

Measuring Cross Section Enhancement of the ${}^7\text{Li}({}^1\text{H},\alpha)\alpha$ Reaction in Lithium Bearing Materials

Preliminary Results

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February 13, 2025

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Outline

Project Background

Theory

Initial Results

Next Steps

Project Background

Project goal: Extend measurement of cross section enhancement

- outstanding question about source of enhancement
- few measurements for ${}^7\text{Li}({}^1\text{H},\alpha)\alpha$
- more for ${}^2\text{H} + {}^2\text{H}$
- exploratory

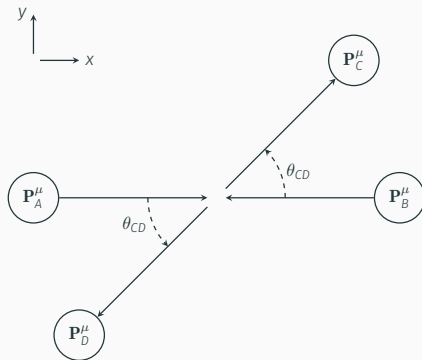
Potential benefit to power generating fusion technology

- directly
- wall materials
- fuel breeding
- other?

Theory

Nuclear Fusion

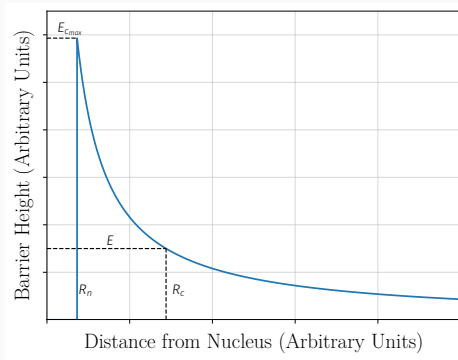
Inelastic scattering of nuclei



Nuclear Fusion

Inelastic scattering of nuclei

Must overcome, or tunnel through, coulombic barrier



Nuclear Fusion

Inelastic scattering of nuclei

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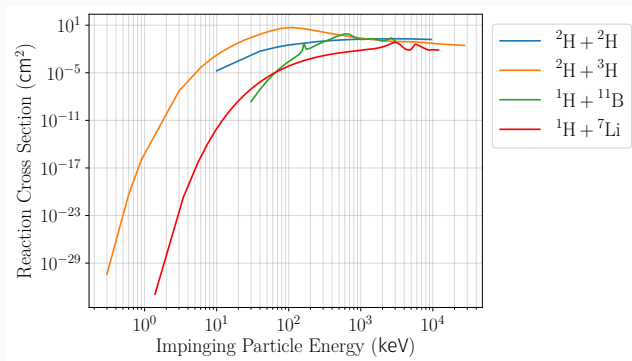
Reaction is probabilistic

$$\sigma(E) = \frac{S(E)}{E} \exp\left(-\sqrt{\frac{E_G}{E}}\right) \quad (1)$$

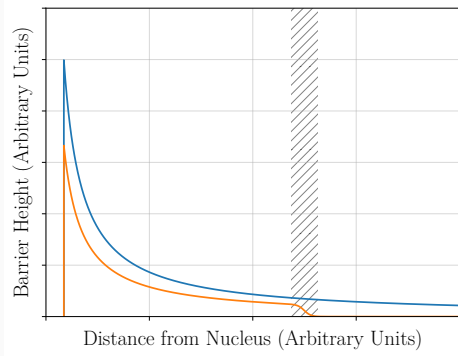
- $S(E)$ Astrophysical S-factor
- E is the CM energy
- E_G is the Gamow Energy— $E_G \equiv (\pi\alpha Z_a Z_b)^2 m_a m_b c^2 / (m_a + m_b)$

Measured Cross Sections

Measured values of cross section for selection of reactions of interest



Electrostatic Screening

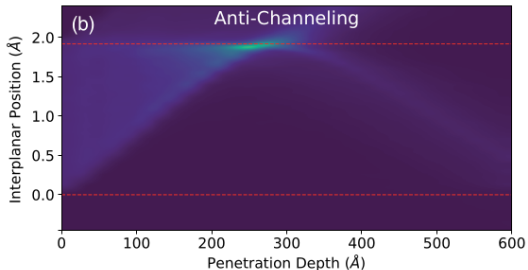
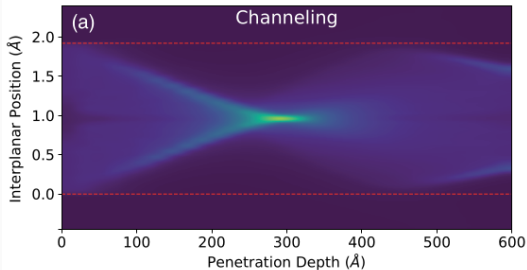
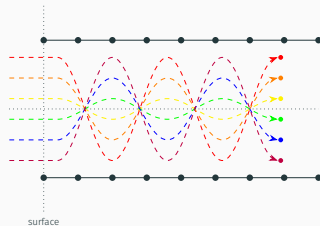


Cross Section Enhancement

Electrostatic Screening

Channeling and Anti-channeling

- Figure by Bagli et al [1]



Cross Section Enhancement

Electrostatic Screening

Channeling and Anti-channeling

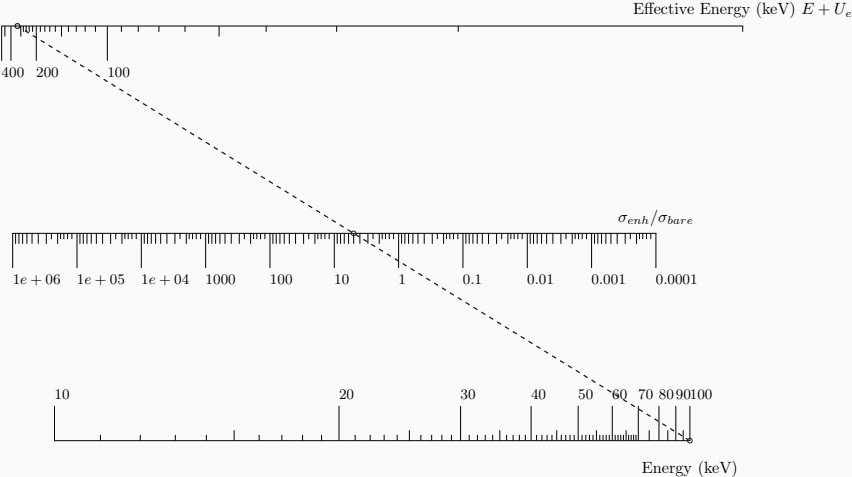
Equation

$$\sigma_{enh} = \frac{S(E)}{\sqrt{E(E + U_e)}} \exp\left(-\sqrt{\frac{E_G}{E + U_e}}\right) \quad (2)$$

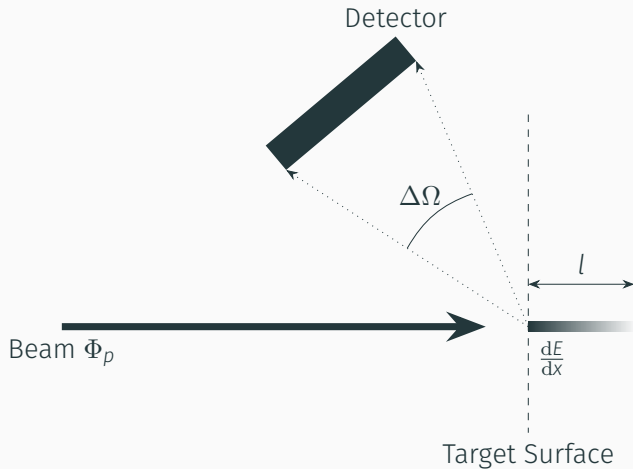
Where U_e is enhancement energy

$$F = \frac{\sigma_{enh}}{\sigma_{bare}} \quad (3)$$

Energy Enhancement Nomograph



Beam-Target Experiments



Reaction rate

$$\frac{dR}{dt} = \Phi_p N_t l \sigma(E) \quad (4)$$

$$Y = n_p N_t l \Delta\Omega \sigma(E) \quad (5)$$

projectile count	n_p
interaction len.	l
solid angle cov.	$\Delta\Omega$
kinematic solid angle	$\frac{d\Omega}{d\Omega'}$
target num. dens.	N_t

Determining Cross Section

Thick Target Yield

$$Y_{\infty} = \frac{n_p N_A \omega_x \Delta \Omega}{4\pi M} \int_{E_i}^0 \sigma(E) \left(\frac{dE}{dx} \right)^{-1} \left(\frac{d\Omega}{d\Omega'} \right)^{-1} dE \quad (6)$$

Differential Yield

$$\frac{dY_{\infty}}{dE} = \frac{n_p N_A \omega_x \Delta \Omega}{4\pi M} \sigma(E) \left(\frac{dE}{dx} \right)^{-1} \left(\frac{d\Omega}{d\Omega'} \right)^{-1} \quad (7)$$

Cross Section from Yield

$$\sigma(E) = \frac{4\pi M}{n_p N_A \omega_x \Delta \Omega} \frac{dY_{\infty}}{dE} \frac{dE}{dx} \frac{d\Omega}{d\Omega'} \quad (8)$$

$^1\text{H} + ^7\text{Li}$ Measurements in Litterature

Beam	Target	Measured U_e (eV)	Ref.
^7Li	Kapton	<600	[2]
	$^1\text{H}-\text{Pd}_{2,34}$	<300	
	Graphite ($^1\text{H}\text{C}_{16,9}$)	10 003(400)	[3]
	$^1\text{H}\text{Pd}_{4,76}$	3 600(700)	
	TiH	3 900(400)	
	$^1\text{H}\text{W}_{23,8}$	5 900(900)	
^1H	$^7\text{Li}\text{Pd}_{99}$	3 790(330)	[4]
	$^7\text{Li}_2\text{WO}_4$	185(150)	
	^7Li	1 280(60)	

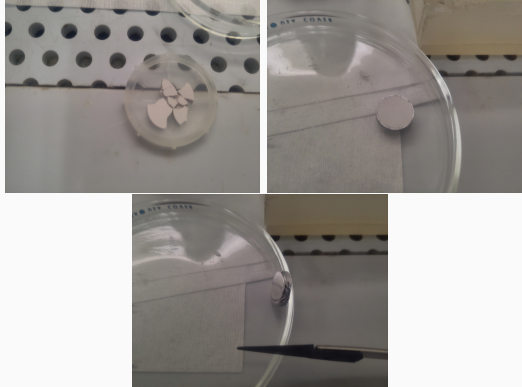
Initial Results

Samples Tested

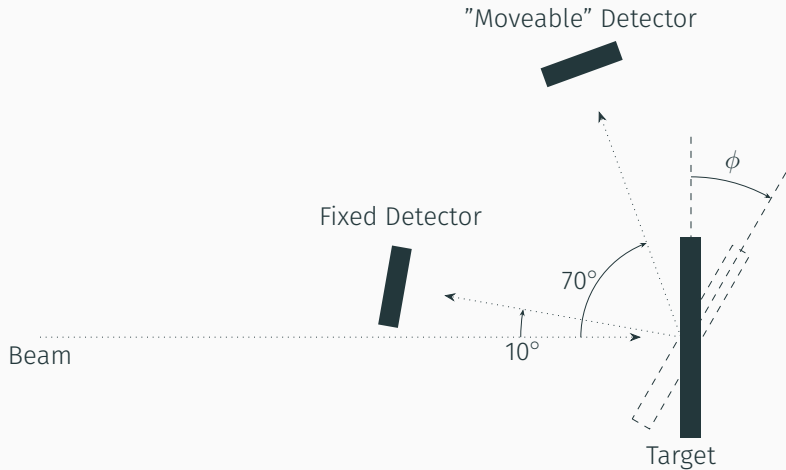
Material	Chem. Form.	No. Samples	Angle Range (°)
Lithium Tungstate	Li_2WO_4	4	0
Lithium Manganate	LiMn_2O_4	4	
Lithium Titanate	$\text{Li}_4\text{Ti}_5\text{O}_{12}$	4	
Lithium Iron Phosphate	LiFePO_4	4	
Lithium Flouride	LiF	1	-0.5 - 1
Lithium Niobate	LiNbO_3	2	

Sample Preparation

- Powdered samples pressed
- Aluminum cup for support
- 15 min under 10^4 kg
- Processed and shipped under atmosphere
- measurements contracted out to Western University



Western Beamline Configuration

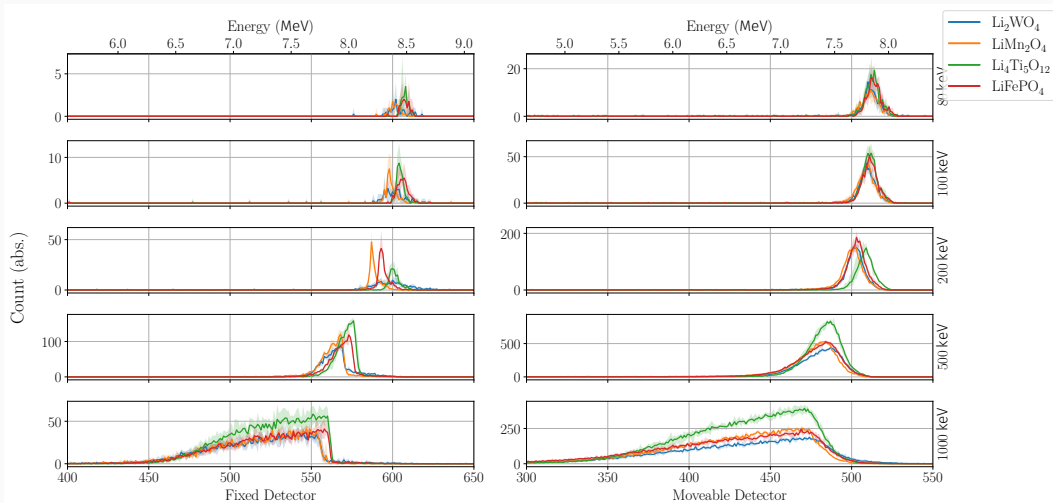


Western Experiment Parameters

Energy keV	Dose μC
80	100
100	100
200	20
500	5
1000	1

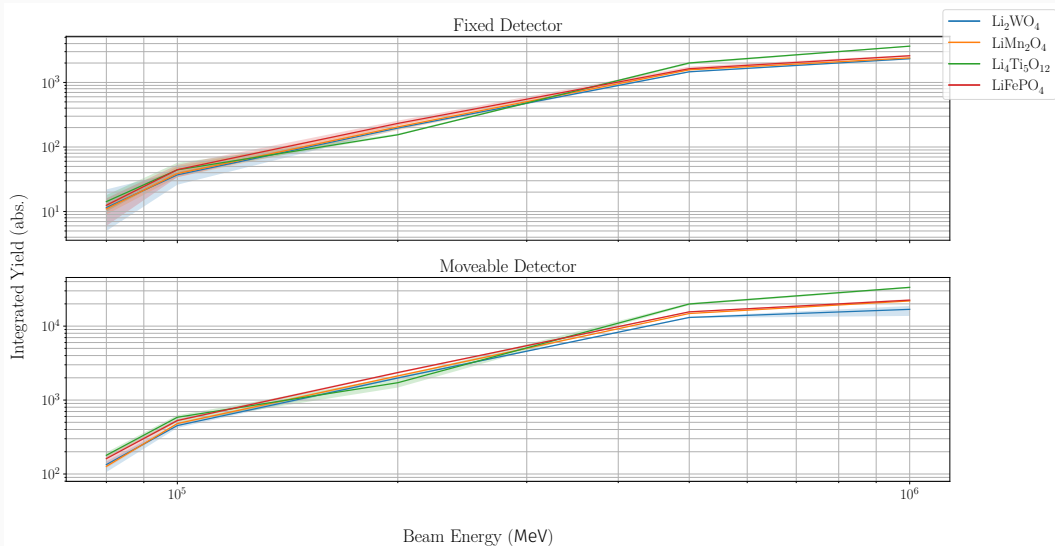
	Fixed	Moveable
Area mm^2	50	450
Solid Angle sr	0.037	0.380
Dist. to Targ. cm	6.9	6.9
Angle. $^\circ$	10	70

Measured Results: Raw Yield

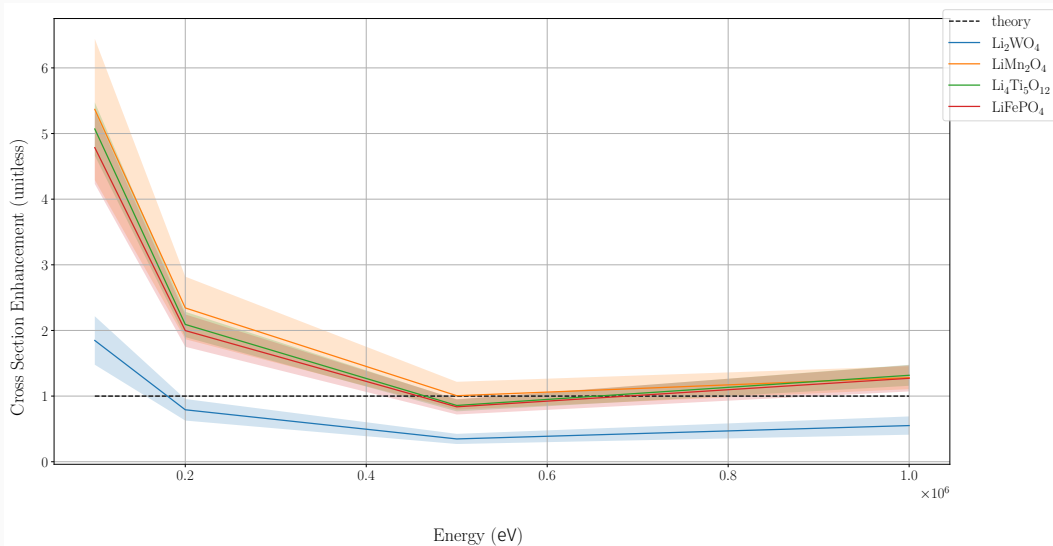


Channel

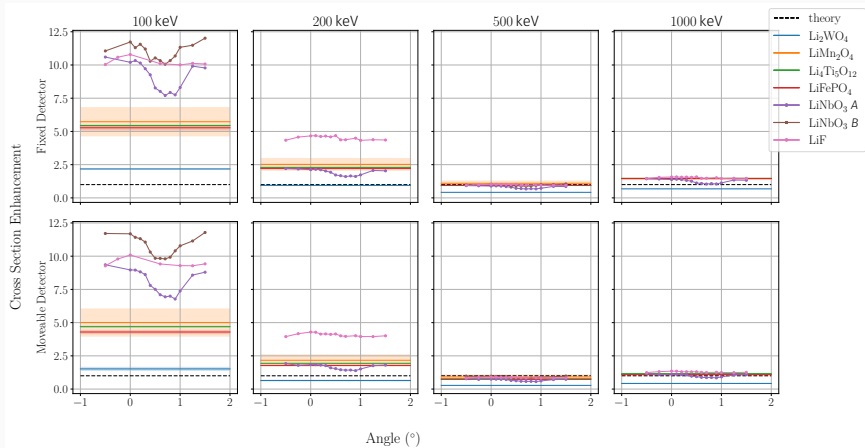
Measured Results: Integrated Yield



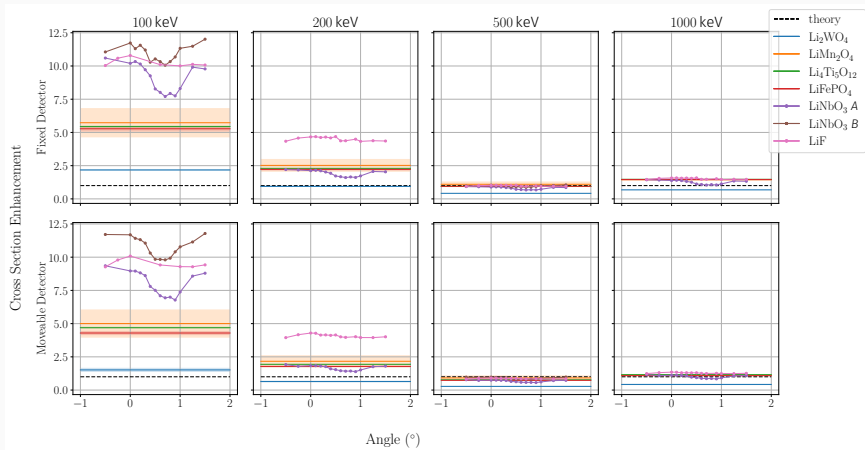
Measured Results: Amorphous



Measured Results: With Crystalline Targets



Measured Results: With Crystalline Targets

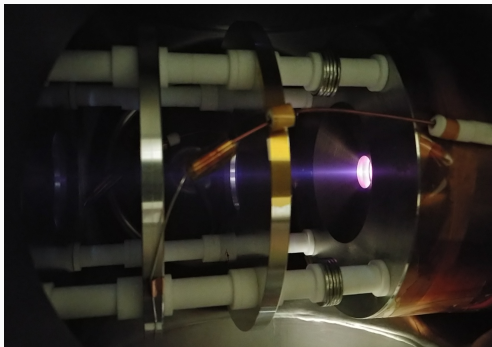


- Beam current nA— long runs
- High cost limited runtime
- low counts at low energies
- need more energy steps

Next Steps

Transitioning to in-house beamline

- higher current 1 mA
- will conduct more measurements in smaller energy steps





SOLEINIUM



Natural Sciences and Engineering
Research Council of Canada

Conseil de recherches en sciences
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Thank You— Questions?

Backmatter

- [1] E. Bagli, D. De Salvador, L. Bacci, *et al.*, “**Enhancement of the Inelastic Nuclear Interaction Rate in Crystals via Antichanneling,**” *Phys. Rev. Lett.*, vol. 123, no. 4, p. 044 801, Jul. 2019, ISSN: 1079-7114. DOI: [10.1103/PhysRevLett.123.044801](https://doi.org/10.1103/PhysRevLett.123.044801).
- [2] M. Lipoglavšek, I. Čadež, S. Markelj, P. Pelicon, and P. Vavpetič, “**Electron screening in the $1\text{H}(7\text{Li},\alpha)4\text{He}$ reaction,**” *European Physical Journal A*, vol. 44, no. 1, pp. 71–75, Apr. 2010, ISSN: 1434-601X. DOI: [10.1140/epja/i2010-10937-7](https://doi.org/10.1140/epja/i2010-10937-7).
- [3] A. Cvetinovic, M. Lipoglavsek, S. Markelj, and J. Vesic, “**Molecular screening in nuclear reactions,**” *Physical Review C*, vol. 92, no. 6, p. 065 801, Dec. 2015, ISSN: 2469-9993. DOI: [10.1103/PhysRevC.92.065801](https://doi.org/10.1103/PhysRevC.92.065801).

- [4] J. Cruz, Z. Fülöp, G. Gyürky, *et al.*, “**Electron screening in ${}^7\text{Li}(p,\alpha)\alpha$ and ${}^6\text{Li}(p,\alpha){}^3\text{He}$ for different environments,**” *Physics Letters B*, vol. 624, no. 3, pp. 181–185, Sep. 2005, ISSN: 0370-2693. DOI: [10.1016/j.physletb.2005.08.036](https://doi.org/10.1016/j.physletb.2005.08.036).

Extras

Nuclear Reactions Table

Reactants			Energy and Pathways	Products	
^1H	+	^7Li	$\xrightarrow{17.2 \text{ MeV}}$	$2 \text{ } ^4\text{He}$ + 8.6 MeV	
^1H	+	^{11}B	$\xrightarrow{8.68 \text{ MeV}}$	$3 \text{ } ^4\text{He}$ 2.9 MeV	
^2H	+	^2H	$\xrightarrow[4.03 \text{ MeV}]{50\%}$	^3H 1.01 MeV	^1H 3.02 MeV
			$\xrightarrow[3.27 \text{ MeV}]{50\%}$	^3He 0.82 MeV	$+ \text{ } n^0$ 2.45 MeV