

# Recent advances in $\beta$ decay and possible future avenues

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Leendert Hayen

DND Meeting, Nov 5th 2020

NC State & TUNL, USA

Introduction

CKM unitarity

    Radiative corrections

    Neutron and nuclear tests

Exotic current searches

Outlook & summary

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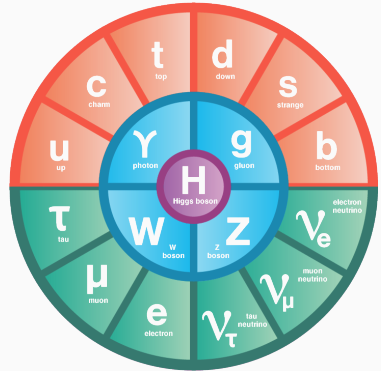
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# Introduction: Standard Model

'Simple' gauge groups:

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

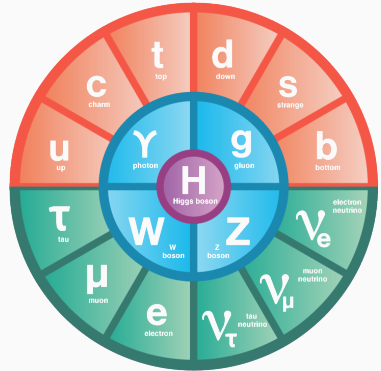


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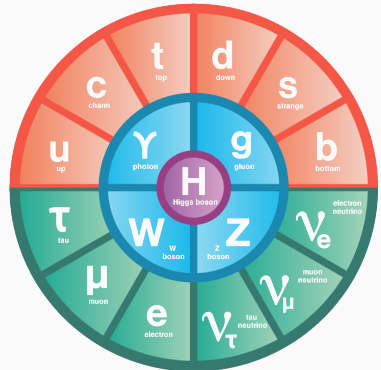
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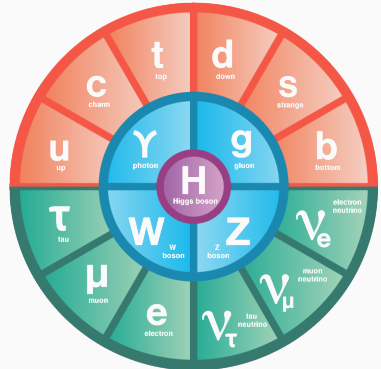
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Open questions: dark matter, gravity, neutrino masses, ...



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- Lorentz structure **Today**
- CKM unitarity **Today**

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# Introduction: $\beta$ decay

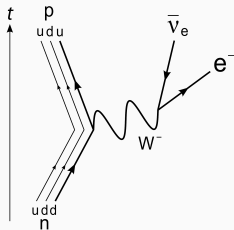
## Advantages

Typical  $\beta$  decay scale  $\ll M_W$

→ V-A 4-point tree level + QCD + QED

→ Constant renormalization of coupling constants

Nuclear chart sandbox



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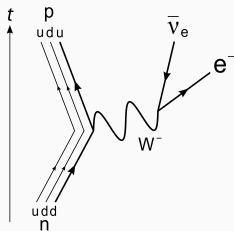
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## Challenges

Strong many-body physics

High precision requires quark → nucleus →  
atom corrections



# Workshops

Lots of activity following 3 timely workshops



- Nov 2018: ACFI UMass
- April 2019: ECT\* Trento
- Nov 2019: INT @ UW

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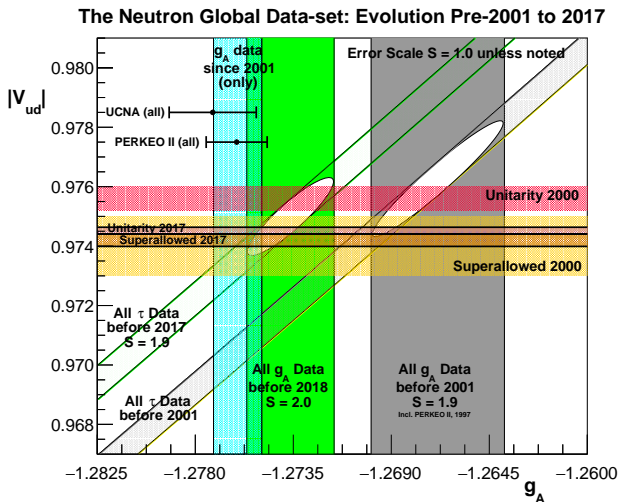
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(nuclear)  $\beta$  decay, meson decay ( $\pi$ , K),  $|V_{ub}|^2 \sim 10^{-5}$

# CKM unitarity: 2001-2017

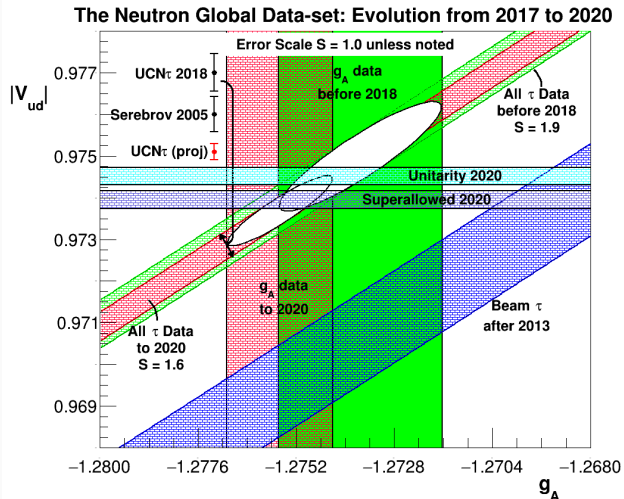
Quite some movement over the years...



Thanks to Albert Young

# CKM unitarity: 2018-2020

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The plot thickens: **disagreement** between  $K/2$  and  $K/3$   $|V_{us}|$   
'Cabibbo angle anomaly'

- $|V_{us}| = 0.2234(8)$  ( $K \rightarrow \pi l \nu$ )
- $|V_{us}| = 0.2253(4)$  ( $K^\pm \rightarrow l^\pm \nu$ )

Early signs of new physics? Lattice QCD artifacts? Time will tell

Czarnecki, Marciano, Sirlin PRD 101 (2020) 019301

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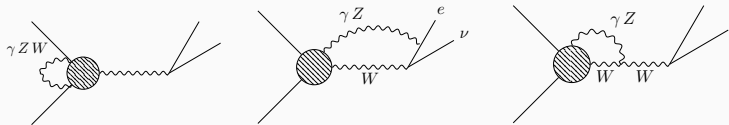
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1. Energy-dependent, QCD-*independent* part:  $\delta_R$
2. Energy-*independent*, QCD-dependent part:  $\Delta_R$

$\delta_R$  sufficiently known.  $\Delta_R$  depends on



vertex correction, box diagrams,  $\sim$  penguin

+ others. Generally well-understood from current algebra & pQCD



## Recent changes: $RC$

Everything OK except (in)famous axial contribution in  $\gamma W$  box

$$\square_{\gamma W}^{VA} = \frac{\alpha}{8\pi} \int_0^\infty dQ^2 \frac{M_W^2}{Q^2 + M_W^2} F(Q^2)$$

sensitive everywhere  $Q^2 \rightarrow 0$  (IR),  $Q^2 \sim M_n^2$  (Nuclear + inelastic),  
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**2006:** Marciano

& Sirlin  $\Delta_R^V = 0.02361(38)$ ,

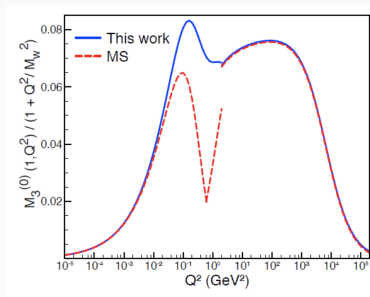
but heuristic uncertainty

from 'intermediate' energy scale

**2018:** Seng,

Gorchtein, Patel, Ramsey-Musolf

$\Delta_R^V = 0.02467(22)$  **4  $\sigma$  shift**



Seng, Gorchtein, Ramsey-Musolf

PRD 100 (2019) 013001

## Recent changes: $RC$

Change in  $\Delta_R^V$  corresponds to change in  $|V_{ud}|$

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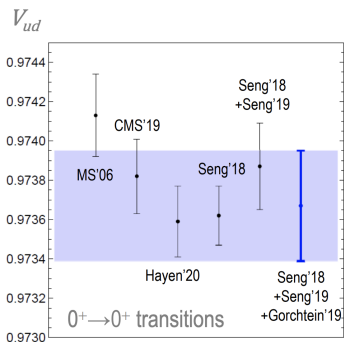
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Additional **quasi/inelastic** nuclear structure should be included

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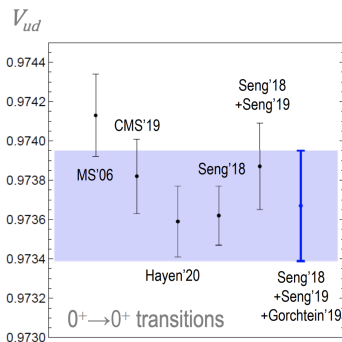
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You win some, ...

Gorchtein, PRL 123 (2019) 042503



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So far only  $\Delta_R^V$  was calculated, what about  $\Delta_R^A$

$$g_A^{\text{exp}} = g_A \left[ 1 + \frac{1}{2}(\Delta_R^A - \Delta_R^V) + \delta_{BSM} \right]$$

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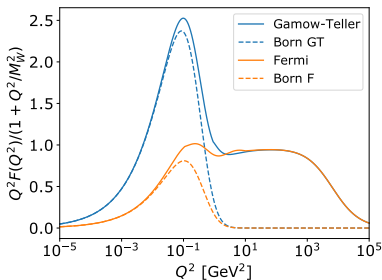
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New calculation

- $\Delta_R^A = 0.02881(30)$
- $\Delta_R^V = 0.02474(31)$

$$\Delta_R^A - \Delta_R^V = 4.07(8) \times 10^{-3}$$



LH, 2010.07262



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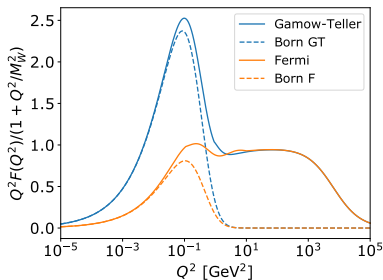
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Much larger than  
usually assumed ( $\lesssim 0.1\%$ )!



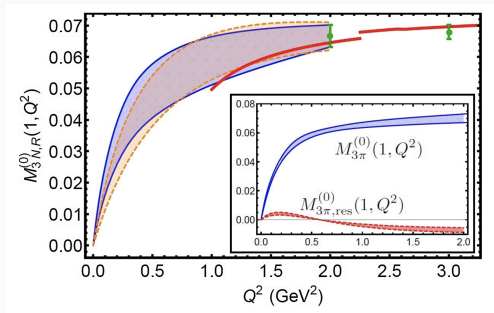
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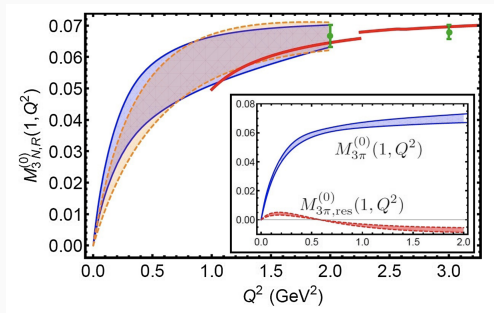


Seng *et al.*, PRD 101 111301

Use pions & relate to nucleon

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Seng *et al.*, PRD 101 111301

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Efforts underway for  $\Delta_R^A + \Delta_R^V$  from  $\chi PT$  & LQCD

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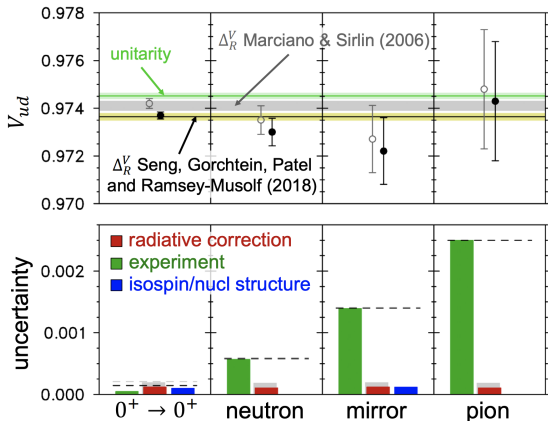
Fermi matrix element known from isospin symmetry

$\rightarrow$  small corrections (+ GT/F from correlation measurement)



# CKM unitarity: $V_{ud}$ precision

Status early 2019



•  $0^+ \rightarrow 0^+$ :  
 $V_{ud} = 0.9742(2)$   
 $\rightarrow 0.9737(1)$

• The neutron  
 $V_{ud} = 0.9735(6)$   
 $\rightarrow 0.9730(6)$

• Mirror transitions  
 $V_{ud} = 0.9727(14)$   
 $\rightarrow 0.9722(14)$

• The pion  
 $V_{ud} = 0.9748(25)$   
 $\rightarrow 0.9743(25)$

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Experimentally, need to know

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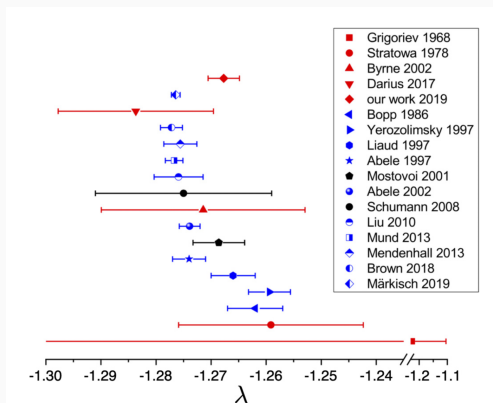
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# The neutron: $\lambda$

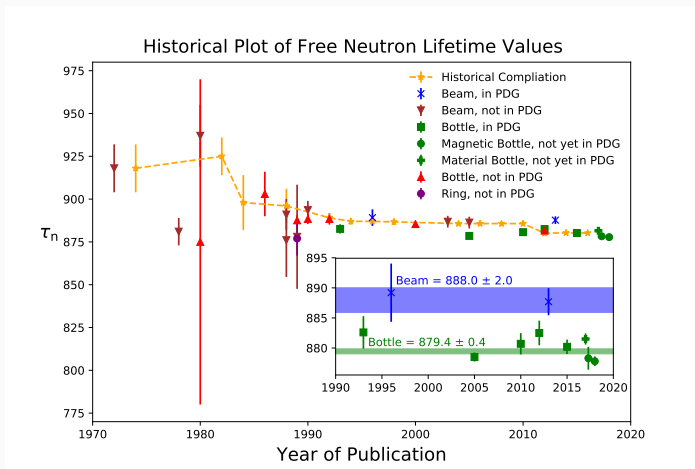
Evolution of  $\lambda = g_A/g_V$



Tension between PERKEO3 and aSPECT, both 2019

# The neutron: $\tau_n$

## Evolution of $\tau_n$



Bottle: Count survivors; Beam: Count decay products

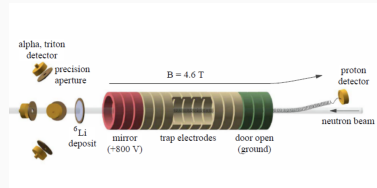
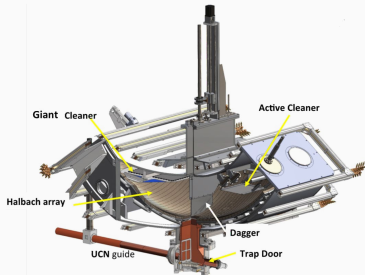
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Current US based efforts mainly **UCN $\tau$  @ LANSCE (bottle)** & **BL2/3 @ NIST (beam)**



Several R&D efforts to combine (UCNProbe, HOPE, ...)





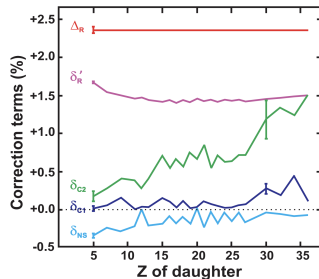
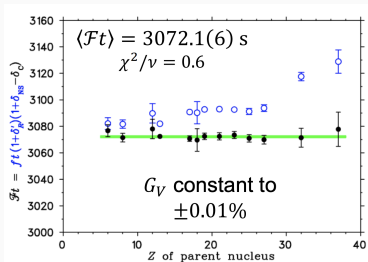
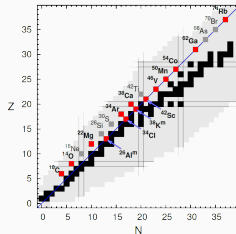
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Pure Fermi transitions,  $M_F = \sqrt{2}$

$$f_V t(1+\delta_R)(1-\delta_C+\delta_{NS}) = \frac{K}{2G_F^2 V_{ud}^2 (1 + \Delta_R^V)}$$

Few small  $\mathcal{O}(0.1\% - 2.5\%)$  corrections

$$\delta V_{ud}/V_{ud} \approx 0.04\%$$



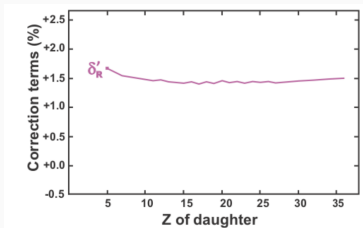
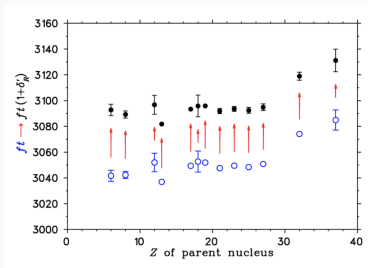
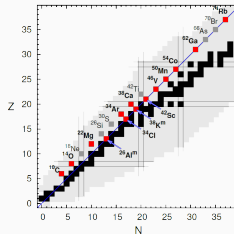
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Additional photonic corrections

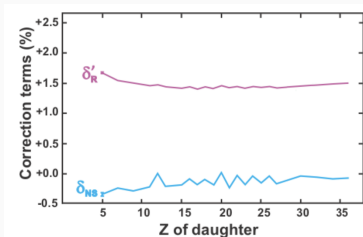
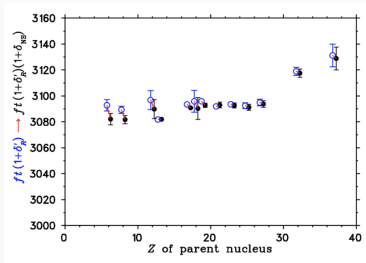
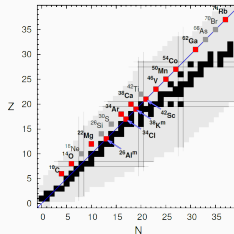
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Nuclear effects in RC (2BC)

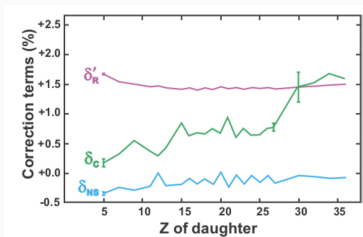
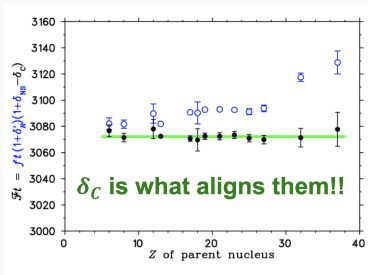
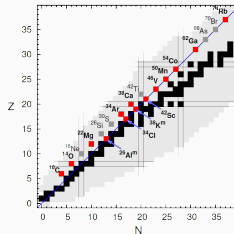
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Isospin breaking. How sure are we of  $\delta_C$ ?

## Nucleus: Isospin breaking corrections

In this context: proton  $\neq$  neutron inside nucleus

$$\rightarrow M_F^2 = 2(1 - \delta_C)$$

- Different radial wave function (Coulomb)
- Configuration interaction difference initial  $\leftrightarrow$  final

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Compilations used Woods-Saxon potentials in shell model, but **ab initio** is maturing

$\rightarrow$  well-defined uncertainties & minimal data fitting

## Nucleus: $T = 1/2$ Mirror decays

Nuclei with same 'core', initial and final state differ only in valence particle (e.g.  ${}^3\text{H}$  &  ${}^3\text{He}$ ,  ${}^{15}\text{O}$  &  ${}^{15}\text{N}$ )



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$M_F = 1$ , but mixed Fermi-Gamow-Teller decay

$$f_V t (1 + \delta_R) (1 - \delta_C + \delta_{NS}) \left[ 1 + \frac{f_A}{f_V} \rho^2 \right] = \frac{K}{G_F^2 V_{ud}^2 (1 + \Delta_R^V)}$$

$\rho$  must be **determined independently** from  $\beta$  correlation,  $f_A/f_V \sim 1$  from theory

## Nucleus: $T = 1/2$ Mirror decays

Nuclei with same 'core', initial and final state differ only in valence particle (e.g.  ${}^3\text{H}$  &  ${}^3\text{He}$ ,  ${}^{15}\text{O}$  &  ${}^{15}\text{N}$ )

$M_F = 1$ , but mixed Fermi-Gamow-Teller decay

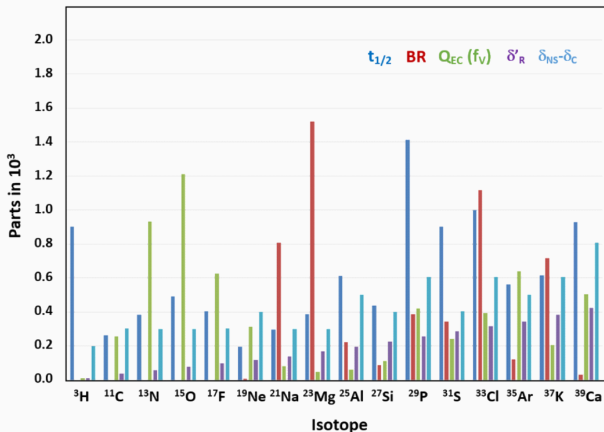
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$$\frac{d\Gamma}{dE_e d\Omega_e d\Omega_\nu} \propto 1 + a_{\beta\nu} \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + b_F \frac{m_e}{E_e} + A \frac{\vec{p}_e}{E_e} \cdot \langle \vec{I} \rangle + \dots$$

# Nucleus: $T = 1/2$ Mirror decays

Current precision status for  $f_V t(1 + \delta_R)(1 + \delta_{NS} - \delta_C)$



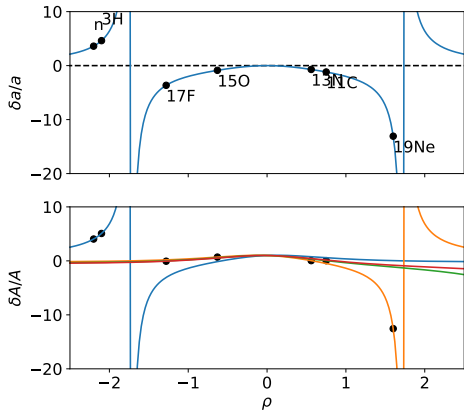
N. Severijns, LH *et al.*, In preparation

# Nucleus: $T = 1/2$ Mirror decays

For  $V_{ud}$  extraction  $\rho$  is typically bottleneck

Mixed transition causes cancellation  $\rightarrow$  enhanced sensitivity

Neutron and  $^{19}\text{Ne}$  have factor 5-13 enhancement for  $\rho$ !



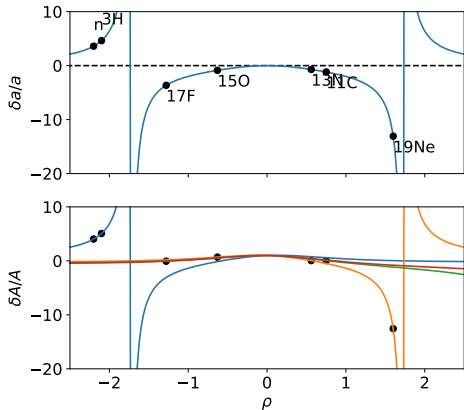
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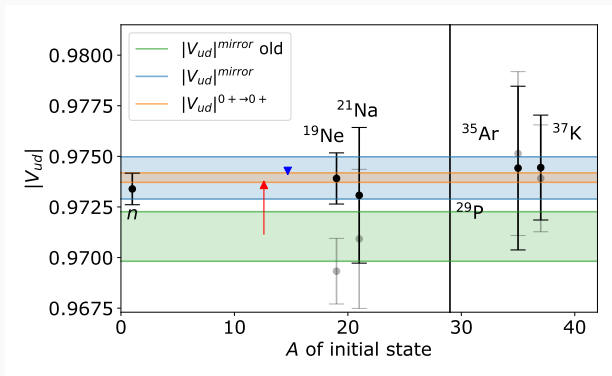
Neutron and  $^{19}\text{Ne}$  have factor 5-13 enhancement for  $\rho$ !

Consistent formalism released (RC, nuclear, geometry), event generator (CRADLE++) in development



# Nucleus: $T = 1/2$ Mirror decays

**Resolved double-counting** in mirror  $RC$  significantly increases precision & agreement

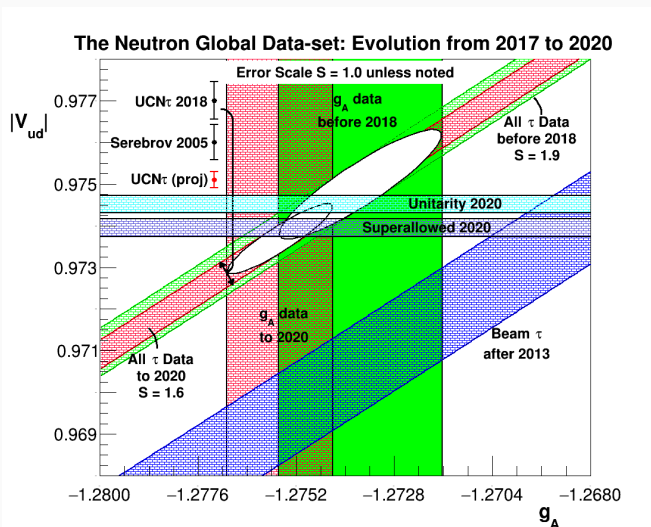


LH, 2010.07262

$$|V_{ud}|^{mirror} = 0.9710(12) \longrightarrow |V_{ud}|^{mirror} = 0.9739(10)$$

# CKM unitarity: 2018-2020

To summarize



Thanks to Albert Young

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## Weak Lorentz structure

Standard Model has  $V$ - $A$  structure, but more generally

$$\mathcal{L}_{\text{eff}} = -\frac{G_F \tilde{V}_{ud}}{\sqrt{2}} \left\{ \bar{e} \gamma_\mu \nu_L \cdot \bar{u} \gamma^\mu [1 - (1 - 2\epsilon_R) \gamma^5] d + \epsilon_S \bar{e} \nu_L \cdot \bar{u} d \right. \\ \left. - \epsilon_P \bar{e} \nu_L \cdot \bar{u} \gamma^5 d + \epsilon_T \bar{e} \sigma_{\mu\nu} \nu_L \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma^5) d \right\} + \text{h.c.},$$

with

$$\tilde{V}_{ud} = V_{ud} (1 + \epsilon_L + \epsilon_R - \delta G_F / G_F)$$

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$$\tilde{V}_{ud} = V_{ud} (1 + \epsilon_L + \epsilon_R - \delta G_F / G_F)$$

All  $\epsilon_i$  are proportional to  $(M_W / \Lambda_{BSM})^2$ , change kinematics

$\epsilon_i \lesssim 10^{-4} \rightarrow \Lambda_{BSM} \gtrsim 15 \text{ TeV}$  assuming natural couplings

## Lattice QCD comparison

Comparison with LQCD is clean test for  $\epsilon_R$

$$g_A^{\text{exp}} = g_A^{\text{LQCD}} \left[ 1 + \frac{1}{2}(\Delta_R^A - \Delta_R^V) \right] (1 - 2\text{Re}\epsilon_R)$$

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FLAG19:

$$g_A = 1.251(33);$$

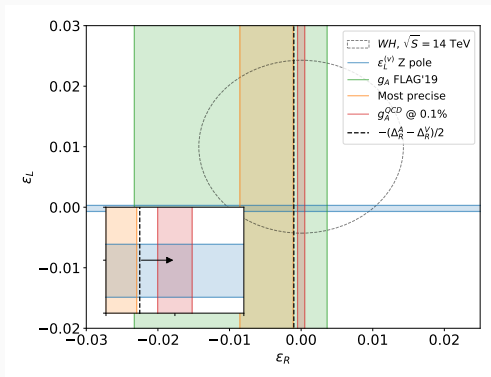
Highest precision:

$$g_A = 1.2642(93)$$

$$\Delta_R^A - \Delta_R^V$$

is  $2\sigma$  effect when

$g_A^{\text{LQCD}}$  reaches 0.1%



# BSM sensitivity

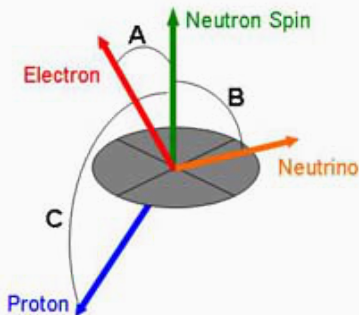
New Lorentz structures change correlations

$$\frac{d\Gamma}{dE_e d\Omega_e d\Omega_\nu} \propto 1 + a_{\beta\nu} \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + b_F \frac{m_e}{E_e} + A \frac{\vec{p}_e}{E_e} \langle \vec{l} \rangle + \dots$$

In practice,  
measure effective correlations

$$\tilde{X} = \frac{X}{1 + b_F \langle \frac{m_e}{E_e} \rangle}$$

BSM sensitivity mainly from  $b_F$



## Fierz interference

Interference term  $\rightarrow$  linear in exotic couplings

$$b_F = \pm 2\gamma \frac{1}{1 + \rho^2} \operatorname{Re} \left\{ \frac{g_S \epsilon_S}{g_V (1 + \epsilon_L + \epsilon_R)} + \rho^2 \frac{4g_T \epsilon_T}{-g_A (1 + \epsilon_L - \epsilon_R)} \right\}$$

i.e. 0 in SM

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Fermi  $\rightarrow$  scalar, Gamow-Teller  $\rightarrow$  tensor



## Fierz interference: Spectrum shape

Measure Fierz directly through the  $\beta$  spectrum shape

$$P(E_e) = \text{Standard Model} \times \left( 1 + b_F \frac{m_e}{E_e} \right)$$

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Extremely demanding for

- Detector linearity, energy losses, pile-up, . . .
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Feasible because simulation quality & new techniques like CRES

Naviliat-Cuncic, Gonzalez-Alonso PRC 94, 035503; LH *et al.*, RMP 90 015008

Ratio measurement has strong benefits

$$\frac{\lambda_{EC}}{\lambda_{\beta^+}} = \sum_{x=K,L,\dots} \frac{f_x}{f_{\beta^+}} \left[ \frac{1+b_F/W_x}{1-b_F/\overline{W}} \right] (1 + 0.001 \times \delta_{\text{theory}})$$

Enhanced sensitivity to  $b_F$  compared to usual  $b_F \langle m_e/E_e \rangle$ !

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- Only sensitive to nuclear structure at  $\mathcal{O}(\leq 10^{-3})$
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Experimentally interesting

- 'Simpler' counting experiment, could be done with 1 detector
- Systematics drop out in ratio

Choose decays to excited nuclear states  $\rightarrow \gamma$  coincidence for BG reduction ( $^{22}\text{Na}$ ,  $^{43}\text{Sc}$ ,  $^{58}\text{Co}$ , ...)

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Interesting test for atomic physics calculations, great progress with  $m_\nu$  searches in  $^{163}\text{Ho}$  (+ use  $K, L, M$  capture for consistency)



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Counting works, energy dependence is even better  $\rightarrow$  distinguish different shell captures & fit  $b_F/W$ . Looking into detector technology

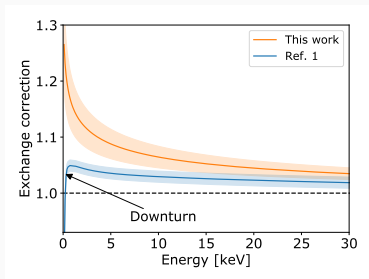
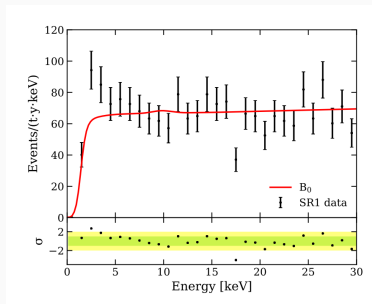
## Atomic physics with $\beta$ decay

$\beta^-$  decay has atomic **exchange** effect:  $e^-$  decays into bound state  
→ **strong** enhancement near low energy

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X1T excess,  $^{214}\text{Pb}$  background



Aprile *et al.*, 2006.09721; LH, Simonucci, Taioli, 2009.08303

DM & ALP backgrounds dominated by  $\beta$  decays → unexplored atomic effects → measure in CRES + atom traps?

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## Summary & Outlook

Past year(s) has seen several significant changes

- New RC are changing the game for  $|V_{ud}|$
- $Kl2/Kl3$  discrepancy for  $|V_{us}|$  opened
- Ab initio entering isospin breaking calculations
- New neutron results confirm  $(\tau_n)$  and create new  $(\lambda)$  tensions

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- Ab initio entering isospin breaking calculations
- New neutron results confirm ( $\tau_n$ ) and create new ( $\lambda$ ) tensions

And several more are coming...

- Better lattice  $g_A$  probes  $\epsilon_R$  (with new RC) +  $\gamma W$  tests
- Mirrors can obtain equal  $V_{ud}$  footing with  $n$ , superallowed  $\rightarrow$  independently test corrections

**Atomic gains:**  $EC/\beta^+$  has very high  $b_F$  sensitivity & measuring atomic exchange necessary for DM & ALP searches

Thank you

Thank you!



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