



# Fine-tunings in Nuclear Physics

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by ERC, EXOTIC



by NRW-FAIR

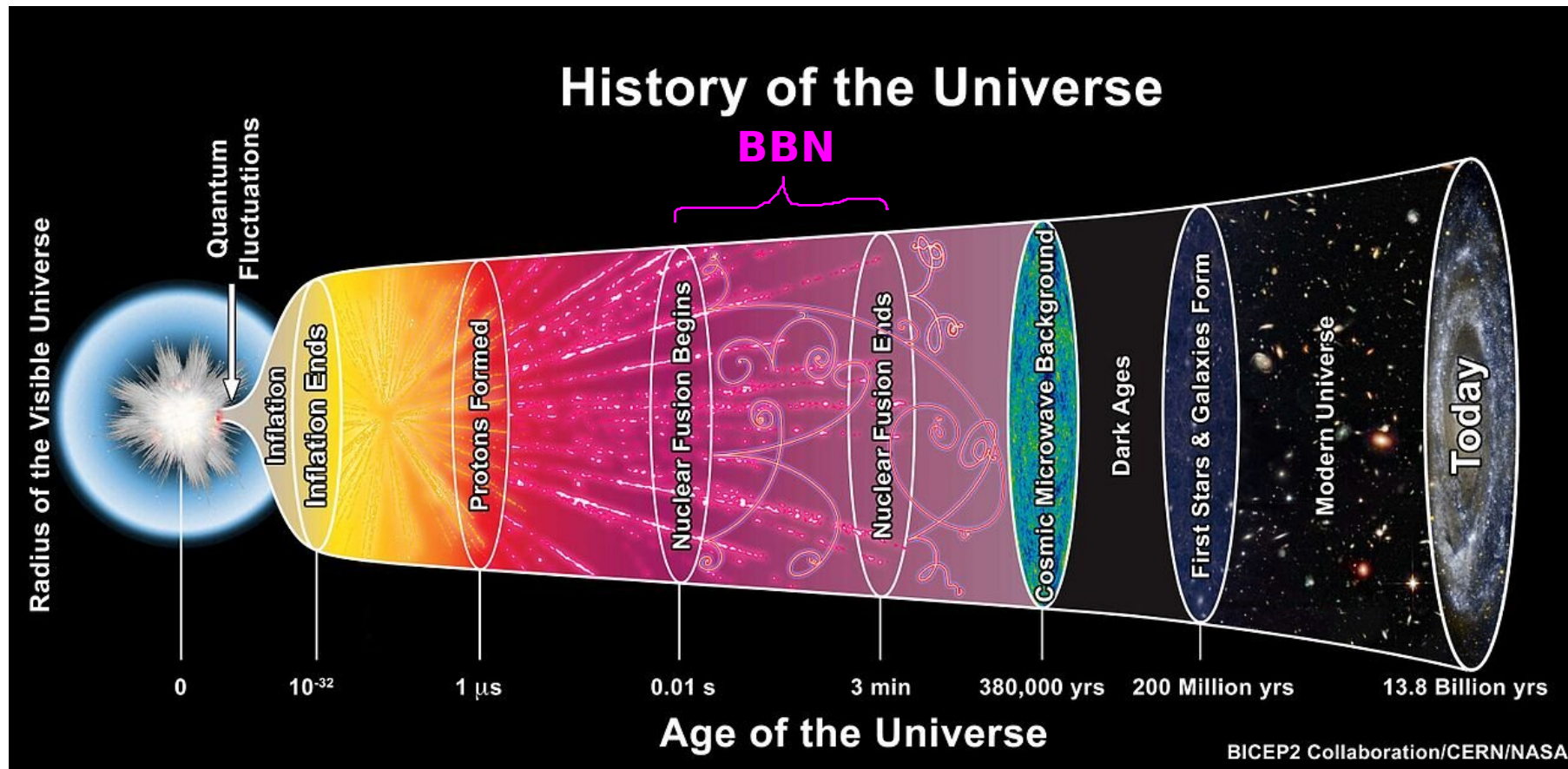


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- BBN: bounds on fundamental parameters
- The fate of carbon-based life as a function of the quark mass
- A dose of philosophy: The anthropic principle
- How fine-tuned is the holy grail of nuclear astrophysics?
- Summary & outlook

# Definition of the physics problem

# History of the Universe



- BBN is a fine probe of our understanding of fundamental physics

Olive et al. (2000), Iocco et al. (2009), Cyburt et al. (2016), Pitrou et al (2018), ...

- Are the fundamental constants really constant?

Dirac (1973), and many others

# Primordial element generation

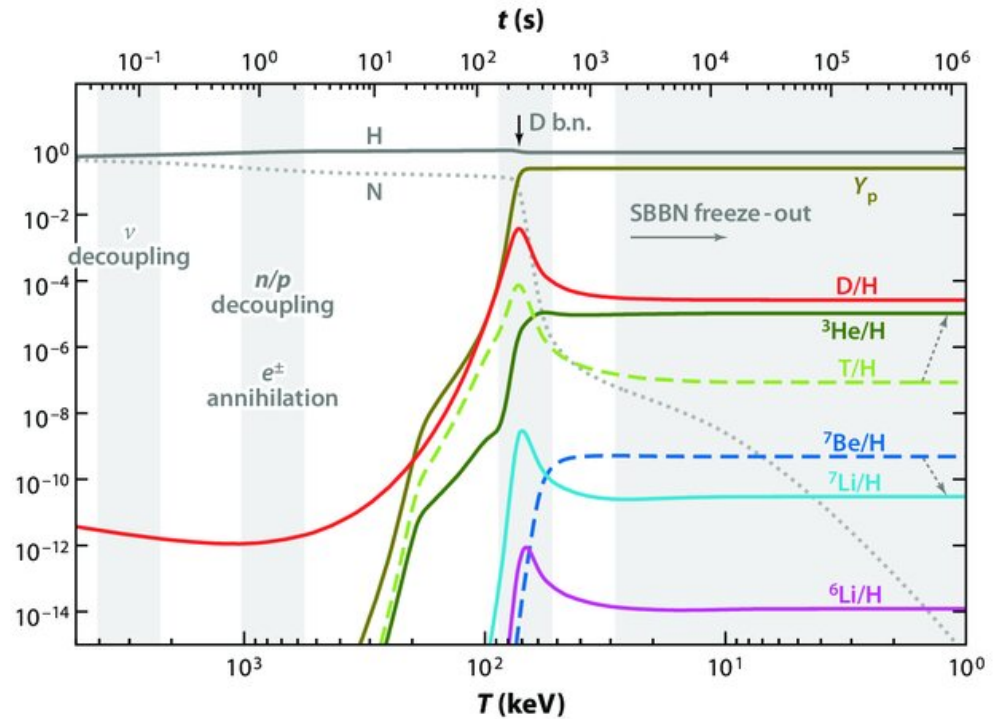
Fusion of  $d$ ,  ${}^3\text{H}$ ,  ${}^3\text{He}$ ,  ${}^4\text{He}$ ,  ${}^6\text{Li}$ ,  ${}^7\text{Li}$  and  ${}^7\text{Be}$

1 min:  
 “deuterium bottleneck”:  
 $n + p \rightarrow d + \gamma$  possible

3 min

1 s:  $n \leftrightarrow p$   
 freeze-out

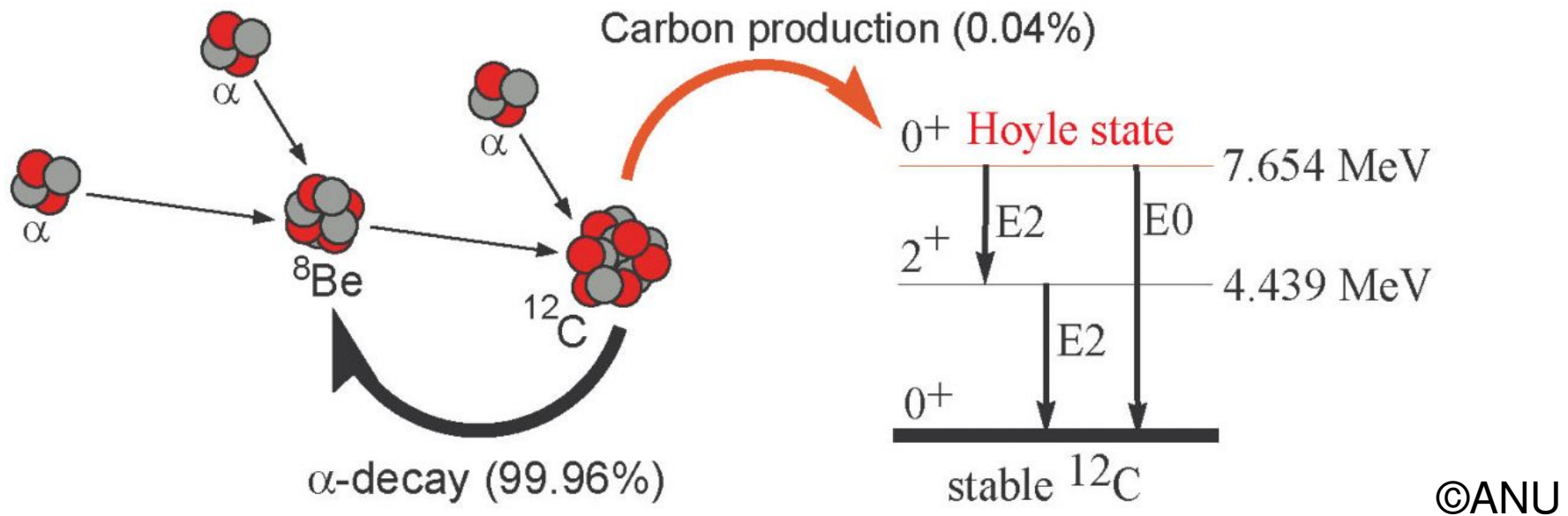
- deuteron weakly bound  
 $\hookrightarrow$  deuterium bottleneck
- $\hookrightarrow$  first nuclear fine-tuning
- also small  $m_n - m_p \dots$



Pospelov, Pradler (2010)

# The triple-alpha process

- Carbon is generated through the fusion of 3 helium nuclei (alpha-particles)



- The  ${}^8\text{Be}$  nucleus is unstable, long lifetime ( $10^{-16}$  s)  $\rightarrow$  3 alpha-particles must meet
- The Hoyle state is located just above the continuum threshold  $\rightarrow$  the excited carbon nuclei decay in various ways

$\hookrightarrow$  we encounter 2 fine-tunings!

# BBN: some technicalities

# Evolution of the abundances

- Abundance defined via  $Y_i = \frac{n_i}{n_b}$

$n_i$  = density of species  $i$

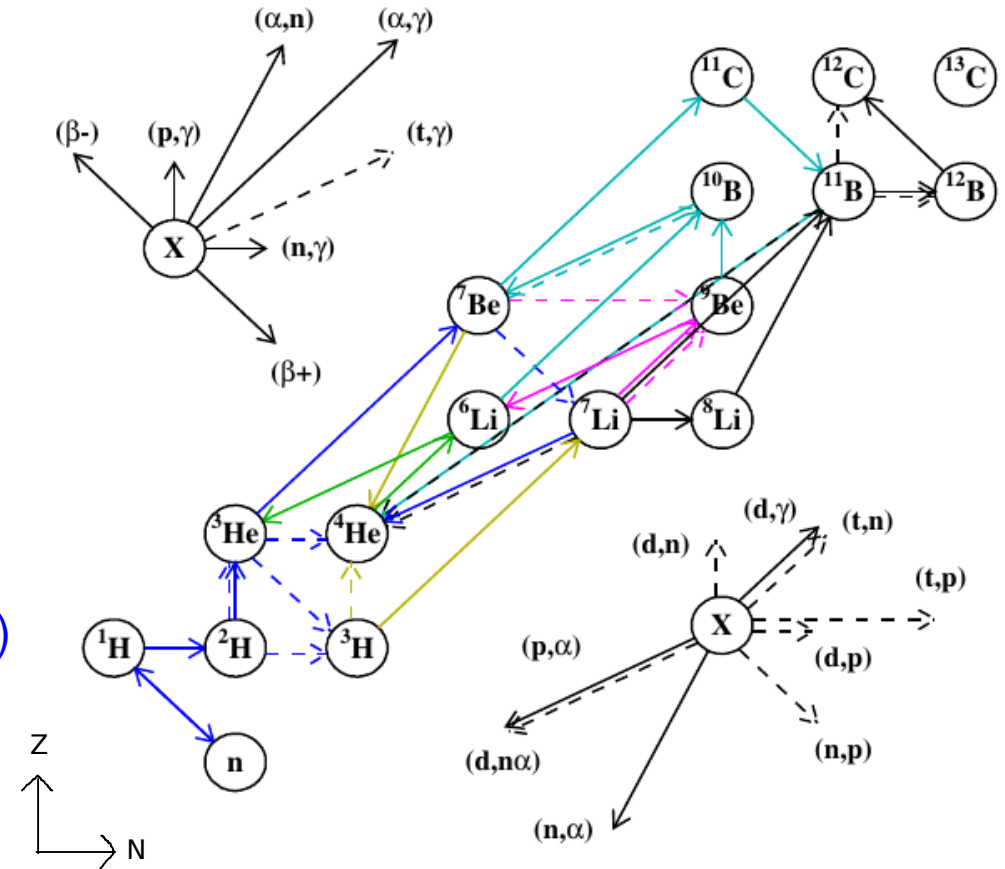
$n_b$  = total baryon density

- Evolution depends on

– cosmological model: Hubble expansion

– **particle reactions** ( $\Gamma_{ij \rightarrow kl} = n_b \langle \sigma v \rangle_{ij \rightarrow kl}$ )  
and **decays** ( $\Gamma_{i \rightarrow \dots}$ )

⇒ need to solve the system of rate equations:



Pitrou et al. (2018)

$$\dot{Y}_i \supset -Y_i \Gamma_{i \rightarrow \dots} + Y_j \Gamma_{j \rightarrow i + \dots} + Y_k Y_l \Gamma_{lk \rightarrow ij} - Y_i Y_j \Gamma_{ij \rightarrow kl}$$

# Evolution of the abundances - results

- 5 different codes:

NUC123 (Kawano-code) [FORTRAN, 88 rate eqs.]

Kawano, FERMILAB-PUB-92-004-A (1992)

PRIMAT [Mathematica, 423 rate eqs.]

Pitrou et al., Phys. Rept. 754 (2018) 1

AlterBBN [C, 100 rate eqs.]

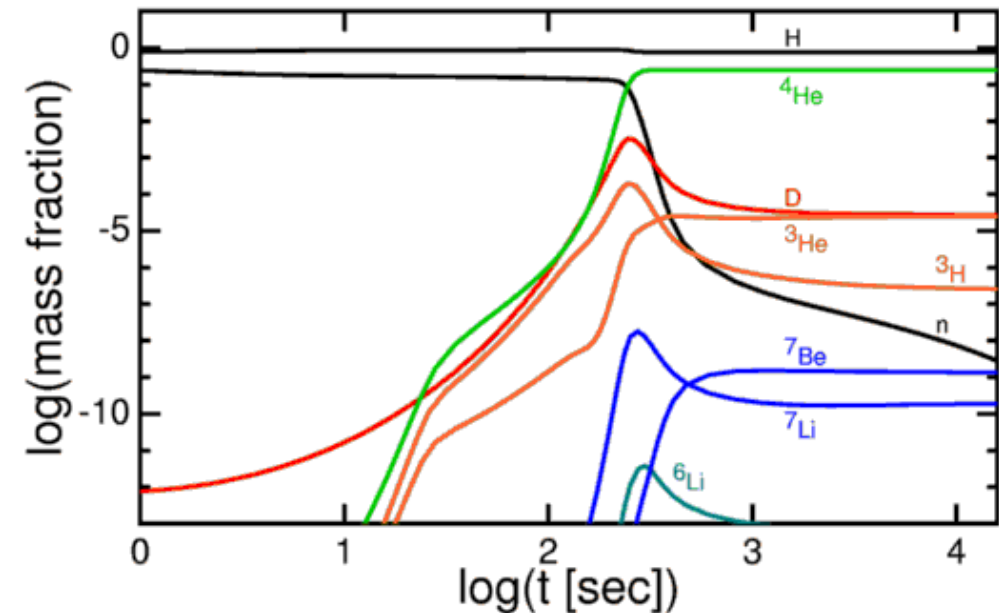
Arbey et al., Comp. Phys. Comm. 248 (2020) 106902

PARthENoPE [FORTRAN, 100 rate eqs.]

Gariazzo et al., Comp. Phys. Comm. 271 (2022) 108205

PRyMordial [Python, 423 rate eqs.]

Burns et al., Eur. Phys. J. C **84** (2024) 86



Burles, Nollett, Turner (2001)

- Altho' the results are by and large consistent in spite of the differences (# of rate eqs, QED, ...)

↪ when considering the variation of fundamental parameters such as  $\alpha_{EM}$ , we must use all these codes to have a grip on the systematics

# Fundamental forces and constants I

- Must consider the strong, electromagnetic and weak interactions ( $v = \text{Higgs VEV}$ )
- **Strong interactions:**  $\Lambda_{\text{QCD}}, m_q (q = u, d, s) \leftrightarrow m_f = g_f v$  (keep  $g_f$  constant)

$$\leftrightarrow \boxed{\Lambda_{\text{QCD}} \sim \left(1 + \frac{\delta v}{v}\right)^{1/4}} \quad \text{Agrawal et al. (1998), Burns et al. (2024)}$$

- In almost all nuclear reactions, strong isospin violation  $m_d/m_u \simeq 2$

can be neglected because  $\frac{m_u - m_d}{\Lambda_{\text{QCD}}} \simeq \frac{1}{100}$

- $m_d \neq m_u$  features prominently in neutron  $\beta$ -decay
- Dominant strange quark effect through the nucleon mass (trace anomaly)

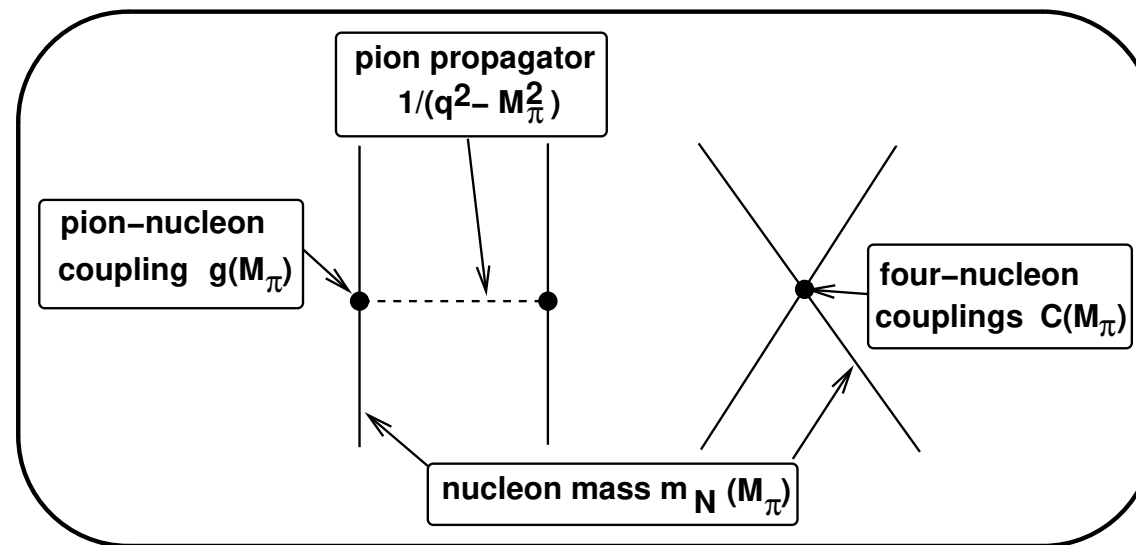
$$m_N^{u,d,s} = \langle N(p) | m_u \bar{u}u + m_d \bar{d}d + m_s \bar{s}s | N(p) \rangle$$

- Quark mass variations = variations of the weak scale  $v$  (Yukawa's fixed)  
Higgs VEV

# A closer look at the strong interactions

- Nuclear forces are given by chiral EFT based on Weinberg's power counting
- ⇒ Pion-exchange contributions and short-distance multi-N operators
- graphical representation of the quark mass dependence of the LO potential

Weinberg 1991



- always use the Gell-Mann–Oakes–Renner relation:  $M_{\pi^\pm}^2 \sim (m_u + m_d)$

- fulfilled to better than 94% in QCD

Colangelo, Gasser, Leutwyler 2001

- use input from lattice QCD and chiral perturbation theory

# Fundamental forces and constants II

- **EM interactions:**  $\leftrightarrow$  variations of the fine-structure constant  $\alpha_{EM}$  around its present day value  $\alpha_0 = 7.2973525693(11) \times 10^{-3}$

- Where does  $\alpha_{EM}$  appear in BBN?

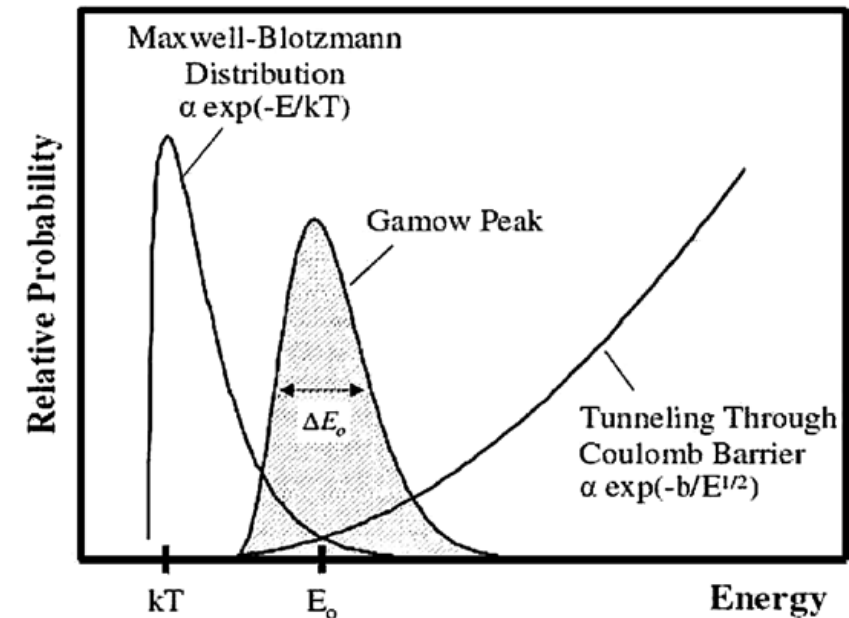
- Nuclear Rates: Coulomb barrier

- Gamow factor Gamow (1928)

- Radiative capture reactions  $\sigma \propto \alpha_{EM}$

- Weak rates: final-state Coulomb interaction in  $n \leftrightarrow p$  rates and  $\beta$ -decays

- Indirectly:  $n$ - $p$  mass difference  $Q_n = m_n - m_p$ , EM contribution to nuclear binding energies → reaction Q-values



from Trache (2010)

- **Weak interactions:**  $\leftrightarrow$  variations of the Fermi constant  $G_F$ ,  $m_f$

# BBN: results

UGM, Metsch, Eur. Phys. J. A **58** (2022) 212 [2208.12600 [nucl-th]]

UGM, Metsch, Meyer, Eur. Phys. J. A **59** (2023) 223 [2305.15849 [hep-th]]

Meyer, UGM, JHEP **06** (2024) 074, JHEP **01** (2025) 033 (err) [2403.09325 [hep-ph]]

UGM, Metsch, Meyer, Eur. Phys. J. A **60** (2024) 200 [2405.09971 [nucl-th]]

UGM, Metsch, Meyer, JHEP **06** (2025) 244 [2502.15409 [hep-ph]]

UGM, Metsch, Meyer, Eur. Phys. J. A **61** (2025) 5, 122 [2503.15162 [nucl-th]]

# Results I: Variations of $\alpha$

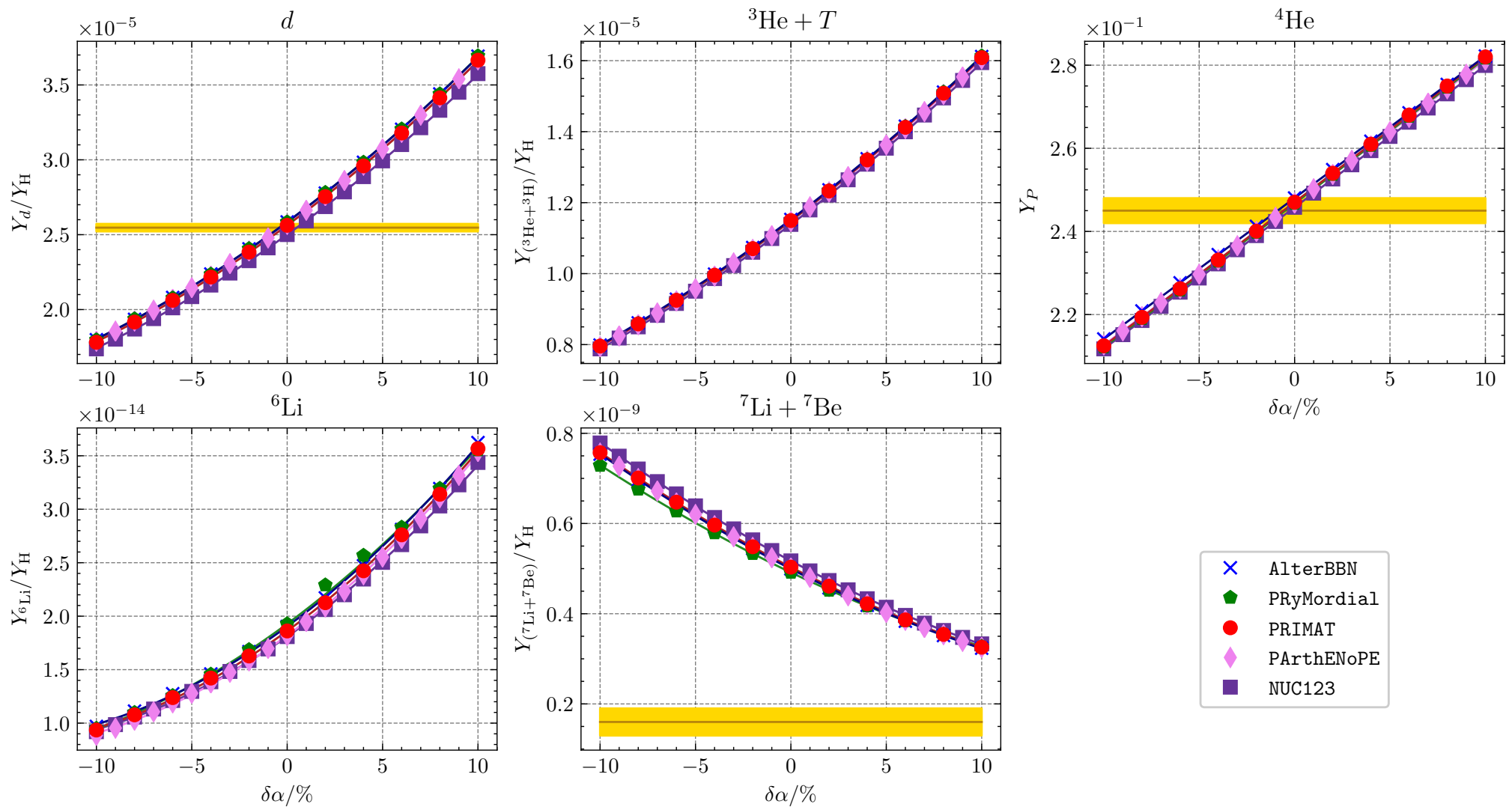
- Consider first the variation in the fine-structure constant  $\alpha$
- Parameter fit at fixed  $\eta = 6.14 \cdot 10^{-10}$  and  $\tau_n = 879.4$  s:

$$\frac{Y(\alpha) - Y(\alpha_0)}{Y(\alpha_0)} = a \cdot \frac{\delta\alpha}{\alpha_0} + b \cdot \left(\frac{\delta\alpha}{\alpha_0}\right)^2$$

- Consider variations in  $\alpha$  up to  $|\delta\alpha/\alpha_0| \leq 0.1$
- Main results:
  - Temperature-dependence of reaction rates at varying  $\alpha$  important
  - For most elements, change in the nuclear reaction rates is the biggest effect
  - ${}^4\text{He}$  abundance indeed very sensitive to  $Q_n^{\text{QED}}$
  - Lithium problem persists

# Results II: Variations of $\alpha$

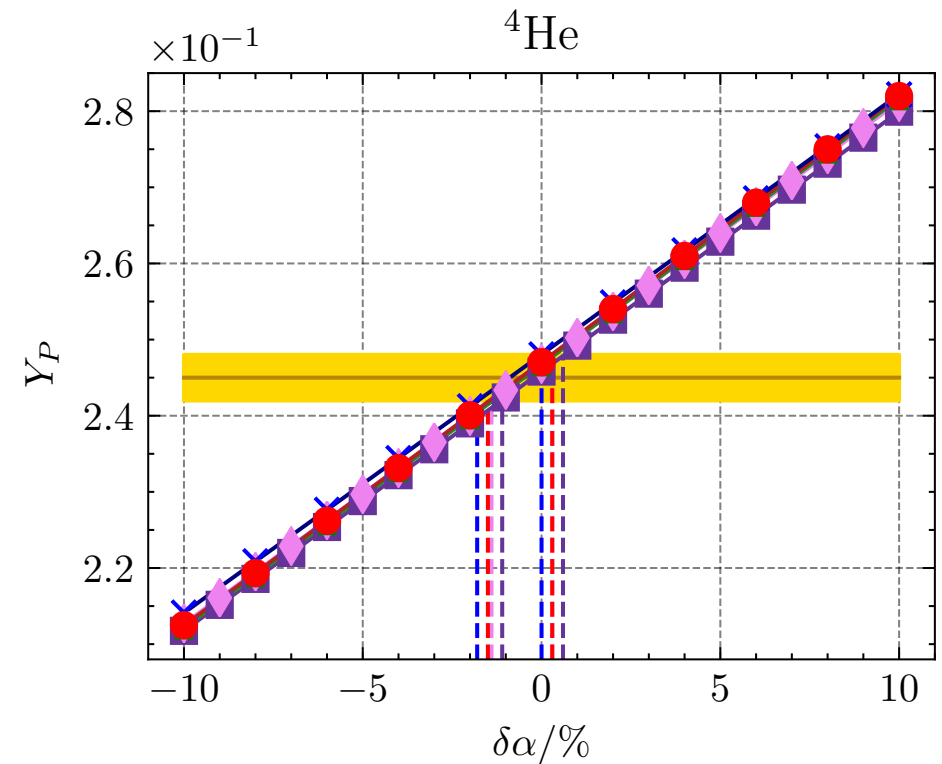
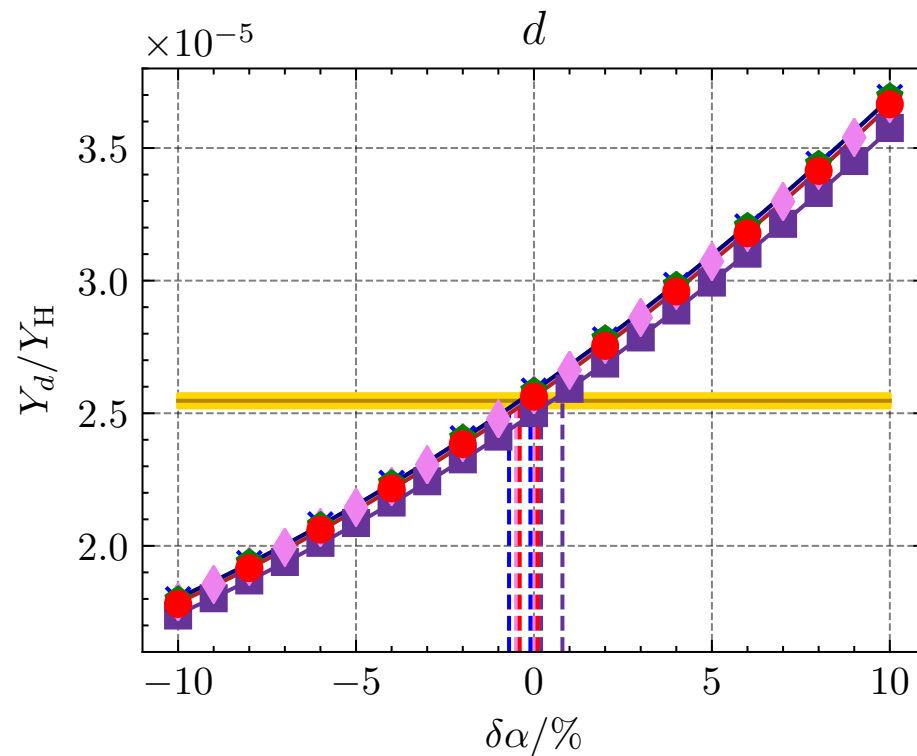
- $\alpha$ -dependence of the abundances:



↪ largely independent of the codes

# Results III: Variations of $\alpha$

- Extract the allowed  $\alpha$ -variation:



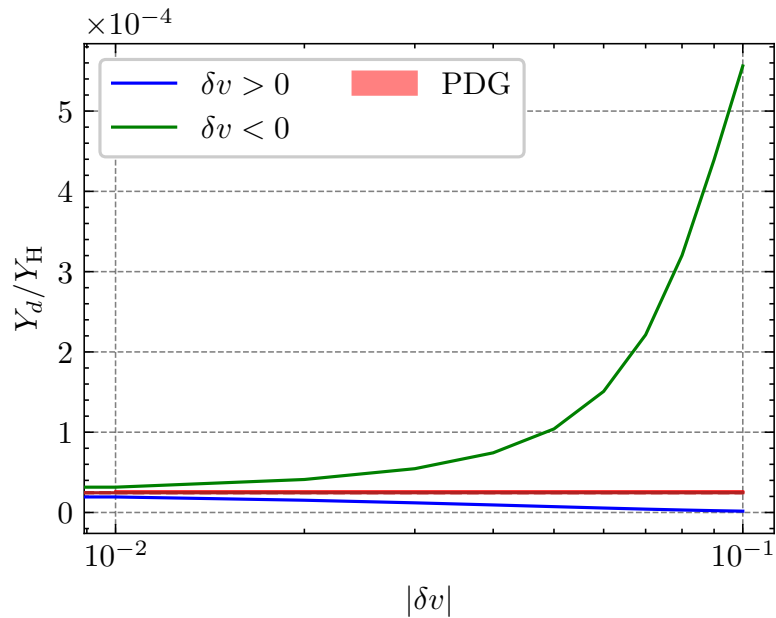
- $1\sigma$ -bounds on  $\alpha$ -variation  $\Rightarrow$  from  ${}^4\text{He}$ :

$$|\delta\alpha| < 1.8\%$$

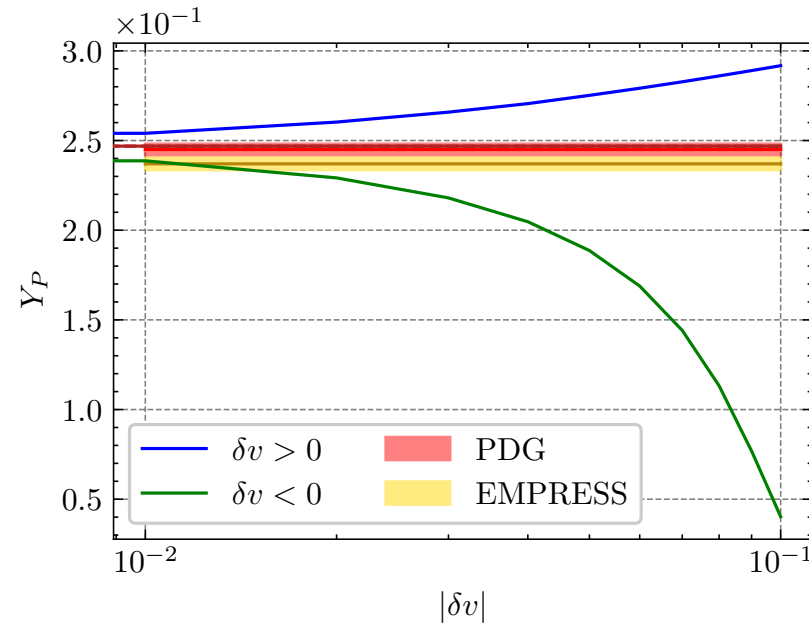
- Stronger bound than found earlier (updated reaction rates, smaller  $Q_n^{\text{QED}}$ ,  $T$ -dependence of the reactions)

# Results IV: Bounds on the Higgs VEV variations

- Consider  $d$  and  ${}^4\text{He}$  abundances



$$\delta v/v \in [-0.0007, -0.0002]$$



$$\delta v/v \in [-0.0069, 0.0039] \quad [\text{PDG}]$$

$$\delta v/v \in [-0.0138, -0.0030] \quad [\text{Empress}]$$

↪ much more stringent than found earlier ( $B_d$  changes in  $np \leftrightarrow d\gamma$ )

↪ same strong bounds on the light quark masses  $m_u, m_d$

↪ in contrast to earlier works, the bound from  $Y_d/Y_H$  is tighter than from  $Y_p$

# Results V: Bounds on strange quark mass variations 18

- Map the  $m_s$  dependence onto the nucleon mass of binding energies and other observables

↪ model the  $m_N$  dependence of nuclear reaction rates

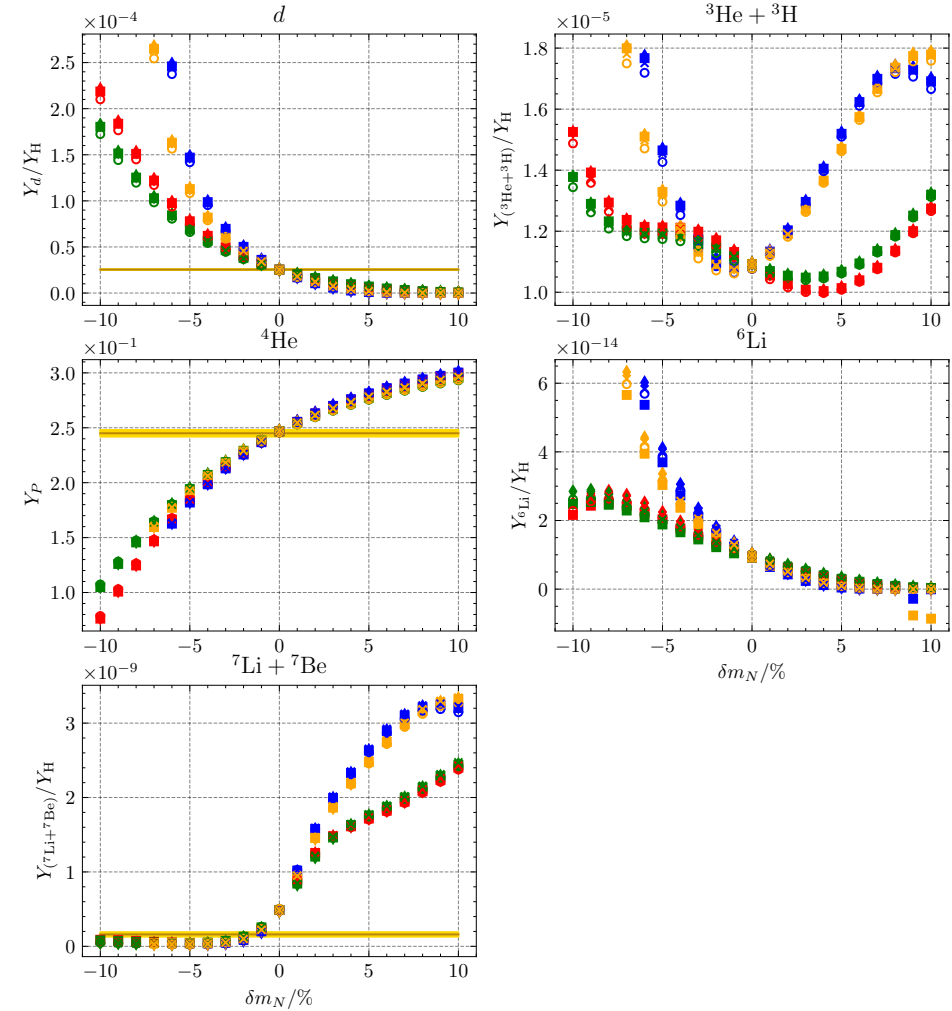
↪ four different ways of doing that (NLEFT, pionless EFT, square-well potential)

↪ use four different codes

↪ get an upper bound on  $m_s$  variations:

$$\left| \frac{\Delta m_s}{m_s} \right| \leq 5.1 \%$$

↪ also bound on variations of  $\Lambda_{\text{QCD}}$ : Less than 1.13% between the BB and now



# The fate of carbon-based life as a function of the quark mass

Epelbaum, Krebs, Lähde, Lee, UGM

Phys. Rev. Lett. **110** (2013) 112502; Eur. Phys. J. **A 48** 82 (2013)

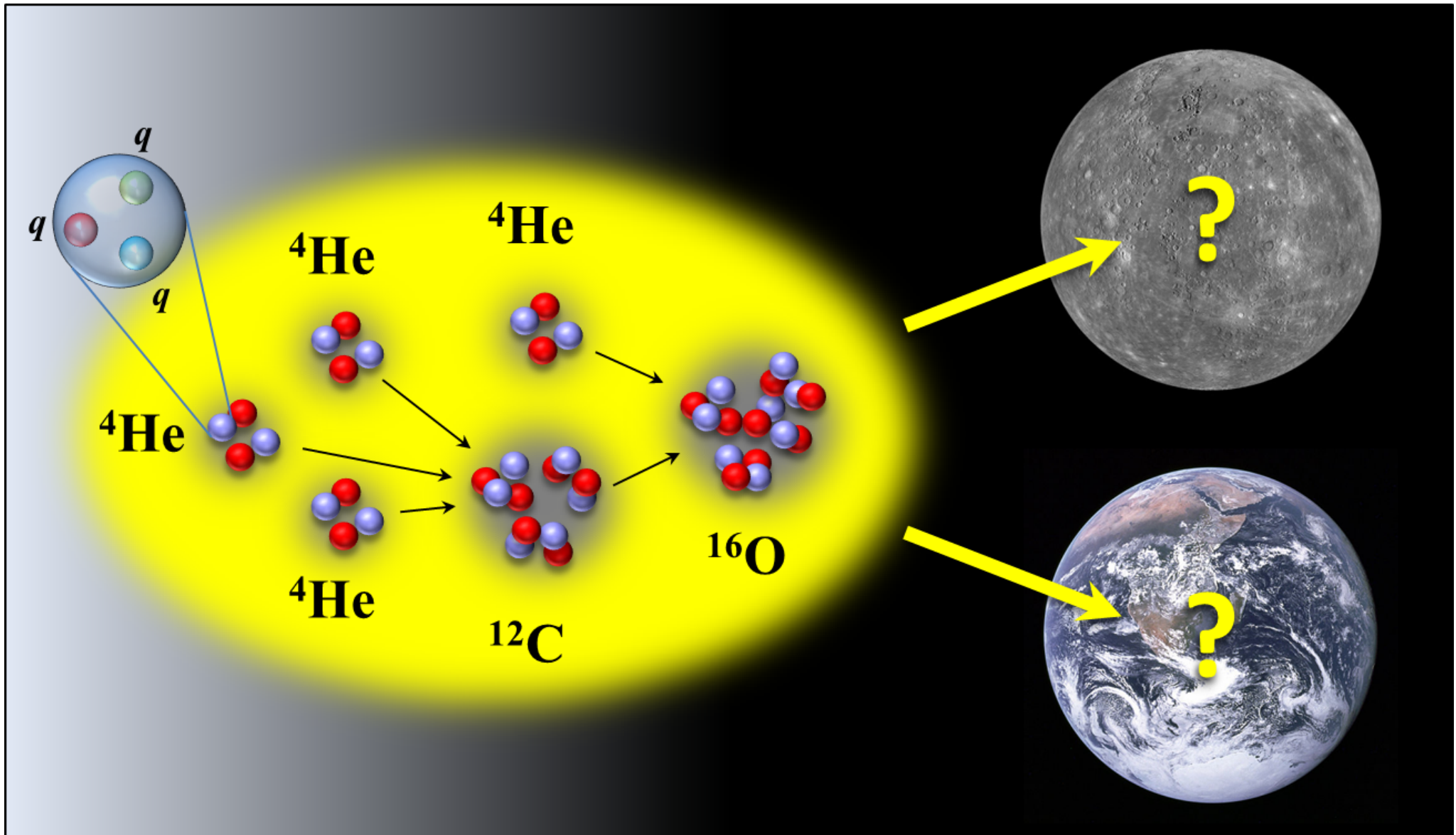
update: Lähde, UGM, Epelbaum, Eur. Phys. J. **A 56** (2020) 89

Elhatisari, Lähde, Lee, UGM, Vonk, JHEP **02** (2022) 001

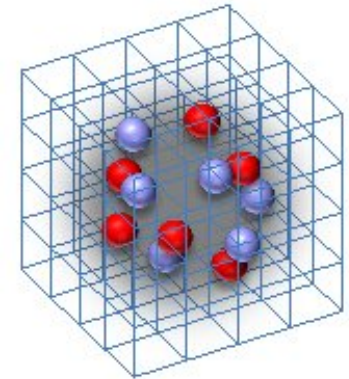
review: UGM, Sci. Bull. **60** (2015) 43

# Fine-tuning of the fundamental parameters

Fig. courtesy Dean Lee



# The tool: Nuclear lattice effective field theory

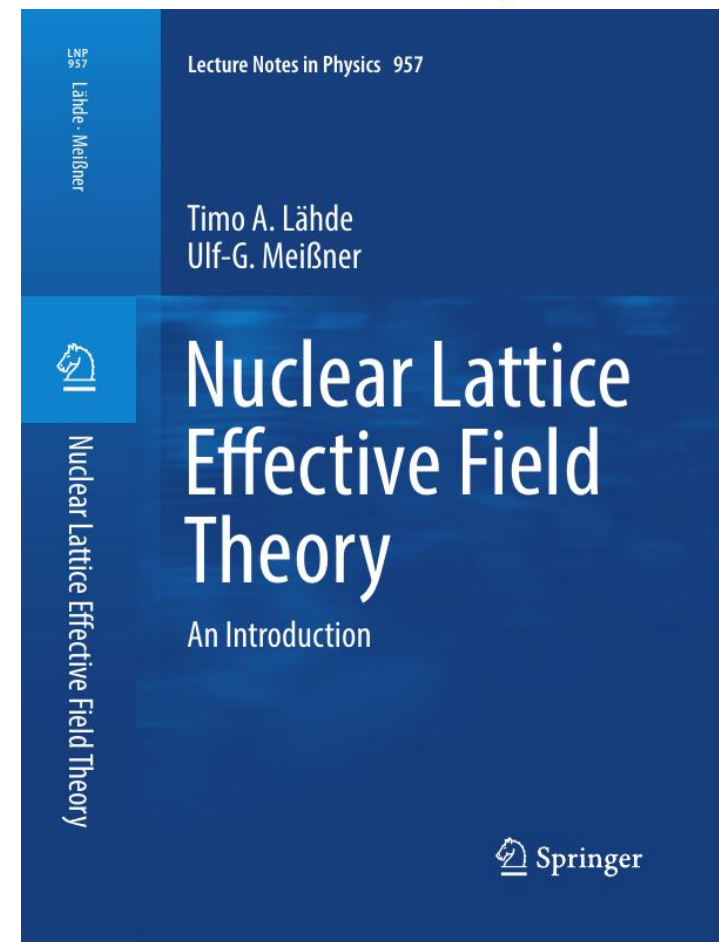


- A new many-body approach: NLEFT
- For all details on chiral EFT on a lattice

T. Lähde & UGM

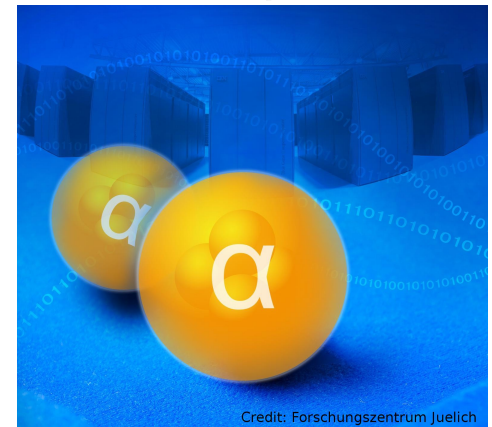
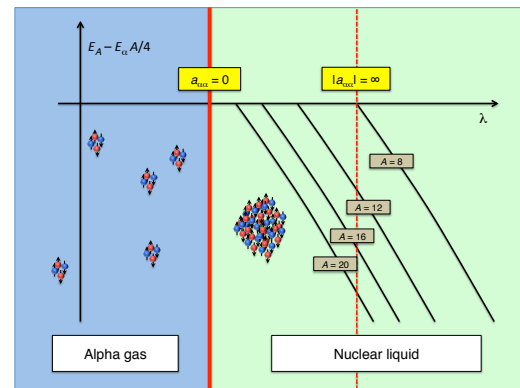
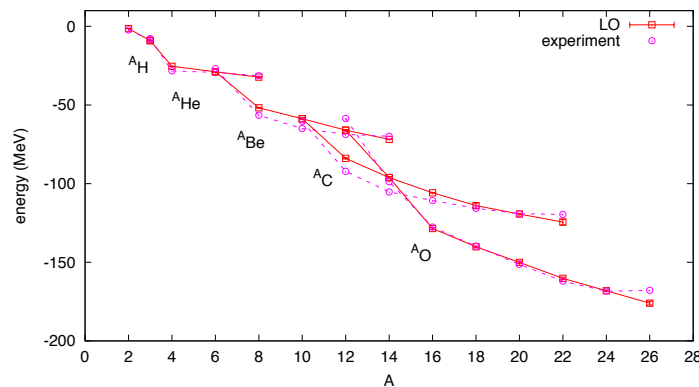
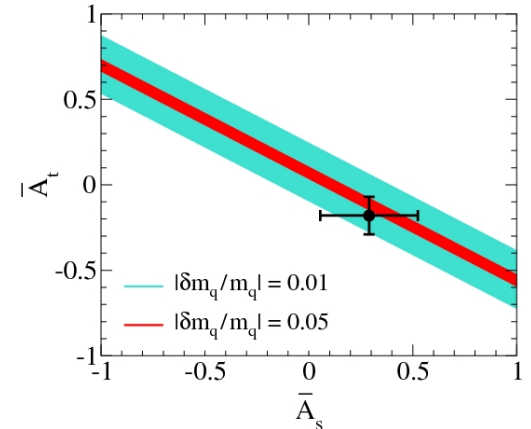
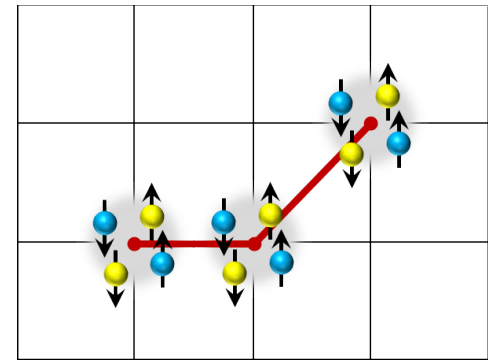
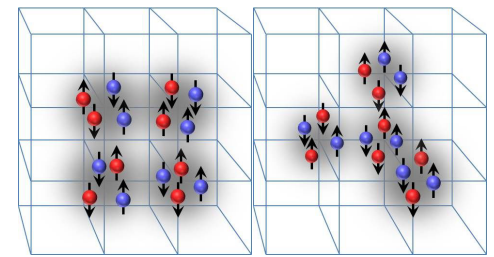
*Nuclear Lattice Effective Field Theory - An Introduction*  
Springer Lecture Notes in Physics **957** (2019) 1 - 396

- Computational equipment



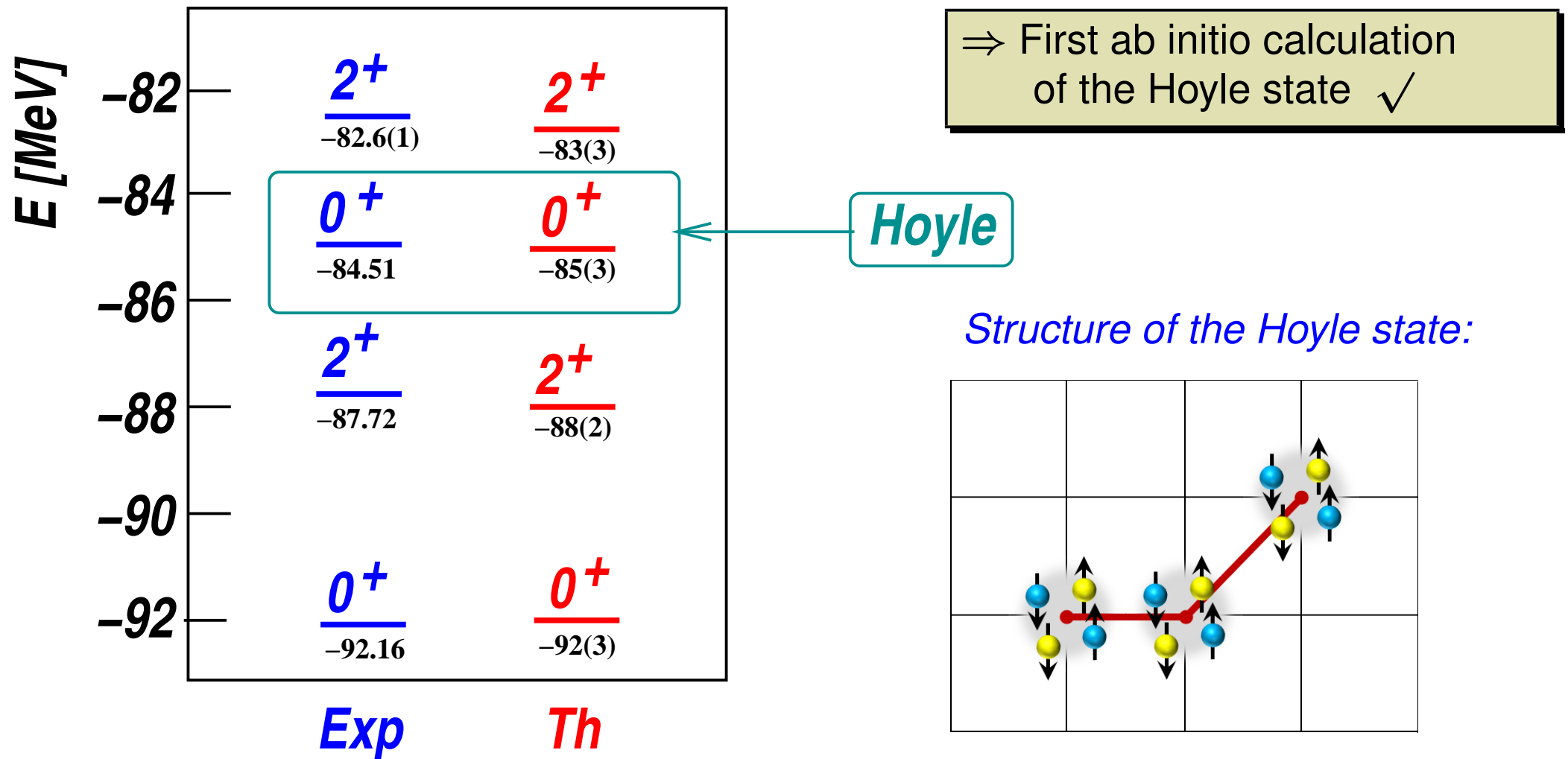
# Early results from NLEFT: Validation

- Lattice EFT calculations for  $A=3,4,6,12$  nuclei, [PRL 104 \(2010\) 142501](#)
- *Ab initio* calculation of the Hoyle state, [PRL 106 \(2011\) 192501](#)
- Structure and rotations of the Hoyle state, [PRL 109 \(2012\) 142501](#)
- Validity of Carbon-Based Life as a Function of the Light Quark Mass  
[PRL 110 \(2013\) 142501](#)
- *Ab initio* calculation of the Spectrum and Structure of  $^{16}\text{O}$ ,  
[PRL 112 \(2014\) 142501](#)
- Lattice effective field theory for medium-mass nuclei, [PLB 732 \(2014\) 110](#)
- *Ab initio* alpha-alpha scattering, [Nature 528 \(2015\) 111](#)
- Nuclear Binding Near a Quantum Phase Transition, [PRL 117 \(2016\) 132501](#)
- *Ab initio* calculations of the isotopic dependence of nuclear clustering,  
[PRL 119 \(2017\) 222505](#) and much more ...



# The spectrum of carbon-12 A.D. 2011

- After  $8 \cdot 10^6$  hrs JUGENE/JUQUEEN (and “some” human work)



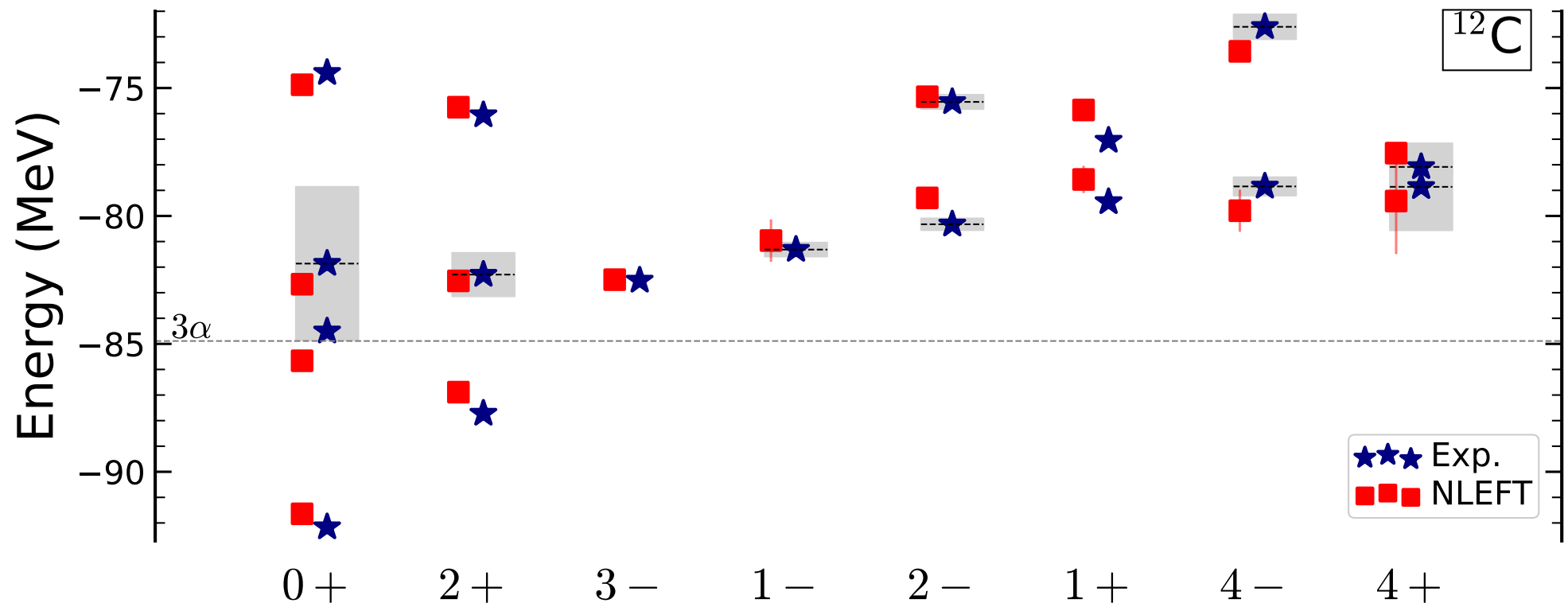
Epelbaum, Krebs, Lee, UGM, Phys. Rev. Lett. **106** (2011) 192501

Epelbaum, Krebs, Lähde, Lee, UGM, Phys. Rev. Lett. **109** (2012) 252501

# The spectrum of carbon-12 A.D. 2023

- with much improved algorithms and methods:

Shen, Lähde, Lee, UGM, Nature Commun. **14** (2023) 2777



→ solidifies earlier NLEFT statements about the structure of the  $0_2^+$  and  $2_2^+$  states

# Pion mass dependence from MC simulations

- Consider pion mass changes as *small perturbations* for an energy (difference)  $E_i$

$$\left. \frac{\partial E_i}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} = \left. \frac{\partial E_i}{\partial M_\pi^{\text{OPE}}} \right|_{M_\pi^{\text{phys}}} + x_1 \left. \frac{\partial E_i}{\partial m_N} \right|_{m_N^{\text{phys}}} + x_2 \left. \frac{\partial E_i}{\partial g_{\pi N}} \right|_{g_{\pi N}^{\text{phys}}} \\ + x_3 \left. \frac{\partial E_i}{\partial C_0} \right|_{C_0^{\text{phys}}} + x_4 \left. \frac{\partial E_i}{\partial C_I} \right|_{C_I^{\text{phys}}}$$

with

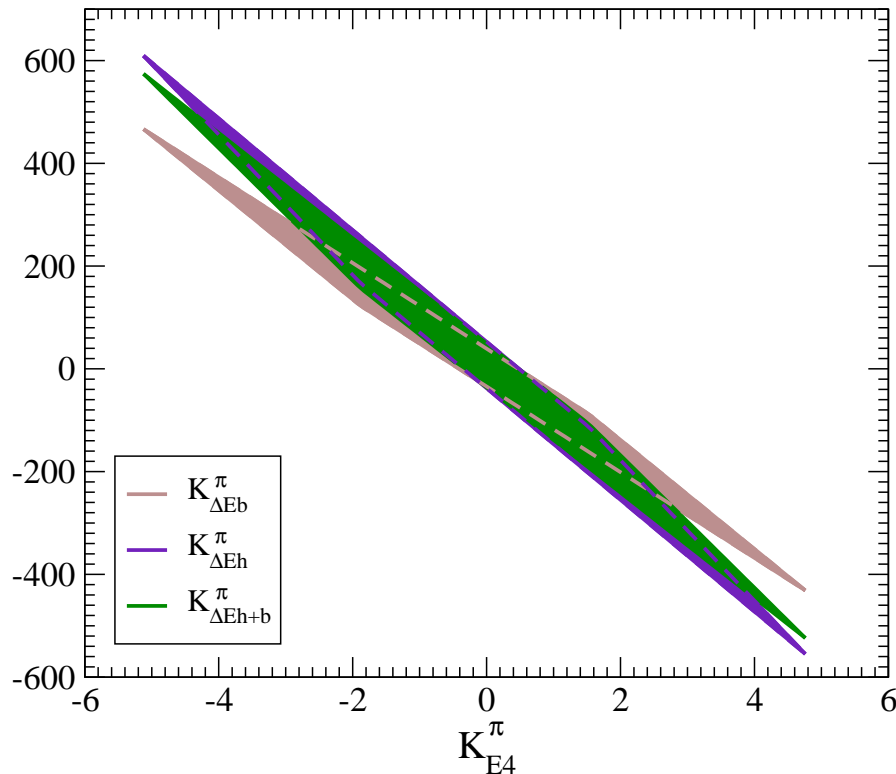
$$x_1 \equiv \left. \frac{\partial m_N}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}}, \quad x_2 \equiv \left. \frac{\partial g_{\pi N}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}}, \quad x_3 \equiv \left. \frac{\partial C_0}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}}, \quad x_4 \equiv \left. \frac{\partial C_I}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}}$$

⇒ problem reduces to the calculation of the various derivatives using AFQMC and the determination of the  $x_i$

- $x_1$  and  $x_2$  can be obtained from LQCD plus CHPT
- $x_3$  and  $x_4$  can be obtained from NN scattering and its  $M_\pi$ -dependence →  $\bar{A}_{s,t}$

# Correlations

- vary the quark mass derivatives of  $\bar{A}_{s,t} = \partial a_{s,t}^{-1} / \partial M_\pi |_{M_\pi^{\text{phys}}}$  within  $-1, \dots, +1$ :



$$\Delta E_b = E(^8\text{Be}) - 2E(^4\text{He})$$

$$\Delta E_h = E(^{12}\text{C}^*) - E(^8\text{Be}) - E(^4\text{He})$$

$$\Delta E_{h+b} = E(^{12}\text{C}^*) - 3E(^4\text{He})$$

$$\frac{\partial O_H}{\partial M_\pi} = K_H^\pi \frac{O_H}{M_\pi}$$

- clear correlations: the two fine-tunings are not independent

⇒ has been speculated before but could not be calculated

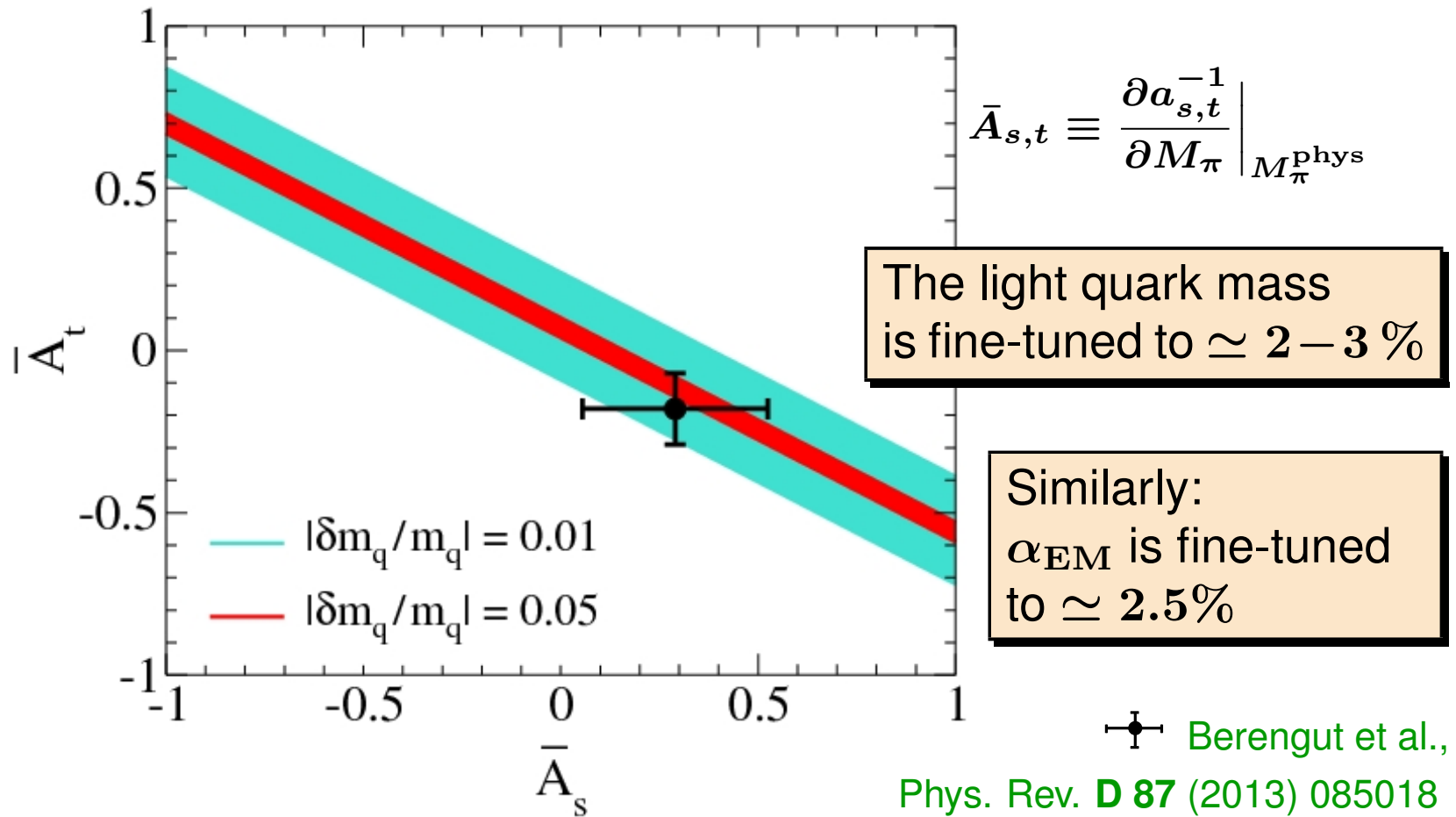
Weinberg (2001)

# The end-of-the-world plot I

- $|\delta(\Delta E_{h+b})| < 100 \text{ keV}$

Oberhummer et al., Science (2000)

$$\rightarrow \left| \left( 0.571(14)\bar{A}_s + 0.934(11)\bar{A}_t - 0.069(6) \right) \frac{\delta m_q}{m_q} \right| < 0.0015$$



# An update on fine-tunings in the triple-alpha process <sup>28</sup>

Lähde, UGM, Epelbaum, Eur. Phys. J A 56 (2020) 89

- Use lattice data to determine  $\bar{A}_s$  and  $\bar{A}_t$  and NN LETs Baru et al., Phys. Rev. C 92 (2015) 014001

$$\bar{A}_s = 0.54(24), \quad \bar{A}_t = 0.33(16)$$

↪  $\bar{A}_s$  is consistent w/ earlier determination

↪  $\bar{A}_t$  changes sign compared to earlier determination

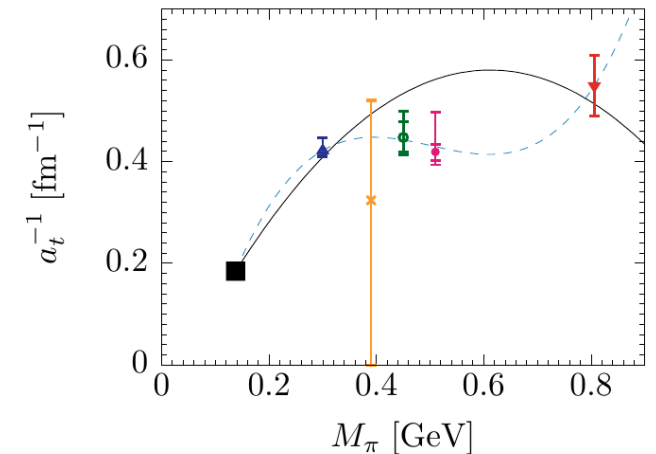
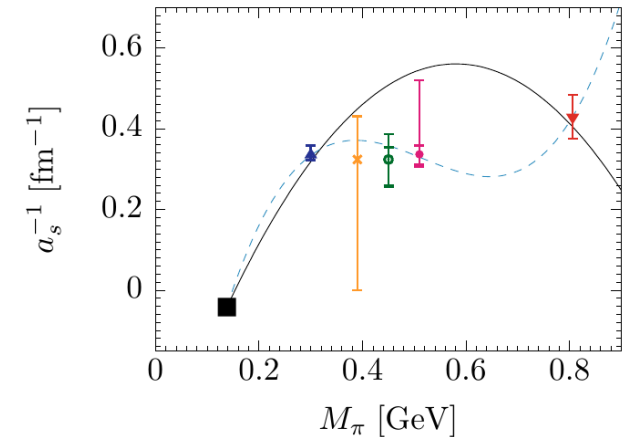
- update  $x_1$  and  $x_2$  using better LQCD data:

$$x_1 = 0.84(7), \quad x_2 = -0.053(16)$$

↪  $x_1$  and  $x_2$  more precise

↪  $x_2$  now has a definite sign

⇒ update end-of-the-world plot



Beane et al. (2012)  
Yamazaki et al. (2015)  
Orginos et al. (2015)  
Beane et al. (2013)  
Yamazaki et al. (2012)

# New end-of-the-world plots

- Improved simulations of carbon and oxygen generation in massive stars  
 → constraints now depend on  $Z$ ,  
 the nucleus and the sign of  $\delta m_q$

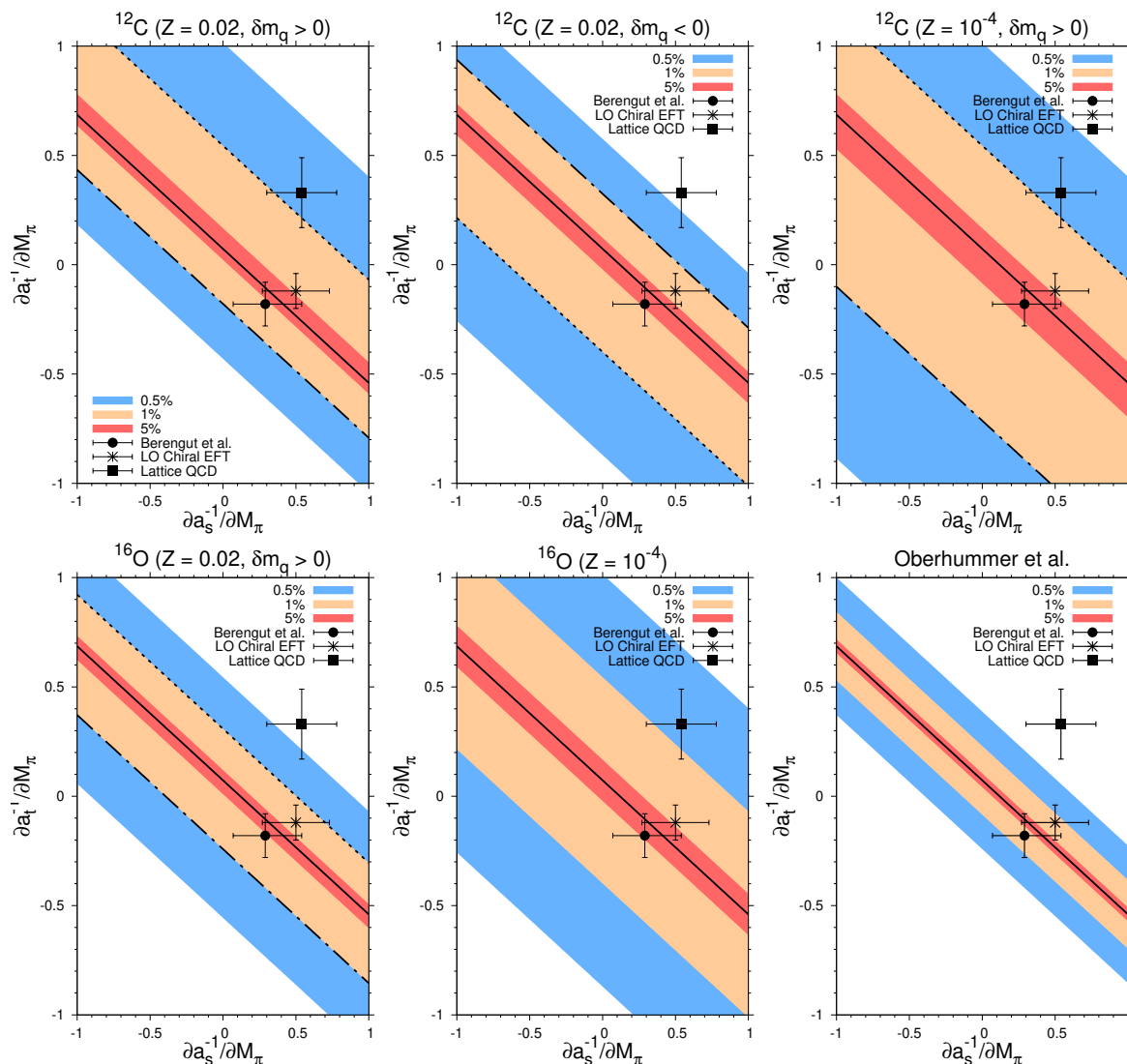
Huang, Adams, Grohs,  
 Astropart. Phys. 105 (2019) 13

- lattice values for  $\bar{A}_{s,t}$ :

The light quark mass is fine-tuned to  $\simeq 0.5\%$

- Bound on  $\alpha_{EM}$  softened ( $\sim 7.5\%$ )

⇒ need better determinations of  $\bar{A}_{s,t}$   
 from lattice QCD with pion masses closer to the physical point!



# A dose of philosophy: The anthropic principle

# Anthropic principle

- The anthropic principle:

“The observed values of all physical and cosmological quantities are not equally probable but they take on values restricted by the requirement that there exist sites where carbon-based life can evolve and by the requirements that the universe be old enough for it to have already done so.”

Carter 1974, Barrow & Tipler 1988, ...

⇒ does this lead to physical/testable consequences?

# Some examples of anthropic reasoning

VOLUME 59, NUMBER 22

PHYSICAL REVIEW LETTERS

30 NOVEMBER 1

## Anthropic Bound on the Cosmological Constant

Steven Weinberg

*Theory Group, Department of Physics, University of Texas, Austin, Texas 78712*  
(Received 5 August 1987)

In recent cosmological models, there is an “anthropic” upper bound on the cosmological constant  $\Lambda$ . It is argued here that in universes that do not recollapse, the only such bound on  $\Lambda$  is that it should not be so large as to prevent the formation of gravitationally bound states. It turns out that the bound is quite large. A cosmological constant that is within 1 or 2 orders of magnitude of its upper bound would help with the missing-mass and age problems, but may be ruled out by galaxy number counts. If so, we may conclude that anthropic considerations do not explain the smallness of the cosmological constant.

1137 citations

Nature Vol. 278 12 April 1979

605

## review article

### The anthropic principle and the structure of the physical world

B. J. Carr\* &amp; M. J. Rees

Institute of Astronomy, Madingley Road, Cambridge, UK

*The basic features of galaxies, stars, planets and the everyday world are essentially determined by a few microphysical constants and by the effects of gravitation. Many interrelations between different scales that at first sight seem surprising are straightforward consequences of simple physical arguments. But several aspects of our Universe—some of which seem to be prerequisites for the evolution of any form of life—depend rather delicately on apparent ‘coincidences’ among the physical constants.*

arXiv:hep-th/0302219v1 27 Feb 2003

## The Anthropic Landscape of String Theory

L. Susskind

Department of Physics  
Stanford University  
Stanford, CA 94305-4060

### Abstract

In this lecture I make some educated guesses, about the landscape of string theory vacua. Based on the recent work of a number of authors, it seems plausible that the landscape is unimaginably large and diverse. Whether we like it or not, this is the kind of behavior that gives credence to the Anthropic Principle. I discuss the theoretical and conceptual issues that arise in developing a cosmology based on the diversity of environments implicit in string theory.

1189 citations

PHYSICAL REVIEW D

VOLUME 57, NUMBER 9

1 MAY 1998

### Viable range of the mass scale of the standard model

V. Agrawal,<sup>1</sup> S. M. Barr,<sup>1</sup> John F. Donoghue,<sup>2</sup> and D. Seckel<sup>1</sup><sup>1</sup>*Bartol Research Institute, University of Delaware, Newark, Delaware 19716*<sup>2</sup>*Department of Physics and Astronomy, University of Massachusetts, Amherst, Massachusetts 01003*

(Received 30 July 1997; published 1 April 1998)

In theories in which different regions of the universe can have different values of certain physical parameters, we would naturally find ourselves in a region where they take values favorable for life. We explore the range of such viable values of the mass parameter in the Higgs potential,  $\mu^2$ . For  $\mu^2 < 0$ , the requirement that complex elements be formed suggests that the Higgs vacuum expectation value  $v$  must have a magnitude less than 5 times its observed value. For  $\mu^2 > 0$ , baryon stability requires that  $|\mu| \ll M_P$ , the Planck mass. Smaller values of  $|\mu^2|$  may or may not be allowed depending on issues of element synthesis and stellar evolution. We conclude that the observed value of  $\mu^2$  appears reasonably typical of the viable range, and a multiple-domain scenario may provide a plausible explanation for the closeness of the QCD scale and the weak scale.

[S0556-2821(98)05509-X]

# A prime example of the AP

- Hoyle (1953):

Prediction of an excited state in the carbon spectrum necessary to generate a sufficient amount of heavy elements ( $^{12}\text{C}$ ,  $^{16}\text{O}$ ,...) in stars

- was later heralded as the prime example for the AP:

“As far as we know, this is the only genuine anthropic principle prediction”

Carr & Rees 1989

“In 1953 Hoyle made an anthropic prediction on an excited state – ‘level of life’ – for carbon production in stars”

Linde 2007

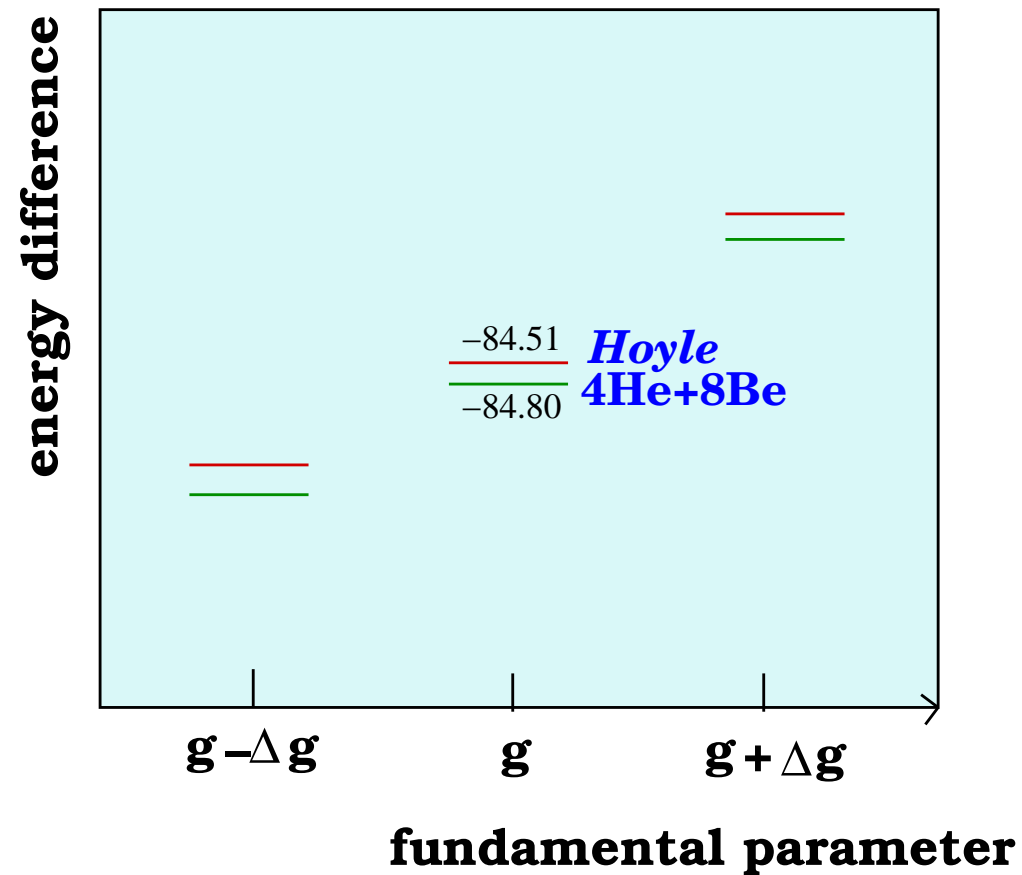
“A prototype example of this kind of anthropic reasoning was provided by Fred Hoyle’s observation of the triple alpha process...”

Carter 2006

⇒ can we find out / test whether this is true?

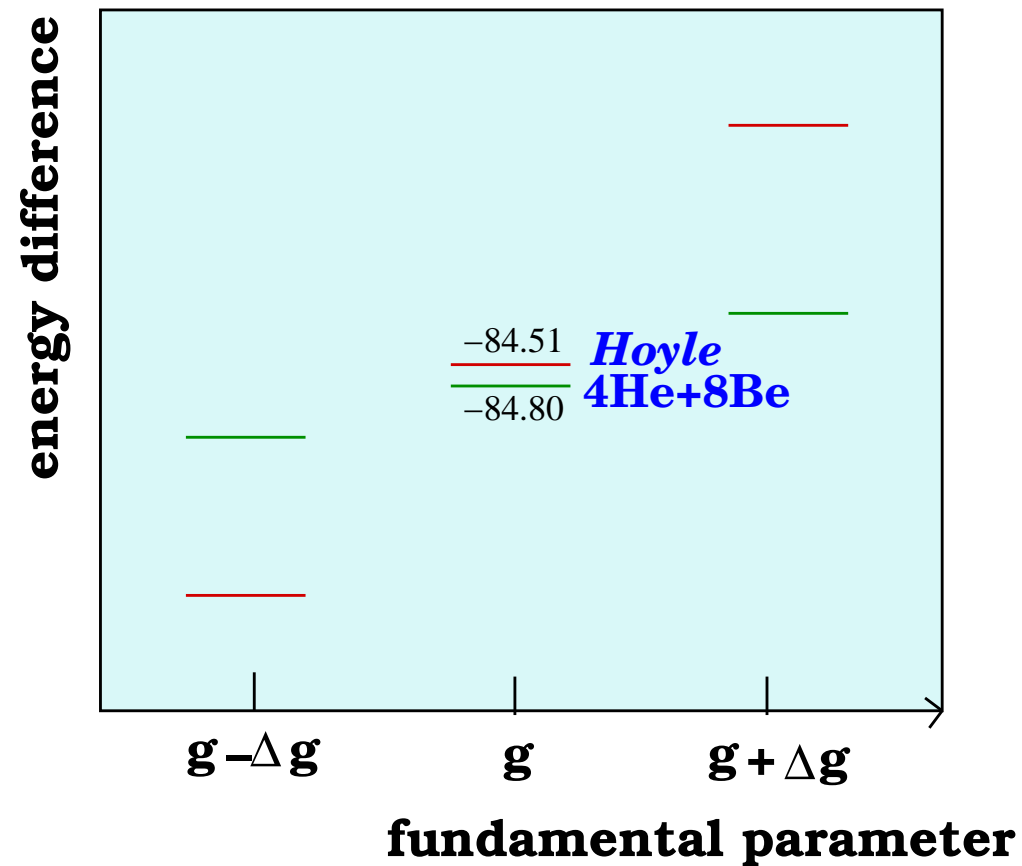
# The non-anthropropic scenario

- Weinberg's assumption: The Hoyle state stays close to the  $4\text{He}+8\text{Be}$  threshold



# The anthropic scenario

- The AP strikes back: The Hoyle state quickly moves away from the  $4\text{He}+8\text{Be}$  threshold



# AP at work

- Our calculations support the anthropic scenario:

$$E_R = E(^{12}\text{C}^*) - 3E(^4\text{He}) = 379.47 \text{ keV} + \boxed{C} \frac{dm_q}{m_q} [\%] \text{ keV}$$

$$\Delta E_h = E(^{12}\text{C}^*) - E(^8\text{Be}) - E(^4\text{He}) = 289 \text{ keV} + \boxed{0.8 C} \frac{dm_q}{m_q} [\%] \text{ keV}$$

- $C$  depends on the precise values of  $\bar{A}_{s,t}$ , here  $C = -372$  (from LQCD+LETs)
- there is one combination of  $\bar{A}_s$  and  $\bar{A}_t$ , where  $C = 0$ 
  - ↪ no more quark mass dependence
  - ↪ does not seem to be realized in Nature (not yet entirely excluded)

# How fine-tuned is the holy grail of nuclear astrophysics?

UGM, Metsch, Meyer, arXiv:2601.11180 [nucl-th]

# The holy grail of nuclear astrophysics

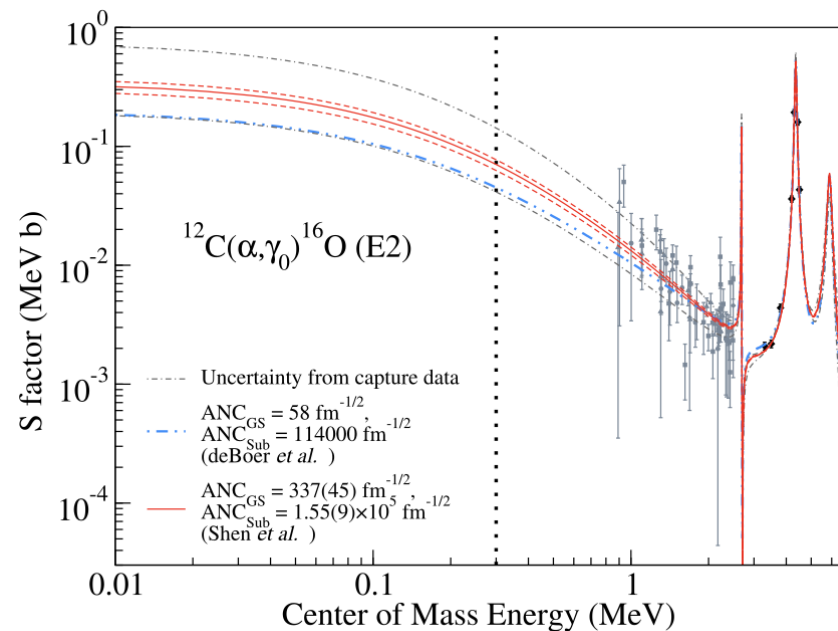
- The holy grail:  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$  at astrophysical energies,  $E_G \simeq 0.3$  MeV

- S-factor

$$S(E) = \sigma(E)E \exp(2\pi k_C/p)$$

$$k_C = Z_1 Z_2 \alpha \mu, \quad E = p^2/2\mu$$

$$\mu = m_1 m_2 / (m_1 + m_2)$$



de Boer *et al.*, *Eur. Phys. J. A* **61** (2025) 70

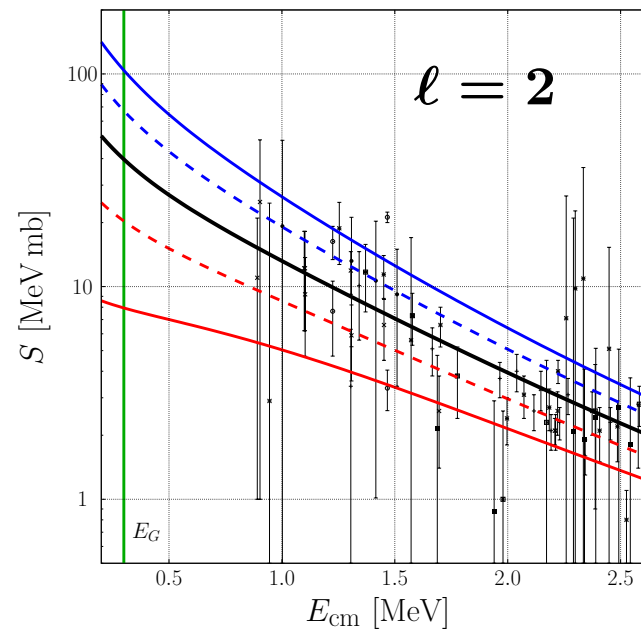
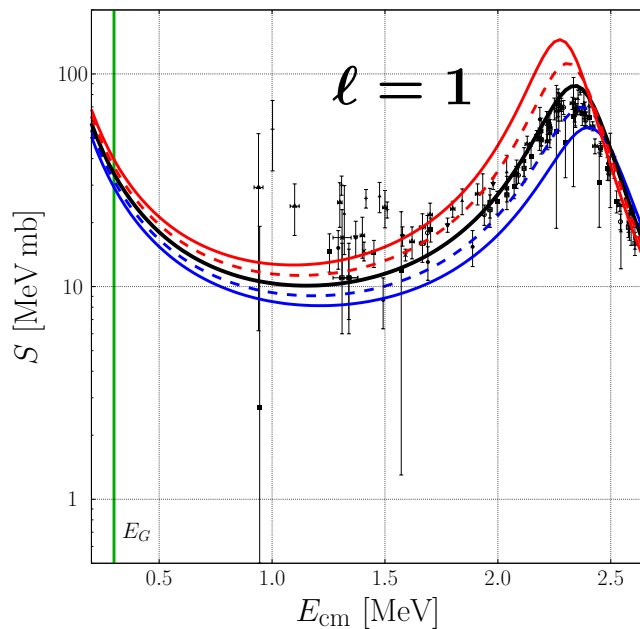
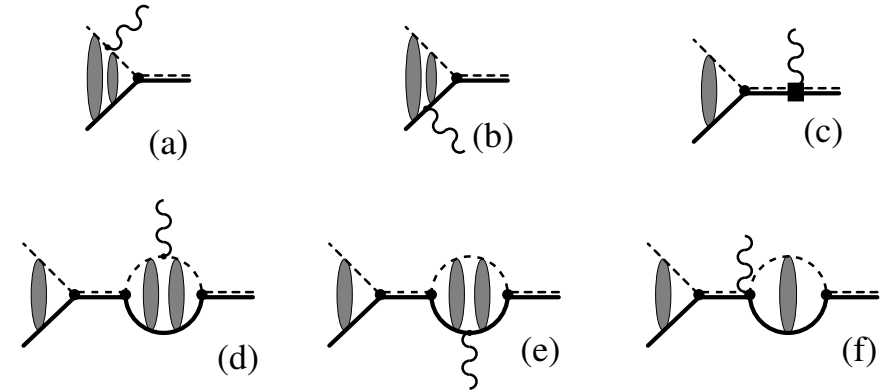
↪ need theory to extrapolate to the Gamov energy

↪ still large uncertainties at the Gamov energy

↪ can we investigate the  $\alpha$  dependence of this reaction?

# Fine-tunings in the holy grail of nuclear astrophysics

- Use cluster EFT ( $\alpha$ ,  $^{12}\text{C}$ ,  $^{16}\text{O}$ )  
Ando, Nucl. Phys. A **1060** (2025) 123108
- Consider  $E1$  and  $E2$  transitions
- $\alpha$  appears at many places (Coulomb ladders)



$\Rightarrow$  extremely fine-tuned!

$$\left| \frac{\delta\alpha}{\alpha} \right| < 0.2 \text{ per mille}$$

- Instead

Eur. Phys. J. A (2025) 61:122  
https://doi.org/10.1140/epja/s10050-025-01587-5

THE EUROPEAN  
PHYSICAL JOURNAL A



Invited Viewpoint and Perspective

## Fine-tunings in nucleosynthesis and the emergence of life: status and perspectives

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Communicated by Thomas Duguet

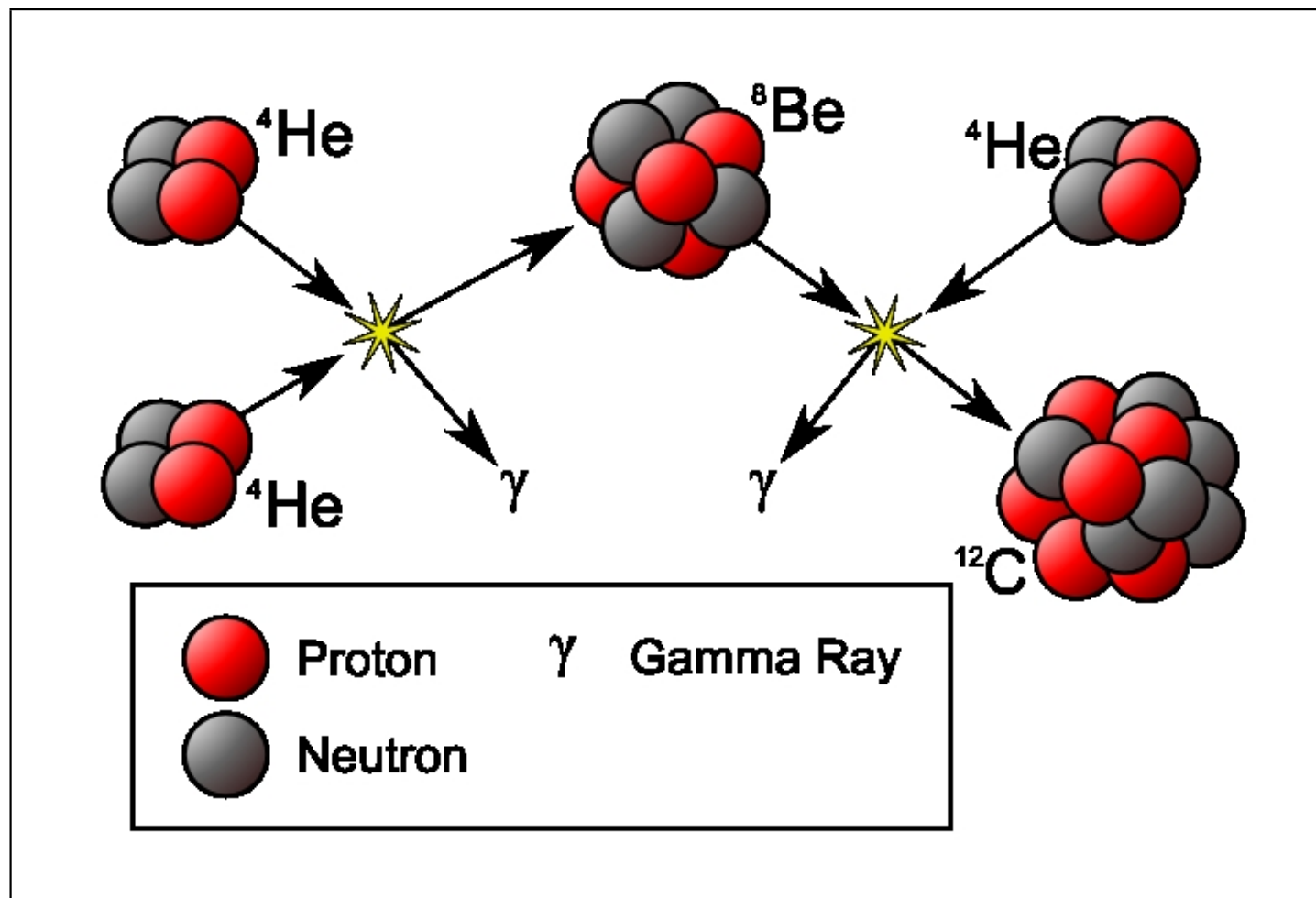
**Abstract** We discuss the fine-tunings of nuclear reactions in the Big Bang and in stars and draw some conclusions on the emergence of the light elements and the life-relevant elements carbon and oxygen. We also stress how to improve these calculations in the future. This requires a concerted effort of different communities, especially in nuclear reaction theory, lattice QCD for few-nucleon systems, stellar evolution calculations, particle physics and philosophy.

Bang and in stars – that is why one often says that we are made of stardust. Of particular relevance are the  $^{12}\text{C}$  and  $^{16}\text{O}$  nuclei, which form the basis of the life on Earth as we know it. These elements are generated in hot, old stars through the triple-alpha process and the radiative capture process  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ , respectively. Both  $^{12}\text{C}$  and  $^{16}\text{O}$  are alpha-type nuclei, that is to a good approximation they can be described as bound states of three, respectively four,  $^4\text{He}$  particles.  $^4\text{He}$  is already generated abundantly shortly after the Big Bang,

# SPARES

# Carbon nucleosynthesis

- Carbon is generated through the fusion of 3 helium nuclei (alpha-particles)



@ Wikipedia

# The electromagnetic fine-structure constant in primordial nucleosynthesis revisited

UGM, Metsch, Meyer, Eur. Phys. J. A **59** (2023) 223 [2305.15849 [hep-th]]



# Nuclear reaction rates: Coulomb barrier

- Reminder:

$$\gamma_{ab \rightarrow cd}(T) = \langle \sigma v \rangle \propto \int_0^\infty dE \sigma_{ab \rightarrow cd}(E) \cdot E \cdot e^{-\frac{E}{k_B T}}$$

$$E = \frac{1}{2} \mu_{ab} v^2$$

$$\mu_{ab} = \frac{m_a m_b}{m_a + m_b}$$

- Coulomb barrier

↪ The cross section is proportional to the penetration factor (in/out)

$$\sigma \propto v_0 = \frac{2\pi\eta}{e^{2\pi\eta} - 1}$$

with the Sommerfeld parameter

$$\eta = \frac{Z_a Z_b \alpha_{EM} c}{\hbar v} = \frac{1}{2\pi} \sqrt{E_G / E}$$

and the Gamow energy

$$E_G = 2\pi^2 Z_a^2 Z_b^2 \alpha_{EM}^2 \mu_{ab} c^2$$

# Nuclear reaction rates: Radiative capture

- Coupling  $\propto e \rightarrow$  cross section  $\sigma \propto e^2 \propto \alpha_{\text{EM}}$
- Capture processes are peripheral  $\rightarrow$  parameterized in  $f(\delta\alpha_{\text{EM}}) \simeq 1$

Nollett, Lopez (2002)

- Assume dipole dominance
- For the leading  $np \rightarrow d\gamma$  reactions use again EFT formalism

Rupak (2000)

$\Rightarrow$   $\alpha$ -dependence of cross sections ( $q_\gamma = 1$  for radiative capture, 0 else)

$$\sigma(\alpha_{\text{EM}}, E) \propto \left( \frac{\sqrt{E_G^{\text{in}}/E}}{e\sqrt{E_G^{\text{in}}/E} - 1} \right) \cdot \left( \frac{\sqrt{E_G^{\text{in}}/(E+Q)}}{e\sqrt{E_G^{\text{in}}/(E+Q)} - 1} \right) \cdot (\alpha_{\text{EM}} f(\delta\alpha_{\text{EM}}))^{q_\gamma}$$

with  $Q = m_a + m_b - m_c - m_d$

$\hookrightarrow$  penetration factors must be modified in there is a neutron in the initial and/or final state

$\hookrightarrow$  for details, see UGM, Metsch, Meyer (2023)

# Weak decay rates

- $\beta$ -decay rate in terms of the Fermi function

Segrè (1964)

$$\lambda = \frac{G_F^2 |\mathcal{M}_{fi}|^2}{2\pi^3 c^3 \hbar^7} \underbrace{\int_0^{p_{e,\max}} \left( W - \sqrt{m_e^2 c^4 + p_e^2 c^2} \right)^2 F(Z, \alpha, p_e) p_e^2 dp_e}_{=f(\alpha, Q)}$$

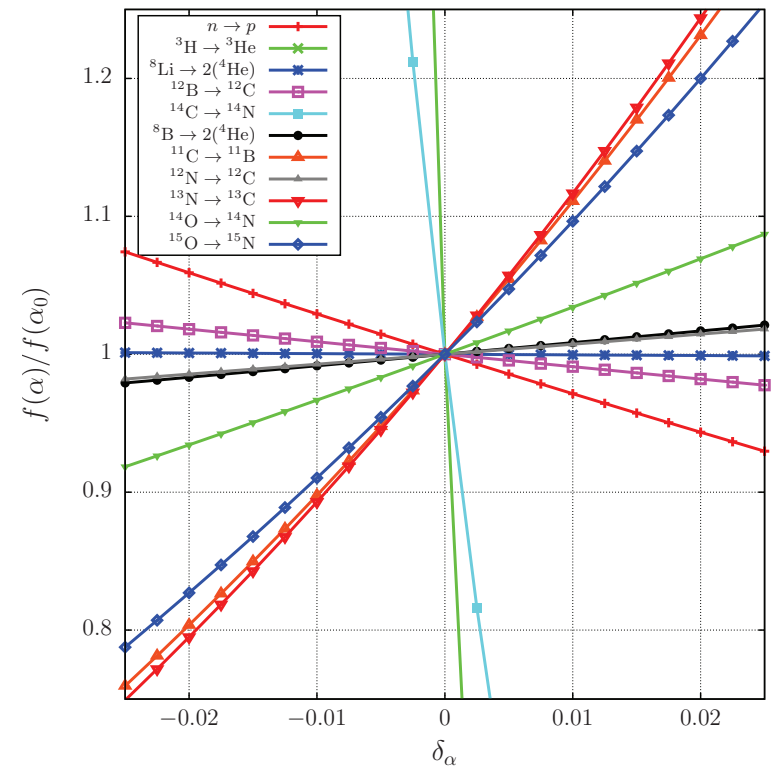
$$p_{e,\max} = \frac{1}{c} \sqrt{W^2 - m_e^2 c^4}, \quad W \simeq m_a - m_b = Q$$

- Fermi function (for  $Z\alpha \ll 1$ ):

$$F(\pm Z, \alpha, \epsilon_e) \simeq \frac{\pm 2\pi\nu}{1 - \exp(\mp 2\pi\nu)}, \quad \nu = \frac{Z\alpha\epsilon_e}{\sqrt{\epsilon_e^2 - 1}}$$

↪  $\alpha$ -dependent rates:

$$\lambda(\alpha) = \lambda(\alpha_0) \frac{f(\alpha, Q)}{f(\alpha_0, Q)}$$



# Neutron decay and $n \leftrightarrow p$ rates

- Consider free neutron decay:

$$\tau_n(\alpha) = \tau_n(\alpha_0) \frac{f(\alpha, Q)}{f(\alpha_0, Q)}$$

- But this ignores the Fermi-Dirac distribution of the neutrino and the electron

⇒ strong  $T$ -dependence in the  $\alpha$ -variation for high  $T$

- $Q_n = m_n - m_p$  has a QED contribution, use the new value:

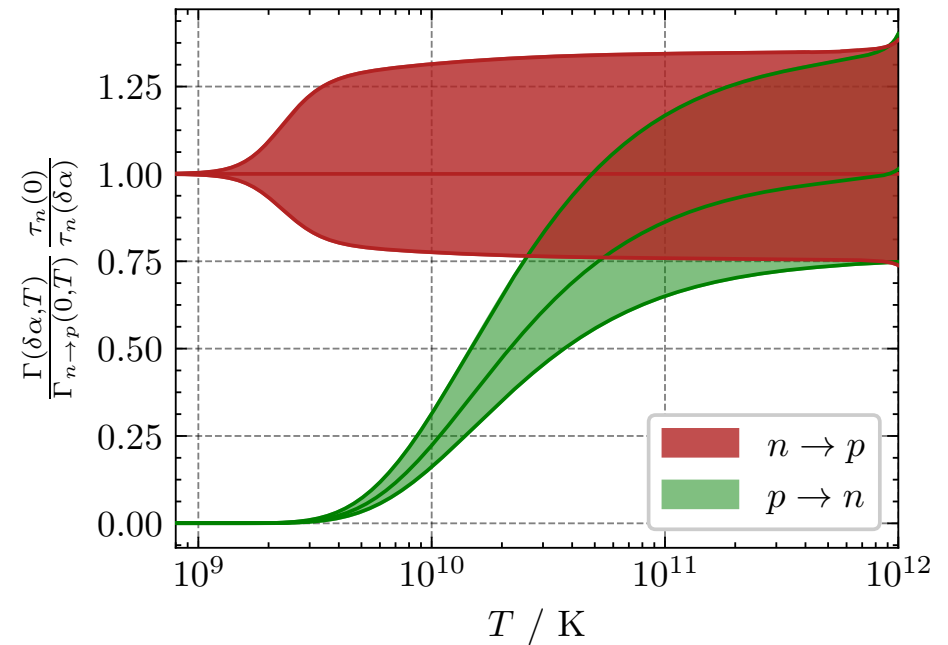
$$\Delta Q_n = Q_n^{\text{QED}} \cdot \delta\alpha = -0.58(16) \text{ MeV} \cdot \delta\alpha$$

Gasser et al. (2021)

↔ affects the weak  $n \leftrightarrow p$  rates →  $^4\text{He}$  abundance very sensitive

↔ affects the  $Q$ -values of the  $\beta$ -decays

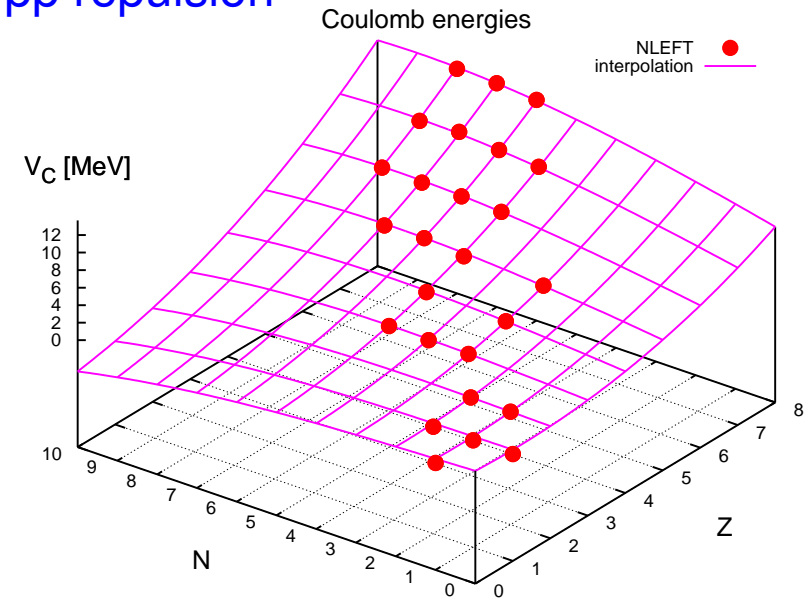
↔  $\alpha$ -dependence of  $m_N = (m_p + m_n)/2$  in  $np \rightarrow d\gamma$  can be neglected



# Indirect effects – binding energies

- EM (Coulomb) contributions to nuclear BEs from pp repulsion
  - calculated in NLEFT Elhatisari et al., Nature 630 (2024) 59
- ↪ change in  $Q$ -values

$$\Delta Q = \delta\alpha \left( -\sum_i B_C^i + \sum_j B_C^j \right)$$



⇒ Nuclear reaction cross sections:

$$\sigma(E, \alpha) \propto \underbrace{(E + Q(\alpha))^{p_\gamma}}_{\text{phase space}} \alpha^{q_\gamma} \frac{\sqrt{E_G^{\text{in}}/E}}{\exp\left(\sqrt{E_G^{\text{in}}/E}\right) - 1} \frac{\sqrt{E_G^{\text{out}}/(E + Q(\alpha))}}{\exp\left(\sqrt{E_G^{\text{out}}/(E + Q(\alpha))}\right) - 1}$$

$$p_\gamma = 3, \quad q_\gamma = 1 \quad \text{for radiative capture}$$

$$p_\gamma = 1/2, \quad q_\gamma = 0 \quad \text{for other reactions}$$

# Comparison to earlier works

- Compare the coefficient  $a$  for various codes and earlier works

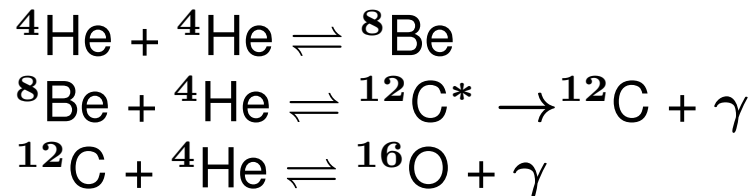
Code/work	$d$	${}^3\text{H}+{}^3\text{He}$	${}^4\text{He}$	${}^6\text{Li}$	${}^7\text{Li}+{}^7\text{Be}$
PRIMAT	3.658	3.534	1.408	6.953	-4.302
AlterBBN	3.644	3.526	1.373	6.856	-4.322
Dent et al. (2007)	3.612	0.948	1.898	6.681	-11.307
Nollett et al. (2002)	3.993	1.033	–	–	-9.296
Bergstoem et al. (2002)	5.129	0.778	1.956	–	-13.619

- largest differences in  ${}^3\text{H}+{}^3\text{He}$  (unmeasured) and  ${}^7\text{Li}+{}^7\text{Be}$  (Li problem)
- Our bounds are stronger due to:
  - ↪ updated experimental values for masses, constants, ..., smaller  $Q_n^{\text{QED}}$
  - ↪ different reaction rates due to cross section parametrizations
  - ↪ calculating the corrections exactly or using  $T$ -dependent approximations

# A SHORT HISTORY of the HOYLE STATE

- Heavy element generation in massive stars: **triple- $\alpha$  process**

Bethe 1938, Öpik 1952, Salpeter 1952, Hoyle 1954, . . .

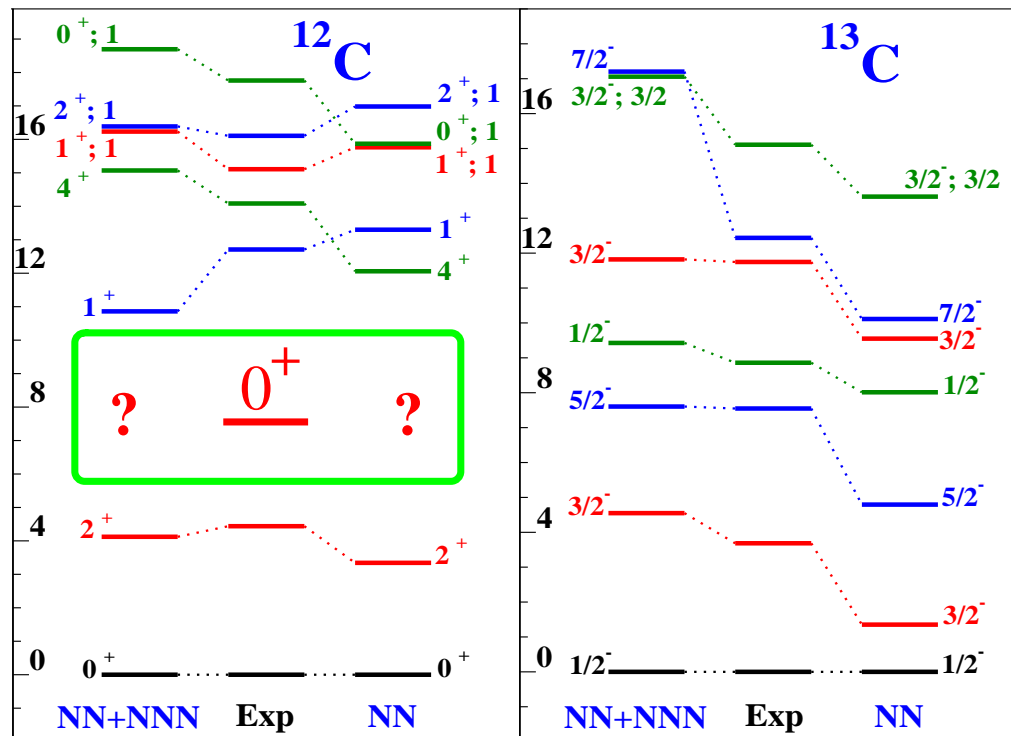


- Hoyle's contribution: calculation of relative abundances of  ${}^4\text{He}$ ,  ${}^{12}\text{C}$  and  ${}^{16}\text{O}$ 
  - $\Rightarrow$  need a resonance close to the  ${}^8\text{Be} + {}^4\text{He}$  threshold at  $E_R = 0.35$  MeV
  - $\Rightarrow$  this corresponds to a  $J^P = 0^+$  excited state 7.7 MeV above the g.s.
- a corresponding state was experimentally confirmed at Caltech at
  - $E - E(\text{g.s.}) = 7.653 \pm 0.008$  MeV Dunbar et al. 1953, Cook et al. 1957
- still on-going experimental activity, e.g. EM transitions at SDALINAC
  - M. Chernykh et al., Phys. Rev. Lett. 98 (2007) 032501
- and how about theory ?  $\rightarrow$  this talk
- side remark: NOT driven by anthropic considerations
  - H. Kragh, Arch. Hist. Exact Sci. 64 (2010) 721

# AN ENIGMA for NUCLEAR THEORY

- Ab initio calculation in the no-core shell model:  $\approx 10^7$  CPU hrs on JAGUAR

P. Navratil et al., Phys. Rev. Lett. **99** (2007) 042501; R. Roth et al., Phys. Rev. Lett. **107** (2011) 072501



$\Rightarrow$  excellent description, but no trace of the Hoyle state

# RESULTS for HEAVIER NUCLEI

- calculate BBN response matrix of primordial abundances  $Y_a$  at fixed baryon/photon ratio :

$$\frac{\delta \ln Y_a}{\delta \ln m_q} = \sum_{X_i} \frac{\partial \ln Y_a}{\partial \ln X_i} K_{X_i}^q$$

⇒

$X$	d	${}^3\text{He}$	${}^4\text{He}$	${}^6\text{Li}$	${}^7\text{Li}$
$a_s$	-0.39	0.17	0.01	-0.38	2.64
$B_{\text{deut}}$	-2.91	-2.08	0.67	-6.57	9.44
$B_{\text{trit}}$	-0.27	-2.36	0.01	-0.26	-3.84
$B_{{}^3\text{He}}$	-2.38	3.85	0.01	-5.72	-8.27
$B_{{}^4\text{He}}$	-0.03	-0.84	0.00	-69.8	-57.4
$B_{{}^6\text{Li}}$	0.00	0.00	0.00	78.9	0.00
$B_{{}^7\text{Li}}$	0.03	0.01	0.00	0.02	-25.1
$B_{{}^7\text{Be}}$	0.00	0.00	0.00	0.00	99.1
$\tau$	0.41	0.14	0.72	1.36	0.43

updated Kawano code

Kawano, FERMILAB-Pub-92/04-A

# RESULTS

- putting pieces together:

$$\left. \frac{\partial \Delta E_h}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} = -0.455(35) \left. \frac{\partial a_s^{-1}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} - 0.744(24) \left. \frac{\partial a_t^{-1}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} + 0.056(10)$$

$$\left. \frac{\partial \Delta E_b}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} = -0.117(34) \left. \frac{\partial a_s^{-1}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} - 0.189(24) \left. \frac{\partial a_t^{-1}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} + 0.012(9)$$

- $x_1$  and  $x_2$  only affect the small constant terms
- also calculated the shifts of the individual energies (not shown here)

# INTERPRETATION

- $(\partial\Delta E_h/\partial M_\pi)/(\partial\Delta E_b/\partial M_\pi) \simeq 4$   
 $\Rightarrow \Delta E_h$  and  $\Delta E_b$  cannot be independently fine-tuned
- Within error bars,  $\partial\Delta E_h/\partial M_\pi$  &  $\partial\Delta E_b/\partial M_\pi$  appear unaffected by the choice of  $x_1$  and  $x_2 \rightarrow$  indication for  $\alpha$ -clustering
- the triple alpha process is controlled by :

$$\Delta E_{h+b} \equiv \Delta E_h + \Delta E_b = E_{12}^* - 3E_4$$

$$\left. \frac{\partial\Delta E_{h+b}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} = -0.571(14) \left. \frac{\partial a_s^{-1}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} - 0.934(11) \left. \frac{\partial a_t^{-1}}{\partial M_\pi} \right|_{M_\pi^{\text{phys}}} + 0.069(6)$$

$\Rightarrow$  quark mass dependence of the scattering lengths discussed earlier

# Probing nuclear observables via primordial nucleosynthesis

UGM, Metsch, Eur. Phys. J. A **58** (2022) 212 [arXiv:2208.12600 [nucl-th]]

# Variations of nuclear observables

- Study the nuclear abundances  $Y_i$  as a function of nuclear observables:
  - binding energies, scattering lengths, neutron lifetime, ...
- Use four different BBN codes to study the systematic error
  - ↪ only if this is small / controlled, it makes sense to look at variations of  $\alpha_{\text{EM}}$  etc.
- Nuclear reactions rates:  $\Gamma_{ab \rightarrow cd} = n_B \gamma_{ab \rightarrow cd}$ 
$$\gamma_{ab \rightarrow cd} = N_A \sqrt{\frac{8}{\pi \mu_{ab} (kT)^3}} \int_0^\infty dE E \sigma_{ab \rightarrow cd}(E) e^{-\frac{E}{kT}}$$
$$\mu_{ab} = m_a m_b / (m_a + m_b)$$
- Inverse reaction (with spin multiplicity  $g_i$ ):
$$\gamma_{cd \rightarrow ab}(T) = \left( \frac{\mu_{ab}}{\mu_{cd}} \right)^{\frac{3}{2}} \frac{g_a g_b}{g_c g_d} e^{-\frac{Q}{kT}} \gamma_{ab \rightarrow cd}(T)$$
- Consider now changes in the binding energies by  $\pm 1$  permille →  $Q$ -factors change

# Variations of the binding energies / Q-values

- Direct reactions  $a + b \rightarrow c + d$

$$\begin{aligned}\gamma_{ab \rightarrow cd}(\tilde{Q}; T) &\approx \gamma_{ab \rightarrow cd}(Q_0; T) + \sqrt{\frac{8}{\pi \mu_{ab} (kT)^3}} \int_0^\infty dE E \sigma(Q_0; E) \\ &\quad \times \left( \frac{\Delta Q}{2(Q_0 + E)} + \frac{\Delta Q \sqrt{E_G}}{2(Q_0 + E)^{\frac{3}{2}}} \right) e^{-\frac{E}{kT}} \\ &= \gamma_{ab \rightarrow cd}(Q_0; T) + \Delta\gamma(T)_{ab \rightarrow cd}\end{aligned}$$

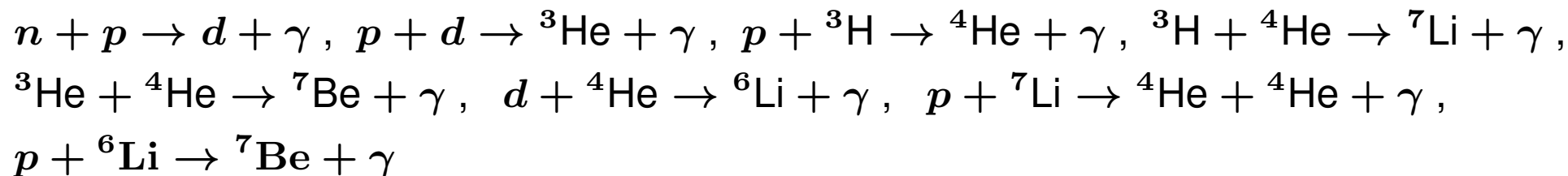
$$\tilde{Q} = Q_0 + \Delta Q \quad \text{change of the } Q\text{-value}$$

$$E_G = 2\pi^2 Z_c^2 Z_d^2 \alpha_{\text{EM}}^2 \mu_{cd} c^2 \quad \text{Gamov energy in the exit channel}$$

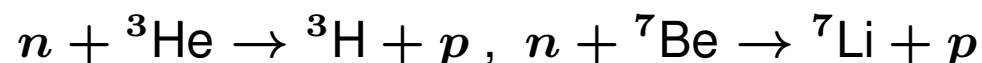
- In all earlier investigations, the  $T$ -dependence of  $\Delta\gamma(T)_{ab \rightarrow cd}$  was neglected
- Similar for radiative capture reactions  $a + b \rightarrow c + \gamma$   
and weak decay rates  $a \rightarrow b + e^\pm + \begin{pmatrix} - \\ \nu \end{pmatrix}$

# Reactions considered

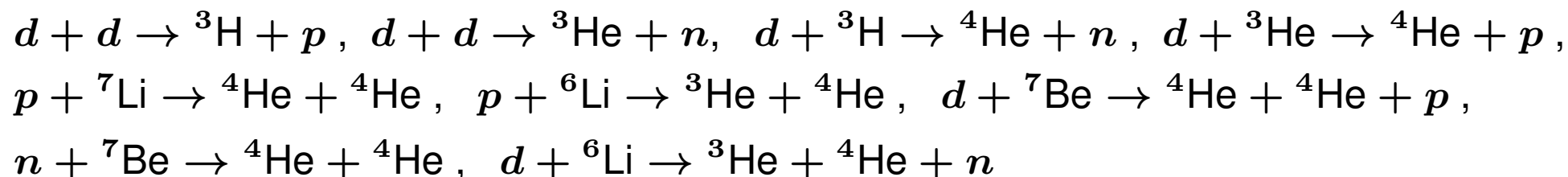
- Radiative capture reactions:



- Charge exchange reactions:

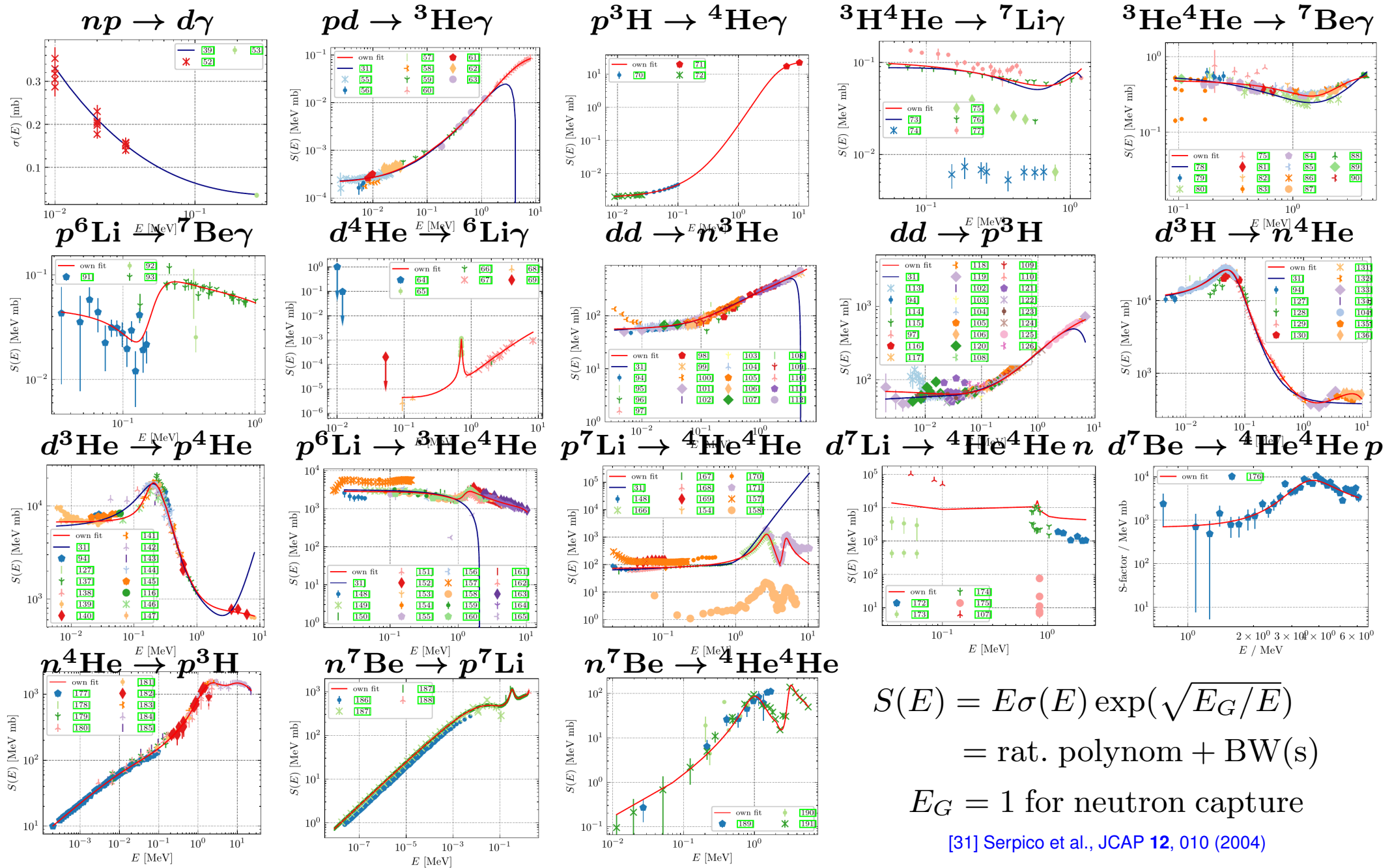


- Direct reactions:



- plus weak decays ....

# Reaction parameterizations

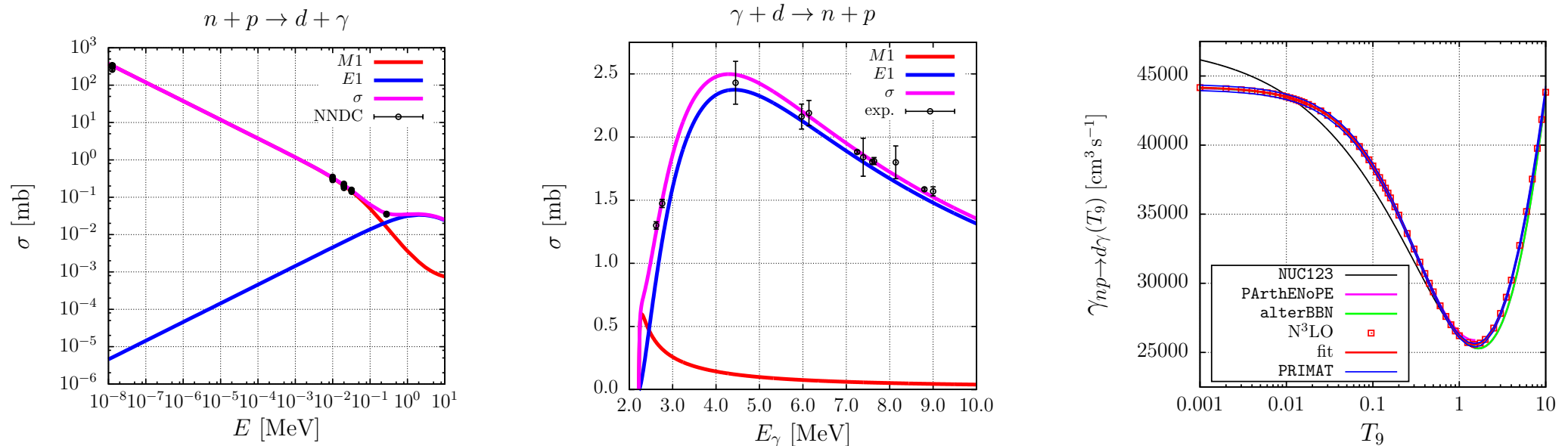


# The leading reaction $n + p \rightarrow d + \gamma$

- Use the pionless EFT description up to N<sup>3</sup>LO

Chen, Savage (1999), Rupak (2000)

$$\sigma_{np \rightarrow d\gamma}(E) = \frac{4\pi \alpha_{\text{EM}} (\gamma^2 + p^2)^3}{\gamma^3 m_n^4 p} \left[ |\chi_{M1}|^2 + |\chi_{E1}|^2 \right], \quad \chi_{E1, M1} = f(a_s, B_d)$$

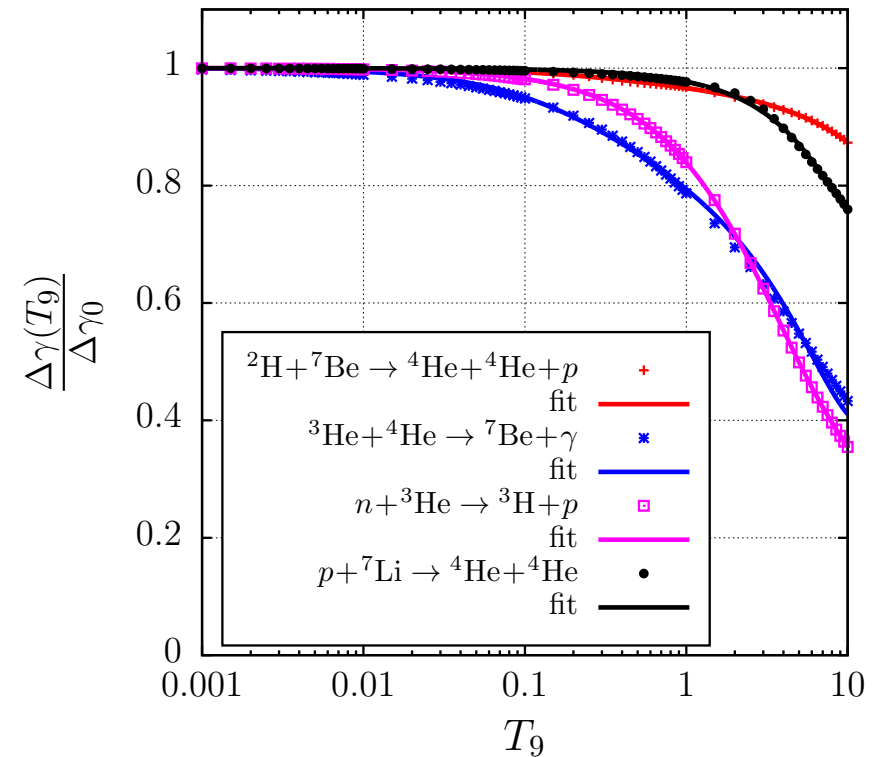
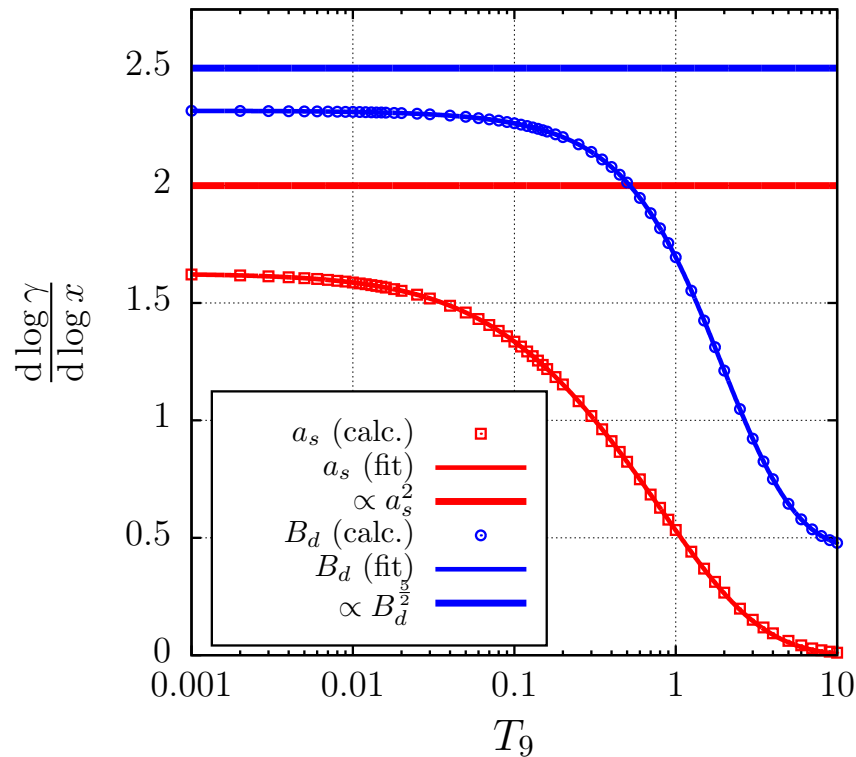


- $M1$  dominance at low energies, all codes agree on the  $T$ -dependence

- LO:  $\gamma_{M1; np \rightarrow d\gamma} \propto B_d^{\frac{5}{2}} a_s^2$ ,  $\frac{\partial \log \gamma}{\partial \log a_s} = 2$ ,  $\frac{\partial \log \gamma}{\partial \log B_d} = \frac{5}{2}$  appear  $T$ -indep.

# Temperature-dependence of nuclear reactions

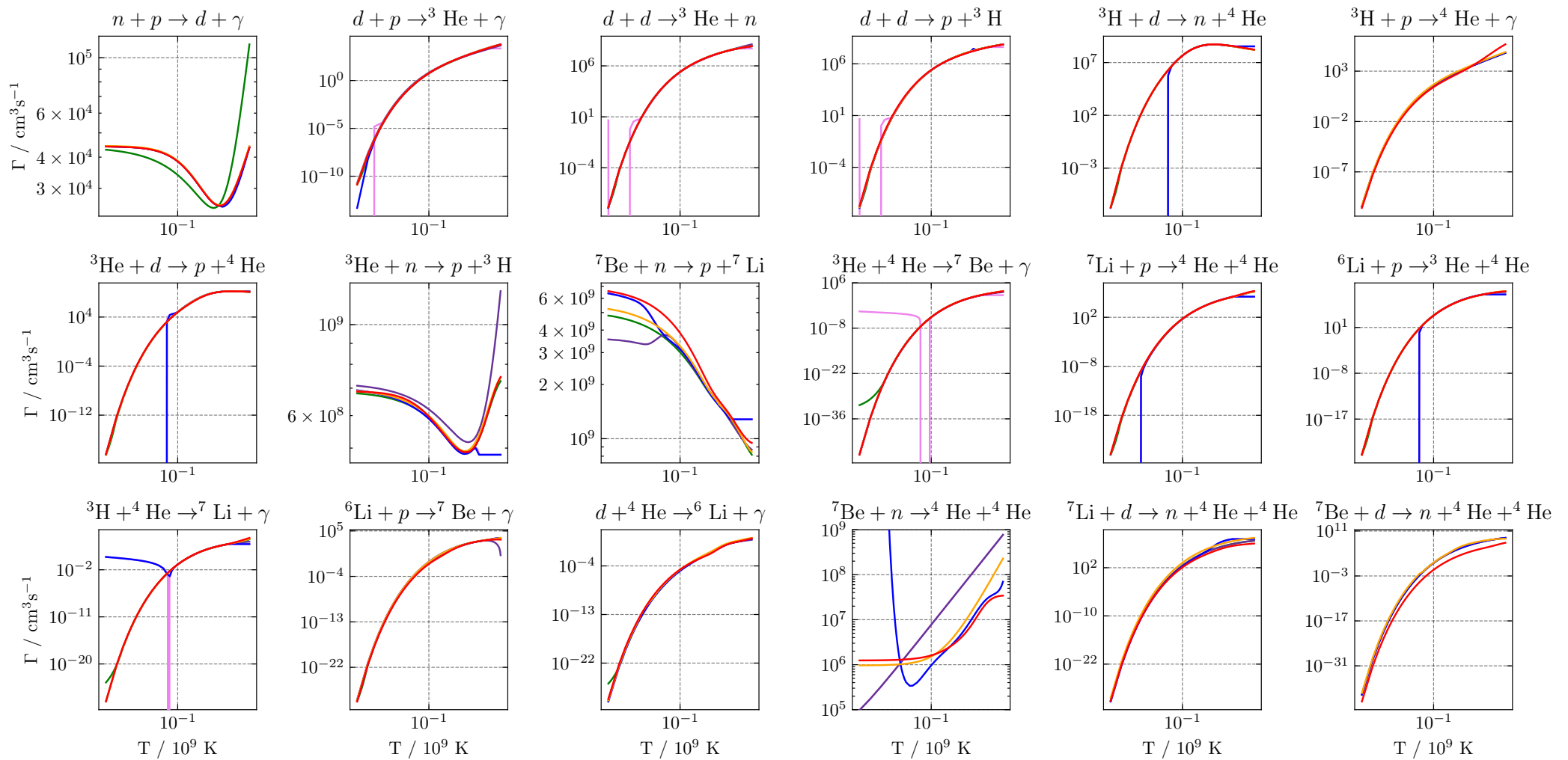
- Consider the leading and the next 17 reactions in the BBN network  
 → integrate reaction formulae ( $T_9 = T/[10^9\text{K}]$ ):



- Strong suppression of the  $a_s$  and  $B_d$  dependence in the leading reactions due to  $T$
- $T$ -effect appreciable for most reactions for  $T_9 \gtrsim 0.1$

# Temperature-dependence of nuclear reactions II

- For all codes, this work and NACRE II [Xu et al., Nucl. Phys. A **918** (2013) 61]



# BBN response matrix

- Calculate the linear dependence of the  $Y_n$  for small changes in  $a_S, B_d, \tau_n$ :

$$\partial \log Y_n / \partial \log X_k, \quad n \in \{^2\text{H}, ^3\text{H} + ^3\text{He}, ^4\text{He}, ^6\text{Li}, ^7\text{Li} + ^7\text{Be}\}$$

- Updating all natural constants, atomic & nuclear masses, and the leading reactions from EFT in all codes ( $\eta = 6.14 \cdot 10^{-10}$ ,  $\tau_n = 879.4$  s)

code	$^2\text{H}$ $\times 10^5$	$^3\text{H} + ^3\text{He}$ $\times 10^5$	$Y_p$	$^6\text{Li}$ $\times 10^{14}$	$^7\text{Li} + ^7\text{Be}$ $\times 10^{10}$
NUC123	2.550	1.040	0.247	1.101	4.577
PArthENoPE	2.511	1.032	0.247	1.091	4.672
AlterBBN	2.445	1.031	0.247	1.078	5.425
PRIMAT	2.471	1.044	0.247	1.198	5.413
PDG (2022)	2.547		0.245		1.6
$\pm$	0.025		0.003		0.3

- Four codes are largely consistent
- Lithium problem prevails

Fields, Ann. Rev. Nucl. Part. Sci. **61** (2011) 47

## Further results

- $T$ -dependence of the reaction rates on changes in  $B_A$  for the first time considered

$$\hookrightarrow \frac{\partial \log Y_n}{\partial \log a_s} \text{ reduced by a factor of three}$$

$$\hookrightarrow \frac{\partial \log Y_n}{\partial \log B_i} \text{ reduced by about 10 percent}$$

- $\eta$ -dependence linear and a minor effect for small changes (for  $\eta \cdot 10^{10} = 5.94 - 6.34$ )

- Code dependence of  $\frac{\partial \log Y_n}{\partial X_k}$  is very small

$\Rightarrow$  Now we are in the position to study the dependence of the  $Y_n$  on the fundamental parameters, especially on  $\alpha_{\text{EM}}$



# The tool: Nuclear lattice effective field theory II

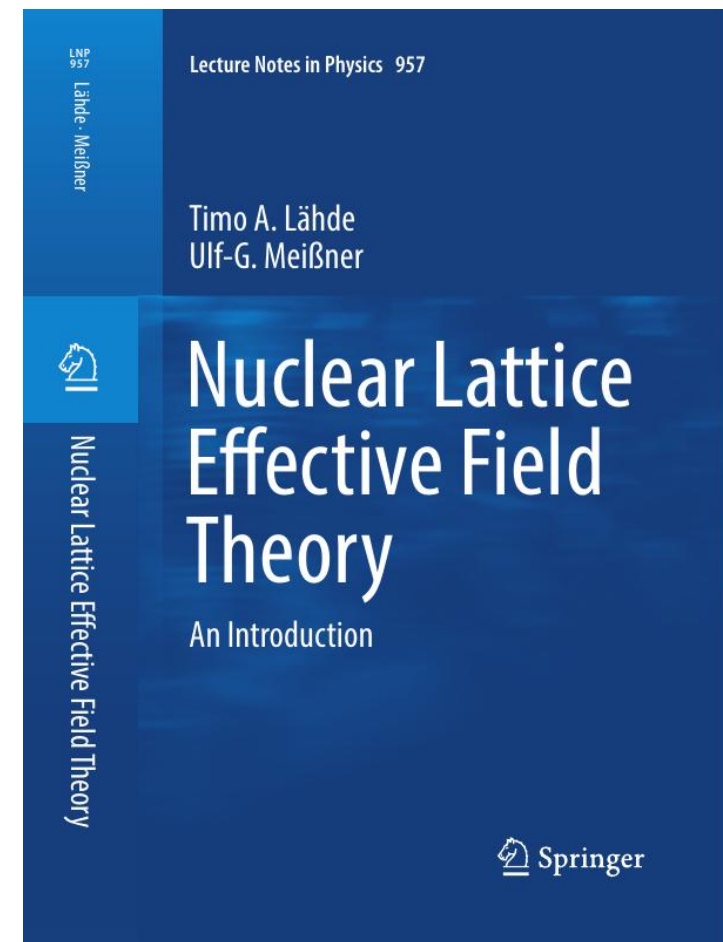
- For all details on chiral EFT on a lattice

T. Lähde & UGM

*Nuclear Lattice Effective Field Theory - An Introduction*

Springer Lecture Notes in Physics **957** (2019) 1 - 396

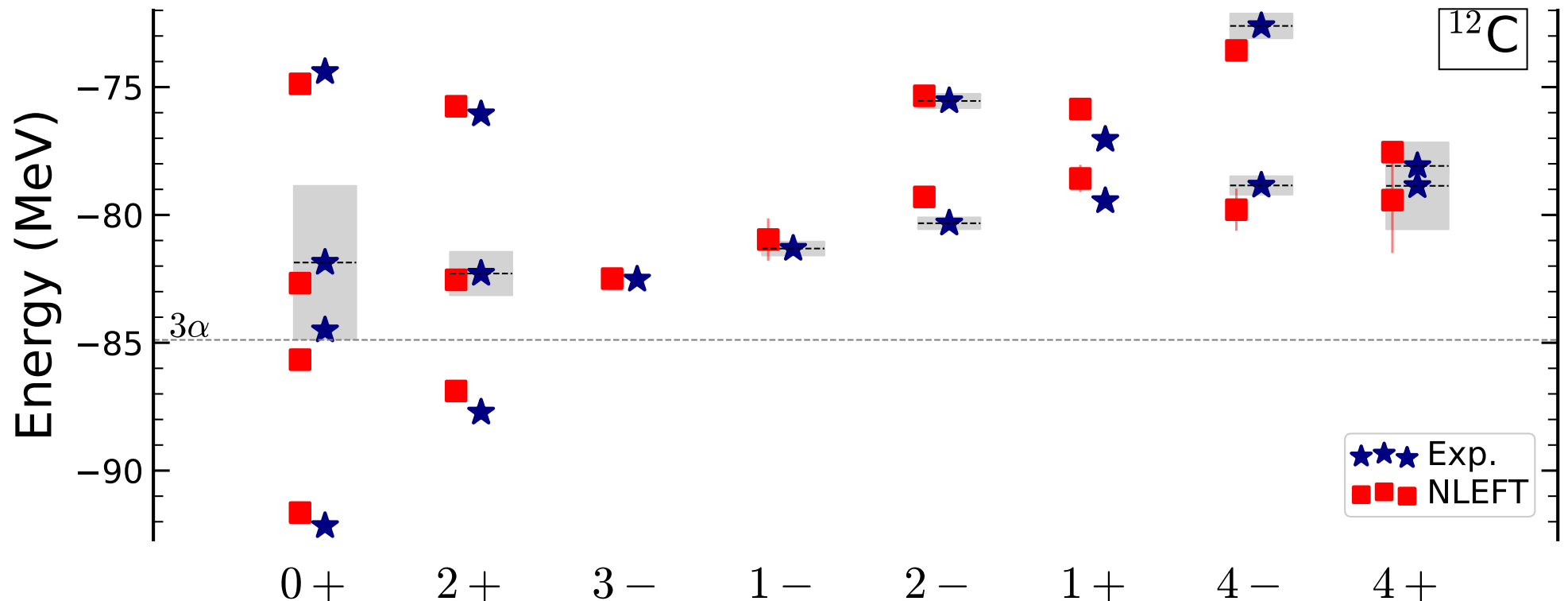
- Computational equipment



# NLEFT @ work: The spectrum of carbon-12 A.D. 2023 <sup>68</sup>

- with much improved algorithms and methods:

Shen, Lähde, Lee, UGM, Nature Commun. **14** (2023) 2777



→ solidifies earlier NLEFT statements about the structure of the  $0_2^+$  and  $2_2^+$  states

# Effects of the neutron lifetime

- The neutron width  $\Gamma_n \sim 1/\tau_n$  is given by:

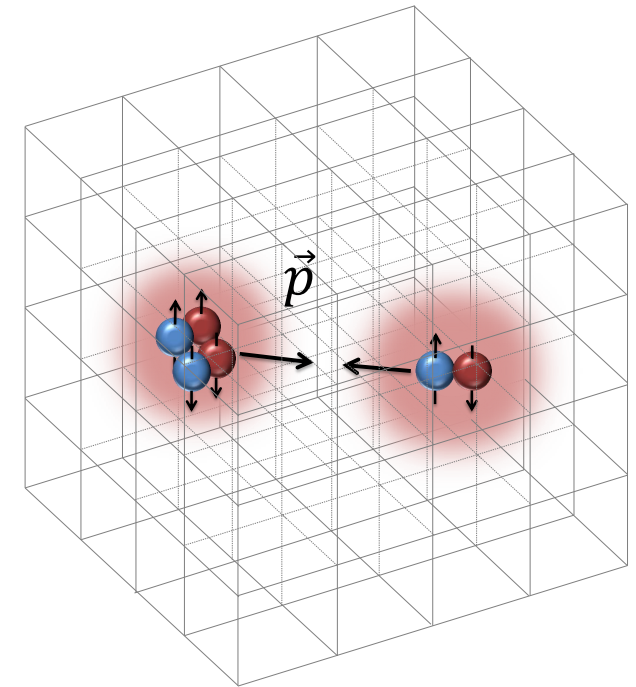
$$\Gamma_n = \frac{(G_F \cos \theta_C)^2}{2\pi^3} m_e^5 (1 + 3g_A^2) f \left( \frac{(m_n - m_p)^{\text{QED}}}{m_e} \right)$$

- BLP assumed that  $m_u/m_d$  stays constant when  $m_q$  changes
  - ↪ induces a large dependence of the function  $f$  on variation in  $m_q$
  - ↪ is model-dependent, as all other parameters are supposed to be unaffected
- A more natural scenario for  $m_u/m_d = \text{constant}$  is that the Higgs VEV changes, while all Yukawa and gauge coupling stay constant
  - ↪ this reduces the dependence of  $\Gamma_n$  on variations of  $m_q$  by a factor of 2
  - ↪ the sensitivity to  $\tau_n$  entirely denotes the  $^4\text{He}$  sensitivity

# Quark mass dependence of alpha-alpha scattering

# Nucleus-nucleus scattering on the lattice

- Processes involving  $\alpha$ -particles and  $\alpha$ -type nuclei comprise a major part of stellar nucleosynthesis, and control the production of certain elements in stars
- Ab initio calculations of scattering and reactions using continuum methods suffer from very unfavorable computational scaling with the number of nucleons  $A$  in the clusters (either factorial or exponential in  $A$ )
- This is very different in NLEFT:



Lattice EFT computational scaling  $\Rightarrow (A_1 + A_2)^2$

Rupak, Lee, Phys. Rev. Lett. **111** (2013) 032502  
Pine, Lee, Rupak, Eur. Phys. J. A **49** (2013) 151  
Elhatisari, Lee, Phys. Rev. C **90** (2014) 064001  
Elhatisari et al., Phys. Rev. C **92** (2015) 054612  
Elhatisari, Lee, UGM, Rupak, Eur. Phys. J. A **52** (2016) 174

# Ab initio alpha-alpha scattering

Elhatisari, Lee, Rupak, Epelbaum, Krebs, Lähde, Luu, UGM, Nature **528** (2015) 111

- Construct the so-called adiabatic Hamiltonian

$$[H_\tau^\alpha]_{\vec{R}\vec{R}'} = \sum_{\vec{R}_n \vec{R}_m} [N_\tau^{-1/2}]_{\vec{R}\vec{R}_n} [H_\tau]_{\vec{R}_n \vec{R}_m} [N_\tau^{-1/2}]_{\vec{R}_m \vec{R}'}$$

↪ two-cluster simulations

- Long-range Coulomb via spherical wall method (huge box)

Lu, Lähde, Lee, UGM, Phys. Lett. B **760** (2016) 309

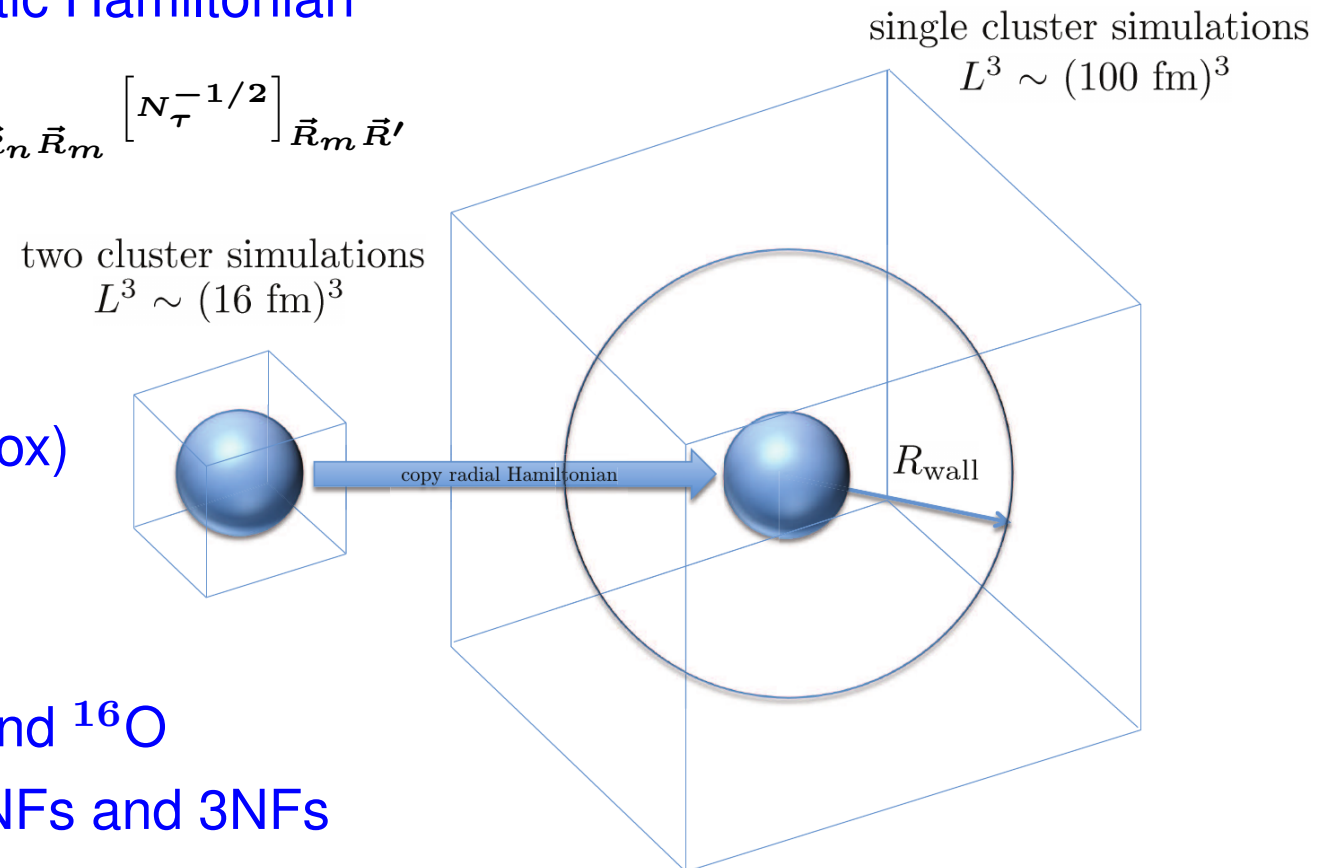
↪ single cluster simulations

- Same action as used for  $^{12}\text{C}$  and  $^{16}\text{O}$   
chiral N2LO Lagrangian w/ 2NFs and 3NFs

↪ all LECs determined before in NN and NNN systems

↪ parameter-free predictions

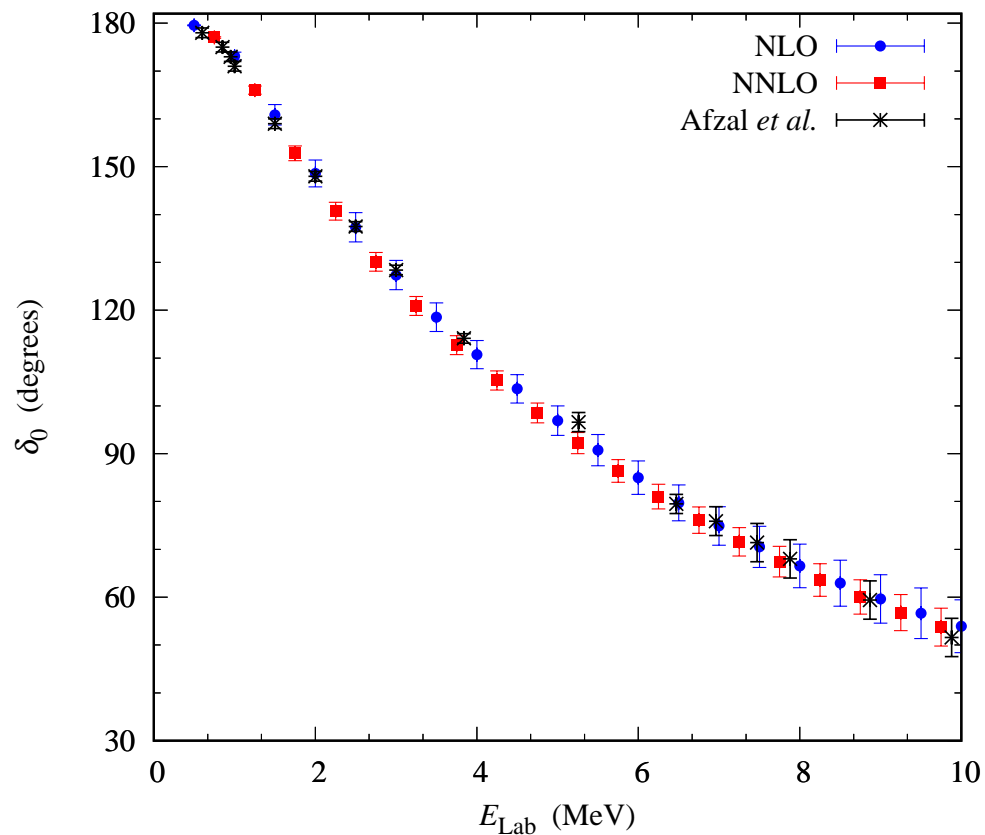
↪ first ever *ab initio* calculation of  $\alpha$ - $\alpha$  scattering



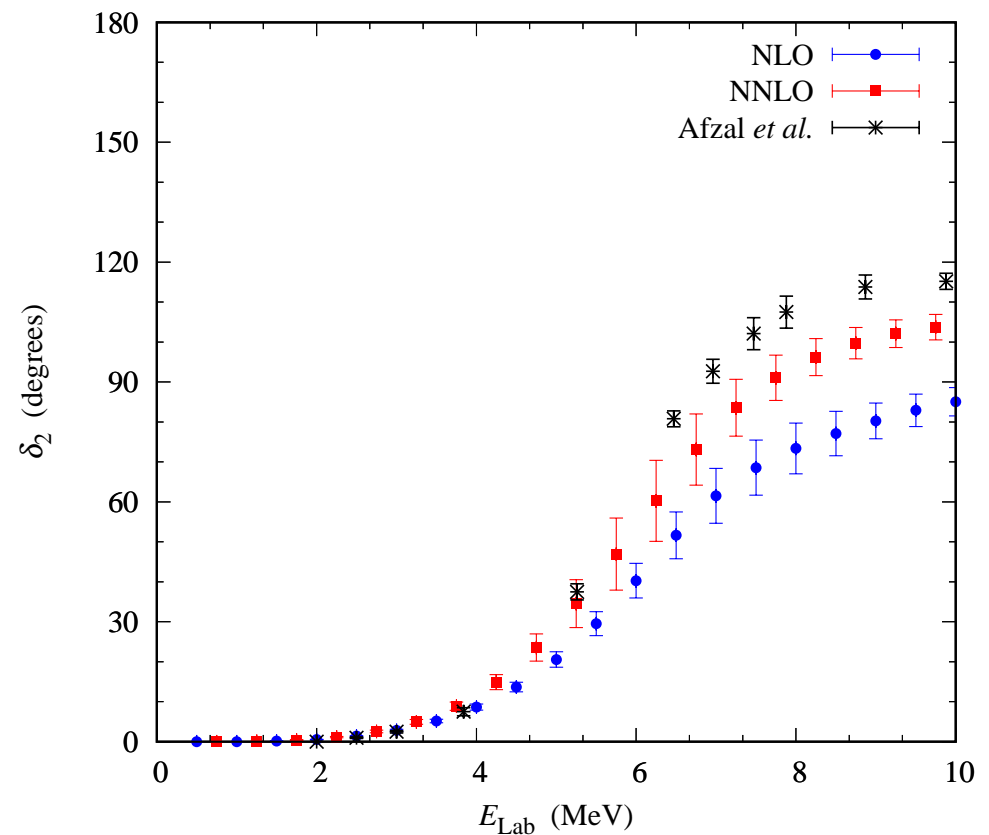
# Phase shifts of alpha-alpha scattering

- S-wave and D-wave phase shifts, updated in 2022

Elhatisari, Lähde, Lee, UGM, Vonk, JHEP **02** (2022) 001



$$E_R^{\text{NNLO}} = -0.11(1) \text{ MeV } [+0.09 \text{ MeV}]$$



$$E_R^{\text{NNLO}} = 2.93(5) \text{ MeV } [2.92(18) \text{ MeV}]$$

$$\Gamma_R^{\text{NNLO}} = 2.00(16) \text{ MeV } [1.35(50) \text{ MeV}]$$

Afzal *et al.*, Rev. Mod. Phys. **41** (1969) 247 [data]

# Alpha-alpha scattering in the multiverse

Elhatisari, Lähde, Lee, UGM, Vonk, JHEP **02** (2022) 001

- Now vary the light quark mass  $m_q$  and the fine-structure constant  $\alpha_{EM}$

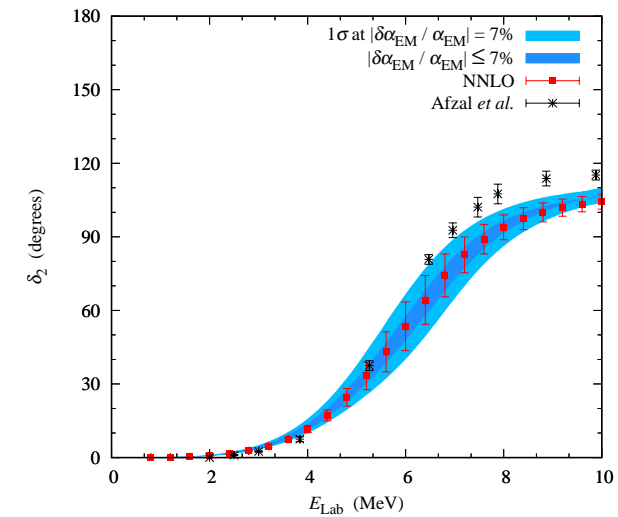
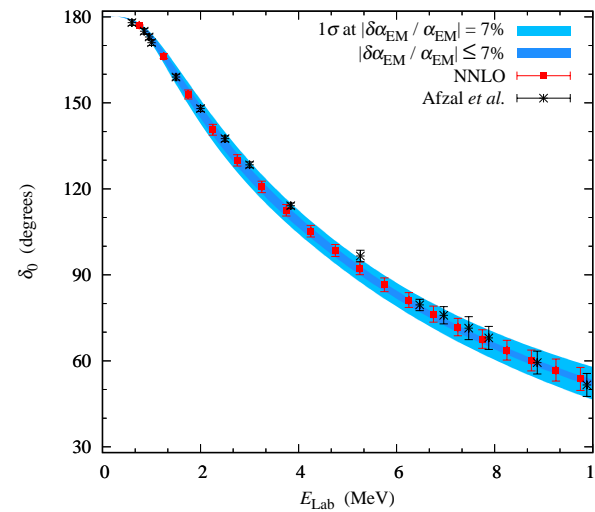
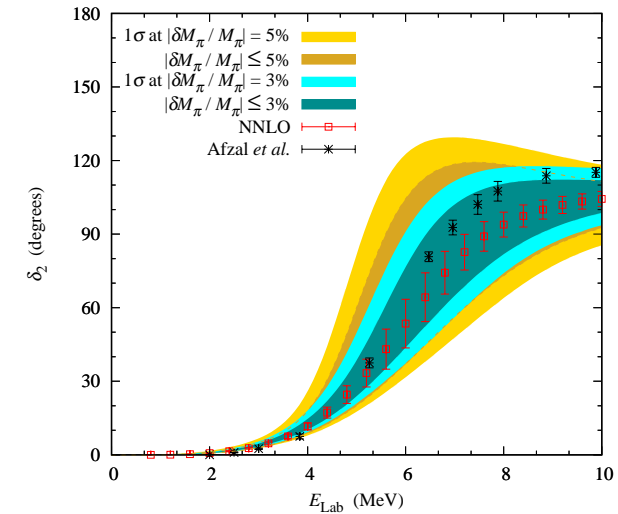
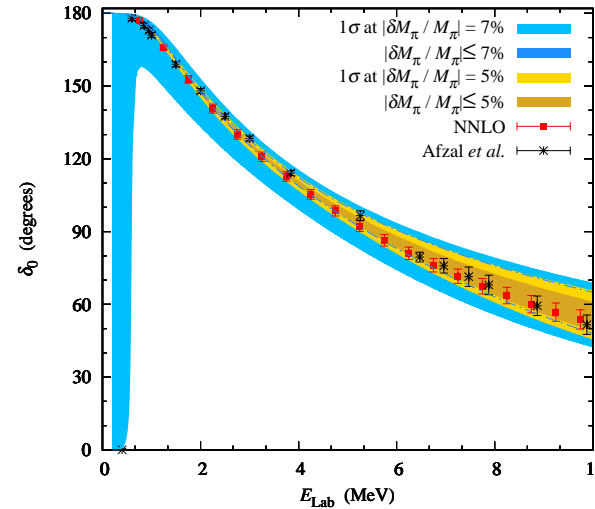
⇒ Dramatic effect in the S-wave  
for  $\delta M_\pi / M_\pi \simeq 7\%$

⇒ D-wave resonance requires  
 $\delta M_\pi / M_\pi \lesssim 3\%$

⇒ S- and D-wave phase shifts  
tolerate  $\delta\alpha_{EM} / \alpha_{EM} \lesssim 7\%$

⇒ weaker bounds as given by the  
position of the Hoyle state  
but independent of stellar modelling!

- in a next step, consider  $\alpha + {}^8\text{Be} \rightarrow {}^{12}\text{C}$   
as function of  $m_q$  and  $\alpha_{EM}$



# Primordial nucleosynthesis at varying quark masses

# General remarks

- Fundamental parameters of the strong interactions:  
the light quark masses  $m_u, m_d$   
also the strange quark mass  $m_s$

- In almost all nuclear reactions, strong isospin violation  $m_d/m_u \simeq 2$   
can be neglected because:

$$\frac{m_u - m_d}{\Lambda_{\text{QCD}}} \simeq \frac{1}{100}$$

- $m_d \neq m_u$  features prominently in neutron  $\beta$ -decay
- Dominant strange quark effect through the nucleon mass (trace anomaly)

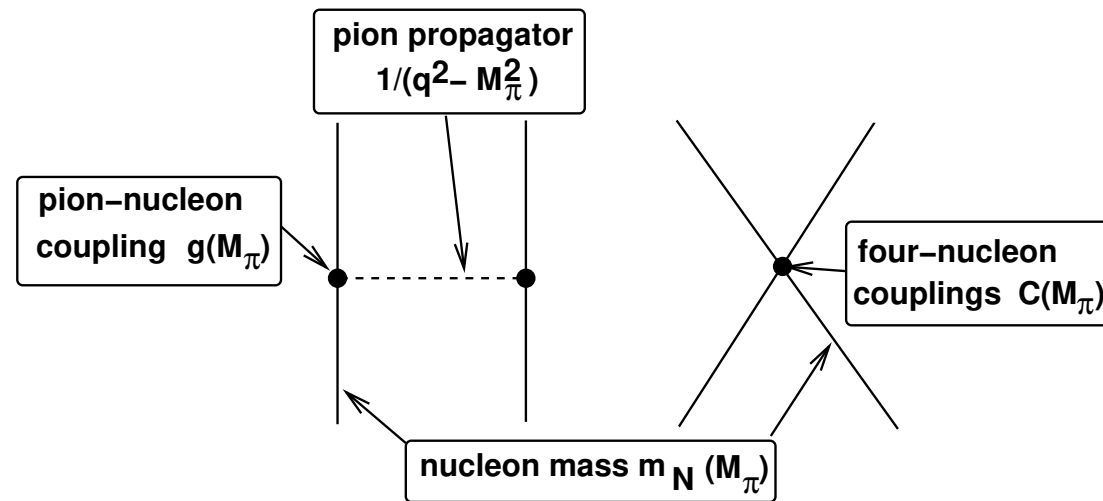
$$m_N^{u,d,s} = \langle N(p) | m_u \bar{u}u + m_d \bar{d}d + m_s \bar{s}s | N(p) \rangle$$

- Quark mass variations = variations of the weak scale  $v$  (Yukawa's fixed)  
Higgs VEV

# Ingredients

- Nuclear forces are given by chiral EFT based on Weinberg's power counting
- ⇒ Pion-exchange contributions and short-distance multi-N operators
- graphical representation of the quark mass dependence of the LO potential

Weinberg 1991



- always use the Gell-Mann–Oakes–Renner relation:

$$M_{\pi^\pm}^2 \sim (m_u + m_d)$$

- fulfilled to better than 94% in QCD

Colangelo, Gasser, Leutwyler 2001

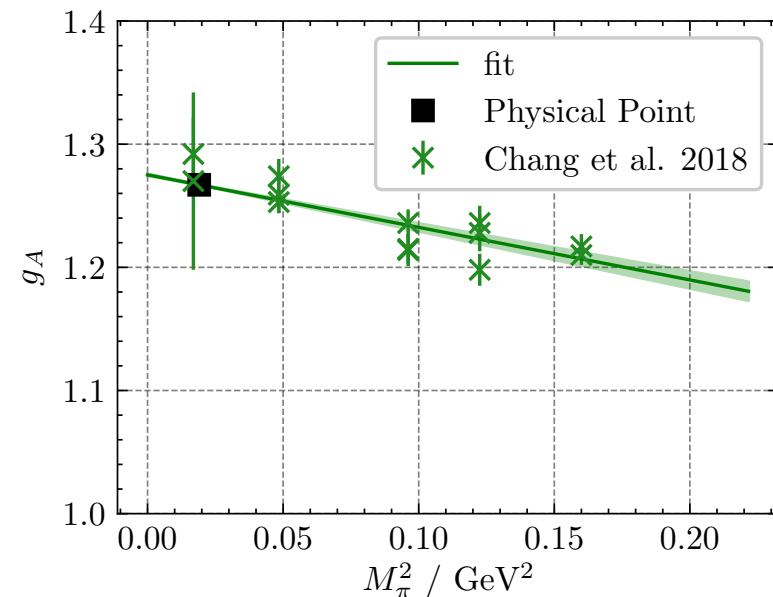
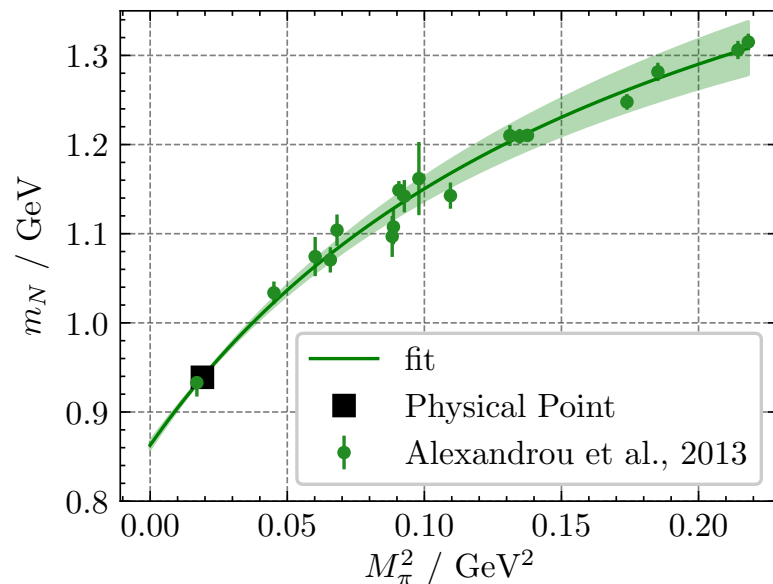
- Strong isospin violation and electromagnetic effects can also be included

# Higgs VEV variations

- Where do variations in  $v$  appear?  $\hookrightarrow$  single nucleon (particle) properties
- Fermi constant  $G_F \sim (1 + \delta v/v)^{-2}$ , electron mass, ...
- Neutron-proton mass difference Gasser, Leutwyler, Rusetsky (2021)

$$\frac{Q_N}{\text{MeV}} = \frac{m_n - m_p}{\text{MeV}} = (1.87 \mp 0.16) \left(1 + \frac{\delta v}{v}\right) - (0.58 \pm 0.16)$$

- Nucleon mass  $m_N$  and axial-vector coupling constant  $g_A$  from lattice QCD



# Higgs VEV variations

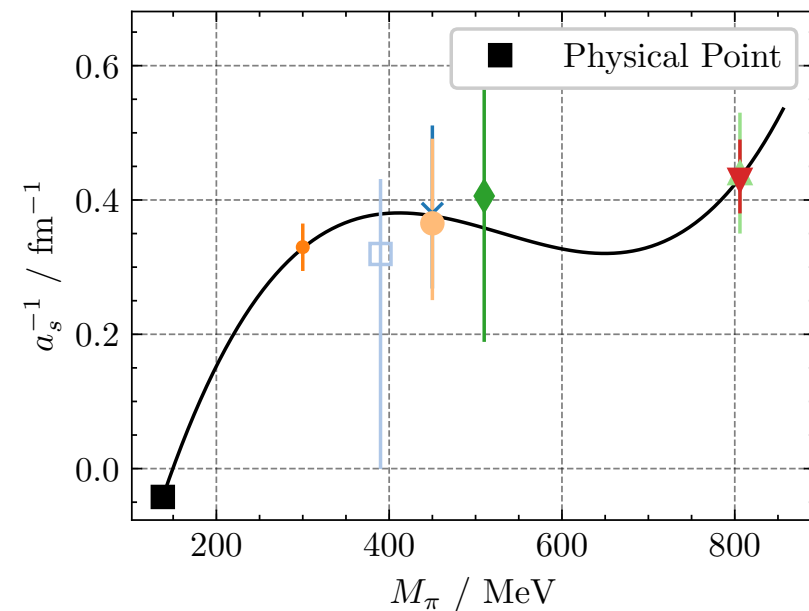
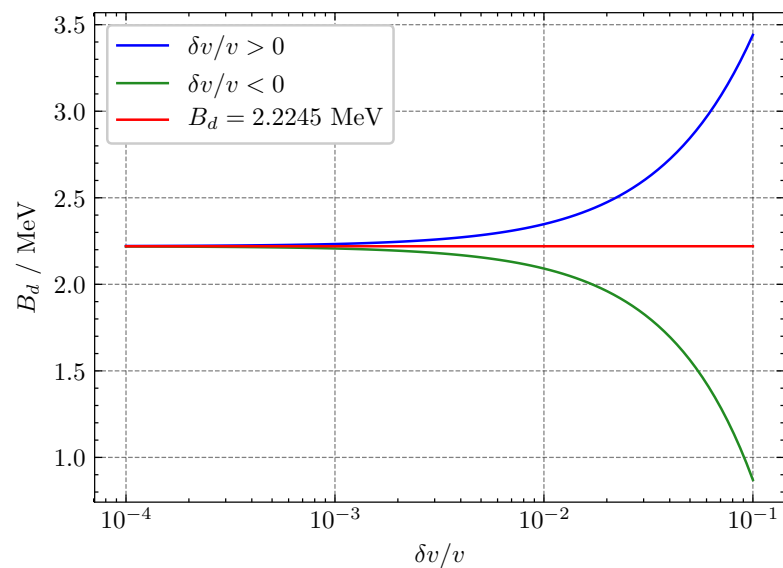
- Where do variations in  $v$  appear?

↪ two-nucleon observables

- Deuteron binding energy and singlet  $np$  scattering length

↪ combine LQCD results with NN ERE low-energy theorems

Baru, Epelbaum, Filin, Gegelia (2015,2016)



● PhysRevD.92.014501   □ PhysRevD.85.054511   ▲ PhysRevD.96.114510  
× PhysRevD.103.054508   ◆ PhysRevD.86.074514   ▼ PhysRevC.88.024003

# Higgs VEV variations

- Where do variations in  $v$  appear?

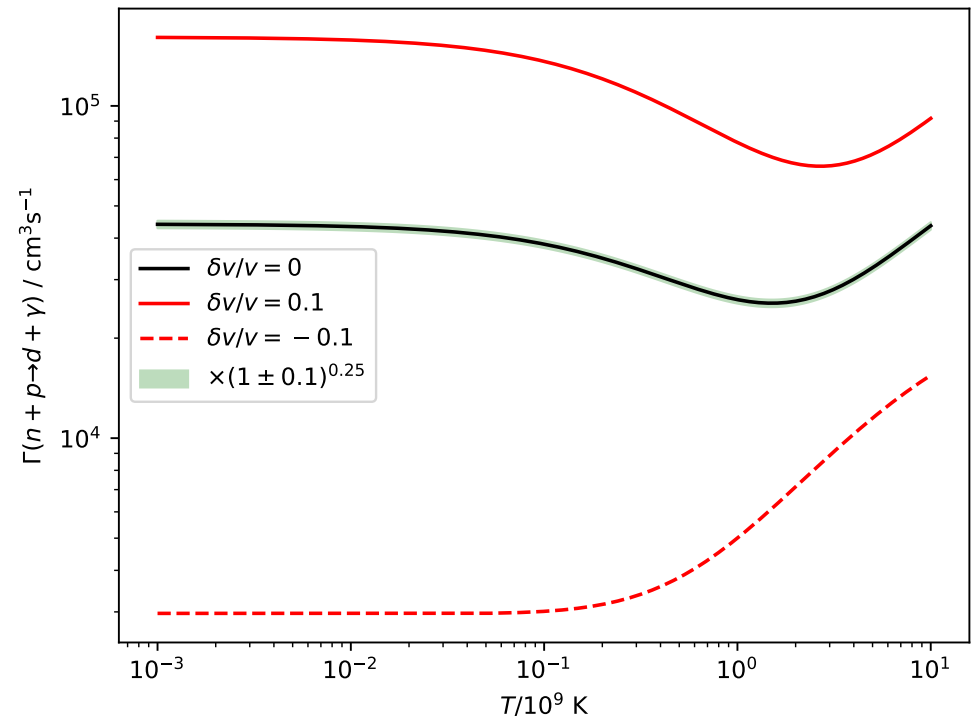
↪ nuclear reactions

- most relevant ist  $n + p \rightarrow d + \gamma$ , its rate depends heavily on

- deuteron binding energy
- nucleon mass
- NN scattering parameters

- $v$  dependence much stronger than expected from naive scaling

Burns et al. (2024)



- **most sensitive** to  $B_d$  is the back-reaction at the d bottleneck

$$\langle \sigma(d\gamma \rightarrow np)v \rangle = \alpha T_9^\beta \exp(\kappa/T_9) \langle \sigma(np \rightarrow d\gamma)v \rangle, \quad \alpha \propto \left( \frac{m_n m_p}{m_d} \right)^{3/2}, \quad \kappa \propto B_d$$

# The tool: Nuclear lattice effective field theory

Frank, Brockmann (1992), Koonin, Müller, Seki, van Kolck (2000), Lee, Schäfer (2004), . . .  
Borasoy, Krebs, Lee, UGM, Nucl. Phys. **A768** (2006) 179; Borasoy, Epelbaum, Krebs, Lee, UGM, Eur. Phys. J. **A31** (2007) 105

- *new method* to tackle the nuclear many-body problem

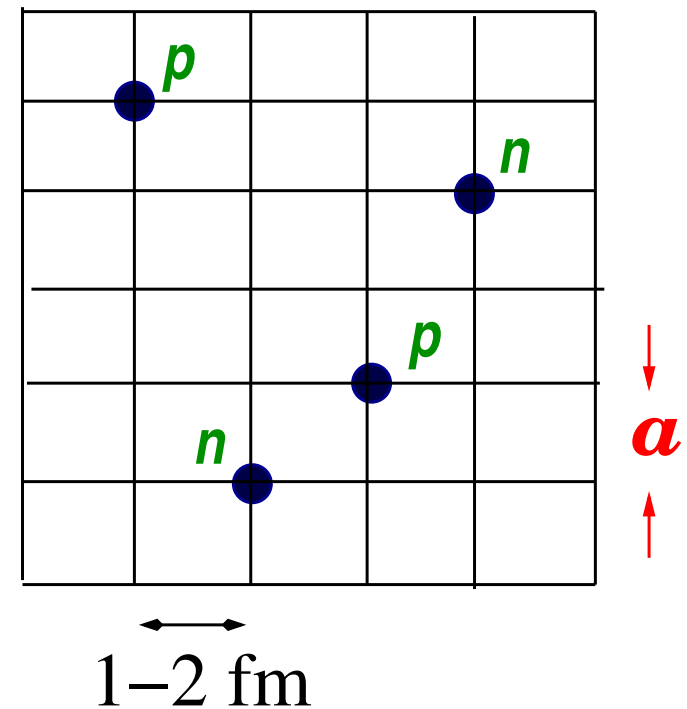
- discretize space-time  $V = L_s \times L_s \times L_s \times L_t$ :  
nucleons are point-like particles on the sites

- discretized chiral potential w/ pion exchanges  
and contact interactions + Coulomb

→ see Epelbaum, Hammer, UGM, Rev. Mod. Phys. **81** (2009) 1773

- typical lattice parameters

$$p_{\max} = \frac{\pi}{a} \simeq 315 - 630 \text{ MeV [UV cutoff]}$$



- strong suppression of sign oscillations due to approximate Wigner SU(4) symmetry

E. Wigner, Phys. Rev. **51** (1937) 106; T. Mehen et al., Phys. Rev. Lett. **83** (1999) 931; J. W. Chen et al., Phys. Rev. Lett. **93** (2004) 242302

- physics independent of the lattice spacing for  $a = 1 \dots 2 \text{ fm}$

Alarcon, Du, Klein, Lähde, Lee, Li, Lu, Luu, UGM, EPJA **53** (2017) 83; Klein, Elhatisari, Lähde, Lee, UGM, EPJA **54** (2018) 121

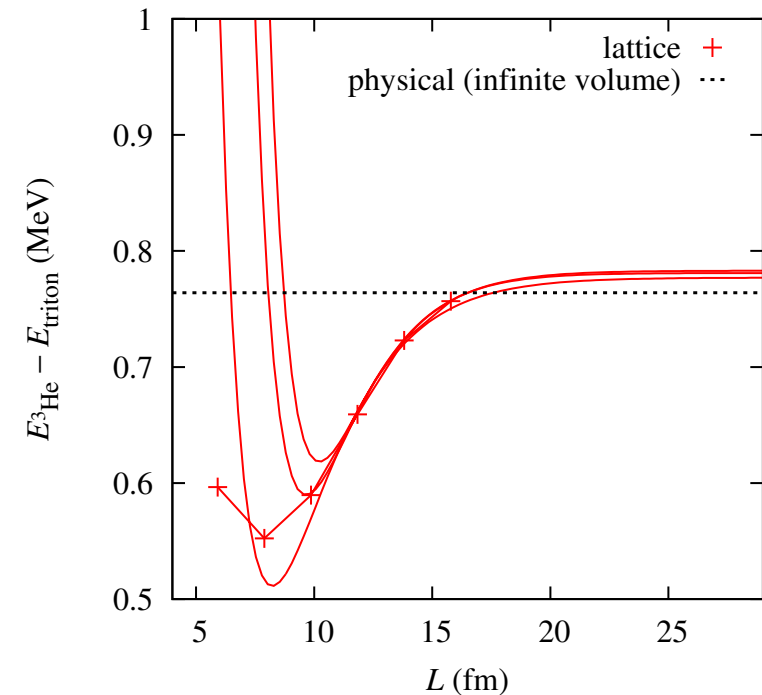
# Some early results: Validation of the method

Epelbaum, Krebs, Lee, UGM, Phys. Rev. Lett. **104** (2010) 142501; Eur. Phys. J. A **45** (2010) 335

Lähde, Epelbaum, Krebs, Lee, UGM, Rupak, Phys. Lett. B **732** (2014) 110; Phys. Rev. Lett. **112** (2014) 102501

- Some groundstate energies and differences

E [MeV]	NLEFT	Exp.
${}^3\text{He} - {}^3\text{H}$	0.78(5)	0.76
${}^4\text{He}$	-28.3(6)	-28.3
${}^8\text{Be}$	-55(2)	-56.5
${}^{12}\text{C}$	-92(3)	-92.2
${}^{16}\text{O}$	-131(1)	-127.6
${}^{20}\text{Ne}$	-166(1)	-160.6
${}^{24}\text{Mg}$	-198(2)	-198.3
${}^{28}\text{Si}$	-234(3)	-236.5



- promising results [much improved by now]
- excited states more difficult, but also doable

