

${}^7\text{Li}$ in the no-core shell model with continuum framework with coupling of mass partitions

Jakub Herko

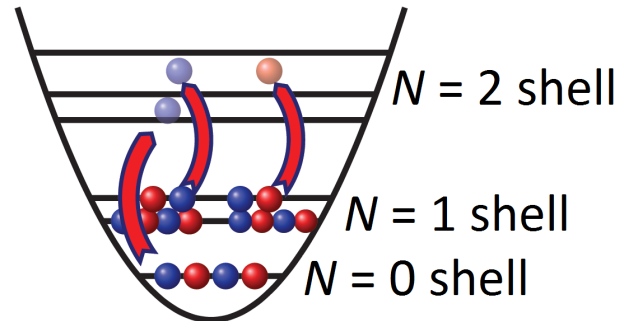
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Outline

- No-core shell model (NCSM)
- No-core shell model with continuum (NCSMC)
- Calculations for ${}^7\text{Li}$ within NCSMC
with coupling of mass partitions ${}^6\text{Li} + n$ and ${}^6\text{He} + p$
 - Bound-state energies
 - Resonances - experimentally observed and predicted
 - Charge-exchange reaction ${}^6\text{Li}(n, p){}^6\text{He}$

No-core shell model (NCSM)

- System of nucleons described by intrinsic Hamiltonian $H = T_{\text{int}} + \sum_{i < j} V_{ij}$
- Schrödinger equation $H|\Psi\rangle = E|\Psi\rangle$ solved as eigenvalue problem for Hamiltonian matrix
- Basis of Slater determinants constructed from harmonic oscillator single-particle states with frequency Ω
- Each basis state carries $N = N_0 + N_{\text{ex}}$ oscillator quanta
 N_0 ... number of oscillator quanta in the lowest Pauli-allowed configuration



- Basis truncated by keeping only states with $N_{\text{ex}} \leq N_{\text{max}}$

Figure courtesy of K. Kravvaris

No-core shell model with continuum (NCSMC)

- Describes both bound and scattering states
- Combines NCSM and NCSM/RGM methods
- NCSM/RGM organizes nucleons into clusters, each described within NCSM
- First, NCSM calculations for the whole system and the clusters are done
- Wave function expanded in terms of NCSM eigenstates and NCSM/RGM binary-cluster states:

$$\Psi = \sum_{\lambda} c_{\lambda} \left| \begin{array}{c} \text{Shell Model} \\ \text{Diagram} \end{array} \right\rangle + \sum_{\nu} \int dr u_{\nu}(r) \left| \begin{array}{c} \text{Binary-Cluster State} \\ \text{Diagram} \end{array} \right\rangle$$

r ... parameter coordinate playing role of distance between clusters

$u_{\nu}(r)$... continuous amplitudes representing intercluster relative motion

- Distribution of nucleons between clusters is called “mass partition”
- Expansion coefficients c_{λ} and amplitudes $u_{\nu}(r)$ calculated by solving NCSMC equations on Lagrange mesh

Figure courtesy of K. Kravvaris

No-core shell model with continuum (NCSMC)

- NCSMC equations can be solved for bound or scattering states by choosing asymptotic form of $u_\nu(r)$
- For scattering states:

$$u_\nu(r \rightarrow \infty) \propto \delta_{\nu i} I_\nu(r) - S_{\nu i} O_\nu(r)$$

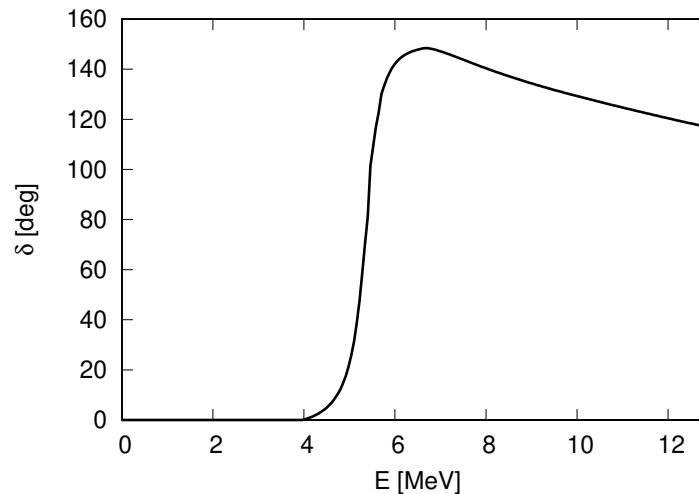
i ... initial channel

$I_\nu(r)$, $O_\nu(r)$... ingoing and outgoing Coulomb wave functions

$S_{\nu i}$... scattering matrix \rightarrow cross sections

- Scattering matrix is unitary \Rightarrow eigenvalues $e^{2i\delta}$

δ ... eigenphase shifts \rightarrow resonances:



Calculations for ${}^7\text{Li}$ within NCSMC with coupling of mass partitions ${}^6\text{Li} + n$ and ${}^6\text{He} + p$

- Motivation: nuclear astrophysics, primordial nucleosynthesis, ${}^3\text{H}$ for fusion energy generation via ${}^6\text{Li}(n, {}^3\text{H}){}^4\text{He}$
- Previous work [1] taking into account relevant mass partitions in separate calculations predicts S -wave $1/2^+$ resonance in ${}^6\text{He} + p$ just above proton separation energy
- No such resonance was experimentally observed [2]
- We include mass partitions ${}^6\text{Li} + n$ and ${}^6\text{He} + p$ in single calculation
- We also predict S -wave $1/2^+$ resonance just above proton separation energy, but only in ${}^6\text{Li} + n$ channel
- Coupling of mass partitions allows for calculation of charge-exchange reaction ${}^6\text{Li}(n, p){}^6\text{He}$

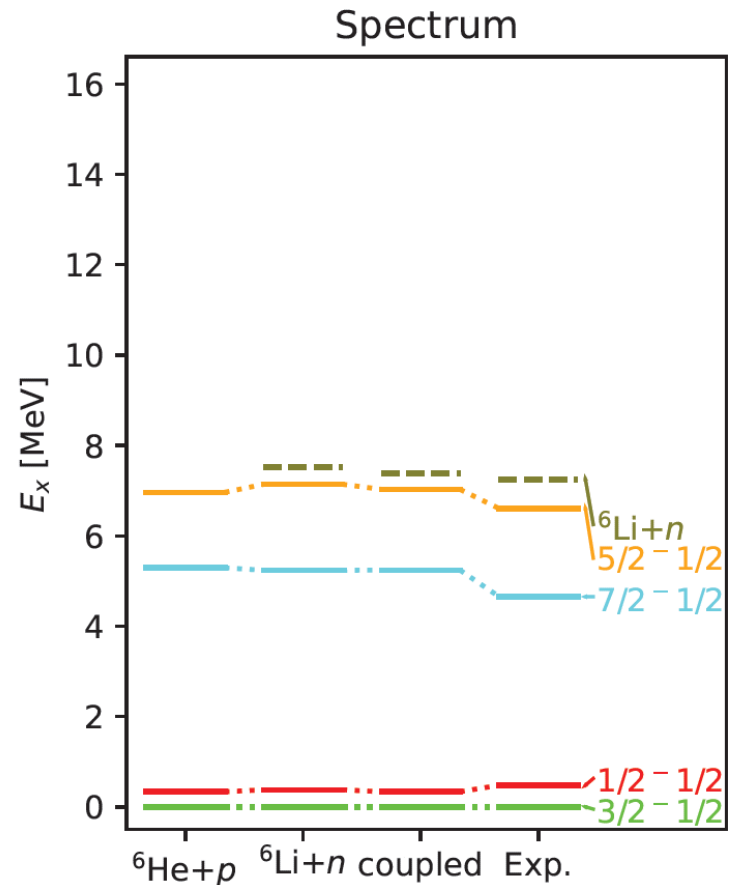
[1] Vorabbi *et al.* Phys. Rev. C **100**, 024304 (2019)

[2] Dronchi *et al.* Phys. Rev. C **107**, L061303 (2023)

Calculations for ${}^7\text{Li}$ within NCSMC with coupling of mass partitions ${}^6\text{Li} + n$ and ${}^6\text{He} + p$

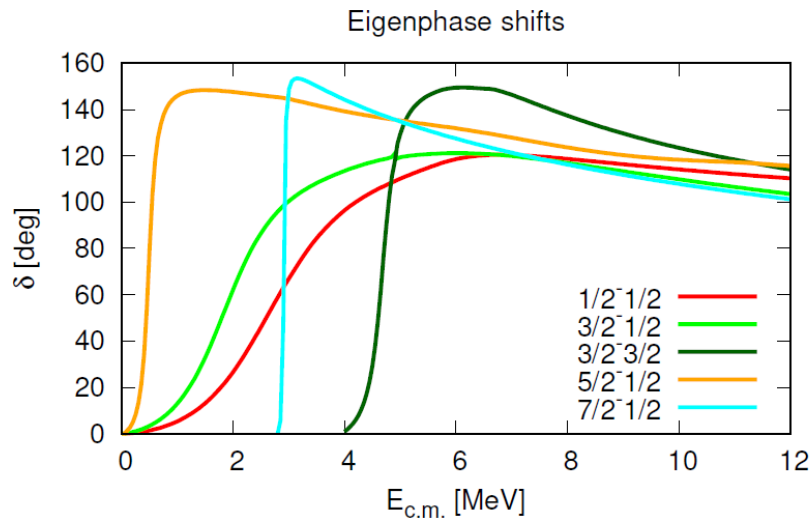
- Chiral N^3LO nucleon-nucleon interaction used
- NCSM eigenstates taken into account:
 - 4 states of ${}^6\text{Li}$: 1^{+0} , 3^{+0} , 0^{+1} , 2^{+1}
 - 2 states of ${}^6\text{He}$: 0^{+1} , 2^{+1}
 - Lowest 12 negative-parity
and lowest 6 positive-parity states of ${}^7\text{Li}$
- $\hbar\Omega = 20 \text{ MeV}$, $N_{\text{max}} = 11$
- Calculated observables: bound-state energies, energies and widths of resonances, cross section of ${}^6\text{Li}(n, p){}^6\text{He}$

Bound-state energies for ${}^7\text{Li}$

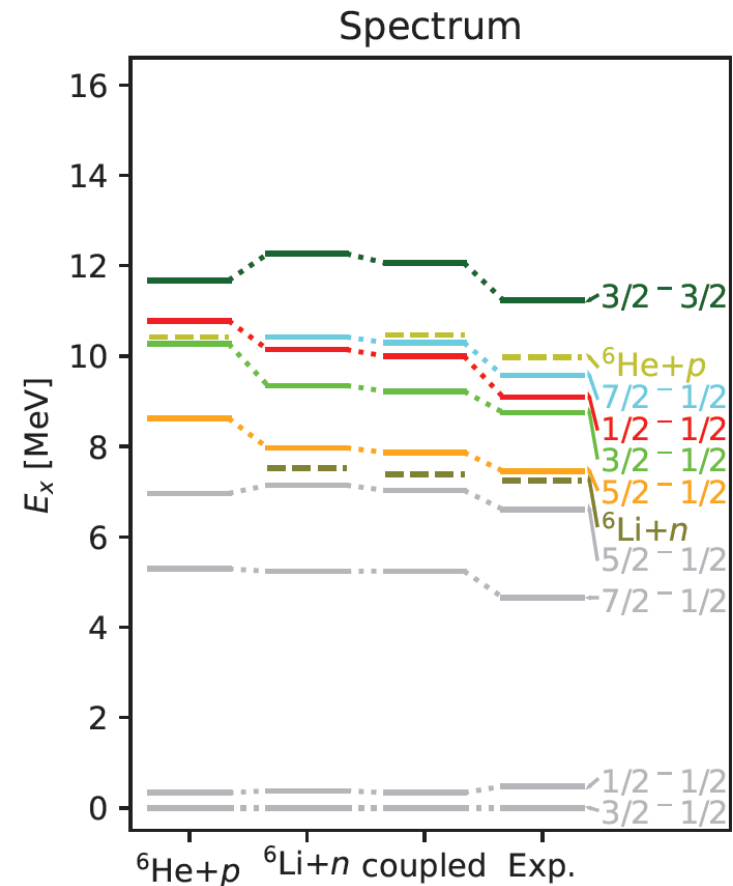


- Bound states reproduced in correct order
- Results almost independent of mass partition - bound states well described by NCSM
- Reasonable agreement between calculated and experimental excitation energies

Resonances in ${}^7\text{Li}$ - experimentally observed

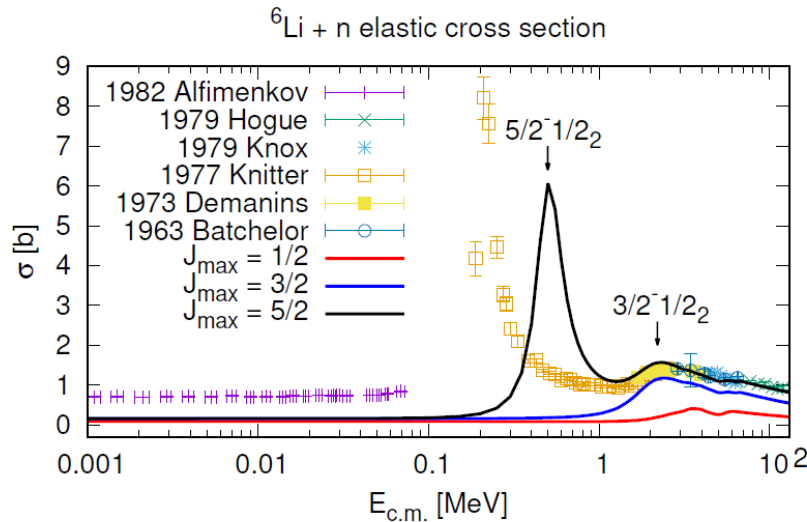


$J^\pi T$	Γ [MeV]			Exp.
	${}^6\text{He} + p$	${}^6\text{Li} + n$	coupled	
$3/2^- 3/2$	0.41	0.36	0.40	0.26
$7/2^- 1/2$		0.04	0.04	0.427
$1/2^- 1/2$		2.81	2.67	2.752
$3/2^- 1/2$		1.90	1.88	4.712
$5/2^- 1/2$		0.22	0.24	0.080

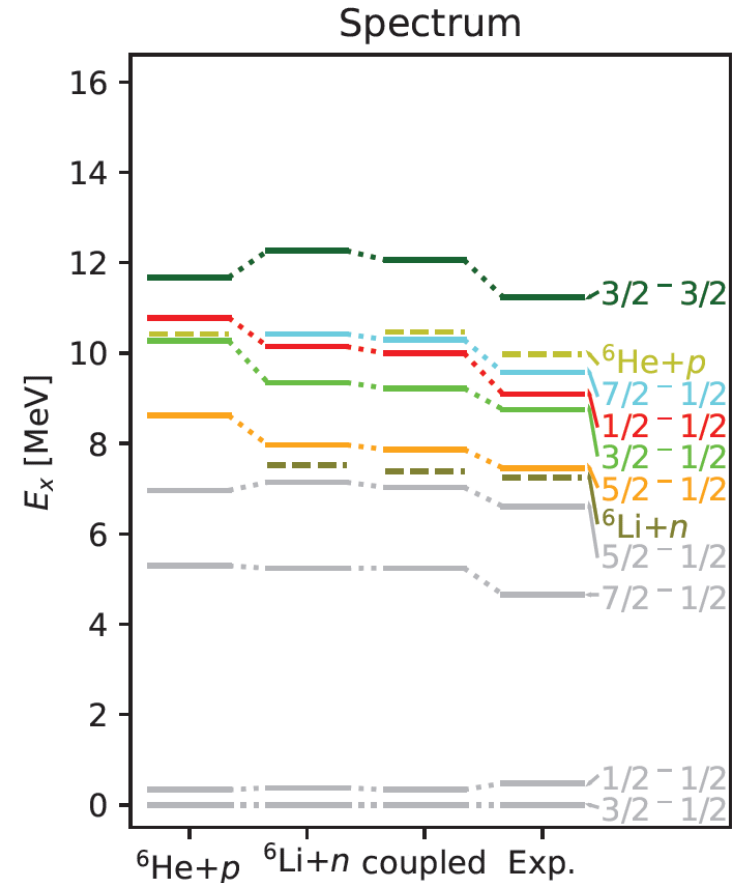


- Experimentally observed resonances reproduced
- Discrepancy between calculated and experimental widths
- Results depend on mass partition

Resonances in ${}^7\text{Li}$ - experimentally observed

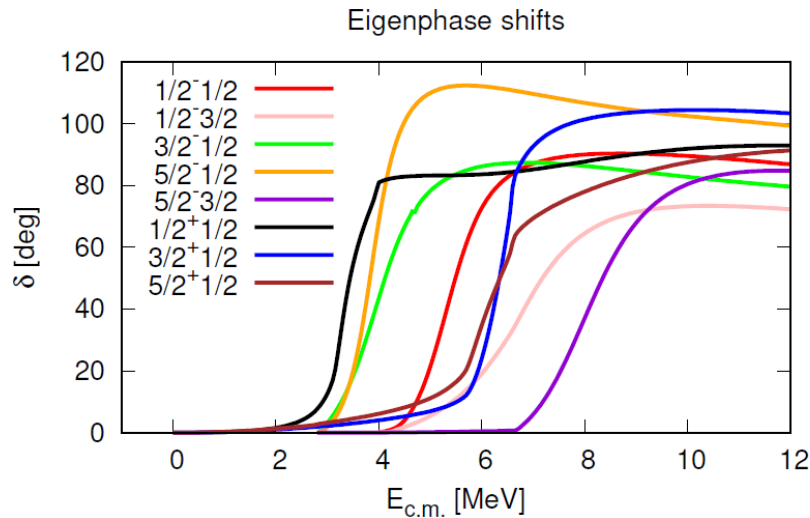


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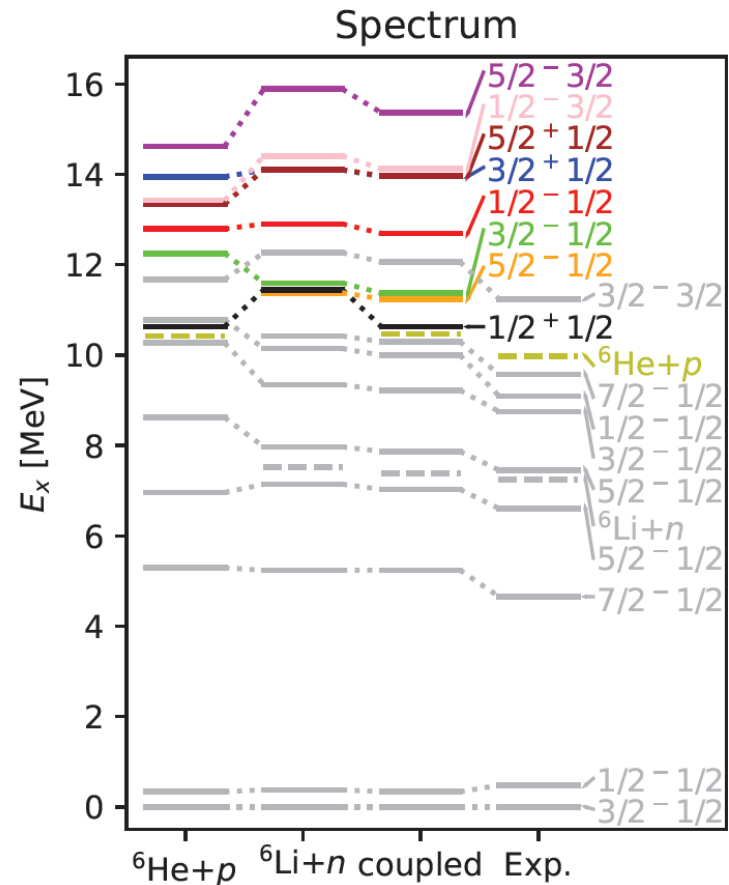


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- Discrepancy between calculated and experimental widths
- Results depend on mass partition

Resonances in ${}^7\text{Li}$ - predicted



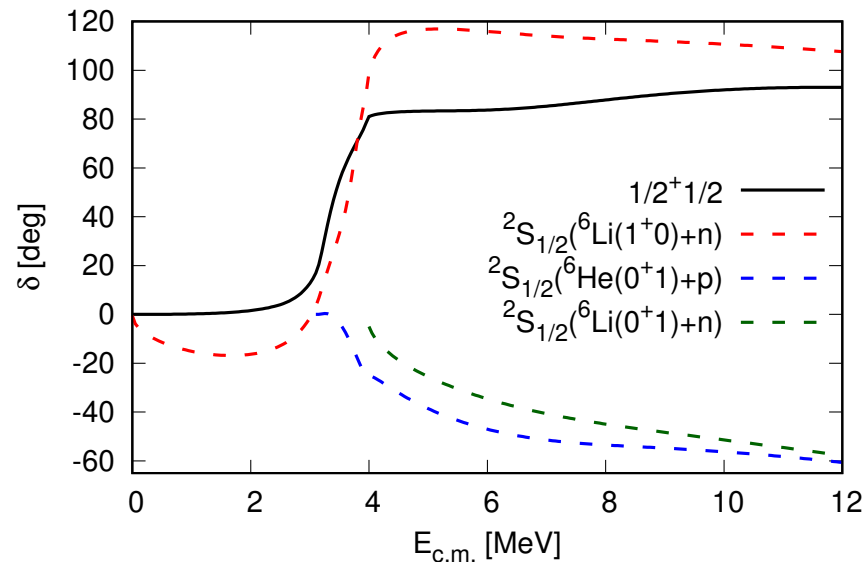
$J^\pi T$	Γ [MeV]		
	${}^6\text{He} + p$	${}^6\text{Li} + n$	coupled
$3/2^+ 1/2$	1.15	0.29	0.86
$1/2^- 1/2$	0.15	1.79	1.87
$3/2^- 1/2$	0.48	2.15	2.09
$5/2^- 1/2$		1.06	1.04
$1/2^+ 1/2$	0.15	0.80	1.01



- Eight resonances predicted
- Results depend on mass partitions
- Effect of coupling

$1/2^+$ eigenphase shift and diagonal phase shifts

- Previous NCSMC calculations neglecting coupling of mass partitions [1] predict S -wave $1/2^+$ resonance in ${}^6\text{He} + p$ just above proton separation energy
- No such resonance was experimentally observed [2]

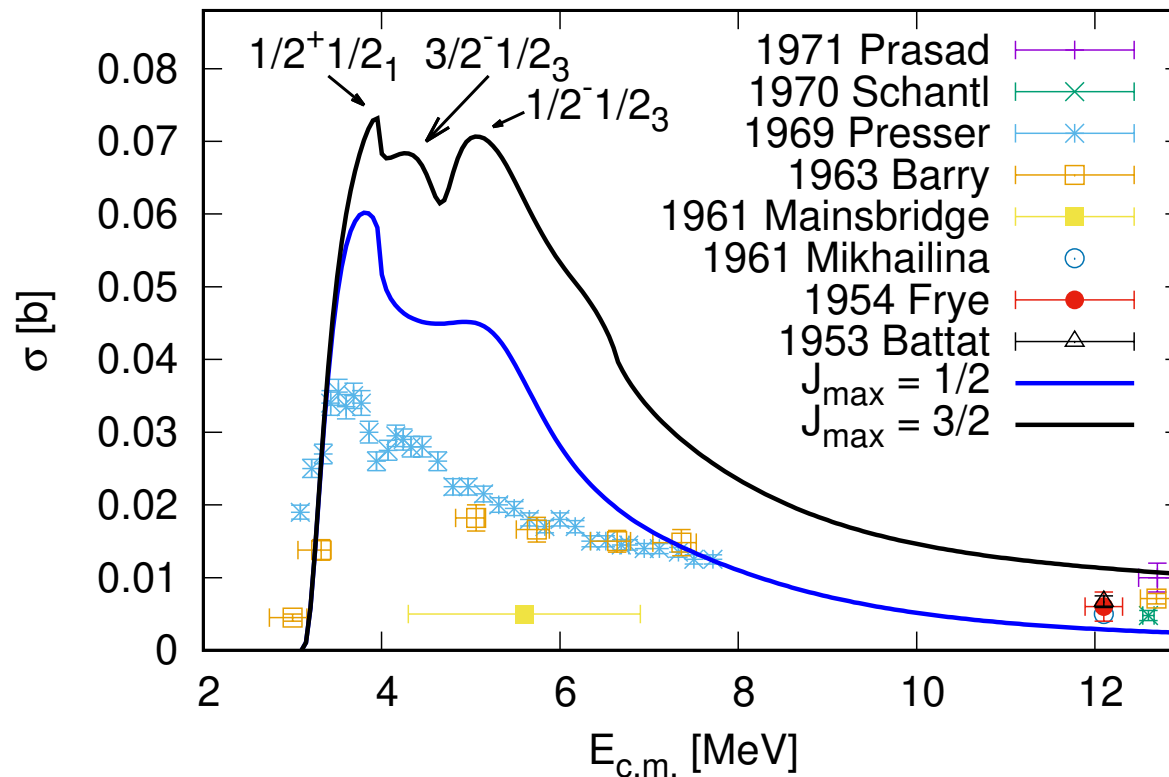


- In present calculation the $1/2^+$ resonance is dominated by ${}^2S_{1/2}({}^6\text{Li}(1^+0) + n)$ channel
- In present calculation no $1/2^+$ resonance found in ${}^6\text{He} + p$ channels

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Cross section of ${}^6\text{Li}(n,p){}^6\text{He}$ reaction



- Threshold and overall shape reproduced
- Values overestimated
- Missing (n, α) channel

Conclusion

- NCSMC calculations for ${}^7\text{Li}$ coupling mass partitions ${}^6\text{Li} + n$ and ${}^6\text{He} + p$ done
- Experimentally observed states reproduced
- Excitation energies in reasonable agreement with experiment
- Widths of resonances differ from experiment probably due to omitted mass partitions
- Energies and widths of resonances affected by coupling of mass partitions
- $1/2^+$ resonance predicted, but only in ${}^6\text{Li} + n$ - discrepancy between previous NCSMC prediction and experiment explained
- Cross section of ${}^6\text{Li}(n, p){}^6\text{He}$ calculated: overall shape reproduced, values overestimated
- Future work: Include ${}^4\text{He} + {}^3\text{H}$ and three-nucleon interaction

Collaborators

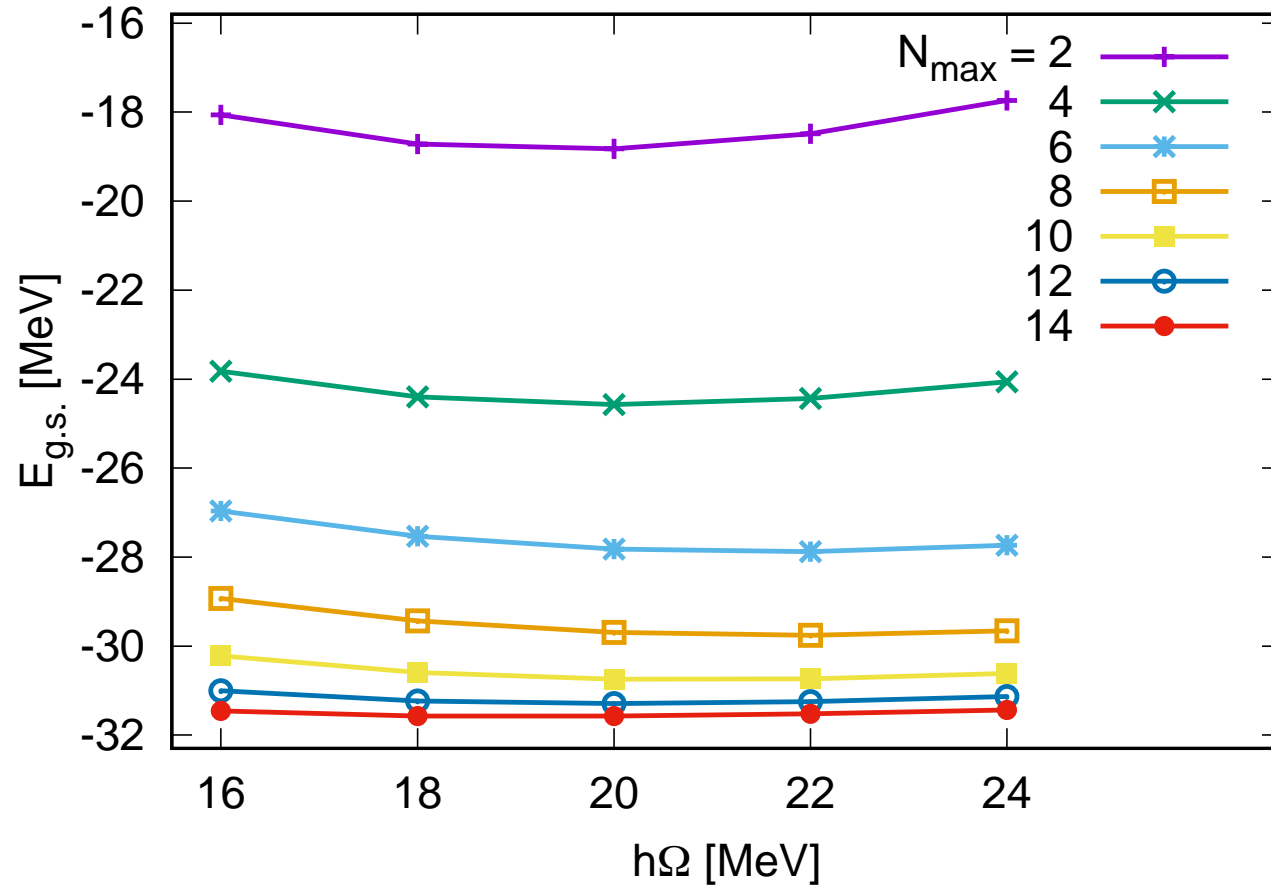
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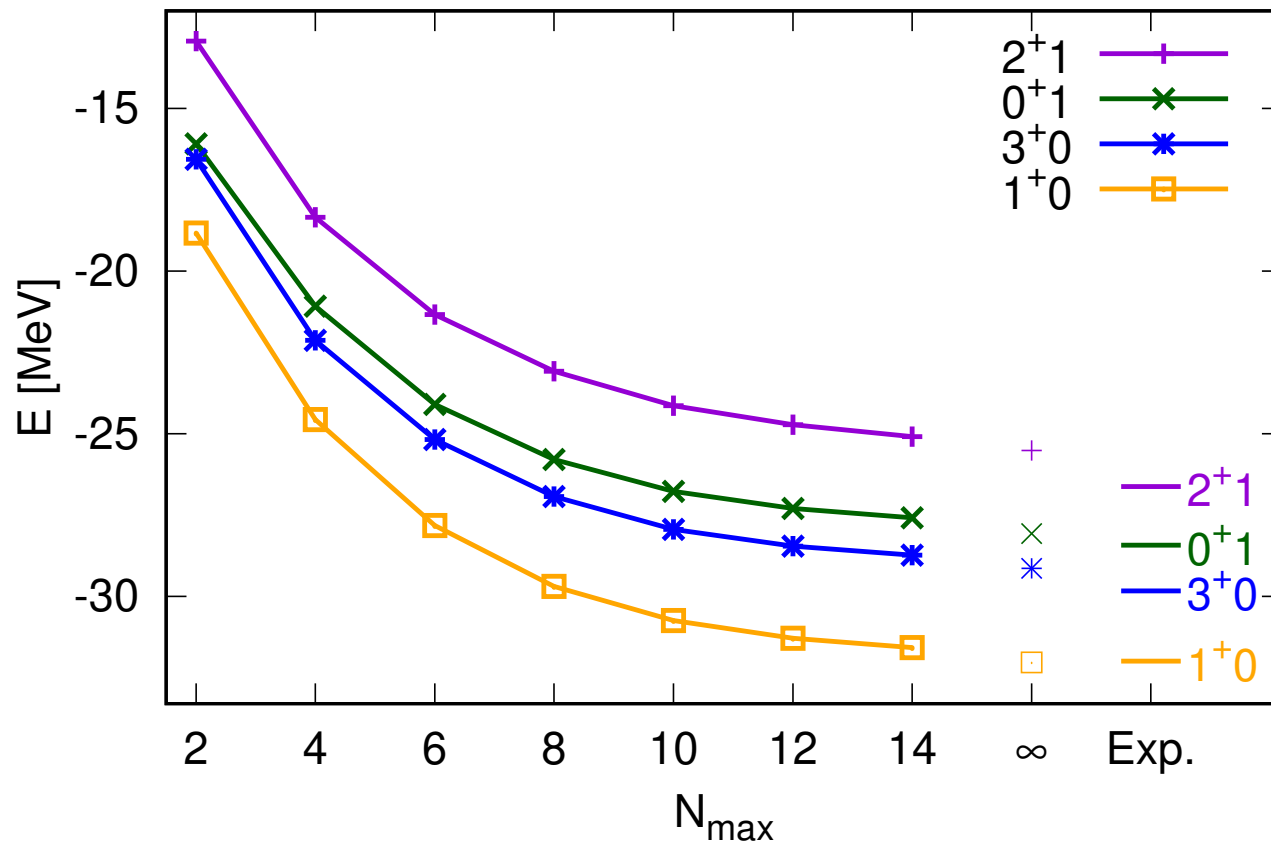
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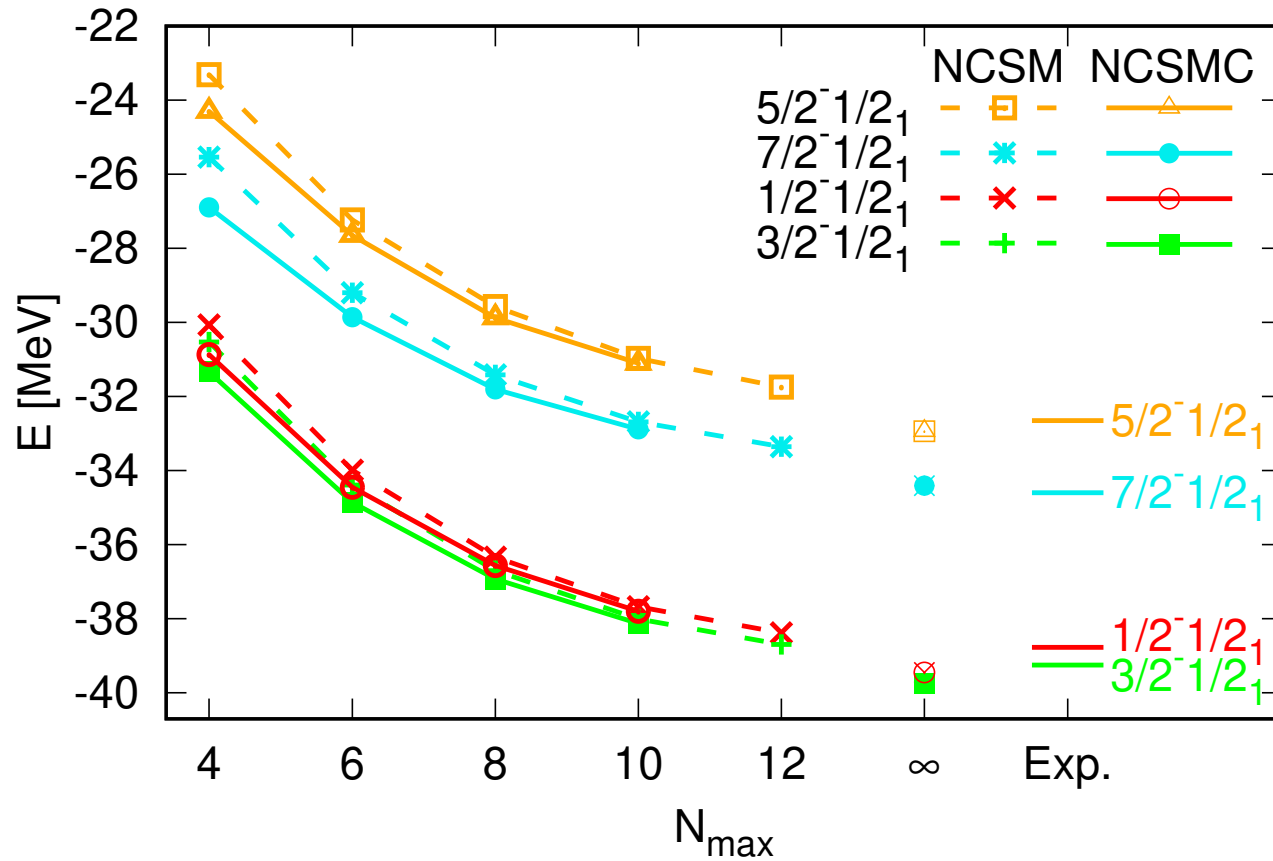
NCSM energy of ground state of ${}^6\text{Li}$



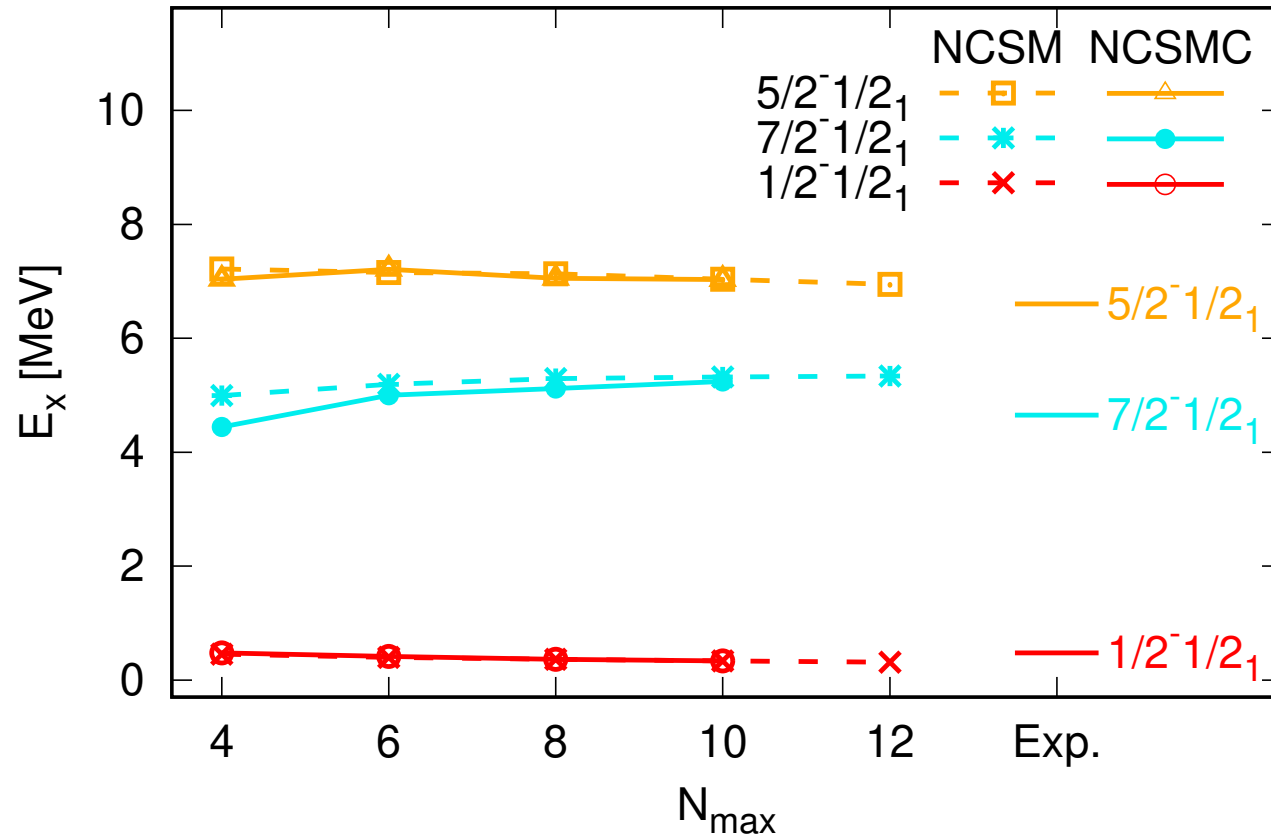
Energies of NCSM states of ${}^6\text{Li}$



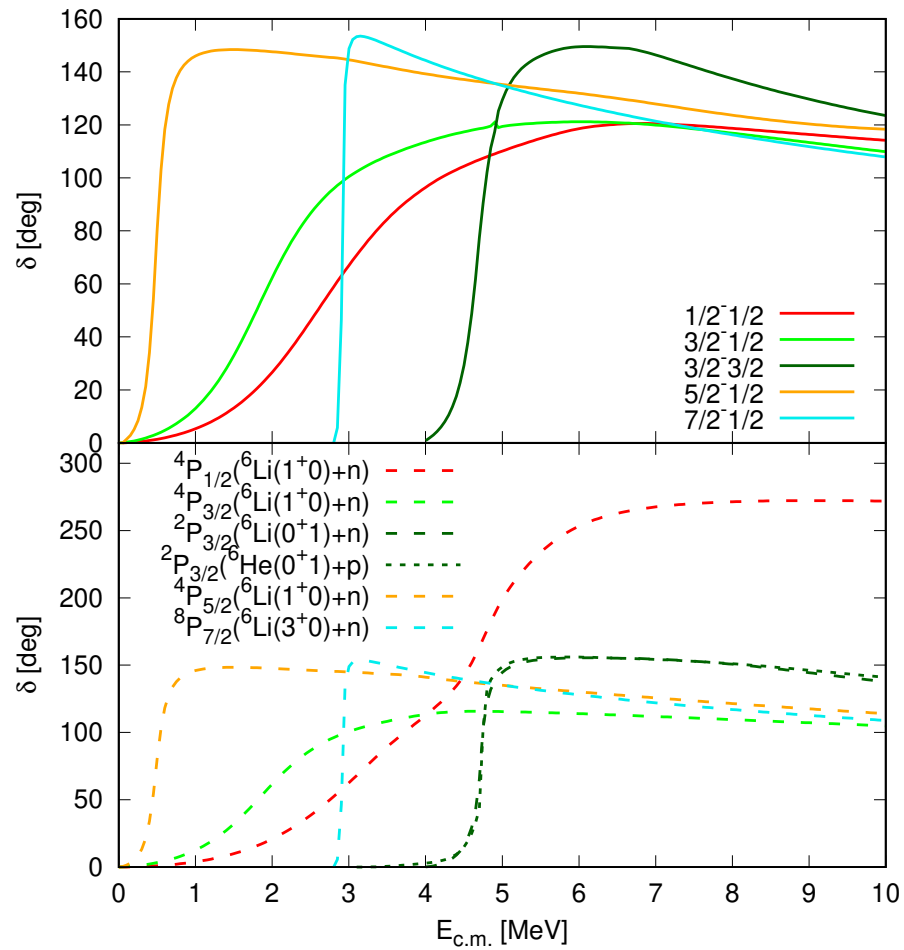
Energies of bound states of ${}^7\text{Li}$



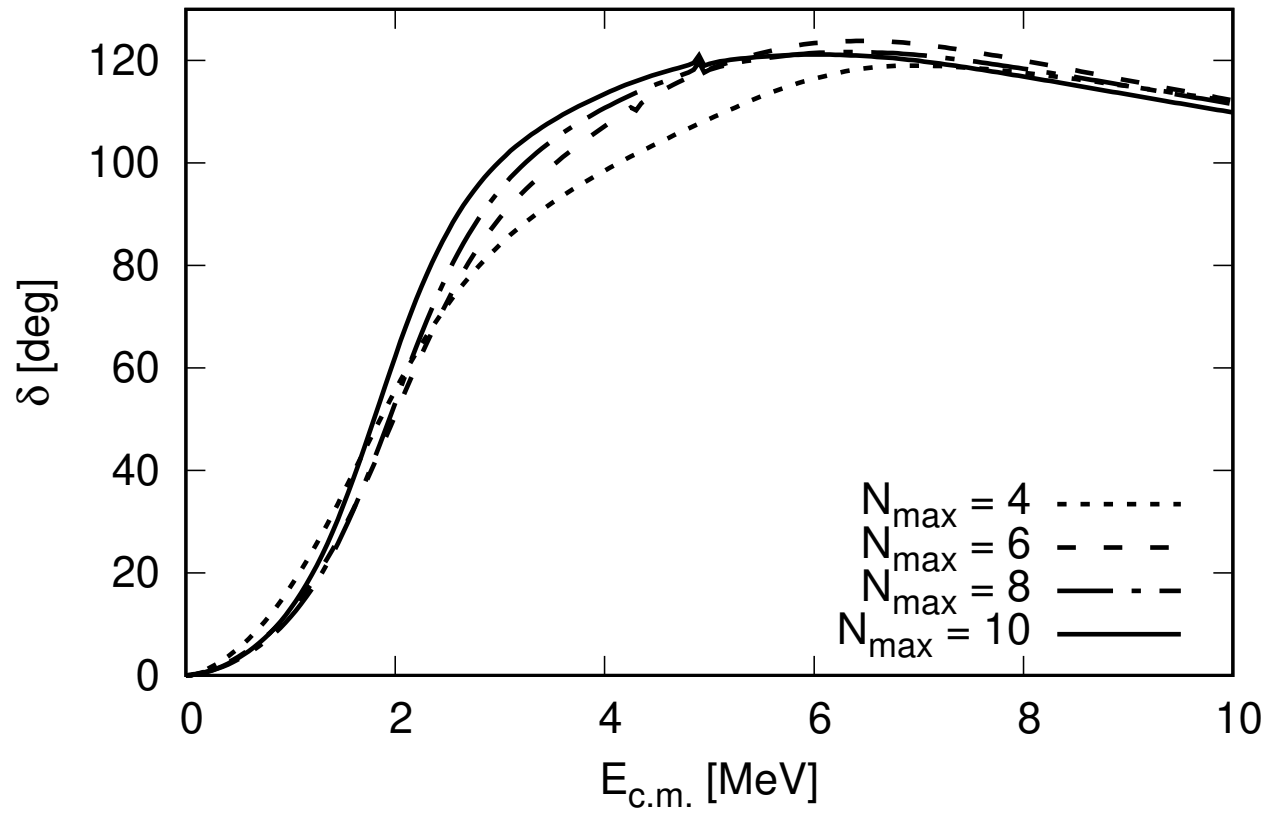
Excitation energies of bound states of ${}^7\text{Li}$



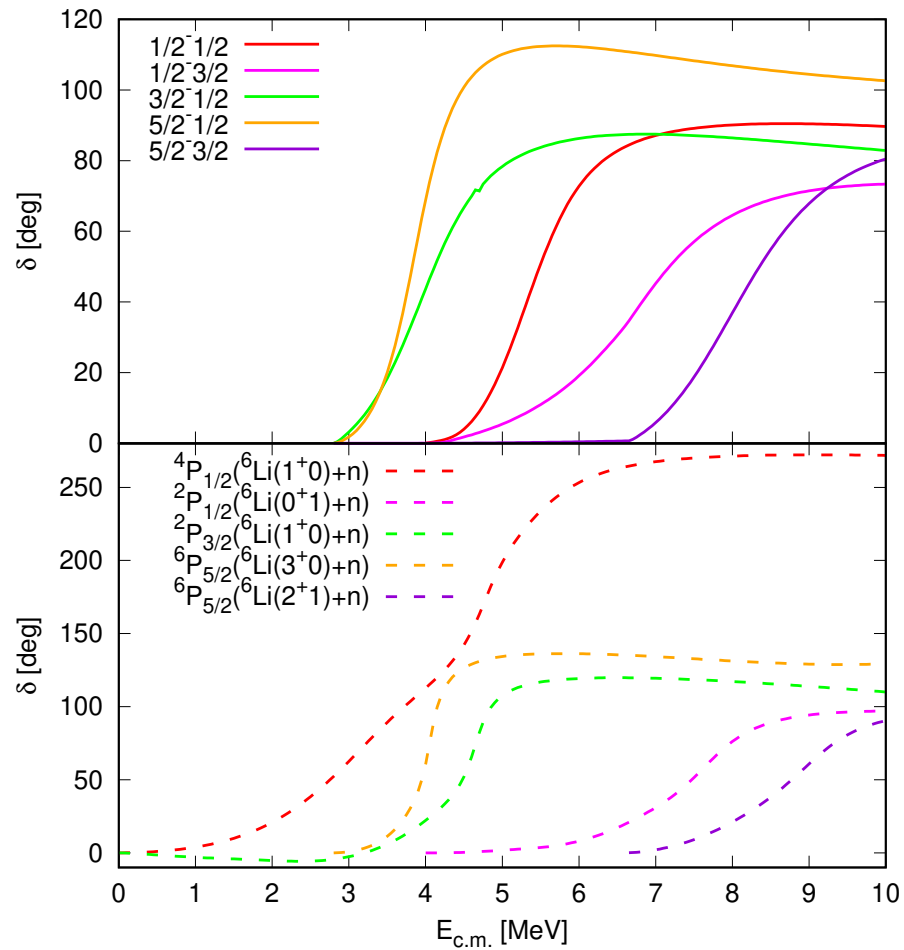
Reproduced resonances in ${}^7\text{Li}$



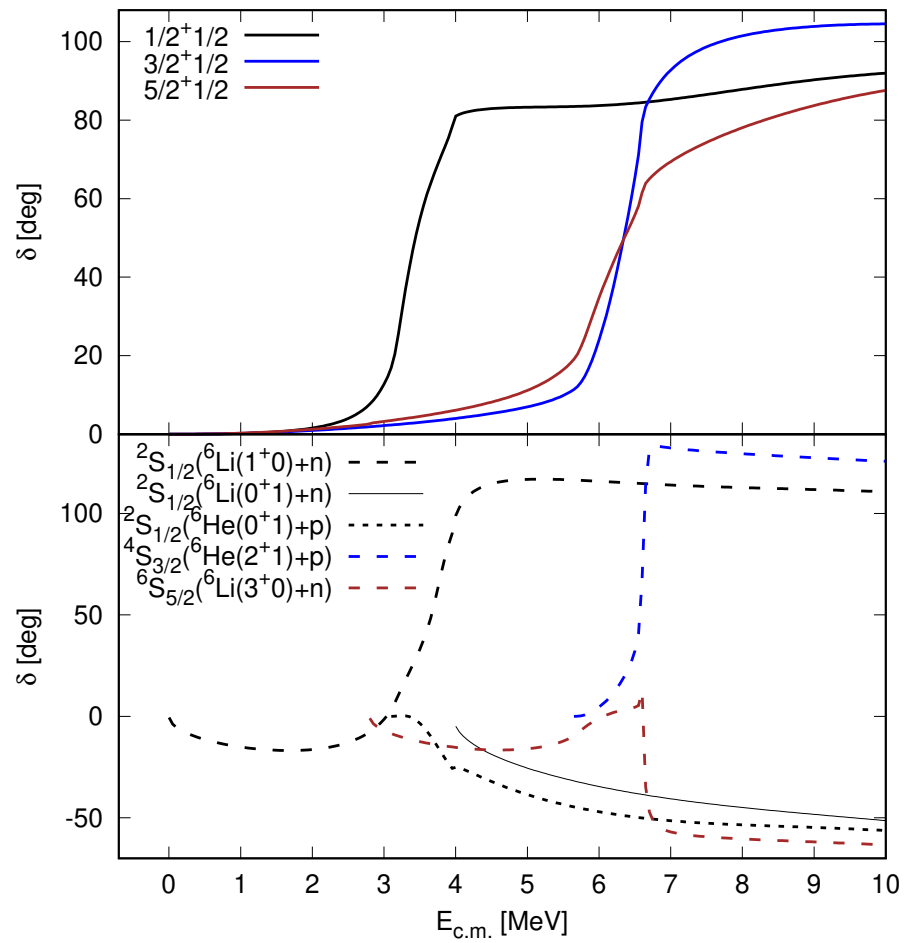
$3/2^-$ eigenphase shift



Predicted negative-parity resonances in ${}^7\text{Li}$



Predicted positive-parity resonances in ${}^7\text{Li}$



$1/2^+$ eigenphase shift

