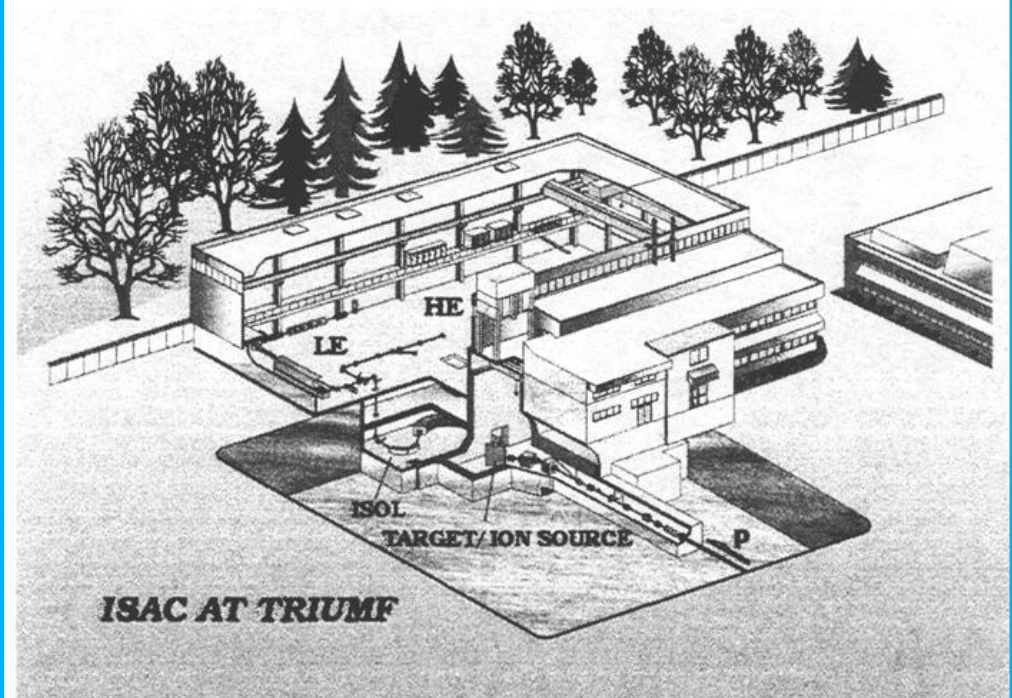
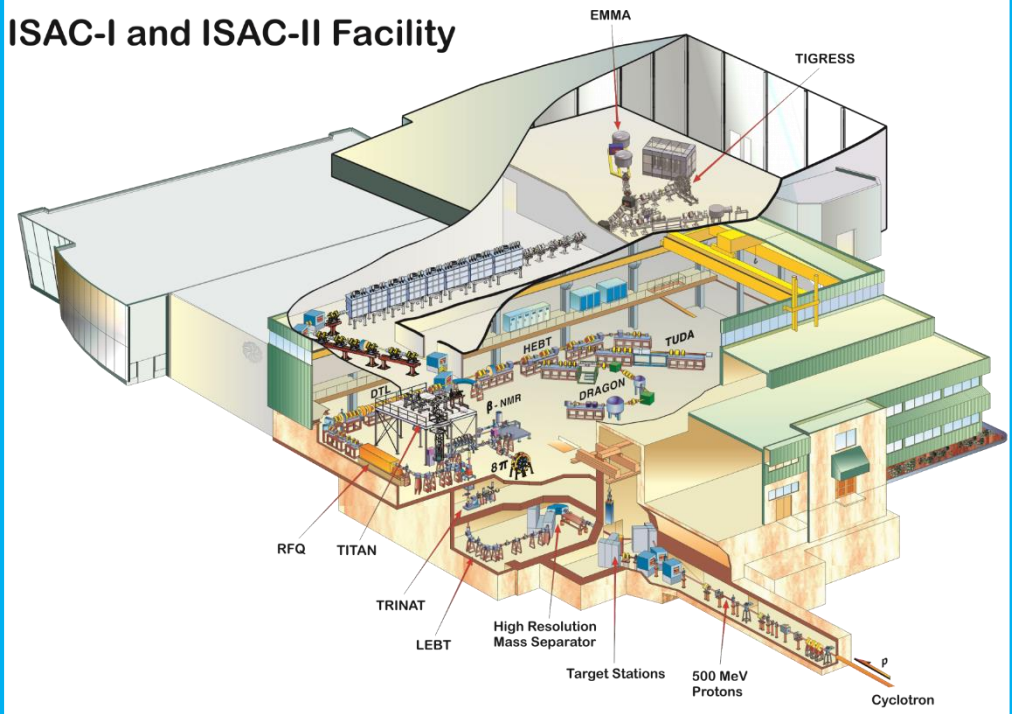


The Emergence of nuclear-shell-model studies

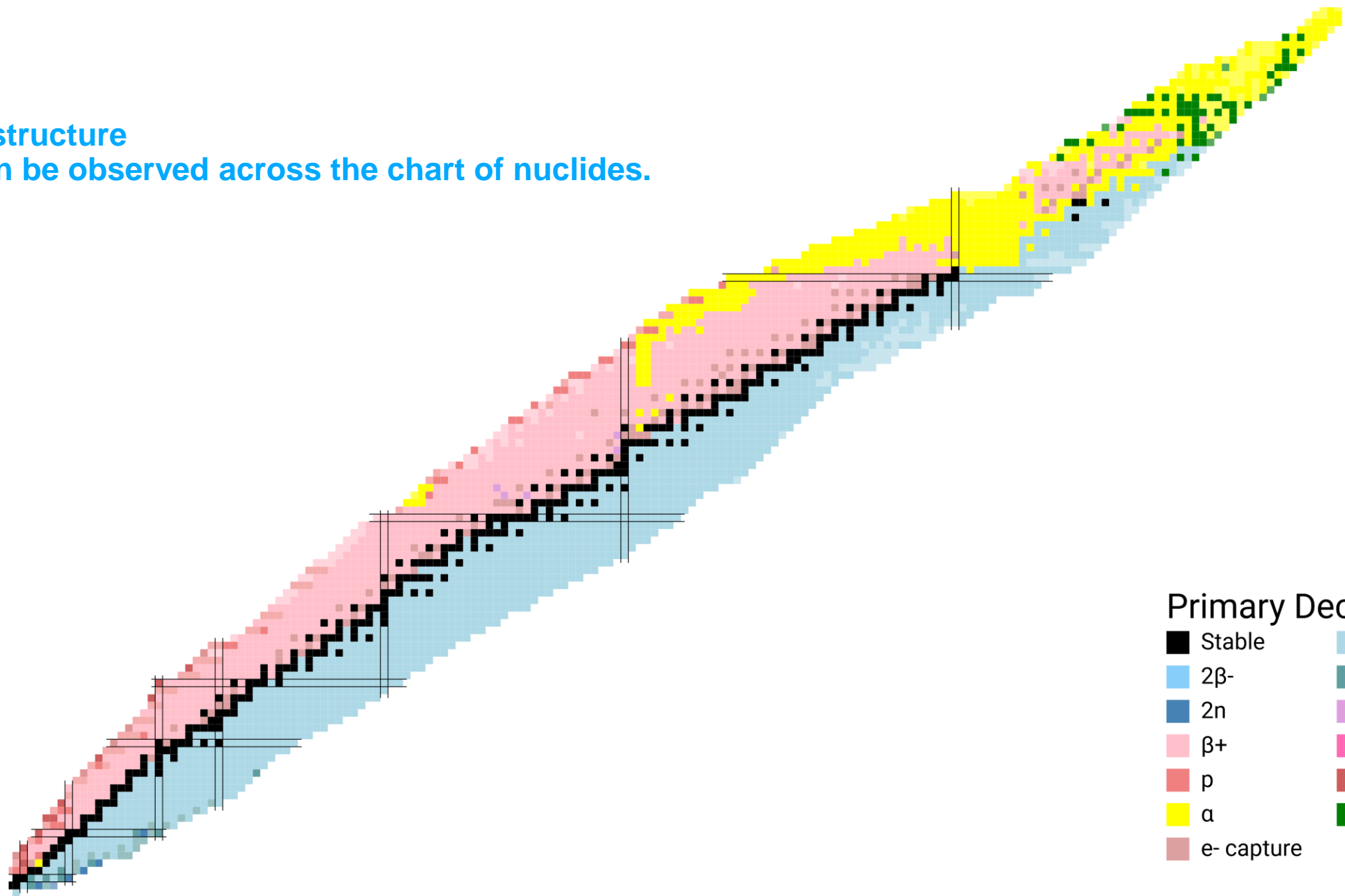
Ania Kwiatkowski
Research Scientist, TRIUMF
Adjunct Professor, UVic



ISAC-I and ISAC-II Facility



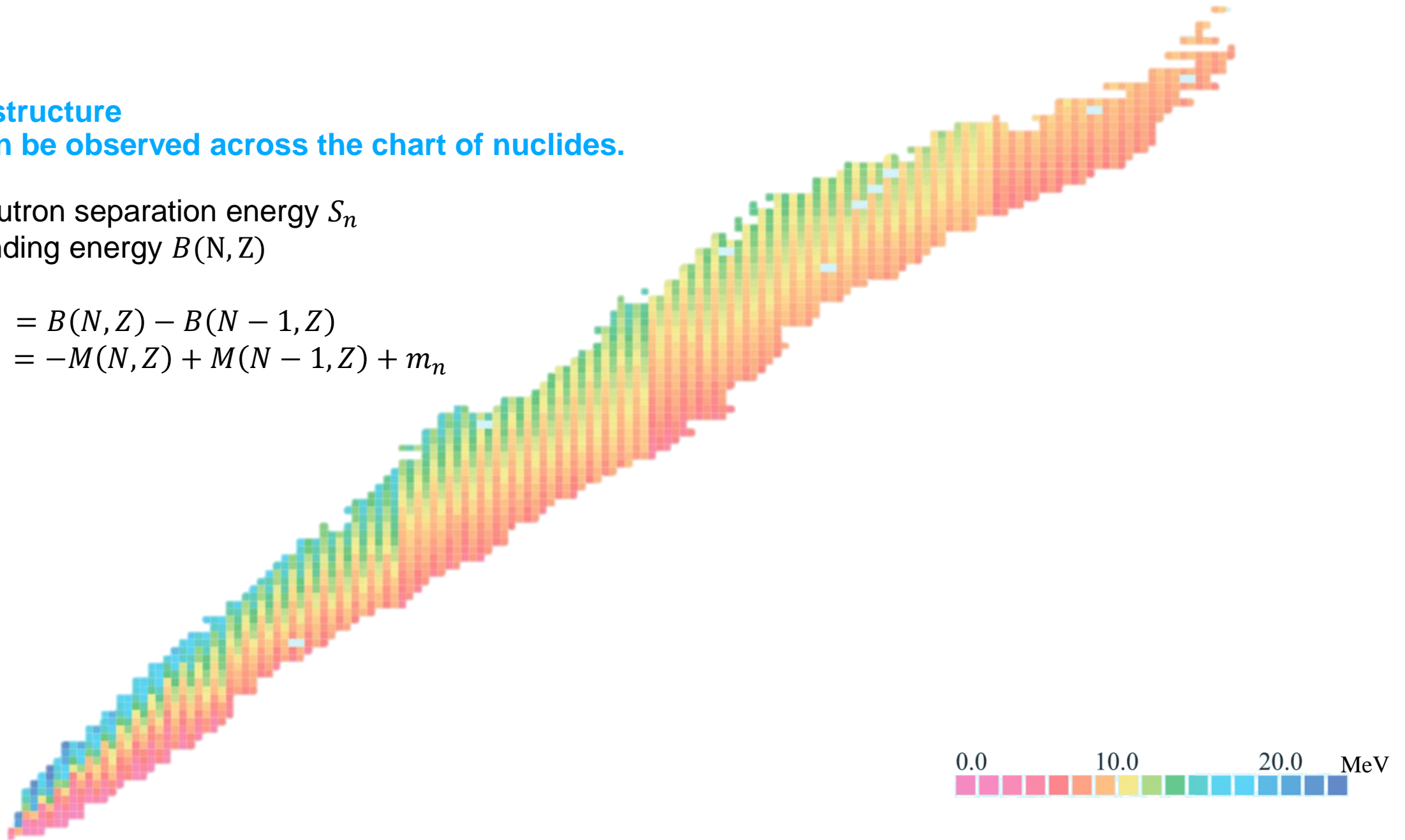
A structure
can be observed across the chart of nuclides.



A structure
can be observed across the chart of nuclides.

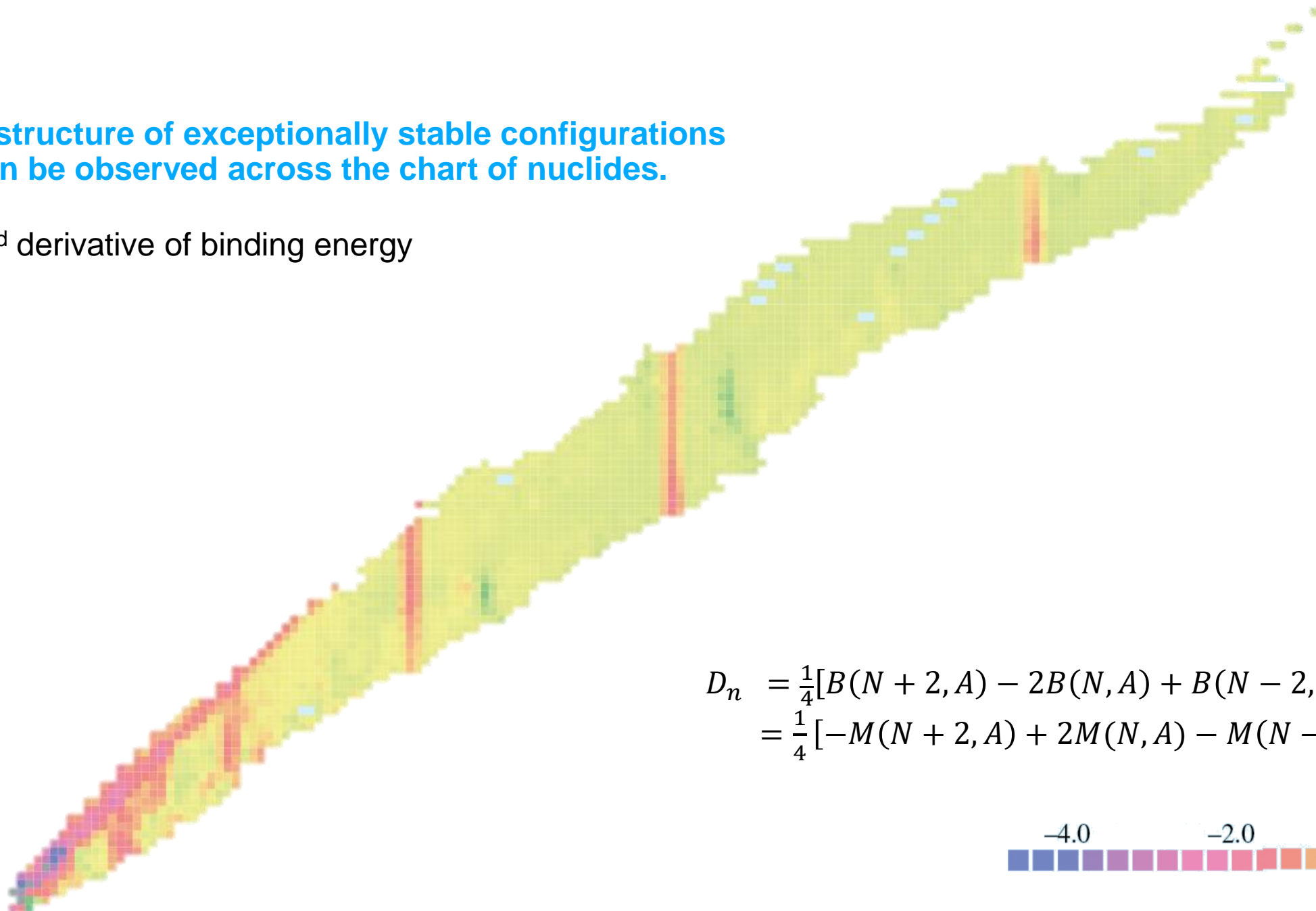
neutron separation energy S_n
binding energy $B(N, Z)$

$$\begin{aligned} S_n &= B(N, Z) - B(N - 1, Z) \\ &= -M(N, Z) + M(N - 1, Z) + m_n \end{aligned}$$

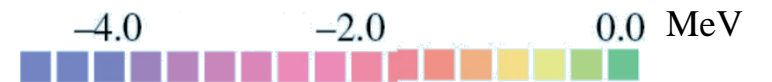


A structure of exceptionally stable configurations can be observed across the chart of nuclides.

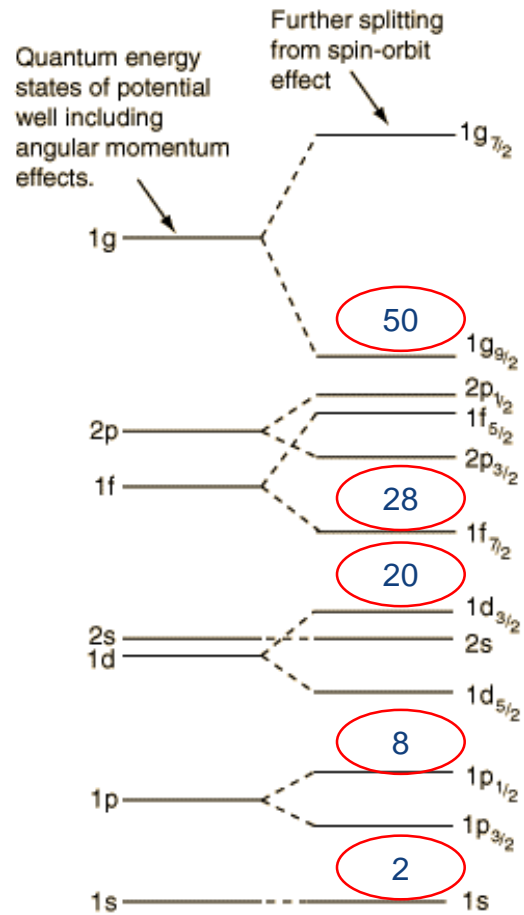
2nd derivative of binding energy



$$D_n = \frac{1}{4}[B(N + 2, A) - 2B(N, A) + B(N - 2, A)]$$
$$= \frac{1}{4}[-M(N + 2, A) + 2M(N, A) - M(N - 2, A)]$$



These shells or “magic numbers” could be derived from a harmonic oscillator.



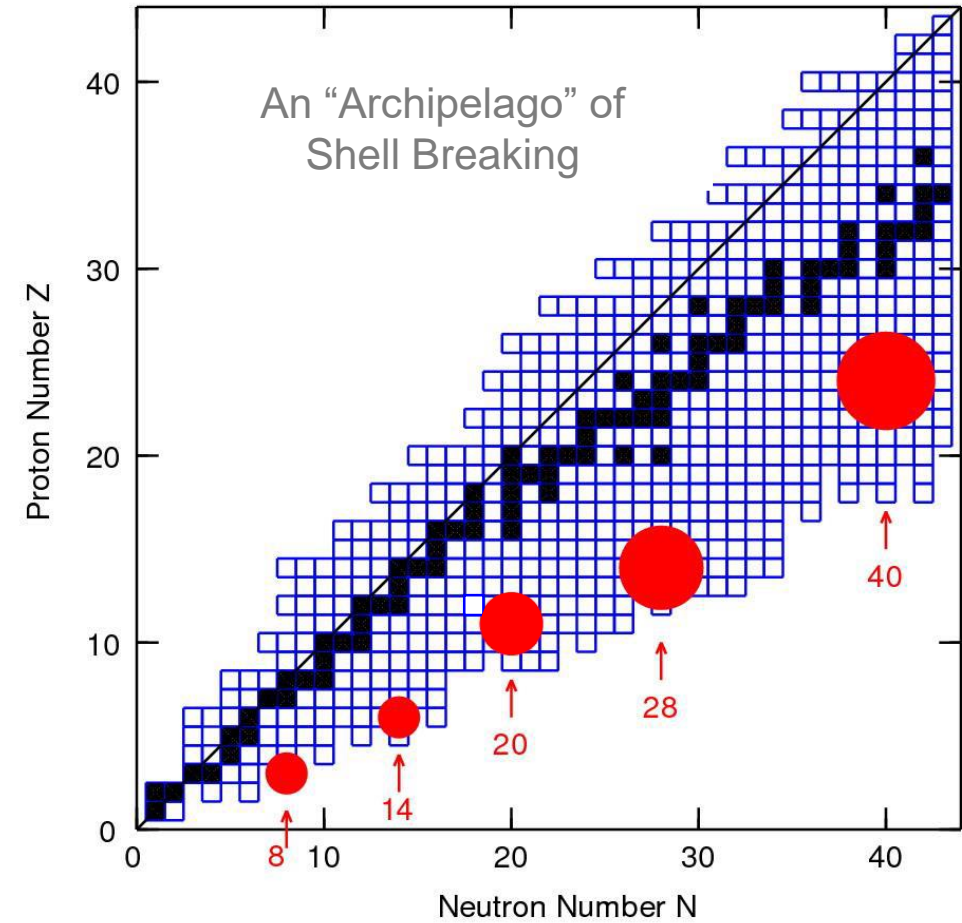
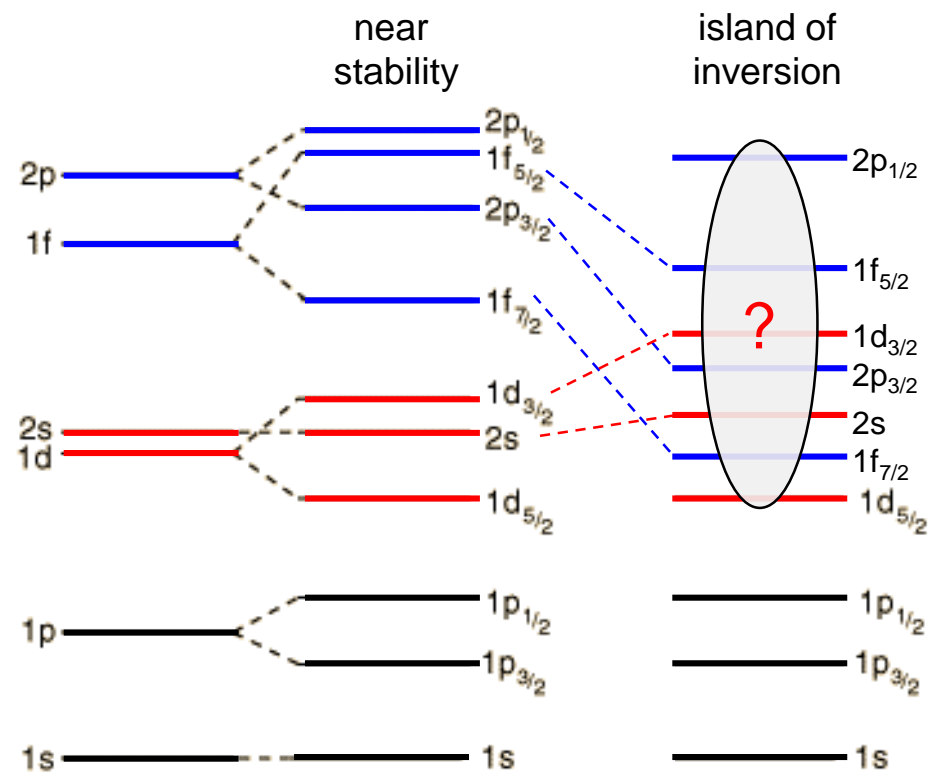
Maria Goeppert-Mayer 1963



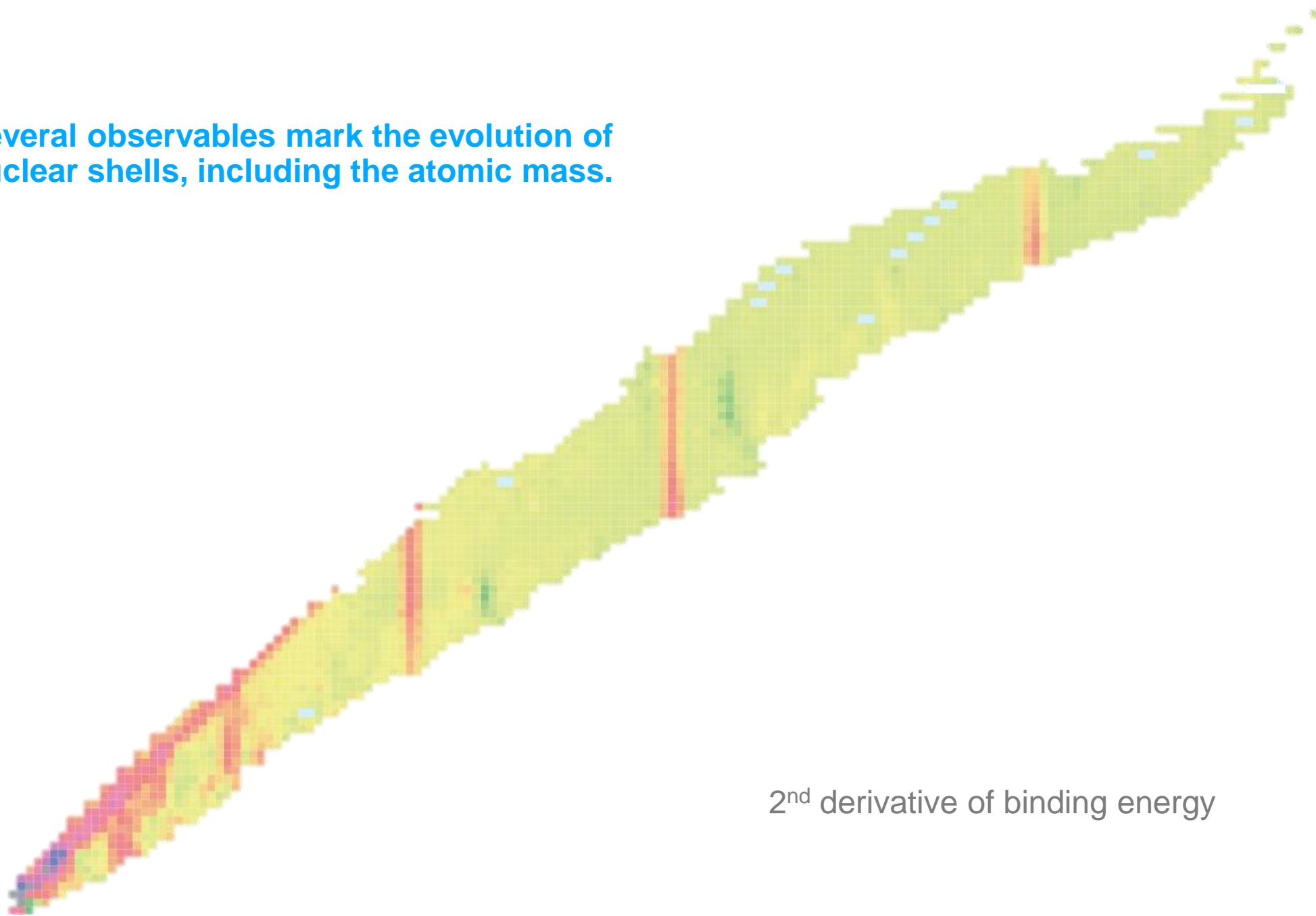
Hans D. Jensen 1963



The disappearance of expected and the emergence of new shells has been observed for several ratios of N/Z .

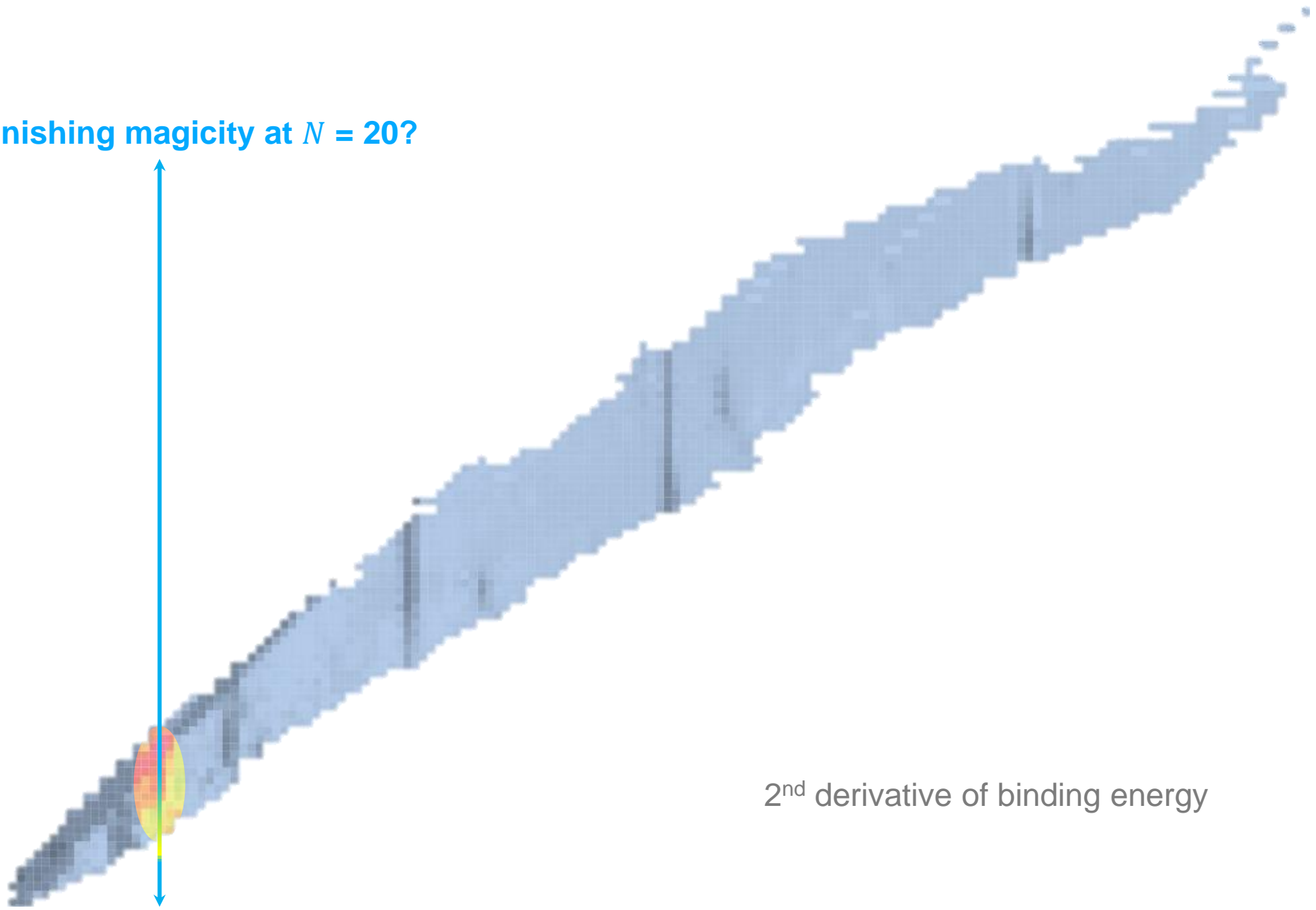


Several observables mark the evolution of nuclear shells, including the atomic mass.



2^{nd} derivative of binding energy

Vanishing magicity at $N = 20$?

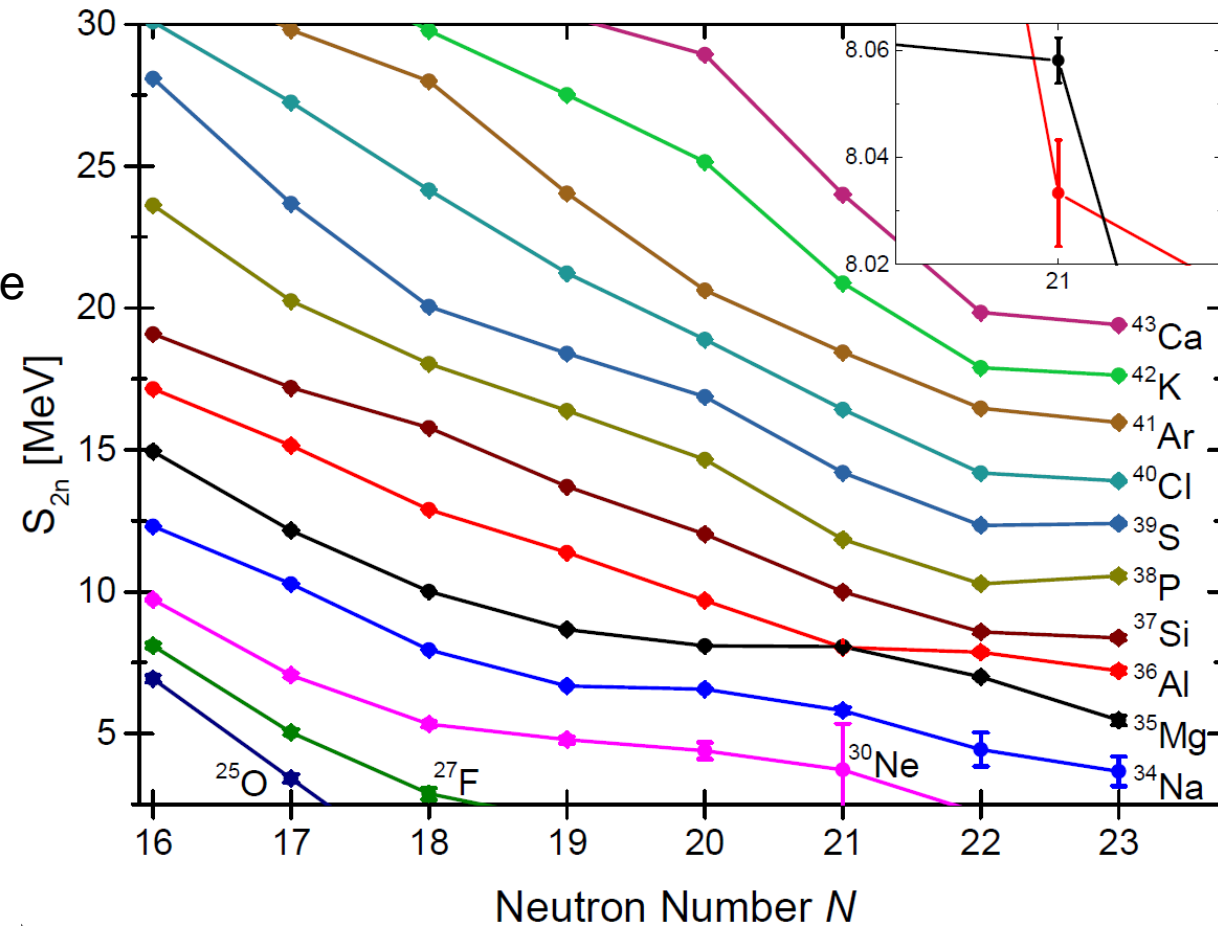
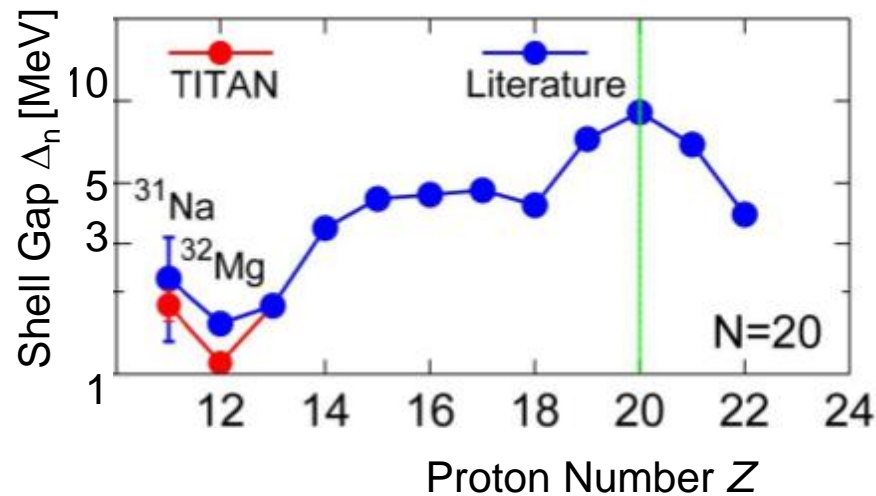


2nd derivative of binding energy

TITAN's mass campaign revealed the smallest shell closure for an expected magic number.

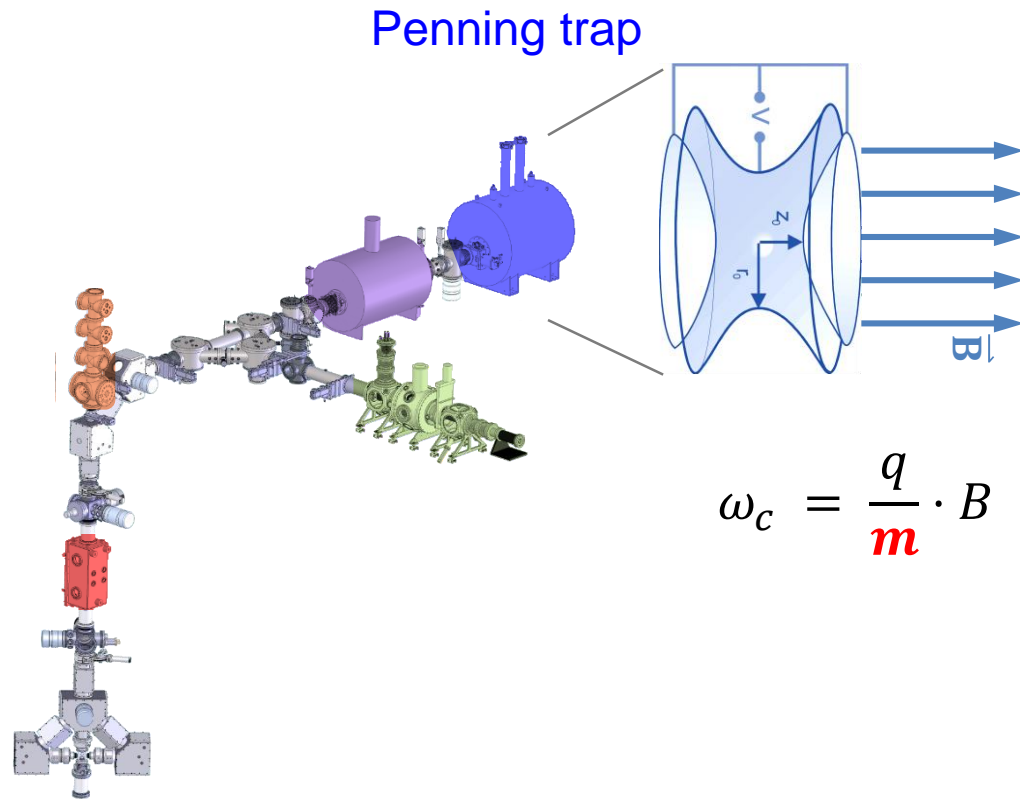
Measured $^{29-32}\text{Na}$, $^{30-34}\text{Mg}$, $^{29-35}\text{Al}$

Shell model calculations revealed strong correlation energy manifests in S_{2n} surface



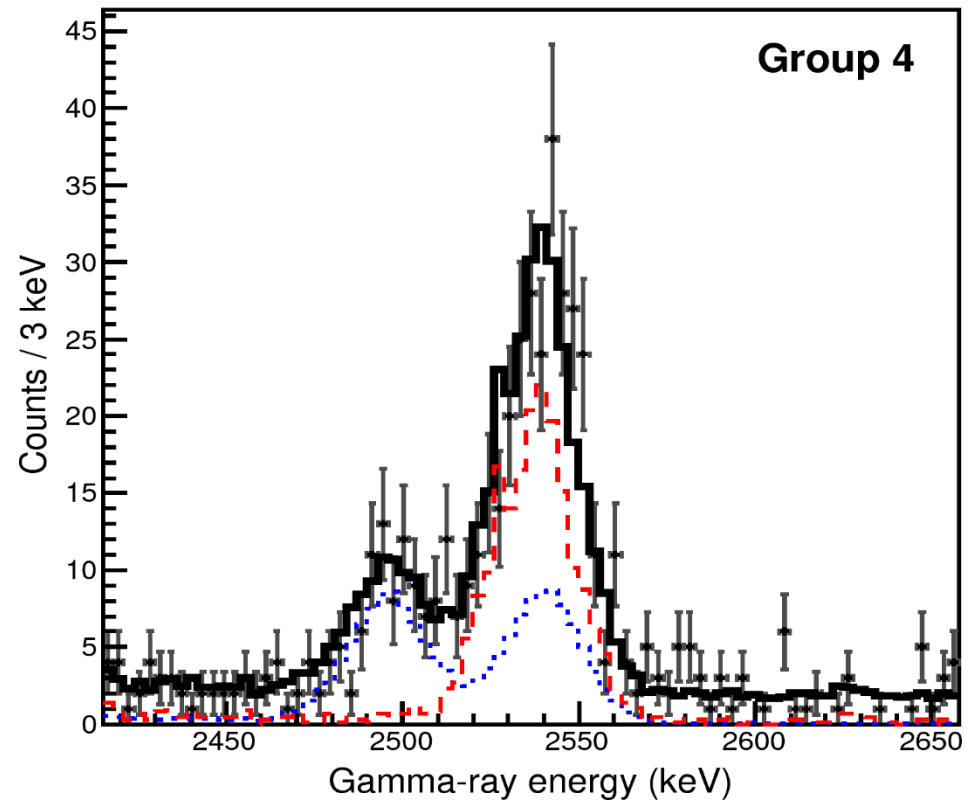
TITAN-ISAC is the only Penning trap mass spectrometer capable to survey the “Island of Inversion”.

- Accuracy: calibrations with stable species
 - vs. spread of TOF measurements
- High Precision: frequency measurement ($\geq 5 \times 10^{-9}$)
 - uncertainty improved $\leq 10x$
- Short $T_{1/2}$: fast beam preparation (world record 9 ms)
 - $\geq T_{1/2} (^{32}\text{Na}) = 12.9 \text{ ms}$



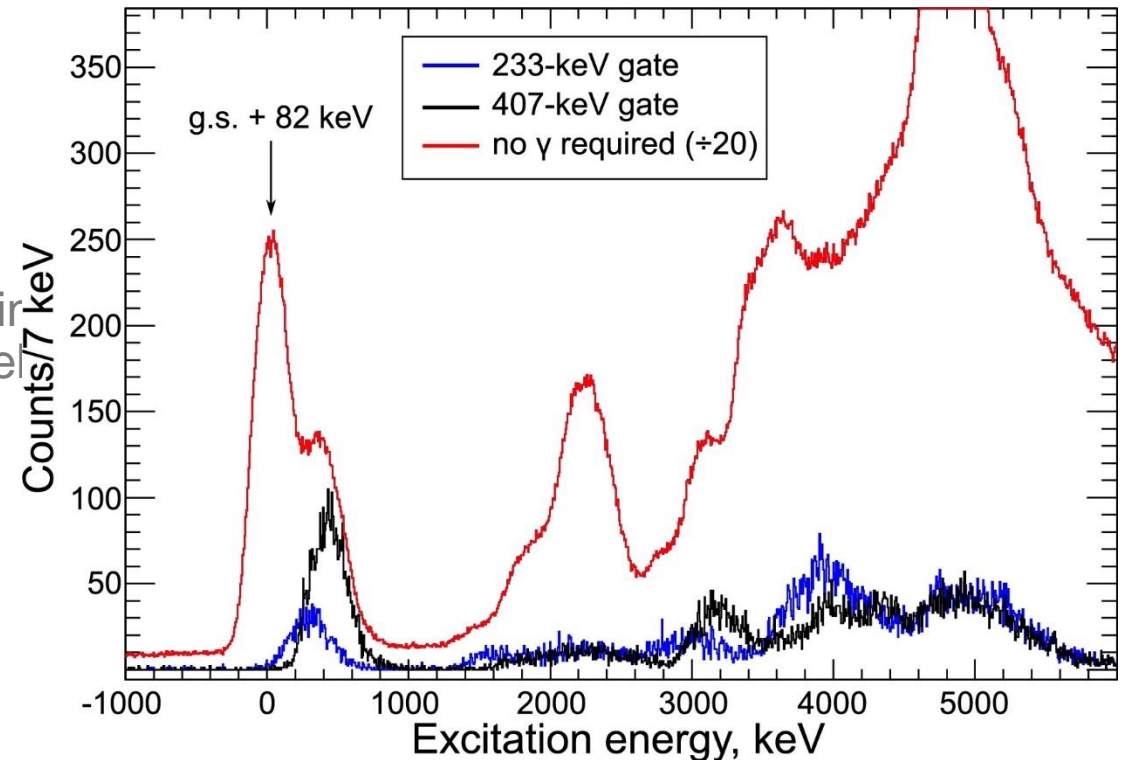
At TIGRESS, ^{28}Mg was studied through γ - γ coincidence, Doppler shift lifetime, & comparison to theory.

- Symmetry-adapted No Core Shell Model can describe enhanced deformation & $B(E2)$ values
- Positive-parity states dominated by sd configurations
- Negative-parity states understood with SPDF-MU interaction as single neutron excitation into pf shell



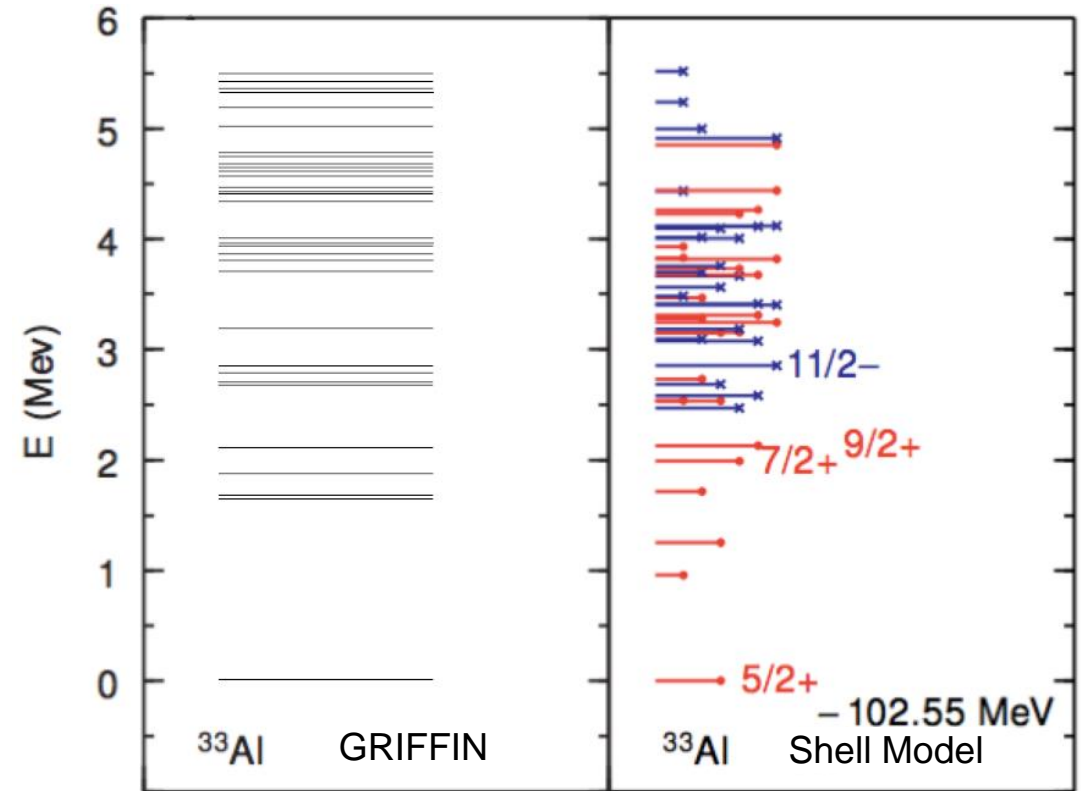
First observation of ^{26}Na levels with single-particle character were performed at TIGRESS.

- $^{25}\text{Na}(d,p\gamma)^{26}\text{Na}$ measured with TIGRESS + SHARC
- Excitation energies & spectroscopic factors in good agreement with $(0+1)\hbar\omega$ shell model calculations in full *spsd pf* basis
- Enhanced role of $\nu 1p_{3/2}$ configuration in structure of low-lying negative parity states (relative to ^{28}Al)

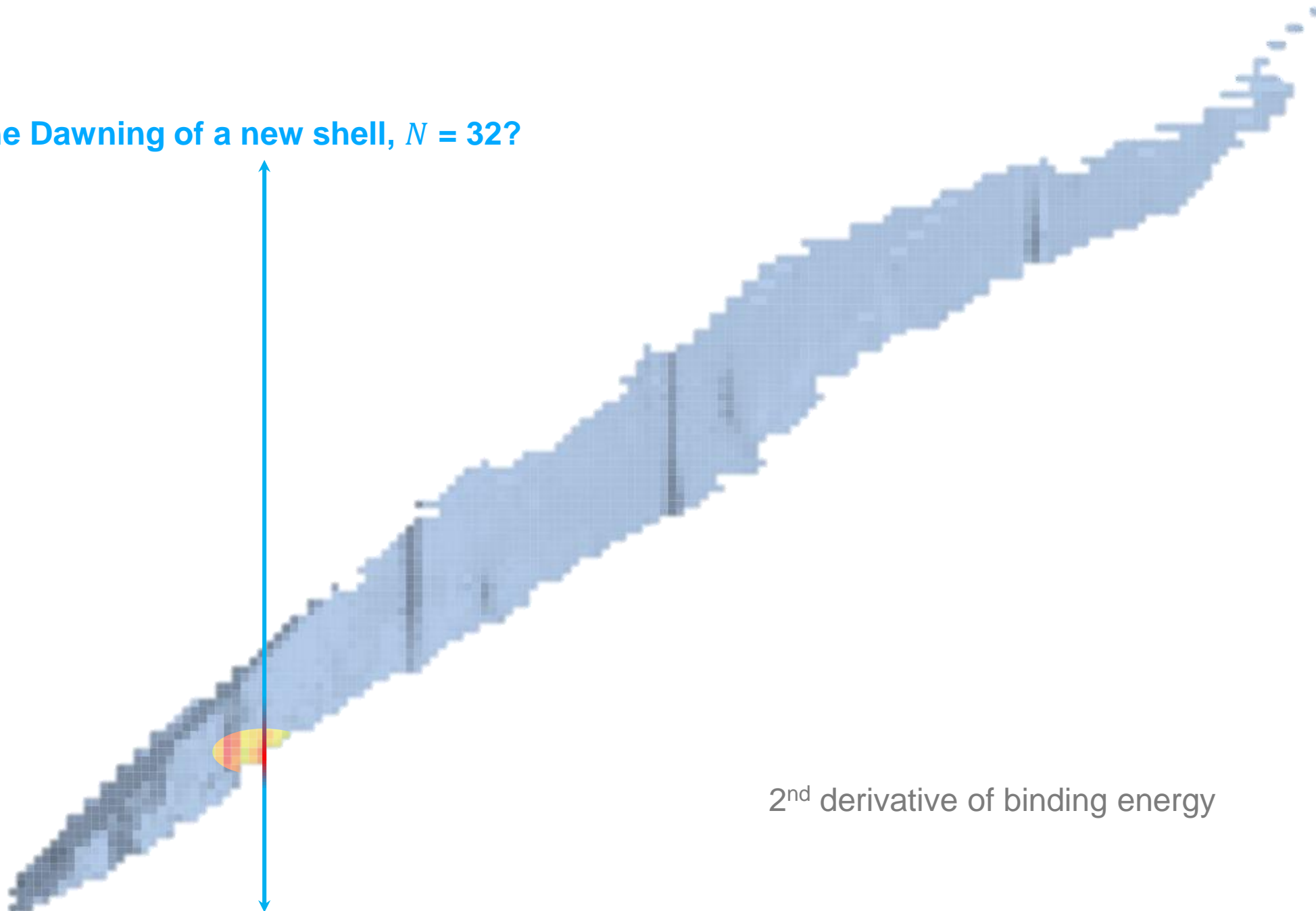


Spectroscopic information of $^{33-35}\text{Mg}$, the center of the “Island of Inversion”, is forthcoming from GRIFFIN

- Decay scheme of ^{33}Al measured with GRIFFIN + SCEPTAR:
 - 32 states & 100 transitions clarified
 - half-lives of ^{33}Mg , $^{32,33}\text{Al}$, ^{33}Si determined
- Decay of $^{34,35}\text{Mg}$ under analysis
- Experiment S1367 will be continued with higher statistics

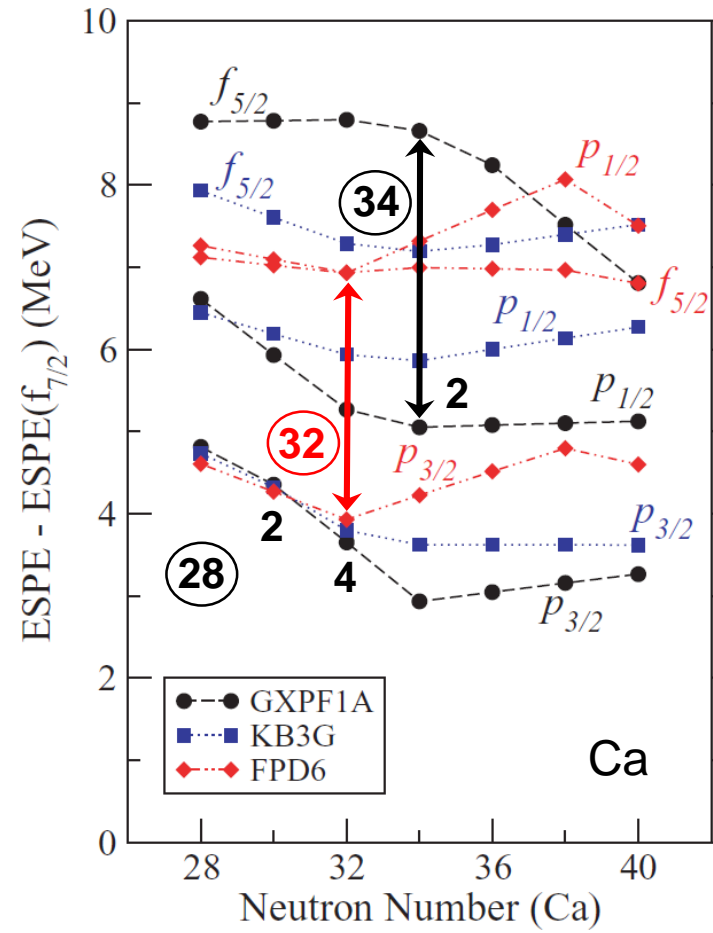


The Dawning of a new shell, $N = 32$?

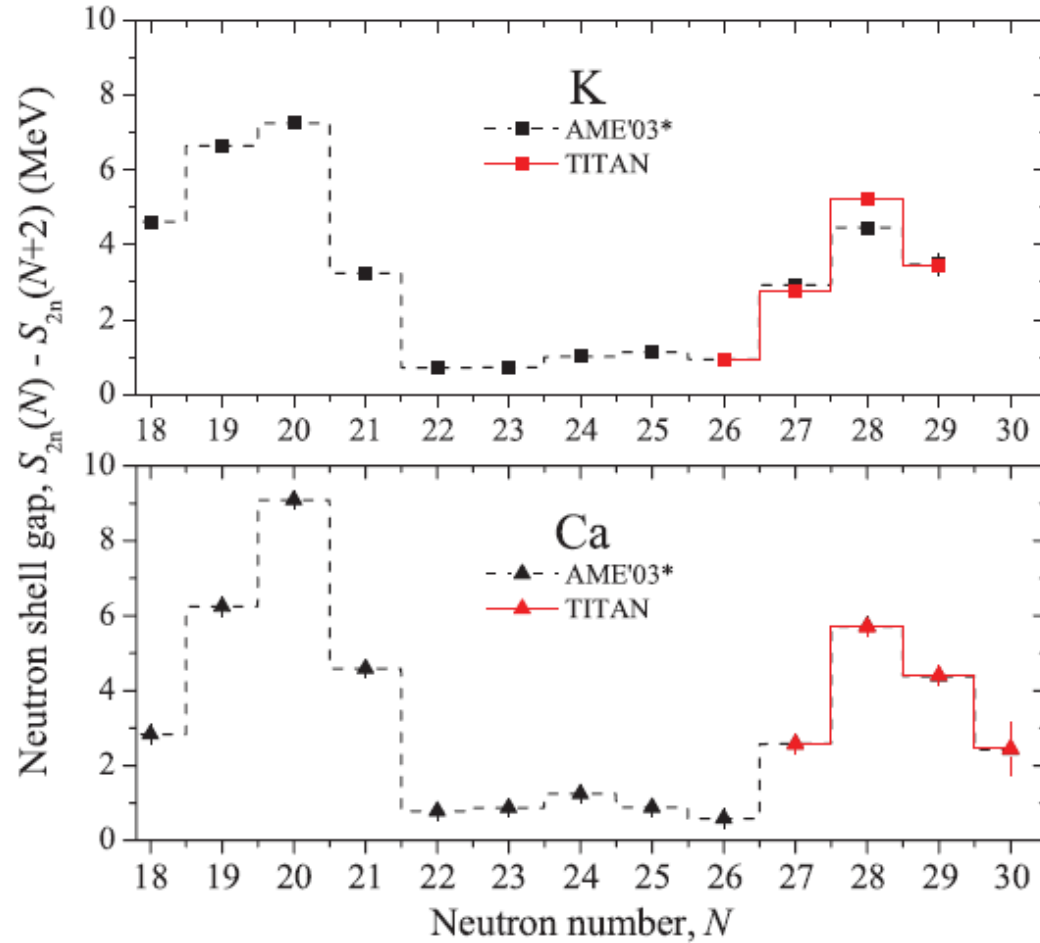
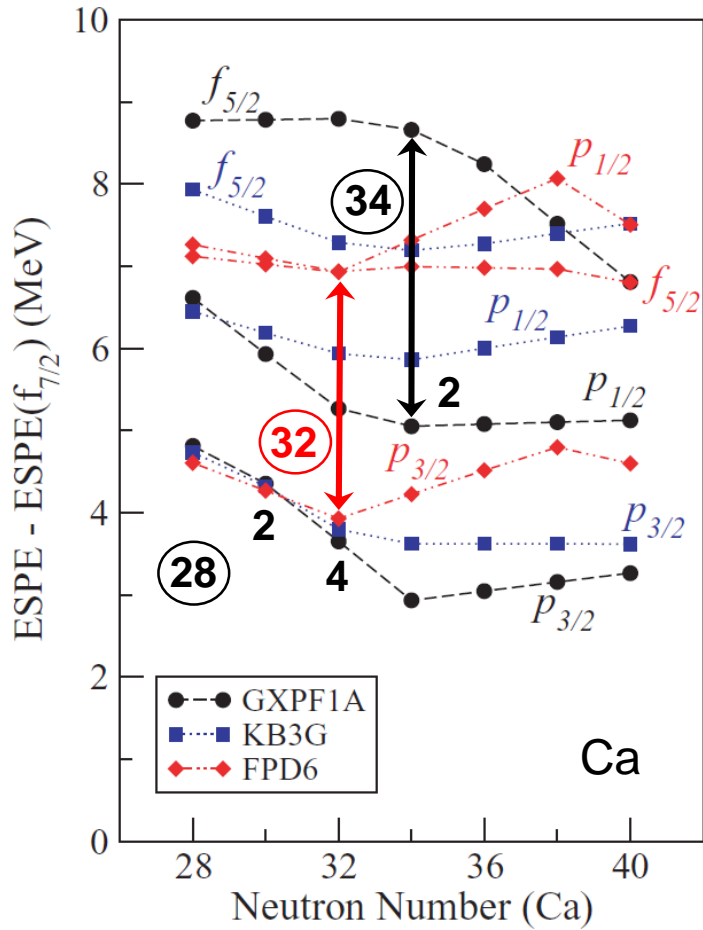


2nd derivative of binding energy

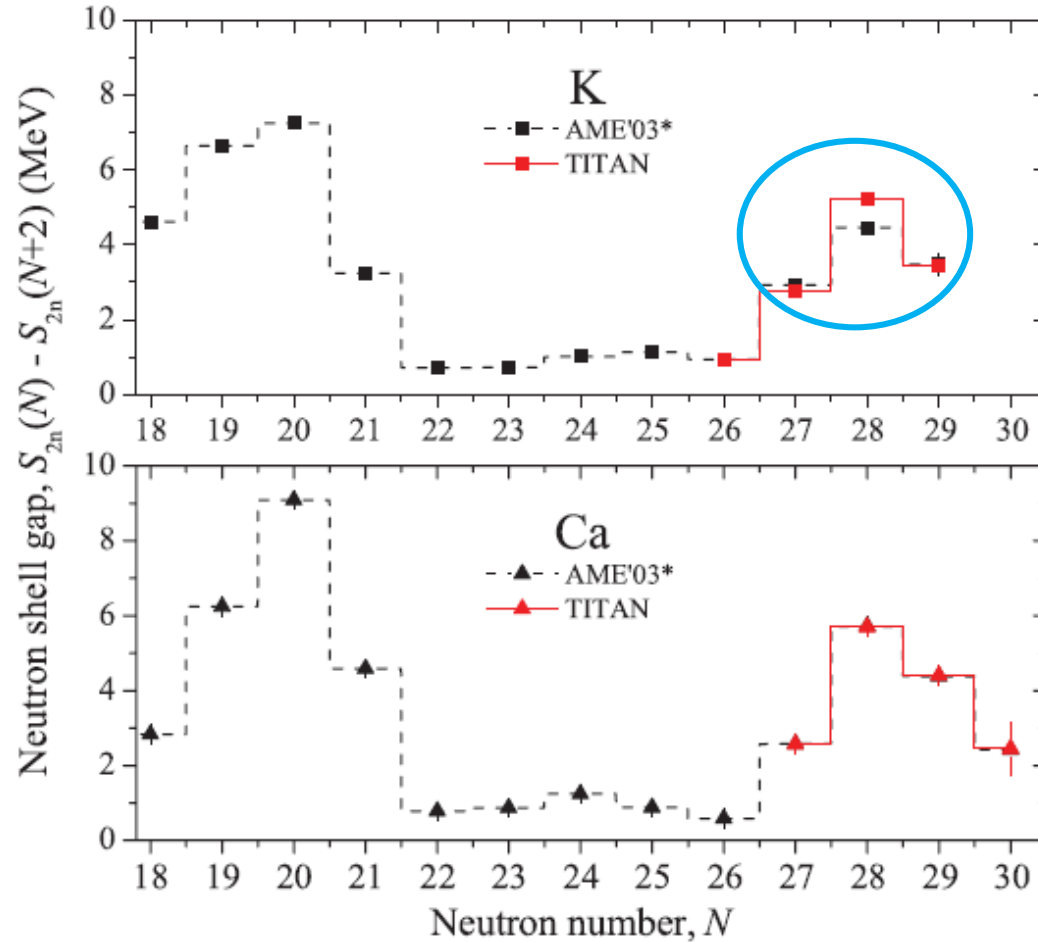
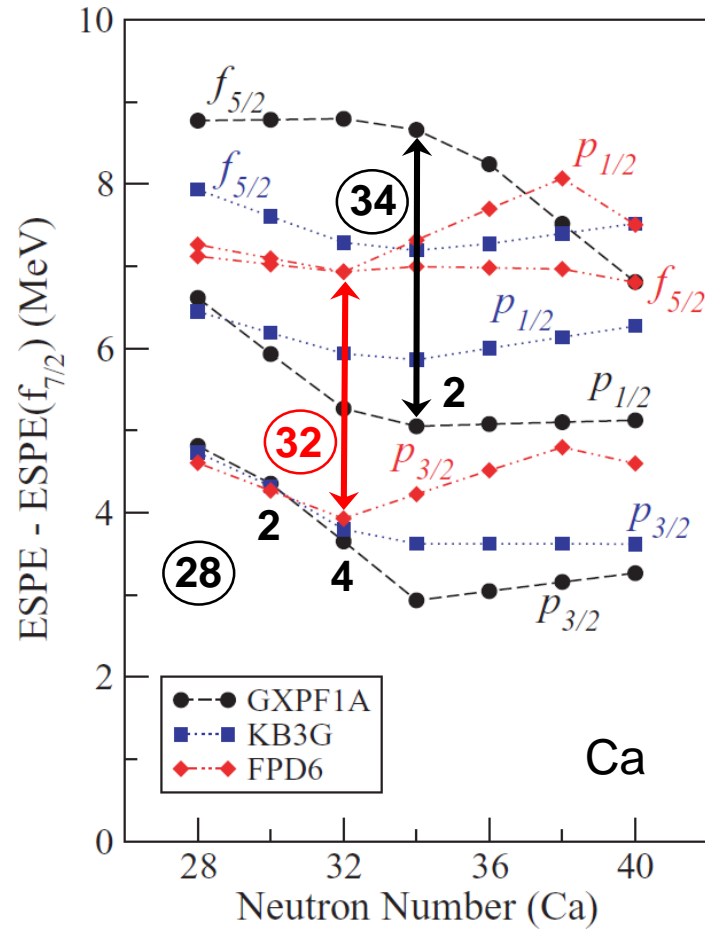
The question of magicity at $N = 32$ was unclear from phenomenological calculations.



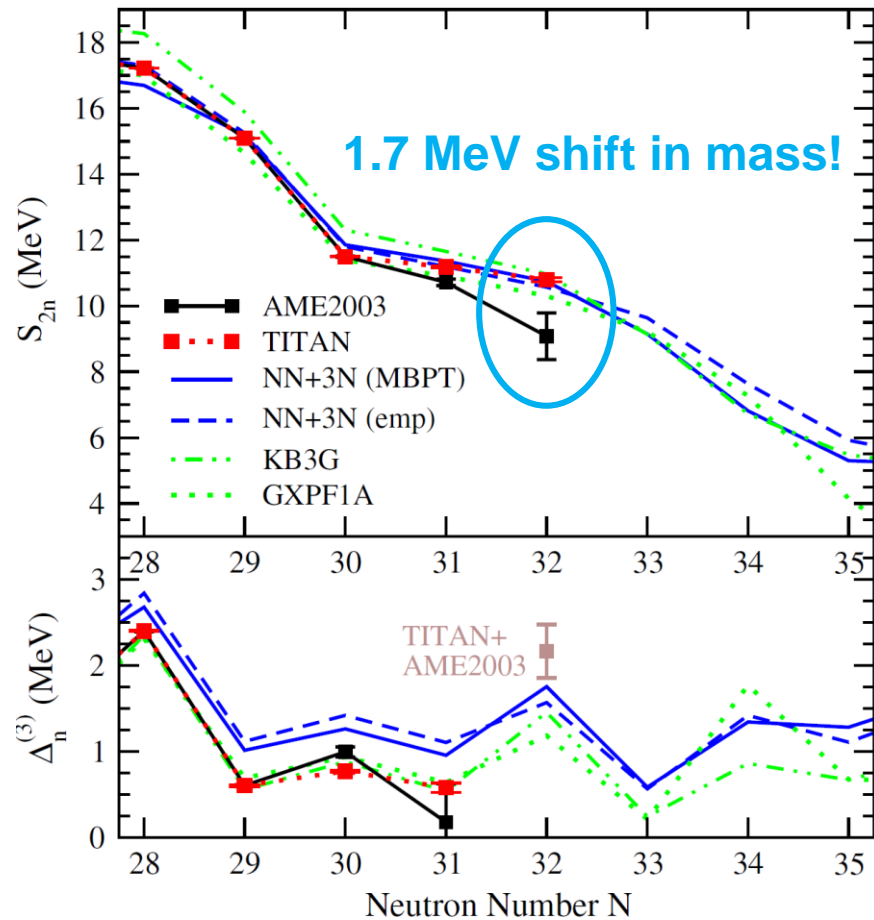
Strategy was to approach from $N = 28$, which was validated through TITAN's mass measurements of K & Ca isotopes.



Strategy was to approach from $N = 28$, which was validated through TITAN's mass measurements of K & Ca isotopes.



With UCx targets, TITAN reached ^{52}Ca and confirmed magicity of $N=32$.



- A 1.7 MeV deviation in $M(^{52}\text{Ca})$ observed!
- Shift confirmed by ISOLTRAP, which measured masses up to ^{54}Ca
- Support of nascent NN and 3N calculations

Systematics of Ca structure can be observed through decay of K isotopes observed at GRIFFIN spectrometer.

- Three beamtime periods with GRIFFIN
- 1 publication (2017), 4 expected in 2019
 - 1 PhD thesis, 2 Masters thesis
 - 1 Masters thesis in progress

Cr48 21.56 h 0+	Cr49 42.3 m 5/2-	Cr50 1.8E+17 y 0+	Cr51 27.702 d 7/2-	Cr52 0+	Cr53 3/2-	Cr54 0+	Cr55 3.497 m 3/2-	Cr56 5.94 m 0+	Cr57 21.1 s 3/2-,5/2-,7/2-	Cr58 7.0 s 0+
EC		ECEC 4.345	EC	83.789	9.501	2.365	β	β	β	β
V47 32.6 m 3/2-	V48 15.9735 d 4+	V49 330 d 7/2-	V50 1.4E+17 y 6+	V51 7/2-	V52 3.743 m 3+	V53 1.61 m 7/2-	V54 49.8 s 3+	V55 6.54 s (7/2-)	V56	V57
EC	EC		EC,β _{0.280}	90 750	β	β	β	β		
Ti46 0+	Ti47 5/2-	Ti48 0+	Ti49 7/2-	Ti50 0+	Ti51 5.76 m 3/2-	Ti52 1.7 m 0+	Ti53 32.7 s (3/2-)	Ti54 0+	Ti55	Ti56 0+
8.0	7.3	73.8	5.5	5.4	β	β	β			
Se45 7/2- 100	Se46 83.79 d 4+	Se47 3.3492 d 7/2-	Se48 43.67 h 6+	Se49 57.2 m 7/2-	Se50 102.5 s 5+	Se51 12.4 s (7/2-)	Se52 8.2 s 3+	Se53	Se54	Se55
*	β	β	β	β	β	β	β			
Ca44 0+	Ca45 162.61 d 7/2-	Ca46 0+	Ca47 4.536 d 7/2-	Ca48 6E+18 y 0+	Ca49 8.718 m 3/2-	Ca50 13.9 s 0+	Ca51 10.0 s (3/2-)	Ca52 4.6 s 0+	Ca53 90 ms (3/2-,5/2-)	Ca54 0+
2.086	β	0.004	β	3,ββ _{0.187}	β	β	β	β	β	β
K43 22.3 h 3/2+	K44 22.13 m 2-	K45 17.3 m 3/2+	K46 105 s (2-)	K47 17.50 s 1/2+	K48 6.8 s (2-)	K49 1.26 s (3/2+)	K50 472 ms (0-,1,2-)	K51 365 ms (1/2+,3/2+)	K52 105 ms	K53 30 ms (3/2+)
β	β	β	β	β	β	β	β	β	β	β
Ar42 32.9 y 0+	Ar43 5.37 m (3/2,5/2)	Ar44 11.87 m 0+	Ar45 21.48 s	Ar46 8.4 s 0+	Ar47 700 ms	Ar48 0+	Ar49	Ar50 0+	Ar51	Ar52 0+
β	β	β	β	β	β	β				

⁵⁰Sc - ⁵⁰Ti, Nov 2016, 1x10⁶pps, ~5hrs
 "Search for particle-hole excitations across the N=28 shell closure", C. Jones, **Masters thesis (Jan 2018)**, Submitted to *Phys. Rev. C* (2019).

⁵⁰Ca - ⁵⁰Sc, Nov 2016, 1x10⁶pps, ~2hrs
 "Spectroscopy of ⁵⁰Sc and the first calculation of B(M3) strengths using *ab initio* methods", A.B. Garnsworthy, *Phys. Rev. C* 96, 044329 (2017).

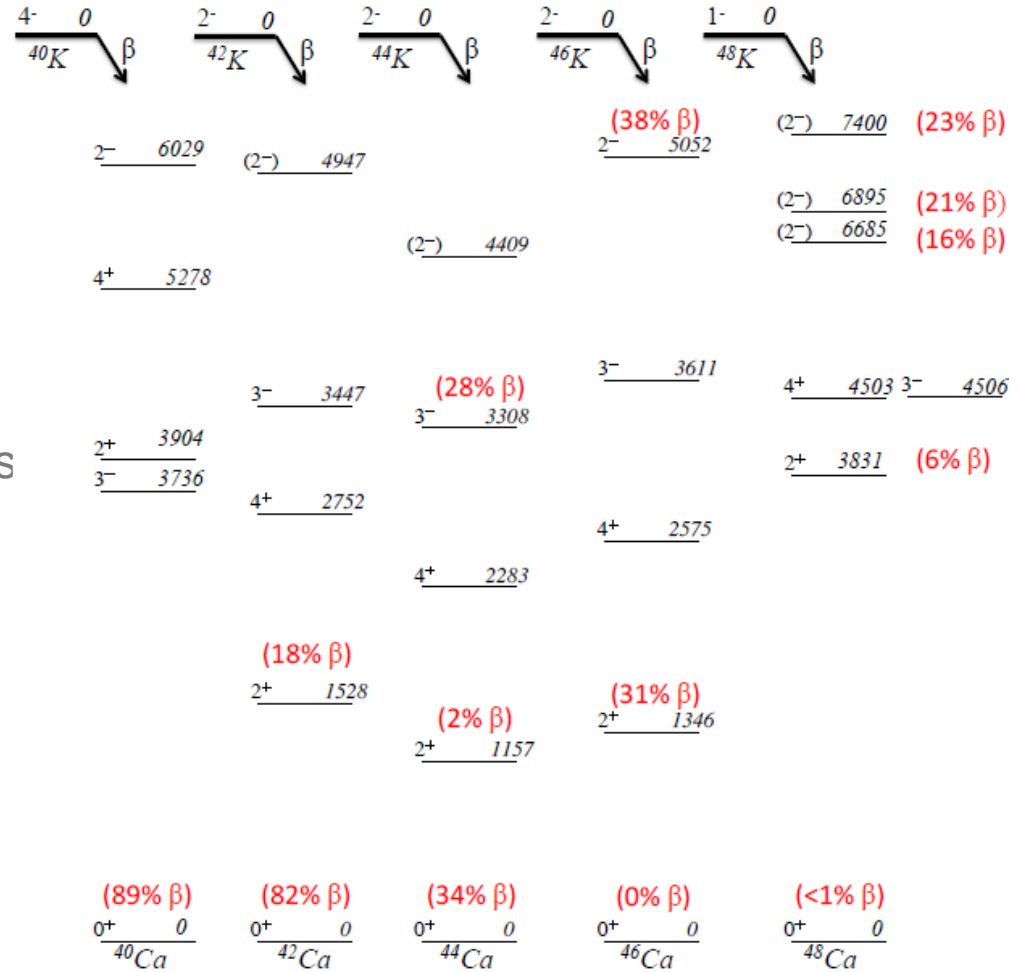
⁵²K - ⁵²Ca, Jul 2018, 300pps, ~48hrs
 "Evolution of Shell Structure in Neutron-Rich Calcium Isotopes", R. Coleman, Masters thesis Univ. of Guelph, in preparation for *Phys. Rev. C* (2019).

⁴⁶K - ⁴⁶Ca, Dec 2014, 4x10⁵pps, ~40hrs
 "Detailed spectroscopy of ⁴⁶Ca: The investigation of the β decay of ⁴⁶K with the GRIFFIN γ-ray spectrometer", J.L. Pore, **PhD thesis (2016) SFU**, submitted to *Phys. Rev. C* (2019).

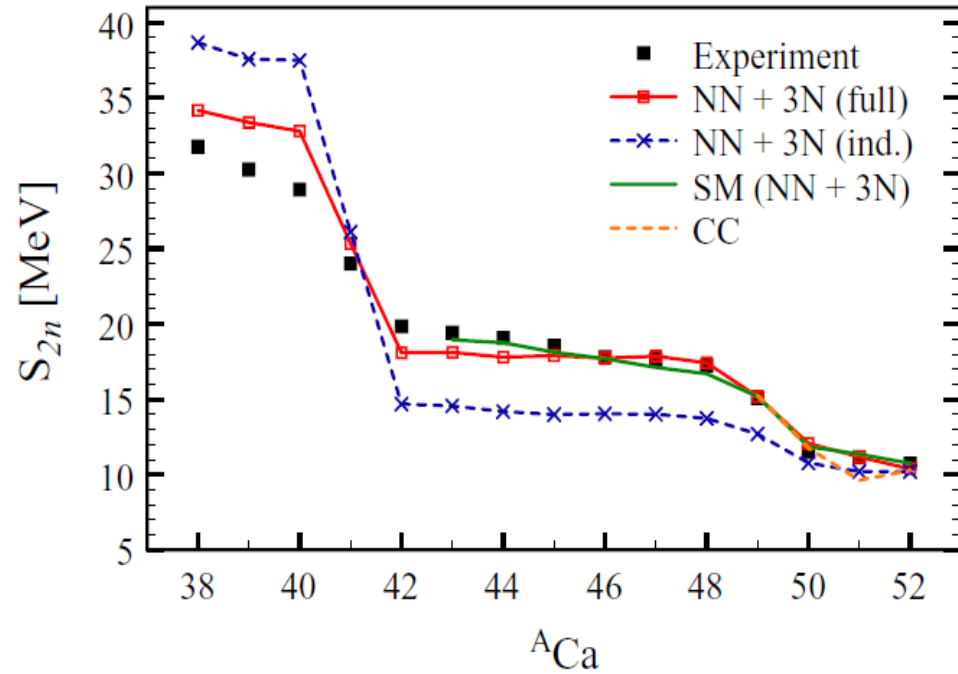
⁴⁷K - ⁴⁷Ca, Dec 2014, 1x10⁵pps, ~90hrs
 "Detailed decay spectroscopy of ⁴⁷Ca", J.K. Smith, in preparation for *Phys. Rev. C* (2019).

The ground state of ^{46}K exhibits more $\pi s_{1/2}$ character than previously believed.

- 150 new γ -ray transitions and 12 new excited states observed
- Angular correlations allowed for spin assignments
- Based on β feeding intensities ^{46}K may be more strongly dominated by $\pi s_{1/2}$ (mixed with $\pi d_{3/2}$)

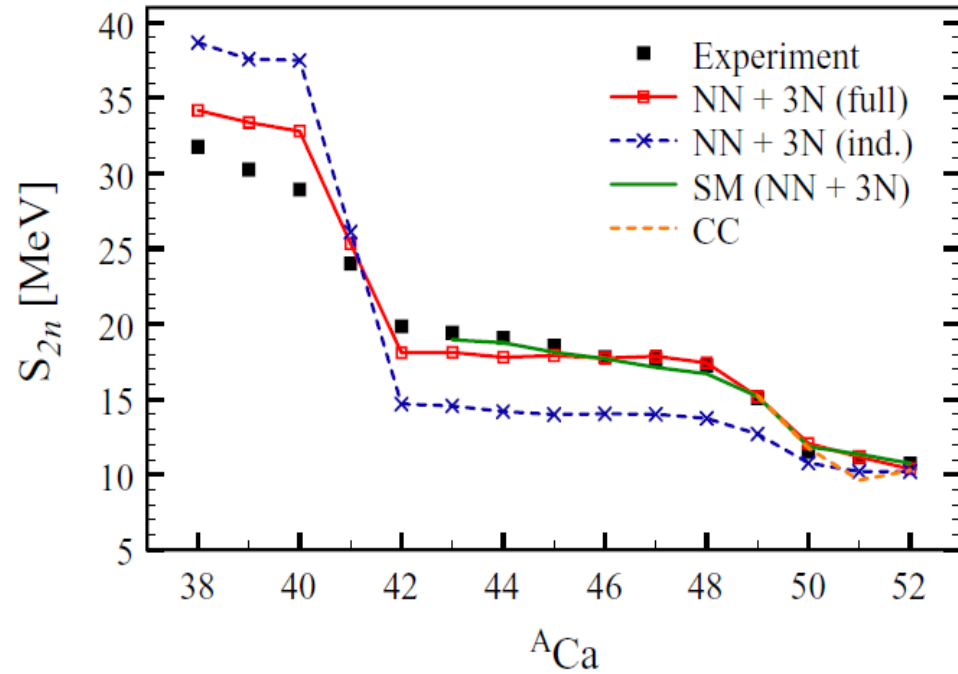


Validated, *ab initio* theory surpassed experiment, reaching the Ca dripline.

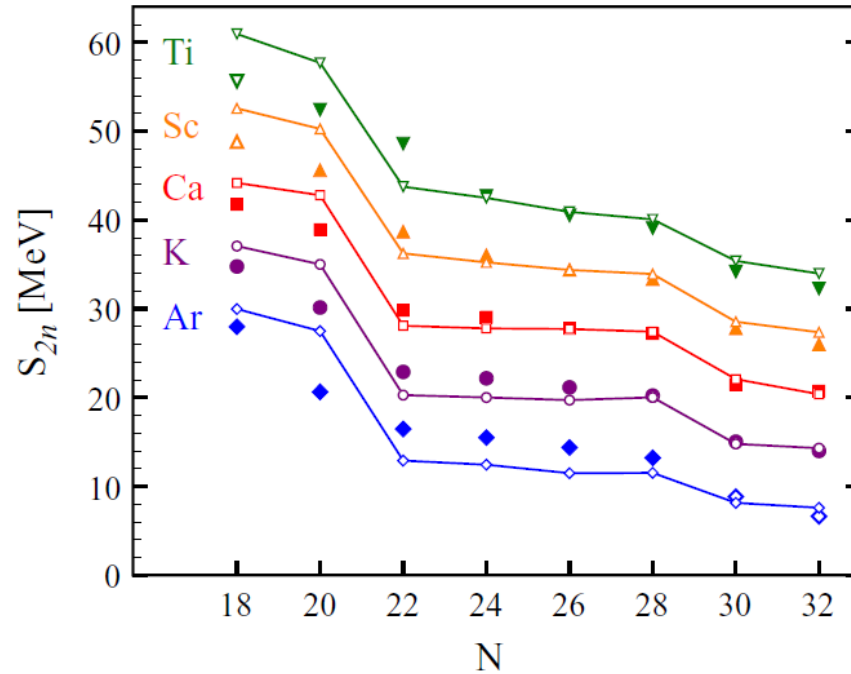


Predictions of dripline near ^{60}Ca are beyond present experimental reach.

Validated, *ab initio* theory surpassed experiment, reaching the Ca dripline.

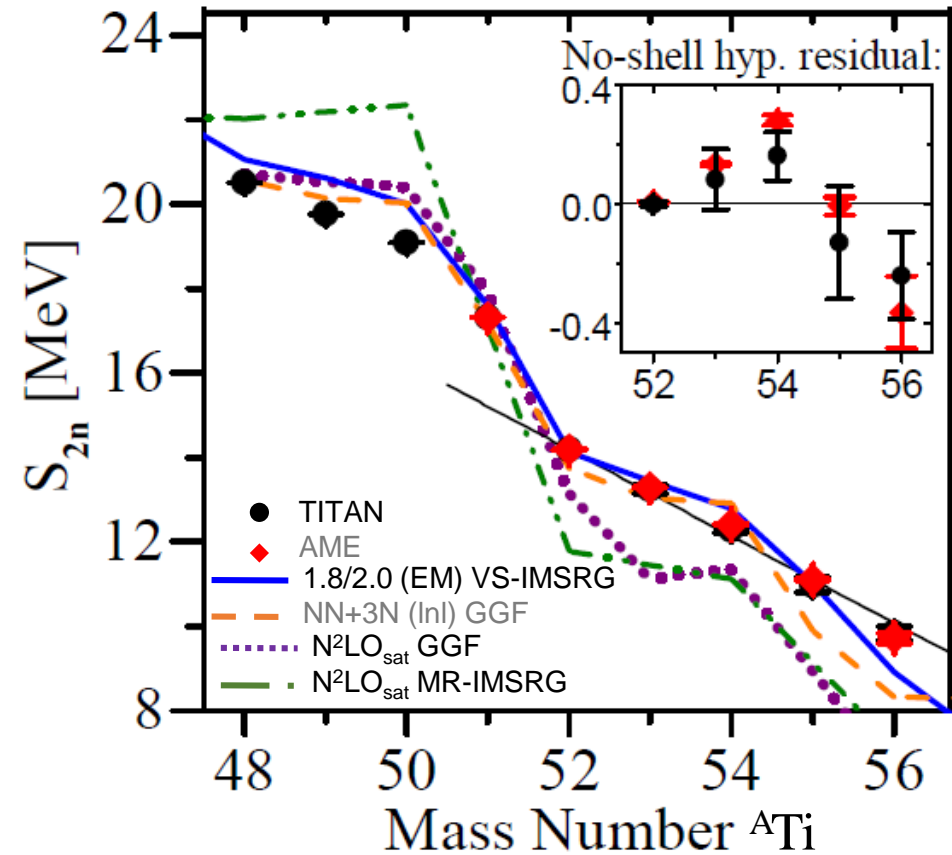


Predictions of dripline near ^{60}Ca are beyond present experimental reach.



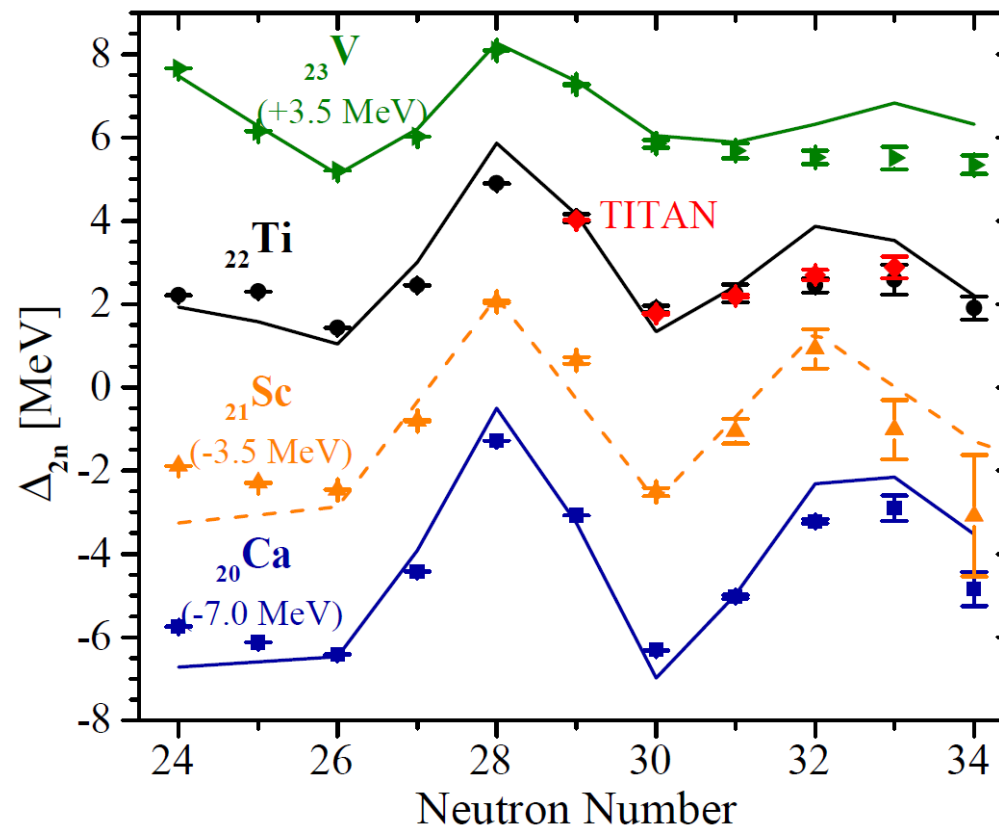
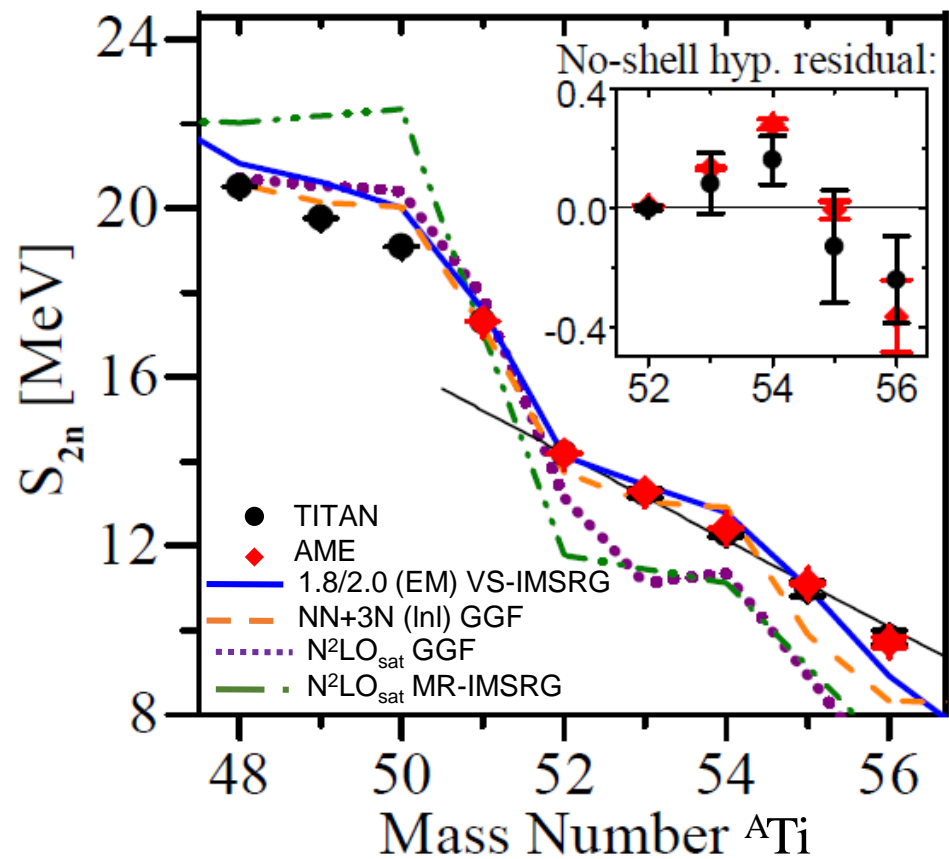
First *ab-initio* predictions for open shells in mid-mass regime from P. Navrátil & collaborators.

TITAN masses of Ti & V demonstrate the transitional role of Ti and were compared to TRIUMF *ab initio* predictions.

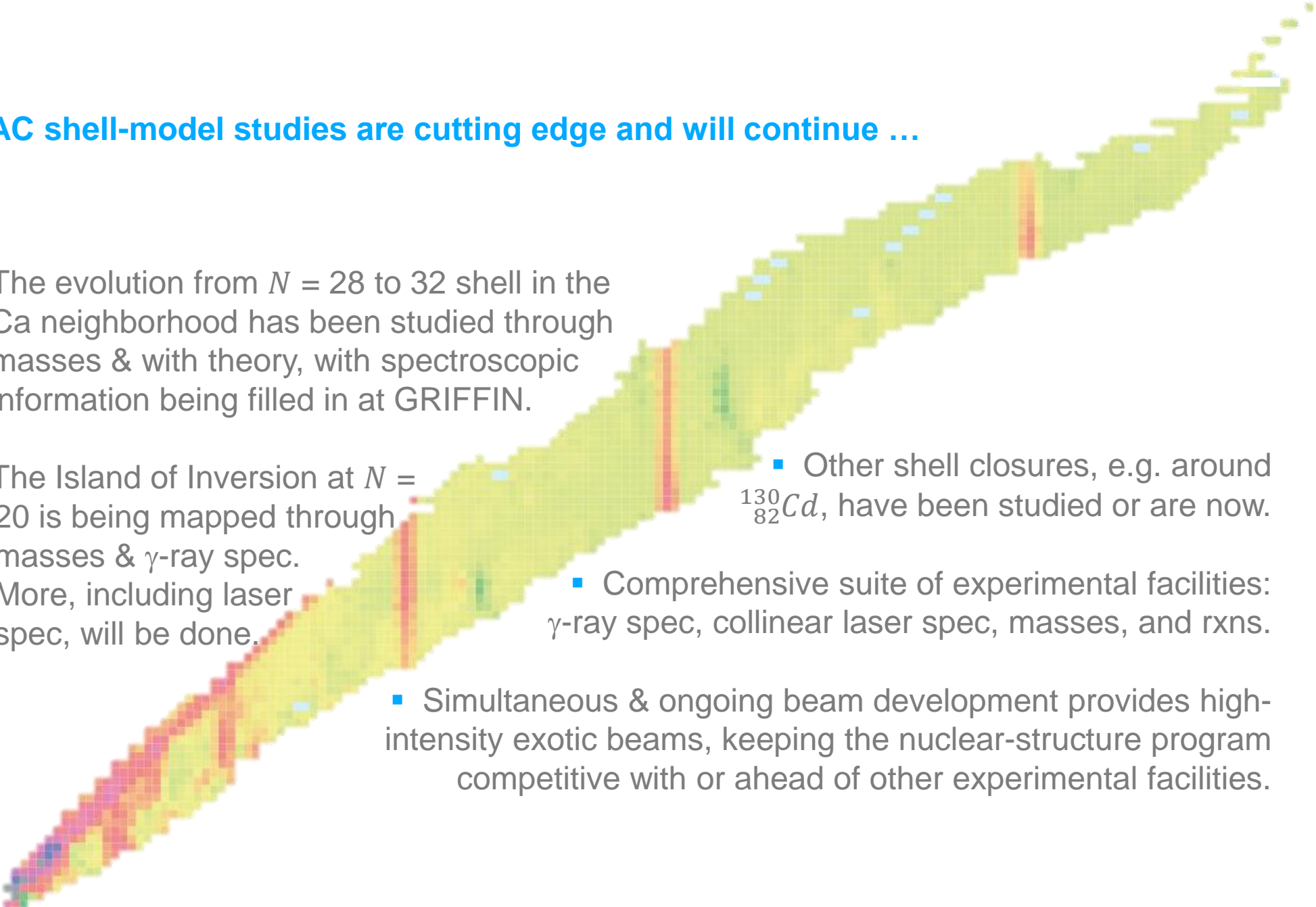


- *Ab initio* calculations from
 - Peter Navrátil & collaborators
 - Jason Holt & collaborators
 - Heiko Hergert

TITAN's mass measurements of Ti & V demonstrate the transitional role of Ti.



ISAC shell-model studies are cutting edge and will continue ...

- 
- The evolution from $N = 28$ to 32 shell in the Ca neighborhood has been studied through masses & with theory, with spectroscopic information being filled in at GRIFFIN.
 - The Island of Inversion at $N = 20$ is being mapped through masses & γ -ray spec. More, including laser spec, will be done.
 - Other shell closures, e.g. around $^{130}_{82}\text{Cd}$, have been studied or are now.
 - Comprehensive suite of experimental facilities: γ -ray spec, collinear laser spec, masses, and rxns.
 - Simultaneous & ongoing beam development provides high-intensity exotic beams, keeping the nuclear-structure program competitive with or ahead of other experimental facilities.

Thank you
Merci

www.triumf.ca

Follow us @TRIUMFLab

