

Investigation of $N = 32$ shell closure through $^{50}\text{Ca}(d,p)^{51}\text{Ca}$

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Supervisor: Dr. Rituparna Kanungo



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Background

Shell closure and magic numbers.

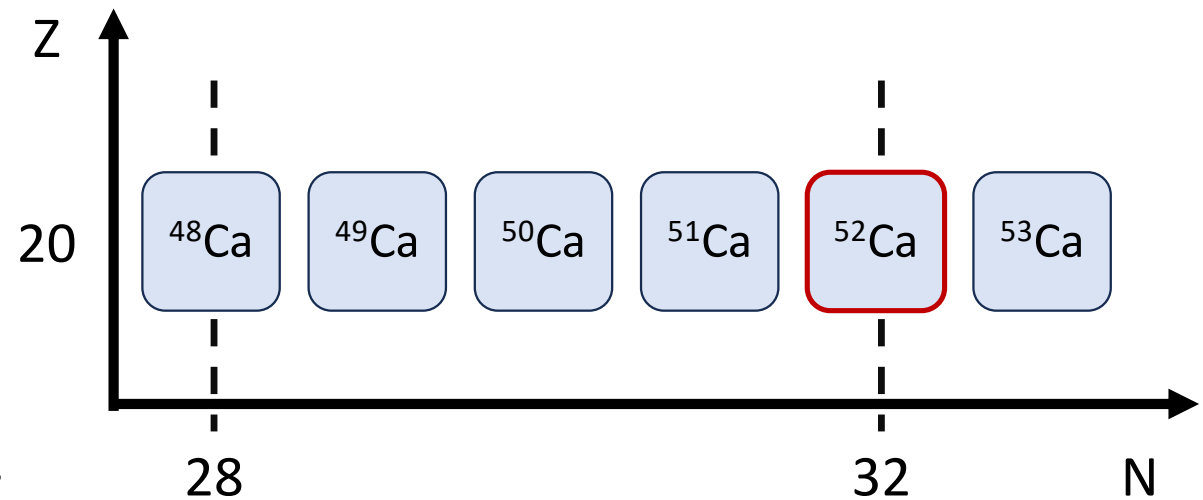
- Extra stability when a certain number of protons/ neutrons filling the shell levels: **2, 8, 20, 28, 50, 82, (126)**.

Neutron-rich nuclei

- Large N/Z ratio
- Short-lived
- Appearance/ disappearance of shell closure

Calcium isotope - ^{52}Ca

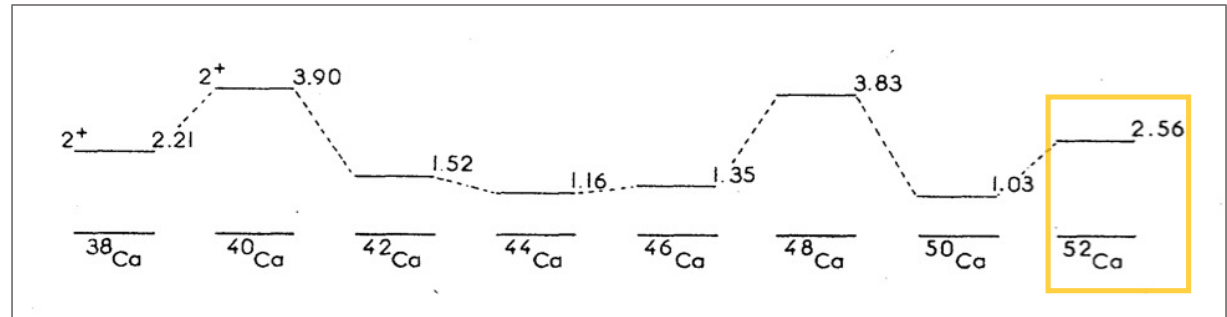
- Proton magic number, $Z = 20$.
- Potential new shell closure at $N = 32$.



Past experiments on ^{52}Ca

Signs of shell closure:

- **Increase** in excitation energy
- **Increase** in neutron separation energy
- **Local minima** in nuclear charge radii

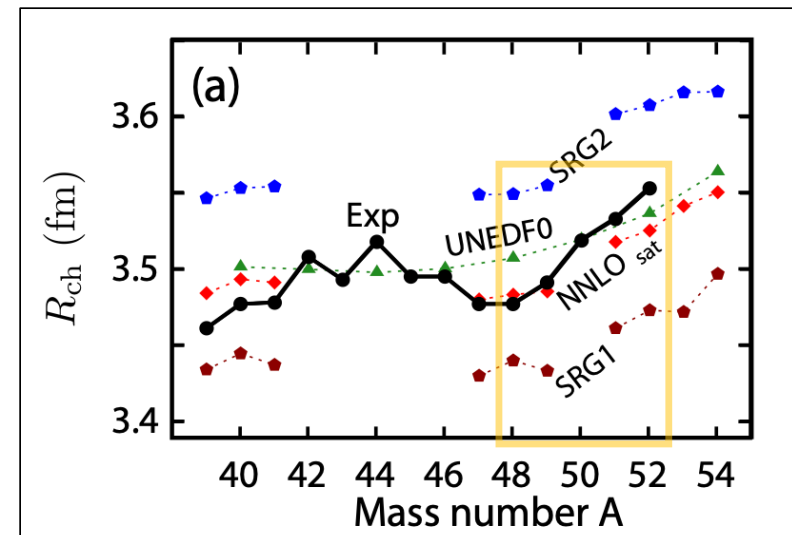


Huck et al. (1985)

Observation of $N = 32$ shell closure

Large charge radii of ^{52}Ca

- Unexpected rate of increase
- Cannot be reproduced by theoretical calculations.



Ruiz et al. (2016)

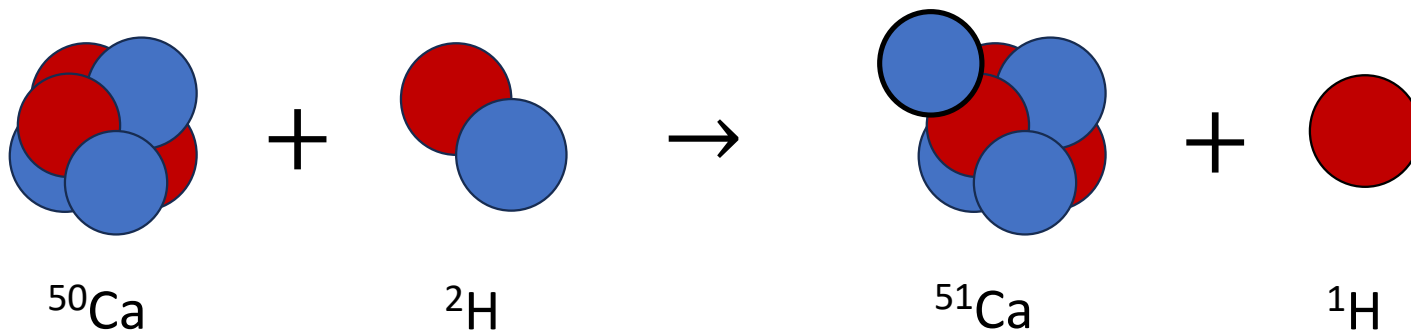
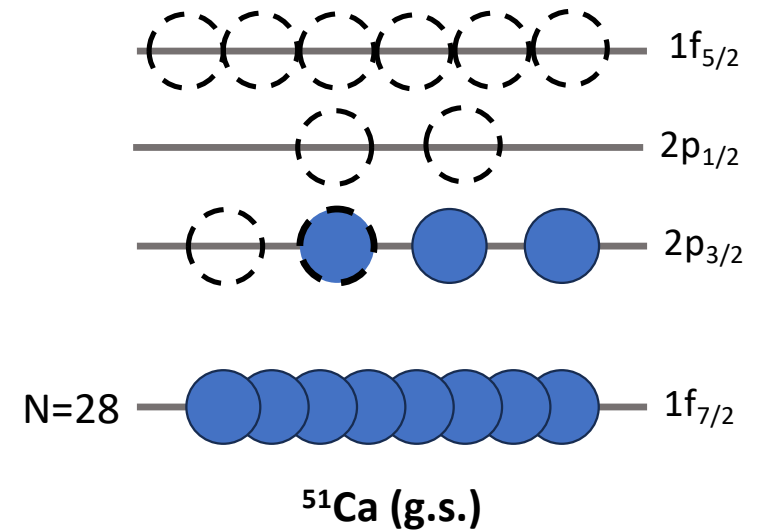
Project summary

Investigation of the reaction $^{50}\text{Ca}(d,p)^{51}\text{Ca}$

- Population of ground and excited states.
- Neutron occupancy in $2p_{3/2}$, $2p_{1/2}$, or $1f_{5/2}$ shell.

Excitation spectrum

- Detection of protons



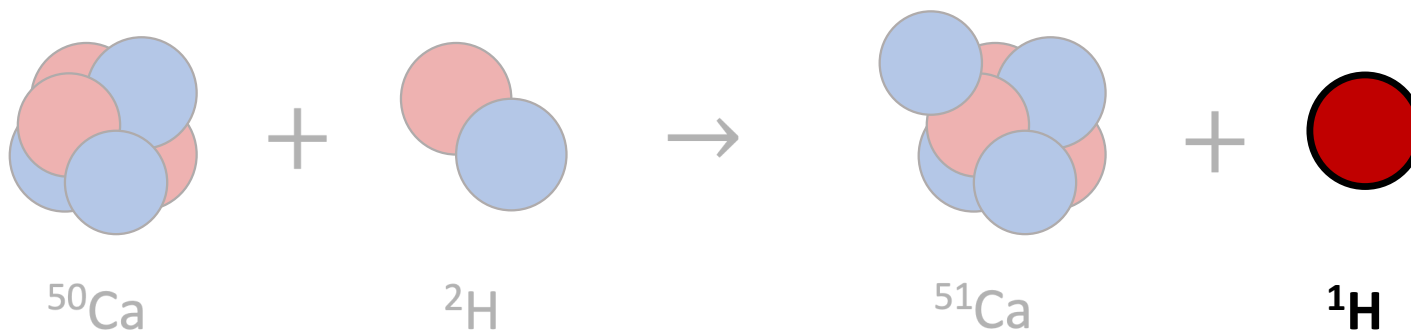
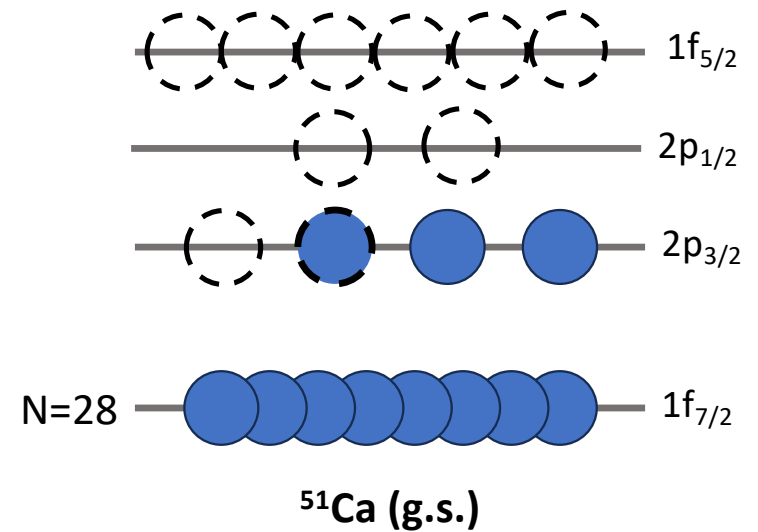
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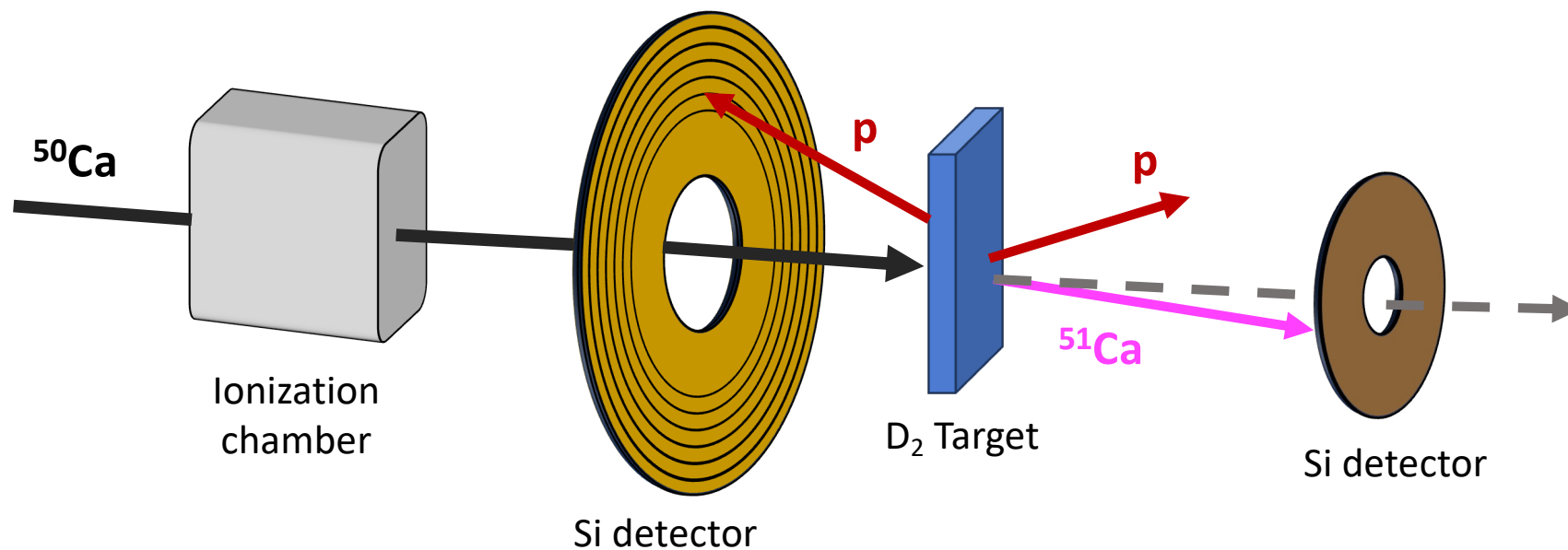
Excitation spectrum

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Experiment setup

IRIS facility at TRIUMF – particle accelerator centre (Vancouver, BC)



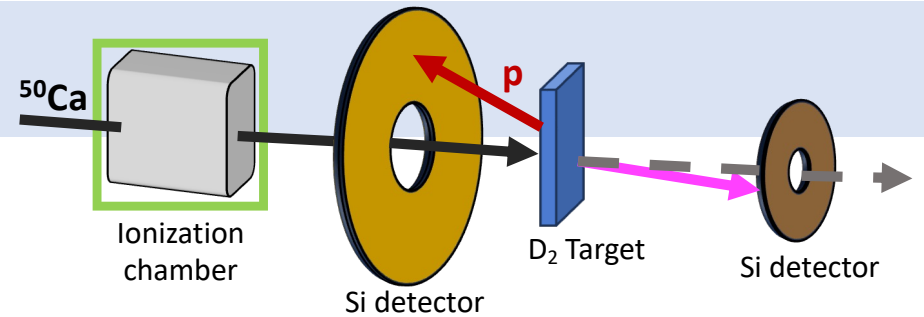
IC - Beam identification

^{50}Ca beam

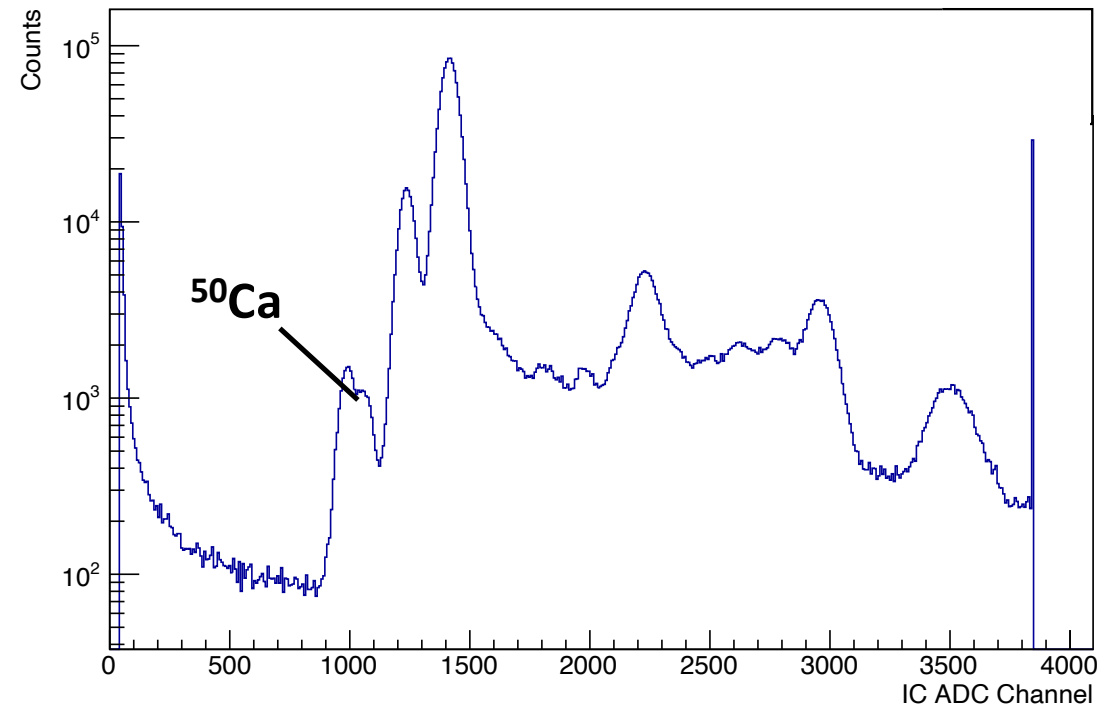
- Produced using Isotope mass Separation On-Line (ISOL) technique.
- Delivered at 7.2 AMeV (360 MeV)

Ionization chamber (IC)

- Isobutane gas
- Beam profile, counts
- $\frac{dE}{dx} \propto \frac{Z^2}{v^2}$

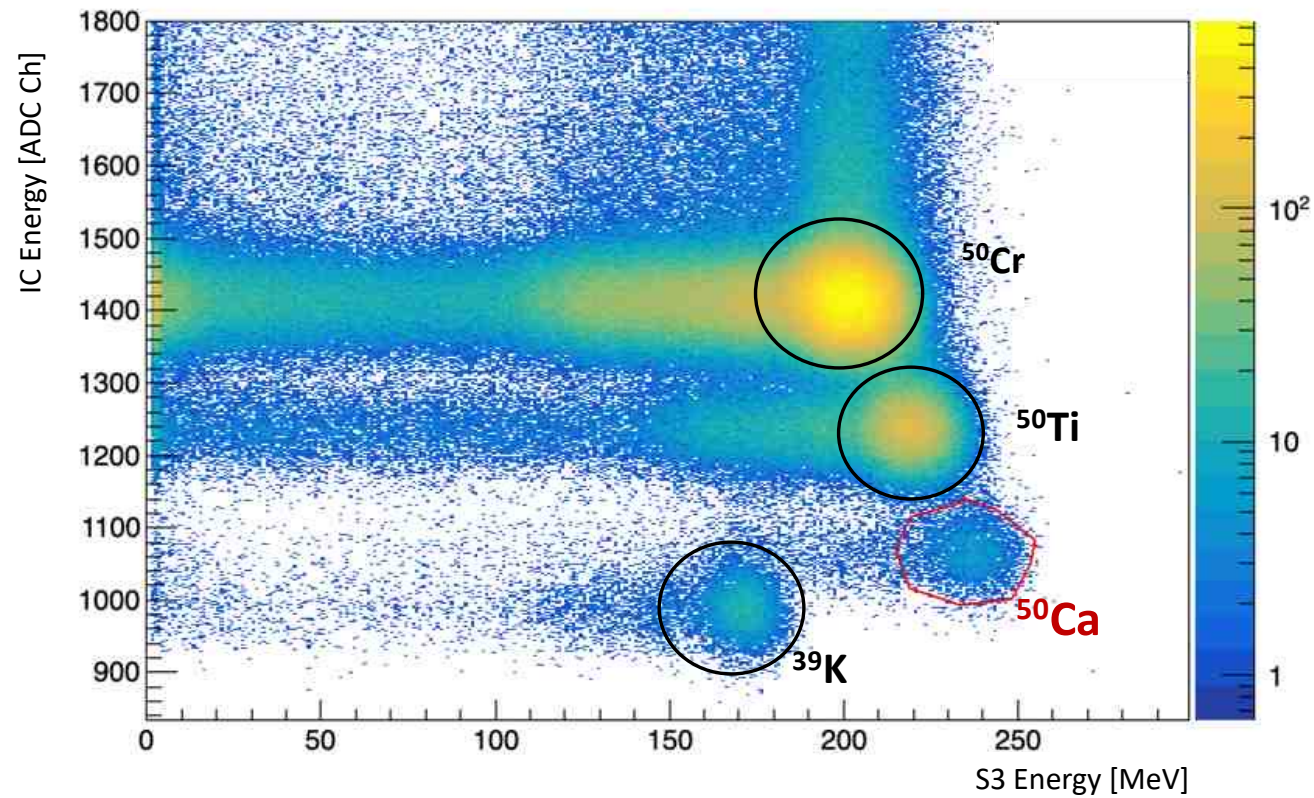
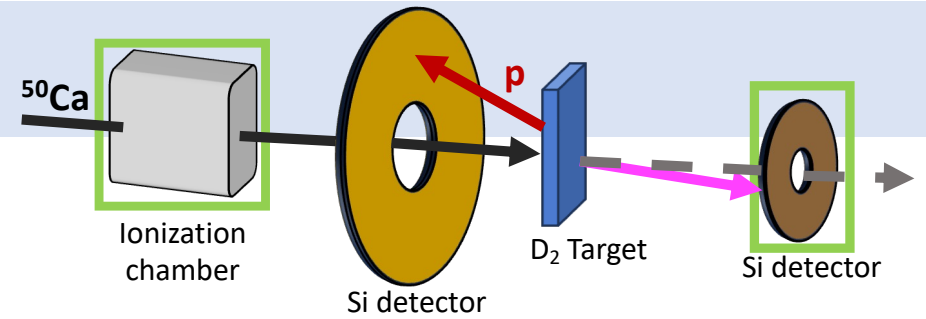


IC Spectrum



IC - Beam identification

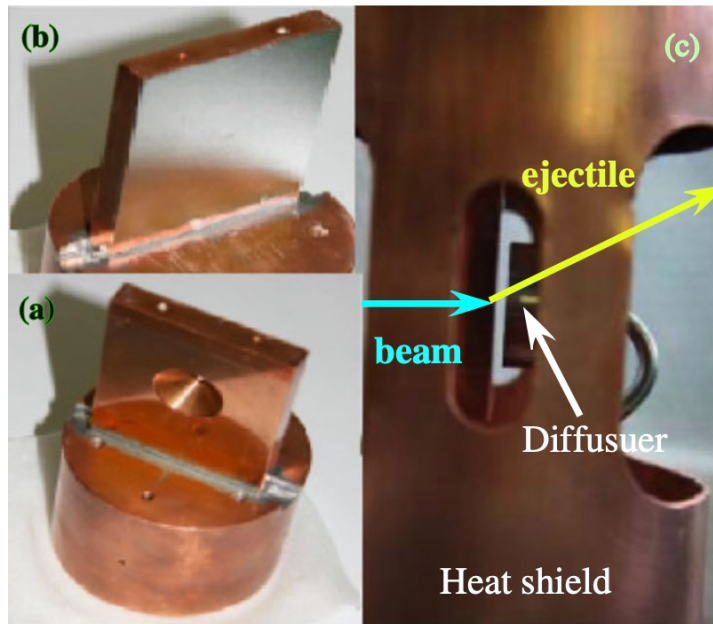
Energy deposit in IC vs Si detector



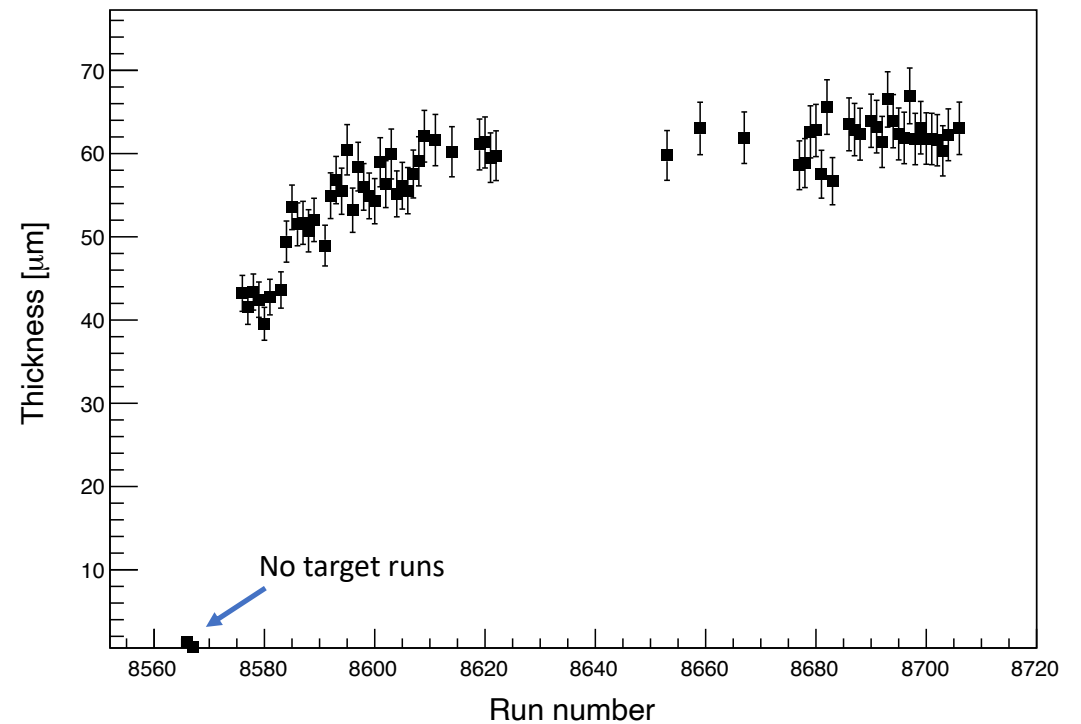
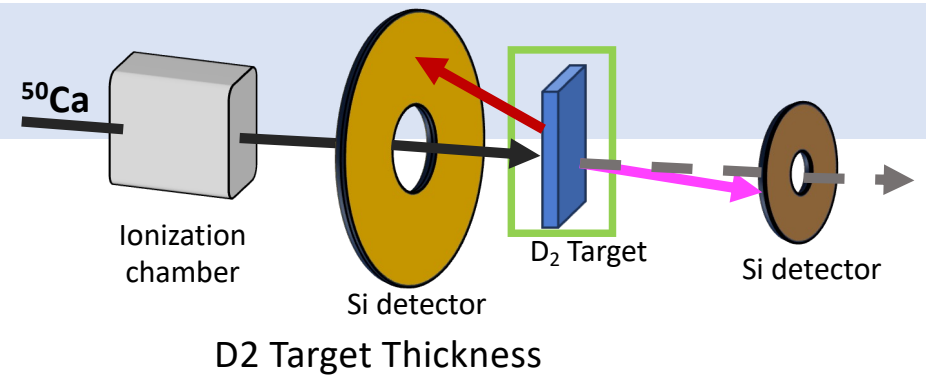
Solid deuterium target

Thin windowless D₂ target

- **Higher density**, better statistics
- Less contaminants/ energy loss



a) Target cell; b) Silver foil backing; c) Heat shield



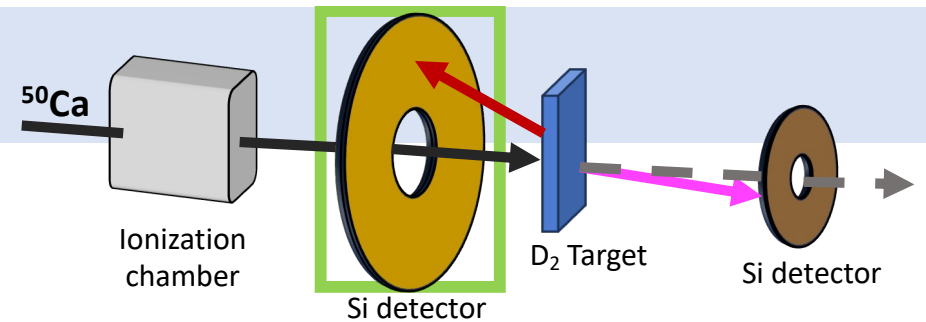
Proton detection

Protons in **upstream** of target

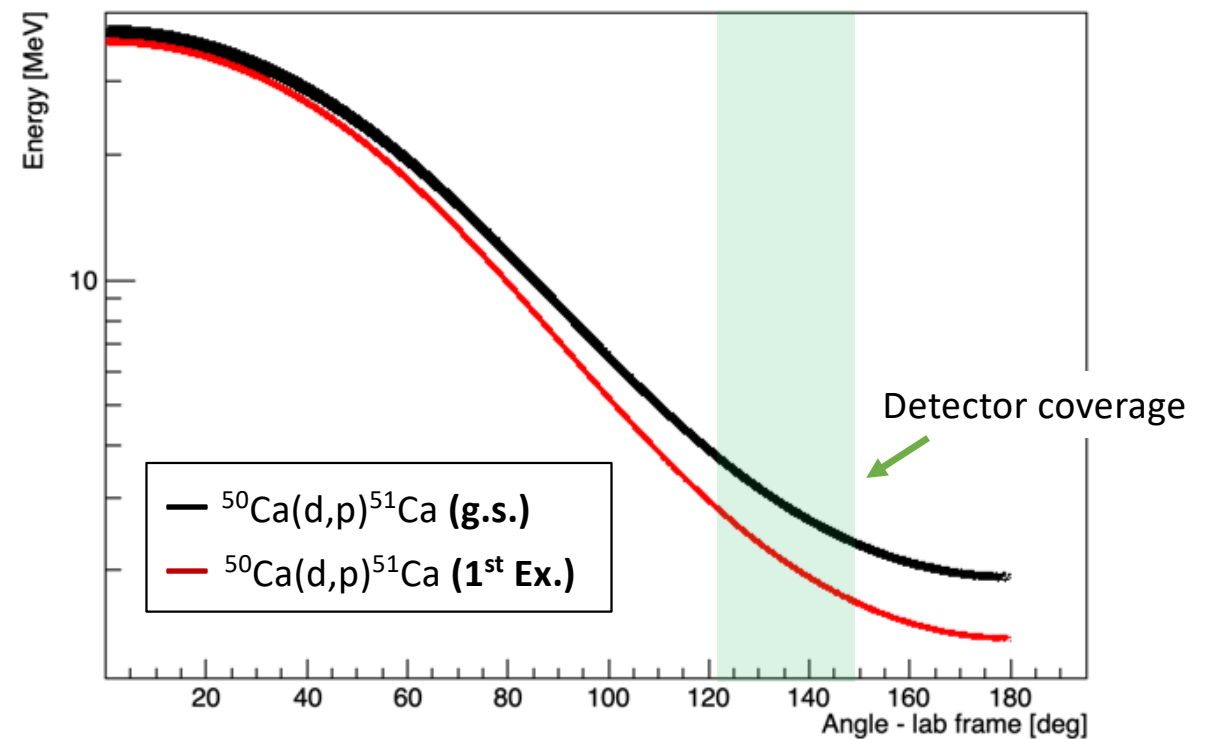
- High reaction cross section
- Distinguishable energy for different states

Upstream detector

- **Annular silicon detector** array
- Wide angle coverage
- Light particles

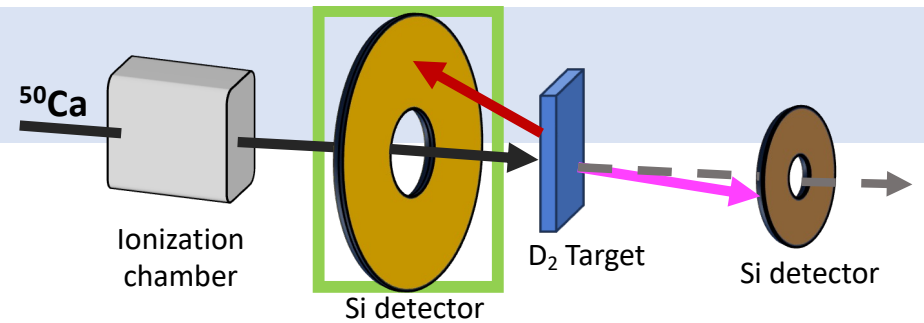


Simulated kinematic plot : proton

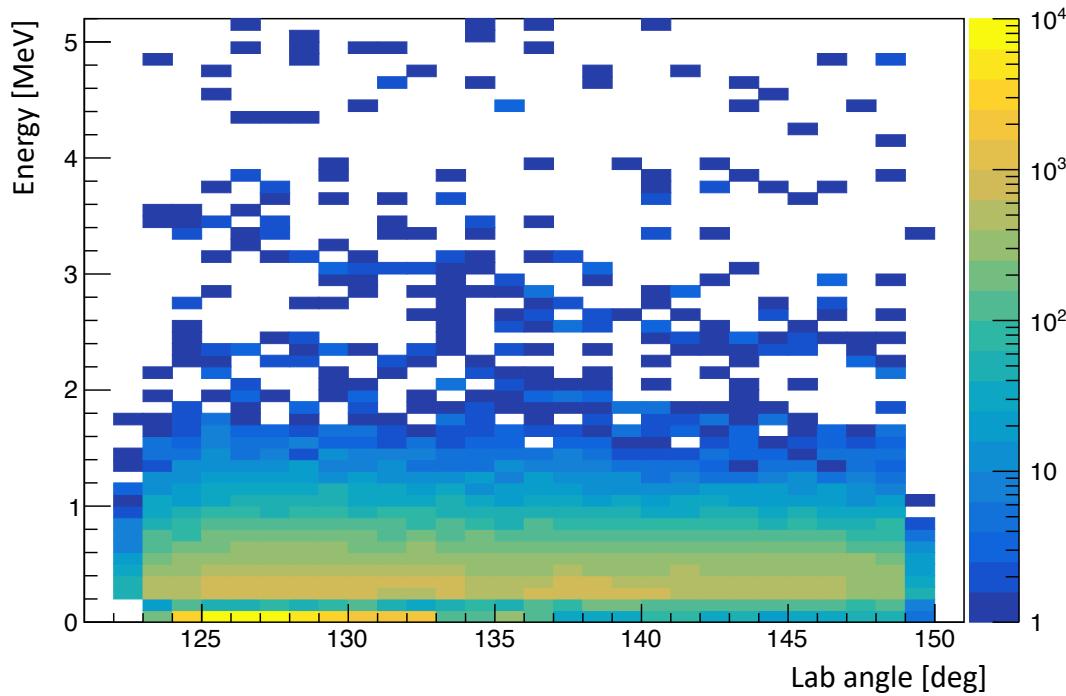


Proton detection

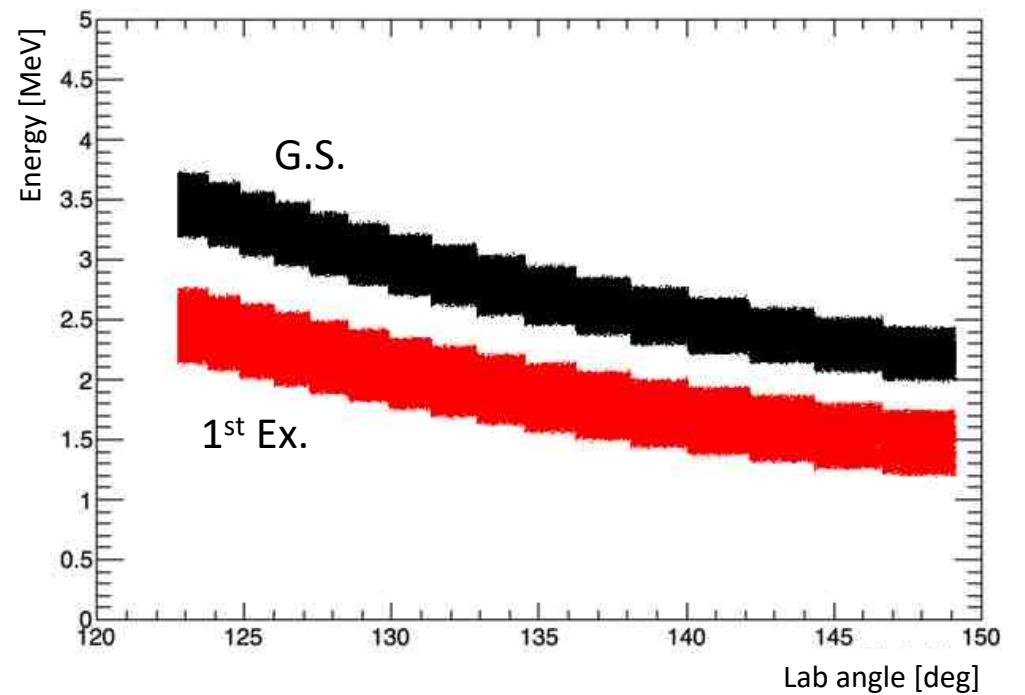
Energy deposit in upstream detector:



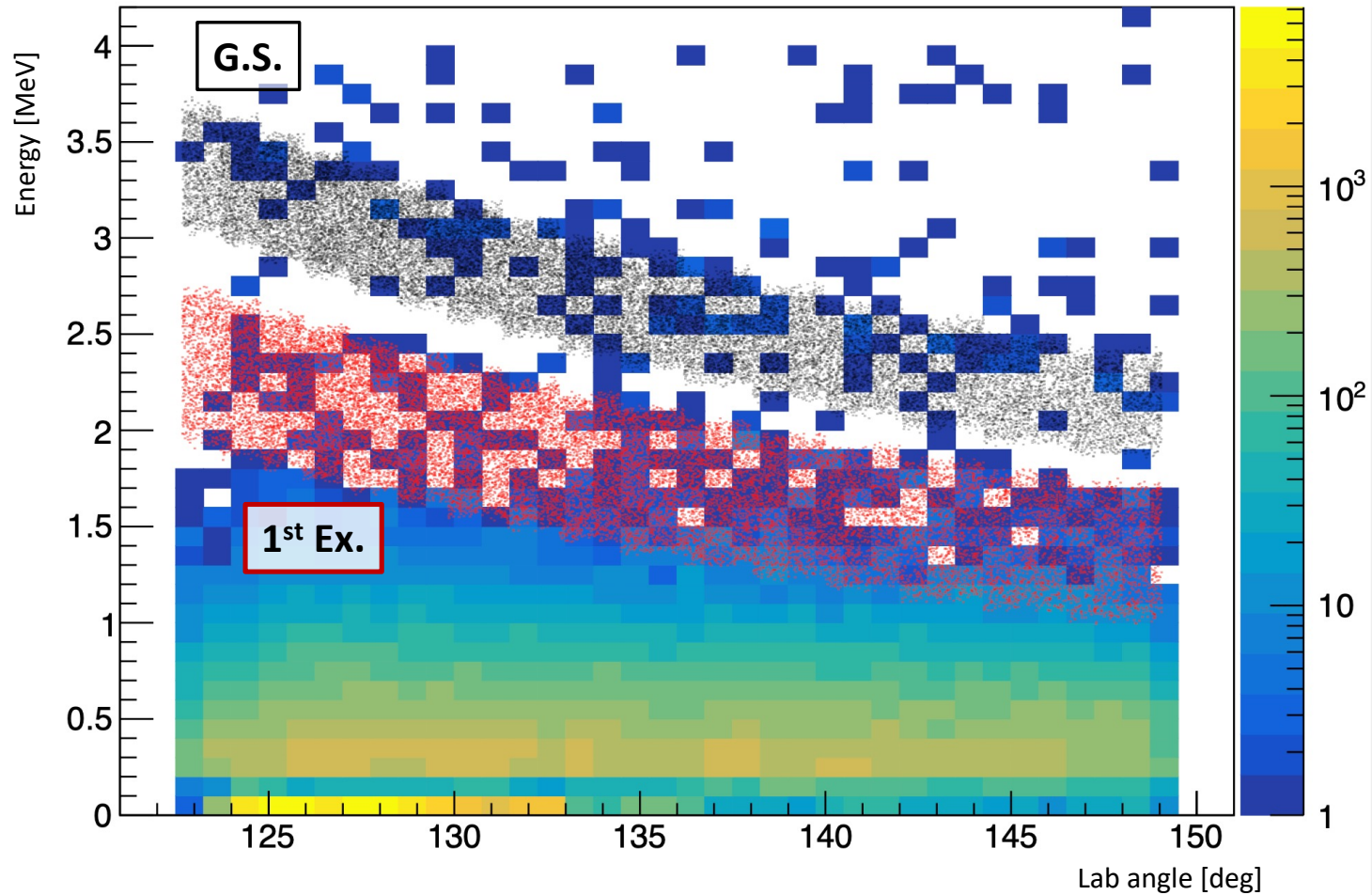
Data



Simulation



Proton detection



Identification of ground / excited state

Missing mass technique - $^{50}\text{Ca}(d,p)^{51}\text{Ca}$

$$Q = m_{^{50}\text{Ca}} + m_d - m_p - m_{^{51}\text{Ca}}$$

$$m_{^{51}\text{Ca}} = \sqrt{\frac{m_{^{50}\text{Ca}}^2 + m_p^2 - m_d^2 + 2(E_{^{50}\text{Ca}} + m_{^{50}\text{Ca}})}{-2(E_{^{50}\text{Ca}} + m_{^{50}\text{Ca}} + m_d)(E_p + m_p) + 2P_{^{50}\text{Ca}}P_p \cos(\theta_p)}}$$

Q : energy released or absorbed

E_A : **kinetic energy** of particle A

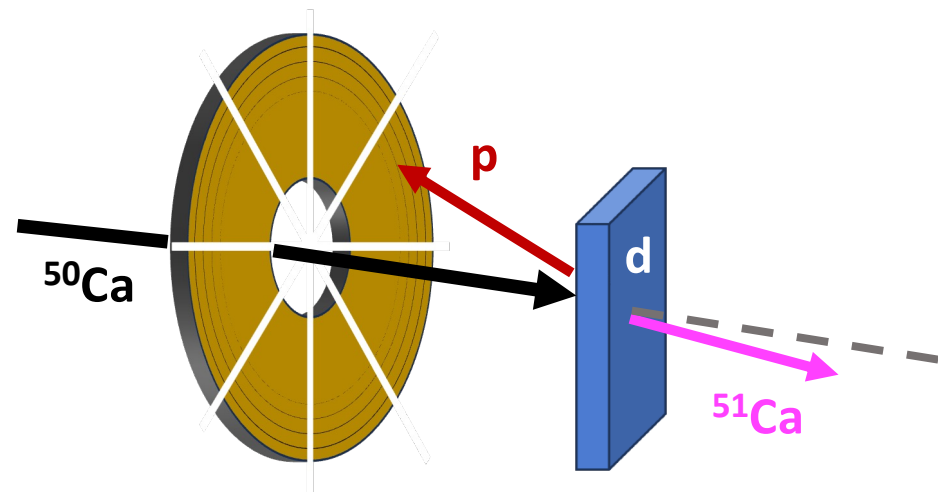
P_A : relativistic **momentum** of A

θ_p : **scattering angle** of proton

Excitation spectrum

$$E_{\text{ex}} = Q_{\text{g.s.}} - Q$$

1st excited state peak around **1.5 MeV**



Identification of ground / excited state

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Q : energy released or absorbed

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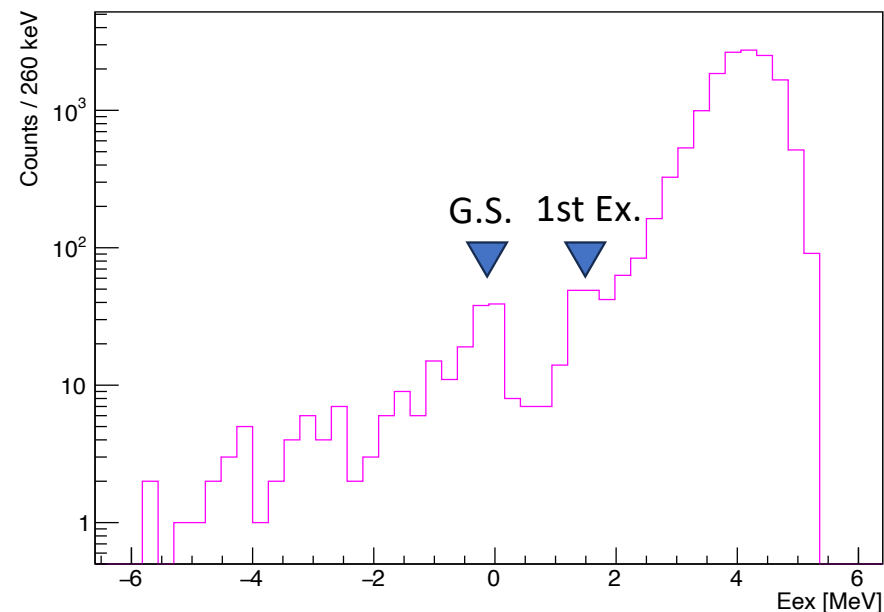
θ_p : scattering angle of proton

Excitation spectrum

$$E_{\text{ex}} = Q_{\text{g.s.}} - Q$$

1st excited state peak around **1.5 MeV**

Excitation spectrum

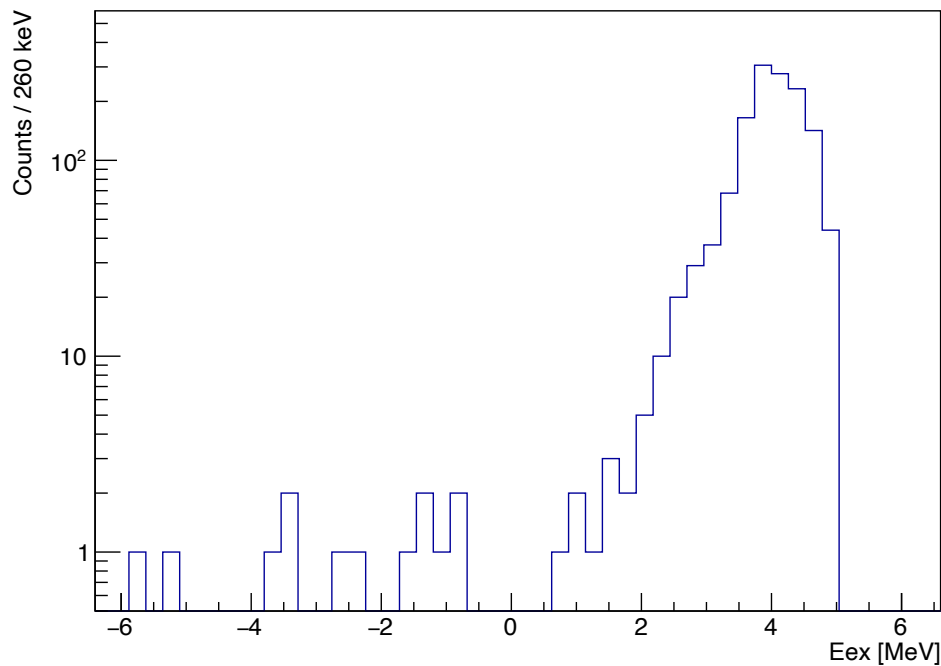


Identification of ground / excited state

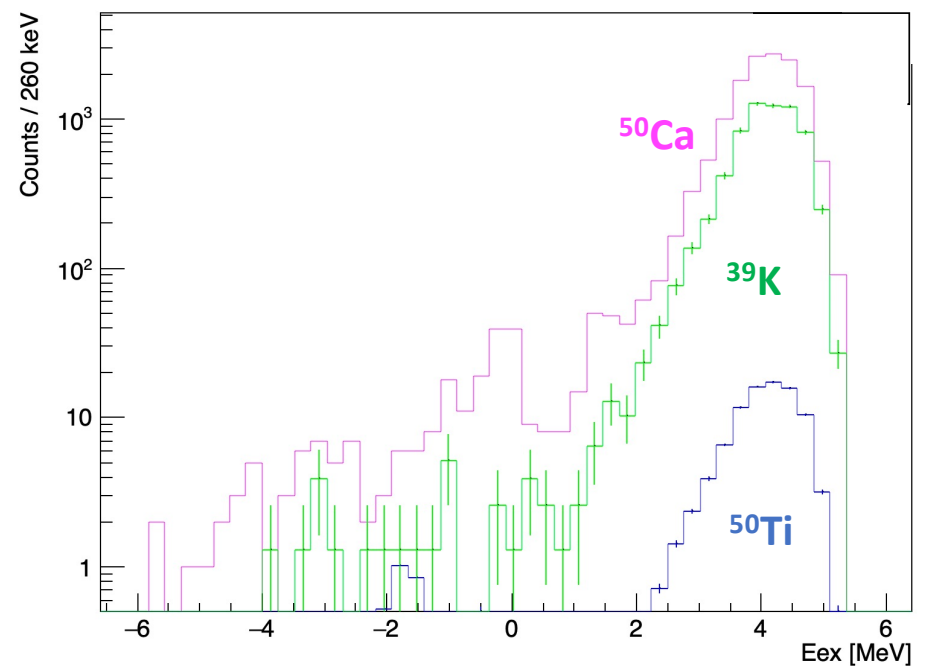
Excitation spectrum

- Signal from **Ag foil** backing
- Contribution from **beam contaminants**

Excitation Spectrum : without D₂ target



Excitation Spectrum



Summary and Future Outlook

- Spectroscopic study of ^{51}Ca via $^{50}\text{Ca}(\text{d,p})^{51}\text{Ca}$ reaction in IRIS facility at TRIUMF.
- Detecting protons from the reaction and investigate the energy of the populated states in ^{51}Ca .
- Clear observation of **ground state** and **1st excited state** (~ 1.5 MeV).
- Resolving contributions from background reaction and beam contaminants.
- Differential cross section of the reaction, provide insights on N=32 shell closure.

Acknowledgement

Dr. Rituparna Kanungo - Supervisor

Dr. Greg Christian - Supervisory committee member

Dr. Ian Short - Supervisory committee member



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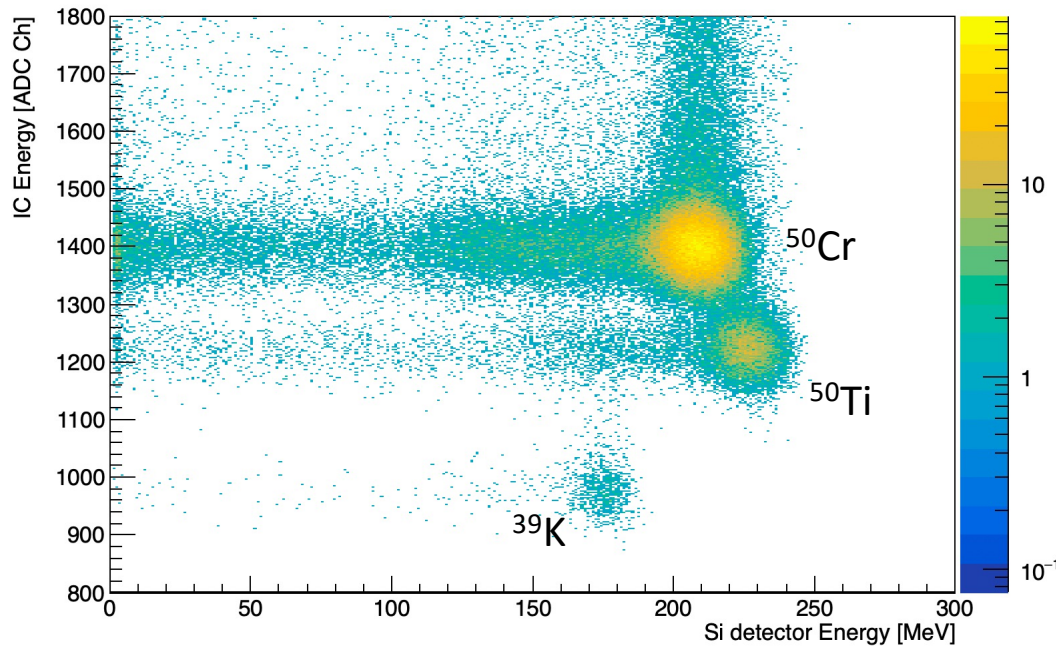
Collaborators:

M. Alcorta, C. Andreoiu, C. Angus, S. Bagchi, N. Bhati, S.S. Bhattacharjee, S. Buck, K. Butler, M. Cavenaile, G. Christian, R. Coleman, G. Desmarais, E.G. Fuakye, P.E. Garrett, G. Grinyer, G. Hackman, K. Kapoor, J. Liang, C. O'Keefe, J. Park, T. Psaltis, M. Rocchini, N. Saei, D. Shah, M. Singh, P. Spagnoletti, M. Talebitaher, S. Upadhyayula, and F. Wu

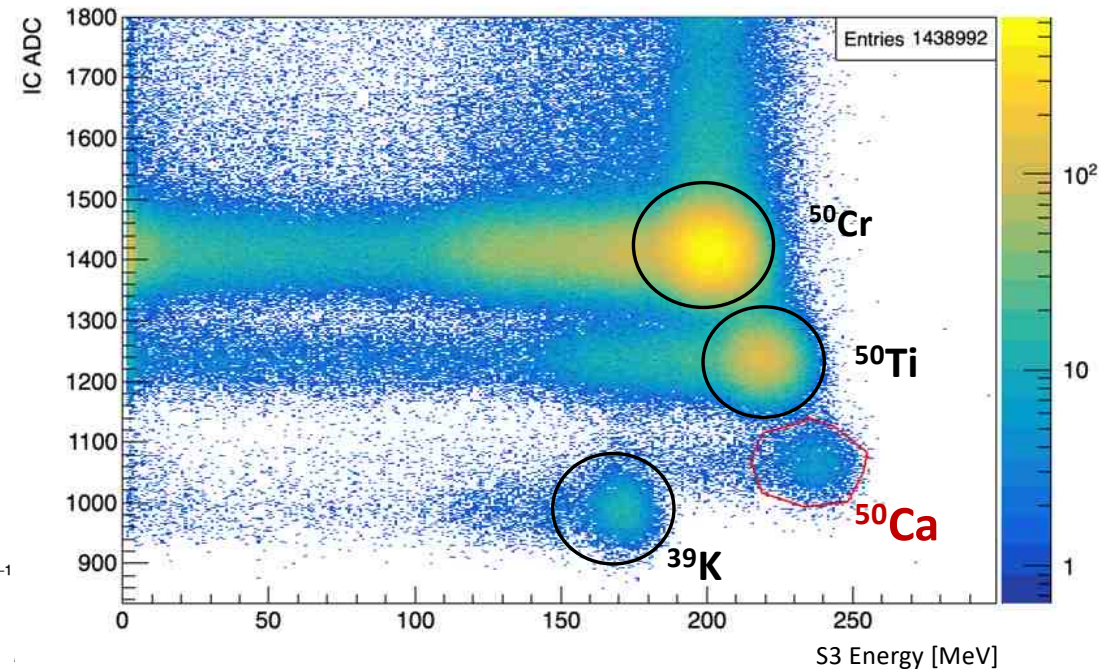


IC – Beam Identification

Without RIB (^{50}Ca) beam

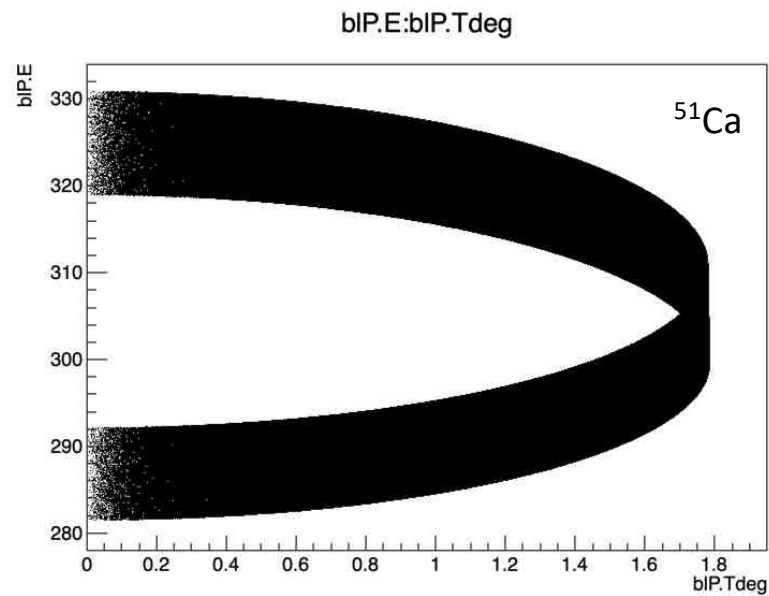
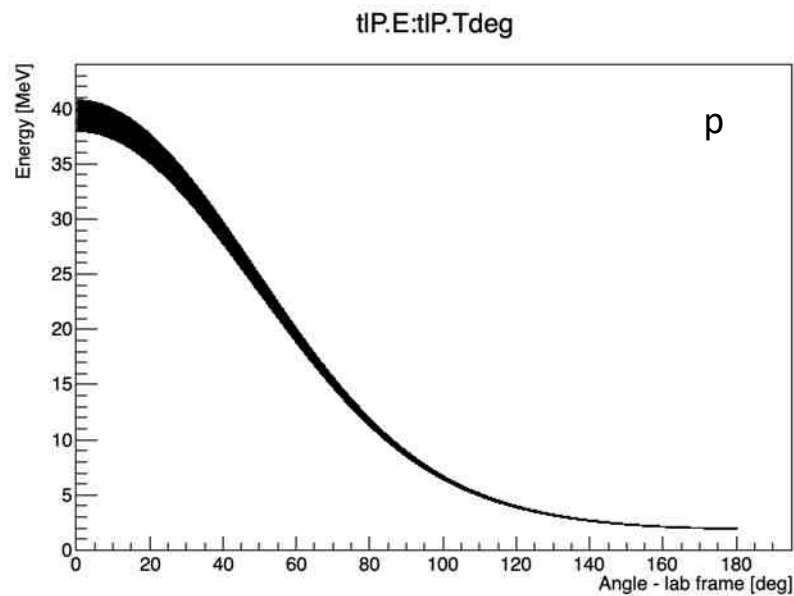


With RIB (^{50}Ca) beam



Simulation - Kinematics

- Detection of **p** and ^{51}Ca :
 - Yu angle coverage: 122.73 deg – 149.09 deg
 - S3d1 angle coverage: 2.65 deg – 8.38 deg



Target Thickness

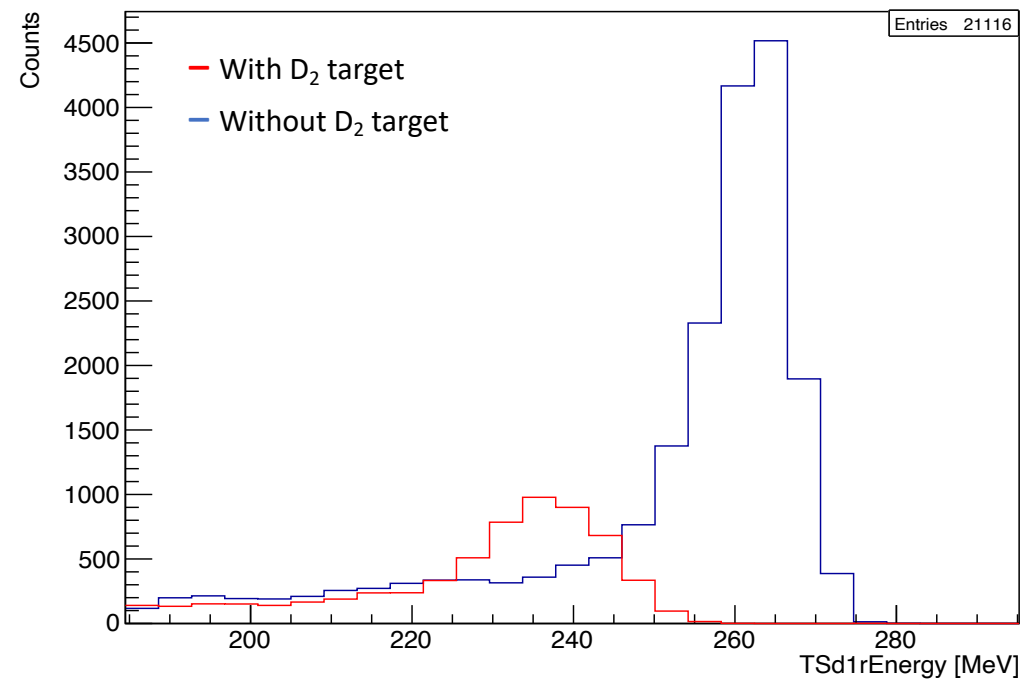
Energy difference between “with-” and “without-target” runs.

$$t = \int_{E_0}^{E_1} \frac{1}{S(E)} dE$$

t: thickness

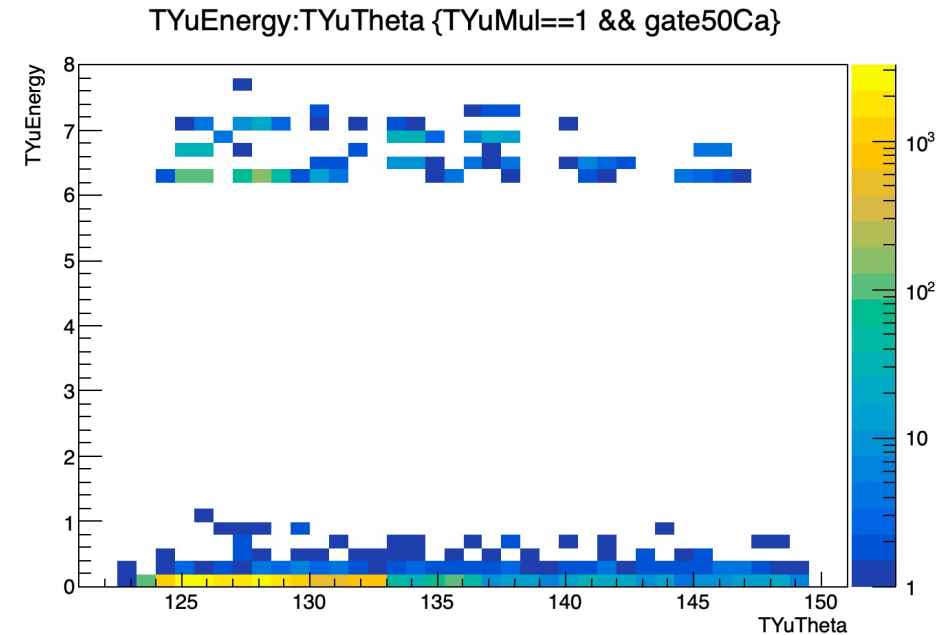
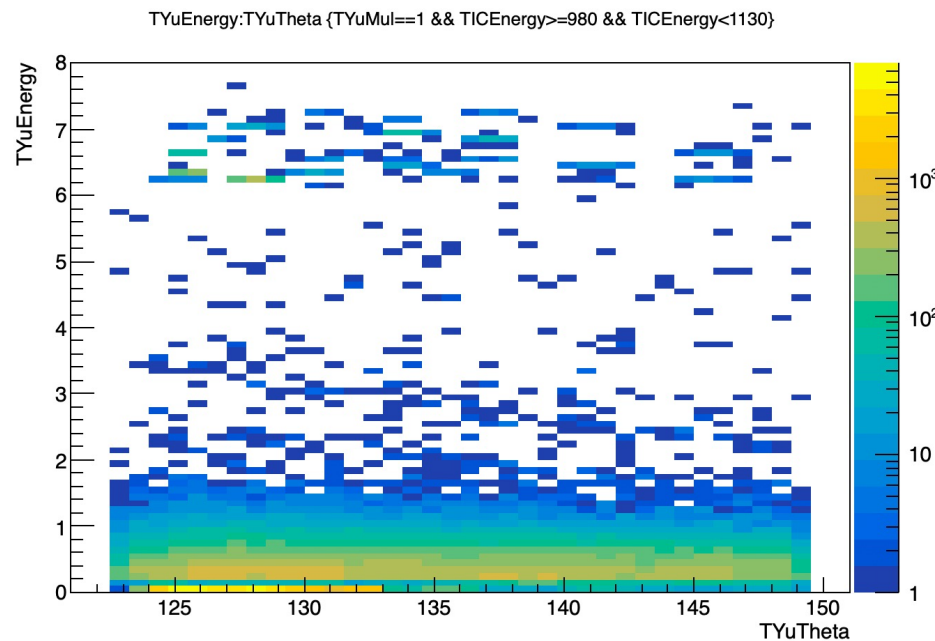
S(E): stopping power (-dE/dx)

Energy peak of ^{50}Ca beam in S3d1 detector



Gate on ^{50}Ca peak

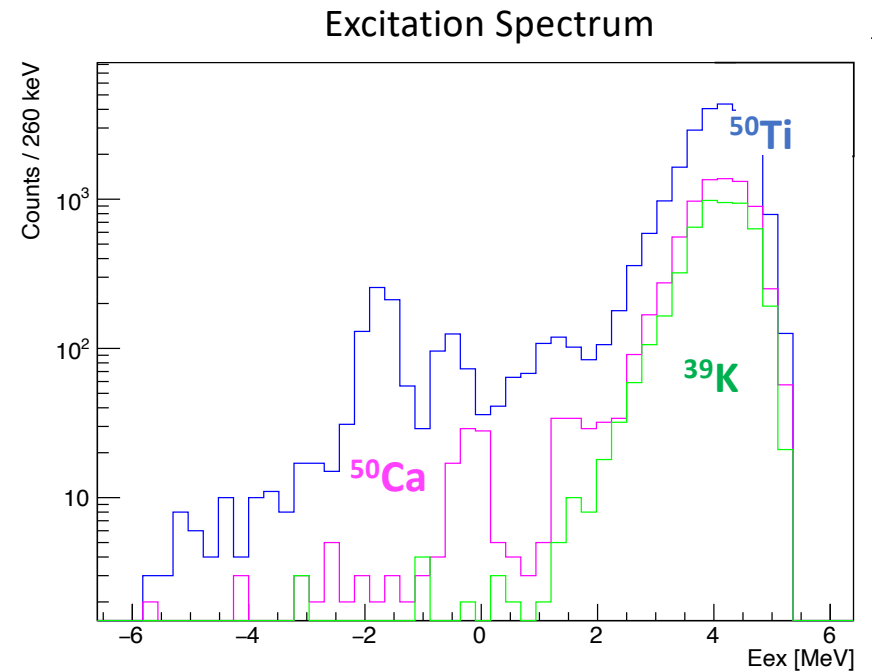
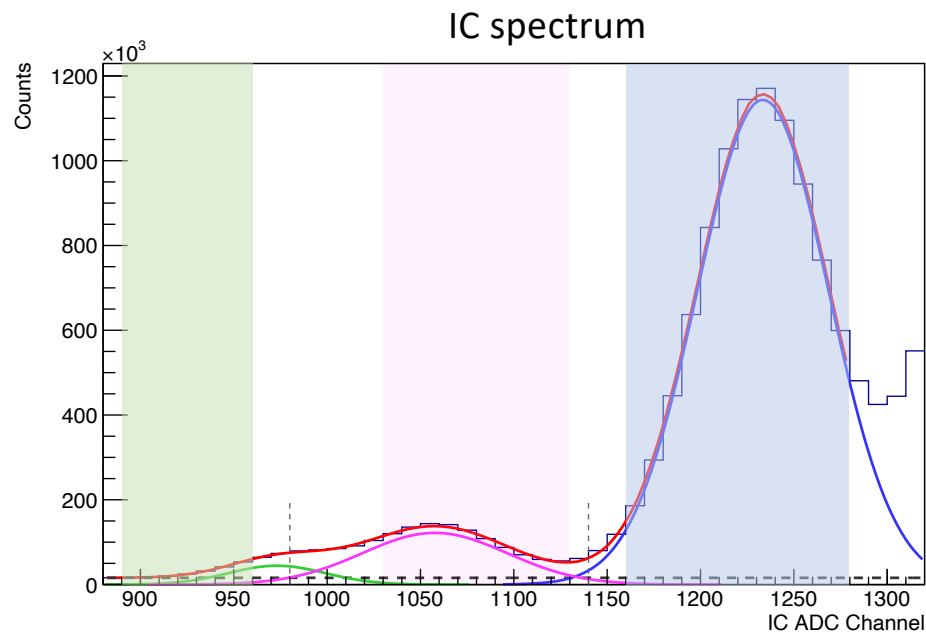
- Gating on the ^{50}Ca peak observed in the IC energy vs Si energy plot
 - Not enough statistics
 - Lose the data in the energy range of interest

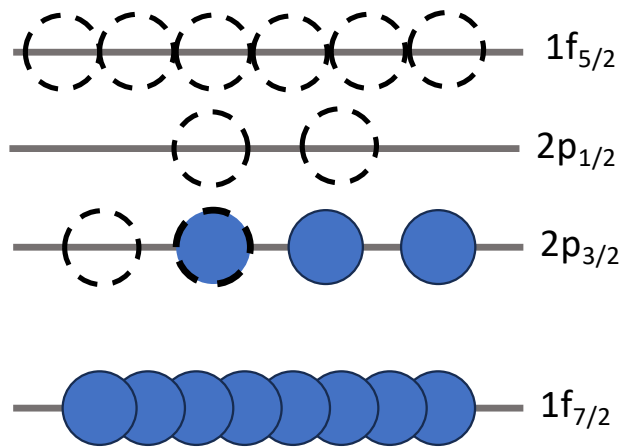


Identification of ground / excited state

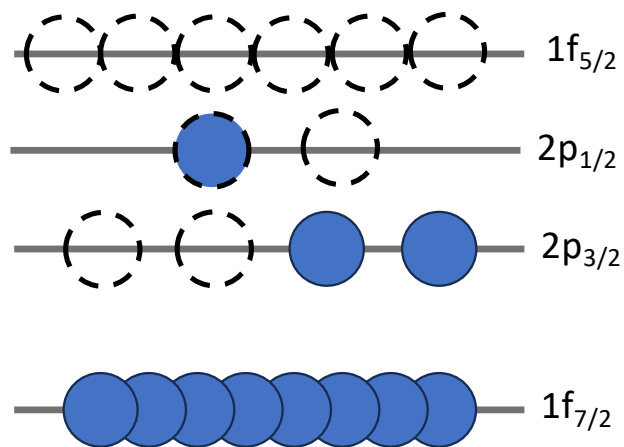
Excitation spectrum

- Contribution from beam contaminants

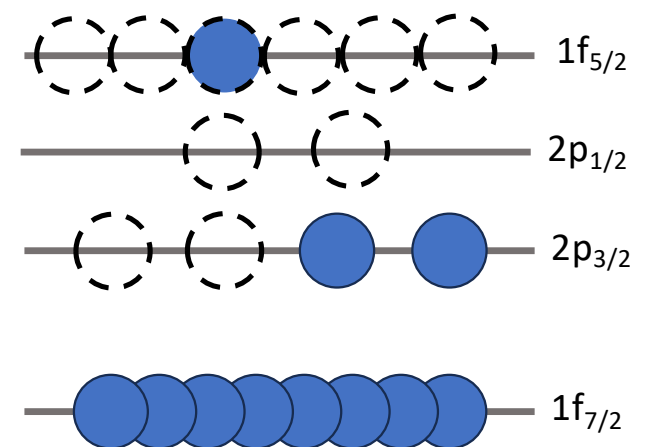




$^{51}\text{Ca}_{3/2-}$ (g.s.)



$^{51}\text{Ca}_{1/2-}$ (1.72 MeV)



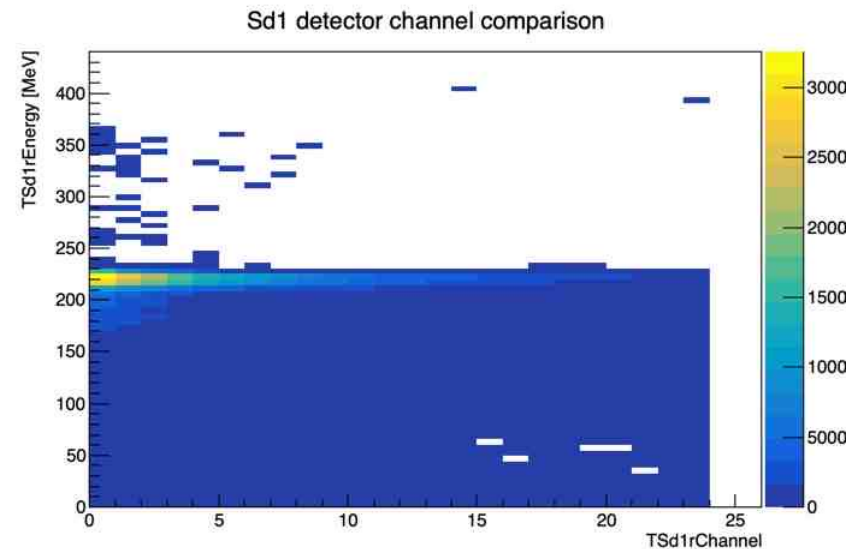
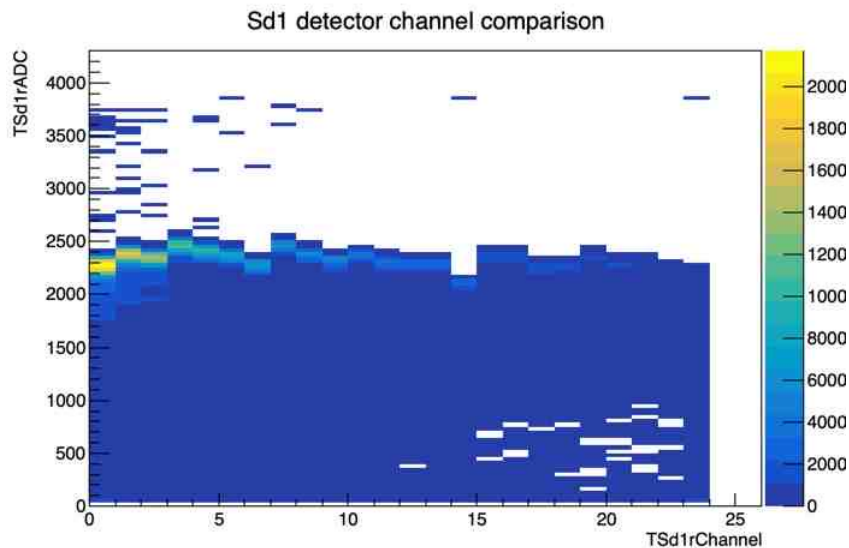
$^{51}\text{Ca}_{5/2-}$ (3.47 MeV)

Detector Calibration

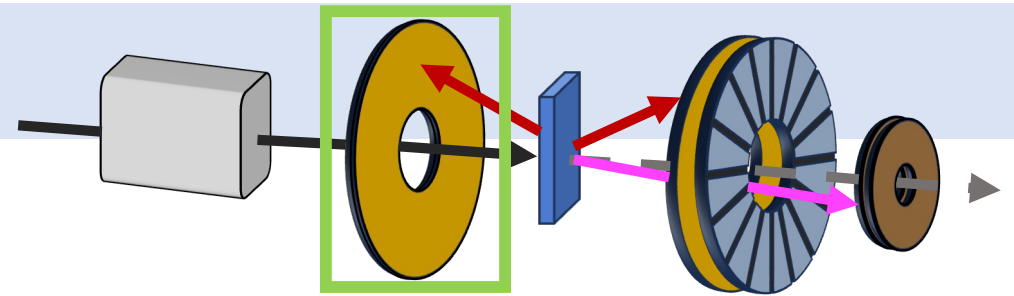
- Alpha source and ^{40}Ar stable beam
- Convert ADC channel to energy value (MeV)

$$E = g(c - p)$$

- Determine gain value g for each channel of the detector



Proton detection

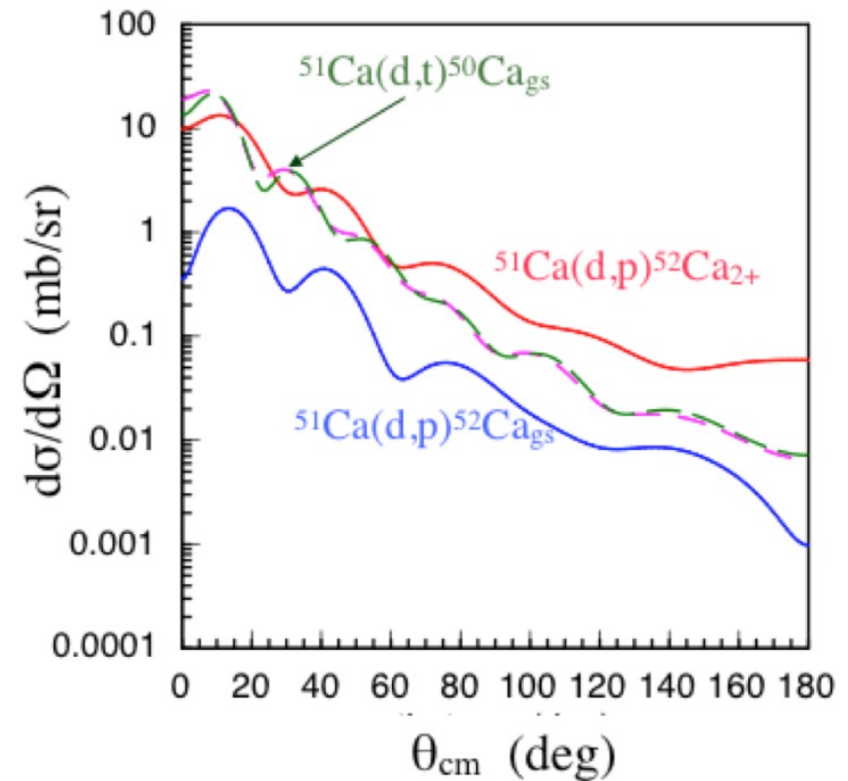


Protons in upstream

- Higher reaction cross section.

Upstream Si detector coverage:

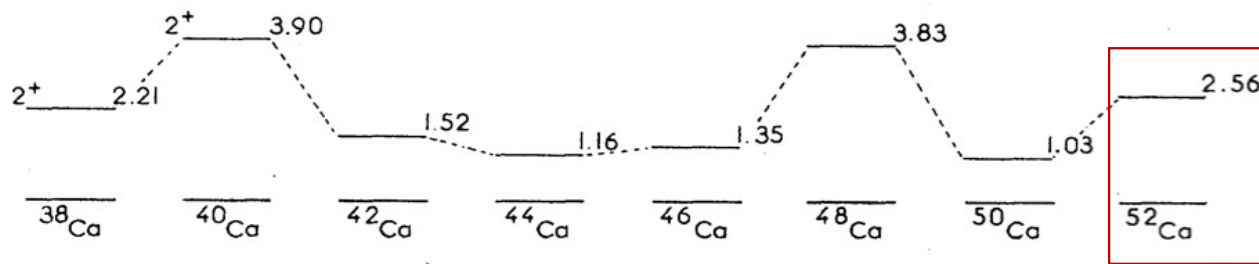
- $\theta_{\text{lab}} = 122^\circ - 149^\circ$
- $\theta_{\text{cm}} \sim 10^\circ - 20^\circ$



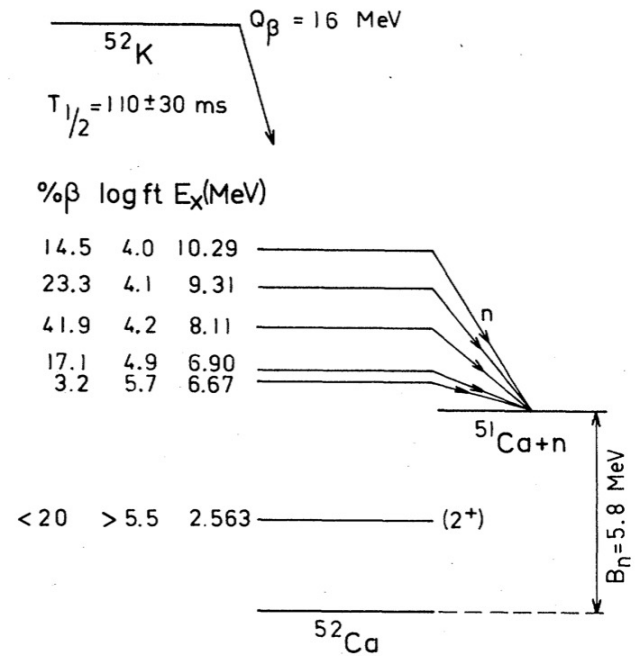
Energy of excited states

An increase in the energy of the first excited state (Huck et al., 1985).

- β -decay of ^{52}K
- Shell level scheme of ^{52}Ca
- Sign of shell closure at $N = 32$



Energy of first excited state of Ca isotope chain
Huck et al. (1985)

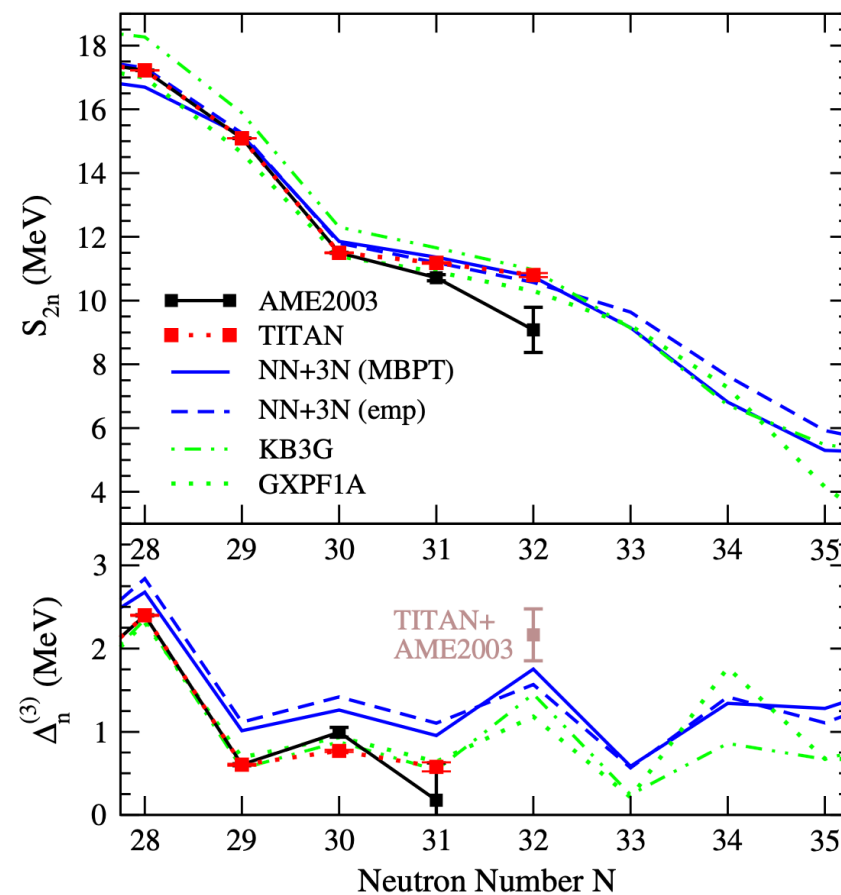


Level scheme of ^{52}Ca
Huck et al. (1985)

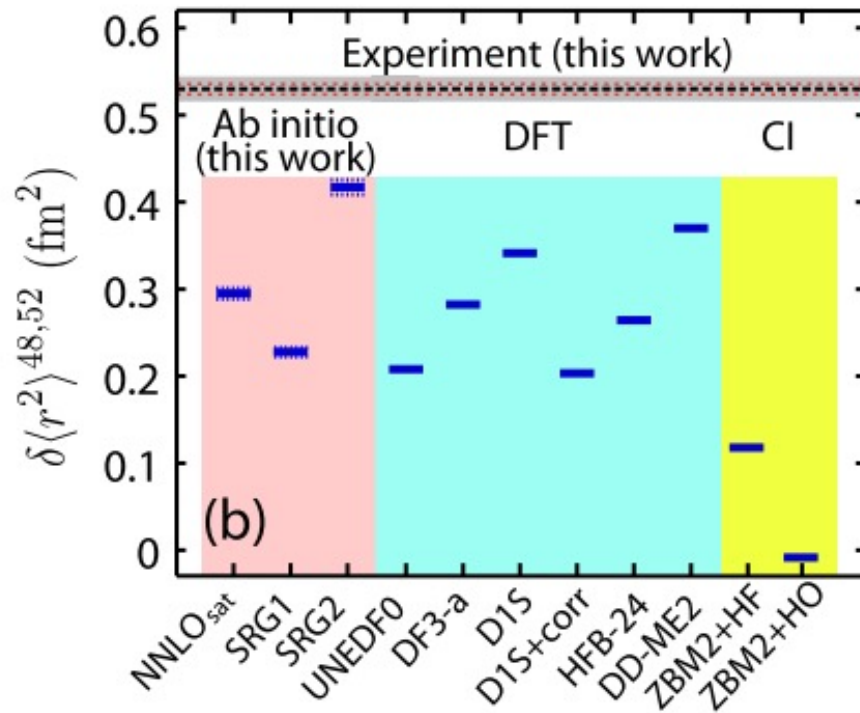
Neutron separation energy

Direct mass measurement of **K** and **Ca** isotopes (Gallant et al., 2012):

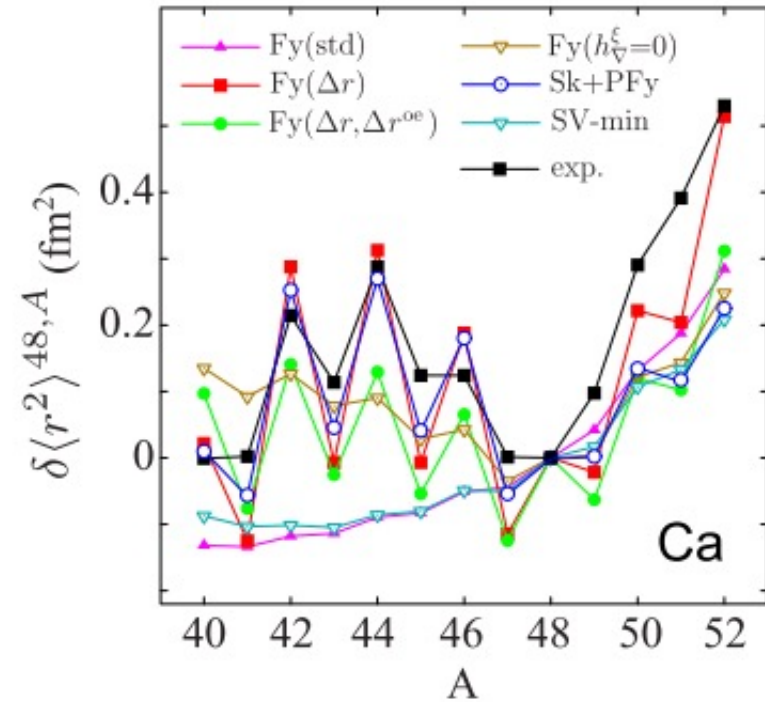
- More precise and accurate mass measurement
- Measurement of neutron separation energy (S_{2n})
- ^{52}Ca more bound by **1.74 MeV** than existing dataset.
- In agreement with the modern theoretical calculations



Charge radii of ^{52}Ca



Ruiz et al. (2016)



Reinhard et al. (2017)

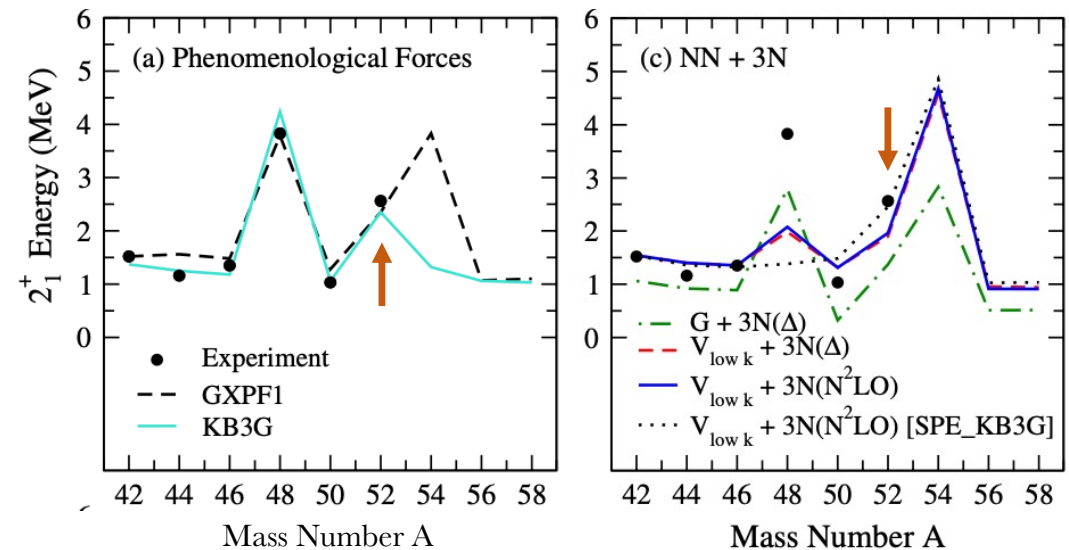
Theoretical aspect

Development of shell model/ interactions:

- Prediction of shell configuration in unstable nuclei.
- More realistic, reaching to non-observable properties.

Signs of shell closure at $N = 32$.

Discrepancy between experiment data and models.



Holt et al. (2012)

Radioactive ion beam – ^{50}Ca

- Beam contaminants share a similar A/Q

