

Lifetime of a muon bound to a light nucleus

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A muon bound in the 1S state of a hydrogen-like ion can decay into an electron and a pair of neutrinos. For small nuclear charge Z , Überall (1960) predicted a suppression of the total rate relative to the free-muon width, $1 - \Gamma/\Gamma_0 \approx (\alpha Z)^{2/2}$, $\alpha \approx 1/137$. The first all-orders numerical calculation in αZ (Watanabe et al., 1993) reported for oxygen ($Z=8$) $\Gamma/\Gamma_0=0.994$, in tension with Überall's analytic expectation ≈ 0.998 . This 4×10^{-3} discrepancy is too large to be explained by the next term $O((\alpha Z)^3)$, which is $\sim 2 \times 10^{-4}$.

In this work we revisit the calculation and trace the discrepancy to slow convergence of the partial-wave sum. Truncation at $\kappa=31$ underestimates the rate; extending the sum to $\kappa=59$ and controlling the tail yields $\Gamma/\Gamma_0=0.9976$ for $Z=8$, now consistent with Überall's prediction within expected $O((\alpha Z)^3)$ effects. Our result resolves the long-standing conflict and clarifies the numerical requirements for reliable bound-state QED calculations. It also supports analogous expansion methods used in heavy-quark physics.

Your current academic level

PhD student

Your email address

davydov@ualberta.ca

Affiliation

University of Alberta

Supervisor email

andrzejc@ualberta.ca

Supervisor name

Andrzej Prus-Czarnecki

Primary author: DAVYDOV, Artem (University of Alberta)

Presenter: DAVYDOV, Artem (University of Alberta)

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