



**TRIUMF**

Canada's national laboratory  
for particle and nuclear physics  
and accelerator-based science

# Single Particle Structure of Exotic Sr Isotopes

Friday 15<sup>th</sup> July 2016

**Steffen Cruz**

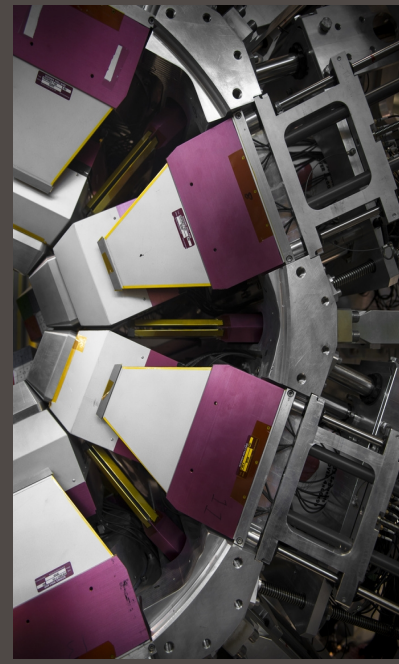
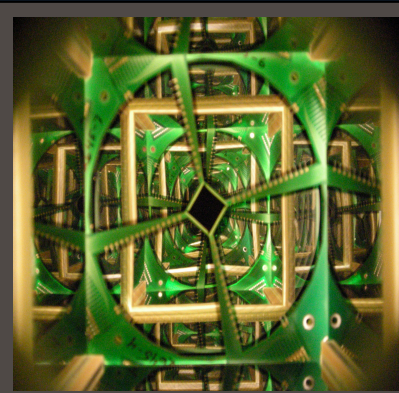
*UBC and TRIUMF*



# TRIUMF

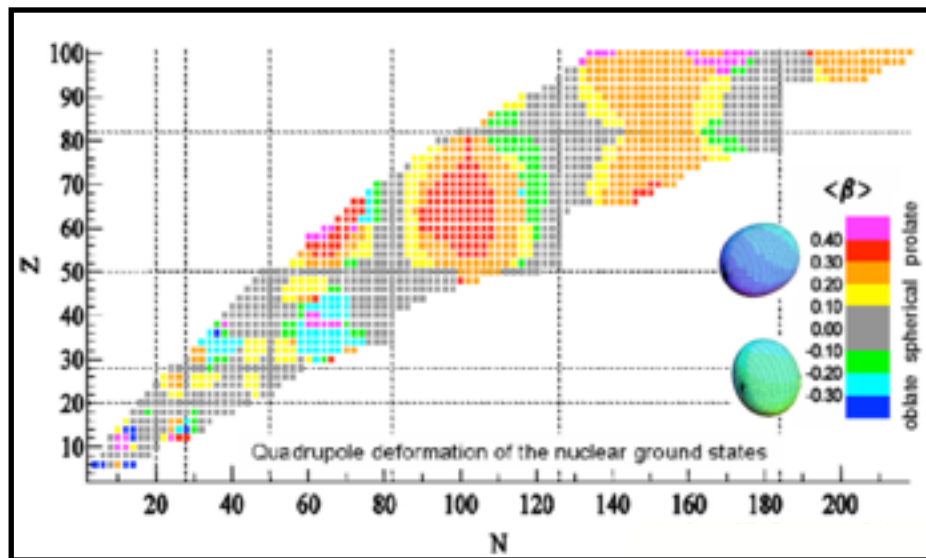
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- Single Particle Configurations
- Shape Coexistence
- $^{95}\text{Sr}(d,p)$  Experiment
- Interpretation of Results



- Shape deformation enables the nucleus to minimize its energy.
- HFB calculation (left) shows expected quadrupole deformation across nuclear chart.

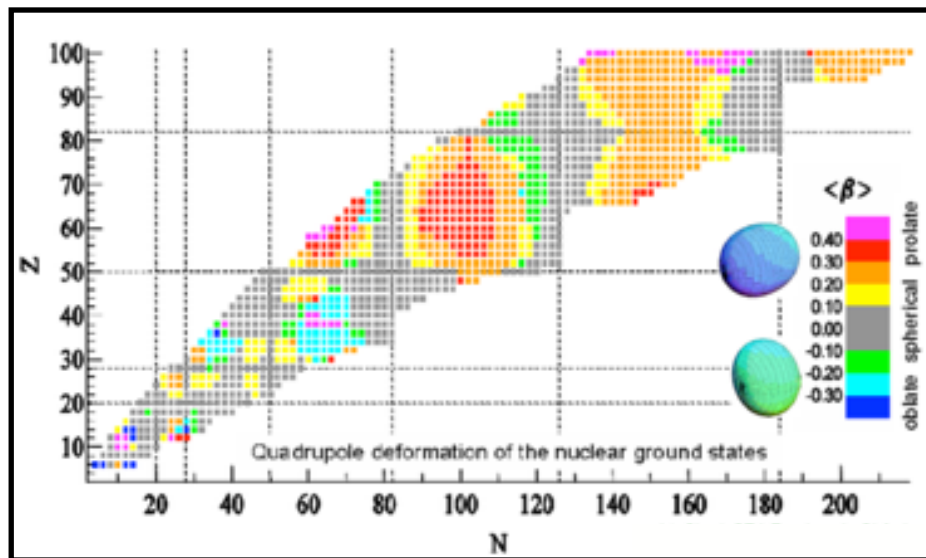
*Quadrupole deformation is a measure of nuclear shape.*



Plot source: M. Girod, CEA

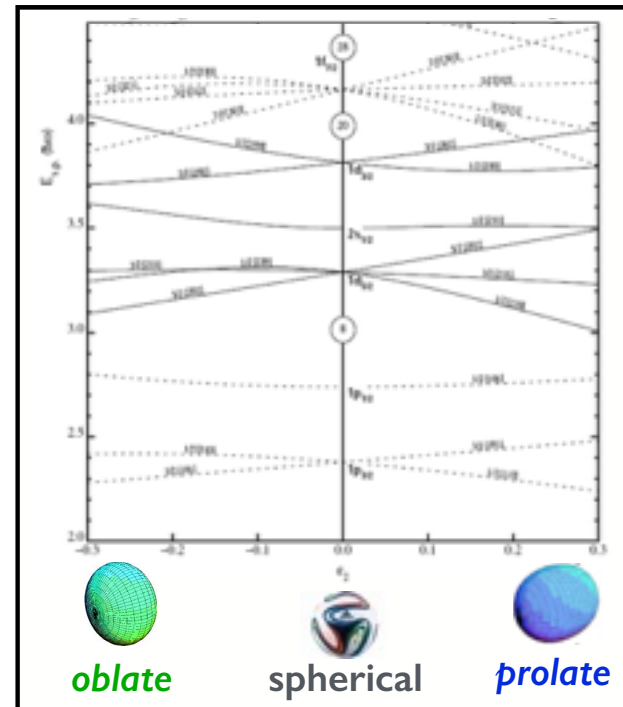
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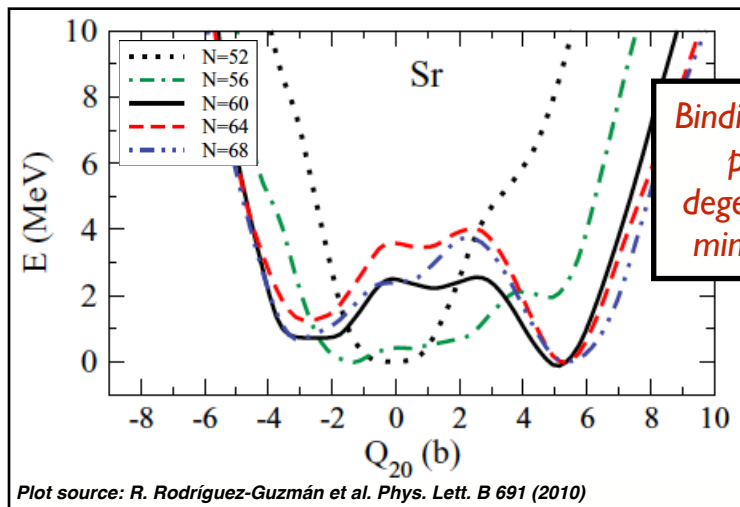
*Nilsson model: Different deformations have different single particle configurations*



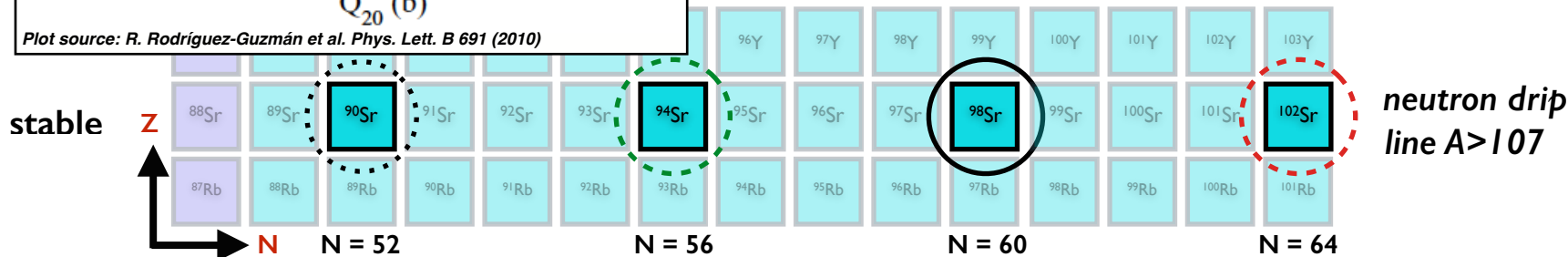
Plot source: R.F. Casten



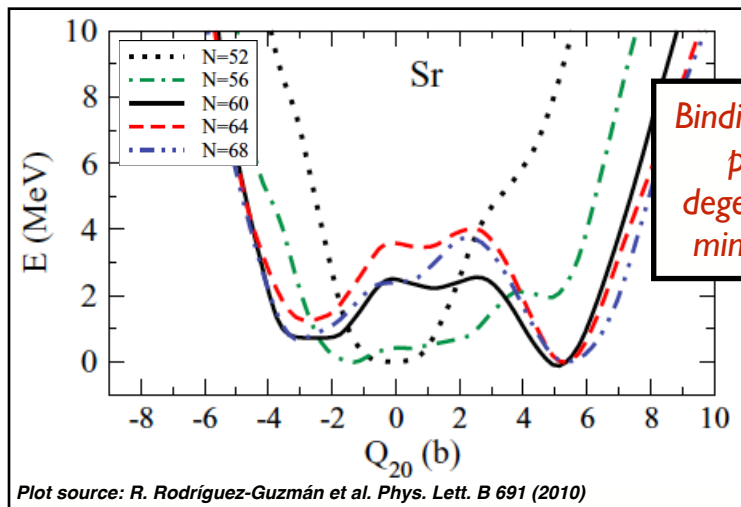
- State of the art (beyond mean field) calculations predict binding energy as a function of deformation.
- Measurements of single particle levels in  $^{95,96,97}\text{Sr}$  essential for a detailed description of this transitional region.



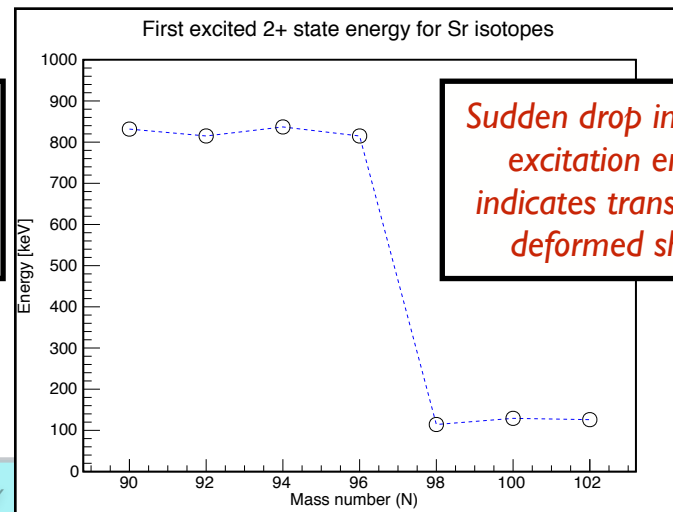
*Binding energy curves predict almost degenerate potential minima at  $N = 60$ .*



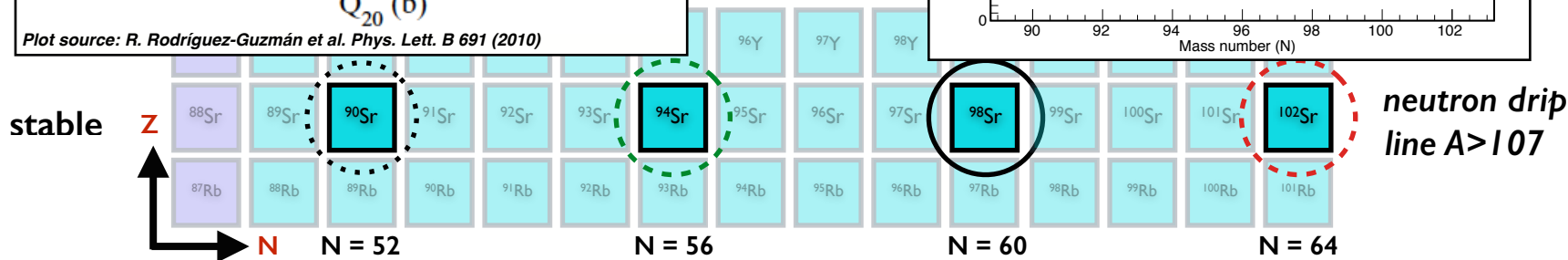
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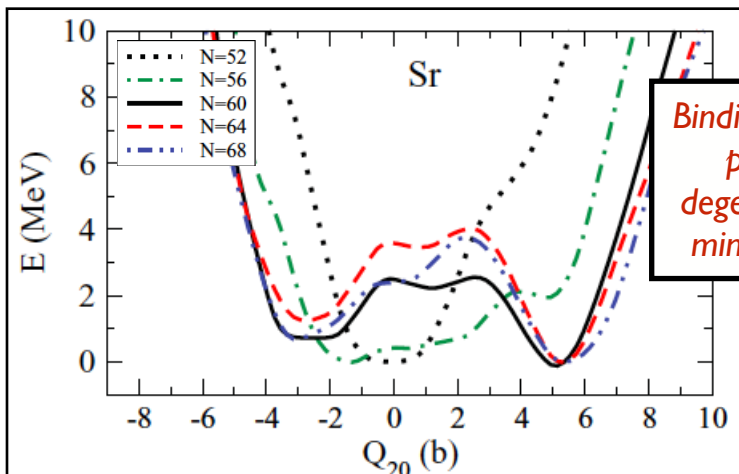
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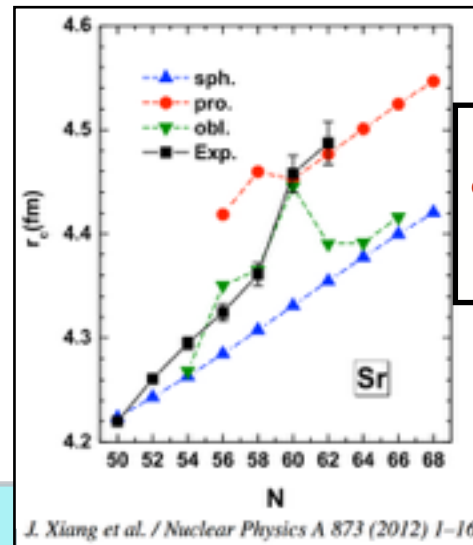
*Sudden drop in first  $2+$  excitation energy indicates transition to deformed shape*



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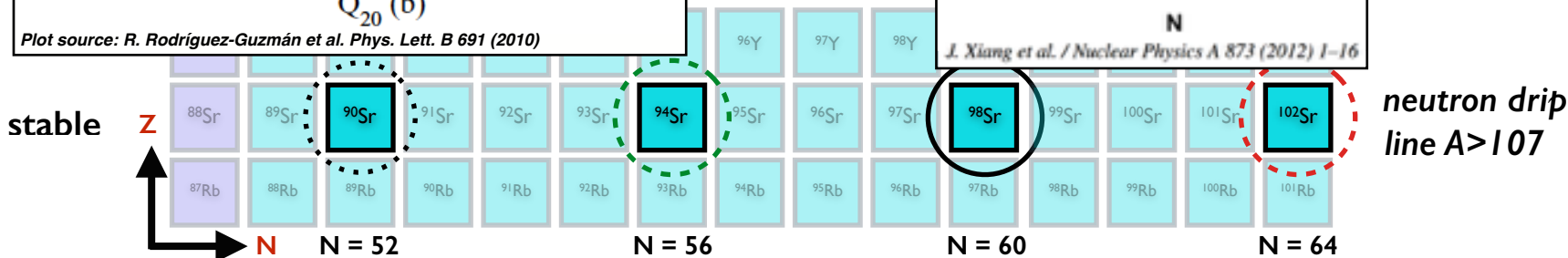
*Binding energy curves predict almost degenerate potential minima at  $N = 60$ .*



*Sudden increase in charge radius suggests change of ground state shape*

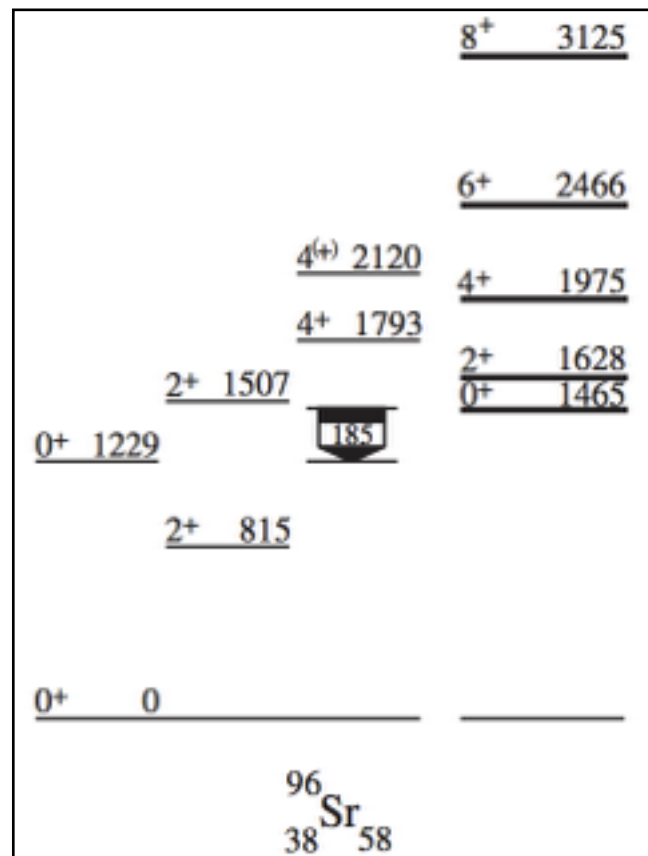
Plot source: R. Rodríguez-Guzmán et al. Phys. Lett. B 691 (2010)

J. Xiang et al. / Nuclear Physics A 873 (2012) 1–16



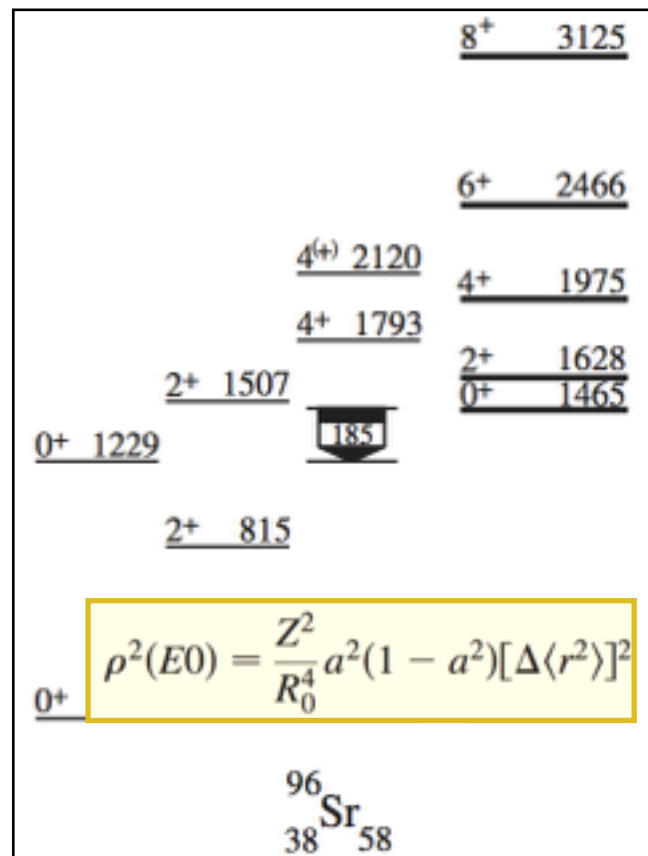
*neutron drip line  $A > 107$*

- The strong  $0_3^+$  (1465 keV)  $\rightarrow 0_2^+$  (1229 keV) E0 transition is characteristic of coexisting shapes.

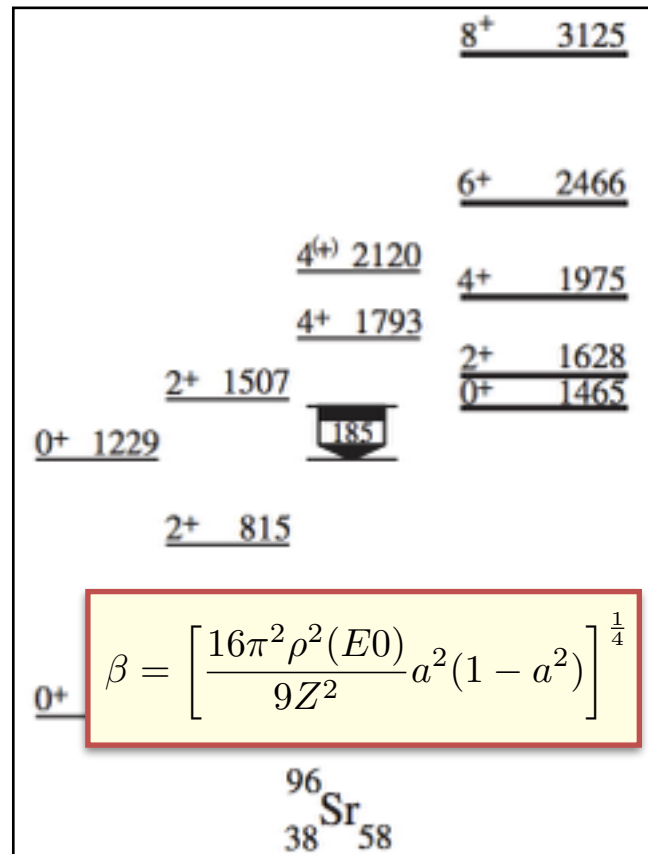




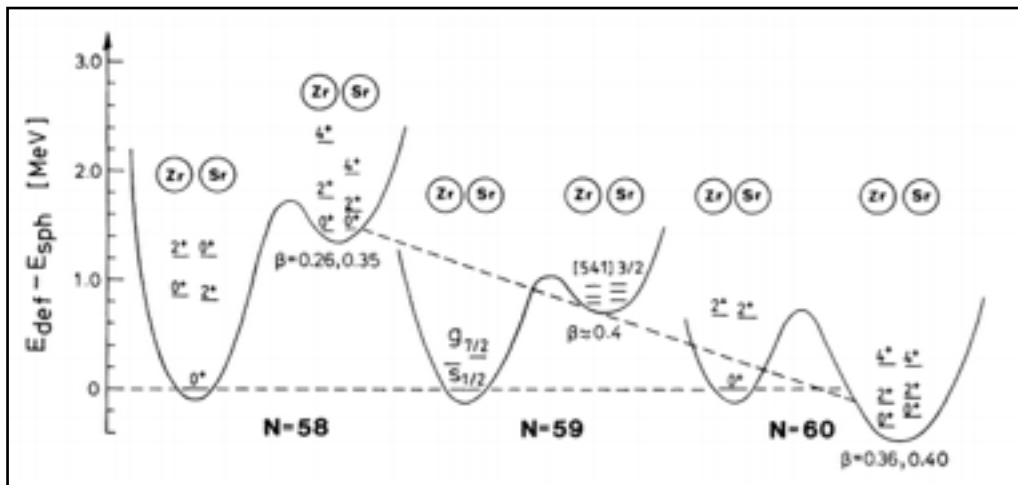
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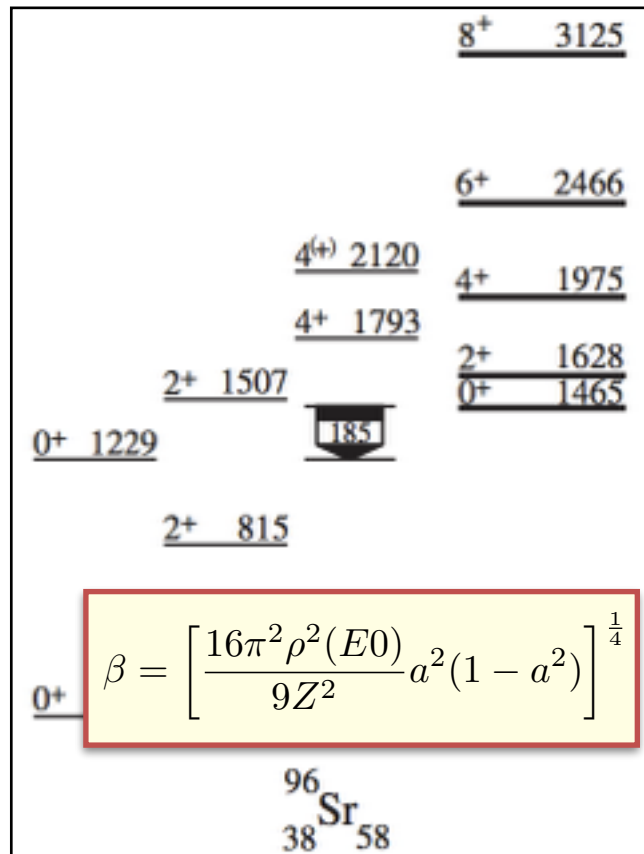
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- The deformed  $0_3^+$  state at 1465 keV is expected to be the same structure as the  $^{98}\text{Sr}$  ground state.

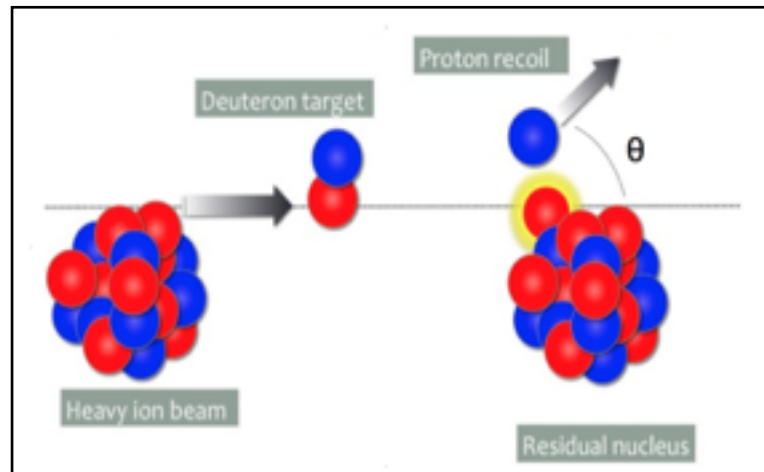


G. Lhersonneau et al., Phys. Rev. C 49, (1994) 1379



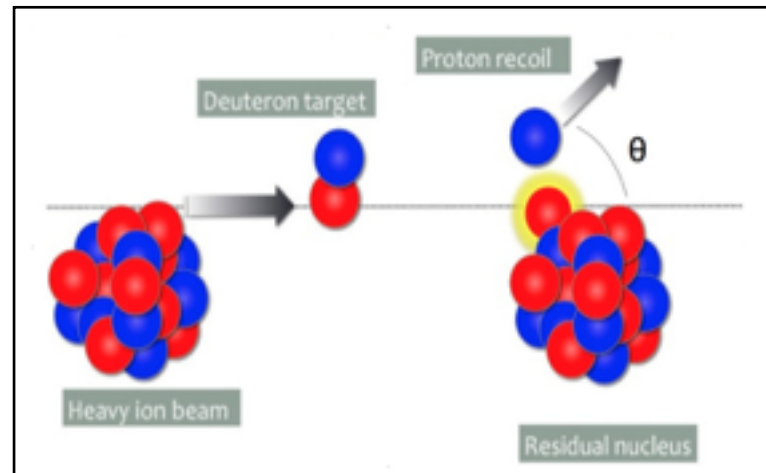
Shape coexistence in atomic nuclei  
[Rev. Mod. Phys. 83, 1467 (2011)]

$^{94,95,96}\text{Sr}(d,p)$  reactions to study evolution of structure in Sr through low energy single particle states.

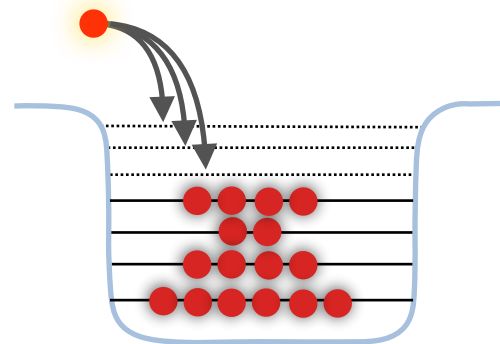




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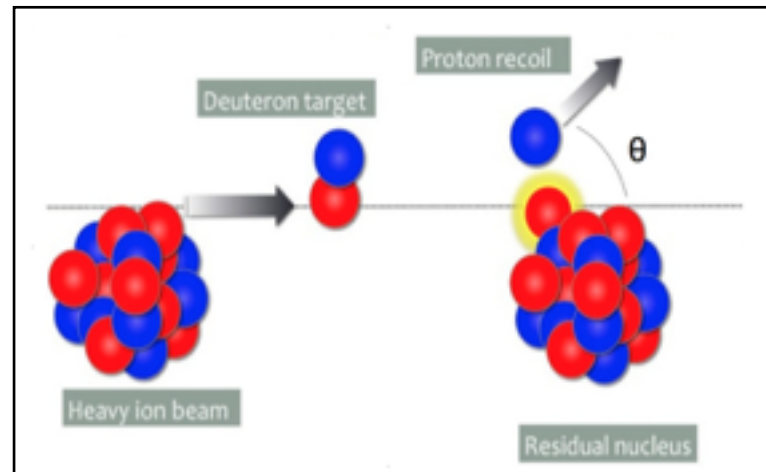
*Neutron populates one of the empty single particle orbitals*



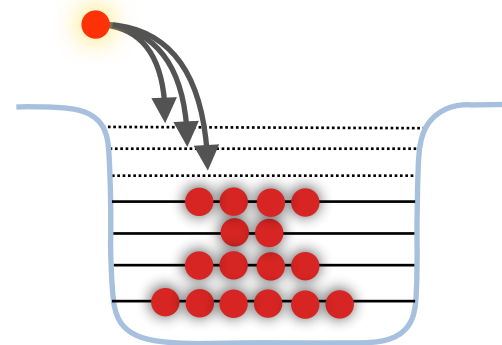
$^{94,95,96}\text{Sr}(d,p)$  reactions to study evolution of structure in Sr through low energy single particle states.

## Aims

- Measure angular momentum of Sr states.
- Measure cross section, which gives orbital occupation number.
- Compare occupation numbers to large scale shell model calculations that will be carried out in collaboration with shell model experts.

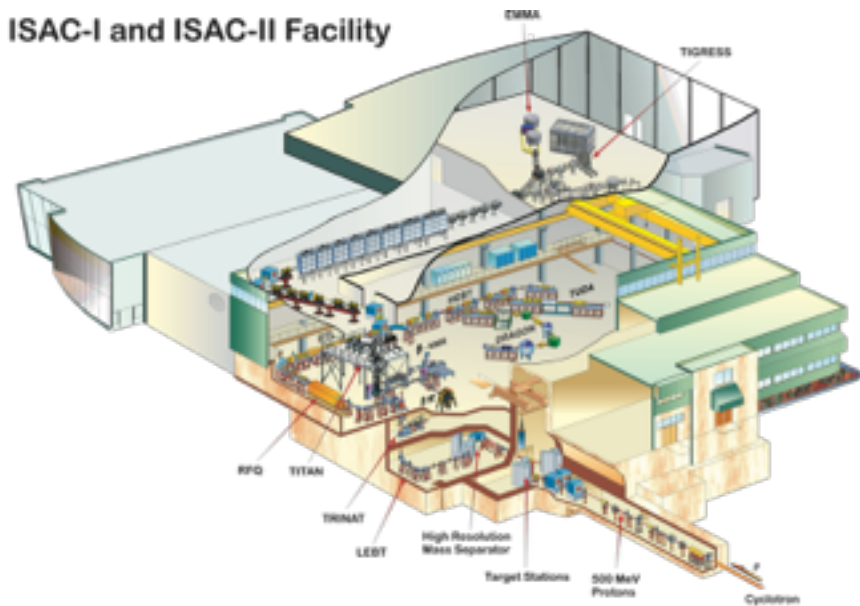


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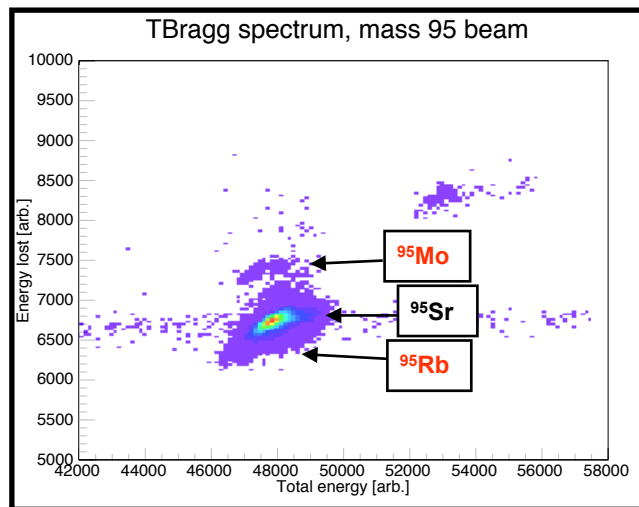
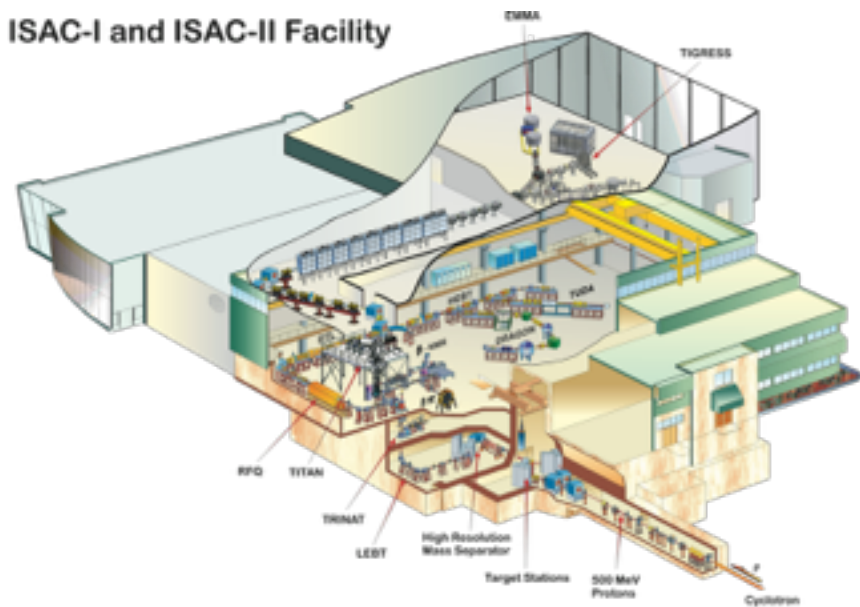
- A 500 MeV proton beam was impinged on a UCx target.
- Extracted isotopes were laser ionized, mass separated and transported to the CSB where the isotopes were charge bred to 16<sup>+</sup>.
- Beam re-accelerated to 5.5 MeV/u and impinged on 0.5mg/cm<sup>2</sup> CD<sub>2</sub> target (~10<sup>6</sup> p.p.s) .

ISAC-I and ISAC-II Facility



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ISAC-I and ISAC-II Facility



Composition of radioactive beam was ~98% <sup>95</sup>Sr.

*Sr experiments were first high mass ( $A > 30$ ) experiment using secondary-accelerated beams at TRIUMF.*

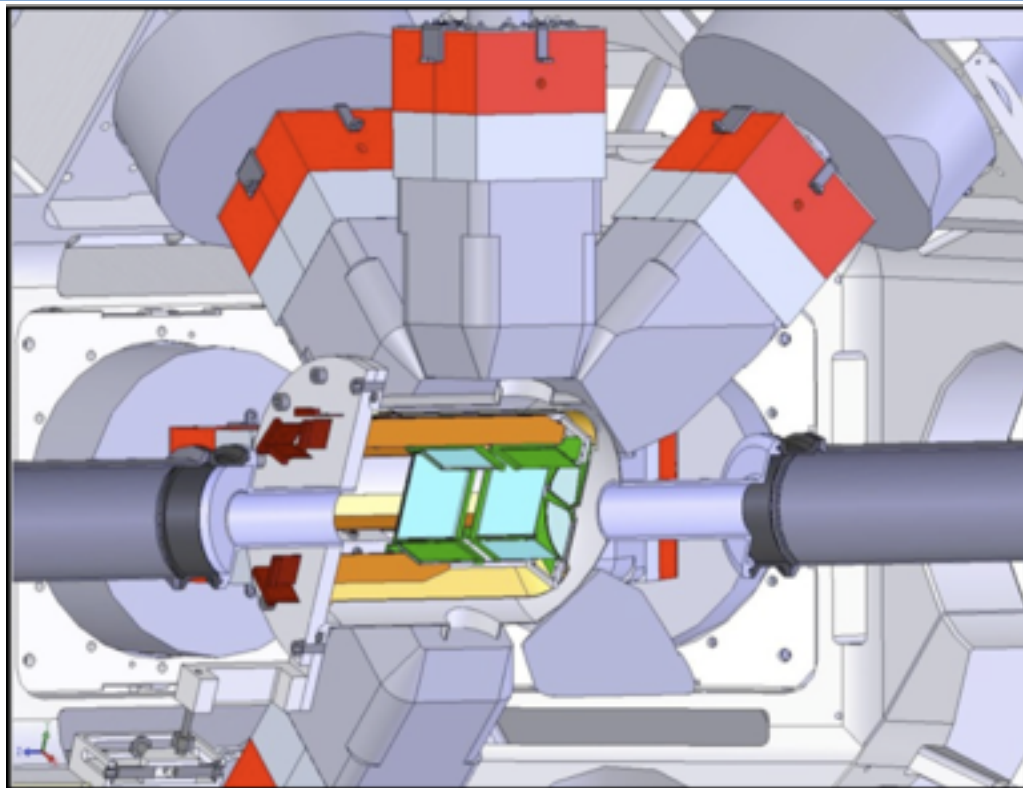


## SHARC

- Silicon detector array.
- Efficiency  $\approx 80\%$ .
- Coverage  $\approx 80\%$  of  $4\pi$ .
- Ang. res.  $\approx 1^\circ$ .

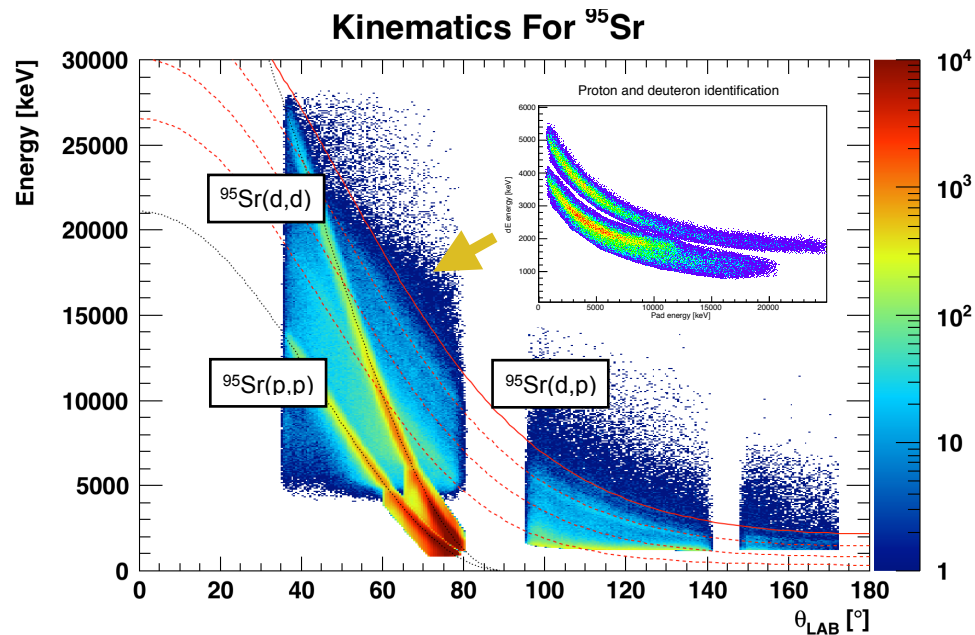
## TIGRESS

- 12 HPGe Clovers.
- Efficiency (1 MeV)  $\approx 10\%$ .
- Coverage  $\approx 2\pi$ .
- Energy res. (1 MeV)  $\approx 2$  keV.

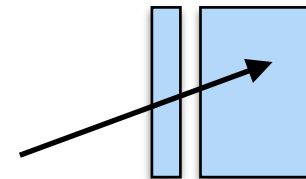


*TIGRESS and SHARC detectors were used to enable p- $\gamma$  coincidence measurements.*

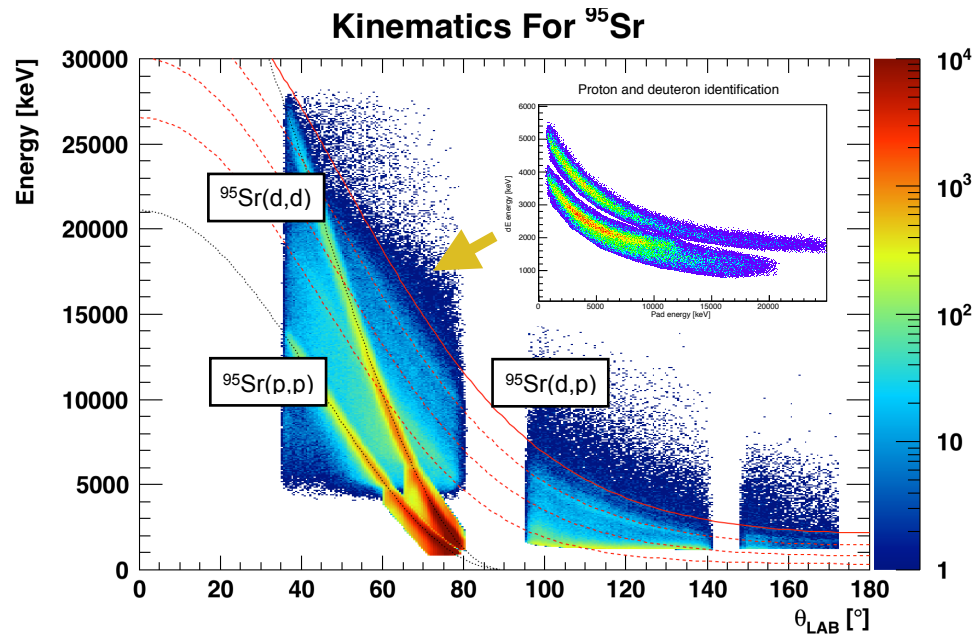
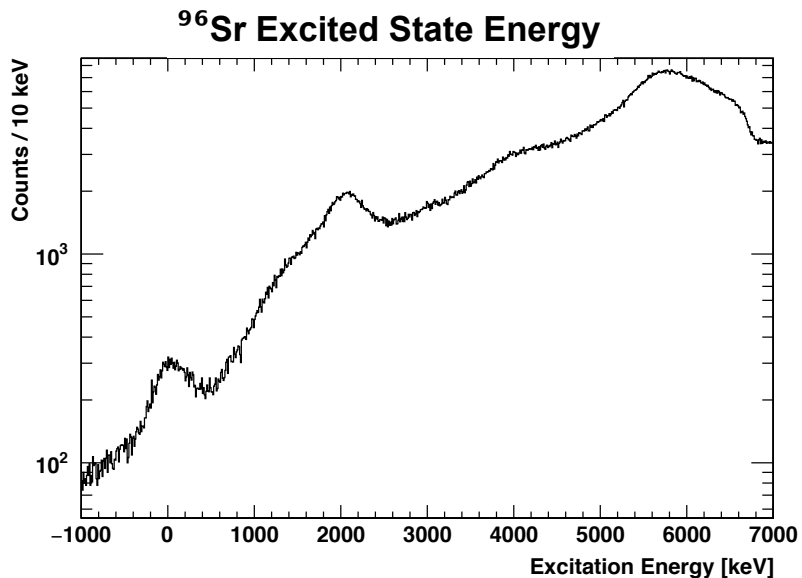
- Energy resolution of SHARC makes extracting  $^{96}\text{Sr}$  states difficult.
- Large amount of  $\beta$  decay background.



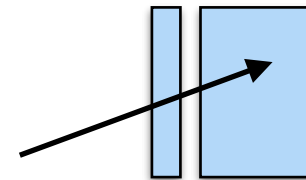
*Particle identification used through dE-E detector arrangement*



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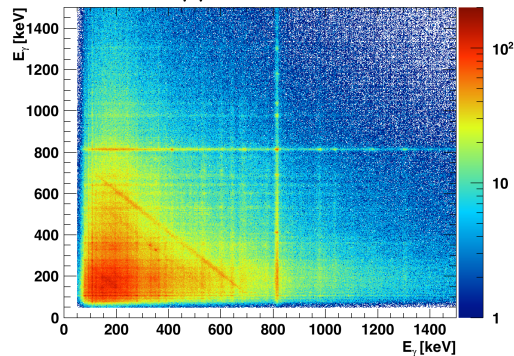
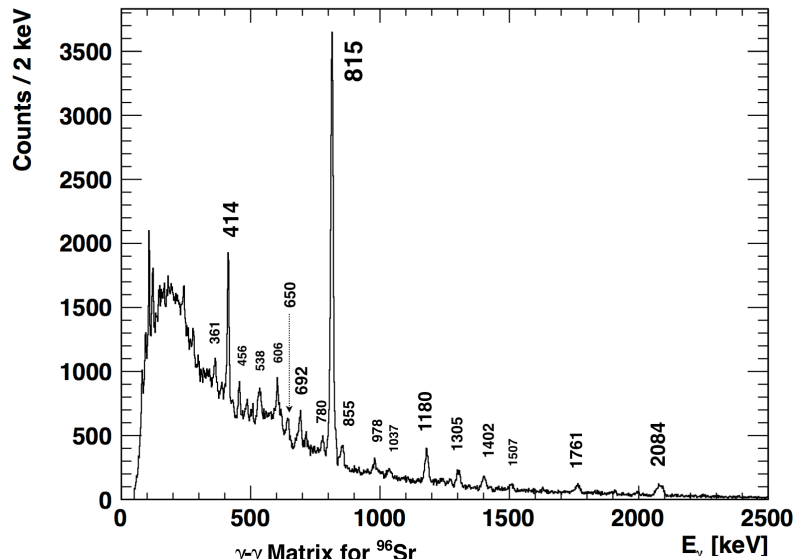


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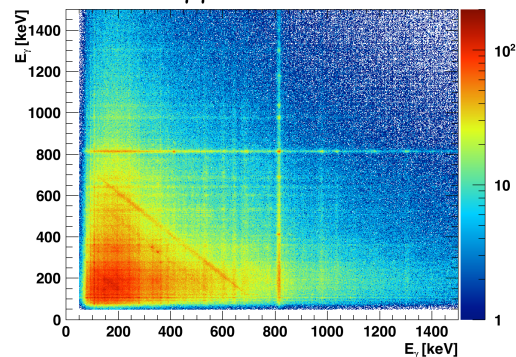
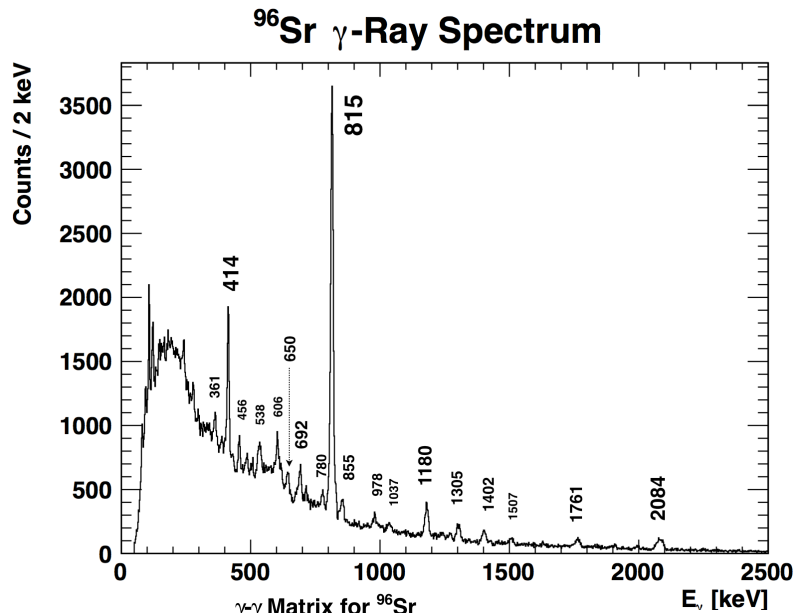
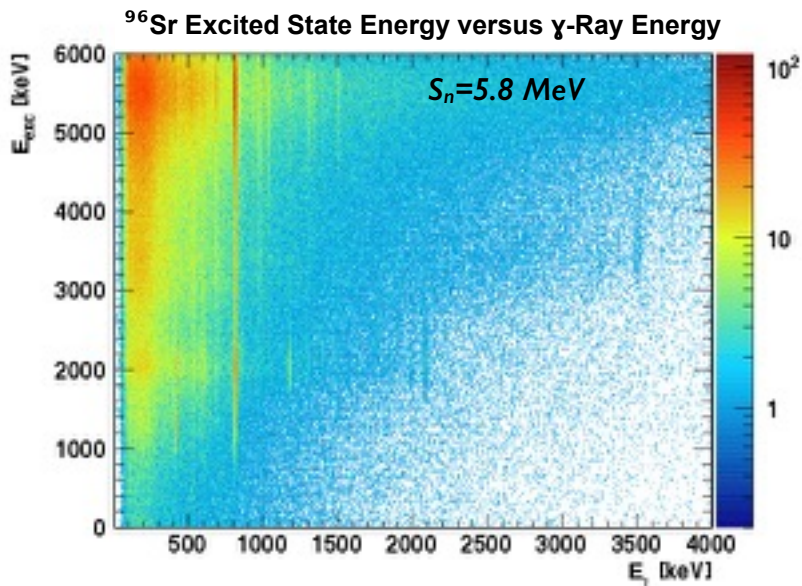


- Many  $^{96}\text{Sr}$  transitions observed, indicating that many levels are populated.
- We only want directly populated states.

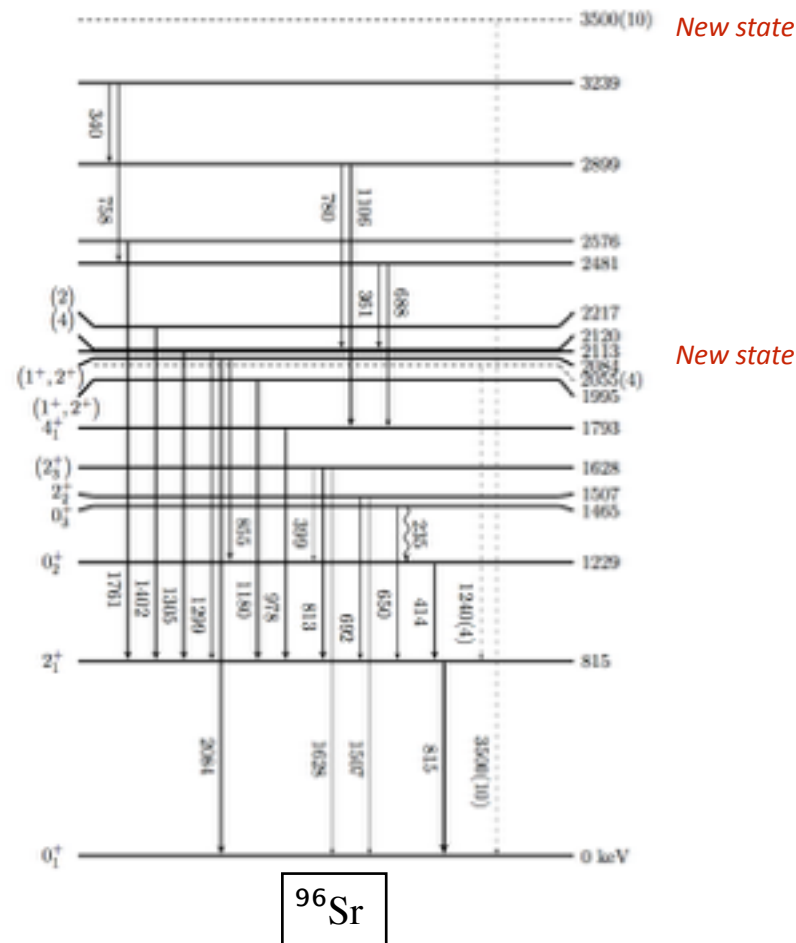
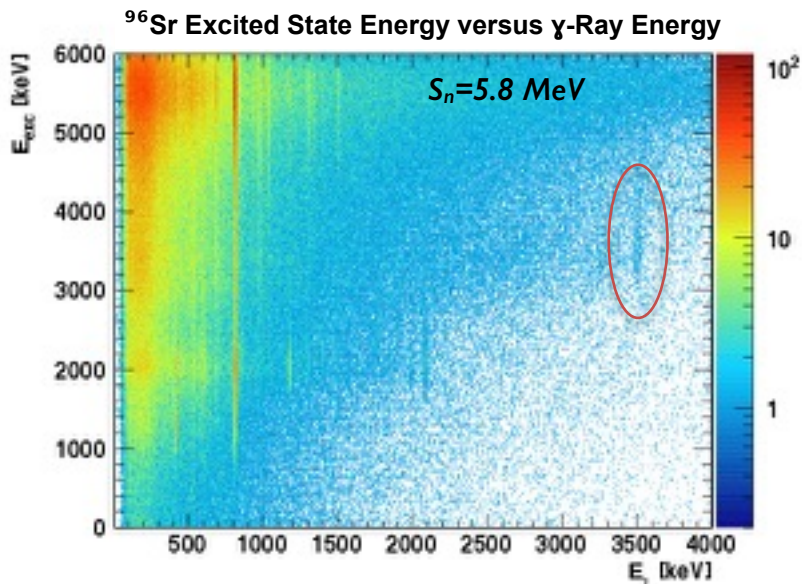
## $^{96}\text{Sr}$ $\gamma$ -Ray Spectrum



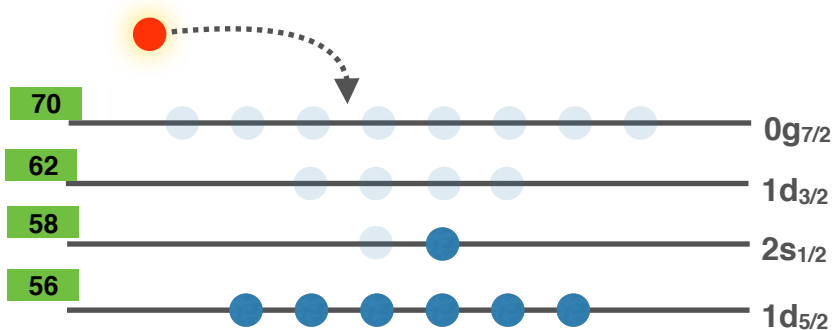
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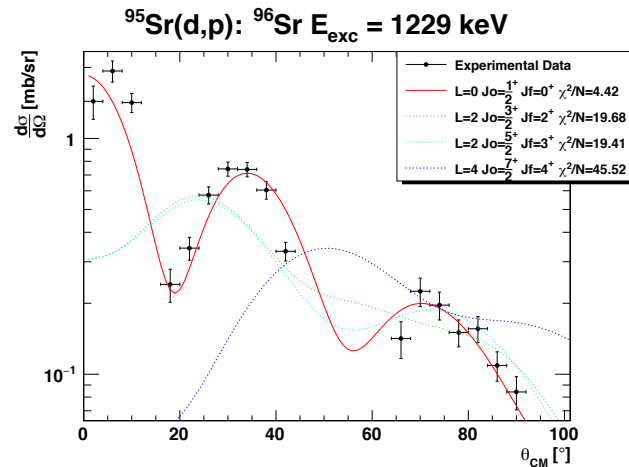
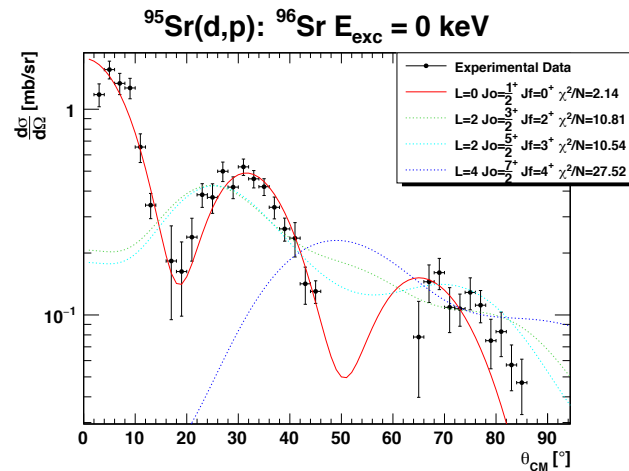
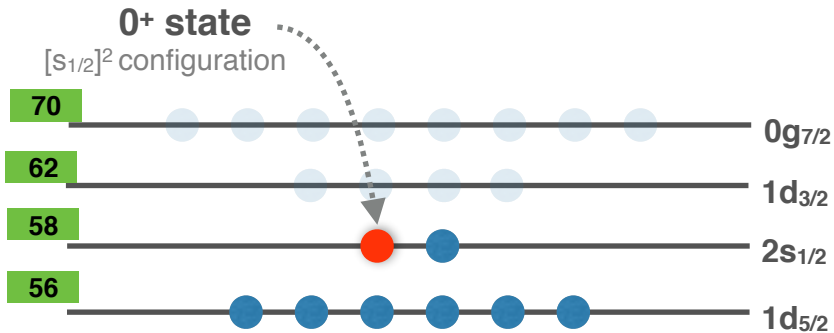


- Transferred neutron populates either  $2s_{1/2}$ ,  $1d_{3/2}$  or  $0g_{7/2}$  orbital.
- Three different orbital angular momentum transfers;  $\ell = 0, 2$  or  $4$ .
- Each scenario has a characteristic angular distribution.
- Fit data to DWBA calculations to determine  $\ell$  and  $\mathcal{S}$ .





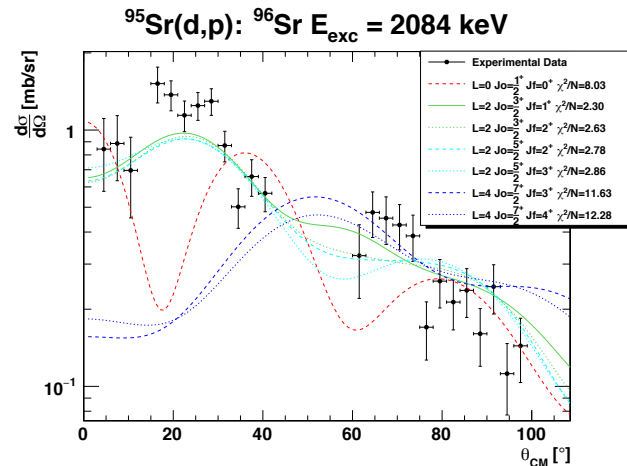
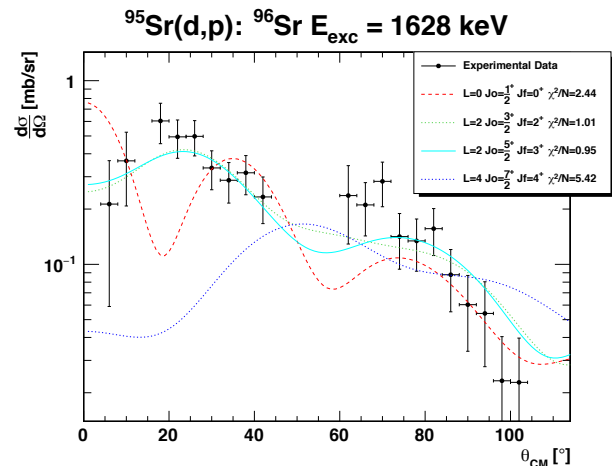
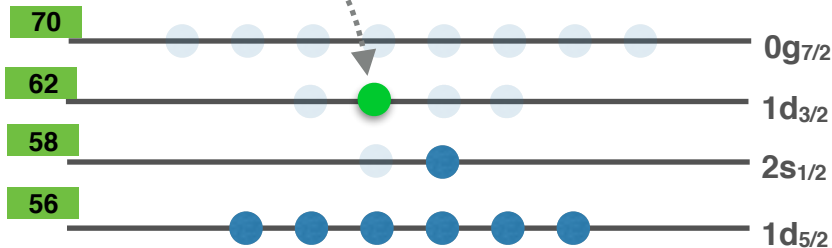
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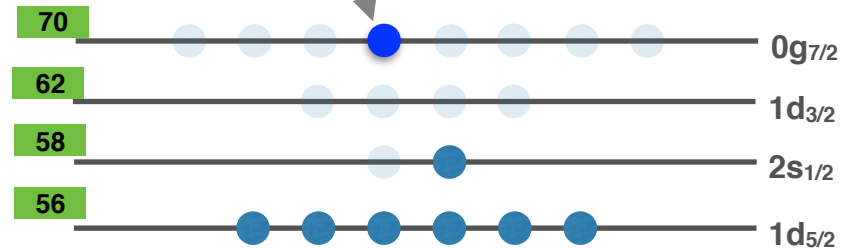
**1<sup>+</sup> or 2<sup>+</sup> state**  
 $[s_{1/2}][d_{3/2}]$  configuration



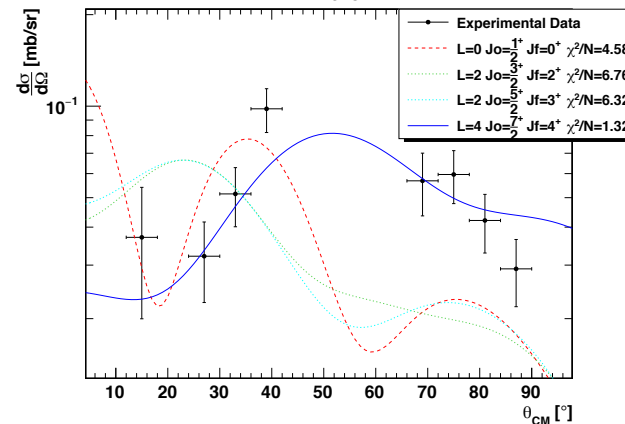
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**3+ or 4+ state**

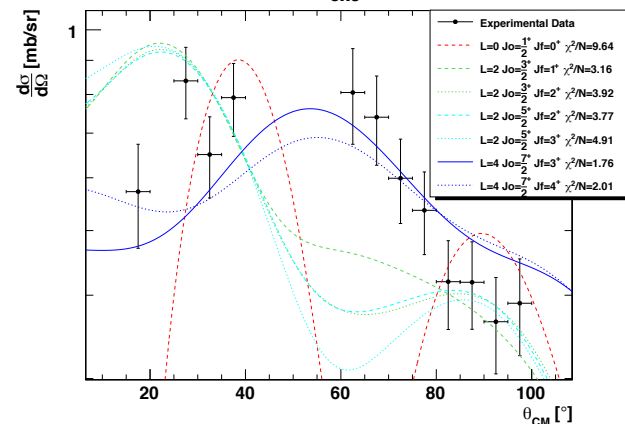
$[s_{1/2}][g_{7/2}]$  configuration



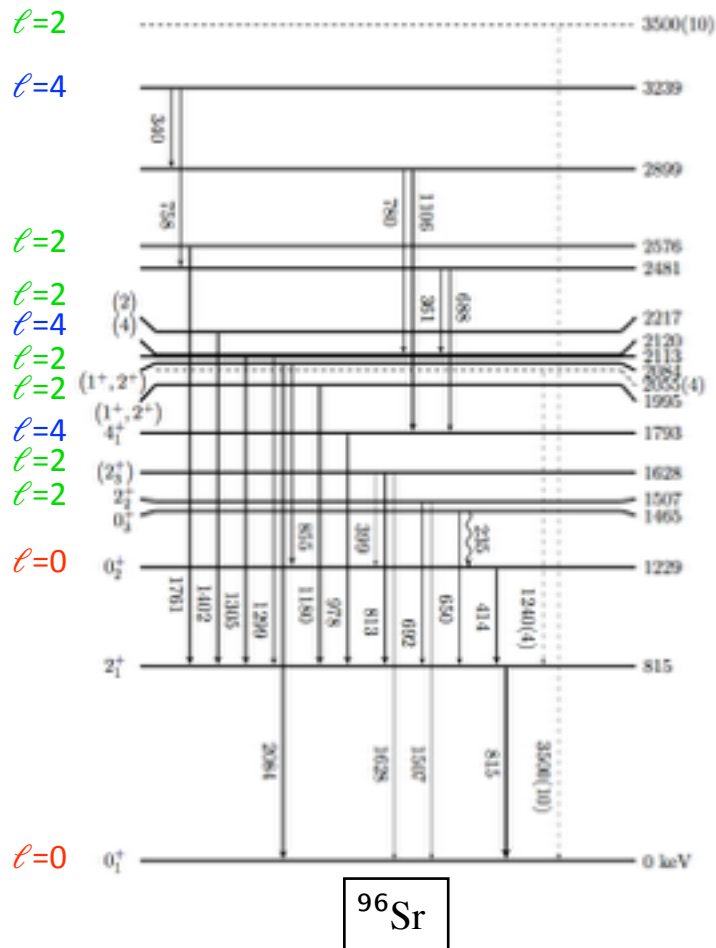
$^{95}\text{Sr}(d,p): ^{96}\text{Sr} E_{\text{exc}} = 1793 \text{ keV}$



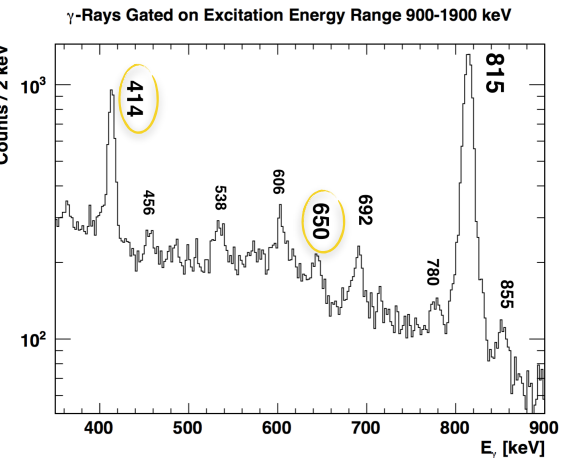
$^{95}\text{Sr}(d,p): ^{96}\text{Sr} E_{\text{exc}} = 3239 \text{ keV}$



- Angular distributions were extracted for 12  $^{96}\text{Sr}$  states.
- Shell model calculations are being carried out to compare spectroscopic factors.
- Insufficient statistics to measure angular distribution of 1465 keV  $^{96}\text{Sr}$  state.



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$\ell=2$

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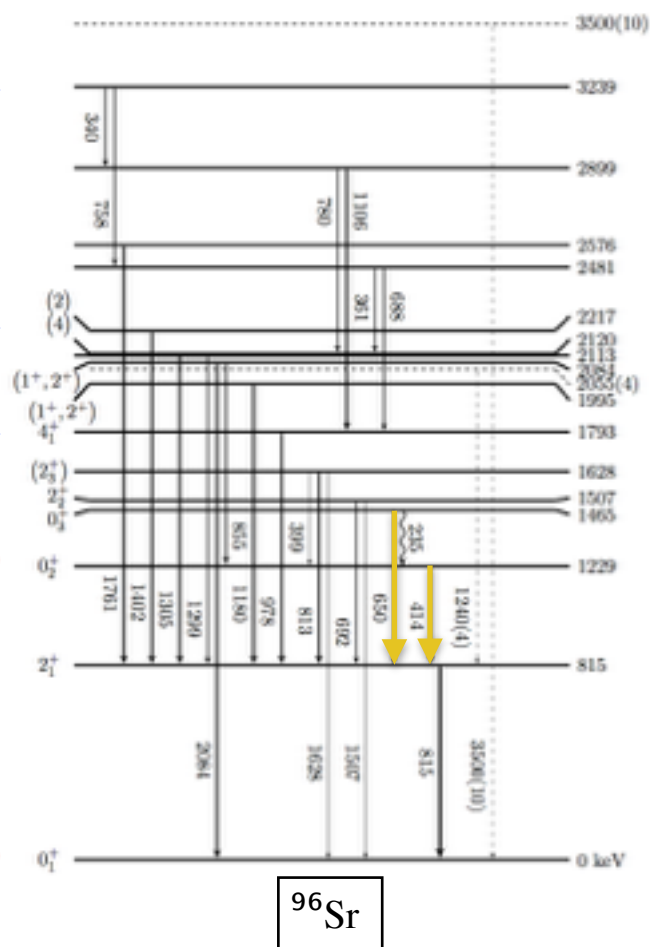
$\ell=4$

$\ell=2$

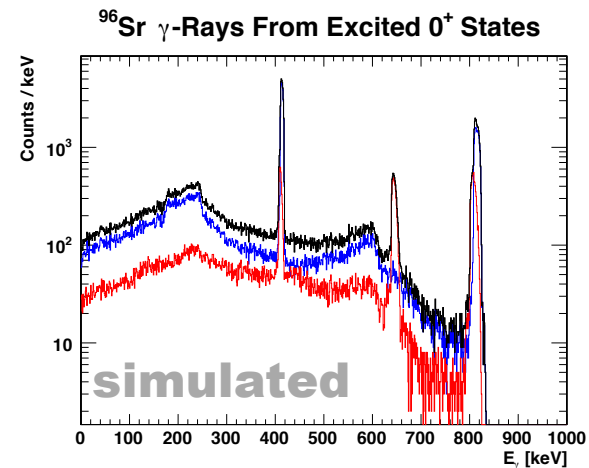
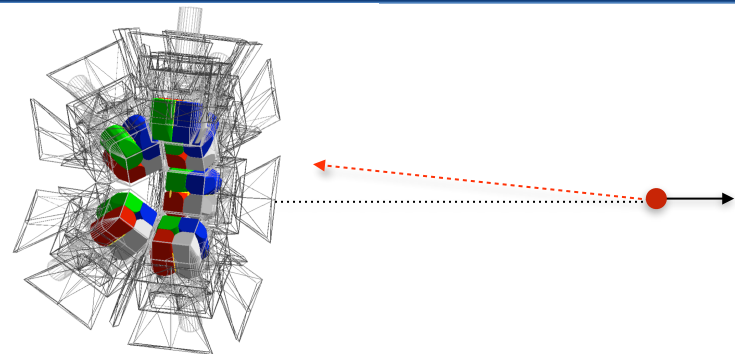
$\ell=2$

$\ell=0$

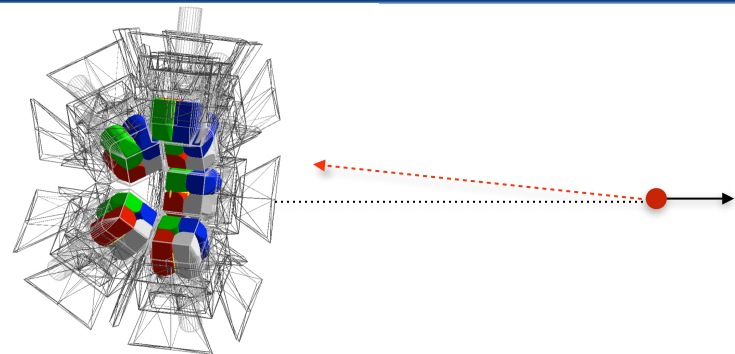
$\ell=0$



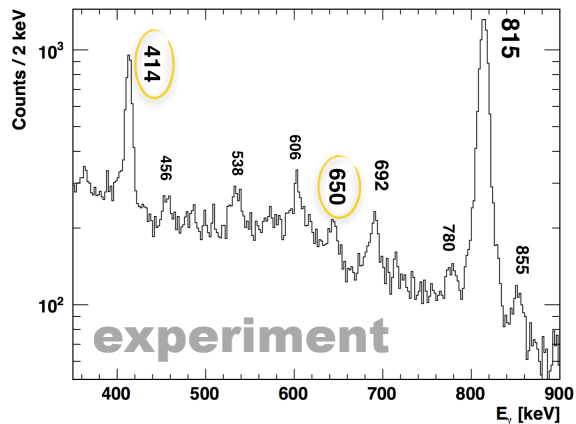
- Simulate decay of 1229 keV & 1465 keV states using realistic *Geant* model and compare counts.



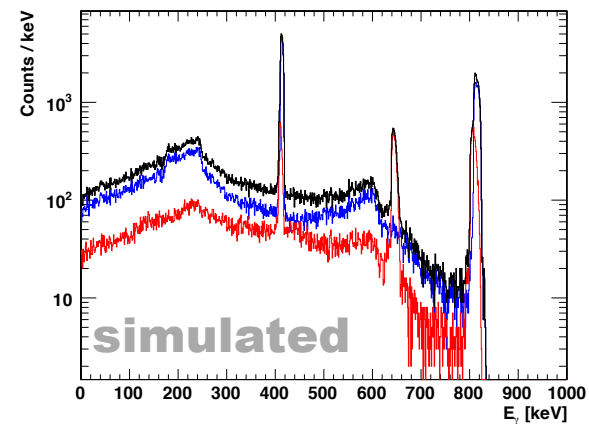
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- Mixing amplitude of  $0_3^+ : 0_2^+$  states,  $a^2 = 0.5(2)$ .



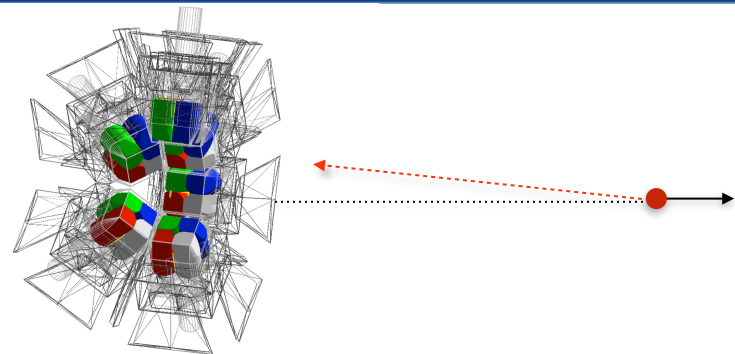
$\gamma$ -Rays Gated on Excitation Energy Range 900-1900 keV



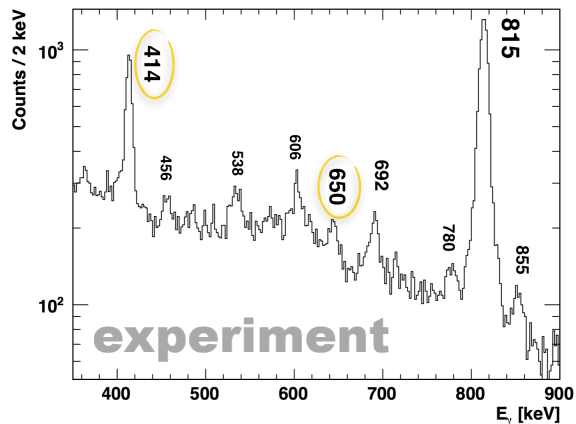
$^{96}\text{Sr}$   $\gamma$ -Rays From Excited  $0^+$  States



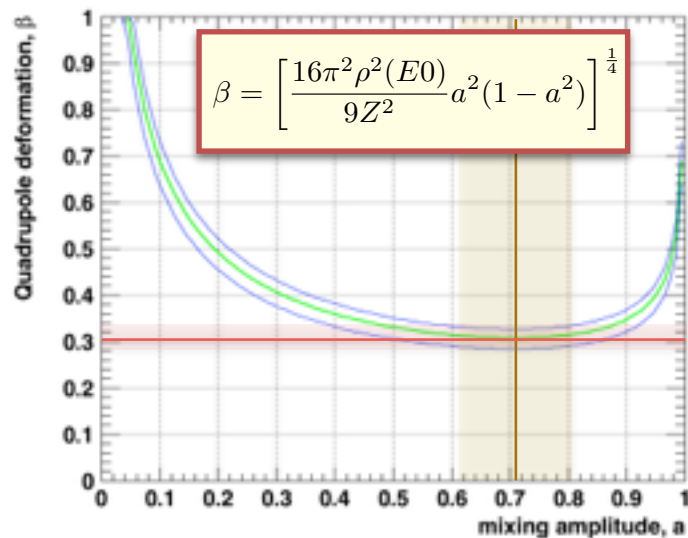
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- Constrains deformation:  $\beta = 0.30(5)$ .



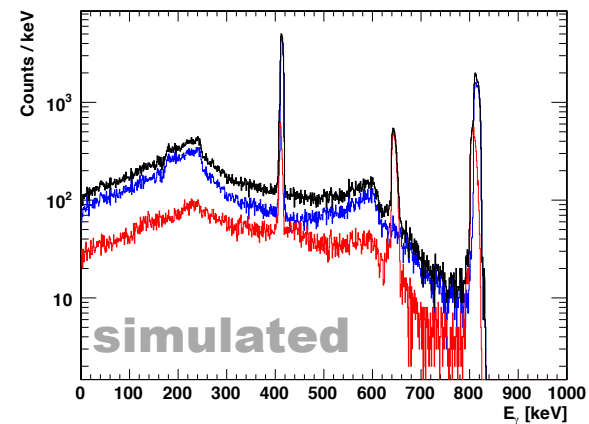
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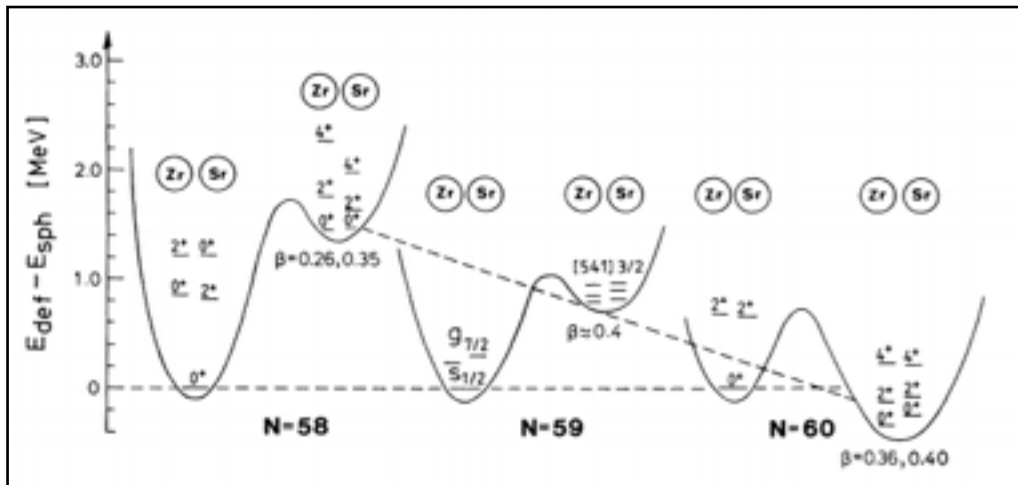
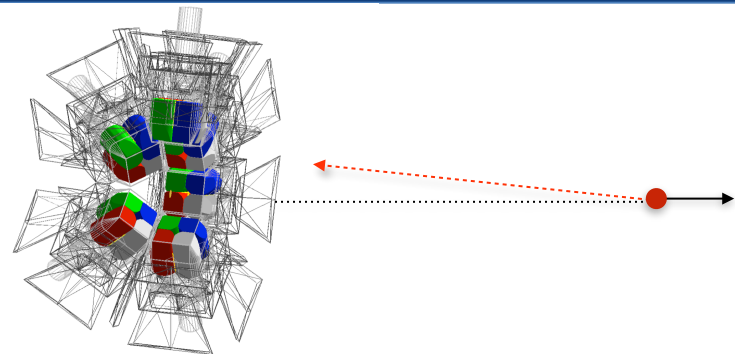
Relationship between  $\beta$  and  $a$  for  $\rho^2(E0) = 0.185(50)$



$^{96}\text{Sr}$   $\gamma$ -Rays From Excited  $0^+$  States



- Simulate decay of 1229 keV & 1465 keV states using realistic *Geant* model and compare counts.
- Mixing amplitude of  $0_3^+ : 0_2^+$  states,  $\alpha^2 = 0.5(2)$ .
- Constrains deformation:  $\beta = 0.30(5)$ .





- $^{95}\text{Sr}(d,p)$  to investigate single particle structure of  $^{96}\text{Sr}$  states.
- First high mass ( $A>30$ ) experiments of this kind at TRIUMF.
- Measured 12 angular distributions, including a new state at  $\sim 3.5$  MeV.
- Extracted information about the state spins and underlying single particle configurations.
- Use  $\gamma$ -ray analysis to measure mixing between excited  $0^+$  states in  $^{96}\text{Sr}$ .

# Many thanks to S1389 Collaboration;

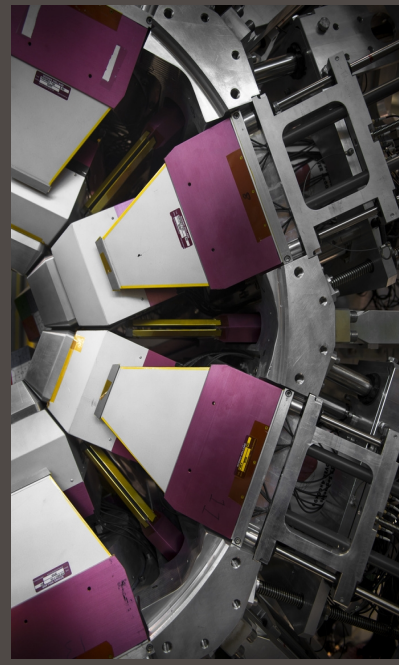
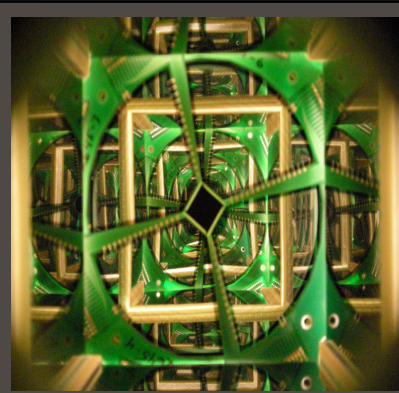
P. C. Bender<sup>2</sup>, R. Krücken<sup>1,2</sup>, K. Wimmer<sup>3</sup>, F. Ames<sup>2</sup>, C. Andreoiu<sup>4</sup>, C. S. Bancroft<sup>3</sup>,  
 R. Braid<sup>5</sup>, T. Bruhn<sup>2</sup>, W. Catford<sup>6</sup>, A. Cheeseman<sup>2</sup>, D. S. Cross<sup>4</sup>, C. Aa. Diget<sup>7</sup>, T. Drake<sup>8</sup>, A.  
 Garnsworthy<sup>2</sup>, G. Hackman<sup>2</sup>, R. Kanungo<sup>9</sup>, A. Knapton<sup>6</sup>, W. Korten<sup>2</sup>, K. Kuhn<sup>5</sup>, J. Lassen<sup>2</sup>, R.  
 Laxdal<sup>2</sup>, M. Marchetto<sup>2</sup>, A. Matta<sup>6</sup>, D. Miller<sup>2</sup>, M. Moukaddam<sup>2</sup>, N. Orr<sup>10</sup>, N. Sachmpazidi<sup>3</sup>, A.  
 Sanetullaev<sup>2</sup>, N. Tempstra<sup>3</sup>, C. Unsworth<sup>2</sup>, P. J. Voss<sup>4</sup>

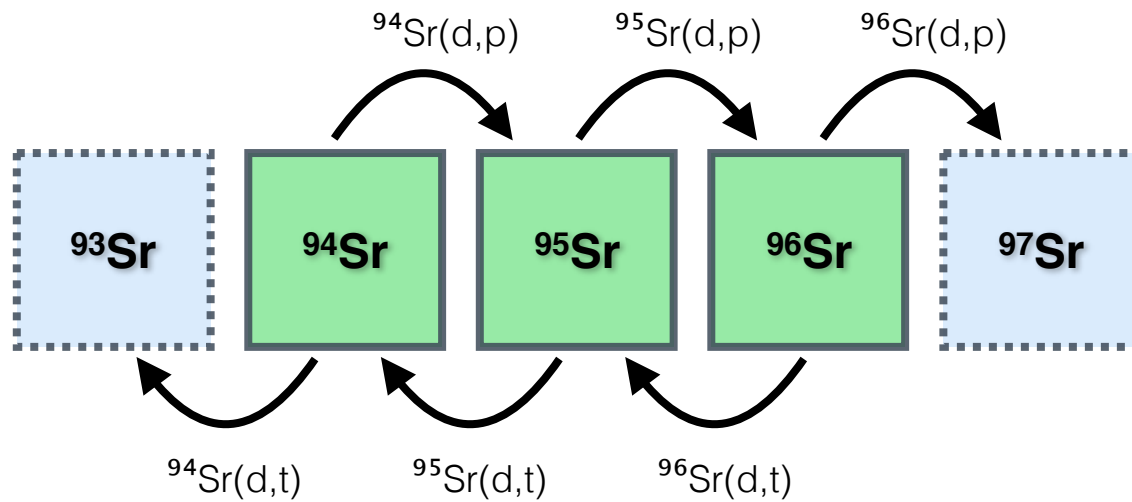
*1. University of British Columbia, 2. TRIUMF, 3. Central Michigan University, 4. Simon Fraser University, 5. Colorado School of  
 Mines, 6. University of Surrey, 7. University of York, 8. University of Toronto, 9. Saint Mary's University, 10. LPC Caen.*



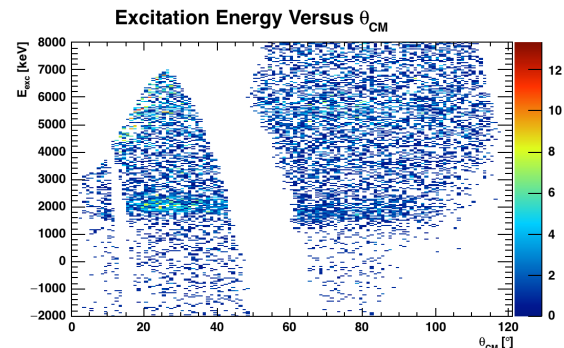
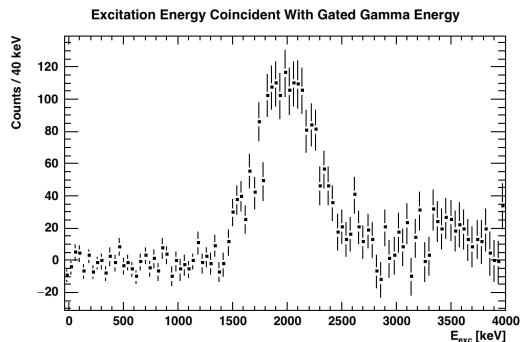
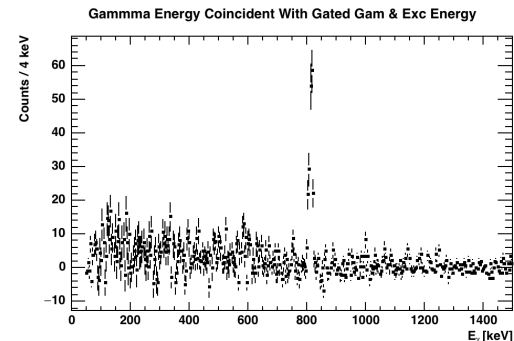
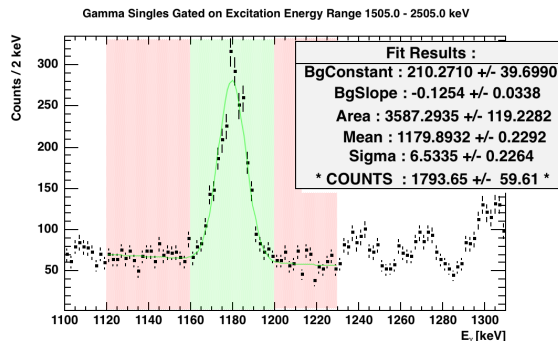
Thank you!  
Merci!

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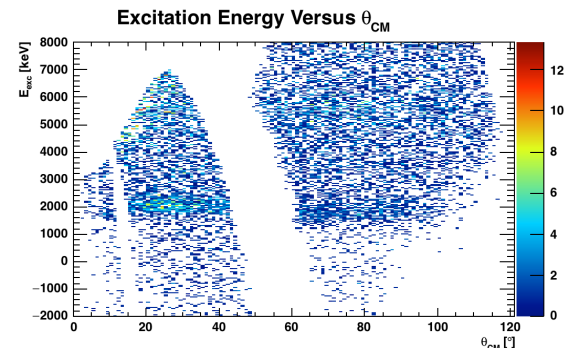
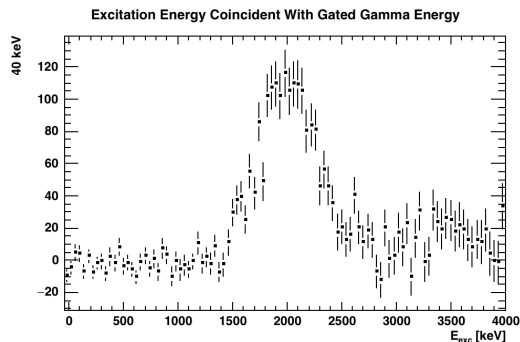
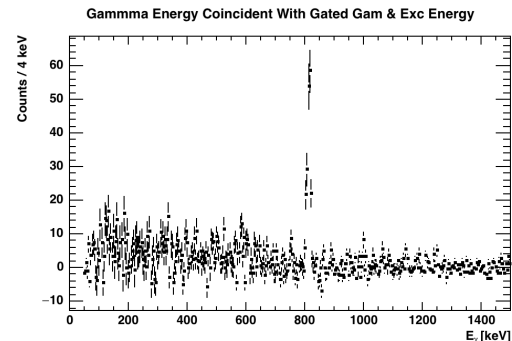
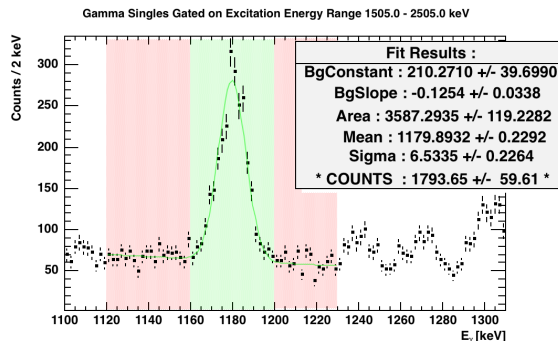
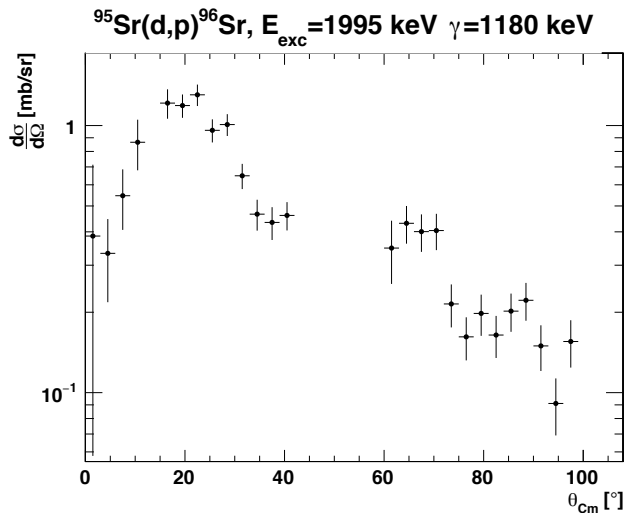




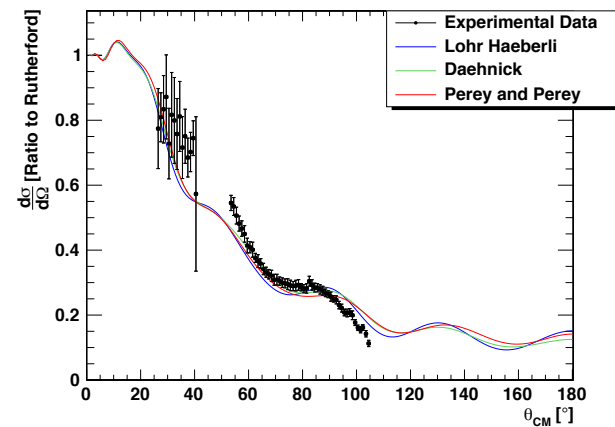
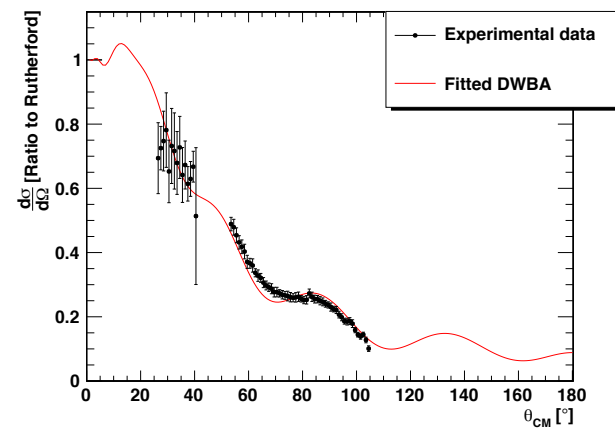
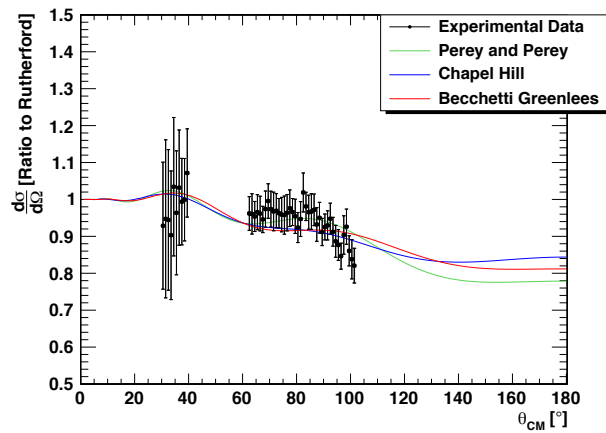
- Upper left: Identified 1180 keV  $\Upsilon$ -ray transition
- Upper right: Coincident  $\Upsilon$ -rays.
- Bottom left: Excitation energy coincident with 1180 keV  $\Upsilon$ -ray.
- Bottom right: Excitation energy versus  $\theta_{cm}$  coincident with 1180 keV  $\Upsilon$ -ray.



- Upper left: Identified 1180 keV  $\gamma$ -ray transition
- Upper right: Coincident  $\gamma$ -rays.
- Bottom left: Excitation energy coincident with 1180 keV  $\gamma$ -ray.
- Bottom right: Excitation energy versus  $\theta_{\text{cm}}$  coincident with 1180 keV  $\gamma$ -ray.



*Angular distribution for 1995 keV  $^{96}\text{Sr}$  state.*

$^{95}\text{Sr}(d,d) @ 5.378 \text{ MeV/u}$ 

 $^{95}\text{Sr}(p,p) @ 5.378 \text{ MeV/u}$ 




Comparison of (d,p) Calculations Between Global and Fitted OM

