



# Ab initio structure input for scattering observables

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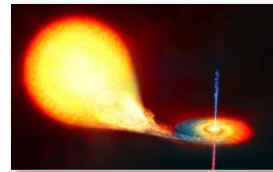
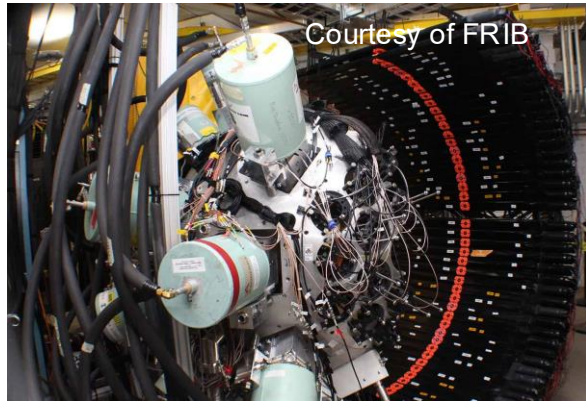
**MICHIGAN STATE**  
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Office of  
Science

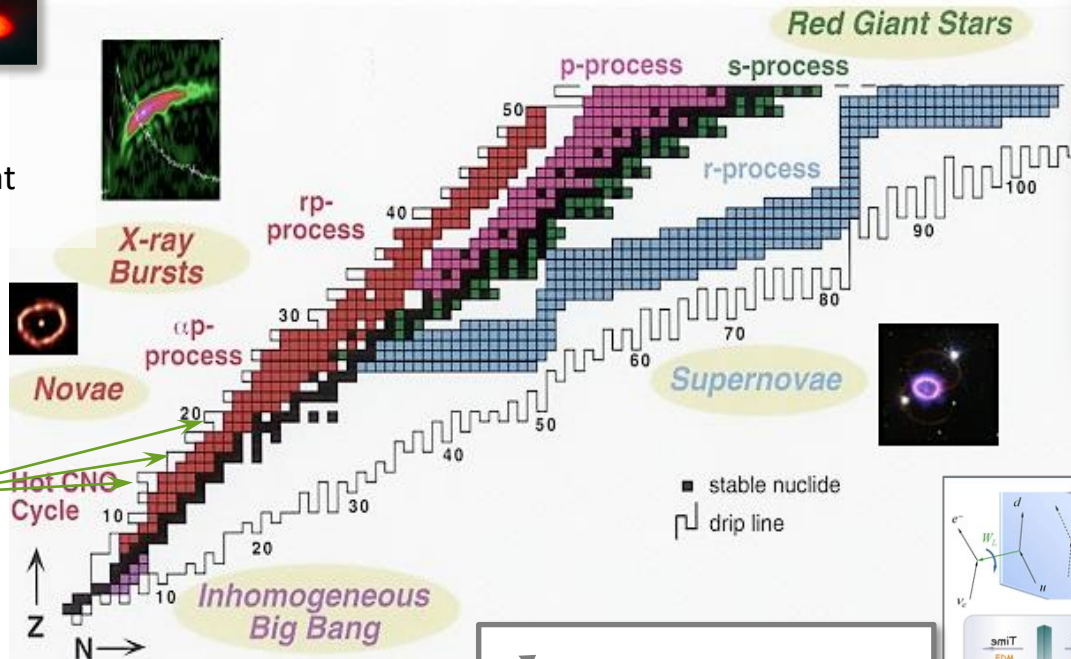
# The era of rare isotope beams



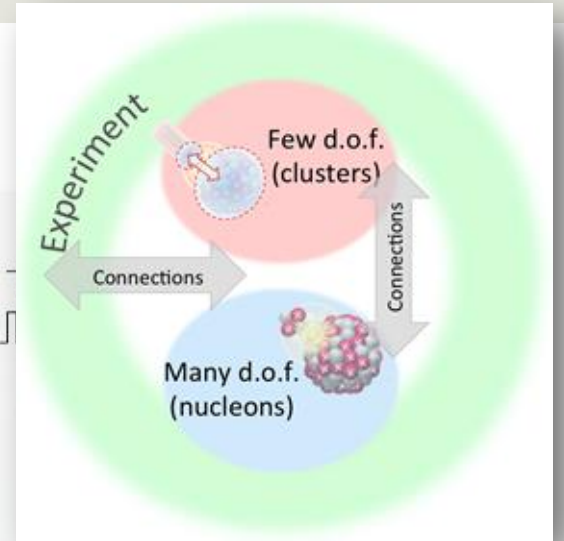
X-ray burst nucleosynthesis

Alpha widths

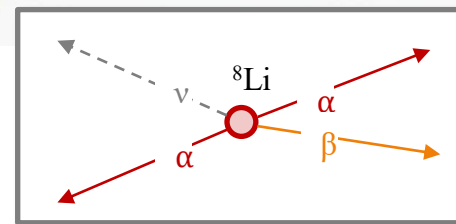
Reaction rates at low energies



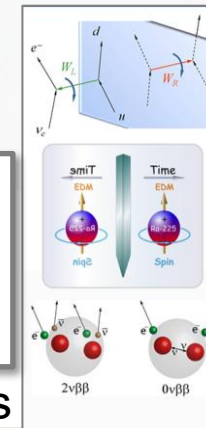
Close proximity of the drip lines



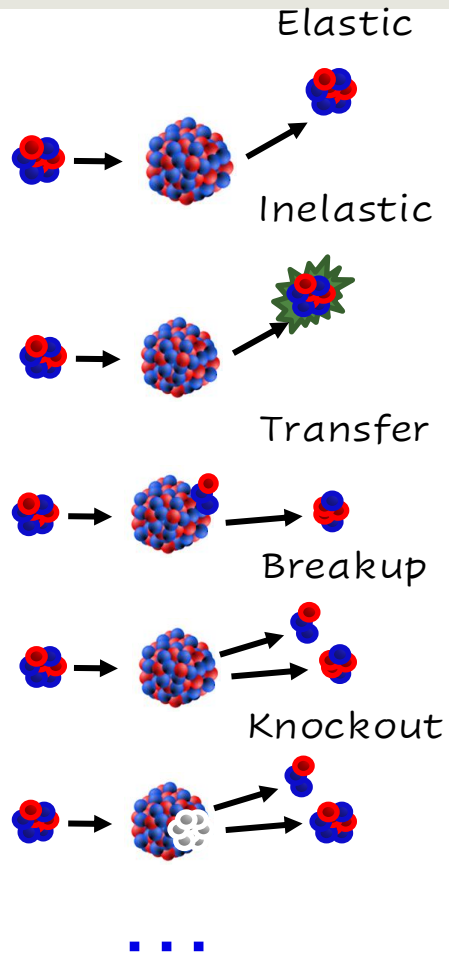
FRIB Theory Alliance topical program (2018)  
“From bound states to the continuum”  
(C. Johnson et al.)



Fundamental symmetries



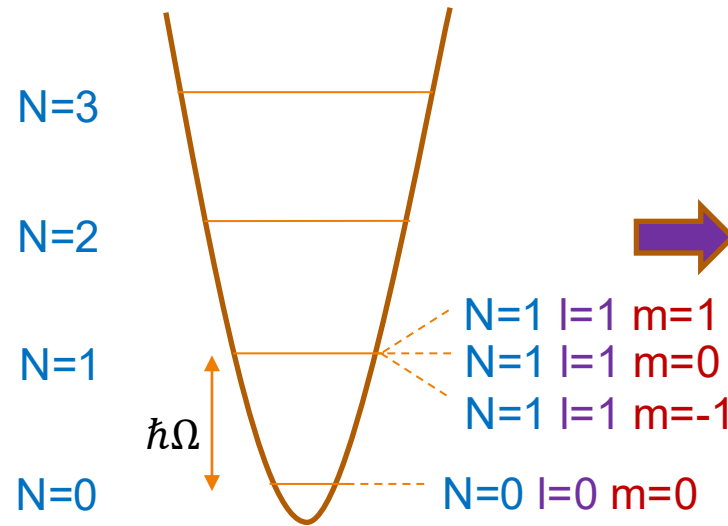
# Reaction models need structure input



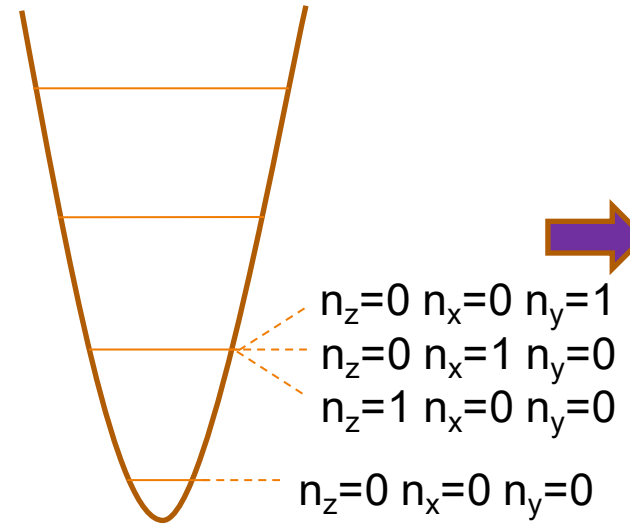
- Experiments need reaction models to interpret measured data
- Various reaction models require structure input (cluster wavefunctions, excitation spectrum, electromagnetic transitions, etc.)
- *Ab initio* structure methods can provide a reliable input especially for the tricky problems



# Symmetry-adapted No-core Shell Model

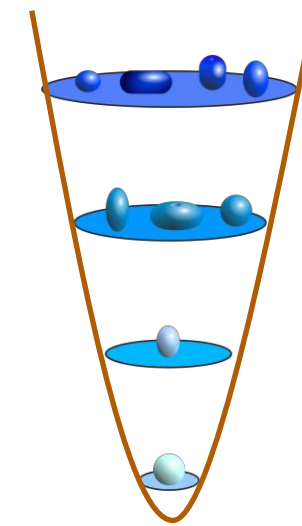


Spherical harmonic oscillator (HO): basis states given by  $\{N \ l \ m\}$

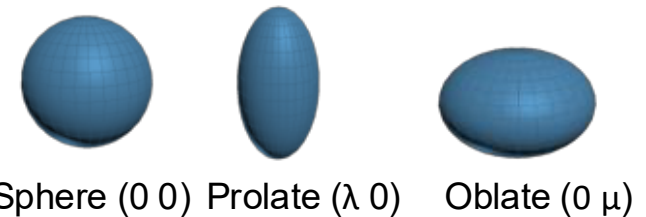


$N = n_z + n_x + n_y$   
 Basis states given by  $\{n_x \ n_y \ n_z\}$

$$a_{Nlm}^+ \equiv a_{(N \ 0)lm}^+$$



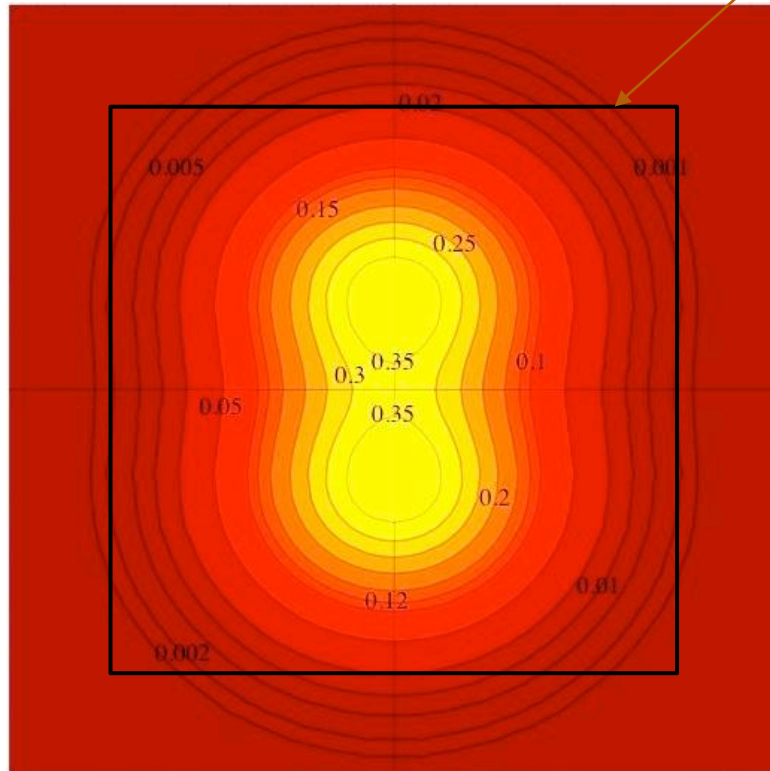
$\lambda = n_z - n_x, \quad \mu = n_x - n_y$  (single particle)  
 Basis states given by  $(\lambda \ \mu)$  quantum numbers



Sphere (0 0) Prolate ( $\lambda \ 0$ ) Oblate ( $0 \ \mu$ )

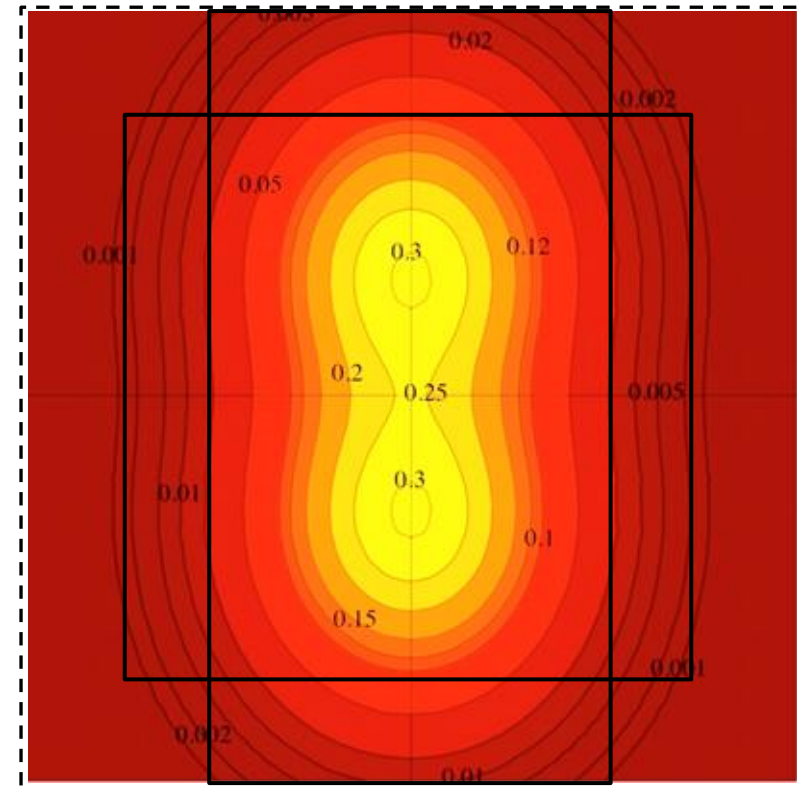
# Symmetry-adapted basis helps reduce the models space size

Conventional Shell Model



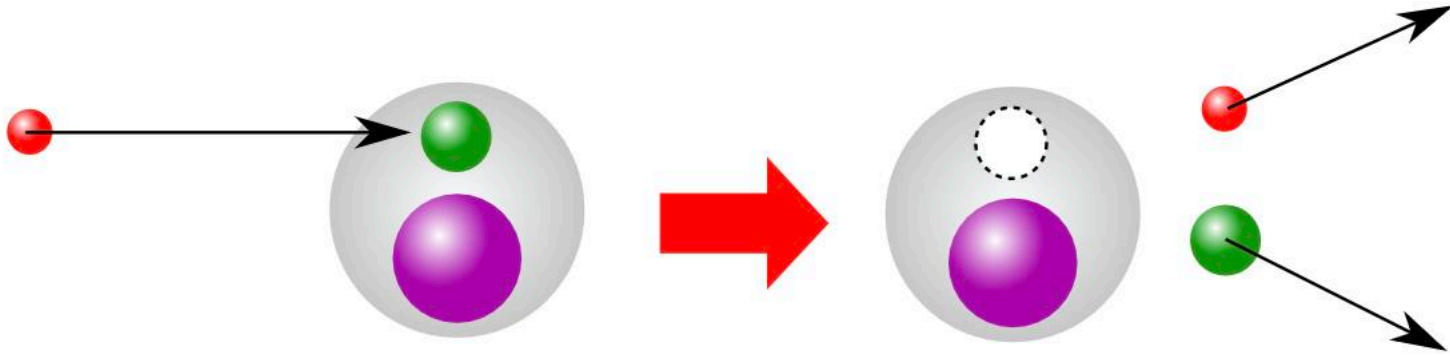
Nucleus in model space

*Ab initio* Symmetry-adapted No-core Shell Model (SA-NCSM)



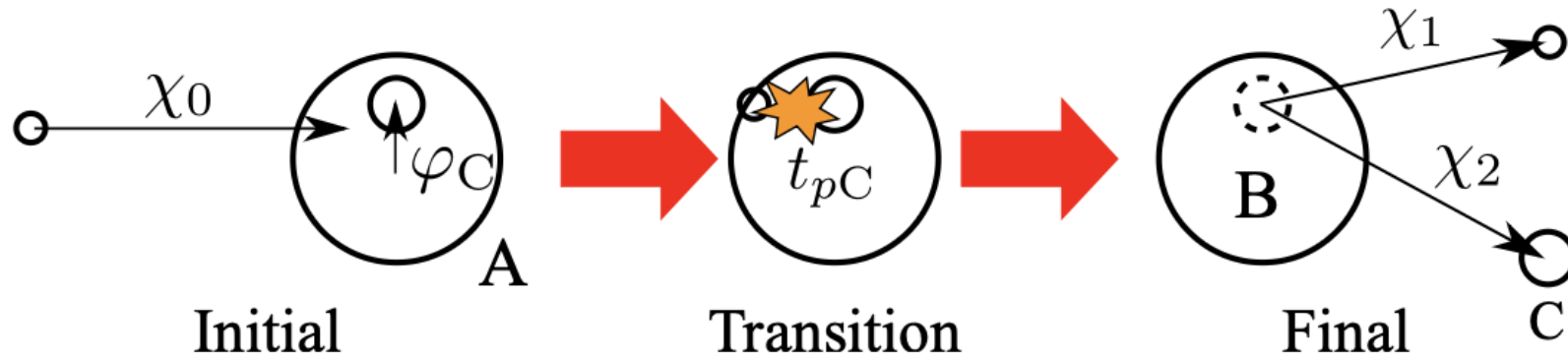
**SU(3) and symplectic symmetry**

# Knockout reaction



- Typically  $>100$  MeV/u incident energy
- Modeled as one-step direct reaction
- Probes mainly the ground state particle clustering in the target

# Reaction model: Distorted Wave Impulse Approximation



Transition matrix

$$T = \langle \chi_1 \chi_2 \Phi_C \Phi_B | t_{pC} | \chi_0 \Phi_A \rangle = \langle \chi_1 \chi_2 | t_{pC} | \chi_0 \varphi_C \rangle$$

$\chi_i$ : Distorted waves under optical potentials

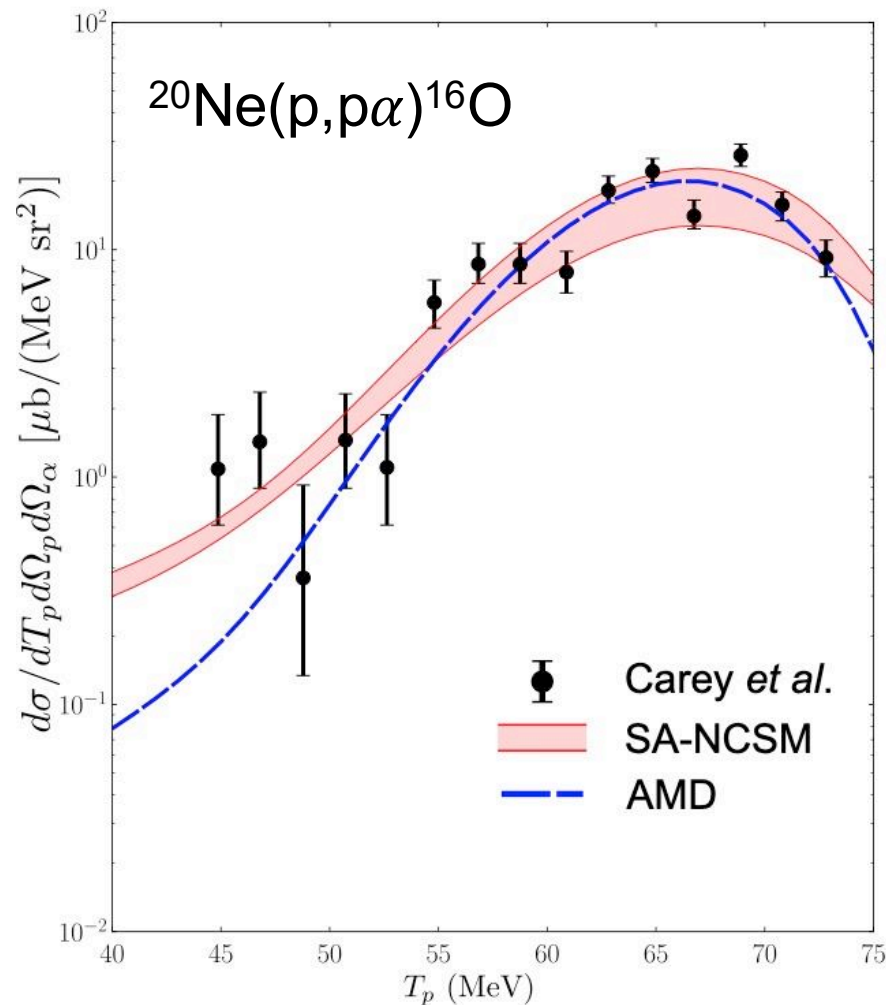
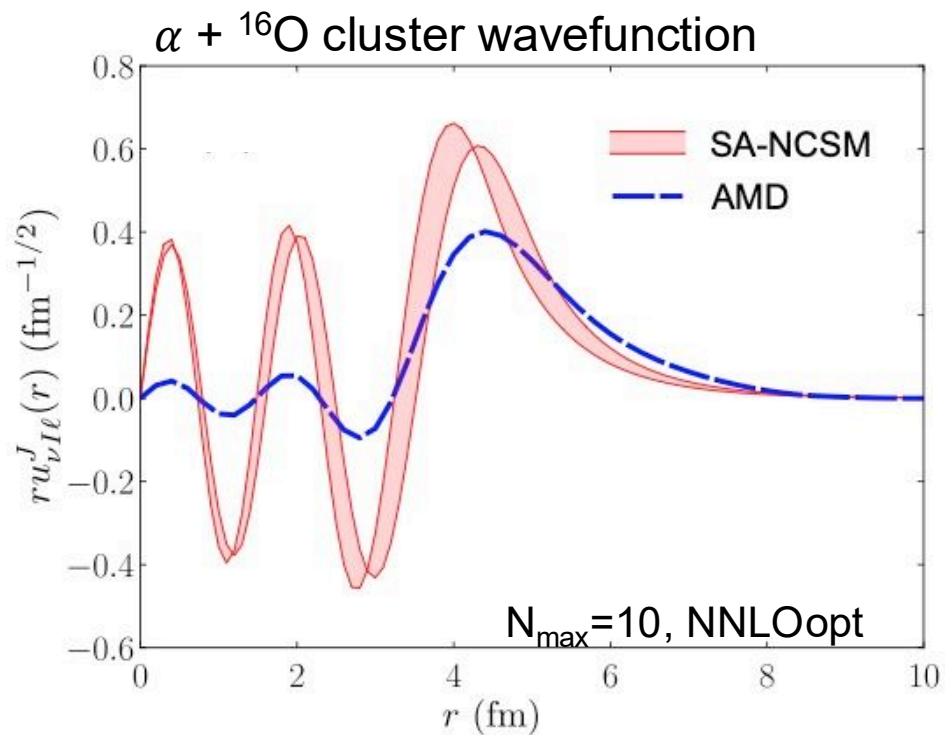
$t_{pC}$ :  $p$ -C effective interaction in free space

$\varphi_C$ : Cluster wave function  $\langle [\Phi_C \otimes \Phi_B] | \Phi_A \rangle$

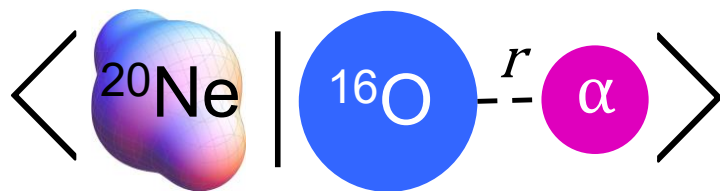
Knockout cross section (Triple differential cross section)

$$\frac{d^3\sigma}{dE_1 d\Omega_1 d\Omega_2} \propto |T|^2$$

# Ab initio informed knockout elucidates $\alpha$ clustering in $^{20}\text{Ne}$

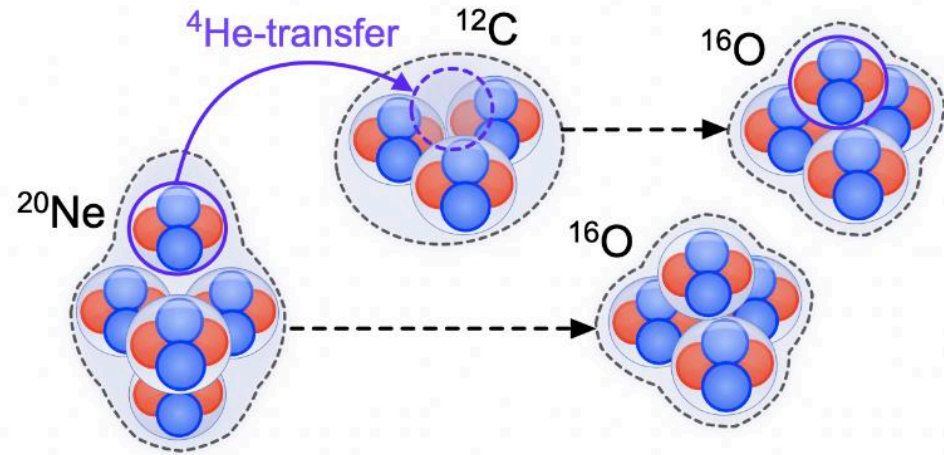


In collaboration with K. Yoshida (Osaka U.) and K. Ogata (Kyushu U.)



# Quantifying $\alpha$ clustering in the ground states of $^{16}\text{O}$ and $^{20}\text{Ne}$

$^{12}\text{C}(^{20}\text{Ne}, ^{16}\text{O})^{16}\text{O}$   $\alpha$ -transfer reaction



Experiment done  
at Texas A&M  
Cyclotron Institute

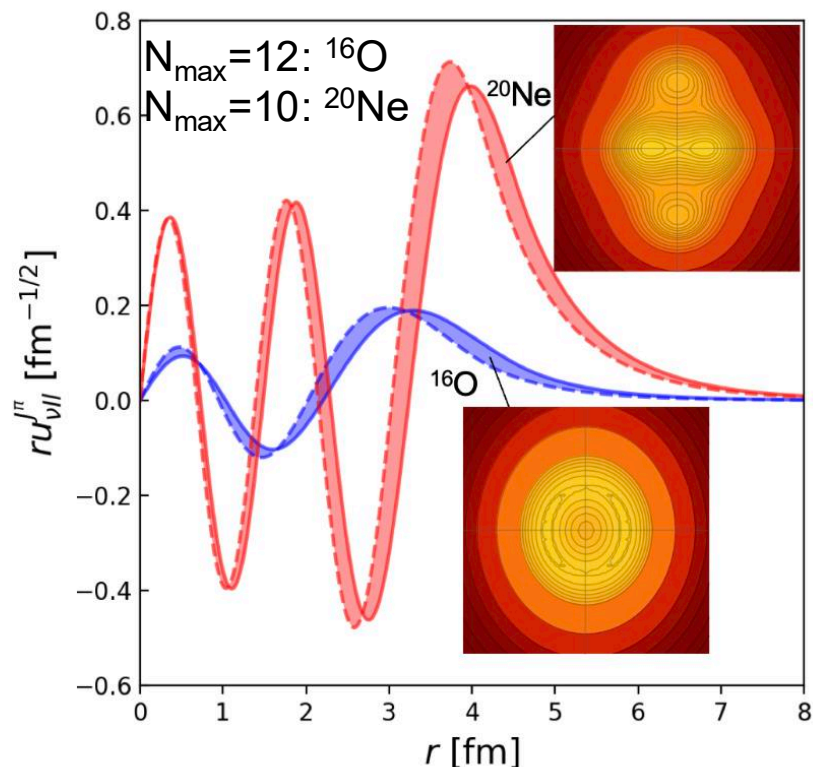


In collaboration with E. Harris  
and G. Rogachev (TAMU)

➤ Reaction model: distorted wave Born approximation (DWBA)

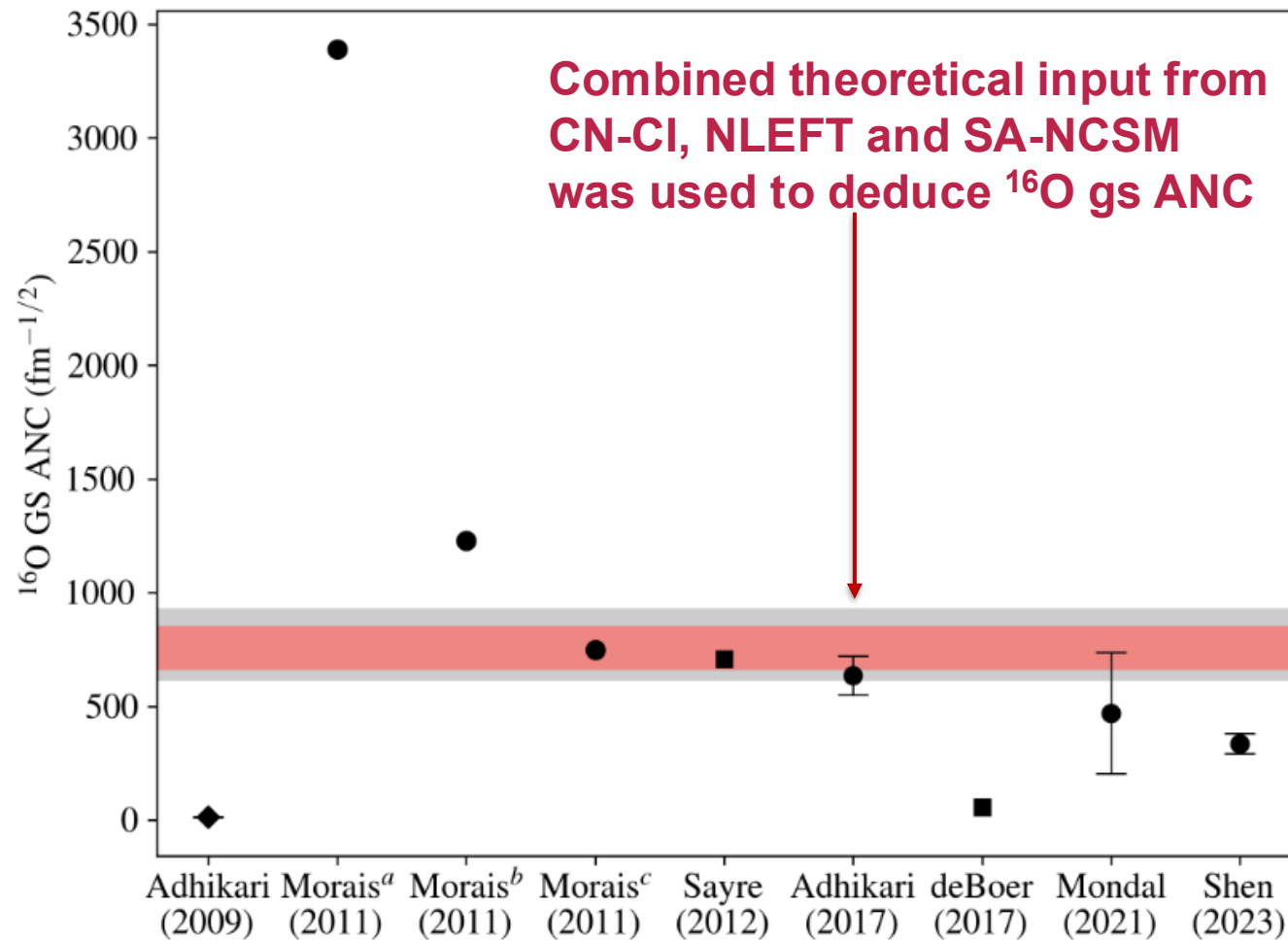
➤ Extracted product of ANCs  $C_{^{16}\text{O}}C_{^{20}\text{Ne}} \propto \left( \frac{d\sigma}{d\Omega} \right)_{transfer} / \left( \frac{d\sigma}{d\Omega} \right)_{elastic}$

# $\alpha$ asymptotic normalization coefficient for $^{16}\text{O}$



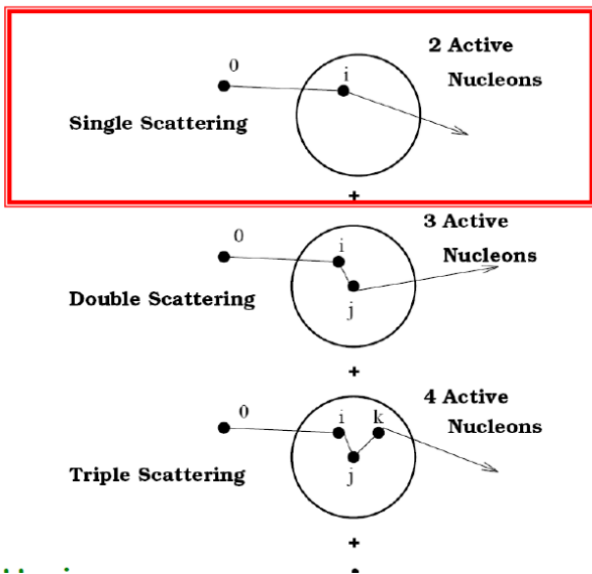
$\alpha + ^{12}\text{C}$  and  $\alpha + ^{16}\text{O}$  cluster wavefunctions from SA-NCSM using  $\text{NNLO}_{\text{opt}}$

$$C_{160} = (C_{160}C_{20\text{Ne}})_{\text{expt}} / (C_{20\text{Ne}})_{\text{theory}}$$



# Ab initio optical potentials for $E > 65$ MeV

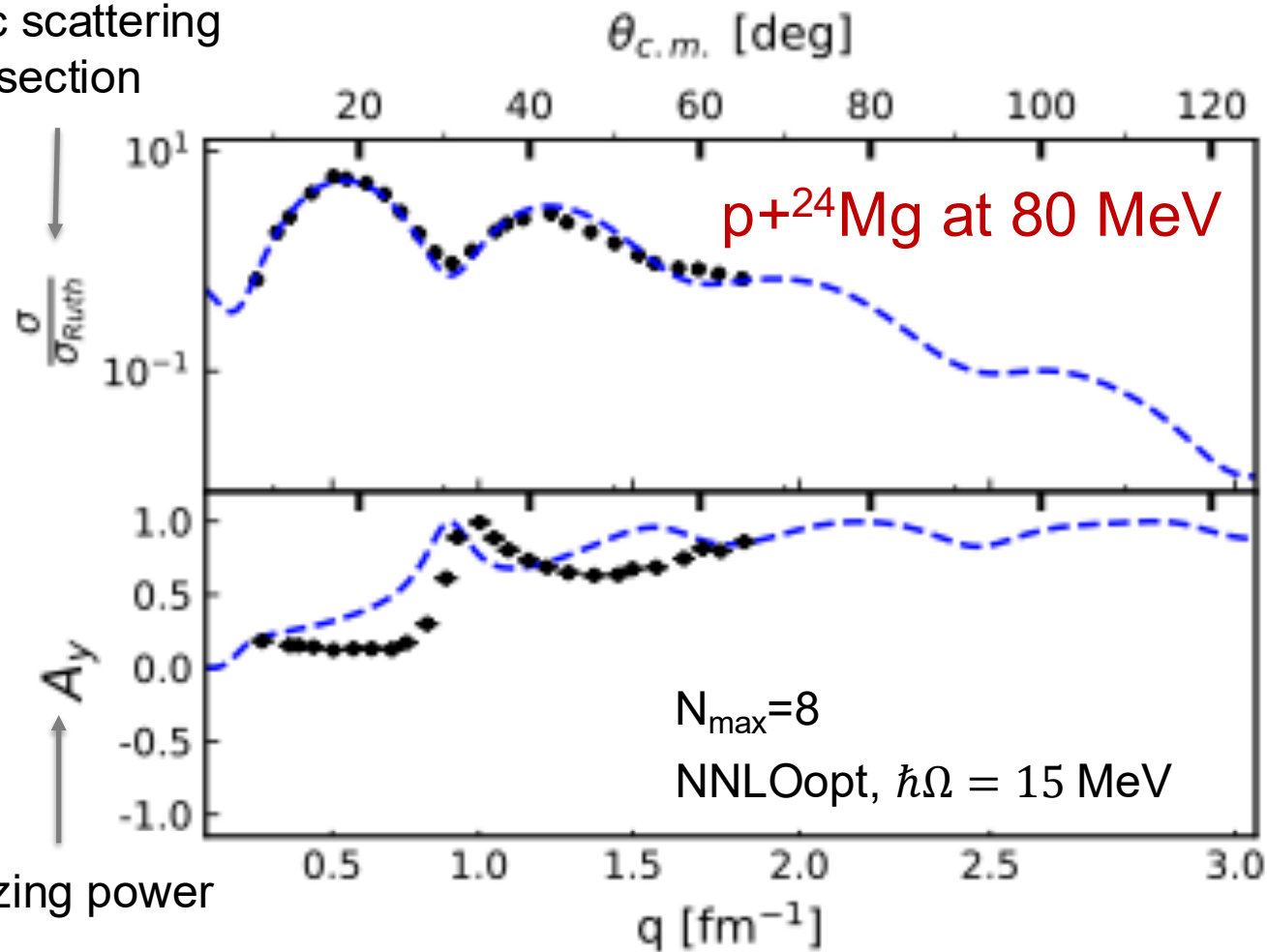
Multiple scattering expansion



In collaboration with C. Elster (OU)

See next talk!

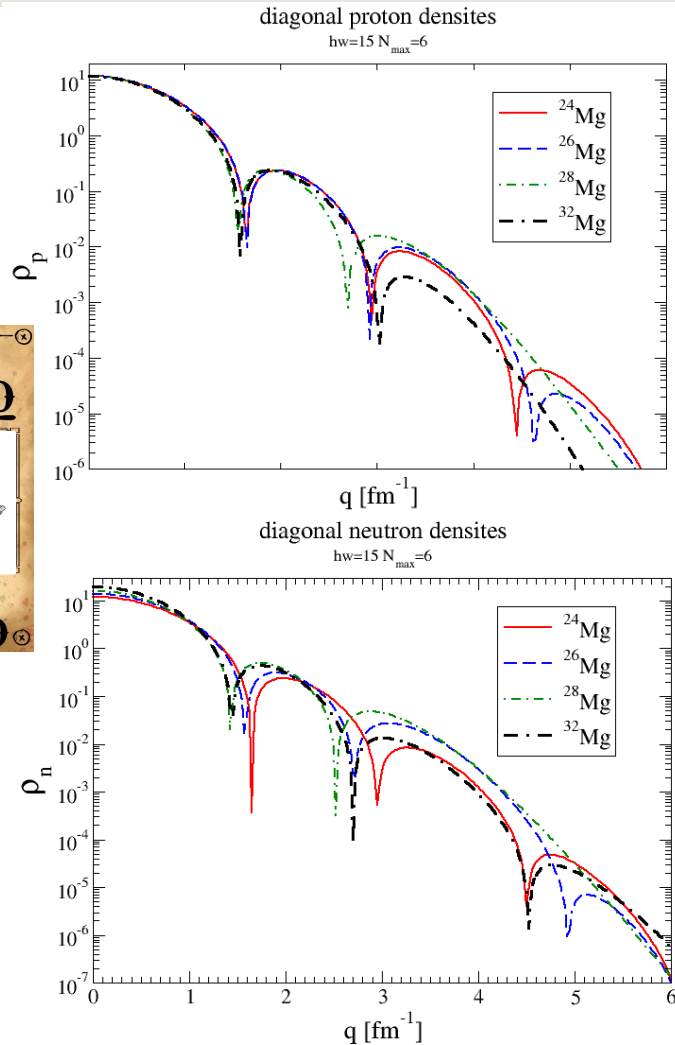
Elastic scattering cross section



Analyzing power

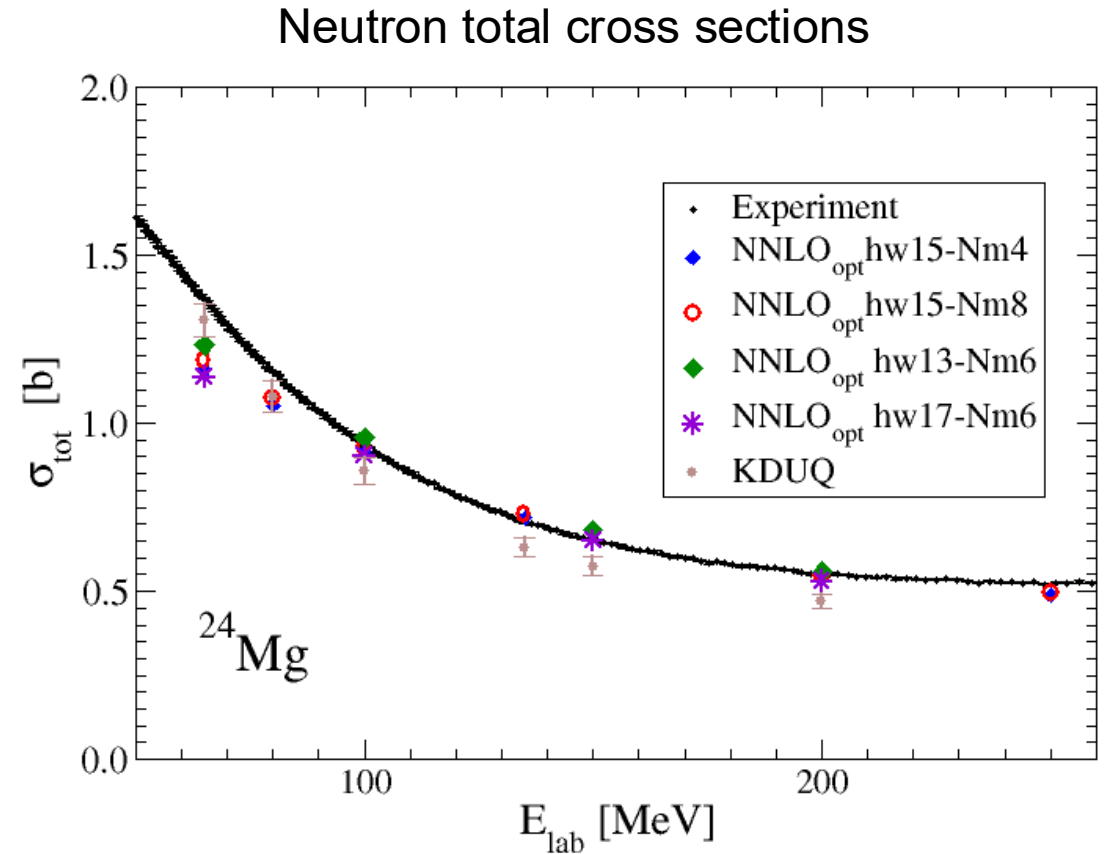
Structure input from SA-NCSM

# One-body densities of Mg isotopes from stable to N=20 lol



$$\begin{aligned}
 \rho_{\alpha}(q, \mathbf{K}_{NA}, \epsilon) &= \sum_{\alpha} \int d^3K_1(q, \mathbf{K}_{NA}, \epsilon) A_{\alpha} \left( q \frac{1}{2} \left( \frac{A+1}{A} \mathbf{K}_{NA} + \mathbf{K} \right) \right) \rho_{\alpha}^{(0)}(\mathbf{P}, \mathbf{P}) \\
 &+ i(\epsilon^{(0)} - \epsilon) \sum_{\alpha} \int d^3K_1(q, \mathbf{K}_{NA}, \epsilon) C_{\alpha} \left( q \frac{1}{2} \left( \frac{A+1}{A} \mathbf{K}_{NA} + \mathbf{K} \right) \right) \rho_{\alpha}^{(0)}(\mathbf{P}, \mathbf{P}) \\
 &+ i \sum_{\alpha} \int d^3K_1(q, \mathbf{K}_{NA}, \epsilon) C_{\alpha} \left( q \frac{1}{2} \left( \frac{A+1}{A} \mathbf{K}_{NA} + \mathbf{K} \right) \right) S_{\alpha}(\mathbf{P}, \mathbf{P}) \\
 &+ i(\epsilon^{(0)} - \epsilon) \sum_{\alpha} \int d^3K_1(q, \mathbf{K}_{NA}, \epsilon) M_{\alpha} \left( q \frac{1}{2} \left( \frac{A+1}{A} \mathbf{K}_{NA} + \mathbf{K} \right) \right) S_{\alpha}(\mathbf{P}, \mathbf{P})
 \end{aligned}$$

= dens



KDUQ: Pruitt et al., Phys. Rev. C **107**, 014602 (2023)

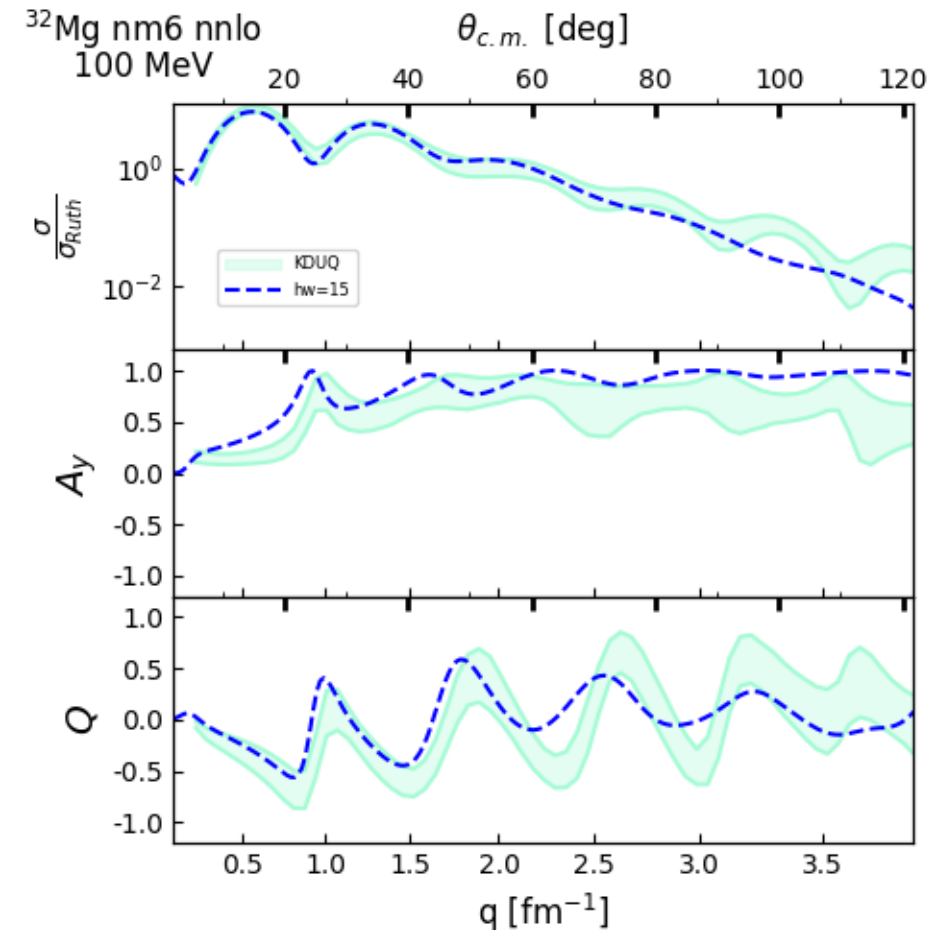
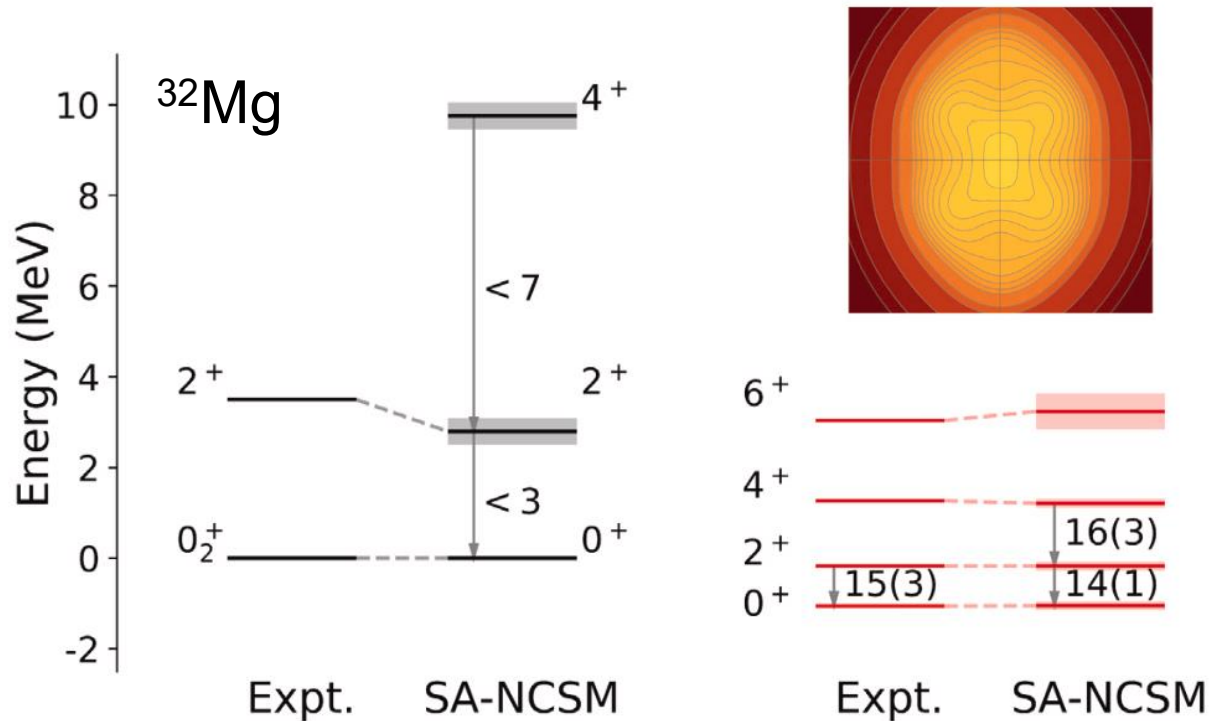
Sargsyan, Fuentealba-Bustamente, Beyer, Elster, in preparation

G. Sargsyan, 26 February 2026, Slide 12



# SA-NCSM structure input of $^{32}\text{Mg}$ for reactions calculations

7 PAC-approved FRIB experiments studying  
N=20 island of inversion nuclei

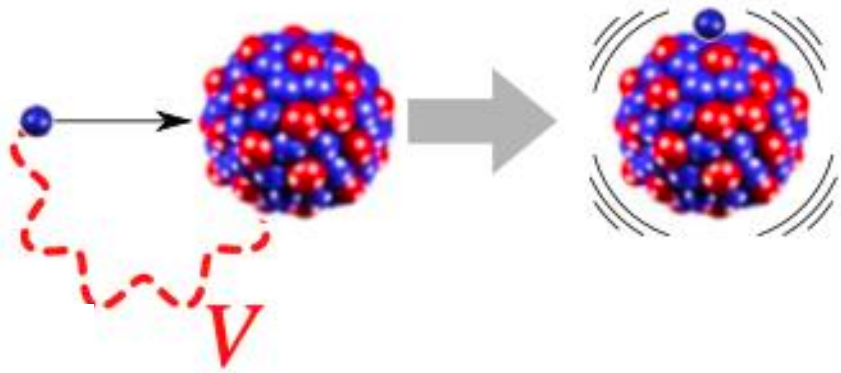


Launey, Sargsyan, et al., *Prog. Part. Nucl. Phys.* **148**, 104233 (2026)

Sargsyan, Fuentealba-Bustamente, Beyer, Elster, in preparation



# Embedding nuclear structure information within OP



Feshbach formalism

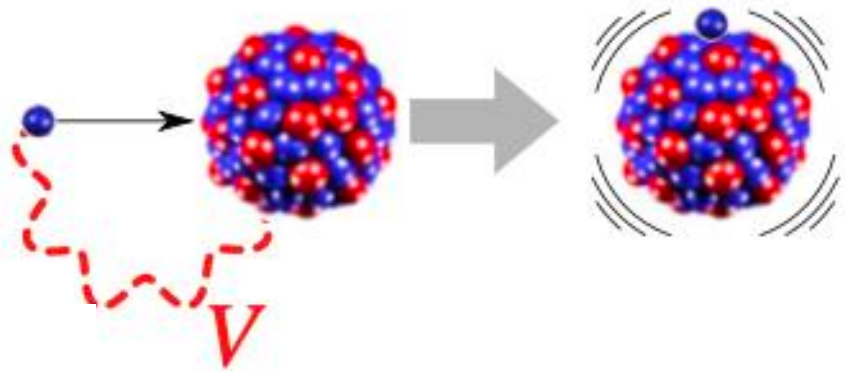
$$\begin{aligned}
 V(\mathbf{r}, \mathbf{r}', E) &= U_0(\mathbf{r}) + V_{PO}(\mathbf{r}, \mathbf{r}', E - E_i) \\
 &= U_0(\mathbf{r}) + \sum_i U_{0i}(\mathbf{r}) G_i(\mathbf{r}, \mathbf{r}', E - E_i) U_{0i}(\mathbf{r}')
 \end{aligned}$$

Static,  
energy-independent  
potential

Polarization potential:  
Requires input from  
nuclear structure

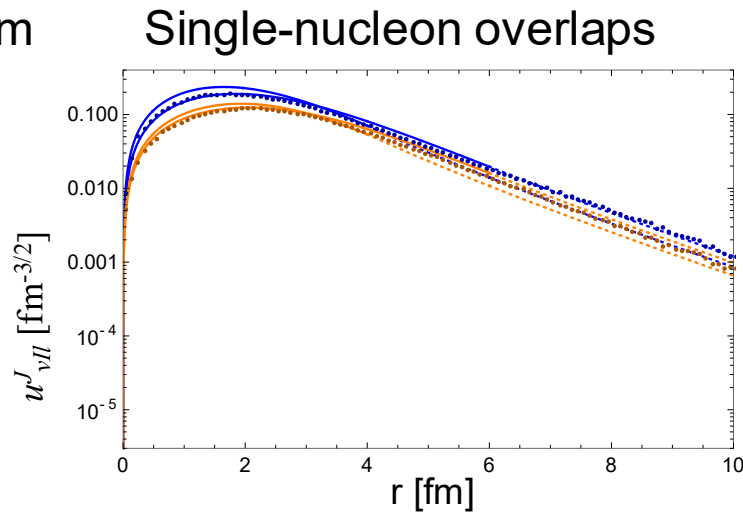
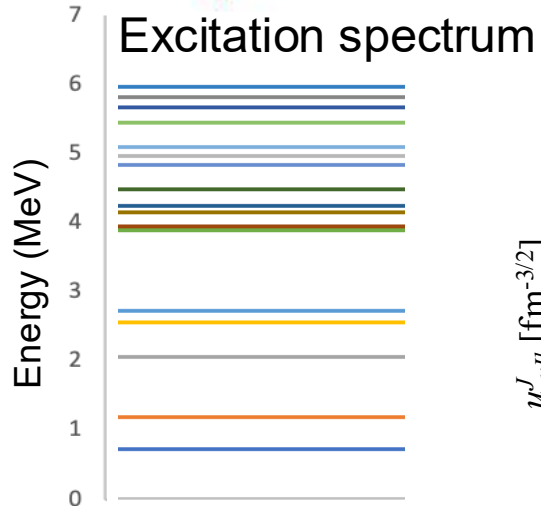
Can be applied to any mass range if  
nuclear structure calculations are  
available

# Embedding nuclear structure information within OP



Feshbach formalism

$$\begin{aligned}
 V(\mathbf{r}, \mathbf{r}', E) &= U_0(\mathbf{r}) + V_{PO}(\mathbf{r}, \mathbf{r}', E - E_i) \\
 &= U_0(\mathbf{r}) + \underbrace{\sum_i U_{0i}(\mathbf{r}) G_i(\mathbf{r}, \mathbf{r}', E - E_i) U_{0i}(\mathbf{r}')}_{\text{Polarization potential: Requires input from nuclear structure}}
 \end{aligned}$$



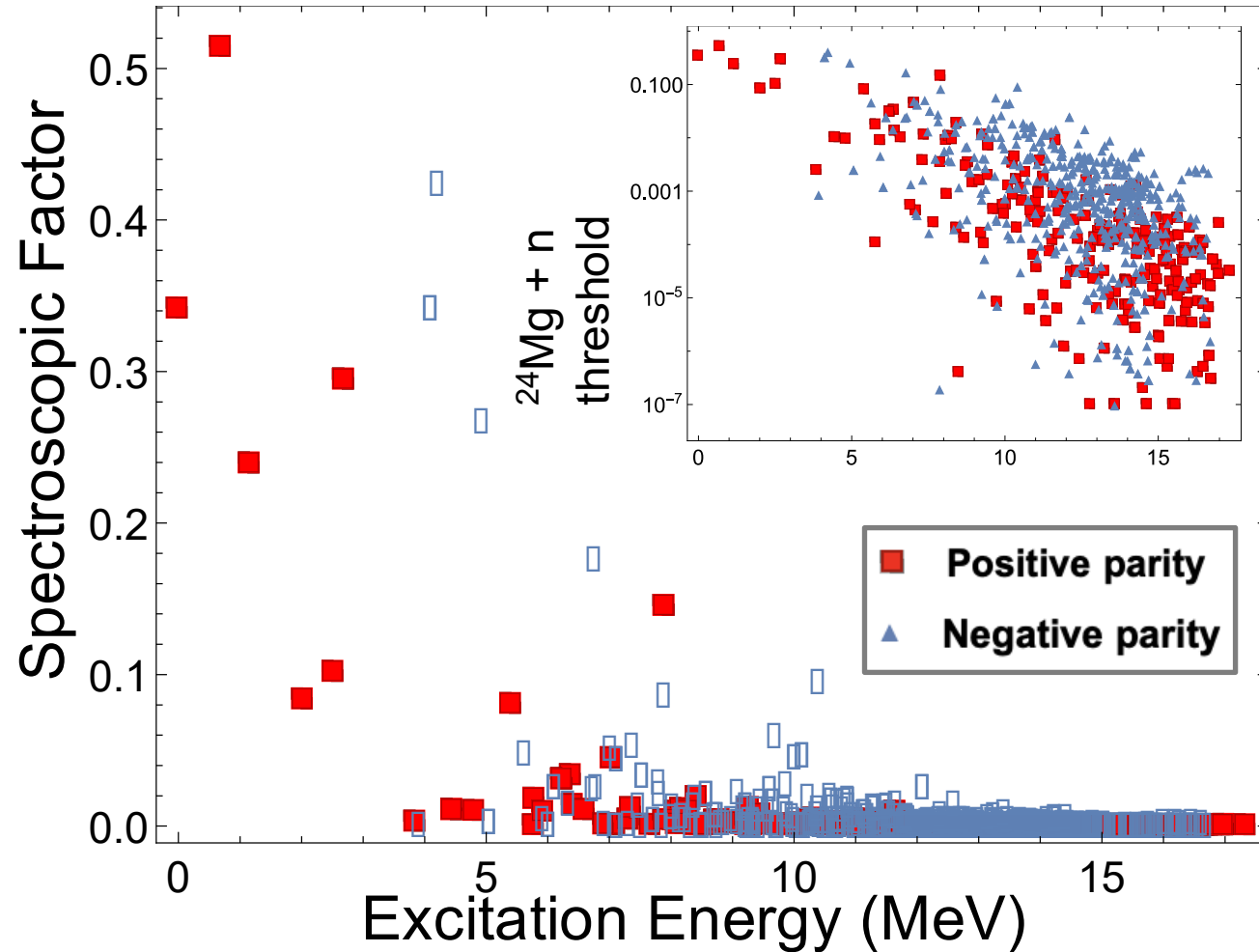
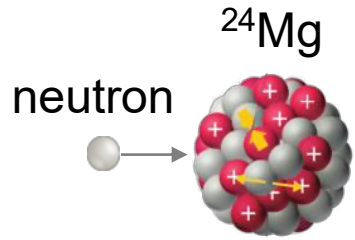
Polarization potential:  
Requires input from  
nuclear structure

e.g., shell model, RPA,  
ab initio models, ...

Sargsyan, et al., PRC 108, 054303 (2023)



# 1<sup>st</sup> ingredient for constructing OP: shell model input



Around 600  
intrinsic states

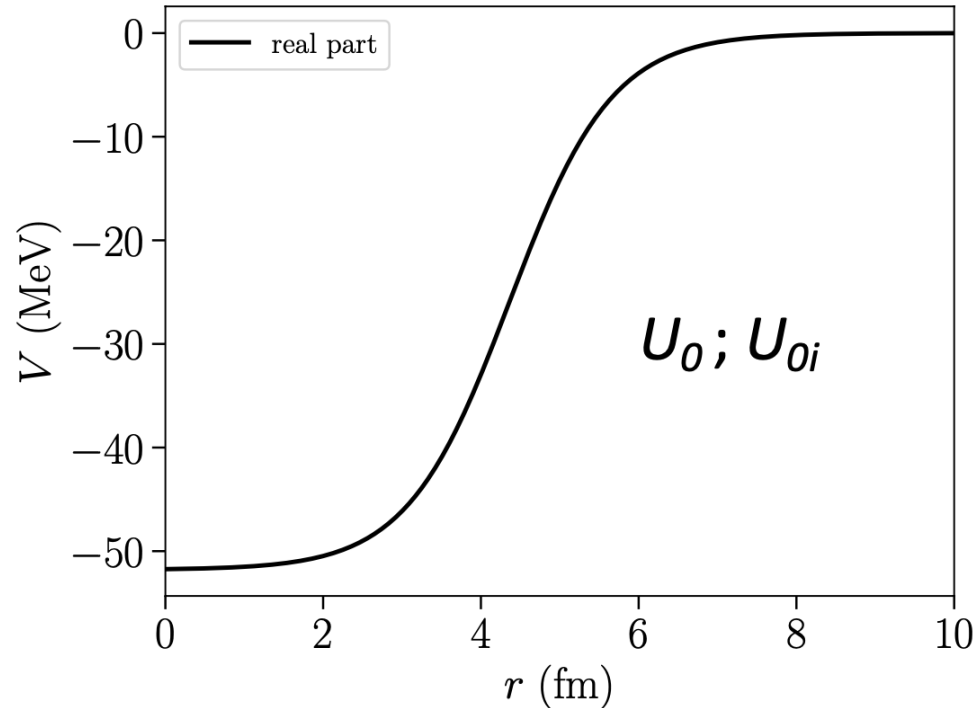
Shell model calculations done using  
**CoSMo**  
PSDPF potential M Bouhelal, *et al.*,  
Nucl. Phys. A 864 (2011)





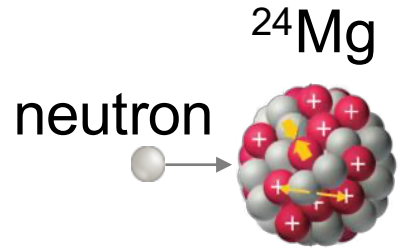
## 2<sup>nd</sup> ingredient: static potential and couplings

$$V(\mathbf{r}, \mathbf{r}', E) = U_0(\mathbf{r}) + \sum_i U_{0i}(\mathbf{r}) G_i(\mathbf{r}, \mathbf{r}', E - E_i) U_{0i}(\mathbf{r}')$$

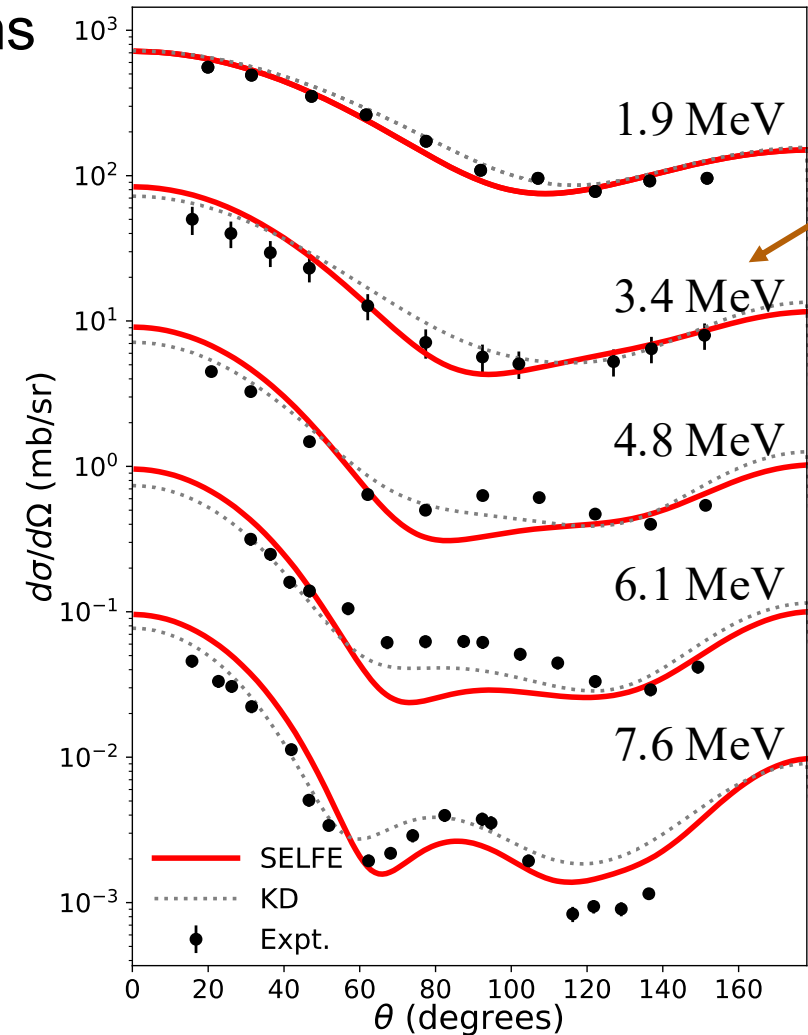
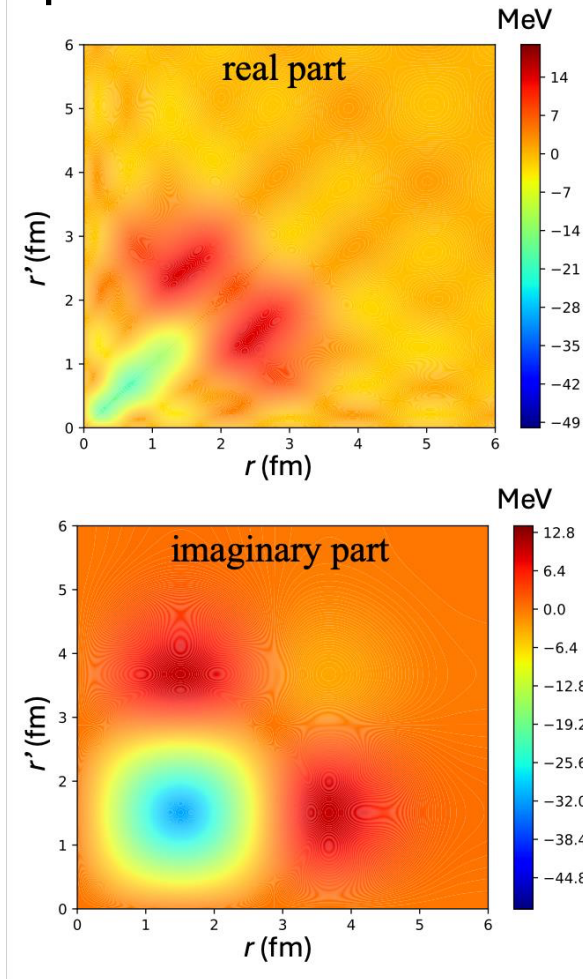


- static potential  $U_0$ : real, local Woods-Saxon adjusted to reproduce binding energy of  $^{25}\text{Mg}$
- couplings  $U_{0i}$ : same real Woods-Saxon, but adjusted to each  $E_i$  and multiplied by spectroscopic factor  $S_i$  from shell model

# Accurate prediction without parameters fitted to experimental scattering data!



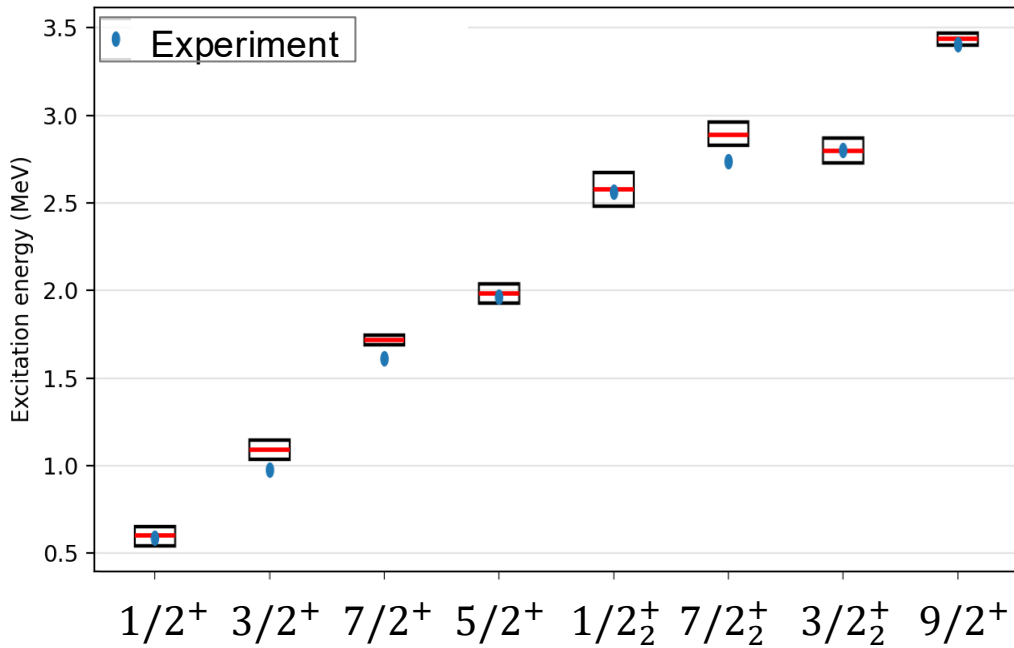
Optical potential for 3.4 MeV neutrons



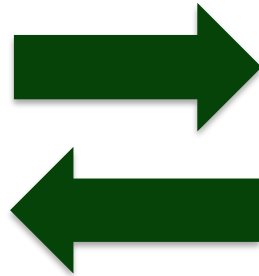
# Propagating structure uncertainties to reactions

Uncertainty quantified shell model potential (USDBUQ)  
 O. Gorton, K. Kravvaris, Phys. Rev. C 112, 014302 (2025)

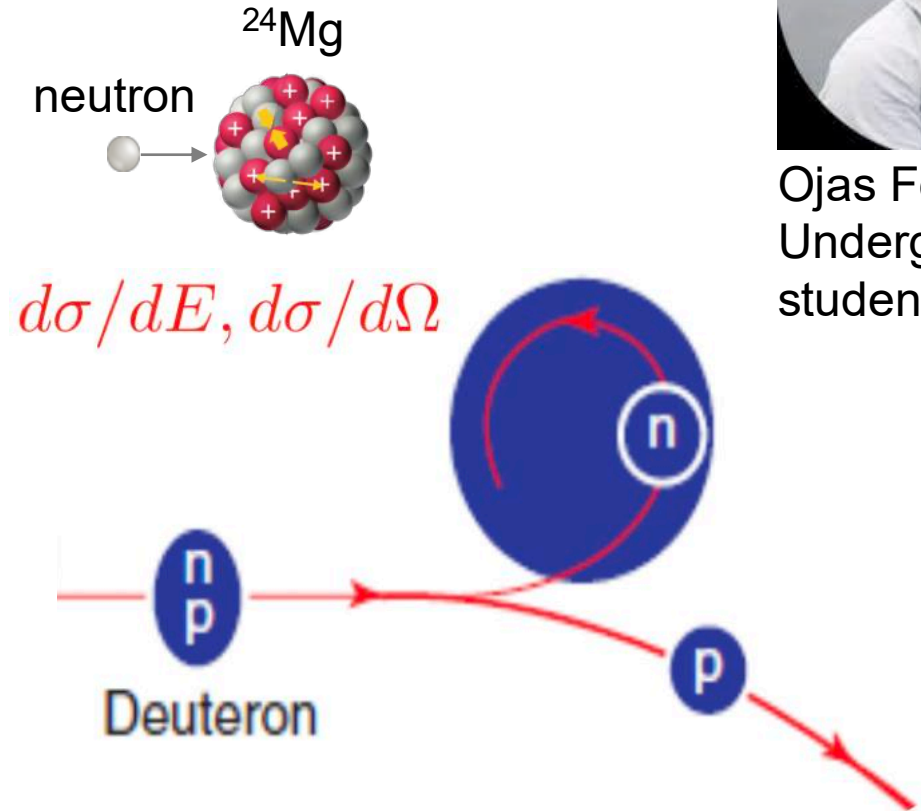
$^{25}\text{Mg}$  spectrum



UQ



Calculations by O. Fernandes

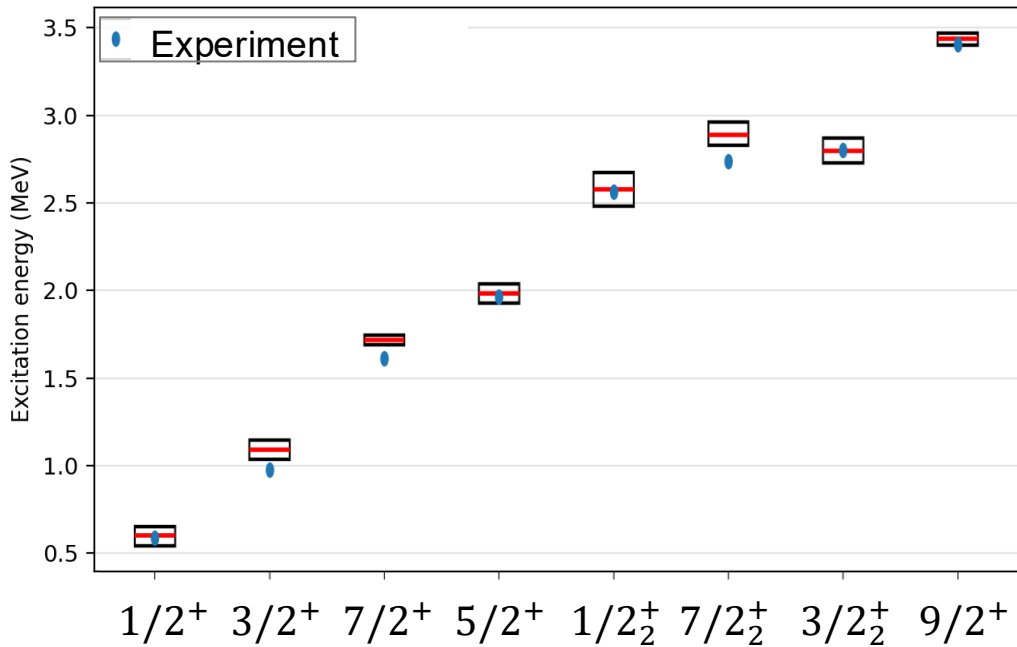


Ojas Fernandes,  
 Undergraduate  
 student @MSU

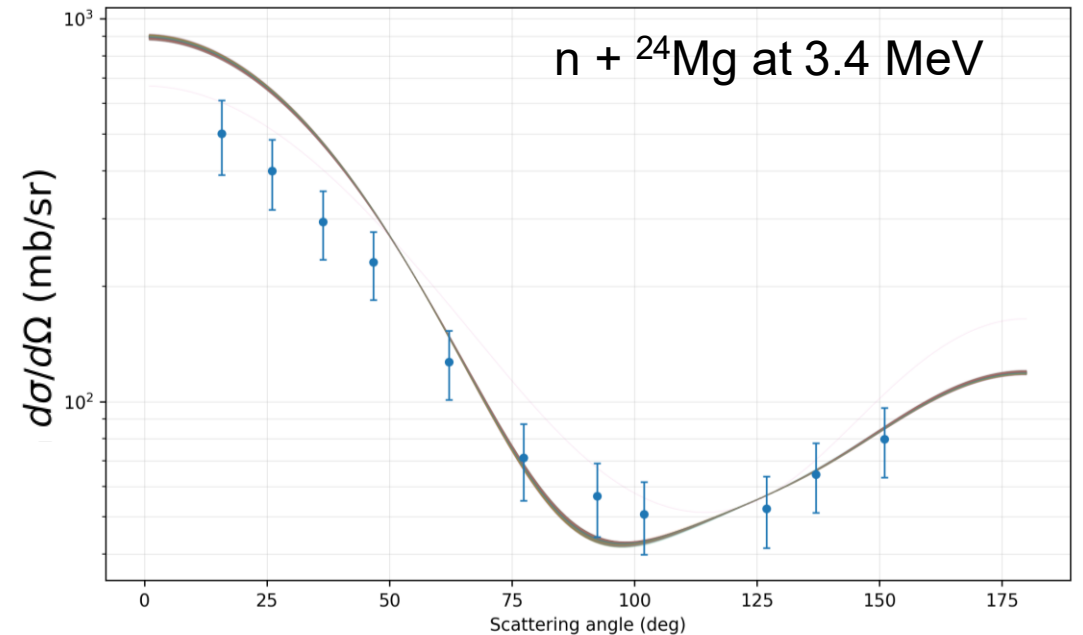
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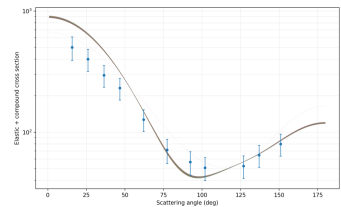
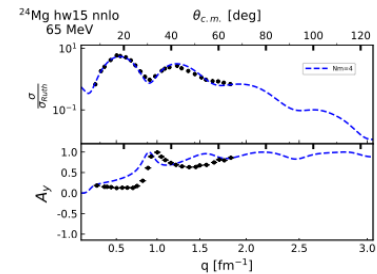
UQ  
→



Calculations by O. Fernandes

# Summary

- Nuclear reaction models need input from structure
- Modern *ab initio* models can provide a reliable input with predictive capabilities
- We have used SA-NCSM to provide input to study alpha clustering in  $^{16}\text{O}$  and  $^{20}\text{Ne}$  via knockout and transfer reactions
- Multiple scattering approach with SA-NCSM densities provides a good description of Mg scattering data for  $>65$  MeV and predictions where no data exists
- Our new approach for low-energy scattering uses spectroscopic factors and excitation energies to build an optical potential
- This approach can propagate structure uncertainties to reaction observables



# Acknowledgements

Charlotte Elster, Jose Fuentealba



Kristina Launey



Oliver Gorton, Kostas Kravvaris



Gregory Potel



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# Thank you!



Theory Alliance  
FACILITY FOR RARE ISOTOPE BEAMS

Grigor Sargsyan