A new class of three-nucleon forces In Chiral EFT

Based on: arXiv:2411.00097

with

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Nuclei as probes of BSM physics









Nuclei as probes of BSM physics

From quarks to nucleons Modern view of nucleon forces



- Possible hadronic interactions determined by (chiral) symmetries
- Expansion in $Q/\Lambda_{\chi}\sim m_{\pi}/\Lambda_{\chi}$, where $\Lambda_{\chi}\sim 1~{\rm GeV}$
- Interaction strengths determined by (unknown) coupling constants
 - Power counting needed to determine their importance

Chiral Effective Theory

Modern view of nucleon forces



Hierarchy of nuclear forces up to N5 LO in ChiPT. Solid lines represent nucleons and dashed lines pions. Entem, Machleidt, Y. Nosyk, (arXiv:1703.05454)

Chiral Effective Theory

Modern view of nucleon forces



Conventional three-body force N2LO contributions



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- *c_i*: πN scattering
 Hoferichter et al Phys. Rept. '15; PRL '15; Phys. Lett. B '16
- *C*_{*D*,*E*}:
 - Nd scattering
 - light nuclei
 - tritium β decay



Conventional three-body force N2LO contributions



- Nd scattering
- light nuclei
- tritium β decay
- Only c_1 and c_3 contribute in neutron matter

Van Kolck '94; Epelbaum Nogga, Glöckle Hamada, Meissner, '02

-1

0 c_D 2

Gazit et al '09

-0.8 -3

-2

Conventional three-body force N3LO contributions



- Consists of
 - Loop diagrams with LO vertices
 - Tree graphs involving relativistic corrections

Conventional three-body force N3LO contributions



- Loop diagrams with LO vertices
- Tree graphs involving relativistic corrections

• No new LECs

Bernard, Epelbaum, Krebs, Meissner '08,'11; Ishikawa, Robillotta '07,

- Bubble diagrams in ${}^{1}S_{0}$ lead to divergences
- Requires short-distance interactions
- Can be absorbed in $C_0' = C_0 + m_\pi^2 D_2$









• Induce 3-nucleon forces through loops



Kaplan, Savage, Wise, '96; Beane, Bedaque, Savage, van Kolck, '03, Nogga, Timmermans, van Kolck, '05, Long, Yang, '12;



D_2, E_2, F_2 currently poorly known

• Estimate from renormalization group:

$$\frac{d}{d\ln\mu} \left[\frac{X}{\tilde{C}_0^2}\right] = \gamma_X \left(\frac{m_N}{4\pi f_\pi}\right)^2, \qquad X \in \{D_2, E_2, F_2\}$$

$$\begin{aligned} \gamma_{D_2} &= g_A^2 / 4 \\ \gamma_{E_2} &= -(1+g_A^2) / 3, \\ \gamma_{F_2} &= -g_A^2 / 3 \end{aligned}$$

- Suggests LO size $X \simeq C_0^2/5 \sim 1/(5 F_\pi^4)$
 - Compared to N2LO Weinberg $X \sim 1/(F_{\pi}^2 \Lambda_{\chi}^2)$

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Beyond Weinberg counting Electroweak/BSM interactions

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Three-nucleon potential from
$$m_{\pi}^2 D_2$$

$$V(\vec{q}_1, \vec{q}_2, \vec{q}_3) = \frac{9g_A^2 D_2 m_\pi^3}{512\pi f_\pi^4} F\left(\frac{\vec{q}_3^2}{4m_\pi^2}\right) \left(1^{(i)} 1^{(j)} - \vec{\sigma}^{(i)} \cdot \vec{\sigma}^{(j)}\right) , \qquad F(b) = \frac{2}{3} \left(1 + \left(\frac{1}{2\sqrt{b}} + \sqrt{b}\right) \tan^{-1}(\sqrt{b})\right) .$$

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• E_2 induces same structure

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Contributions from
$$\sim E_{\pi}^2 E_2$$

•
$$E_2$$
 Negligible for $n \leq 2n_{\rm sat}$
• With $m_{\pi}^2 \rightarrow \left(\vec{q}^2/m_N\right)^2$

Contributions from $\sim \vec{q}^2 F_2$

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Impact in dense matter

Effect in dense matter Hartree-Fock estimate

- Expectation value of $V_{D_2, {\cal F}_2}$ in Fermi gas state
 - Diagrammatically; contract nucleons in all possible ways
 - Finite, no need for additional regulators

$$\left\langle \mathscr{H}(0) \right\rangle = \int_{\vec{p}_1, \vec{p}_2, \vec{p}_3 \leq k_f} \left[V_{ijk}^{ijk}(0, 0, 0) - V_{ijk}^{ikj}(0, \vec{p}_{32}, \vec{p}_{23}) + V_{ijk}^{jki}(\vec{p}_{21}, \vec{p}_{32}, \vec{p}_{13}) + V_{ijk}^{kij}(\vec{p}_{31}, \vec{p}_{12}, \vec{p}_{21}) - V_{ijk}^{kji}(\vec{p}_{31}, 0, \vec{p}_{13}) - V_{ijk}^{jik}(\vec{p}_{21}, \vec{p}_{12}, 0) \right]$$

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- Need the size of the LECs
 - Use expectation from RGE for a first estimate:

$$D_2 \le 1/(5F_\pi^4), \qquad |F_2| \le 1/(5F_\pi^4)$$

New class of three-nucleon forces Effects in dense matter

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- D_2, F_2 induce a stronger density dependence
- Scheme and regulator dependent
 - Roughly ~ 1/3 smaller using dispersive regulator scheme [for $\Lambda = 500$ MeV at $n_{\rm sat}$]
 - Requires consistent combination with `usual' N3LO three-nucleon force
- Crucially depend on the size of D_2, F_2

Impact Beyond the Standard Model

• D_2 induces m_{π} dependence of NN interactions

Several BSM scenarios lead to different quark masses

- Variations of fundamental constants
 - E.g. dilatons scenarios, couplings to background fields
 - Lead to $m_q(t)$

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 - Axion could condense in dense matter like neutron stars
 - Would change $m_{\pi}(\theta = 0) \rightarrow m_{\pi}(\theta = \pi) \simeq 80 \,\mathrm{MeV}$

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- Axion scenarios
 - Axion could condense in dense matter like neutron stars
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- Can be probed through their effect on the nuclear force
 - Requires m_{π} dependence of the nuclear force

Determining the LECs

From theory:

- First principles determination using Lattice QCD
 - Currently only calculations at unphysical m_{π}

e.g. Beane, Bedaque, Orginos, Savage, '06; Beane et al '15;

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From experiment:

- Determine D_2, F_2 together with $c_{D,E}$ from
 - Light systems:
 - Nd scattering
 - Binding energies
 - tritium β decay
 - Properties of dense matter
 - Properties of neutron stars
 - π -nucleus scattering

See Isak Svensson's talk yesterday Urban Vernik's poster later today

e.g. Beane, Bedaque, Orginos, Savage, '06; Beane et al '15;

Properties of dense matter

- Naive implementation
 - Combines HF estimates of 3-nucleon force with 2nucleon contributions
 - Fits to properties of dense matter near saturation

Properties of dense matter

- Inconsistent: 2- and 3-nucleon forces using different regulators, Hartree-Fock estimates...
- Does suggest dense matter can help pin down D_2, F_2

• A consistent determination is work in progress (w/C. Drischler, M. Kumamoto, M. Dawid, S. Reddy)

- Renormalization requires $\pi^2 NN$ interactions at LO
- Induce 3-nucleon forces through loops
- Significant contributions in dense matter
 - Important for neutron stars (equation of state)
 - Nuclei
- Crucially depends on the value of the LECs
 - Need to be fit to data

Outlook

- Determining the LECs from
 - Light nuclei
 - Properties of dense matter
 - Properties of neutron stars
- Investigate impact on
 - Dense systems
 - BSM scenarios & m_{π} dependence on nuclear force

