.655>

$$\frac{1}{2} = \frac{1}{2} \sum_q \Delta q + \Delta g + L_q + L_g$$

In the forward limit the GPDs  $H$  and  $\tilde{H}$  are related to the parton distributions studied in deep inelastic scattering

$$\begin{aligned} H(x, \xi, t)|_{\xi=t=0} &= q(x) \\ \tilde{H}(x, \xi, t)|_{\xi=t=0} &= \Delta q(x) \end{aligned} \quad (30)$$

GPDs contain vital information about quark total angular momentum in the nucleon. Ji's sum-rule (Ji, 1997b) relates  $J_q$  to the forward limit of the second moment in  $x$  of the spin-independent quark GPDs

$$J_q = \frac{1}{2} \int_{-1}^{+1} dx x \left[ H^q(x, \xi, t=0) + E^q(x, \xi, t=0) \right]. \quad (32)$$

The gluon “total angular momentum” could then be obtained through the equation

$$\sum_q J_q + J_g = \frac{1}{2}. \quad (33)$$

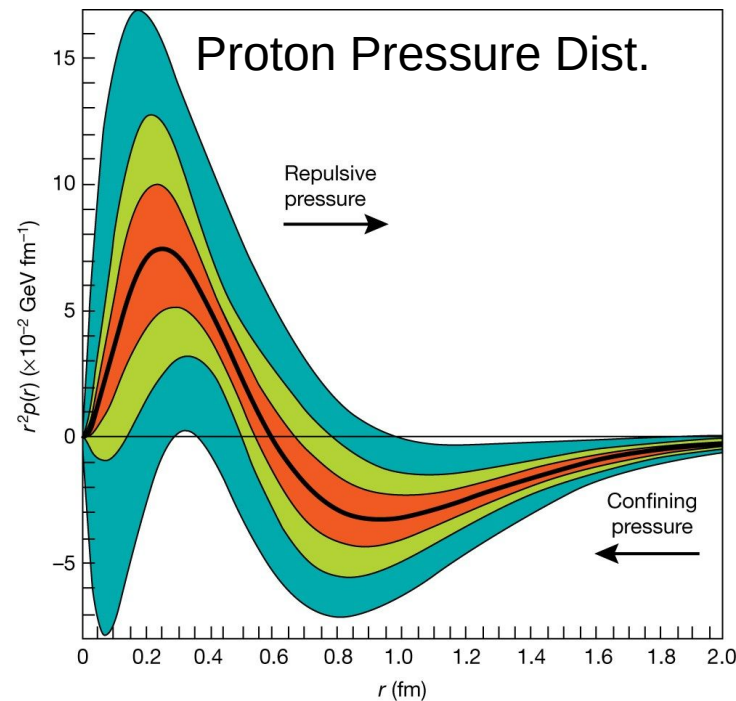
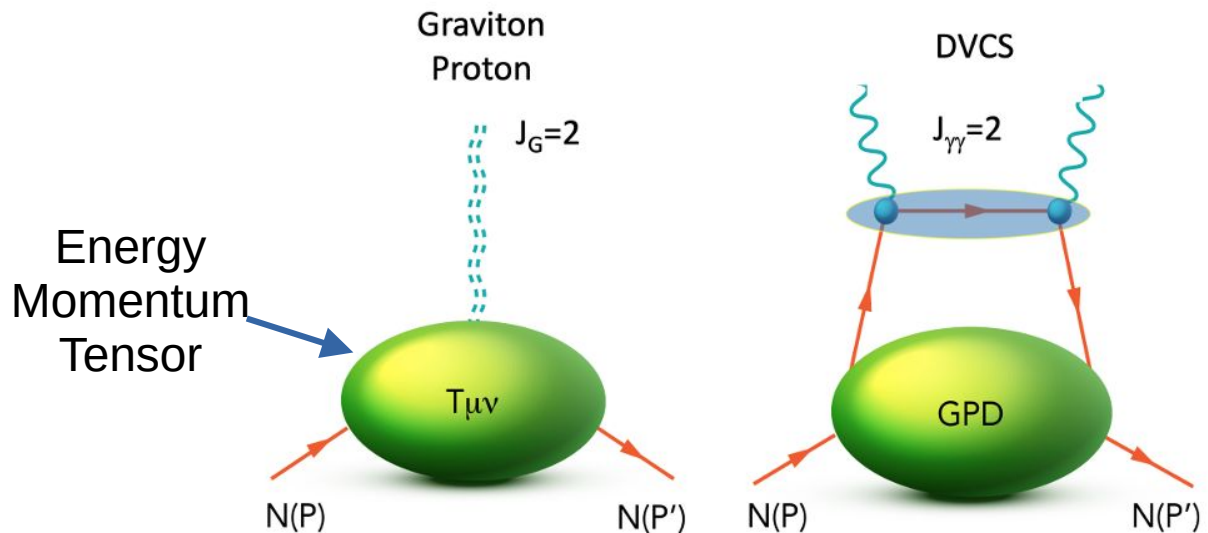
# Pressure/Mass distribution

Recent papers show equivalence between hypothetical graviton-proton scattering and DVCS interaction:

Burkert, V.D., Elouadrhiri, L. & Girod, F.X. The pressure distribution inside the proton. Nature 557, 396–399 (2018). <https://doi.org/10.1038/s41586-018-0060-z>

V.D. Burkert, L. Elouadrhiri, F.X. Girod. The mechanical radius of the proton arXiv:2310.11568

Allows extraction of Pressure, shear, and mass distribution from GPDs

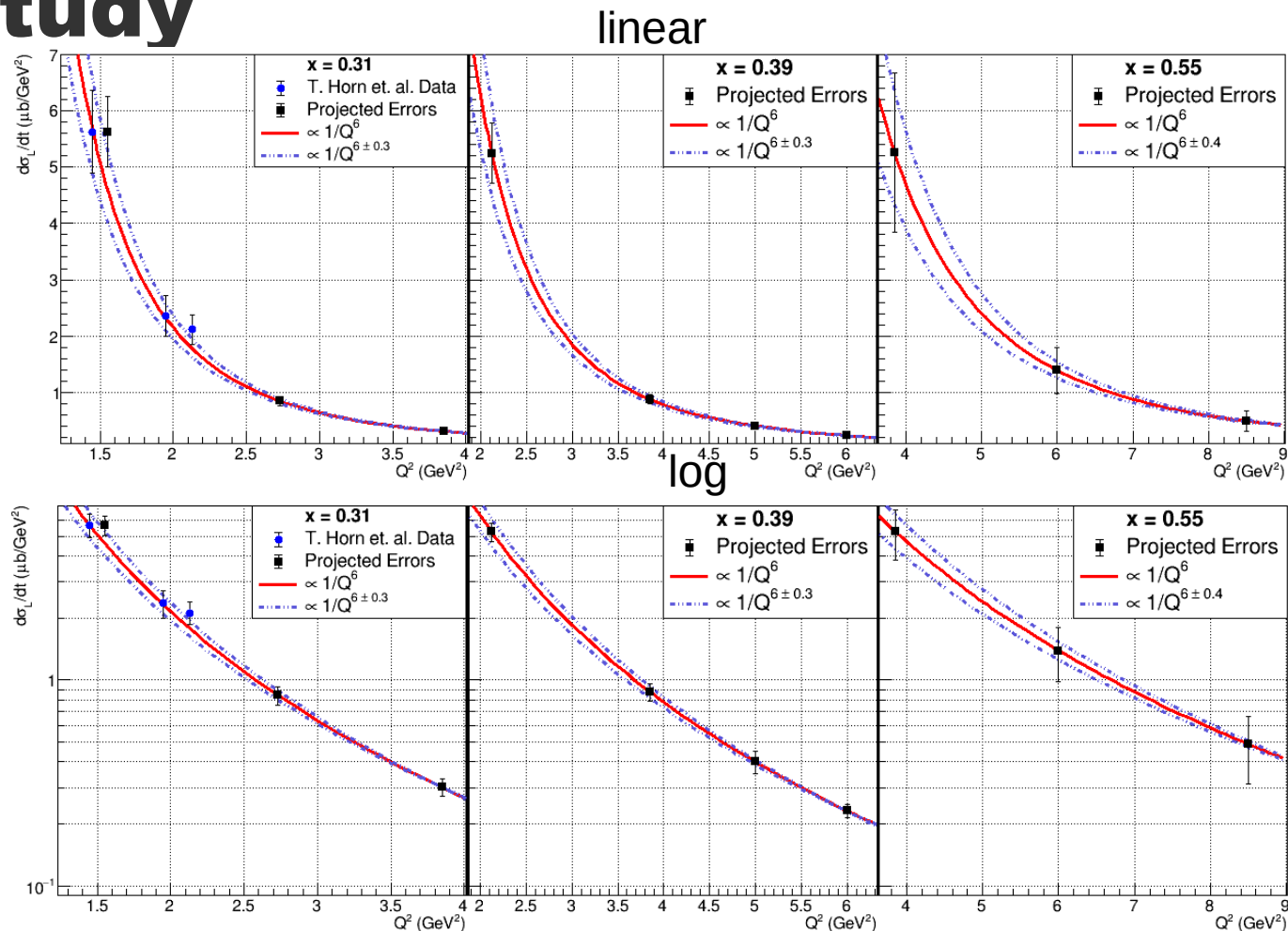




# Scaling study

Factorization regime will have characteristic  $1/Q^6$  scaling of  $\sigma_L$  with fixed  $x_B$

It should also have  $\sigma_L \gg \sigma_T$

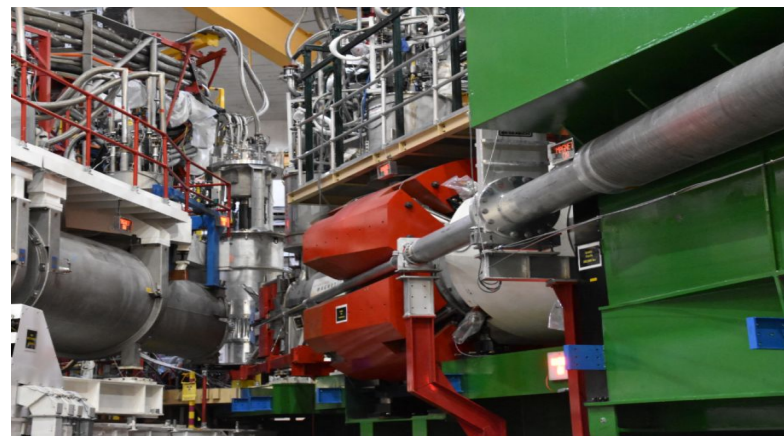
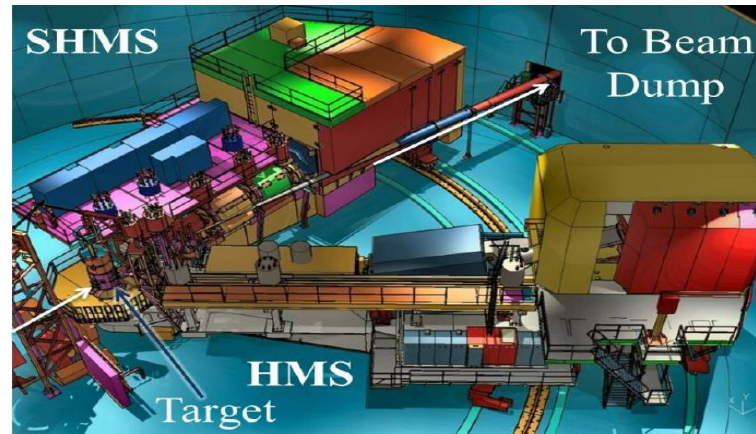


# Hall C

The Hall Contains two highly sophisticated magnetic spectrometers

- Target can have Liquid H<sub>2</sub>, Liquid D<sub>2</sub>, or solid targets
  - Takes high power beam (~800kW)
- High Momentum Spectrometer (HMS) and Super High Momentum Spectrometer (SHMS):
  - Both arms have 3 Quadrupole and 1 Dipole super conducting magnet, the SHMS has an additional dipole before the first Quadrupole
  - Dipole allows studies at specific momenta
  - Both contain similar detector packages that support high rate (<1MHz)

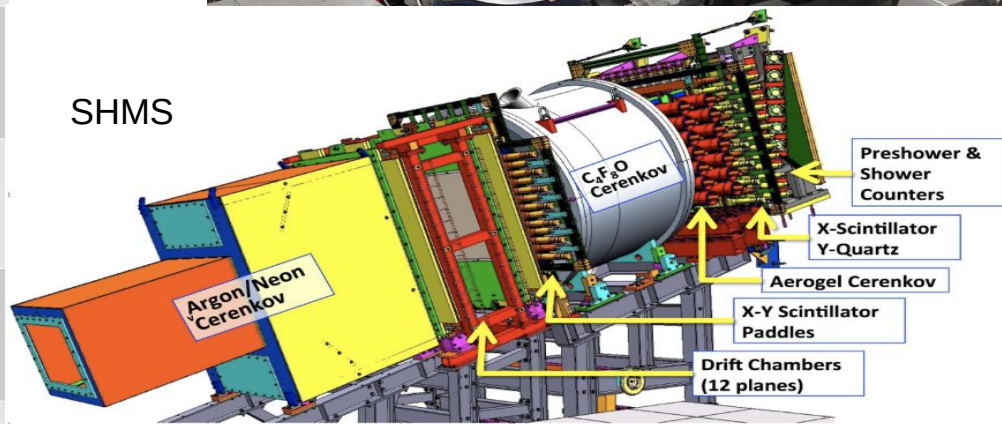
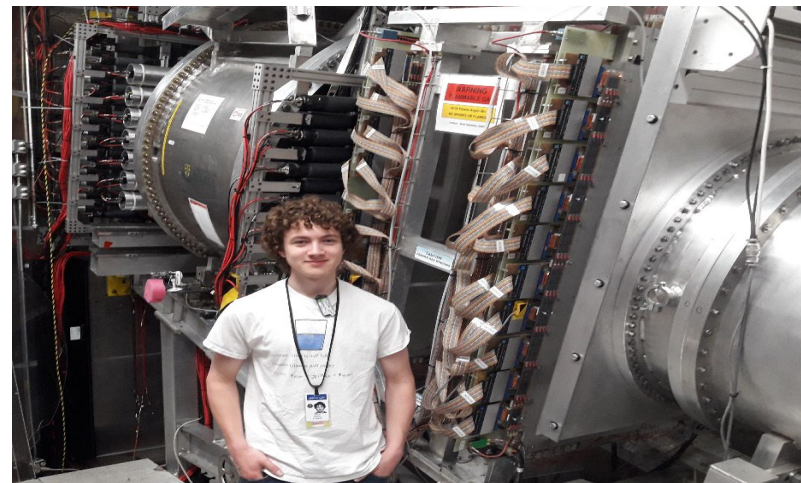
Spectrometer	Angle Range (Degrees)	Momentum Range (GeV/c)
HMS	10.5 - 90	0.5 - 7
SHMS	5.5 - 40	0.5 - 11



# Detector Stack

Both the Spectrometers have a detector stack in their focal plane. Which give high momentum resolution and particle Identification

Detector	Purpose	Notes
Aerogel Cerenkov	Particle ID, $K^+$ / $p$ discrimination	$n = 1.011, 1.015, 1.03, 1.05$
Heavy Gas Cerenkov (HGC)	Particle ID, Trigger, $\pi^\pm/K^\pm$ discrimination	$C_4F_{10}$ –Vary pressure to set $n$ at $K^\pm$ threshold
Noble Gas Cerenkov	Particle ID, Trigger. $e^+/\pi^+$ at high momentum	Only in SHMS
Hodoscopes	Trigger, Time reference, Measure $\beta$	
Drift Chambers	Momentum measurement, Tracking	5mm max. Drift, 300 micron resolution
Preshower and Shower Counters (Calorimeters)	Particle ID, Trigger, $e^\pm$ Tagging	



# Elastic Cross-section

Elastic Cross section is used to check systematic uncertainties

Studies this is used for:

- Spectrometer Offsets
- Target Boiling
- Detector rate dependence
- Tracking efficiency

Roughly 1 month from finishing study

## $p(e, e'p)$ Reaction

W Distribution

